Binary Classification via a Reinforcement Learner

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Abstract

The purpose of this project is to solve a Kaggle competition using manually constructed neural networks and reinforcement learning techniques. The competition in question is sponsored by Red Hat. Given situational (an "action" data set) and customer (a "people" data set) information, the goal is to predict customer behavior for a given action. Customer behavior is a binary classification; customers either take an action or they do not. This project will use these two data sources and neural network/reinforcement learning techniques to prepare an algorithm capable of predicting outcomes against a third situational (a "test action" data set) source. The infrastructure designed and built for this project is informed by and informs the work, the Containerized Jupyter Platform. This work is accompanied by a set of Jupyter notebooks and a docker-compose.yml file that can be run in order to validate all information here presented.

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Definition

Please refer to notebook 1 Definition.

1.1 Problem Statement

In this Kaggle competition, Red Hat seeks an optimal algorithm for using information about a given action and information about a given customer to predict the customer's behavior with regard to that action. A completed product will take the form of a csv with two items per row - an action_id from the test set, and a predicted outcome from the set 0, 1.

The following is a sample of the required format for a solution submission:

\$ head data/sample_submission.csv

```
activity_id,outcome
act1_1,0
act1_100006,0
act1_100050,0
act1_100065,0
act1_100068,0
act1_100100,0
```

Data is provided in the form of three separate data sets encoded as CSV:

- people.csv
- act_train.csv
- act_test.csv.

We will store our data in two tables in a PostgreSQL Database. The action (act_train.csv) table makes reference to the people (people.csv) table. Beyond this, the sets have been scrubbed of any domain specific knowledge. Rather attributes are referred to generically as char_1, char_2, etc. As such the competition presents an interesting challenge, in which domain knowledge is completely useless. The competition is in essence a "pure machine learning problem."

1.2 Approach

We take the following approach to completing this task:

- 1. Seed a PostgreSQL database with the three csv files.
- One-Hot Encode the data and store the one-hot encoded vector as an array in the action table
- 3. Train and Assess a Series of Learners

Note that while the Kaggle Challenge includes a set of test-data, for the purposes of this study we will be holding a separate test set aside that we are able to run our own local accuracy metrics. At the time of this writing, the competion is closed to new submissions.

1.3 Metrics

We will look at three different properties of our test set in order to measure the success of our learner:

- 1. a confusion matrix
- 2. accuracy
- 3. F1 Score

We will assess the learner against the test set throughout the training process as a way of assessing the development of our learner. However, the results of the development of the assessment will not be uses for training and can thus be used repeatedly as an impartial measure of progress.

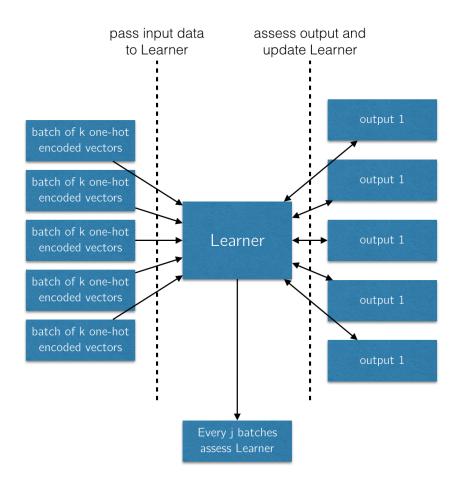


Figure 1.1: Learner Training and Assessment

1.3.1 Infrastructure

We have designed a special infrastructure geared toward a "back-end"/server-side implementation of our processes. This system uses Jupyter notebooks as its main interface, thought it is possible to interface with the system via the terminal. Additionally, a browser-based control panel exists for tracking the progress of our workers. We use to data management systems, a PostgreSQL database and Redis. Finally, we have a worker layer of n scalable worker cpus built using Python's $\tt rq$ framework.

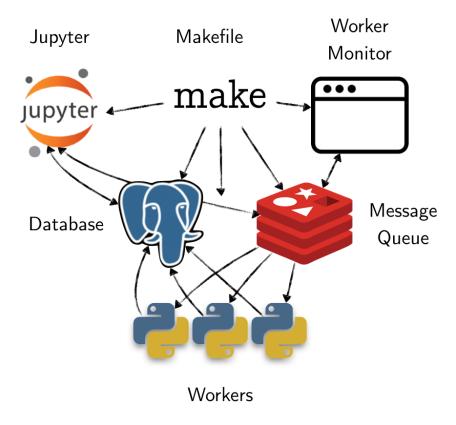


Figure 1.2: Infrastructure

Preliminary Data Analysis

2.1 Connecting to PostgreSQL

Please refer to notebook 2.01 Preliminary Data Analysis - Connecting to PostgreSQL.

