

Homework 3

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Problem 1

===== Part 1 =====

```
water = read.table(file = "~/Documents/Math189/water.txt", header = TRUE)
```

```
# we test if the concentration of Zinc in bottom water(m1)  
# and concentration of Zinc in surface water is the same(m2)  
# H0: m1 = m2  
# H1: m1 not= m2
```

```
# checking the summary statistics first  
summary(water)
```

```
##      bottom      surface  
## Min.   :0.2660   Min.    :0.2380  
## 1st Qu.:0.4845   1st Qu.:0.4103  
## Median :0.5780   Median :0.4690  
## Mean   :0.5649   Mean    :0.4845  
## 3rd Qu.:0.6930   3rd Qu.:0.6080  
## Max.   :0.7230   Max.    :0.6320
```

```
t.test(water$bottom, water$surface, paired = TRUE)
```

```
##  
## Paired t-test  
##  
## data: water$bottom and water$surface  
## t = 4.8638, df = 9, p-value = 0.0008911  
## alternative hypothesis: true difference in means is not equal to 0  
## 95 percent confidence interval:  
##  0.043006 0.117794  
## sample estimates:  
## mean of the differences  
##              0.0804
```

===== Part 2 =====

```
# I'm going to chose if out assumption failed the practice of  
# normality. Assumptions for ANOVA is considered a good and rigorous  
# rigoroust test against the normality of assumption. This means  
# if our assumption was violated in practice of normality,  
# meaning that this will tolerates the violations to its normality  
# assumption rather well. As regard with the normality of group data,  
# the Assumption for ANOVA can tolerate data that is-non normal or skewed  
# with only a small efect on the Type of I error in statistics.
```

Problem 2

===== Part 1 =====

```
#install.packages('HSAUR3')
library("HSAUR3")
```

```
## Loading required package: tools
##
## Attaching package: 'HSAUR3'
## The following object is masked _by_ '.GlobalEnv':
##
##      water
```

```
data("pottery")
class(pottery)
```

```
## [1] "data.frame"
```

```
v1 = data.frame(pottery[c(1)], pottery[c(10)])
v2 = data.frame(pottery[c(2)], pottery[c(10)])
v3 = data.frame(pottery[c(3)], pottery[c(10)])
v4 = data.frame(pottery[c(4)], pottery[c(10)])
v5 = data.frame(pottery[c(5)], pottery[c(10)])
v6 = data.frame(pottery[c(6)], pottery[c(10)])
v7 = data.frame(pottery[c(7)], pottery[c(10)])
v8 = data.frame(pottery[c(8)], pottery[c(10)])
v9 = data.frame(pottery[c(9)], pottery[c(10)])
```

```
anova1 = aov(Al2O3~kiln, data = v1)
anova2 = aov(Fe2O3~kiln, data = v2)
anova3 = aov(MgO~kiln, data = v3)
anova4 = aov(CaO~kiln, data = v4)
anova5 = aov(Na2O~kiln, data = v5)
anova6 = aov(K2O~kiln, data = v6)
anova7 = aov(TiO2~kiln, data = v7)
anova8 = aov(MnO~kiln, data = v8)
anova9 = aov(BaO~kiln, data = v9)
```

===== Part 2 =====

```
p.adjust(anova1$residuals, method = "bonferroni")
```

```
##      1      2      3      4      5
## 1.0000000 -0.8571429 1.0000000 -0.8571429 1.0000000
##      6      7      8      9     10
## 1.0000000 -18.8571429 1.0000000 -50.3571429 -104.3571429
##     11     12     13     14     15
## -144.8571429 -104.3571429 -95.3571429 1.0000000 -5.3571429
##     16     17     18     19     20
## -50.3571429 1.0000000 -0.8571429 1.0000000 1.0000000
##     21     22     23     24     25
## 1.0000000 1.0000000 1.0000000 1.0000000 -47.6250000
##     26     27     28     29     30
## 1.0000000 -74.6250000 -110.6250000 -43.1250000 -65.6250000
```

```
##          31          32          33          34          35
##  1.0000000 -7.1250000  1.0000000 -4.5000000  1.0000000
##          36          37          38          39          40
##  1.0000000 -107.1000000 -8.1000000 -8.1000000  1.0000000
##          41          42          43          44          45
##  1.0000000  1.0000000 -27.9000000 -113.4000000  1.0000000
```

```
p.adjust(anova2$residuals, method = "bonferroni")
```

```
