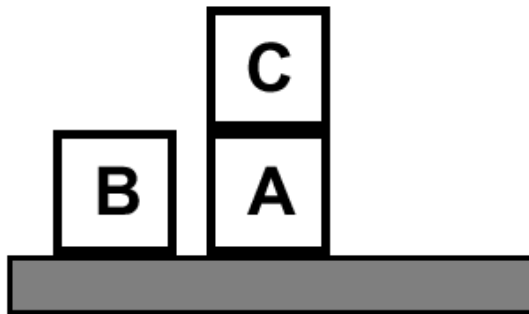
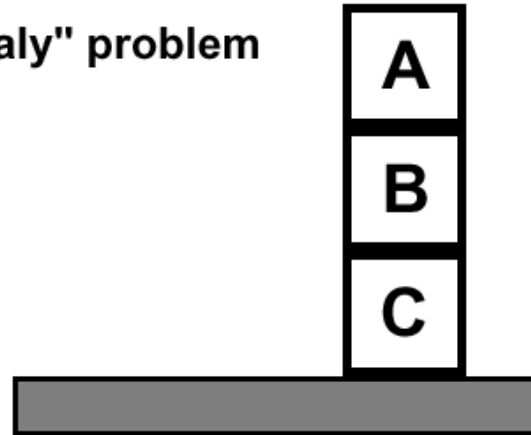


# Sussman Anomaly in the block world

"Sussman anomaly" problem



Start State



Goal State

$Clear(x) \ On(x,z) \ Clear(y)$

PutOn(x,y)

$\sim On(x,z) \ \sim Clear(y)$   
 $Clear(z) \ On(x,y)$

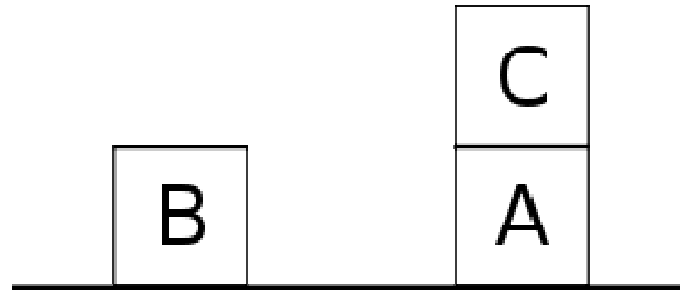
$Clear(x) \ On(x,z)$

PutOnTable(x)

$\sim On(x,z) \ Clear(z) \ On(x, Table)$

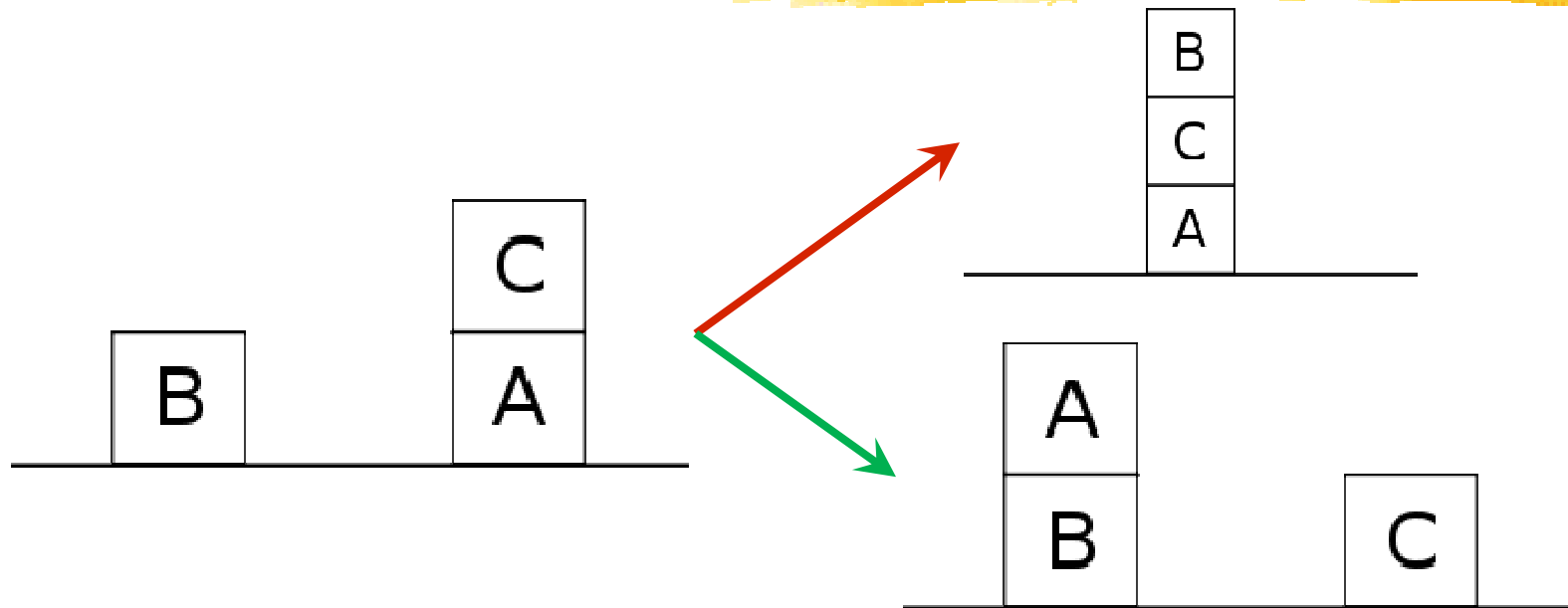
+ several inequality constraints

# Sussman Anomaly



- The Sussman Anomaly shows the limitations of non-interleaved planning methods
- Before this was described, people used to do planning by considering different subgoals in SEQUENCE
- The Anomaly will show that naively pursuing one subgoal X after you satisfy the other subgoal Y may not work because steps required to accomplish X might undo things subgoal Y

# Sussman Anomaly

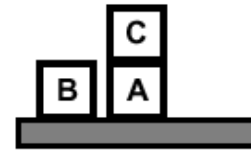


- Final state requires  $\text{On}(A,B)$  and  $\text{On}(B, C)$
- Top diagram tries to focus on subgoal:  $\text{On}(B,C)$  -- Now trying to put A on top of B cannot be done without undoing  $\text{On}(B, C)$
- Bottom diagram tries to focus on subgoal:  $\text{On}(A, B)$  first; but now trying to put B on top of C would cause  $\text{On}(A,B)$  to be undone!