We store all included data in a PostgreSQL database. By and large, we access this database using the <code>psycopg2</code> library. Here, we make use of a development pattern we will use throughout the project in which more complicated are abstracted into modules in <code>lib</code>. Here, we import <code>connect_to_postgres</code> from <code>lib/helpers/database_helper.py</code> and use it to connect to our database. Then, we run a simple query on the database, verifying that all is functioning well.

```
>>> from os import chdir; chdir('../')
>>> from lib.helpers.database_helper import connect_to_postgres
>>> conn, cur = connect_to_postgres()
>>> cur.execute("SELECT COUNT(*) FROM people"); print(cur.fetchone())
>>> cur.execute("SELECT COUNT(*) FROM action"); print(cur.fetchone())
(189118,)
(2695978,)
>>> conn.close()
```

2.2 Data Exploration

The data to be used here consists of three datasets:

- people.csv sample
- act_train.csv sample
- act_test.csv sample

We will do the following to analyze the datasets.

- 1. seeding the database
- 2. basic postgres descriptor (\d+)
- 3. define the basic structure rows, columns, data types
- 4. identify unique labels for each column and the counts for each label
- 5. run aggregates on columns mean, median, max, min
- 6. identify duplicate records, if they exist
- 7. search for NULL data
- 8. create histograms of data

2.3 Seeding the Database

This is handled during the building of the Docker image for our PostgreSQL database and is written into our database Dockerfile.

In order to run the commands in this Dockerfile we use the docker-compose tool to build our image.

\$ docker-compose build

During the building of the image, any .sql or .sh files located in /docker-entrypoint-initdb.d will be executed. We have defined the tables we will be using in the tables.sql file. The structure will be shown in a moment when we run the postgres descriptors. The full structure can be viewed in the seeding file here. This functionality is part of the PostgreSQL public Docker image.

2.4 Basic PostgreSQL Descriptors

Having built and run our images, we now have a running PostgreSQL database that has been seeded with our csv data.

2.4.1 Descriptor for database

We use the PostgreSQL descriptor command to display basic attributes of our database.

postgres=## \d+

Schema	Name	Type				Description
public	action people	table	postgres postgres	Ì	235 MB	•

2.4.2 Descriptor for action table

We can repeat the same for a particular table. The tables have been trimmed so as not to show columns of repeating type.

```
postgres=## \d+ action
```

Tab	le "public.action"	
Column	Туре	1
people_id	,	-
- · · · -	timestamp without time zone	
<pre>act_category act char 1</pre>		1
u00_011u1_1		•
act_char_10	text	
act_outcome	boolean	
Indexes:		

[&]quot;action_pkey" PRIMARY KEY, btree (act_id)

Foreign-key constraints:

[&]quot;action_people_id_fkey" FOREIGN KEY (people_id) REFERENCES people(people_id)

2.4.3 Descriptor for people table

```
postgres=## \d+ people
            Table "public.people"
  Column | Type | Modifiers |
-----+
people_id | text
                                   | not null |
ppl_char_1 | text
ppl_group_1 | text
ppl_char_2 | text
ppl_char_3 | text
ppl_char_9 | text
ppl_char_10 | boolean
ppl_char_11 | boolean
ppl_char_12 | boolean
ppl_char_37 | boolean
ppl_char_38 | real
Indexes:
   "people_pkey" PRIMARY KEY, btree (people_id)
Referenced by:
   TABLE "action" CONSTRAINT "action_people_id_fkey"
      FOREIGN KEY (people_id) REFERENCES people(people_id)
```

2.5 Define the Basic Structure

Please refer to notebook 2.05 Preliminary Data Analysis - Define the Basic Structure.

The number of rows in a set can be identified by a query using the COUNT() function. Our test and training sets can be identified by the fact that the test set has NULL values in the act_outcome column.

2.5.1 Number of Rows in database tables

database	number of rows	number of training rows
people action	189118 2695978	N/A 498687

2.5.2 Number of Columns per Data Type

database	text	boolean	timestamp	real
people	11	28	1	0
action	13	1	1	1

2.6 Identify Unique Labels

2.6.1 Number of Unique Labels for people

label	unique
people_id	189118
ppl_group_1	34224
ppl_date	1196
ppl_char_1	2
ppl_char_2	3
ppl char 3	43
ppl char 4	25
ppl char 5	9
ppl char 6	7
ppl char 7	25
ppl char 8	8
ppl_char_9	9

Additionally we do not show the final group of columns for the following reasons. ppl_char_10 through ppl_char_37 are boolean and have only two labels - TRUE and FALSE.

ppl_char_38 is a continuous valued column.

