

ZigZag

**A CHAUTAUQUA ON J
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Syntax

- Statements are exactly one line long
- Numbers may be written `2, _2, 0.5, 5, 1e3, 2j5, 2r7, 16b1f, 2p1, _, __`
- Adjacent numbers make a list: `3 5 2e3 7`
- Strings have single-quotes: `'hello'`
- Everything else is a built-in or user-defined word:
 - Verbs: `+, -, %, etc.`
 - Adverbs: `~, /, }, etc.`
 - Conjunctions: `^:, ", @, &, etc.`
 - Others: `=., =:, NB., etc.`

You do not need to trouble yourself with the distinction between integers, floats, and complex numbers. If it's a number, J will handle it properly.

J for C Programmers

Evaluation Rules

Forget the table of operator precedence!

J for C Programmers

RTL Evaluation:

$$2 * 4 + 5$$

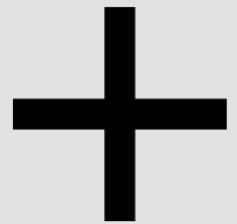
18

$$2 + 4 * 5$$

22

$$(2 * 4) + 5$$

13



+ 0 0 0

Conjugate

$+y$ is the conjugate of y . For example, $+3j4$ is $3j_4$.

Plus

$+$ is defined as in elementary arithmetic, and is extended to complex numbers as usual.

Verb

- 0 0 0

Negate

Minus

-y is the
negative of
y . That is,
it is defined
as $0 - y$.
Thus, $-2 = 2$
is $-2 = 2$.

- is defined as
in elementary
arithmetic, and
is extended to
complex numbers
as usual.

Verb



* 0 0 0

Signum Times

*y is _1 if y
is negative, 0
if it is zero,
1 if it is
positive; more
generally, *y
is the
intersection
of the unit
circle with
the line from
the origin
through the
argument y in
the complex
plane.

Verb

%

% 0 0 0

Reciprocal

% y is the reciprocal of y , that is,
 $1/y$.

Divided by

x % y is division of x by y as defined in elementary math, except that 0% is 0.

Verb

Monads & Dyads

%

% 0 0 0

Reciprocal

% y is the reciprocal of y , that is, $1\%y$.



y is right arg

Divided by

x % y is division of x by y as defined in elementary math, except that $0\%0$ is 0 .



x is left arg,
y is right arg

Verb

Monad vs. Dyad %:

2%7

0.285714

7%2

3.5

%7

0.142857

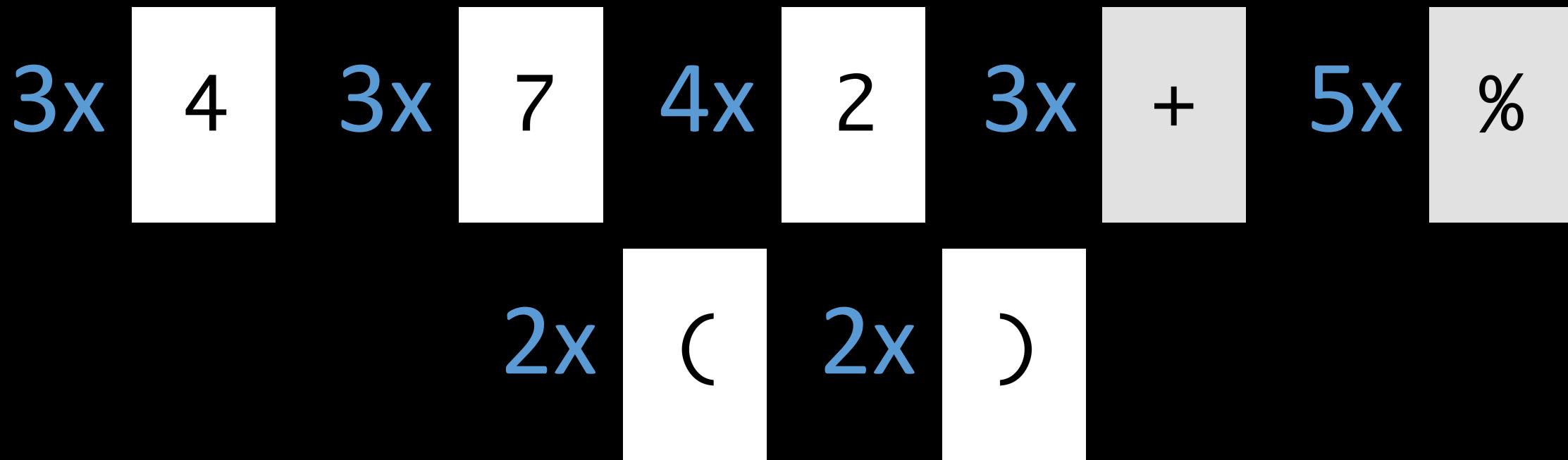
%2

0.5

Challenge!

Compute the arithmetic mean of 4 and 7.

Find three solutions using all of these cards simultaneously:



= _ 0 0

Self-Classify Equal

=y classifies x=y is 1 if x
the items of is equal to
the nub of y y , and is
(that is, ~.y) otherwise 0 .
according to
equality with
the items of
y , producing
a boolean
table of shape
#~.y by #y .

Verb



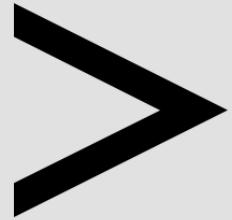
||

| 0 0 0

Magnitude Residue

`ly == %:y*y .` The familiar
use of residue
is in determ-
ining the
remainder on
dividing a
non-negative
integer by a
positive.

Verb



> 0 0 0

Open

Open is the inverse of box, that is, $>y$ is y . When applied to an open array (that has no boxed elements), open has no effect. Opened atoms are brought to a common shape.

Larger Than

$x>y$ is 1 if x is tolerantly larger than y . Tolerance t is provided by $>!.t$.

Verb

~

•

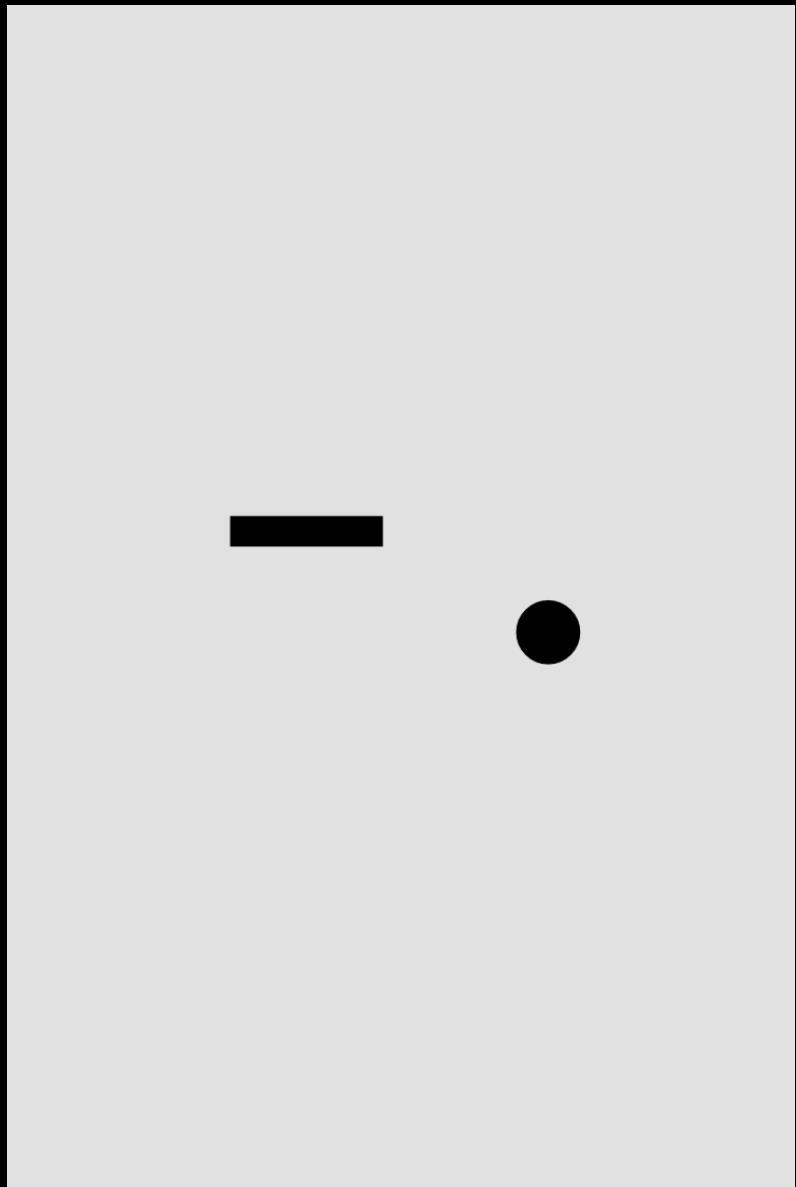
•

$\sim : _ \theta \theta$

Nub Sieve Not Equal

$\sim : y$ is the
boolean list b is tolerantly
such that $b \# y$ unequal to y .
is the nub of
 y .

Verb



- . \emptyset — —

Not Less

$-y$ is $1-y$; $x-y$ includes all
for a boolean items of x except
argument it is for those that
the complement are cells of y .
(not); for a
probability,
it is the
complementary
probability.

Verb

Challenge!

Compute whether a number, say 8, is even (gives 1 if even, 0 otherwise).