##          1          2          3          4          5          6
##  1.0000000 -4.4357143  1.0000000 -6.2357143 -8.4857143  0.9642857
##          7          8          9         10         11         12
## -17.0357143 -0.3857143 -12.5357143 -25.1357143 -71.9357143 -30.0857143
##          13         14         15         16         17         18
## -16.1357143  1.0000000  1.0000000  1.0000000  1.0000000  1.0000000
##          19         20         21         22         23         24
##  1.0000000  1.0000000 -6.6857143  1.0000000  1.0000000  1.0000000
##          25         26         27         28         29         30
##  1.0000000  1.0000000 -3.6000000 -93.6000000 -25.2000000 -38.2500000
##          31         32         33         34         35         36
##  1.0000000 -9.4500000  1.0000000 -1.1250000  1.0000000 -19.4400000
##          37         38         39         40         41         42
##  1.0000000 -9.5400000  1.0000000 -9.0900000 -17.6400000 -16.7400000
##          43         44         45
## -26.6400000  1.0000000  1.0000000
```

```
p.adjust(anova3$residuals, method = "bonferroni")
```

```
##          1          2          3          4          5          6
##  1.0000000 -8.6571429 -1.0071429 -12.7071429 -0.5571429  1.0000000
##          7          8          9         10         11         12
## -1.4571429  1.0000000 -10.0071429 -7.7571429 -15.4071429 -9.5571429
##          13         14         15         16         17         18
## -10.0071429  1.0000000  0.7928571  1.0000000  1.0000000 -0.5571429
##          19         20         21         22         23         24
##  1.0000000  1.0000000  1.0000000 -28.4250000 -67.5750000 -47.3250000
##          25         26         27         28         29         30
##  1.0000000  1.0000000 -65.7750000 -30.2250000  1.0000000 -18.5250000
##          31         32         33         34         35         36
##  1.0000000  1.0000000  1.0000000 -3.8250000  1.0000000 -0.1800000
##          37         38         39         40         41         42
## -1.9800000 -0.1800000  0.2700000  1.0000000 -2.0700000  1.0000000
##          43         44         45
## -3.4200000  1.0000000 -0.2700000
```

```
p.adjust(anova4$residuals, method = "bonferroni")
```

```
##          1          2          3          4          5          6
## -6.7071429 -4.4571429 -7.6071429 -8.0571429 -0.8571429 -3.1071429
##          7          8          9         10         11         12
##  1.0000000  1.0000000 -10.3071429 -8.0571429 -12.5571429  1.0000000
##          13         14         15         16         17         18
##  1.0000000 -4.9071429 -4.4571429 -5.8071429 -3.1071429  1.0000000
##          19         20         21         22         23         24
## -4.9071429 -11.2071429 -5.8071429 -2.2875000 -3.6375000 -3.1875000
##          25         26         27         28         29         30
```

```
## -1.8375000 -0.0375000 -1.3875000 -0.0375000 -0.9375000 1.0000000
##          31          32          33          34          35          36
##  1.0000000  0.8625000  1.0000000 -0.2250000  0.2250000  0.1800000
##          37          38          39          40          41          42
## -0.7200000 -0.7200000 -0.7200000  1.0000000  0.3600000  0.3600000
##          43          44          45
## -1.8900000 -0.9900000  1.0000000
```

```
p.adjust(anova5$residuals, method = "bonferroni")
```

```
##          1          2          3          4          5          6
##  1.0000000  1.0000000  1.0000000  1.0000000  1.0000000 -4.3071429
##          7          8          9         10         11         12
## -0.7071429 -2.9571429  1.0000000 -0.7071429 -9.7071429 -6.5571429
##          13         14         15         16         17         18
## -4.7571429  1.0000000  1.0000000  1.0000000  1.0000000  1.0000000
##          19         20         21         22         23         24
## -9.7071429 -10.1571429 -7.4571429  1.0000000 -3.8250000 -2.4750000
##          25         26         27         28         29         30
## -5.1750000 -2.4750000 -1.5750000 -3.3750000 -4.2750000  1.0000000
##          31         32         33         34         35         36
## -2.4750000  1.0000000 -0.6750000  0.4500000 -0.4500000 -1.0800000
##          37         38         39         40         41         42
## -0.6300000  0.2700000 -0.6300000  1.0000000  0.5400000  0.0900000
##          43         44         45
##  0.0900000  0.0900000 -0.8100000
```

