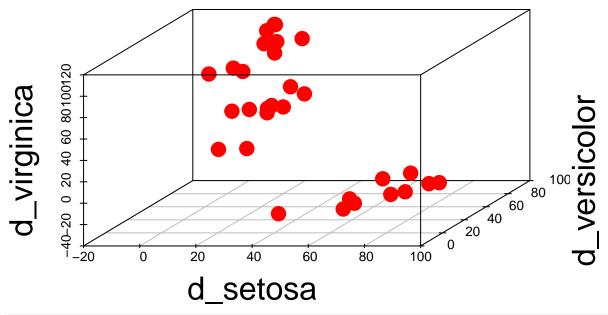
Homework 4

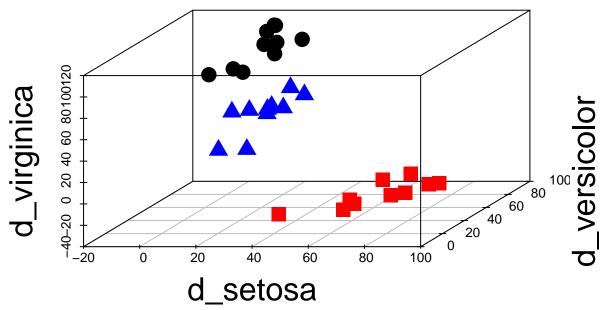
Joshua Oswari - A14751270 5/1/2019

Problem 1

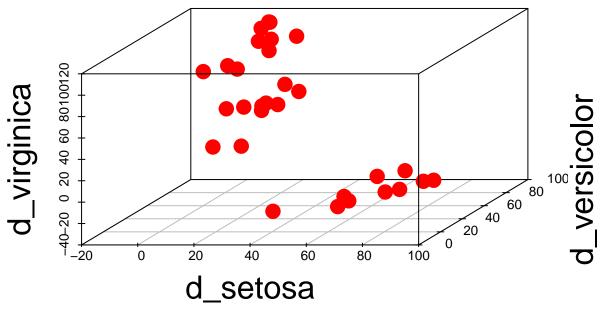
```
data = read.csv(file = "~/Documents/Math189/iris.csv", header = TRUE, fill = TRUE)
iris = data[,2:6]
#Divide data into train and test
train=iris[c(1:40,51:90, 101:140),]
test1=iris[c(41:50,91:100, 141:150),]
#Sample size
n_{setosa=40}
n versicolor=40
n_virginica=40
#Prior=relative sample size in train data
#1st prior
p_setosa1=0.8
p_versicolor1=0.1
p_virginica1=0.1
Mean_setosa=colMeans(train[1:40,1:4])
Mean_versicolor=colMeans(train[41:80,1:4])
Mean_virginica=colMeans(train[81:120,1:4])
#Sample variance-covariance matrix for each species
S_setosa=cov(train[1:40,1:4])
S_versicolor=cov(train[41:80,1:4])
S_virginica=cov(train[81:120,1:4])
#Complete fomula
S_pooled= ((n_setosa-1)*S_setosa+(n_versicolor-1)*S_versicolor+(n_virginica-1)*S_virginica)/(n_setosa+n
S_inv=solve(S_pooled)
########### Calculate alpha_i ##############
alpha setosa = -0.5* t(Mean setosa) %*% S inv %*% Mean setosa + log(p setosa1)
alpha_versicolor= -0.5* t(Mean_versicolor) %*% S_inv %*% Mean_versicolor + log(p_versicolor1)
alpha_virginica= -0.5* t(Mean_virginica) %*% S_inv %*% Mean_virginica + log(p_virginica1)
```

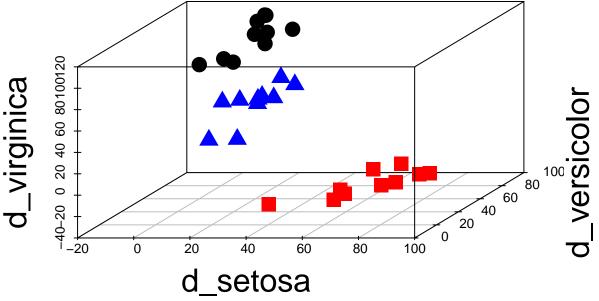
```
beta setosa=S inv ** Mean setosa
beta_versicolor=S_inv %*% Mean_versicolor
beta_virginica=S_inv %*% Mean_virginica
prediction=c()
d_setosa_vec=c()
d_versicolor_vec=c()
d_virginica_vec=c()
label=c("setosa", "versicolor", "virginica")
for(i in 1:nrow(test1)){
  #Read an observation in test data
  x=t(test1[i,1:4])
  #Calculate linear discriminant functions for each species
  d_setosa=alpha_setosa+ t(beta_setosa) %*% x
  d_versicolor=alpha_versicolor+ t(beta_versicolor) %*% x
  d_virginica=alpha_virginica+ t(beta_virginica) %*% x
  #Classify the observation to the species with highest function value
  d_vec=c(d_setosa, d_versicolor, d_virginica)
  prediction=append(prediction, label[which.max( d_vec )])