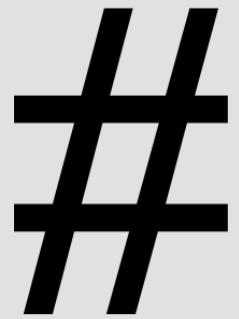
Find four solutions using all of these cards simultaneously:

$$\begin{array}{ccccccccc} 1x & \boxed{0} & 2x & \boxed{1} & 4x & \boxed{8} & 1x & = & 4x & \boxed{1} \\ & & & & & & & & & \\ 4x & \boxed{2} & 1x & \sim : & 1x & > & 1x & - . & \end{array}$$

Arrays

Any variable can be an array. As for what the type and dimensioning is: you assigned the variable, didn't you? It contains whatever you put into it, a number, a string, an array, a structure... J will remember. If your program logic requires you to find out the current attributes of a variable, J can tell you.

J for C Programmers



_ 1 _

Tally

#y is the number of items in y . If the arguments have an equal number of items, then x#y copies +/x items from y, with i{x repetitions of item i{y . Otherwise, if one is an atom it is repeated to make the item count of the arguments equal.

Verb

Copy

Variable assignment and array size:

```
a := 5 3 7 9
```

```
a
```

```
5 3 7 9
```

```
#a
```

```
4
```

```
s := 'hello'
```

```
#s
```

```
5
```

In J, every operator has a loop built in.

J for C Programmers

Automatic element-by-element operations:

```
      1 2 3 + 4 5 6
5 7 9
      1 + 4 5 6
5 6 7
      1 2 + 4 5 6
|length error
| 1 2      +4 5 6
```

i.

i. 1 —

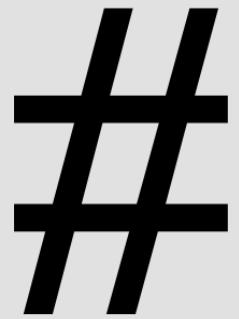
Integers

The shape of $i.y$ is ly , and its atoms are the first $*/ly$ non-negative integers. A negative element in y causes reversal of the atoms along the corresponding axis.

Verb

Index Of

If rix is the rank of an item of x , then the shape of the result of $x i.y$ is $(-rix)\}$. \$y . Each atom of the result is either $\#x$ or the index of the first occurrence among the items of x of the corresponding rix-cell of y .



_ 1 _

Tally

#y is the number of items in y . If the arguments have an equal number of items, then x#y copies +/x items from y, with i{x repetitions of item i{y . Otherwise, if one is an atom it is repeated to make the item count of the arguments equal.

Verb

Copy

i.4

0 1 2 3

3+i.4

3 4 5 6

3#i.4

0 0 0 1 1 1 2 2 2 3 3 3

#3#i.4

12

3##i.4

4 4 4

?

? 0 0 0

Roll

? y yields a uniform random selection from the population i.y if y is a positive integer, or from the interval of numbers greater than 0 and less than 1 if y is 0.

Deal

x ? y is a list of x items randomly chosen without repetition from i.y .

Verb

?5

1

?5

4

?0

0.654682

?5 2 3 6

3 1 0 4

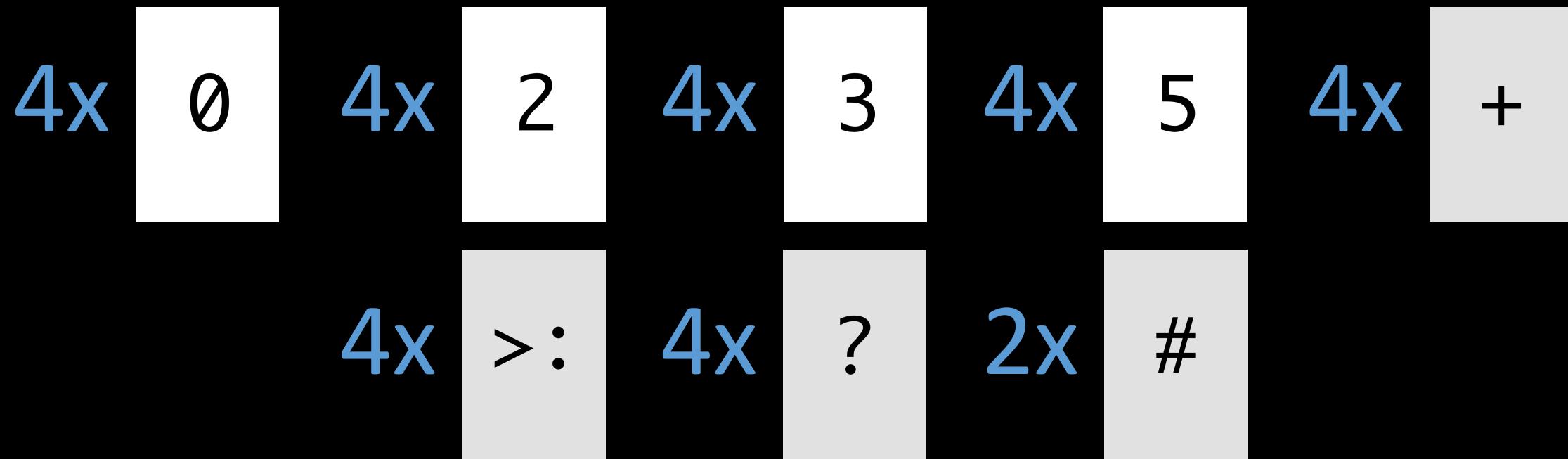
3?7

1 4 2

Challenge!

Roll five d20 dice with +3 modifiers on all rolls.

Find four solutions using all of these cards simultaneously:



Adverbs

A noun holds data; a verb operates on one or two nouns to produce a result which is a noun; an adverb operates on one noun or verb to produce a derived entity.

J for C Programmers

m/ u/ _ _ _

m/ u/ _ _ _

Insert

u/y applies the dyad u between the items of y . m/y inserts successive verbs from the gerund m between items of y, extending m cyclically as required. Thus, +`*/i.6 is 0+1*2+3*4+5 .

Table

If x and y are numeric lists, then x */ y is their multiplication table.

Adverb

1+2+3+4+5

15

+/1 2 3 4 5

15

*/1 2 3 4 5

120

New version of “arithmetic mean”:

```
vals:=3 _4 7 9 _2 3  
+/vals  
16  
#vals  
6  
(+/vals)%(#vals)  
2.66667  
+/vals%#vals  
2.66667
```

u~

u~ _ ru lu

Reflexive

$u~ y == y u y .$
For example, $^~$
 3 is 27 , and $+/_$
 $\sim i.$ n is an
addition table.

Passive

\sim commutes or
crosses
connections to
arguments: $x u~$
 $y == y u x .$

Adverb

{

{ 1 0 _

Catalogue From

{y forms a catalogue from the atoms of its argument, its shape being the chain of the shapes of the opened items of y . The common shape of the boxed results is \$y .

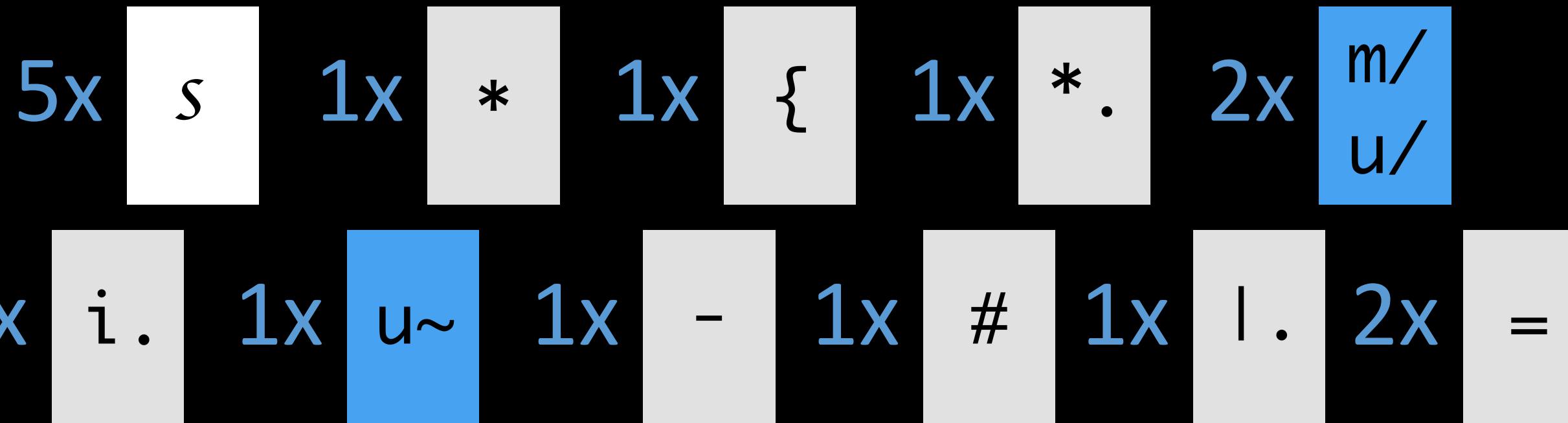
If x is an integer in the range from -n=: #y to n-1 , then x{y selects item n|x from y .

Verb

Challenge!

Given a string (or any array) s, determine if it's a palindrome.

