nne from scratch

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[1]: import numpy as np
     np.__version__
[1]: '1.21.4'
[2]: class SGDOptimizer:
         def __init__(self,lr :float):
            self.lr = lr
         def apply(self,vector,dvector):
             return vector - dvector * self.lr
     class DenseLayer():
         def __init__(self,input_nodes : int,output_nodes : int):
             self.learnable = True
             self.input_nodes = input_nodes
             self.output_nodes = output_nodes
             self.weight = np.random.randn(self.output_nodes * self.input_nodes).
      →reshape((self.output_nodes, self.input_nodes))
             self.bias = np.random.randn(self.output nodes)
             self.gradient_weight = None
             self.gradient_bias = None
             self.input = None
         def forward(self,X : np.ndarray) -> np.ndarray:
             self.input = X
             return self.weight @ X + self.bias
         def backward(self,delta):
             self.gradient_weight = delta.reshape((self.output_nodes,1))  @ self.
      →input.reshape((1,self.input_nodes))
             self.gradient bias = delta
             dX = self.weight.T @ delta
             return dX
         def apply(self,opt):
             self.weight = opt.apply(self.weight,self.gradient_weight)
             self.bias = opt.apply(self.bias,self.gradient_bias)
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[3]: sample_input = np.array([0.5,0.5])
      dense_layer = DenseLayer(2,4)
 [4]: dense_layer.forward(sample_input)
 [4]: array([ 0.08896882, -0.13611622, -1.72671291, -0.65042457])
 [5]: dense_layer.backward(np.array([1,1,0,2]))
 [5]: array([-2.25026662, 0.37713448])
[40]: class ReluActivation:
          def __init__(self):
              self.learnable = False
              self.input = None
              self.gradient = None
          def forward(self,X):
              self.input = X
              return np.maximum(X,0)
          def backward(self,delta):
              drelu = 1. * (self.input > 0)
              return drelu * delta
      class SigmoidActivation:
          def __init__(self):
              # self.input = None
              self.learnable = False
              self.gradient = None
              self.output = None
          def forward(self,X):
              \# self.input = X
              self.output = 1 / (1 + np.exp(-X))
              return self.output
          def backward(self,delta):
              dsigmoid = self.output * (1 - self.output)
              return dsigmoid * delta
[41]: sigmoid_activation = SigmoidActivation()
      sigmoid_activation.forward(np.array([-0.5,2,0]))
      sigmoid_activation.backward(np.array([0.3,0.2,0.1]))
[41]: array([0.07050111, 0.02099872, 0.025
                                               ])
[42]: relu activation = ReluActivation()
      relu_activation.forward(np.array([-25,0,125]))
[42]: array([ 0,
                  0, 125])
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[43]: class MSELoss:
          def forward(self,y_true,y_pred):
              return 0.5 * np.mean((y_true - y_pred)**2)
          def backward(self,y_true,y_pred):
              return y_pred - y_true
[44]: mse = MSELoss()
      mse.backward(np.array([1,2]),np.array([2,0]))
[44]: array([ 1, -2])
[45]: class NeuralNetwork:
          def __init__(self,layers,loss,opt):
              self.layers = layers
              self.loss = loss
              self.opt = opt
          def forward(self,X):
              current_input = X
              for layer in layers:
                  current_input = layer.forward(current_input)
              return current_input
          def backward(self,y_true,y_pred):
              dloss = self.loss.backward(y_true,y_pred)
              current delta = dloss
              for layer in reversed(layers):
                  current_delta = layer.backward(current_delta)
          def apply(self):
              for layer in layers:
                  if layer.learnable:
                      layer.apply(self.opt)
          def fit(self,X,y_true):
              y_pred = self.forward(X)
              loss = self.loss.forward(y_true,y_pred)
              self.backward(y_true,y_pred)
              self.apply()
              return loss
[66]: Xs = np.array([[0,1],[1,1],[1,0],[1,1]])
      Ys = np.array([[1],[0],[1],[0]])
      layers = [
          DenseLayer(2,2),
          SigmoidActivation(),
          DenseLayer(2,1),
          SigmoidActivation()
      ]
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nn = NeuralNetwork(layers, MSELoss(), SGDOptimizer(0.3))
[67]: nn.fit(Xs[0],Ys[0])
[67]: 0.09145182576909387
[68]: EPOCHS = 10000
      for i in range(EPOCHS):
          loss = 0
          random_inds = np.arange(4)
          np.random.shuffle(random_inds)
          for x, y in zip(Xs[random_inds], Ys[random_inds]):
              loss += nn.fit(x,y)
          loss /= Xs.shape[0]
          if i % 1000 == 0:
              print(f"EPOCH {i}: {loss:.4f}")
     EPOCH 0: 0.1418
     EPOCH 1000: 0.0038
     EPOCH 2000: 0.0010
     EPOCH 3000: 0.0005
     EPOCH 4000: 0.0004
     EPOCH 5000: 0.0003
     EPOCH 6000: 0.0002
     EPOCH 7000: 0.0002
     EPOCH 8000: 0.0002
     EPOCH 9000: 0.0001
[65]: for x,y in zip(Xs,Ys):
          y_pred = nn.forward(x)
          print(f"Target={y},Predicted={y_pred}")
     Target=[1],Predicted=[1.]
     Target=[0],Predicted=[0.]
     Target=[1],Predicted=[1.]
     Target=[0],Predicted=[0.]
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