 d_setosa_vec=append(d_setosa_vec, d_setosa)
 d_versicolor_vec=append(d_versicolor_vec, d_versicolor)
 d_virginica_vec=append(d_virginica_vec, d_virginica)
#Combine the predicted results to the test dataset.
test1$prediction=prediction
#3D scatter plot
library("scatterplot3d")
col_vec=c(rep("red", 10), rep("blue", 10), rep("black", 10))
pch_vec=c(rep(15, 10), rep(17, 10), rep(19, 10))
scatterplot3d(x = d_setosa_vec, y = d_versicolor_vec, z=d_virginica_vec,
             xlab = "d_setosa", ylab = "d_versicolor", zlab="d_virginica",
             color="red", pch=19, angle = 55 , cex.symbols=2, cex.lab=2
```





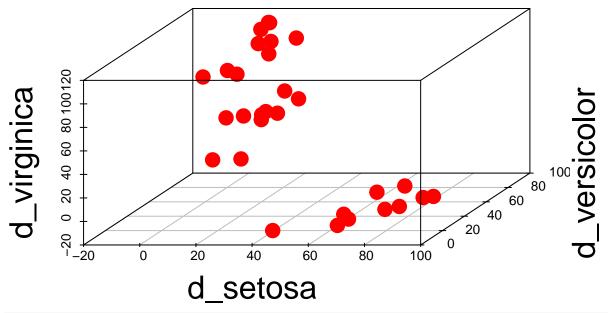
```
p_setosa2=0.1
p_versicolor2=0.8
p_virginica2=0.1
Mean_setosa=colMeans(train[1:40,1:4])
Mean_versicolor=colMeans(train[41:80,1:4])
Mean_virginica=colMeans(train[81:120,1:4])
#Sample variance-covariance matrix for each species
S_setosa=cov(train[1:40,1:4])
S_versicolor=cov(train[41:80,1:4])
S_virginica=cov(train[81:120,1:4])
#Complete fomula
S_pooled= ((n_setosa-1)*S_setosa+(n_versicolor-1)*S_versicolor+(n_virginica-1)*S_virginica)/(n_setosa+n
S_inv=solve(S_pooled)
alpha_setosa = -0.5* t(Mean_setosa) %*% S_inv %*% Mean_setosa + log(p_setosa2)
alpha_versicolor= -0.5* t(Mean_versicolor) %*% S_inv %*% Mean_versicolor + log(p_versicolor2)
alpha_virginica = -0.5* t(Mean_virginica) %*% S_inv %*% Mean_virginica + log(p_virginica2)
beta_setosa=S_inv ** Mean_setosa
beta_versicolor=S_inv %*% Mean_versicolor
beta_virginica=S_inv %*% Mean_virginica
prediction=c()
d_setosa_vec=c()
d_versicolor_vec=c()
d_virginica_vec=c()
label=c("setosa", "versicolor", "virginica")
for(i in 1:nrow(test2)){
 #Read an observation in test data
 x=t(test2[i,1:4])
 #Calculate linear discriminant functions for each species
 d_setosa=alpha_setosa+ t(beta_setosa) %*% x
 d_versicolor=alpha_versicolor+ t(beta_versicolor) %*% x
 d_virginica=alpha_virginica+ t(beta_virginica) %*% x
 #Classify the observation to the species with highest function value
 d_vec=c(d_setosa, d_versicolor, d_virginica)