# Anomaly Illustrates the Need for Interleaved Plans

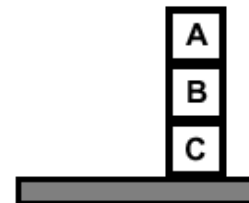
START

*On(C,A) On(A,Table) Cl(B) On(B,Table) Cl(C)*

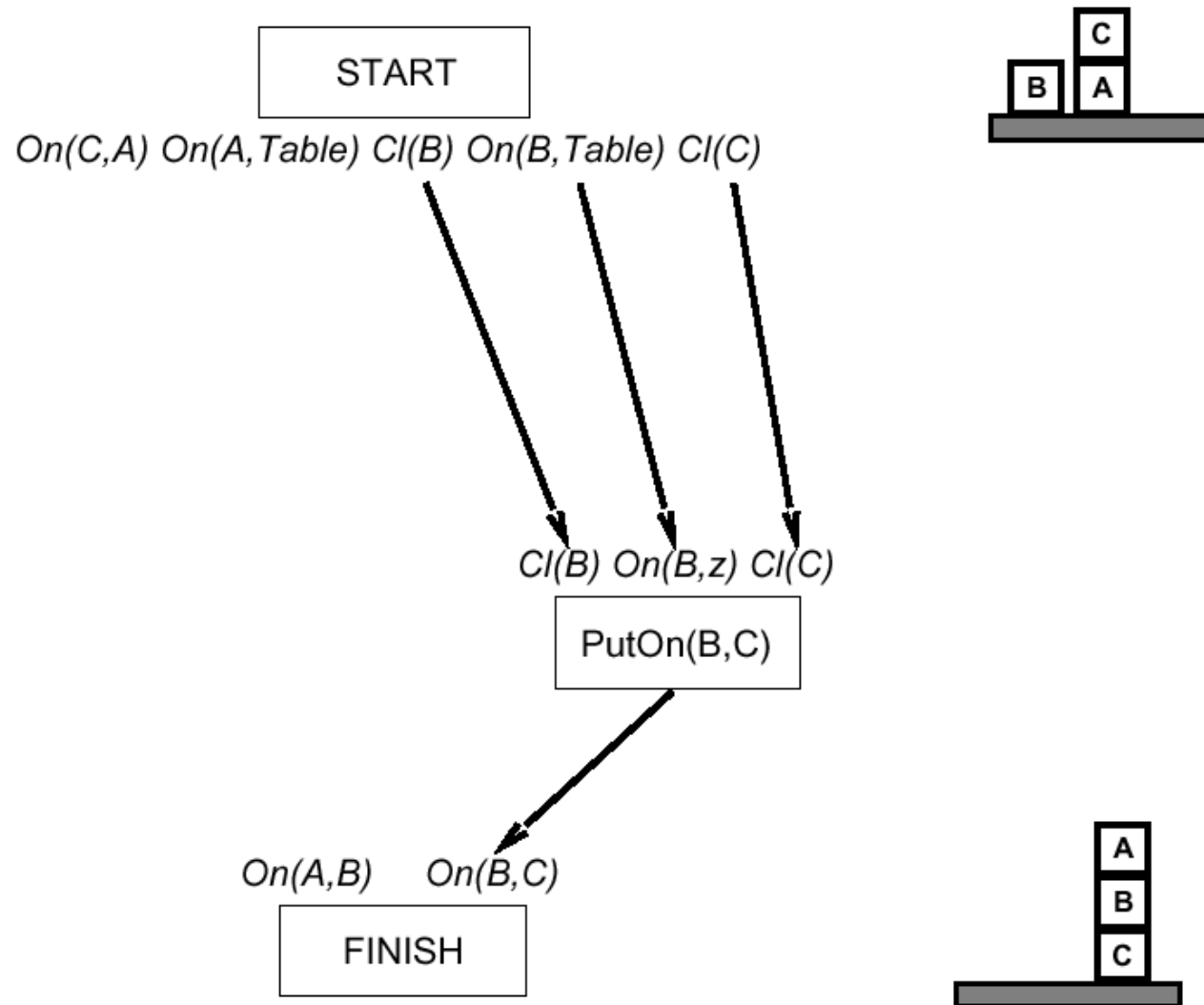


*On(A,B) On(B,C)*

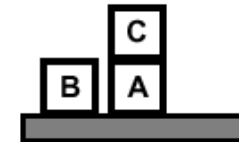
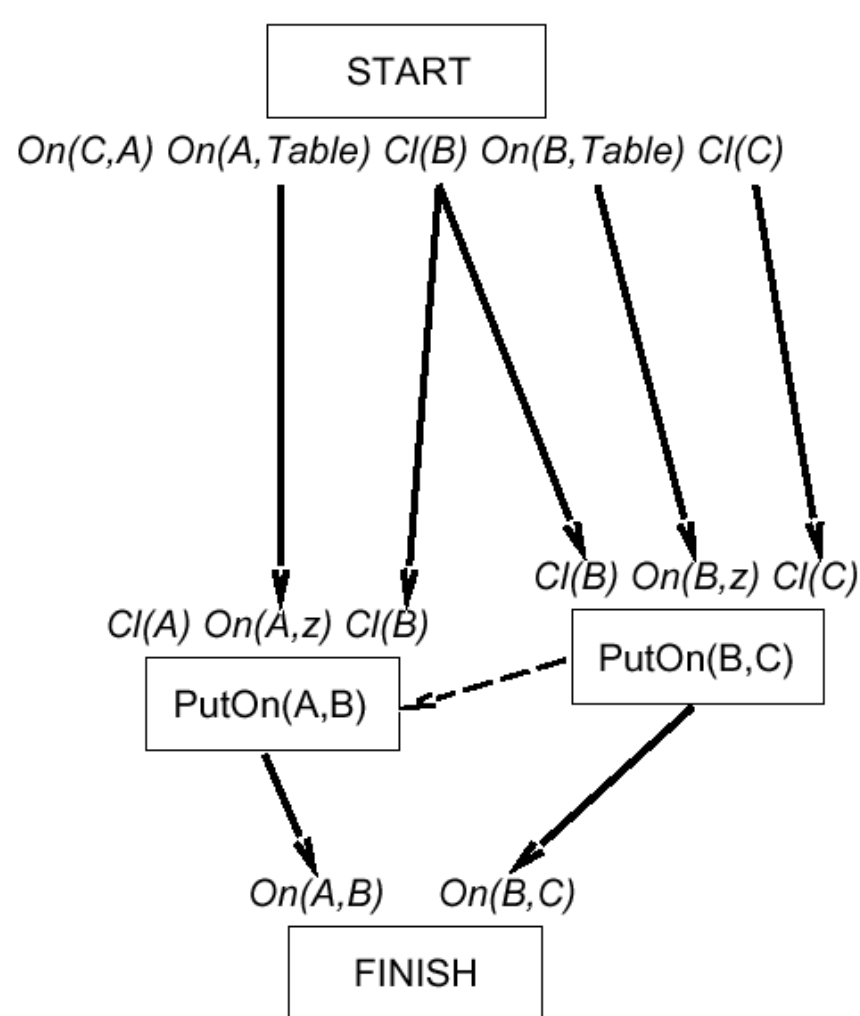
FINISH