2.6.2 Number of Unique Labels for action

Again we first show columns that have too many labels. However, upon second consideration we should use the column act_category.

unique
2695978
411
7
51
32
11
7
7
5
8
18
19
6969

We do not show the outcome act_outcome because it is boolean.

2.7 Run Aggregates on Columns

Next we take the average of our boolean columns. Note that all of them skew to the negation, most of them heavily so. The only exception is act_outcome which, while still toward the negation, is closer to the middle.

label	mean		
ppl_char_10	(0.2509)		
ppl_char_11	(0.2155)		
ppl_char_12	(0.2403)		
ppl_char_13	(0.3651)		
ppl_char_14	(0.2598)		
ppl_char_15	(0.2695)		
ppl_char_16	(0.2821)		

label	mean
ppl_char_17	(0.2920)
ppl_char_18	(0.1876)
ppl_char_19	(0.2847)
ppl_char_20	(0.2291)
ppl_char_21	(0.2850)
ppl_char_22	(0.2911)
ppl_char_23	(0.2985)
ppl_char_24	(0.1904)
ppl_char_25	(0.3278)
ppl_char_26	(0.1670)
ppl_char_27	(0.2381)
ppl_char_28	(0.2889)
ppl_char_29	(0.1683)
ppl_char_30	(0.2069)
ppl_char_31	(0.2786)
ppl_char_32	(0.2849)
ppl_char_33	(0.2178)
ppl_char_34	(0.3565)
ppl_char_35	(0.2103)
ppl_char_36	(0.3437)
ppl_char_37	(0.2855)
act_outcome	(0.4440)

Then we take the average, maximum, and minimum of the single real-valued column.

2.8 Identify Duplicate Records

Note that there are 189118 people_id values, one for each row. We can take this to mean that there are no duplicate entries in the people dataset. The same is true with actions with 2695978 unique act_id values.

2.9 Search for NULL Data

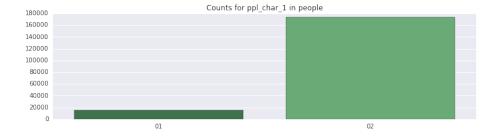
There is null data in these datasets, in two locations. There are null values in the boolean variables attached to the action table. We will be handling this data, however, when we process the data for handoff to the neural network. Additionally, there are null values in the act_outcome column, but this is functional as a null value in this field signifies a test action as opposed to a train action.

2.10 Exploratory Visualization

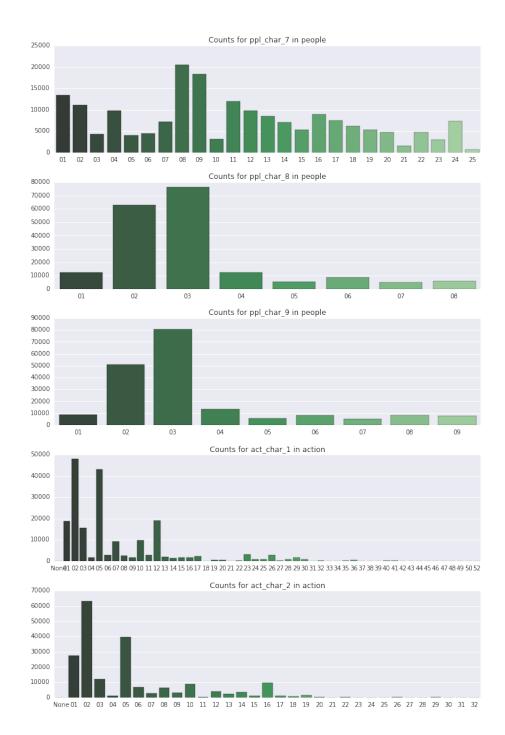
Please refer to notebook 2.10 Preliminary Data Analysis - Create Histograms of Data.

Finally, we use the Python library seaborn to create plots of our data as histograms. We import a method bar_plot to present a histogram for each categorical parameter.