```
p.adjust(anova6$residuals, method = "bonferroni")
```

```
##          1          2          3          4          5          6
##  1.0000000 -2.3785714 -1.4785714 -2.3785714  0.7714286  1.0000000
##          7          8          9         10         11         12
##  1.0000000  1.0000000  1.0000000 -1.9285714 -38.3785714 -3.7285714
##          13         14         15         16         17         18
## -3.2785714  1.0000000 -7.7785714  1.0000000  1.0000000 -0.5785714
##          19         20         21         22         23         24
##  1.0000000  1.0000000  1.0000000  1.0000000  0.7500000  1.0000000
##          25         26         27         28         29         30
## -10.5000000  1.0000000 -32.5500000 -36.1500000 -19.0500000 -4.2000000
##          31         32         33         34         35         36
##  1.0000000  1.0000000  1.0000000 -2.9250000  1.0000000 -5.2200000
##          37         38         39         40         41         42
## -6.1200000  1.0000000 -3.4200000  1.0000000  1.0000000  1.0000000
##          43         44         45
## -9.2700000  1.0000000 -9.7200000
```

```
p.adjust(anova7$residuals, method = "bonferroni")
```

```
##          1          2          3          4          5          6
##  1.0000000  1.0000000  1.0000000  1.0000000 -0.3428571  1.0000000
##          7          8          9         10         11         12
##  0.5571429  1.0000000 -0.3428571 -1.2428571 -8.4428571 -3.0428571
##          13         14         15         16         17         18
## -3.4928571 -0.3428571  0.1071429  1.0000000  1.0000000  0.5571429
##          19         20         21         22         23         24
##  1.0000000 -0.3428571 -1.6928571  1.0000000  1.0000000  1.0000000
```

```
##          25          26          27          28          29          30
## -0.4875000  0.4125000 -1.8375000 -4.9875000 -2.2875000 -3.1875000
##          31          32          33          34          35          36
## -0.4875000 -0.0375000  0.8625000 -0.6750000  0.6750000 -17.8200000
##          37          38          39          40          41          42
##  1.0000000 -5.6700000  1.0000000  1.0000000 -9.1800000 -4.6800000
##          43          44          45
## -3.7800000  1.0000000  1.0000000
```

```
p.adjust(anova8$residuals, method = "bonferroni")
```

```
##          1          2          3          4          5          6
##  0.26357143 -0.18642857  0.71357143 -0.36642857 -0.45642857  0.03857143
##          7          8          9         10         11         12
## -0.23142857  0.03857143 -0.41142857 -0.72642857 -1.67142857 -0.72642857
##          13         14         15         16         17         18
##  0.39857143  0.84857143  1.00000000  1.00000000  0.44357143  0.93857143
##          19         20         21         22         23         24
##  0.03857143 -1.62642857 -0.18642857  1.00000000  1.00000000  0.13500000
##          25         26         27         28         29         30
## -1.53000000 -0.90000000 -0.54000000  1.00000000 -1.75500000 -1.84500000
##          31         32         33         34         35         36
##  1.00000000  1.00000000 -1.21500000  0.56250000 -0.56250000 -0.05400000
##          37         38         39         40         41         42
## -0.05400000 -0.05400000  0.17100000 -0.00900000 -0.14400000  0.08100000
##          43         44         45
## -0.00900000 -0.05400000  0.12600000
```