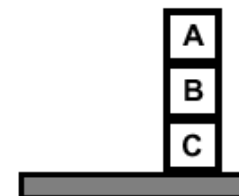
## Example: continued



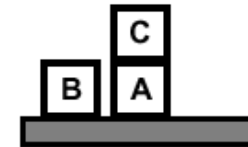
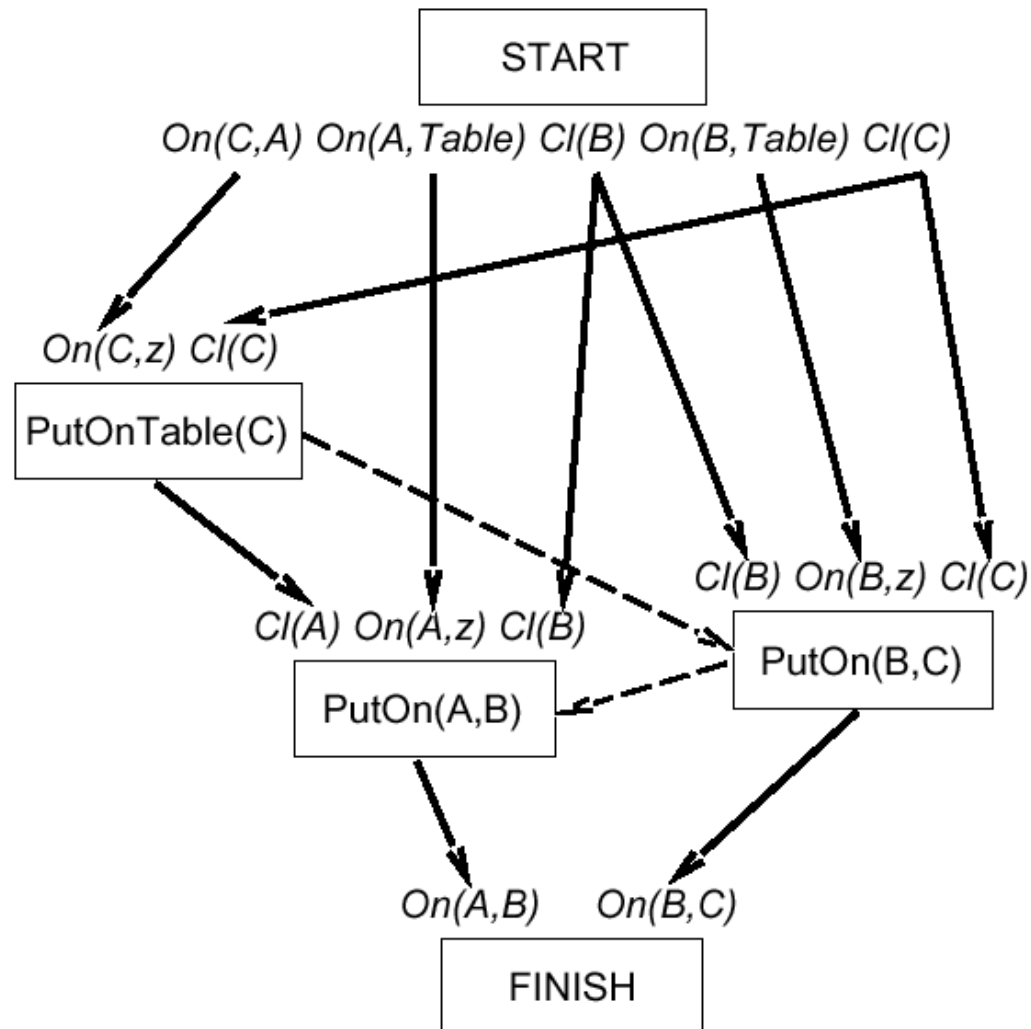
# Need to Re-Order Plan Steps Dynamically



PutOn(A,B)  
clobbers Cl(B)  
=> order after  
PutOn(B,C)

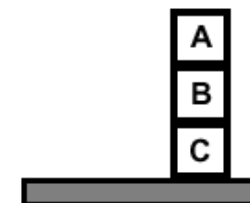


## Example (cont.)



PutOn(A,B)  
clobbers Cl(B)  
=> order after  
PutOn(B,C)

PutOn(B,C)  
clobbers Cl(C)  
=> order after  
PutOnTable(C)



## Conclusion from the Blocks Example



- Problem can be solved, BUT not by trying to apply ALL operators to achieve a single goal at a time sequentially – satisfying one goal seems to clobber earlier achieved goals.
- The issue: we are forcing an order on operators when they do not need to be mutually ordered.
- We need an approach that allows INTERLEAVING of steps for multiple goals
- This observation motivates the next planning approach: PARTIAL ORDER PLANNING - to be covered next class...



# Partial-order planning



- Progression and regression planning are *totally ordered plan search* forms.
  - They cannot take advantage of problem decomposition.
    - Decisions must be made on how to sequence actions on all the subproblems
- Least commitment strategy:
  - Delay choice during search

# Shoe example



Goal(RightShoeOn  $\wedge$  LeftShoeOn)

Init()

Action(RightShoe,    PRECOND: RightSockOn  
                        EFFECT: RightShoeOn)

Action(RightSock,    PRECOND:  
                        EFFECT: RightSockOn)

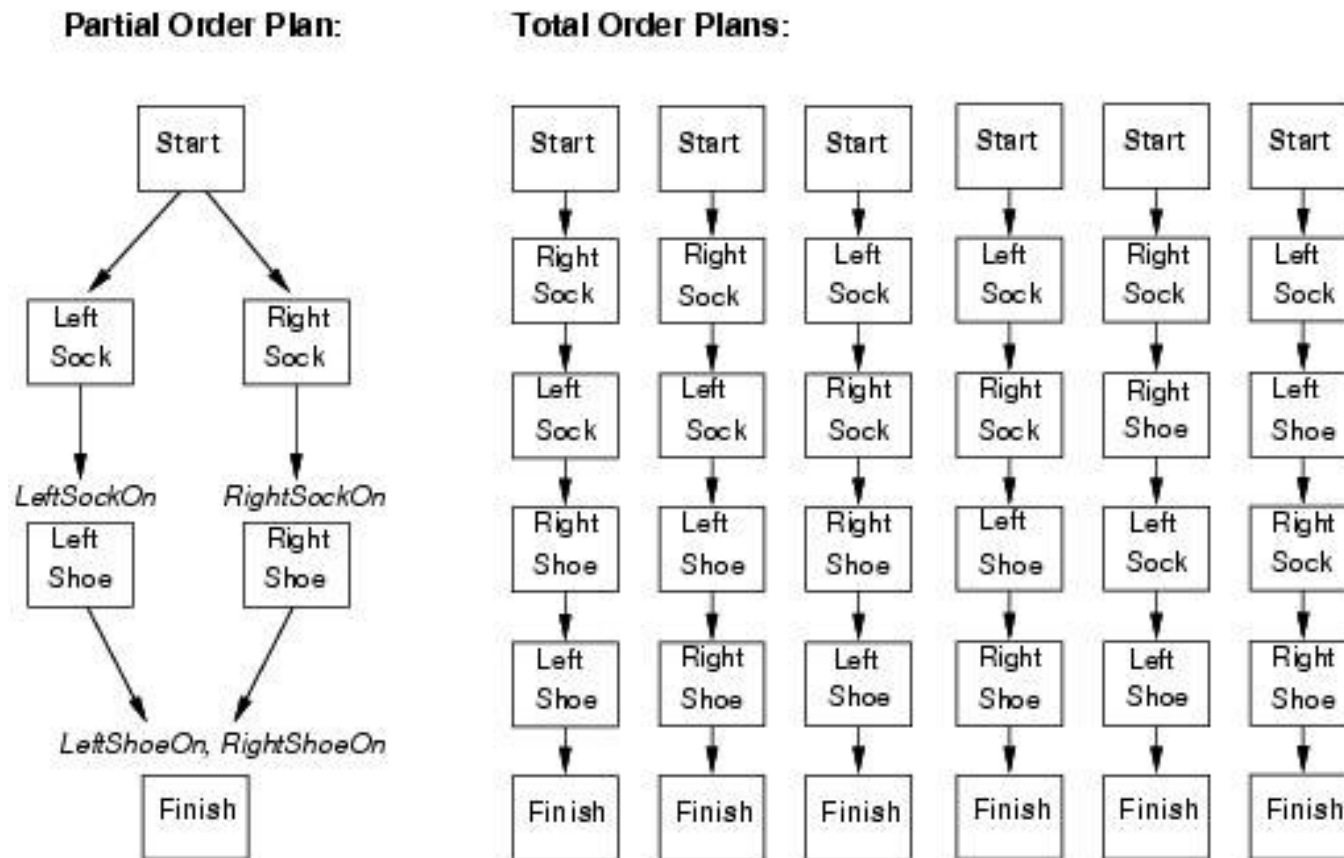
Action(LeftShoe,                      PRECOND: LeftSockOn  
                        EFFECT: LeftShoeOn)