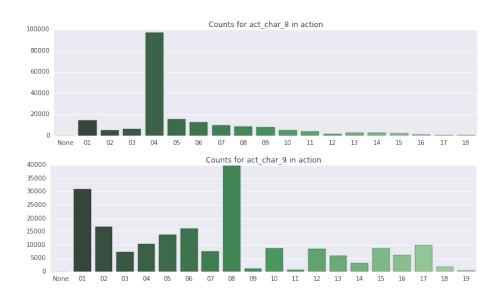
```
>>> from os import chdir; chdir('../')
>>> from lib.helpers.plot_helper import bar_plot
>>> bar_plot('ppl_char_1','people')
>>> bar_plot('ppl_char_2','people')
>>> bar_plot('ppl_char_3','people')
>>> bar_plot('ppl_char_4', 'people')
>>> bar_plot('ppl_char_5','people')
>>> bar_plot('ppl_char_6','people')
>>> bar_plot('ppl_char_7','people')
>>> bar_plot('ppl_char_8','people')
>>> bar_plot('ppl_char_9','people')
>>> bar_plot('act_char_1','action')
>>> bar_plot('act_char_2','action')
>>> bar_plot('act_char_3','action')
>>> bar plot('act char 4', 'action')
>>> bar_plot('act_char_5','action')
>>> bar_plot('act_char_6','action')
>>> bar_plot('act_char_7','action')
>>> bar_plot('act_char_8','action')
>>> bar_plot('act_char_9', 'action')
```











Algorithms and Techniques

3.1 One-Hot Encoding

Please refer to notebook 3.01 Algorithms and Techniques - One-Hot Encoding Example.

We will use the One-Hot Encoding algorithm to convert our categorical data to numerical data. It may be tempting to merely convert our categories to numbers i.e. type $01 \rightarrow 1$, type $02 \rightarrow 2$, however, such an encoding of data implies a linear relationship between our categories, where there may be none.

In one-hot encoding, a separate bit of state is used for each state. It is called one-hot because only one bit is "hot" or TRUE at any time. (Harris, David, and Sarah Harris. Digital design and computer architecture. Elsevier, 2012.)

This algorithm is also referred to as 1-of-K encoding. An example will be helpful in illustrating the concept.

3.1.1 One-Hot Encoding Example

```
>>> import numpy as np
>>> from os import chdir; chdir('../')
>>> from lib.helpers.database_helper import connect_to_postgres
>>> conn, cur = connect_to_postgres()
>>> cur.execute("SELECT ppl char 1,ppl char 2 FROM people LIMIT 10")
>>> this_row = cur.fetchone()
>>> one hot = []
>>> while this_row:
        one_hot.append([
            this_row[0] == 'type 1',
            this_row[0] == 'type 2',
            this_row[1] == 'type 1',
            this_row[1] == 'type 2',
            this_row[1] == 'type 3',
        ])
    this_row = cur.fetchone()
>>> print(np.array(one_hot, dtype=int))
[[0 1 0 1 0]
 [0 1 0 0 1]
 [0 1 0 0 1]
 [0 1 0 0 1]
 [0 1 0 0 1]
 [0 1 0 0 1]
 [0 1 0 1 0]
 [0 1 0 0 1]
 [0 1 0 0 1]
 [0 1 0 0 1]]
```

Here, we select two columns from our database. For each available type for each column, we do a Boolean check and then cast this check to an integer. The result is that for a given group of columns corresponding to a single column in our original database, there will be a single 1 and the remainder will be 0. We use one-hot coding because the categorical and boolean nature of the vast majority of our data lends itself to this technique.

3.2 Linear Classification via Neural Network

Linear classification will be the core algorithm upon which we will build our neural network classifier. We borrow heavily for this approach from Andrej Karpathy's notes for his Convolutional Neural Networks course:

The approach will have two major components: a **score function** that maps the raw data to class scores, and a **loss function** that quantifies the agreement between the predicted scores and the ground truth labels.

3.2.1 Score Function

We will develop a score function that maps input vectors to class scores

$$f: \mathbb{R}^{\mathbb{D}} \mapsto \mathbb{R}^2$$

where D is the dimension of our one-hot encoded vectors and 2 represents the 2 classes of our binary classifier. Then,

$$f(x_i, W, b) = Wx_i + b = y$$

where x_i is a particular input vector, W is a matrix of weights (dimension $2 \times n$), b is a bias vector, and y is a score vector with a score for each class.

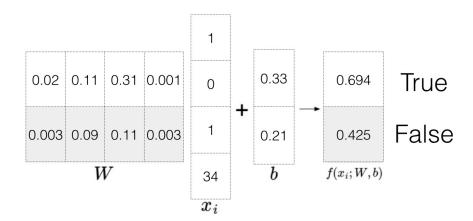


Figure 3.1: A Linear Classifier

3.2.2 Loss Function

Note that of the inputs to our score function we do not have control over the x_i s. Instead, we must change W and b to match a set of given ys. To do this we will define a loss function that measures our performance. We will use one of

the most common loss functions the multiclass support vector machine. Here the loss for a given vector is

$$L_i = \sum_{j \neq y_i} \max(0, s_j - s_{y_i} + \Delta)$$

Here, s is the vector result of our score function and y_i is the correct class. Our loss function computes a scalar value by comparing each incorrect class score to the correct class score. We expect the score of the correct class to be at least Δ larger than the score of each incorrect class.