```
p.adjust(anova9$residuals, method = "bonferroni")
```

```
##          1          2          3          4          5
## -0.096428571  0.038571429 -0.141428571  0.083571429  0.083571429
##          6          7          8          9         10
## -0.006428571  0.083571429 -0.006428571 -0.006428571 -0.231428571
##          11         12         13         14         15
## -0.231428571 -0.051428571 -0.051428571  0.128571429  0.128571429
##          16         17         18         19         20
##  0.083571429  0.038571429  0.263571429 -0.096428571 -0.006428571
##          21         22         23         24         25
## -0.006428571  0.123750000  0.168750000  0.123750000 -0.326250000
##          26         27         28         29         30
##  0.213750000 -0.281250000  0.033750000 -0.056250000 -0.011250000
##          31         32         33         34         35
##  0.033750000 -0.056250000  0.033750000  0.045000000 -0.045000000
##          36         37         38         39         40
## -0.108000000 -0.108000000 -0.018000000  0.252000000 -0.018000000
##          41         42         43         44         45
## -0.117000000  0.153000000 -0.117000000 -0.027000000  0.108000000
```

```
===== Part 3 =====
```

```
p.adjust(anova1$residuals, method = "hochberg")
```

```
##          1          2          3          4          5
##  1.00000000 -0.4761905  1.0000000 -0.4571429  1.0000000
##          6          7          8          9         10
##  1.00000000 -12.9904762  1.0000000 -39.1666667 -92.7619048
```

```
##          11          12          13          14          15
## -144.8571429 -95.0809524 -82.6428571  1.0000000 -3.2142857
##          16          17          18          19          20
## -40.2857143  1.0000000 -0.4380952  1.0000000  1.0000000
##          21          22          23          24          25
##  1.0000000  1.0000000  1.0000000  1.0000000 -35.9833333
##          26          27          28          29          30
##  1.0000000 -63.0166667 -105.7083333 -31.6250000 -53.9583333
##          31          32          33          34          35
##  1.0000000 -4.4333333  1.0000000 -2.6000000  1.0000000
##          36          37          38          39          40
##  1.0000000 -99.9600000 -5.2200000 -5.4000000  1.0000000
##          41          42          43          44          45
##  1.0000000  1.0000000 -19.8400000 -110.8800000  1.0000000
```

```
p.adjust(anova2$residuals, method = "hochberg")
```

```
##          1          2          3          4          5          6
##  1.0000000 -2.5628571  1.0000000 -3.7414286 -5.4685714  0.4714286
##          7          8          9         10         11         12
## -13.6285714 -0.1971429 -9.1928571 -21.7842857 -70.3371429 -28.0800000
##          13         14         15         16         17         18
## -12.1914286  1.0000000  1.0000000  1.0000000  1.0000000  1.0000000
##          19         20         21         22         23         24
##  1.0000000  1.0000000 -4.1600000  1.0000000  1.0000000  1.0000000
##          25         26         27         28         29         30
##  0.6000000  1.0000000 -2.0000000 -93.6000000 -22.4000000 -36.5500000
##          31         32         33         34         35         36
##  1.0000000 -6.5100000  1.0000000 -0.6000000  0.5250000 -16.4160000
##          37         38         39         40         41         42
##  1.0000000 -6.7840000  1.0000000 -6.0600000 -14.5040000 -13.0200000
##          43         44         45
## -24.2720000  1.0000000  1.0000000
```

```
p.adjust(anova3$residuals, method = "hochberg")
```

```