Find two solutions using all of these cards simultaneously:



Hooks & Forks

Hooks fg

Monadic $fg\ y == y\ f\ (g\ y)$
 $-%\ y == y\ -\ (%\ y)$

Dyadic $x\ fg\ y == x\ f\ (g\ y)$
 $x\ -%\ y == x\ -\ (%\ y)$

```
f =: monad : '0=2|y'      NB. checks that y is even  
i.10  
0 1 2 3 4 5 6 7 8 9  
f i.10  
1 0 1 0 1 0 1 0 1 0
```

NB. use # operator to keep only evens
(f i.10) # i.10
0 2 4 6 8

NB. use a hook
(#~f) i.10 NB. i.e., i.10 #~ (f i.10)
0 2 4 6 8 NB. i.e., (f i.10) # i.10

Forks

fgh

Monadic

$fgh\ y == (f\ y)\ g\ (h\ y)$
 $-+%\ y == (-\ y)\ + (\%\ y)$

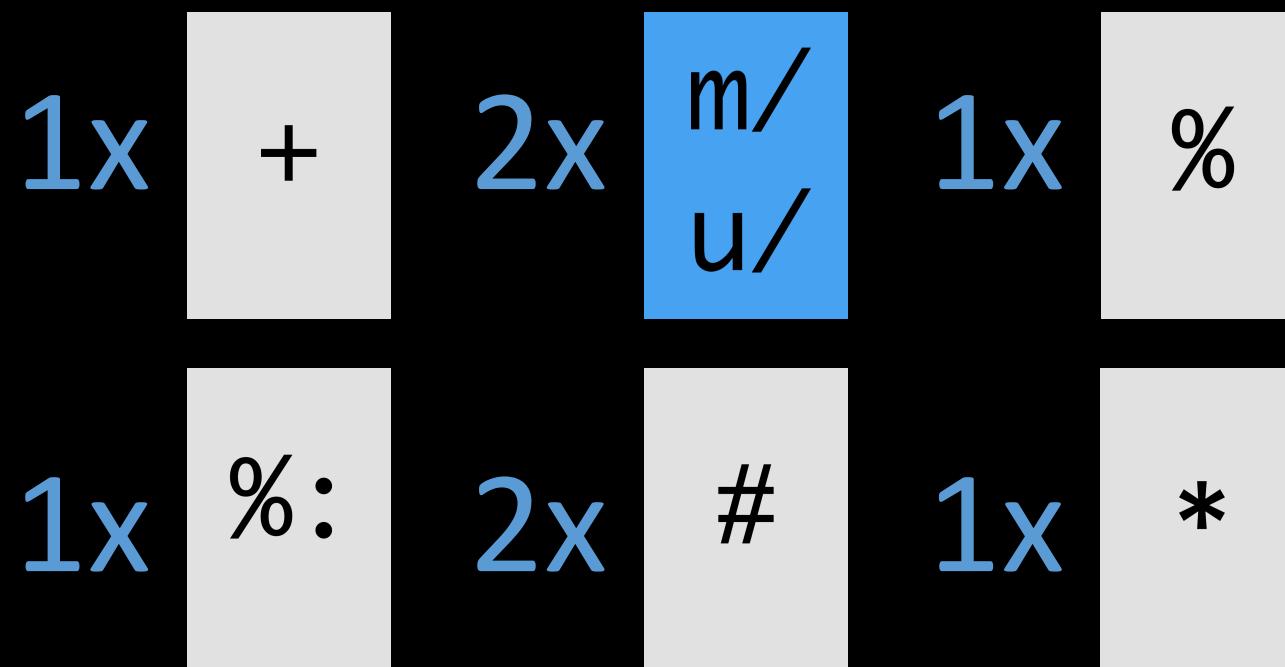
Dyadic

$x\ fgh\ y == (x\ f\ y)\ g\ (x\ h\ y)$
 $x\ -+%\ y == (x\ -\ y)\ + (x\ \% y)$

Challenge!

Define the arithmetic mean and geometric mean for any list of numbers. Geometric mean = $(x_1 * x_2 * \dots * x_n)^{(1/n)}$.

Find one solution for each kind of mean using all of these cards simultaneously:



Conjunctions

J uses the names x, y, u, v, m, and n to represent arguments to verbs and other entities. You should avoid using these names for other purposes.

J for C Programmers

m&v

u&n

m&v u&n _ 0 _

Bond

m&v y is defined as
m v y ; that is, the
left argument m is
bonded with the dyad

v to produce a
monadic function.

Similarly, u&n y is
defined as y u n ;
in other words, as
the dyad u provided
with the right
argument n to
produce a monadic
function.

x m&v y ==
m&v^:x y
x u&n y ==
u&n^:x y

Conjunction

```
f  =: 5&+
f 1 2 3 4 5
6 7 8 9 10
g  =: -&5
g 1 2 3 4 5
_4 _3 _2 _1 0
```

u&v

u&v mv mv mv

Compose

$u \& v \ y == u \ v \ y$. Thus $+ \& - 7$ is $_14$ (double the negation). Moreover, the monads $u \& v$ and $u @ v$ are equivalent.

$x \ u \& v \ y == (v \ x) \ u \ (v \ y)$. For example, $3 + \& ! 4$ is 30 , the sum of factorials.

Conjunction

```
f =: -&%
f 1 2 3 4 5
_1 _0.5 _0.333333 _0.25 _0.2
 10 f 1 2 3 4 5
_NB. i.e., -(%y)

_NB. i.e., (%x)-(%y)

g =: -%
g 1 2 3 4 5
0 1.5 2.66667 3.75 4.8
 10 g 1 2 3 4 5
9 9.5 9.66667 9.75 9.8
_NB. compare with hook
_NB. i.e., y-(%y)
_NB. i.e., x-(%y)
```

u@:v

u@:v _ _ _

At

$u@:v \ y == u \ v \ y . \ x \ u@:v \ y == u \ x \ v$
For example, $y .$ For example,
 $+:@:- 7$ is $_14$ $3 +:@:- 7$ is $_8$
(double the
negation).
(double the
difference).

Moreover, the
monadic uses of
 $u@v$ and $u&v$ are
equivalent.

Conjunction

```

f =: -@:%
NB. same as & in monadic form

f 1 2 3 4 5
_1 _0.5 _0.333333 _0.25 _0.2

10 f 1 2 3 4 5           NB. i.e., - (x % y)
_10 _5 _3.33333 _2.5 _2

f =: +/@:%
NB. i.e., +/ (% y)

f 1 2 3 4 5           NB. i.e., sum reciprocals of y
2.28333

```

Challenge!

Define the L¹, L², and L[∞] norms.

L¹ = sum(absval(x_i)) for all x_i

L² = sqrt(sum(x_i²) for all x_i)

L[∞] = max(x_i) for all x_i

Find one solution for each norm using all of these cards simultaneously:

2x +

3x m/
u/

3x u@:v

1x |

1x * :

1x %:

1x > .

*Atoms, Lists,
Tables, et al.*

,

,

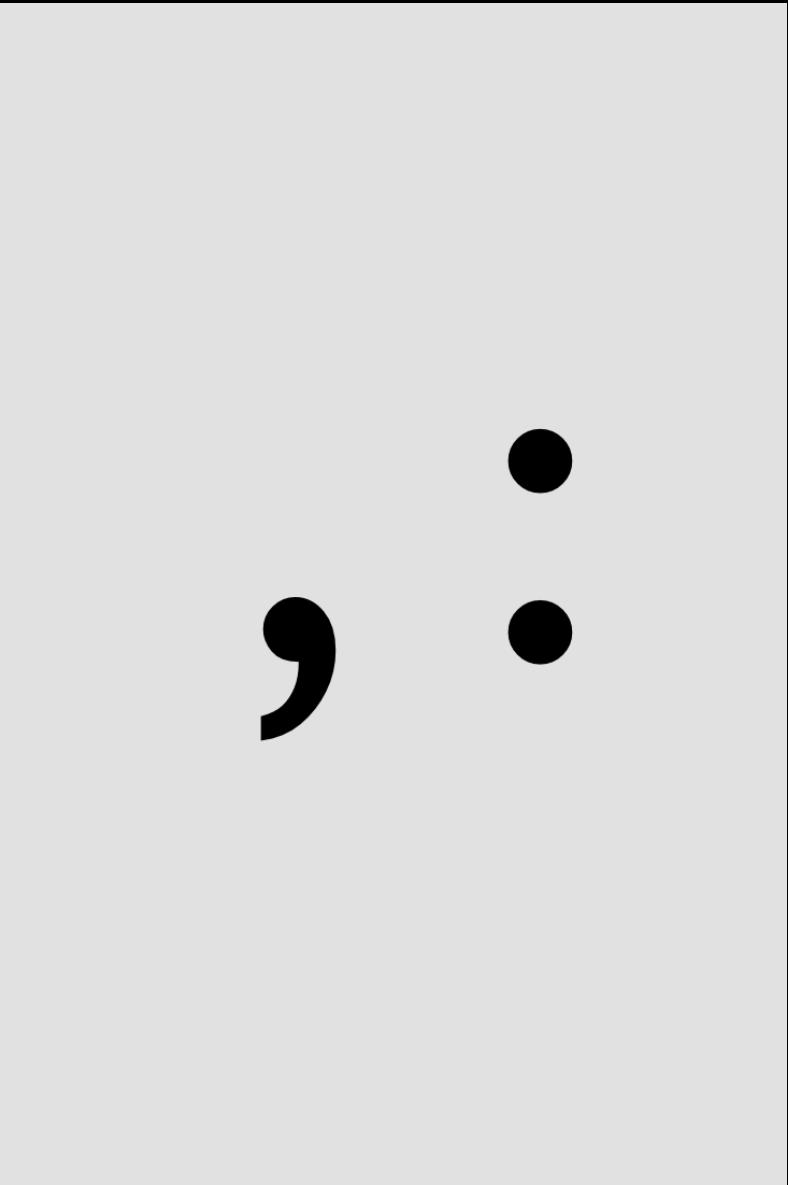
— — —

Ravel Append

,y gives a list
of the atoms of
y in “normal”
order: the
result is
ordered by
items, by items
within items,
etc. The result
shape is 1\$*/\$
y .