3.2.3 Regularization Penalty

It is possible that more than one set of weights could provide an optimal response to our loss function. In order to prioritize the smallest possible weights we will add a regularization penalty to our loss function. Again we will go with a common technique and use the L2 norm.

$$R(W) = \sum_{k} \sum_{l} W_{k,l}^2$$

Additionally, including a regularization penalty has the added benefit of helping to prevent overfitting.

3.2.4 Final Loss Function

$$L = \frac{1}{N} \sum_{i} L_{i} + \lambda R(W)$$

Here, λ is a hyper parameter to be fit by cross-validation and N is a batch size.

3.3 Optimization

Possibile methods:

3.3.1 Generate a Random Weights Matrix

• we initialize a weights matrix, W

3.3.2 Randomly guessing

- we initialize a weights matrix, W_{cur}
- for each vector (or batch of vectors) passed to the learner, we generate a new weights matrix, W_i
- if the new weights, W_i is better in score than W_{cur} , we assign it to W_{cur}

$$W_{cur} \to W_i$$

• repeat for all of our test vectors

3.3.3 Random Local Search

- we initilialize a weights matrix, W
- for each batch of vectors passed, we generate a random matrix, ΔW , of the same dimension as W and scaled by some factor, ν
- we measure the loss against the sum $W + \nu \Delta W$.
- If $W + \nu \Delta W$ has a better score than W, we assign it to W

$$W + \nu \Delta W \to W$$

• repeat for all of our test vectors

3.3.4 Gradient Descent

- compute the best direction along which we should change our weight matrix that is mathematically guaranteed to be the direction of the steepest descent
- the gradient is a vector of derivatives for each dimension in the input space
- calculate the gradient and use this calculation to update the weight matrix

$$W_{new} = W - \nabla L$$

3.4 Benchmark

Of note is that, while the outcome is clearly defined by the contest, for the purposes of this project, we will be using a portion of the training set as our benchmark. Of note is that we modified our performance metric during the refinement phase.

As previously noted, we will look at three different properties of our test set in order to measure the success of our learner:

- 1. a confusion matrix
- 2. accuracy
- 3. F1 Score

3.4.1 Confusion Matrix

A confusion matrix is a table that allows the visualization of the algorithm performance. Each row represents the actual classes of our target variable: 1 or 0. Each column represents the predicted classes of our target variable: 1 or 0. We will then measure the true and false positives as well as the true and false negatives.

3.4.2 Accuracy

Accuracy will be calculated in the following manner:

$$\label{eq:accuracy} \text{Accuracy} = \frac{\text{True Postives} + \text{True Negative}}{\text{Postives} + \text{Negatives}}$$

We will be trying to maximize this value.

3.4.3 F1 Score

F1 Score will be calculated as

$$F_1 = 2 \cdot \frac{\text{precision} \cdot \text{recall}}{\text{precision} + \text{recall}}$$

where

$$\mathrm{precision} = \frac{\mathrm{True\ Positives}}{\mathrm{True\ Positive} + \mathrm{False\ Positives}}$$

and

$$\text{recall} = \frac{\text{True Positivess}}{\text{True Positives} + \text{False Negatives}}$$

We will be trying to maximize this value.

Free-Form Visualization

4.1 Visualizing the Loss Function

Please refer to notebook 4.01 Exploratory Visualization - Visualizing the Loss Function.

A relevant visualization to this task is that of the loss function. For this visualization, we again turn to Andrej Karpathy's notes.

While we will have difficulty visualizing the loss function over the complete weight space, we can visualize it over a smaller space to begin to understand our approach.

For the purposes of this visualization, let us consider a small random weight matrix (2, p) for a binary classifier, i.e., one weight vector for each classifier.

```
>>> W = np.random.rand(2,7)
```

We then generate a random input vector x (with 6 parameters, and then a trailing bias) and and a vector of outputs.

```
>>> x = np.random.randint(2, size=7)
>>> x[6] = 1
```

Finally, we randomly select a correct outcome for a binary classifier.

```
>>> correct_class = np.random.randint(2)
```

We vary the loss function for a single input with different weights for a single parameter, param, then plot this function along various values of variable_weight for all of our params values.

```
>>> render_all_plots_1d(correct_class,x,W)
```

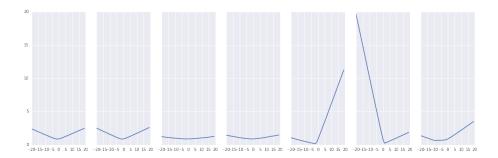


Figure 4.1: Visualizing Loss Function change along one Parameter

It is of note that every parameter is convex and can be minimized.