 prediction=append(prediction, label[which.max( d_vec )])
 d_setosa_vec=append(d_setosa_vec, d_setosa)
```

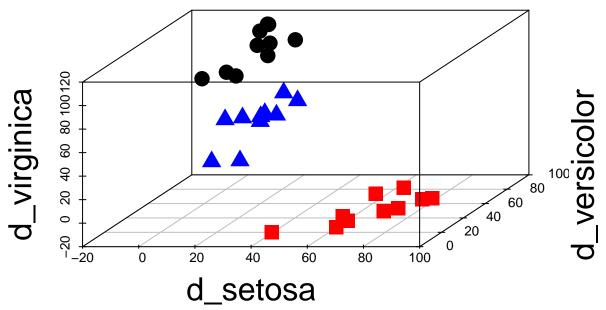




```
#----- 3rd Prior
#Divide data into train and test
train=iris[c(1:40,51:90, 101:140),]
test3=iris[c(41:50,91:100, 141:150),]
#Prior=relative sample size in train data
#3rd prior
p_setosa3=0.1
p_versicolor3=0.1
p_virginica3=0.8
########## Calculate sample mean vectors ##############
Mean_setosa=colMeans(train[1:40,1:4])
Mean_versicolor=colMeans(train[41:80,1:4])
Mean_virginica=colMeans(train[81:120,1:4])
#Sample variance-covariance matrix for each species
S setosa=cov(train[1:40,1:4])
S_versicolor=cov(train[41:80,1:4])
S_virginica=cov(train[81:120,1:4])
#Complete fomula
S_pooled= ((n_setosa-1)*S_setosa+(n_versicolor-1)*S_versicolor+(n_virginica-1)*S_virginica)/(n_setosa+n
S_inv=solve(S_pooled)
alpha_setosa= -0.5* t(Mean_setosa) %*% S_inv %*% Mean_setosa + log(p_setosa3)
alpha_versicolor= -0.5* t(Mean_versicolor) %*% S_inv %*% Mean_versicolor + log(p_versicolor3)
alpha_virginica = -0.5* t(Mean_virginica) %*% S_inv %*% Mean_virginica + log(p_virginica3)
```

```
beta setosa=S inv ** Mean setosa
beta_versicolor=S_inv %*% Mean_versicolor
beta_virginica=S_inv %*% Mean_virginica
prediction=c()
d_setosa_vec=c()
d_versicolor_vec=c()
d_virginica_vec=c()
label=c("setosa", "versicolor", "virginica")
for(i in 1:nrow(test3)){
  #Read an observation in test data
  x=t(test3[i,1:4])
  #Calculate linear discriminant functions for each species
  d_setosa=alpha_setosa+ t(beta_setosa) %*% x
  d_versicolor=alpha_versicolor+ t(beta_versicolor) %*% x
  d_virginica=alpha_virginica+ t(beta_virginica) %*% x
  #Classify the observation to the species with highest function value
  d_vec=c(d_setosa, d_versicolor, d_virginica)
  prediction=append(prediction, label[which.max( d_vec )])
 d_setosa_vec=append(d_setosa_vec, d_setosa)
 d_versicolor_vec=append(d_versicolor_vec, d_versicolor)
 d_virginica_vec=append(d_virginica_vec, d_virginica)
#Combine the predicted results to the test dataset.