Verb

```
(i.3) (i.5)
| syntax error
|           (i.3)(i.5)
(i.3),(i.5)
0 1 2 0 1 2 3 4
```



, : - - -

Itemize

`,:y` adds a leading unit axis to `y` , giving a result of shape `1,$y` .

Verb

Laminate

An atomic argument in `x,:y` is first reshaped to the shape of the other (or to a list if the other argument is also atomic); the results are then itemized and catenated, as in `(,:x)`, `(,:y)` .

```
pt1  := 5.1 3.5 1.4 0.2
pt2  := 4.9 3.0 1.4 0.2
pt3  := 4.7 3.2 1.3 0.2
pt1 , pt2 , pt3
5.1 3.5 1.4 0.2 4.9 3 1.4 0.2 4.7 3.2 1.3 0.2
pt1 , pt2 ,: pt3
5.1 3.5 1.4 0.2
4.9   3 1.4 0.2
4.7 3.2 1.3 0.2
```



\$ _ 1 _

Shape Of

`$ y` yields the shape of `y`. For example, the shape of a 2-by-3 matrix is `2 3`, and the shape of the scalar `3` is an empty list (whose shape is `0`). The rank of an argument `y` is `#@$ y`.

Shape

The shape of `x` `$y` is `x,siy` where `siy` is the shape of an item of `y`; `x$y` gives a length error if `y` is empty and `x,siy` does not contain a zero.

Verb

```
      pt1 , pt2 , pt3
5.1 3.5 1.4 0.2 4.9 3 1.4 0.2 4.7 3.2 1.3 0.2
      $ pt1 , pt2 , pt3
12
      pt1 , pt2 ,: pt3
5.1 3.5 1.4 0.2
4.9   3 1.4 0.2
4.7 3.2 1.3 0.2
      $ pt1 , pt2 ,: pt3
3 4
```

Rank

The rank of a noun is the count of its axes. An atom has rank 0, a list rank 1, a table rank 2, and an array with 5 axes has rank 5.

J Primer

```
$ pt1 , pt2 , pt3  
12  
# $ pt1 , pt2 , pt3 NB. ## computes rank  
1  
$ pt1 , pt2 ,: pt3  
3 4  
# $ pt1 , pt2 ,: pt3  
2  
NB. etc.
```

Ask the rank of a verb.

+ b.θ

θ θ θ

- b.θ

θ θ θ

i. b.θ

1 - - \$ b.θ

- 1 - , : b.θ

— — —

If you don't know the rank of a verb, you don't know the verb. Using a verb of unknown rank is like wiring in a power-supply of unknown voltage—it will do something when you plug it in; it might even work; but if the voltage is wrong it will destroy what it's connected to. Avoid embarrassment! Know the rank of the verbs you use.

J Primer

u"n

u"n

Rank

The verb u"n applies u to each cell as specified by the rank n . The full form of the rank used is 3\$&.l.n . For example, if n=:2 , the three ranks are 2 2 2 , and if n=: 2 3, they are 3 2 3 . A negative rank is complementary: u"(-r) y is equivalent to u"(0>.(#\$y)-r)"_ y .

Conjunction

```
 100 200 300 + (1 2 3 4)
|length error
| 100 200 300      +(1 2 3 4)
```

```
 100 200 300 +"0 _ (1 2 3 4)
101 102 103 104
201 202 203 204
301 302 303 304
```

```
 100 200 300 +"_ 0 (1 2 3 4)
101 201 301
102 202 302
103 203 303
104 204 304
```

Show how a verb would be applied.

```
load 'general/misc/fndisplay'  
defverbs 'divide'  
setfnform 'J'  
8 divide 10
```

```
8 divide 10
```

```
4 8 divide 10 20
```

```
(4 8) divide 10 20
```

4 8 (divide"0) 10 20

| | |
|-------------|-------------|
| 4 divide 10 | 8 divide 20 |
|-------------|-------------|

4 8 (divide"1) 10 20

| |
|--------------------|
| (4 8) divide 10 20 |
|--------------------|

i.2 3
0 1 2
3 4 5
4 (divide"0) i.2 3

| | | |
|------------|------------|------------|
| 4 divide 0 | 4 divide 1 | 4 divide 2 |
| 4 divide 3 | 4 divide 4 | 4 divide 5 |

4 (divide"1) i.2 3

| | |
|----------------|----------------|
| 4 divide 0 1 2 | 4 divide 3 4 5 |
|----------------|----------------|

4 (divide"_) i.2 3

| |
|-------------------------------|
| 4 divide 2 3\$(0 1 2) (3 4 5) |
|-------------------------------|

(i.2 3) (divide"0 0) i.2 3

| | | |
|------------|------------|------------|
| 0 divide 0 | 1 divide 1 | 2 divide 2 |
| 3 divide 3 | 4 divide 4 | 5 divide 5 |

(i.2 3) (divide"1 0) i.2 3

| | | |
|------------------|------------------|------------------|
| (0 1 2) divide 0 | (0 1 2) divide 1 | (0 1 2) divide 2 |
| (3 4 5) divide 3 | (3 4 5) divide 4 | (3 4 5) divide 5 |

(i.2 3) (divide"1 1) i.2 3

| | |
|----------------------|----------------------|
| (0 1 2) divide 0 1 2 | (3 4 5) divide 3 4 5 |
|----------------------|----------------------|

(i.2 3) (divide"1 _) i.2 3

| | |
|-------------------------------------|-------------------------------------|
| (0 1 2) divide 2 3\$(0 1 2) (3 4 5) | (3 4 5) divide 2 3\$(0 1 2) (3 4 5) |
|-------------------------------------|-------------------------------------|

(i.2 3) (divide"_ 0) i.2 3

| | | |
|----------------------------------|----------------------------------|----------------------------------|
| (2 3\$(0 1 2) (3 4 5)) divide 0 | (2 3\$(0 1 2) (3 4 5)) divide 1 | (2 3\$(0 1 2) (3 4 5)) divide 2 |
| (2 3\$(0 1 2) (3 4 5)) divide 3 | (2 3\$(0 1 2) (3 4 5)) divide 4 | (2 3\$(0 1 2) (3 4 5)) divide 5 |

(i.2 3) (divide"0 _) i.2 3

| | | |
|-------------------------------|-------------------------------|-------------------------------|
| 0 divide 2 3\$(0 1 2) (3 4 5) | 1 divide 2 3\$(0 1 2) (3 4 5) | 2 divide 2 3\$(0 1 2) (3 4 5) |
| 3 divide 2 3\$(0 1 2) (3 4 5) | 4 divide 2 3\$(0 1 2) (3 4 5) | 5 divide 2 3\$(0 1 2) (3 4 5) |

(i.2 3) (divide"_ _) i.2 3

| |
|---|
| (2 3\$(0 1 2) (3 4 5)) divide 2 3\$(0 1 2) (3 4 5) |
|---|

In J, every operator has a loop built in.

J for C Programmers

Coding Challenge!

Write code that fills in the blanks and produces the given output.

Compute the column sums of a table.

| | | | | | |
|----|----|----|-------|----|----|
| | | | i.4 | 6 | |
| 36 | 40 | 44 | 48 | 52 | 56 |
| | | | <hr/> | | |

Compute the arithmetic mean of every row in a pair of tables.

Recall the arithmetic mean is `+/%#`

| | | | | |
|-------|------|------|---|---|
| | | i.2 | 3 | 6 |
| 2.5 | 8.5 | 14.5 | | |
| 20.5 | 26.5 | 32.5 | | |
| <hr/> | | | | |

Recursion

$u^{:n}$

$u^{:v}$

$u^{:n}$ $u^{:v}$

Power

The verb u is applied n times. An infinite power n produces the limit of the application of u . If n is negative, the obverse $u^{:_{-1}}$ is applied $|n|$ times.

$$\begin{aligned} x \ u^{:n} y &= \\ x \& u^{:n} y \end{aligned}$$

Conjunction

The case of $\wedge:$ with a verb right argument is defined in terms of the noun right argument case ($u^{:n}$) as follows:

$u^{:v} y ==$
 $u^{:((v) y)} y ;$
 $x \ u^{:v} y ==$
 $x \ u^{:((x) v) y}$

```
vals=:4 3 2 $ 24?100      Recursive “Larger of” >.  
./vals  
96 95  
70 85  
60 89  
.>./.>./vals  
96 95  
.>./.>./vals  
96  
. ./^:_3 vals NB. recursive application, 3 times  
96  
. ./^:_ vals NB. 'limit' of >./, works on any shape  
96
```

| | |
|----|-------------------------------|
| | NB. interesting cases of u^:n |
| 11 | NB. do-once (>:^:1) 10 |
| | NB. increment once |
| 15 | NB. do-many (>:^:5) 10 |
| | NB. increment five times |
| 10 | NB. don't (>:^:0) 10 |
| | NB. returns y |

NB. interesting cases of u[:]n

NB. do various times

(>:^:(i.10)) 10 NB. increment 0, 1, ..., 9 times

10 11 12 13 14 15 16 17 18 19

NB. obverse (aka inverse)