Action(LeftSock,      PRECOND:  
                        EFFECT: LeftSockOn)

Planner: combine two action sequences (1)leftsock, leftshoe  
         (2)rightsock, rightshoe

# Partial-order planning

- Any planning algorithm that can place two actions into a plan without commitment about which comes first is a Partial Order Plan



# Partial Order Planning as a search problem

- States are (mostly unfinished) plans.
  - The empty plan contains only start and finish actions.
- Each plan has 4 components:
  - A set of actions (steps of the plan)
  - A set of ordering constraints:  $A < B$ 
    - Cycles represent contradictions.
  - A set of causal links  $A \xrightarrow{p} B$ 
    - The plan may not be extended by adding a new action C that conflicts with the causal link. (if the effect of C is  $\neg p$  and if C could come after A and before B)
  - A set of open preconditions.
    - If precondition is not achieved by action in the plan.

## POP as a search problem



- A plan is *consistent* iff there are no cycles in the ordering constraints and no conflicts with the causal links.
- A consistent plan with no open preconditions is a *solution*.
- A partial order plan is executed by repeatedly choosing *any* of the possible next actions.
  - This flexibility is a benefit in non-cooperative environments.

# Solving POP



- Assume propositional planning problems:
  - The initial plan contains *Start* and *Finish*, the ordering constraint *Start* < *Finish*, no causal links, all the preconditions in *Finish* are open.
  - Successor function :
    - picks one open precondition  $p$  on an action  $B$  and
    - generates a successor plan for every possible consistent way of choosing action  $A$  that achieves  $p$ .
- Test goal

# Enforcing consistency



- When generating successor plan:
  - The causal link  $A \rightarrow p \rightarrow B$  and the ordering constraint  $A < B$  is added to the plan.
    - If A is new also add  $\text{start} < A$  and  $A < B$  to the plan
  - Resolve conflicts between new causal link and all existing actions
  - Resolve conflicts between action A (if new) and all existing causal links.

## Process summary



- Operators on partial plans
  - Add link from existing plan to open precondition.
  - Add a step to fulfill an open condition.
  - Order one step w.r.t another to remove possible conflicts
- Gradually move from incomplete/vague plans to complete/correct plans
- Backtrack if an open condition is unachievable or if a conflict is unresolvable.



# Example: Spare tire problem

*Init*(*At*(Flat, Axle)  $\wedge$  *At*(Spare, trunk))

*Goal*(*At*(Spare, Axle))

*Action*(*Remove*(Spare, Trunk))

PRECOND: *At*(Spare, Trunk)

EFFECT:  $\neg$ *At*(Spare, Trunk)  $\wedge$  *At*(Spare, Ground))

*Action*(*Remove*(Flat, Axle))

PRECOND: *At*(Flat, Axle)

EFFECT:  $\neg$ *At*(Flat, Axle)  $\wedge$  *At*(Flat, Ground))

*Action*(*PutOn*(Spare, Axle))

PRECOND: *At*(Spare, Ground)  $\wedge$   $\neg$ *At*(Flat, Axle)

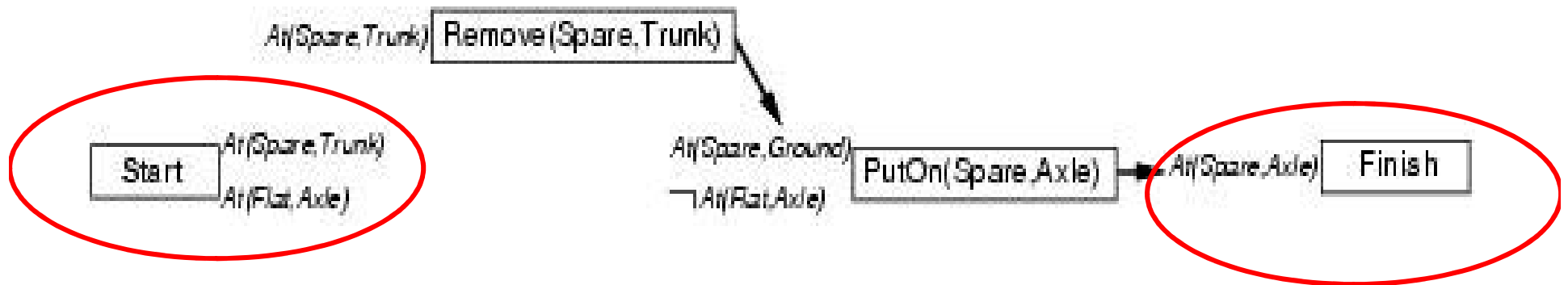
EFFECT: *At*(Spare, Axle)  $\wedge$   $\neg$ *At*(Spare, Ground))

*Action*(*LeaveOvernight*

PRECOND:

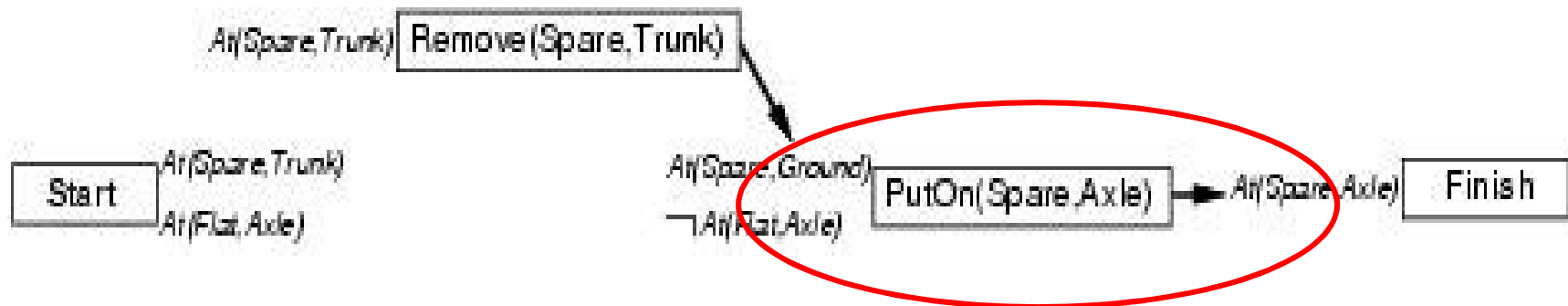
EFFECT:  $\neg$  *At*(Spare, Ground)  $\wedge$   $\neg$  *At*(Spare, Axle)  $\wedge$   $\neg$  *At*(Spare, trunk)  $\wedge$   $\neg$  *At*(Flat, Ground)  $\wedge$   $\neg$  *At*(Flat, Axle) )