We can also do the same for a comparison of two varied parameters. Again, note that each of these plots is convex.

>>> render_all_plots_2d(correct_class,x,W)

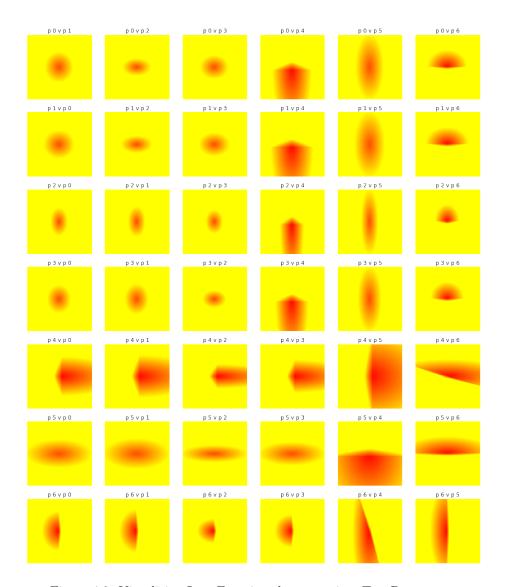


Figure 4.2: Visualizing Loss Function change against Two Parameters $\,$

Data Preprocessing

5.1 CSV Manipulation

The dataset was a set provided by Kaggle. As such, it was already well structured and clean. Still, in order to facilitate processing, some work had to be done on the csv data itself.

5.1.1 act_train.csv

An additional column had to be added to the csv in order to ultimately provide a null space in which to insert our act_one_hot_encoded binary value. This was done via the sed command line tool by adding a comma to each line.

```
$ sed -e 's/$/,/' -i act_train.csv > new_act_train.csv
```

5.1.2 act_test.csv

For the test data set, we needed to add two columns, one for the null outcome (test and train are stored in the same table and distinguished by having a true, false or null value) and the same null space in which to insert the act_one_hot_encoded binary value.

```
$ sed -e 's/$/,/' -i act_test.csv > new_act_test.csv
```

5.1.3 All Sets

Additionally, we wanted to convert all attributes to double digit attributes i.e. char $1 \rightarrow$ char 01.

In this section, all of your preprocessing steps will need to be clearly documented, if any were necessary. From the previous section, any of the abnormalities or characteristics that you identified about the dataset will be addressed and corrected here. Questions to ask yourself when writing this section:

5.2 One-Hot Encoding

We will be storing our one-hot encoded numpy arrays as binary data in the action table column act_one_hot_encoded.

Implementation

6.1 Steps to Implementation

- 1. Seed a PostgreSQL database with the three csv files.
- 2. One-Hot Encode the data and store the one-hot encoded vector as an array in the action table
- 3. Train and Assess a Series of Learners

6.2 Seed a PostgreSQL database with the three csy files.

This step is done at instantiation of the system. Refer to Seeding the Database.

6.3 One-Hot Encode the data and store the onehot encoded vector as an array in the action table

Please refer to notebook 6.03 Implementation - Write One-Hot to Action Table.

```
>>> from os import chdir; chdir('../')
>>> from lib.app import Q
>>> from lib.helpers.database_helper import connect_to_postgres
>>> from lib.helpers.database_helper pull_actions_and_one_hot_encode
```

```
>>> for i in range(1000):
        Q.enqueue(pull_actions_and_one_hot_encode, 1000, i*1000)

>>> conn, cur = connect_to_postgres()

>>> cur.execute("SELECT count(*) FROM action where act_one_hot_encoding is not null;")

>>> cur.fetchone()
(372666,)
```

We have written a library to handle the one-hot encoding of the data. pull_actions_and_one_hot_encode does a join on the action and people tables, converts the tables and categories to one-hot encoded data, converts this to a binary numpy vector, and writes this binary to the action table, for actions from the action table that do not yet have one-hot encoded vectors.

Note that we are also using our delayed job system to do the conversion. Once jobs have been enqueued, the status of enqueued jobs can be tracked here.

6.4 Prediction on Random Weights Matrix With No Training

Please refer to notebook 6.04 Implementation - Prediction on Random Weights Matrix With No Training.

We first establish a baseline competency by examining performance of a totally untrained learner.

```
>>> from os import chdir; chdir('../')
>>> from numpy import mean
>>> from random import shuffle, seed
>>> from lib.helpers.database_helper import pull_actions, pull_and_shape_batch
>>> from lib.nn.functions import measure_accuracy, random_matrix
```

6.4.0.1 Pull Training and Test Rows

We seed the shuffling mechanism for deterministic results. We then pull a set of 90000 action_ids from the action table. We shuffle these ids and designtate the first 75000 as our training set and the last 15000 as our test set. To reiterate, we are not using the Kaggle competitions test set as we do not have the actual outcomes for that set and we can thus not measure the accuracy of our learner.