(>:^:_1) 10 NB. decrement once

9

NB. do-infinitely-many-times

(cos^:_) 1 NB. compute y=cos(y)

0.739085

$u^{:n}$

$u^{:v}$

$u^{:n}$ $u^{:v}$

Power

The verb u is applied n times. An infinite power n produces the limit of the application of u . If n is negative, the obverse $u^{:_{-1}}$ is applied $|n|$ times.

$$\begin{aligned} x \ u^{:n} y &= \\ x \& u^{:n} y \end{aligned}$$

Conjunction

The case of $\wedge:$ with a verb right argument is defined in terms of the noun right argument case ($u^{:n}$) as follows:

$u^{:v} y ==$
 $u^{:_{(v\ y)}} y ;$
 $x \ u^{:v} y ==$
 $x \ u^{:_{(x\ v\ y)}} y$

NB. highly interesting cases of u^:v

NB. do sometimes

```
1 2 3 4 5 ((>:@[)^:])"0 (1 0 0 1 0)  
2 2 3 5 5
```

NB. explanation:

NB.] keeps right side, [keeps left side

NB. >:@[means "increment vals of left argument"

NB. ^:] means apply power (^:) n times, where n
NB. comes from right side

NB. finally, "0 means apply ^: to each value

NB. written another way...

```
myfunc =: >: NB. define function to apply  
if =: adverb define  
''  
NB. no monadic form  
:  
y u@]^:["0 x NB. here is the dyadic form  
)
```

```
1 2 3 4 5 myfunc if 1 0 0 1 0  
2 2 3 5 5
```

NB. more fancy

```
even =: monad : '0=2|y'    NB. checks that y is even  
myfunc =: >:
```

NB. use a hook!

```
(myfunc if even) 1 2 3 4 5  
1 3 3 5 5
```

NB. the above turned into:

```
NB. 1 2 3 4 5 (myfunc if) (even 1 2 3 4 5)
```

```
NB. 1 2 3 4 5 (myfunc if) 0 1 0 1 0
```

NB. do while...

NB. $(u^{:}v)^{:}_-$ ends when the output of v is the same
NB. as the prior time; supposing v is boolean (0/1),
NB. then $^{:}_-$ stops when v produces 0, yielding $u^{:}0$

```
dowhile =: conjunction define
(u^:(v@:]^:_"0) y
:
x (u^:(v@:]^:_"0) y
)
```

NB. continue doubling a number until it's ≥ 100

```
2 * dowhile (100&>) 1 3 5 7 9 11
```

```
128 192 160 112 144 176
```

NB. defining “if” and “dowhile” as a J adverb (if)
NB. and conjunction (dowhile) gives us the benefits
NB. of automatic looping:

(2&* if even) i. 2 3 2

0 1

4 3

8 5

12 7

16 9

20 11

NB. defining “if” and “dowhile” as a J adverb (if)
NB. and conjunction (dowhile) gives us the benefits
NB. of automatic looping:

```
(2&* dowhile (100&>)) i. 2 3 2
```

```
0 128
```

```
128 192
```

```
128 160
```

```
192 112
```

```
128 144
```

```
160 176
```

Coding Challenge!

Write code that fills in the blanks and produces the given output.

Given a number N and a list of scores, compute the average of the scores after dropping the lowest N scores. Create one solution using ^: and one solution without using ^:. Feel free to use define.

1 _____ 90 70 80 75 NB. drop 1 score
81.6667

2 _____ 90 70 80 75 NB. drop 2 scores
85

3 _____ 95 60 0 55 80 0 90 NB. drop 3 scores
78.333

Big Data

You may at first worry that you're using too much memory, or that you might misuse the processor's caches; get over it. Apply verbs to large operands.

J for C Programmers

Jd, the J relational database.

```
load 'jd'
```

NB. create a database folder
jdadminx'bbjd'

NB. set path to CSV files to load
CSVFOLDER=:F=:'/home/jeckroth/chautauquas/zigzag/'

NB. create a "cdefs" file that describes the dataset
jd'csvcdefs /h 1 backblaze-2013-2016.csv'

```
NB. load the backblaze data (60mil rows)
jd'csvrd backblaze-2013-2016.csv backblaze'
```

NB. the data are stored as one binary file per column;
NB. when you come back, just type jdadmin'mydbname'

NB. show the db schema

```
jd'info schema'
```

| table | column | type | shape |
|-----------|----------------|---------|-------|
| backblaze | date | edate | _ |
| backblaze | serial_number | byte | 15 |
| backblaze | model | byte | 23 |
| backblaze | capacity_bytes | int | _ |
| backblaze | failure | boolean | _ |
| backblaze | smart_187_raw | int | _ |

```
NB. read some data  
jd'reads date,capacity_bytes from backblaze'
```

```
...  
| 2013-04-10 | 3000592982016 |  
| 2013-04-10 | 3000592982016 |  
| 2013-04-10 | 3000592982016 |  
| 2013-04-10 | 2000398934016 |  
| 2013-04-10 | 2000398934016 |
```

```
...  
| 2016-12-29 | 322056190273242112 |  
| 2016-12-30 | 322052189486212096 |  
| 2016-12-31 | 322056190273242112 |
```

```
NB. save result  
capacity_by_day =: (...above...)
```

NB. results are "boxed" (each box can hold a different type)

NB. so let's unbox just the capacities

capacities =. ,/ > 1 1 { capacity_by_day

capacities

54041214222213120 54041214222213120 54041214222213120

53861178805862400 55657532182339584 55657532182339584

55792558378819584 55796559165849600 55796559165849600

55796559165849600 55796559165849600 55795058863939584

55795058863939584 55930085548130304 ...

\$ capacities

1360

NB. find min, max capacity

<./ capacities

_8946789308003949568

>./ capacities

1282429594186119424

NB. avg capacity
(+/%#) capacities

3.55142e12

NB. or ask jd to compute avg using one of several agg verbs
jd'info agg'

aggs

avg

count

countunique

first

last

max

min

sum

jd'reads avg capacity_bytes from backblaze

capacity_bytes

3.55142e12

NB. 5sec

```
NB. compute overall failure rate
failures =: ,/0{1{ jd'reads failure from backblaze'
$ failures
59654783
+/failures          NB. total failures
5806
overallAFR =: 365*100*(+/failures)%(#failures)
overallAFR
3.55242
```

```
NB. compute failures by year
dates =: >0{1{ jd'reads date from backblaze'
$ dates
59654783 10          NB. ugh, dates are strings now
2 {. dates
2013-04-10
2013-04-10
(4&{.".1) 2 {. dates  NB. keep only first four digits
2013
2013
NB. 0". converts strings to numbers
years =: 0 ". (4&{.".1) dates
$ years
59654783
```

NB. ok, we have years

NB. how do we sum failures per year?

NB. note /. adverb, known as "key"

m/.
u/.

m/. u/. _ _ _

Oblique Key

u/.y applies u to each of the oblique lines of a table y . m/.y applies successive verbs from the gerund m to the oblique lines of _2-cells of y, extending m cyclically as required.

Adverb

x u/.y == (=x) u@# y , that is, items of x specify keys for corresponding items of y and u is applied to each collection of y having identical keys. x m/.y applies successive verbs from the gerund m to the collections of y, extending m cyclically as required.

NB. ok, we have years

NB. how do we sum failures per year?

NB. note /. adverb, known as "key"

NB. example usage:

```
2013 2013 2014 2015 2015 +//. 2 3 7 11 12  
5 7 23
```

NB. hence:

```
driveFailuresYears =: years +//. failures      NB. 1sec  
driveFailuresYears
```

```
740 2206 1429 1431
```

NB. likewise:

```
driveDays =: years #/. failures
```

```
driveDays
```

```
5091501 12582414 17509251 24471617
```

NB. get unique years (in order of data) to match

NB. the driveFailuresYears result

```
uniqueYears =: ~.years
```

NB. 1sec

```
uniqueYears
```

```
2013 2014 2015 2016
```

NB. hence hence:

```
yearlyAFR =: 365*100*driveFailuresYears%driveDays
```

```
uniqueYears ,: yearlyAFR
```

```
2013 2014 2015 2016
```

```
5.30492 6.39933 2.97891 2.13437
```

The big slide with timing data.

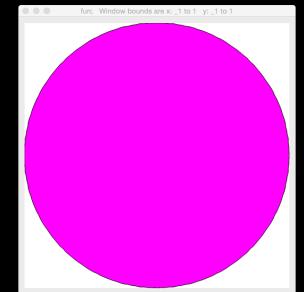
| Task | Jd | R (dplyr) | MySQL |
|---------------------------------------|--------|------------------|---------|
| Import CSV data | 50 sec | 2 min (read_csv) | 11 min |
| Space on disk | 3.6 GB | 374 MB | 5.2 GB |
| Load data into variable | 55 sec | 1 min 45 sec | NA |
| Select sum(capacity) group by date | ~1 sec | ~1 sec | 4.5 min |
| Select avg(capacity) | ~1 sec | ~1 sec | 38 sec |

Note, original CSV data was 3.2 GB.