# Solving the problem



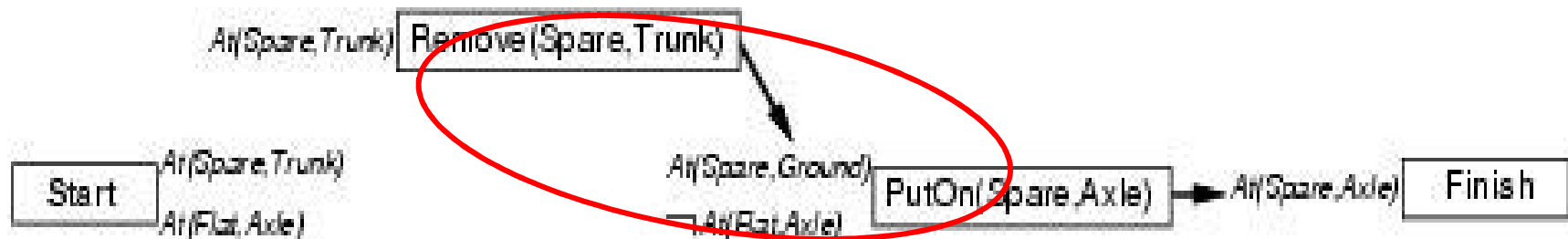
- Initial plan: Start with EFFECTS and Finish with PRECOND.

# Solving the problem



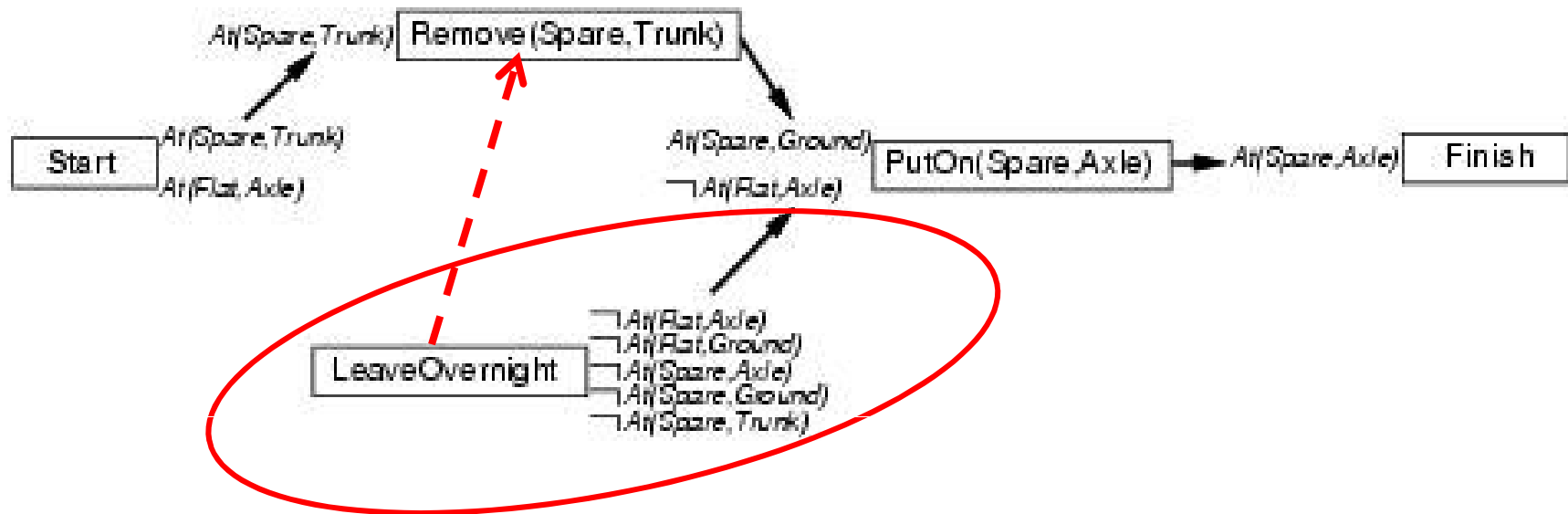
- Initial plan: Start with EFFECTS and Finish with PRECOND.
- Pick an open precondition:  $At(Spare, Axle)$
- Only  $PutOn(Spare, Axle)$  is applicable
- Add causal link:  $PutOn(Spare, Axle) \xrightarrow{At(Spare, Axle)} Finish$
- Add constraint :  $PutOn(Spare, Axle) < Finish$

# Solving the problem



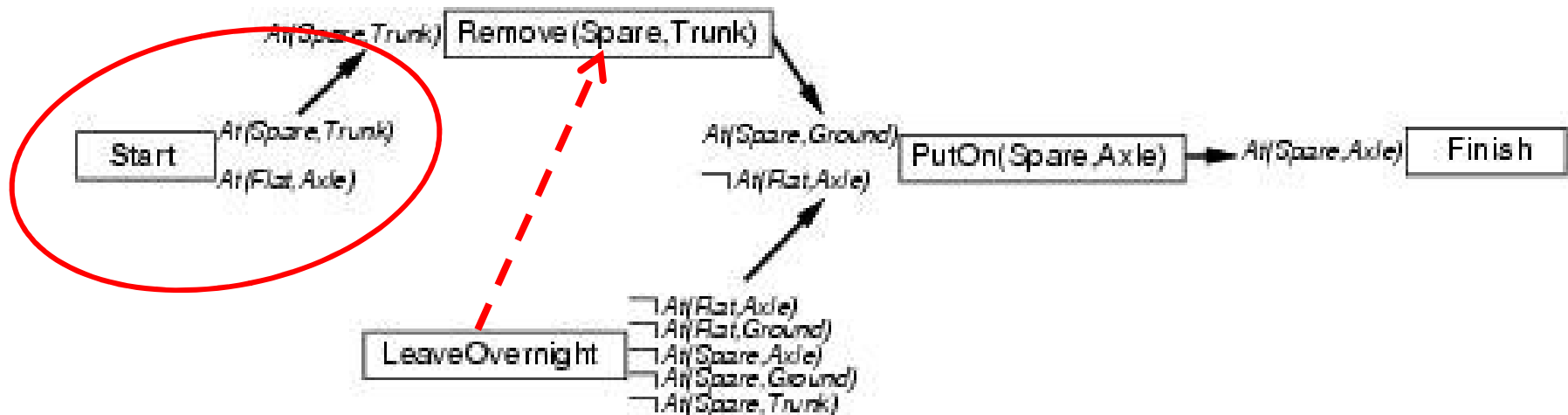
- Pick an open precondition:  $At(Spare, Ground)$
- Only  $Remove(Spare, Trunk)$  is applicable
- Add causal link:  $Remove(Spare, Trunk) \xrightarrow{At(Spare, Ground)} PutOn(Spare, Axle)$
- Add constraint :  $Remove(Spare, Trunk) < PutOn(Spare, Axle)$