##          1          2          3          4          5          6
##  1.0000000 -6.5409524 -0.6042857 -10.7304762 -0.3219048  1.0000000
##          7          8          9         10         11         12
## -0.9066667  1.0000000 -8.0057143 -5.6885714 -13.3528571 -7.4333333
##          13         14         15         16         17         18
## -8.2280952  1.0000000  0.3523810  1.0000000  1.0000000 -0.3095238
##          19         20         21         22         23         24
##  1.0000000  1.0000000  1.0000000 -25.8983333 -67.5750000 -45.2216667
##          25         26         27         28         29         30
##  1.0000000  1.0000000 -64.3133333 -28.2100000  1.0000000 -16.4666667
##          31         32         33         34         35         36
##  1.0000000  1.0000000  1.0000000 -2.7200000  1.0000000 -0.0880000
##          37         38         39         40         41         42
## -1.2760000 -0.0920000  0.1260000  0.8740000 -1.3800000  1.0000000
##          43         44         45
## -2.3560000  1.0000000 -0.1440000
```

```
p.adjust(anova4$residuals, method = "hochberg")
```

```
##          1          2          3          4          5
```

```
## -5.81285714 -3.36761905 -6.76190476 -7.52000000 -0.41904762
##          6          7          8          9         10
## -2.00238095  0.79095238  0.48761905 -9.84904762 -7.34095238
##          11         12         13         14         15
## -12.55714286  0.79095238  0.79095238 -3.81666667 -3.26857143
##          16         17         18         19         20
## -4.77476190 -2.07142857  0.79095238 -3.92571429 -10.95809524
##          21         22         23         24         25
## -4.90380952 -1.42333333 -2.58666667 -2.19583333 -1.06166667
##          26         27         28         29         30
## -0.01333333 -0.77083333 -0.01416667 -0.47916667  0.53500000
##          31         32         33         34         35
##  0.53500000  0.21083333  0.54583333 -0.09000000  0.07000000
##          36         37         38         39         40
##  0.06000000 -0.30400000 -0.32000000 -0.33600000  0.43200000
##          41         42         43         44         45
##  0.09600000  0.09600000 -1.13400000 -0.52800000  0.43200000
```

```
p.adjust(anova5$residuals, method = "hochberg")
```

```
##          1          2          3          4          5          6
##  0.4342857  0.4342857  0.4342857  0.4342857  0.4842857 -3.6371429
##          7          8          9         10         11         12
## -0.4085714 -2.2342857  0.4342857 -0.4242857 -9.2757143 -5.9742857
##          13         14         15         16         17         18
## -4.1228571  0.4842857  0.4842857  0.4842857  0.4342857  0.4842857
##          19         20         21         22         23         24
## -9.4914286 -10.1571429 -6.9600000  0.4842857 -3.0600000 -1.7050000
##          25         26         27         28         29         30
## -4.6000000 -1.7600000 -1.0500000 -2.6250000 -3.5150000  0.4342857
##          31         32         33         34         35         36
## -1.8150000  0.4842857 -0.3750000  0.1700000 -0.2200000 -0.6960000
##          37         38         39         40         41         42
## -0.3220000  0.1080000 -0.3360000  0.4342857  0.1920000  0.0380000
##          43         44         45
##  0.0380000  0.0380000 -0.5040000
```

```
p.adjust(anova6$residuals, method = "hochberg")
```

```
##          1          2          3          4          5          6
##  0.7666667 -1.5328571 -0.8871429 -1.5857143  0.4114286  0.7666667
##          7          8          9         10         11         12
##  0.7666667  0.7666667  0.7666667 -1.2000000 -38.3785714 -2.8171429
##          13         14         15         16         17         18
## -2.3314286  0.6242857 -6.5685714  0.7666667  0.7666667 -0.3342857
##          19         20         21         22         23         24
##  0.7666667  0.7666667  0.7666667  0.7666667  0.4114286  0.7666667
##          25         26         27         28         29         30
## -9.5666667  0.7666667 -31.1033333 -35.3466667 -17.7800000 -3.2666667
##          31         32         33         34         35         36
##  0.7666667  0.7666667  0.7666667 -2.0150000  0.7666667 -4.1760000
##          37         38         39         40         41         42
## -5.0320000  0.7480000 -2.5080000  0.7666667  0.7666667  0.7666667
##          43         44         45
## -8.0340000  0.7666667 -8.6400000
```