Visualization

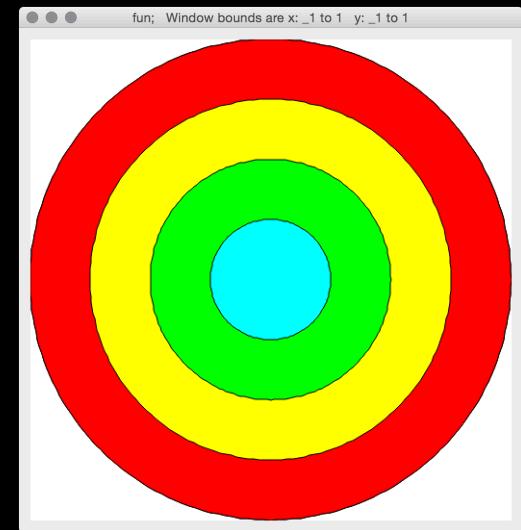
```
load '~addons/graphics/fvj4/dwin.ijs'  
_1 _1 1 1 dwin 'fun'      NB. open window, -1:1 axes  
1 o. 1r6p1                  NB. sin(1/6 pi^1)  
0.5  
2 o. 1r6p1                  NB. cos(1/6 pi^1)  
0.866025  
  
NB. define x,y coordinates of a circle with 200 pts  
circ =: |: 2 1 o./ 1r100p1*i.200  
1          0  
0.999507  0.0314108  
0.998027  0.0627905  
0.995562  0.0941083  
...
```

NB. plot a circle with a color
255 0 255 dpoly circ



circ4 =: 1 0.75 0.5 0.25 */ circ NB. four circles
colr4 =: 255 0 0, 255 255 0, 0 255 0,: 0 255 255

NB. plot four circles with individual colors
colr4 dpoly circ4

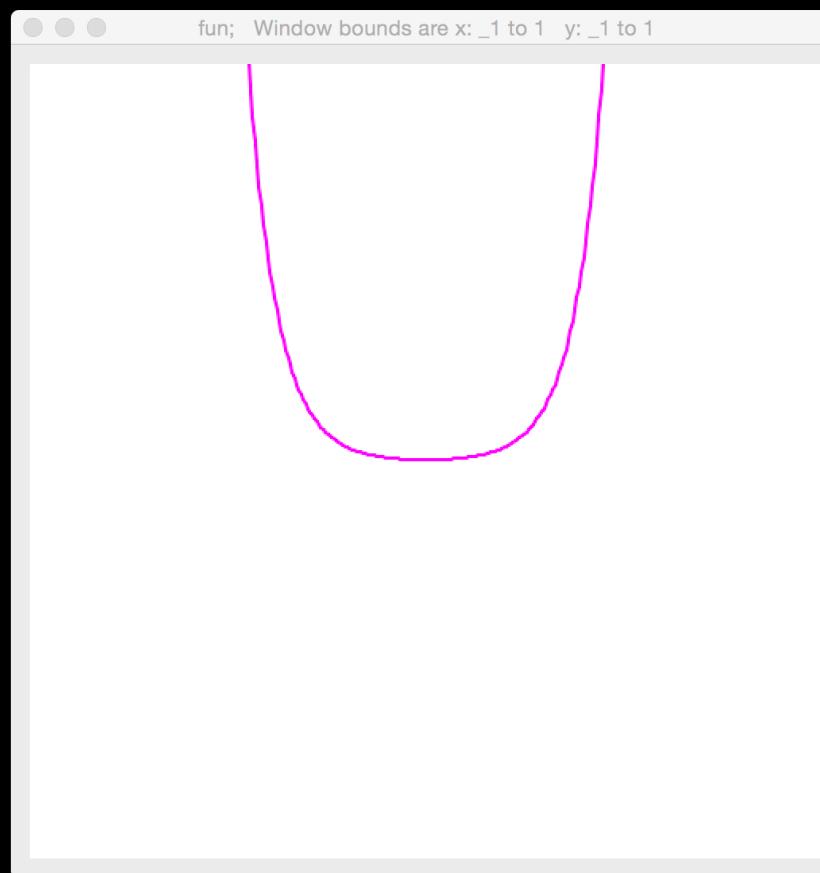


```
NB. generate some exponential values  
(^ 0.1 * i.80) % 100  
0.01 0.0110517 0.012214 0.0134986 ...
```

```
NB. generate some x,y values for a symmetric curve  
xs =: ((i.180) * %180) - 0.5  
ys =: ((|. (^0.075*i.90)), (^0.075*i.90))%400  
curve =: |: xs ,: ys  
curve  
_0.5 1.98087  
_0.494444 1.83774  
_0.488889 1.70495  
...
```

| curve | |
|-------------|------------|
| _0.5 | 1.98087 |
| _0.494444 | 1.83774 |
| _0.488889 | 1.70495 |
| ... | |
| _0.0111111 | 0.00269471 |
| _0.00555556 | 0.0025 |
| 0 | 0.0025 |
| 0.00555556 | 0.00269471 |
| 0.0111111 | 0.00290459 |
| ... | |
| 0.483333 | 1.70495 |
| 0.488889 | 1.83774 |
| 0.494444 | 1.98087 |

NB. plot the curve
 255 0 255 dline curve



Rotation can be defined as
matrix multiplication of a vector
representing the point: [x,y,1]
and a rotation matrix:

```
M = [ cos(theta) -sin(theta) 0
      sin(theta)  cos(theta) 0
      0          0 1 ]
```

After multiplying $M^*[x,y,1]^T$, the
result will be [x',y',z]; divide z
out of x' and y' to get final
coordinates. In our case,
however, z will always be 1.

```
NB. define matrix mult.
mp =: +/ . *
```

```
NB. allow simple trig names
load 'trig'
```

```
NB. define rotation matrix
rotm =: (cos, sin, 0:),
(-@sin, cos, 0:),
(0:, 0:, 1:)
```

```
rotm 1r4p1
0.707107 0.707107 0
-0.707107 0.707107 0
0          0 1
```

Likewise, a translation matrix is defined as:

```
M = [ 1 0 xtrans  
      0 1 ytrans  
      0 0 1 ]
```

Translation & rotation matrices can be combined with matrix multiplication, e.g.,

```
TransM * RotM * [x,y,1]T
```

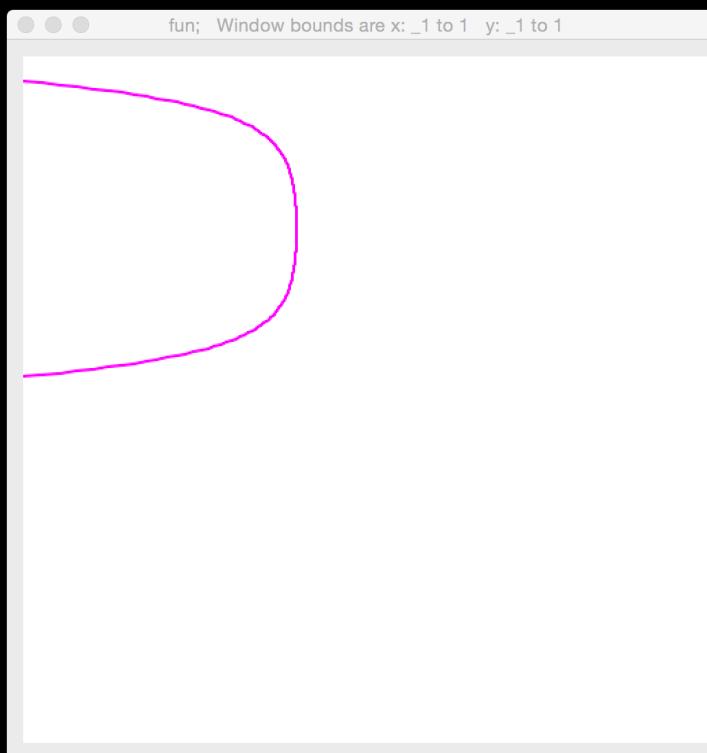
NB. trans. matrix as verb
trans =: monad define
1 0 0, 0 1 0,: (y,1)
)
trans 5 2
1 0 0
0 1 0
5 2 1
(trans 5 2) mp (rotm 1r4p1)
0.707107 0.707107 0
_0.707107 0.707107 0
2.12132 4.94975 1
(3 2 1) mp (... above ...)
2.82843 8.48528 1

```
NB. add extra z=1 dimension to curve  
curve =: curve,.1
```

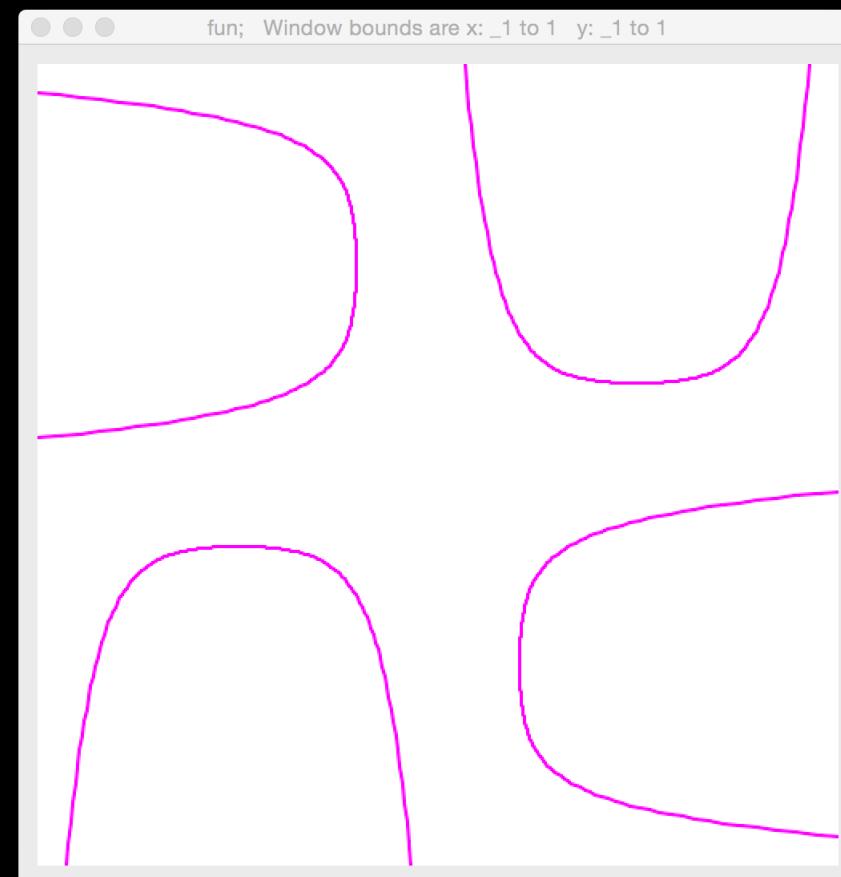
```
NB. draw a translated, rotated curve
```

```
dclear''
```

```
255 0 255 dline curve mp (trans 0.5 0.2) mp (rotm 1r2p1)
```