test3$prediction=prediction
#3D scatter plot
library("scatterplot3d")
col_vec=c(rep("red", 10), rep("blue", 10), rep("black", 10))
pch_vec=c(rep(15, 10), rep(17, 10), rep(19, 10))
scatterplot3d(x = d_setosa_vec, y = d_versicolor_vec, z=d_virginica_vec,
             xlab = "d_setosa", ylab = "d_versicolor", zlab="d_virginica",
             color="red", pch=19, angle = 55 , cex.symbols=2, cex.lab=2
```





```
# Report:
# No, the LDA Method is not sensitive to the choices of prior
# between all those three tests, we get the same answer between
# the species and predicition.
```

```
#Sample size
n_{setosa=30}
n_versicolor=30
n_virginica=30
#Prior=relative sample size in train data
p setosa=n setosa/90
p_versicolor=n_versicolor/90
p_virginica=n_virginica/90
########## Calculate sample mean vectors ##############
Mean_setosa=colMeans(train1[1:30,1:4])
Mean_versicolor=colMeans(train1[31:60,1:4])
Mean_virginica=colMeans(train1[61:90,1:4])
#Sample variance-covariance matrix for each species
S_setosa=cov(train1[1:30,1:4])
S_versicolor=cov(train1[31:60,1:4])
S_virginica=cov(train1[61:90,1:4])
#Complete fomula
S_{pooled} = ((n_{setosa-1})*S_{setosa+(n_{versicolor-1})*S_{versicolor+(n_{virginica-1})*S_{virginica})/(n_{setosa+n_{versicolor-1})} 
S_inv=solve(S_pooled)
#Simple way
\#S\_pooled = (S\_setosa + S\_versicolor + S\_virginica)/3
############ Calculate alpha_i ##############
alpha_setosa= -0.5* t(Mean_setosa) %*% S_inv %*% Mean_setosa
alpha_versicolor= -0.5* t(Mean_versicolor) %*% S_inv %*% Mean_versicolor
alpha_virginica= -0.5* t(Mean_virginica) %*% S_inv %*% Mean_virginica
beta_setosa=S_inv ** Mean_setosa
beta_versicolor=S_inv %*% Mean_versicolor
beta_virginica=S_inv %*% Mean_virginica
prediction=c()
d_setosa_vec=c()
d_versicolor_vec=c()
d_virginica_vec=c()
label=c("setosa", "versicolor", "virginica")
for(i in 1:nrow(test1)){
 #Read an observation in test data
```

```
x=t(test1[i,1:4])
 #Calculate linear discriminant functions for each species
 d_setosa=alpha_setosa+ t(beta_setosa) %*% x
 d_versicolor=alpha_versicolor+ t(beta_versicolor) %*% x
 d_virginica=alpha_virginica+ t(beta_virginica) %*% x
 #Classify the observation to the species with highest function value
 d_vec=c(d_setosa, d_versicolor, d_virginica)
 prediction=append(prediction, label[which.max( d_vec )])
 d_setosa_vec=append(d_setosa_vec, d_setosa)
 d_versicolor_vec=append(d_versicolor_vec, d_versicolor)
 d_virginica_vec=append(d_virginica_vec, d_virginica)
#Combine the predicted results to the test dataset.
test1$prediction=prediction
#result from test1: there are 2 wrong in the prediction
#----#
#Divide data into train and test size 60
train2=iris[c(1:20,51:70, 101:120),]
test2=iris[c(21:50,71:100, 121:150),]
#Sample size
n_setosa=20
n_versicolor=20
n_virginica=20
#Prior=relative sample size in train data
p_setosa=n_setosa/60
p_versicolor=n_versicolor/60
p_virginica=n_virginica/60
Mean_setosa=colMeans(train2[1:20,1:4])
Mean_versicolor=colMeans(train2[21:40,1:4])
Mean_virginica=colMeans(train2[41:60,1:4])
#Sample variance-covariance matrix for each species
S_{\text{setosa}=\text{cov}}(\text{train2}[1:20,1:4])
S_versicolor=cov(train2[21:40,1:4])
S_virginica=cov(train2[41:60,1:4])
#Complete fomula
S_pooled= ((n_setosa-1)*S_setosa+(n_versicolor-1)*S_versicolor+(n_virginica-1)*S_virginica)/(n_setosa+n