# Solving the problem



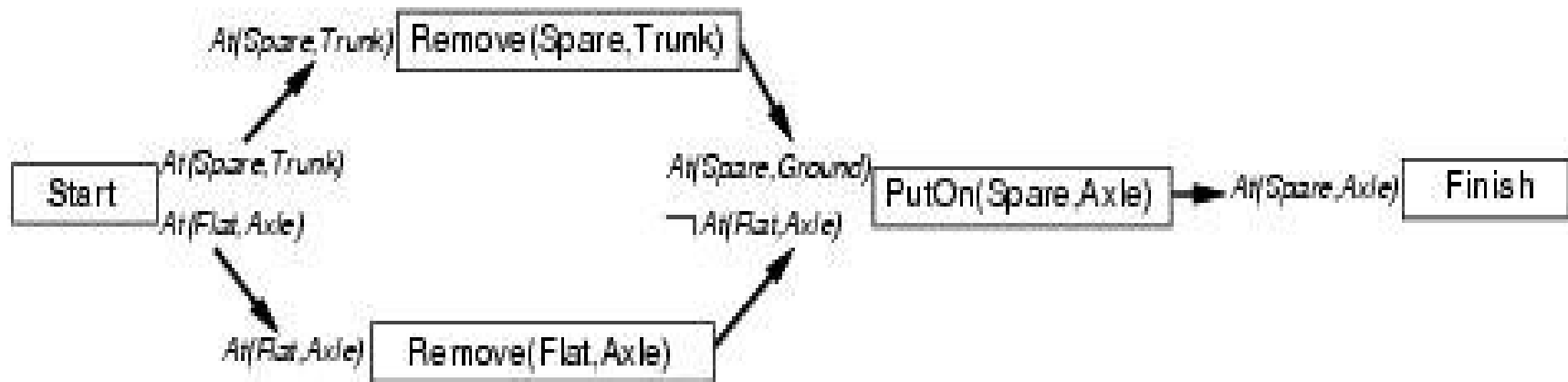
- Pick an open precondition:  $\neg At(Flat, Axle)$
- *LeaveOverNight* is applicable
- conflict:  $Remove(Spare, Trunk) \xrightarrow{At(Spare, Ground)} PutOn(Spare, Axle)$
- Because *LeaveOverNight* also makes  $\neg At(Spare, Ground)$
- To resolve, add constraint :  $LeaveOverNight < Remove(Spare, Trunk)$

# Solving the problem



- Pick an open precondition:  $At(Spare, Trunk)$
- Only *Start* is applicable
- Add causal link:  $Start \xrightarrow{At(Spare, Trunk)} Remove(Spare, Trunk)$
- Conflict: of causal link with effect  $\neg At(Spare, Trunk)$  in *LeaveOverNight*
  - *No re-ordering solution possible.*
- Backtrack to a prior move since there is no way to fix this

## Solving the problem



- Backtracking step: Remove *LeaveOverNight* and its causal links
- Now try *Remove(Flat, Axle)* as a way to satisfy  $\neg At(Flat, Axle)$
- That one works... and the partial plan can be completed as above

## Some details ...



- What happens when a **first-order** representation that includes variables is used?
  - Complicates the process of detecting and resolving conflicts.
  - Can be resolved by introducing inequality constraints
- CSP's most-constrained-variable constraint can be used for planning algorithms to select a PRECOND.



# Planning graphs



- Used to achieve better heuristic estimates.
  - A solution can also directly extracted using GRAPHPLAN.
- Consists of a sequence of levels that correspond to time steps in the plan.
  - Level 0 is the initial state.
  - Each level consists of a set of literals and a set of actions.
    - *Literals* = all those that *could* be true at that time step, depending upon the actions executed at the preceding time step.
    - *Actions* = all those actions that *could* have their preconditions satisfied at that time step, depending on which of the literals actually hold.

# Planning graphs



- “Could”?
  - Records only a restricted subset of possible negative interactions among actions.
- They work only for propositional problems.

- Example:

Init(Have(Cake))

Goal(Have(Cake)  $\wedge$  Eaten(Cake))

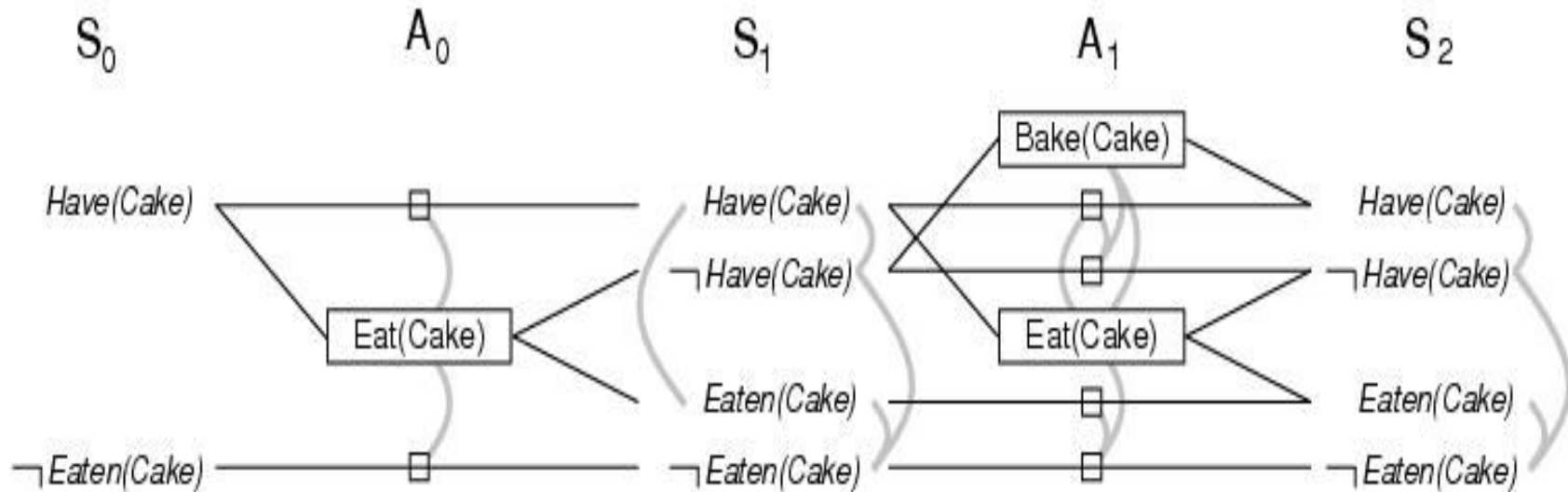
Action(Eat(Cake), PRECOND: Have(Cake)

EFFECT:  $\neg$ Have(Cake)  $\wedge$  Eaten(Cake))

Action(Bake(Cake), PRECOND:  $\neg$  Have(Cake)