```
p.adjust(anova7$residuals, method = "hochberg")
```

```
##           1           2           3           4           5           6
##  0.3460000  0.3460000  0.3460000  0.3460000 -0.2133333  0.3460000
##           7           8           9          10          11          12
##  0.2476190  0.3460000 -0.1904762 -0.8838095 -8.0676190 -2.4342857
##          13          14          15          16          17          18
## -2.9495238 -0.1980952  0.0547619  0.3460000  0.3460000  0.2476190
##          19          20          21          22          23          24
##  0.3460000 -0.2057143 -1.2414286  0.3460000  0.3460000  0.3460000
##          25          26          27          28          29          30
## -0.3141667  0.2016667 -1.3883333 -4.5441667 -1.7791667 -2.6208333
##          31          32          33          34          35          36
## -0.3250000 -0.0200000  0.3450000 -0.4650000  0.2850000 -17.8200000
##          37          38          39          40          41          42
##  0.3460000 -5.2920000  0.3460000  0.3460000 -8.9760000 -4.1600000
##          43          44          45
## -3.2760000  0.3460000  0.3460000
```

```
p.adjust(anova8$residuals, method = "hochberg")
```

```
##           1           2           3           4           5           6
##  0.04200000 -0.12014286  0.04200000 -0.26057143 -0.34485714  0.01628571
##           7           8           9          10          11          12
## -0.15942857  0.01628571 -0.30171429 -0.59728571 -1.59714286 -0.61342857
##          13          14          15          16          17          18
##  0.04200000  0.04200000  0.04200000  0.04200000  0.04200000  0.04200000
##          19          20          21          22          23          24
##  0.01628571 -1.51800000 -0.12428571  0.04200000  0.04200000  0.04200000
##          25          26          27          28          29          30
## -1.39400000 -0.78000000 -0.42000000  0.04200000 -1.71600000 -1.84500000
##          31          32          33          34          35          36
##  0.04200000  0.04200000 -1.08000000  0.04200000 -0.45000000 -0.02880000
##          37          38          39          40          41          42
## -0.03000000 -0.03120000  0.04200000 -0.00440000 -0.08960000  0.03240000
##          43          44          45
## -0.00460000 -0.03240000  0.04200000
```

```
p.adjust(anova9$residuals, method = "hochberg")
```

```
##           1           2           3           4           5
## -0.077142857  0.005857143 -0.128857143  0.005857143  0.005857143
##           6           7           8           9          10
## -0.003000000  0.005857143 -0.003142857 -0.003285714 -0.216000000
##          11          12          13          14          15
## -0.221142857 -0.035428571 -0.036571429  0.005857143  0.005857143
##          16          17          18          19          20
##  0.005857143  0.005857143  0.005857143 -0.075000000 -0.003428571
##          21          22          23          24          25
## -0.003571429  0.005857143  0.005857143  0.005857143 -0.326250000
##          26          27          28          29          30
##  0.005857143 -0.275000000  0.005857143 -0.041250000 -0.006500000
##          31          32          33          34          35
##  0.005857143 -0.042500000  0.005857143  0.005857143 -0.030000000
##          36          37          38          39          40
```



```
## -0.088800000 -0.091200000 -0.010800000 0.005857143 -0.011200000
##          41          42          43          44          45
## -0.101400000 0.005857143 -0.104000000 -0.017400000 0.005857143
```