```

```
S_inv=solve(S_pooled)
#Simple way
\#S_pooled = (S_setosa + S_versicolor + S_virginica)/3
alpha setosa= -0.5* t(Mean setosa) %*% S inv %*% Mean setosa
alpha_versicolor= -0.5* t(Mean_versicolor) %*% S_inv %*% Mean_versicolor
alpha_virginica= -0.5* t(Mean_virginica) %*% S_inv %*% Mean_virginica
beta_setosa=S_inv ** Mean_setosa
beta_versicolor=S_inv %*% Mean_versicolor
beta_virginica=S_inv %*% Mean_virginica
prediction=c()
d_setosa_vec=c()
d_versicolor_vec=c()
d_virginica_vec=c()
label=c("setosa", "versicolor", "virginica")
for(i in 1:nrow(test2)){
 #Read an observation in test data
 x=t(test2[i,1:4])
 #Calculate linear discriminant functions for each species
 d_setosa=alpha_setosa+ t(beta_setosa) %*% x
 d_versicolor=alpha_versicolor+ t(beta_versicolor) %*% x
 d_virginica=alpha_virginica+ t(beta_virginica) %*% x
 #Classify the observation to the species with highest function value
 d_vec=c(d_setosa, d_versicolor, d_virginica)
 prediction=append(prediction, label[which.max( d_vec )])
 d_setosa_vec=append(d_setosa_vec, d_setosa)
 d_versicolor_vec=append(d_versicolor_vec, d_versicolor)
 d_virginica_vec=append(d_virginica_vec, d_virginica)
}
#Combine the predicted results to the test dataset.
test2$prediction=prediction
#result from test2: there are 3 wrong in the prediction
#-----#
#Divide data into train and test size 30
```

```
train3=iris[c(1:10,51:60, 101:110),]
test3=iris[c(11:50,61:100, 111:150),]
#Sample size
n_setosa=10
n_versicolor=10
n_virginica=10
#Prior=relative sample size in train data
p_setosa=n_setosa/30
p_versicolor=n_versicolor/30
p_virginica=n_virginica/30
Mean_setosa=colMeans(train3[1:10,1:4])
Mean_versicolor=colMeans(train3[11:20,1:4])
Mean_virginica=colMeans(train3[21:30,1:4])
#Sample variance-covariance matrix for each species
S_{\text{setosa}=\text{cov}}(\text{train3}[1:10,1:4])
S_versicolor=cov(train3[11:20,1:4])
S_virginica=cov(train3[21:30,1:4])
#Complete fomula
S_pooled= ((n_setosa-1)*S_setosa+(n_versicolor-1)*S_versicolor+(n_virginica-1)*S_virginica)/(n_setosa+n
S_inv=solve(S_pooled)
#Simple way
#S_pooled=(S_setosa+S_versicolor+S_virginica)/3
alpha_setosa= -0.5* t(Mean_setosa) %*% S_inv %*% Mean_setosa
alpha_versicolor= -0.5* t(Mean_versicolor) %*% S_inv %*% Mean_versicolor
alpha_virginica= -0.5* t(Mean_virginica) %*% S_inv %*% Mean_virginica
beta_setosa=S_inv ** Mean_setosa
beta_versicolor=S_inv %*% Mean_versicolor
beta_virginica=S_inv %*% Mean_virginica
prediction=c()
d_setosa_vec=c()
d_versicolor_vec=c()
d_virginica_vec=c()
label=c("setosa", "versicolor", "virginica")
```

```
for(i in 1:nrow(test3)){
  #Read an observation in test data
  x=t(test3[i.1:4])
  #Calculate linear discriminant functions for each species
  d_setosa=alpha_setosa+ t(beta_setosa) %*% x
  d_versicolor=alpha_versicolor+ t(beta_versicolor) %*% x
  d_virginica=alpha_virginica+ t(beta_virginica) %*% x
  #Classify the observation to the species with highest function value
  d_vec=c(d_setosa, d_versicolor, d_virginica)
  prediction=append(prediction, label[which.max( d_vec )])
 d_setosa_vec=append(d_setosa_vec, d_setosa)
  d_versicolor_vec=append(d_versicolor_vec, d_versicolor)
  d_virginica_vec=append(d_virginica_vec, d_virginica)
#Combine the predicted results to the test dataset.