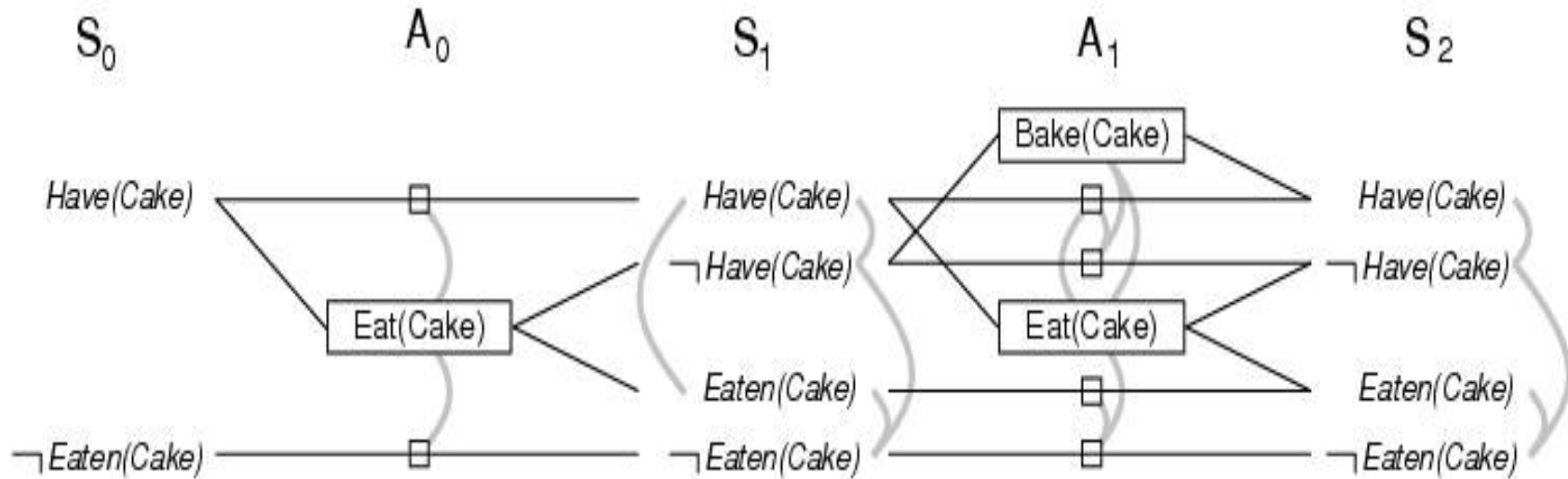
EFFECT: Have(Cake))

# Cake example



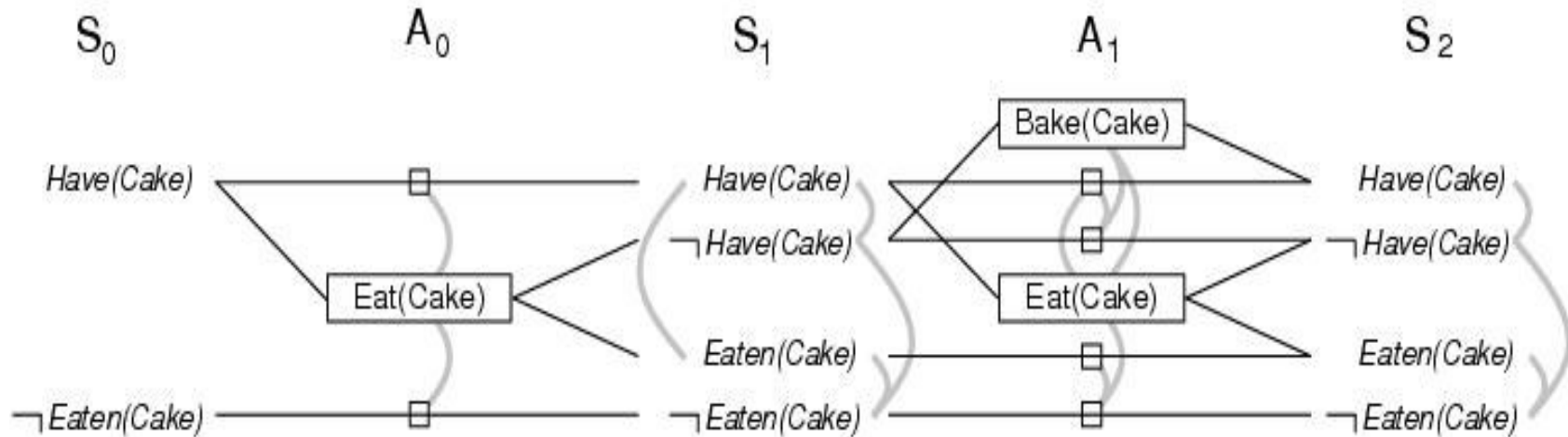
- Start at level  $S_0$  and determine action level  $A_0$  and next level  $S_1$ .
  - $A_0 \gg$  all actions whose preconditions are satisfied in the previous level.
  - Connect precondition and effect of actions  $S_0 \rightarrow S_1$
  - Inaction is represented by persistence actions.
- Level  $A_0$  contains the actions that could occur
  - Conflicts between actions are represented by *mutex* links

# Cake example



- Level  $S_1$  contains all literals that could result from picking any subset of actions in  $A_0$ 
  - Conflicts between literals that cannot occur together are represented by mutex links.
  - $S_1$  defines multiple states and the mutex links are the constraints that define this set of states.
- Continue until two consecutive levels are identical: *leveled off*
  - Or contain the same amount of literals (explanation follows later)

# Cake example



- A mutex relation holds between **two actions** when:
  - *Inconsistent effects*: one action negates the effect of another ( $Have(Cake)$  and  $Eat(Cake)$  for example)
  - *Interference*: one of the effects of one action is the negation of a precondition of the other.  $Eat(Cake)$  negates the precondition of  $Have(Cake)$  persistence and therefore interferes with it
  - *Competing needs*: one of the preconditions of one action is mutually exclusive with the precondition of the other. For example,  $Bake(Cake)$  competes with  $Eat(Cake)$  on the  $Have(Cake)$  pre condition.
- A mutex relation holds between **two literals** when (*inconsistent support*):
  - If one is the negation of the other OR
  - if each possible action pair that could achieve the literals is mutex.

# Plan Graphs and heuristic estimation



- PG's provide information about the problem
  - A literal that does not appear in the final level of the graph cannot be achieved by any plan.
    - Useful for backward search (cost = inf).
  - Level of appearance can be used as cost estimate of achieving any goal literals = *level cost*.
  - Small problem: several actions can occur
    - Restrict to one action using serial PG (add mutex links between every pair of actions, except persistence actions).
  - Max-level, sum-level and set-level heuristics.

PG is a relaxed problem.