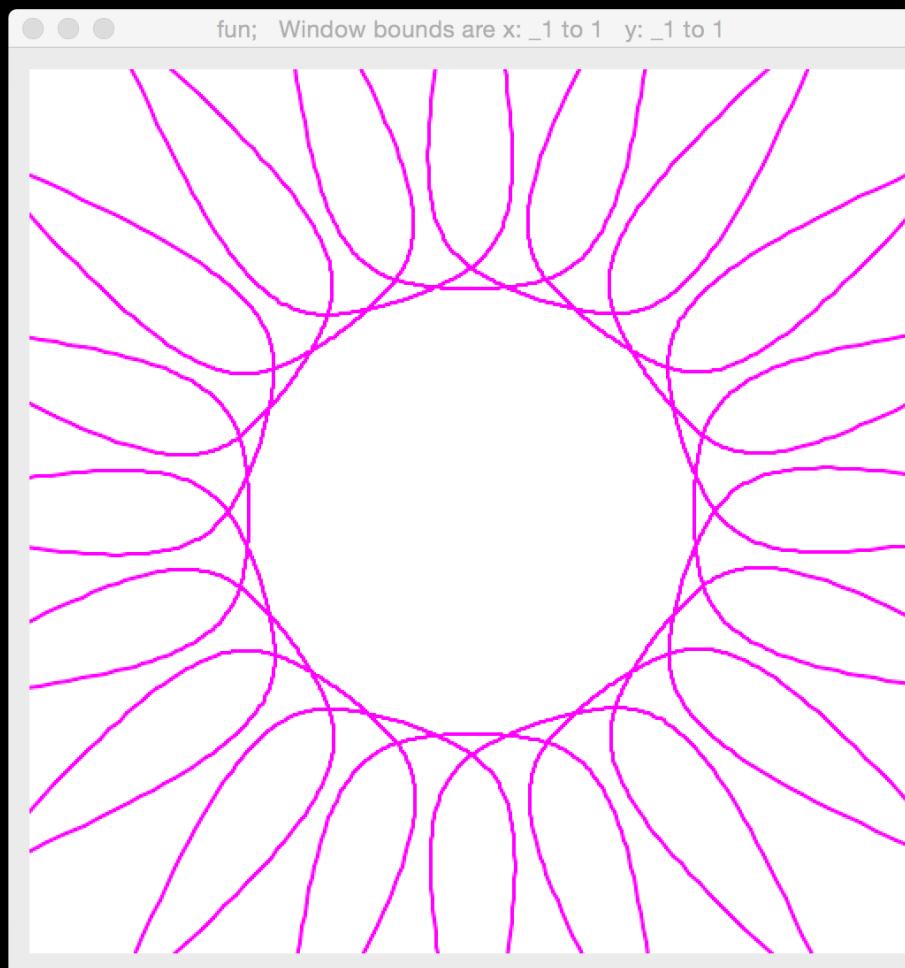
```
NB. define a verb for drawing curve with translate + rotate  
NB. use dyad form, x=translate, y=rotate  
dcurveRot =: dyad define  
255 0 255 dline curve mp (trans x) mp (rotm y)  
)  
dclear''  
0.5 0.2 dcurveRot 1r2p1  
0.5 0.2 dcurveRot 2r2p1  
0.5 0.2 dcurveRot 3r2p1  
0.5 0.2 dcurveRot 4r2p1
```



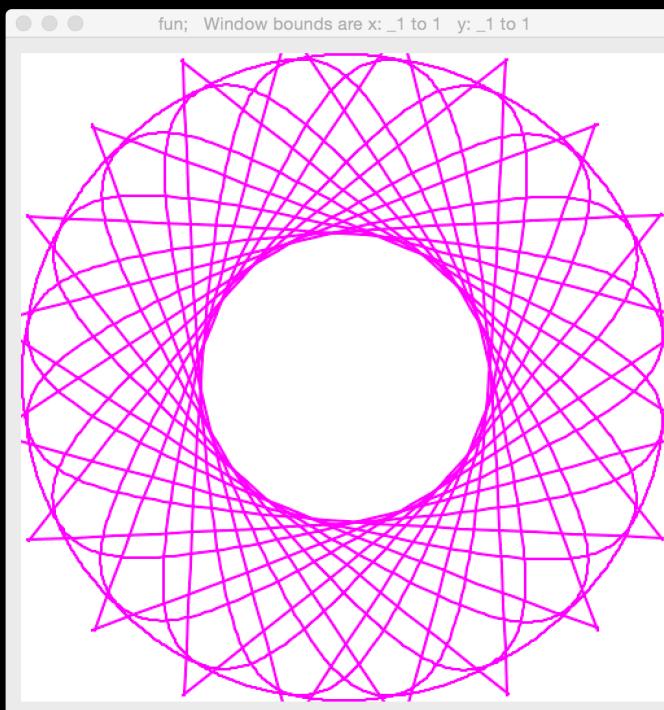
NB. draw many!

dclear''

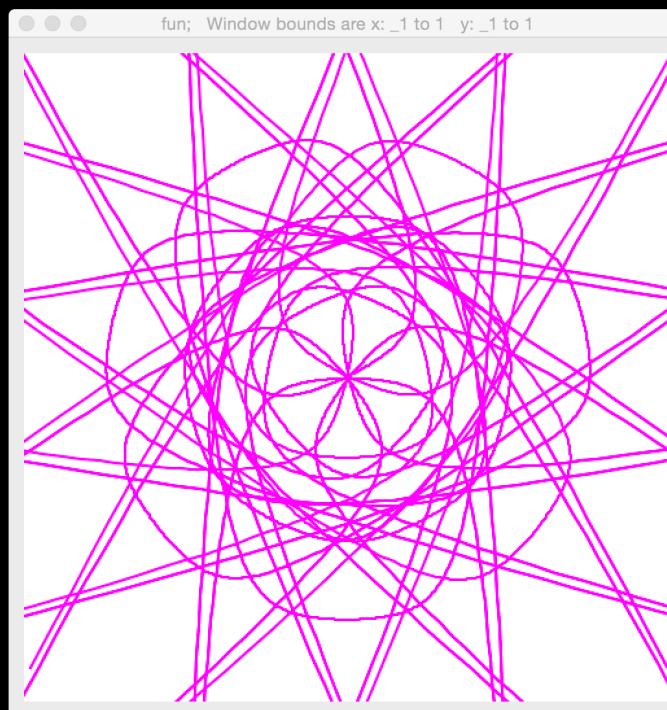
(0 0.5 & dcurveRot)"0 (1r10p1 * i.20)



```
NB. unrotate by pi as the last step before drawing,  
NB. and eliminate x-coordinate of translation parameter  
dcurveRot =: dyad define  
255 0 255 dline curve mp (rotm _1p1) mp (trans 0,x) mp (rotm y)  
)  
dclear''  
1 dcurveRot"0 (1r10p1 * i.20)
```



```
NB. generate 4 translations 0.25 apart  
translations =: 0.25 * i.4  
NB. generate 14 rotations 1/7 pi apart  
rotations =: 1r7p1 * i.14  
NB. draw each rotation/translation pairing (48 pairings)  
dclear''  
(48$translations) dcurveRot"0 (48$rotations)
```



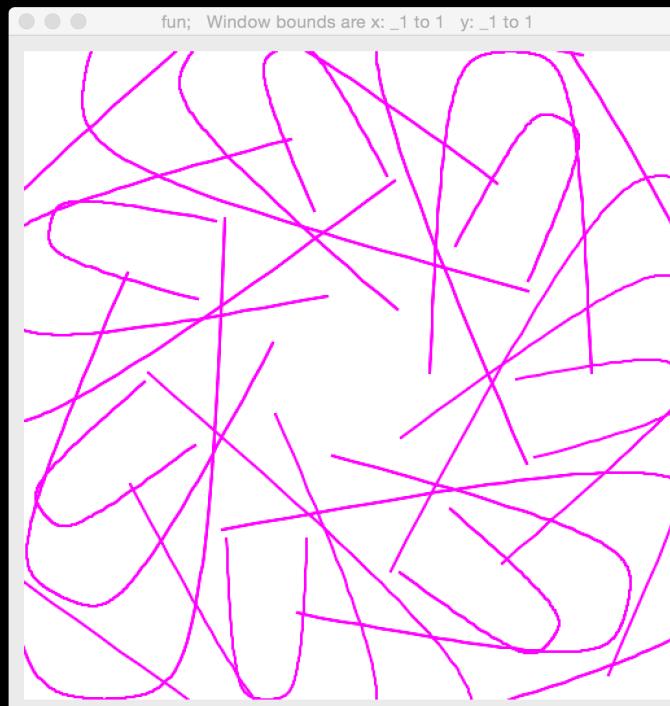
A scaling (zooming)
matrix can be defined as:

```
M = [ s  0  0  
      0  s  0  
      0  0  1 ]
```