test3$prediction=prediction
#result from test3: there are >3 wrong in the prediction
# In conclusion the smaller the sample size it goes, then
# the more fail prediction it will get. Vice versa, the larger
# the sample size we chose then the more accurate the prediction we
# will get. Here, we can see from sample size 90 , 60, 30.
# sample size 60 failed 2 predictions, and then it goes
# exponentially the more failure prediction we got.
```

```
#train 50
#test 100
trainsample = sample(1:150, 50, replace=FALSE)
testsample = sample(1:150, 100, replace= FALSE)
b = 100
for(i in 1:b){
#Divide data into train and test
train = iris[trainsample[b],]
test = train[testsample[b],]
#Sample size
n_setosa=trainsample[b]
n_versicolor=trainsample[b]
n_virginica=trainsample[b]
#Prior=relative sample size in train data
p_setosa=trainsample[1]/50
p versicolor=trainsample[1]/50
p_virginica=trainsample[1]/50
```

```
Mean_setosa=colMeans(train[trainsample[b],1:4])
Mean_versicolor=colMeans(train[trainsample[b],1:4])
Mean_virginica=colMeans(train[trainsample[b],1:4])
#Sample variance-covariance matrix for each species
S_setosa=cov(train[trainsample[b],1:4])
S_versicolor=cov(train[trainsample[b],1:4])
S_virginica=cov(train[trainsample[b],1:4])
#Complete fomula
S_pooled= ((n_setosa-1)*S_setosa+(n_versicolor-1)*S_versicolor+(n_virginica-1)*S_virginica)/(n_setosa+n
S_inv=solve(S_pooled)
#Simple way
\#S_pooled = (S_setosa + S_versicolor + S_virginica)/3
alpha_setosa = -0.5* t(Mean_setosa) %*% S_inv %*% Mean_setosa + log(p_setosa)
alpha versicolor= -0.5* t(Mean versicolor) %*% S inv %*% Mean versicolor + log(p versicolor)
alpha_virginica = -0.5* t(Mean_virginica) %*% S_inv %*% Mean_virginica + log(p_virginica)
beta_setosa=S_inv %*% Mean_setosa
beta_versicolor=S_inv %*% Mean_versicolor
beta_virginica=S_inv %*% Mean_virginica
prediction=c()
d setosa vec=c()
d_versicolor_vec=c()
d_virginica_vec=c()
label=c("setosa", "versicolor", "virginica")
for(i in 1:nrow(test)){
 #Read an observation in test data
 x=t(test[i,1:4])
 #Calculate linear discriminant functions for each species
 d_setosa=alpha_setosa+ t(beta_setosa) %*% x
 d_versicolor=alpha_versicolor+ t(beta_versicolor) %*% x
 d_virginica=alpha_virginica+ t(beta_virginica) %*% x
 #Classify the observation to the species with highest function value
 d_vec=c(d_setosa, d_versicolor, d_virginica)
```

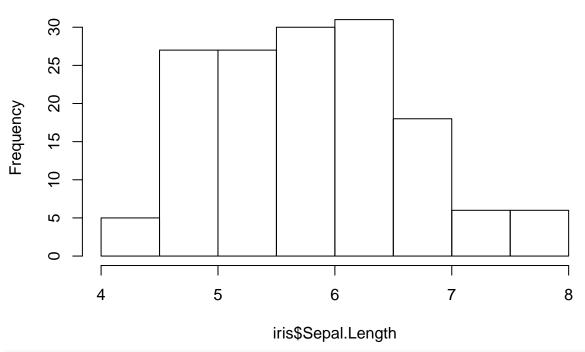
```
prediction=append(prediction, label[which.max( d_vec )])

d_setosa_vec=append(d_setosa_vec, d_setosa)
d_versicolor_vec=append(d_versicolor_vec, d_versicolor)
d_virginica_vec=append(d_virginica_vec, d_virginica)
}

#test$prediction=prediction
}

#plot a hist
x <- hist(iris$Sepal.Length)</pre>
```

Histogram of iris\$Sepal.Length



y = hist(iris\$Sepal.Width)

Histogram of iris\$Sepal.Width