6.4.0.2 Train Learner and Assess Learner Accuracy

We are not actually training a learner here. We are merely generating a random matrix of the appropriate size. We then check the accuracy of this random matrix against our test set. This is done four times via the **%timeit** ipython magic function.

```
>>> accuracies = []
%%timeit
>>> # initialize a random_weights matrix
>>> random_weights = random_matrix(2, 7326)
>>> features, outcomes = pull_and_shape_batch(action_ids=test_set)
>>> accuracy = measure_accuracy(random_weights, features, outcomes)
>>> print(accuracy)
>>> accuracies.append(accuracy)

0.5552
0.636933333333
0.544133333333
0.5514666666667
1 loop, best of 3: 1min 30s per loop

We take the mean of this.
>>> mean(accuracies)
```

So a purely random matrix performs a little bit better than guessing. I suspect that were this to be repeated many times, the mean would be close to the expected 0.50.

0.57193333333333334

Refinement

Slightly better than guessing is a pretty poor performance. In order to improve upon our performance, we will try a series of improvements upon our learner in order to obtain better performance.

7.1 Learning via Random Search

Please refer to notebook 7.01 Refinement - Learning via Random Search.

As a first attempt at improvement, we will work in batches through our training set. For each batch we will:

- 1. generate a random weights matrix
- 2. evaluate the random weight matrix against the loss function
- 3. if the loss function is lower than the previous lowest loss function
- 4. store the loss function as the best_loss and the weights matrix as weights_matrix

It is of note that we will be doing the training via distributed processing. As such, we can not store the best_loss and weights_matrix in memory. Instead, we store the values in Redis. We have written a few methods to handle the storage and retrieval of these values.

- read_best_loss
- read_weights_matrix
- write_best_loss
- write_weights_matrix

7.1.1 Establish State of Training Session

7.1.2 Assess Results

```
>>> weights_matrix = get_weights_matrix()
>>> features, outcomes = pull_and_shape_batch(action_ids=test_set)
>>> measure_accuracy(weights_matrix, features, outcomes)
0.762133333333333333
```

We also prepared a plot of the loss function over the course of the training. Note hthat we saw improvement take place once, and never again.

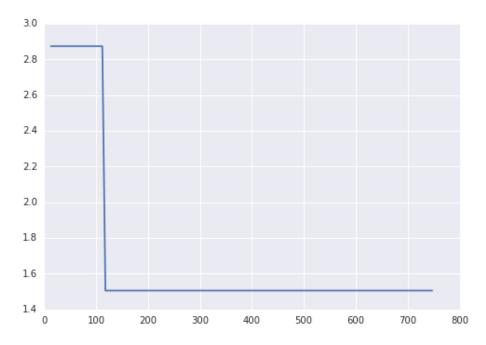


Figure 7.1: Loss Function over Random Search Training

7.2 Learning via Random Local Search

Please refer to notebook 7.02 Refinement - Learning via Random Local Search.ipynb.

Next, we attempt to improve our initial random matrix via microchanges in the local vicinity. Again, we will work in batches through our training set. For each batch we will:

- 1. generate a random weights matrix delta
- 2. add the delta to our current weights matrix
- 3. evaluate the temporary weight matrix against the loss function
- 4. if the loss function is lower than the previous lowest loss function
- 5. store the loss function as the best_loss and the temporary weights matrix as weights_matrix

7.2.1 Establish State of Training Session

7.2.2 Assess Results

```
>>> weights_matrix = get_weights_matrix()
>>> features, outcomes = pull_and_shape_batch(action_ids=test_set[:100])
>>> measure_accuracy(weights_matrix, features, outcomes)
0.64000000000000001
```

Here, we actually have a lower accuracy result. This largely speaks to the instability of this method.

If we look at the plot of the loss function over the training, we can see that there was significantly greater improvement over the course of the training using this method.

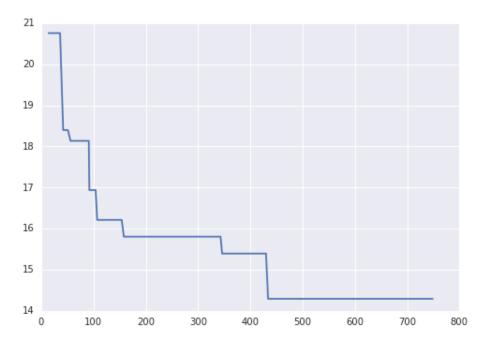


Figure 7.2: Loss Function over Random Local Search Training

7.3 Learning via Gradient Descent

Please refer to notebook 7.03 Refinement - Learning via Gradient Descent.