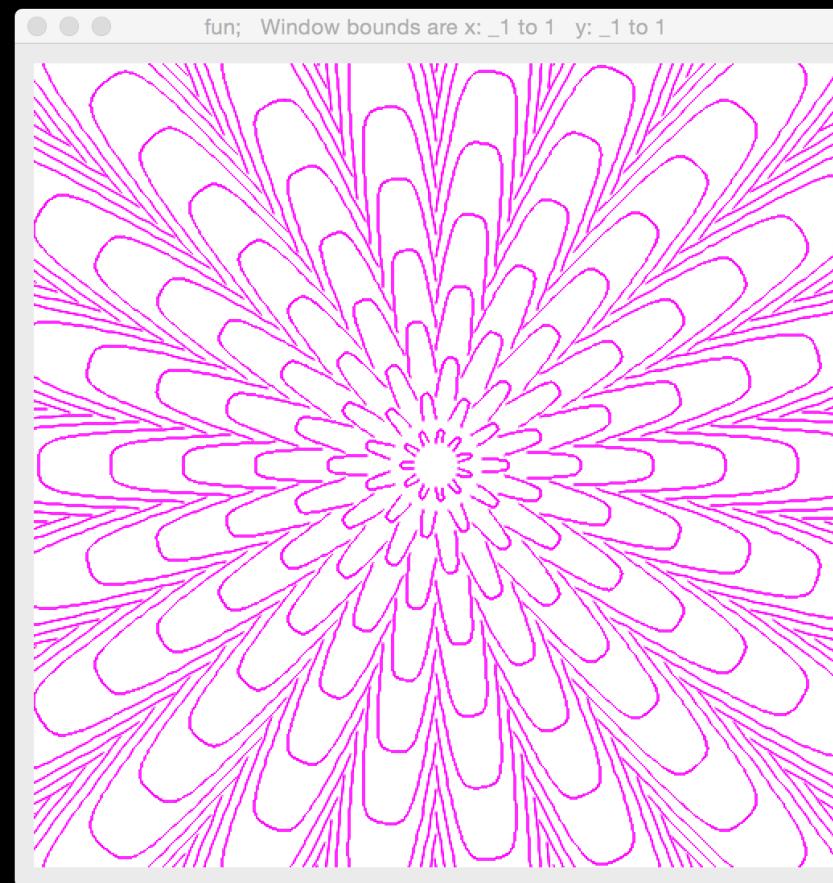
```
NB. scaling matrix as verb  
scale =: monad define  
  (y, 0 0), (0, y, 0), : 0 0 1  
  )  
  scale 5  
  5 0 0  
  0 5 0  
  0 0 1  
  (scale 5) mp (trans 5 2) mp (rotm 1r4p1)  
  3.53553 3.53553 0  
 _3.53553 3.53553 0  
 2.12132 4.94975 1  
  (3 2 1) mp (... above ...)  
  5.65685 22.6274 1
```

NB. update dcurveRot to use scale based on translation size

```
dcurveRot =: dyad define
m =. (scale x) mp (rotm _1p1) mp (trans x) mp (rotm y)
255 0 255 dline curve mp m
)
dclear'
(48$translations) dcurveRot"0 (48$rotations)
```



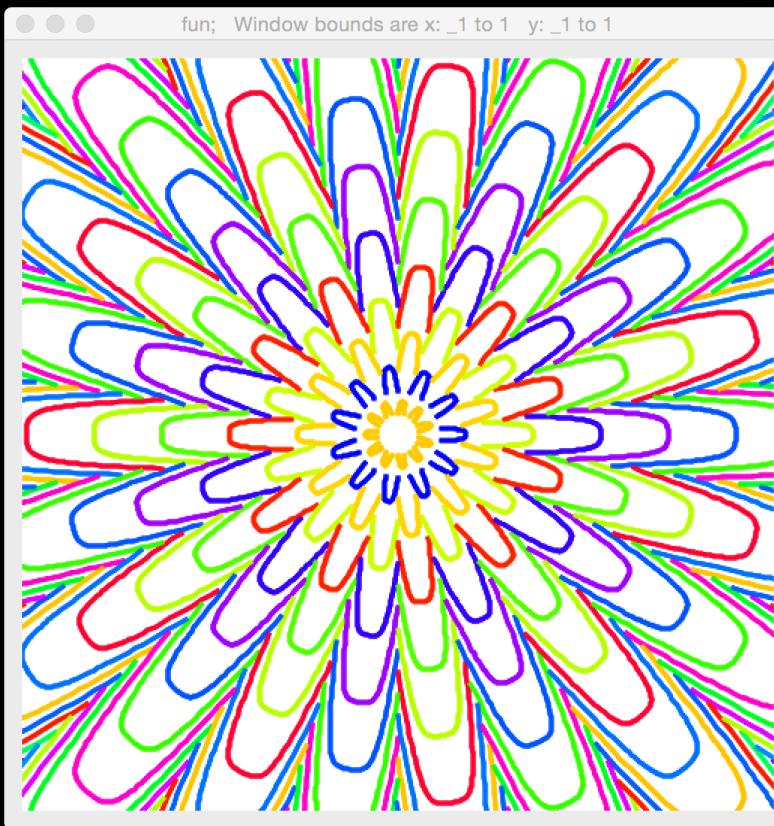
NB. update dcurveRot to use (scale 0.185*x) and
NB. obsessively fine-tune numbers to arrive at:
translations =: 0.09*i.50
rotations =: 1r22p1+1r11p1*i.22
(1100\$translations) dcurveRot"0 (1100\$rotations)



NB. next we need to set the color based on x;

NB. we'll use HSV scale for gradual color changes

```
dcurveRot =: dyad define  
m =. (scale 0.185*x) mp (rotm _1p1) mp (trans 0,x) mp (rotm y)  
(hsv2rgb ((360|90000*x^0.015),1.0 1.0 1.0)) dline curve mp m  
)
```

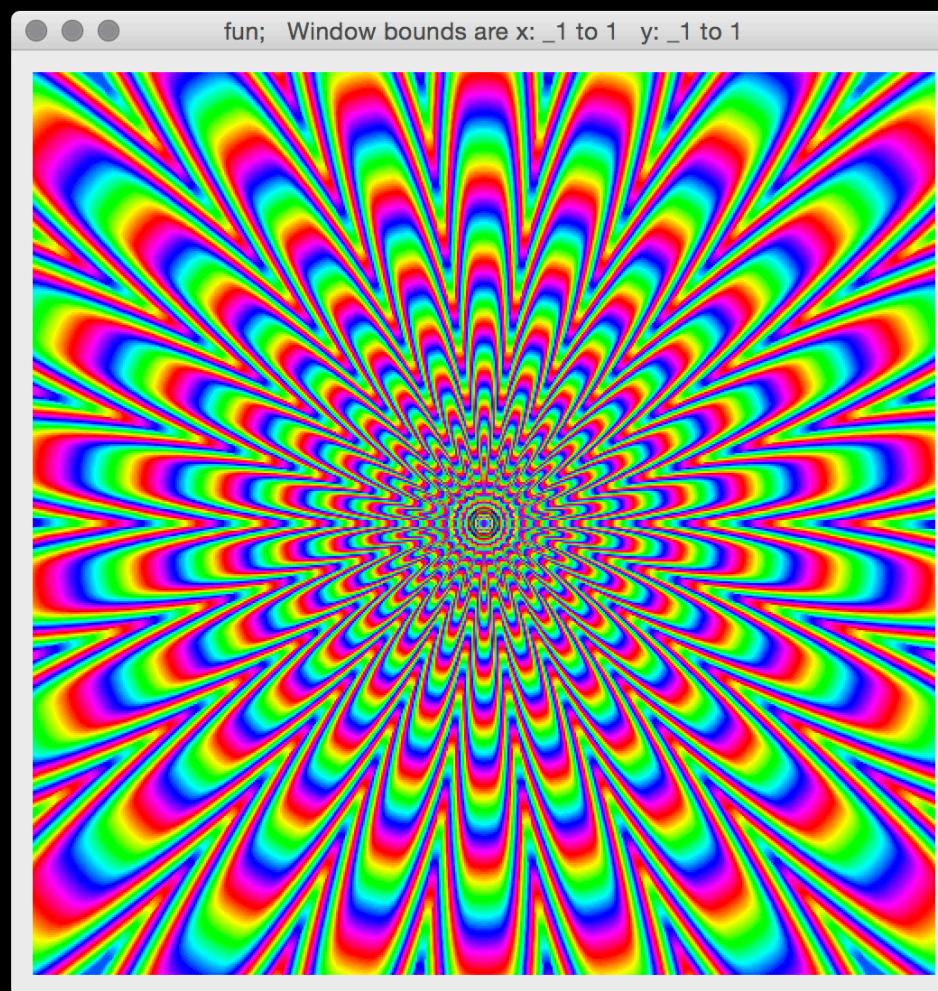


NB. MOAR CURVES

translations =: 0.005 * i.400

rotations =: 1r11p1*i.22

(22#translations) dcurveRot"0 (8800\$rotations)



NB. add those extra curves rotated $\pi/22$ and call it a day