As one might imagine there is actually a better for local optimization than a random step. We will improve upon our prediction by taking a step in the *optimal* direction at each learning phase. The loss function is the function that we are attempting to minimize. The gradient of this loss function will tell use the direction in which the loss function is most rapidly decreasing.

Consider our loss function in one-dimension (without regularization):

$$L_i = \sum_{j \neq y+i} \max(0, s_j - s_{y_i} + \Delta)$$

Where s_i is the score for our correct class and s_j is the score for incorrect class(es).

We obtain the gradient by differentiating with respect to the weights to obtain, for the row of the weight matrix corresponding to the correct class:

$$\nabla_{w_{y_i}} L_i = -\left(\sum_{j \neq y_i} \mathbb{1}(w_j^T x_i - w_{y_i}^T x_i + \Delta > 0)\right) x_i$$

and for the row(s) of the weight matrix corresponding to the incorrect class(es):

$$\nabla_{w_j} L_i = \mathbb{1}(w_j^T x_i - w_{y_i}^T x_i + \Delta > 0) x_i$$

Here $\mathbb{1}$ is the indicator function that is one if if the condition inside is true or zero otherwise.

7.3.1 Establish State of Training Session

7.3.2 Assess Results

```
>>> weights_matrix = get_weights_matrix()
>>> features, outcomes = pull_and_shape_batch(action_ids=test_set)
>>> measure_accuracy(weights_matrix, features, outcomes)
0.421800000000000001
```

This is the first training method not based on random chance. We note:

- it has performed very poorly
- we see the exponential growth of our loss function

At this point, we did some deep consideration of our approach. The exponential growth of the loss function is a problem of implementation. We are not minimizing with respect to a regularized loss function. This is not necessarily the cause of our poor performance. Most likely, the cause of our poor performance is the curse of dimensionality.

act_char_10 has 6969 unque labels. In order to properly one-hot encode this column, we require as many binary features. This one column multiples the size of our fetures space by seven. Given that complexity grows exponentially, we are pinning the poor performance of our learner on this column and discard it for our next pass.

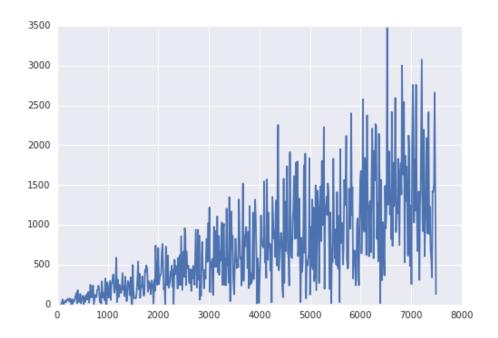


Figure 7.3: Loss Function over Gradient Search Training

7.4 Recover from Curse of Dimensionality

Please refer to notebook 7.04 Refinement - Recover from Curse of Dimensionality.

In order to drop act_char_10, we must change the way that we are performing our one-hot encoding. We create a new table of columns called one_hot_indices_min.py.

7.5 Rewrite One-Hot to Action Table

Please refer to notebook 7.05 Refinement - Rewrite One-Hot to Action Table.

7.6 Learning via Gradient Descent, Part 2

Please refer to notebook 7.03 Refinement - Learning via Gradient Descent.

Results

(approx. 2-3 pages)

8.1 Model Evaluation and Validation

The work in this project has been invaluable in developing an understanding of the work that goes into developing a high-performance computing environment. That said, I am not satisfied with the model developing during the implementation. The final state of the model was of a single node using gradient descent that was stuck at an implementation of regularization to the update. As can be seen in figure 7.3, without the inclusion of regularization the loss function increases exponentially over time. While this does not actually affect the validity of the accompanying weight matrix, it does make it difficult to draw a comparison between the gradient descent method and the other methods implemented herein.

We have found the primary illumnination provided by the gradient descent is that our feature space is too large.

Conclusion

9.1 Reflection

It is important to note that nearly very line of code in this project was written by me. In this sense, there has been great value in attempting to implement some of the most challenging machine learning concepts from scratch. That said, it is clearly not the best solution to this task. Tensorflow or a similar library should have been brought to bear on this task. It is of note that tensorflow has been developed by a team of more than 20 people. While I have learned a lot in writing this code base, especially in terms of writing clean Python, perhaps the most important thing I have learned is that it is okay to stand on the shoulders of giants. I don't need to do everything from scratch.