# The GRAPHPLAN Algorithm



- How to extract a solution directly from the PG

**function** GRAPHPLAN(*problem*) **return** *solution* or failure

*graph*  $\leftarrow$  INITIAL-PLANNING-GRAPH(*problem*)

*goals*  $\leftarrow$  GOALS[*problem*]

**loop do**

**if** *goals* all non-mutex in last level of graph **then do**

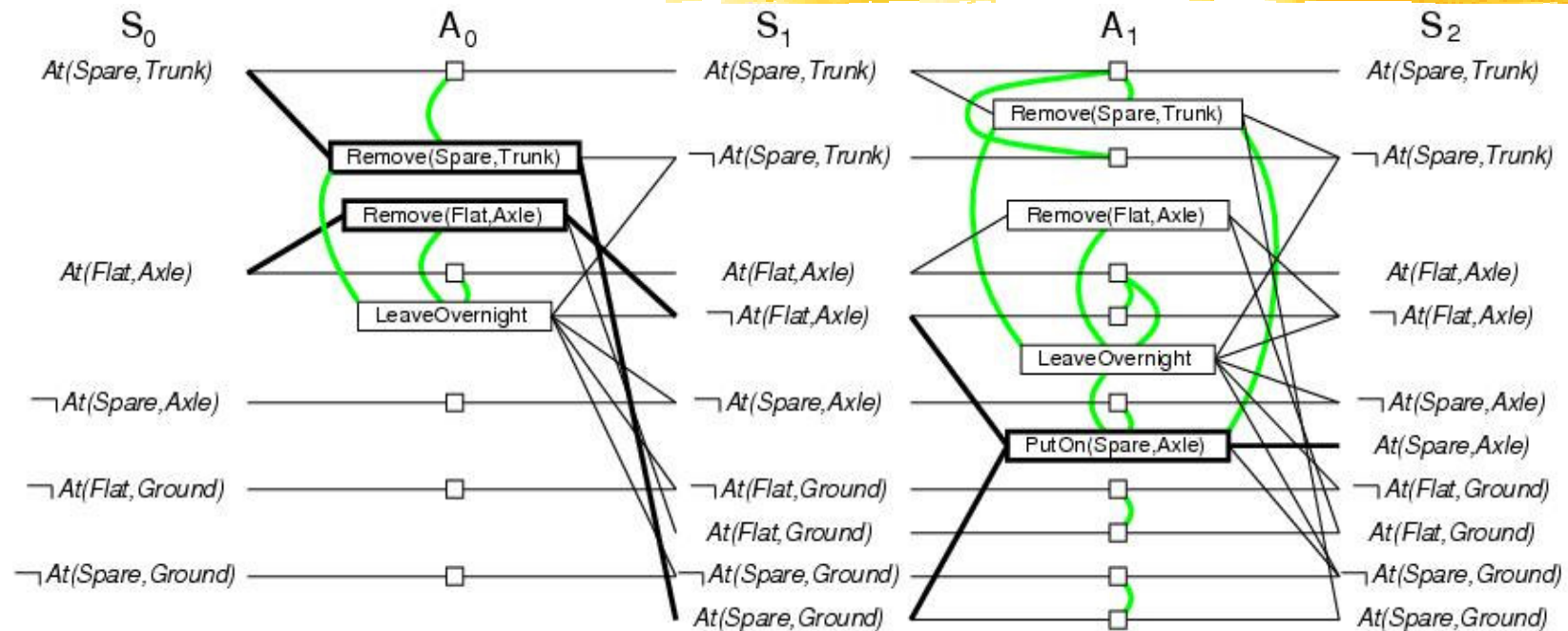
*solution*  $\leftarrow$  EXTRACT-SOLUTION(*graph*, *goals*, LENGTH(*graph*))

**if** *solution*  $\neq$  failure **then return** *solution*

**else if** NO-SOLUTION-POSSIBLE(*graph*) **then return** failure

*graph*  $\leftarrow$  EXPAND-GRAPH(*graph*, *problem*)

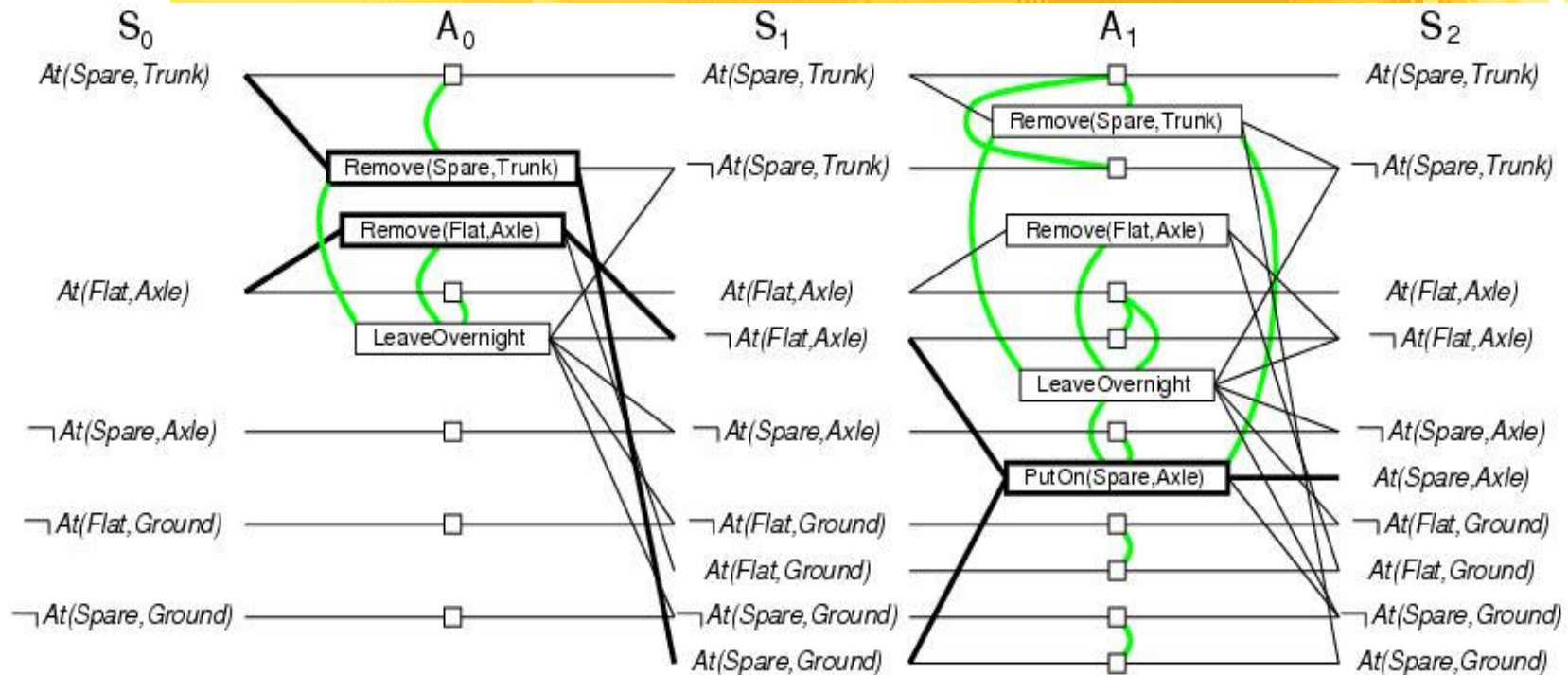
# GRAPHPLAN example



- Initially the plan consist of 5 literals from the initial state and the CWA literals ( $S_0$ ).
- Add actions whose preconditions are satisfied by EXPAND-GRAPH ( $A_0$ )
- Also add persistence actions and mutex relations.
- Add the effects at level  $S_1$
- Repeat until goal state appears in some level

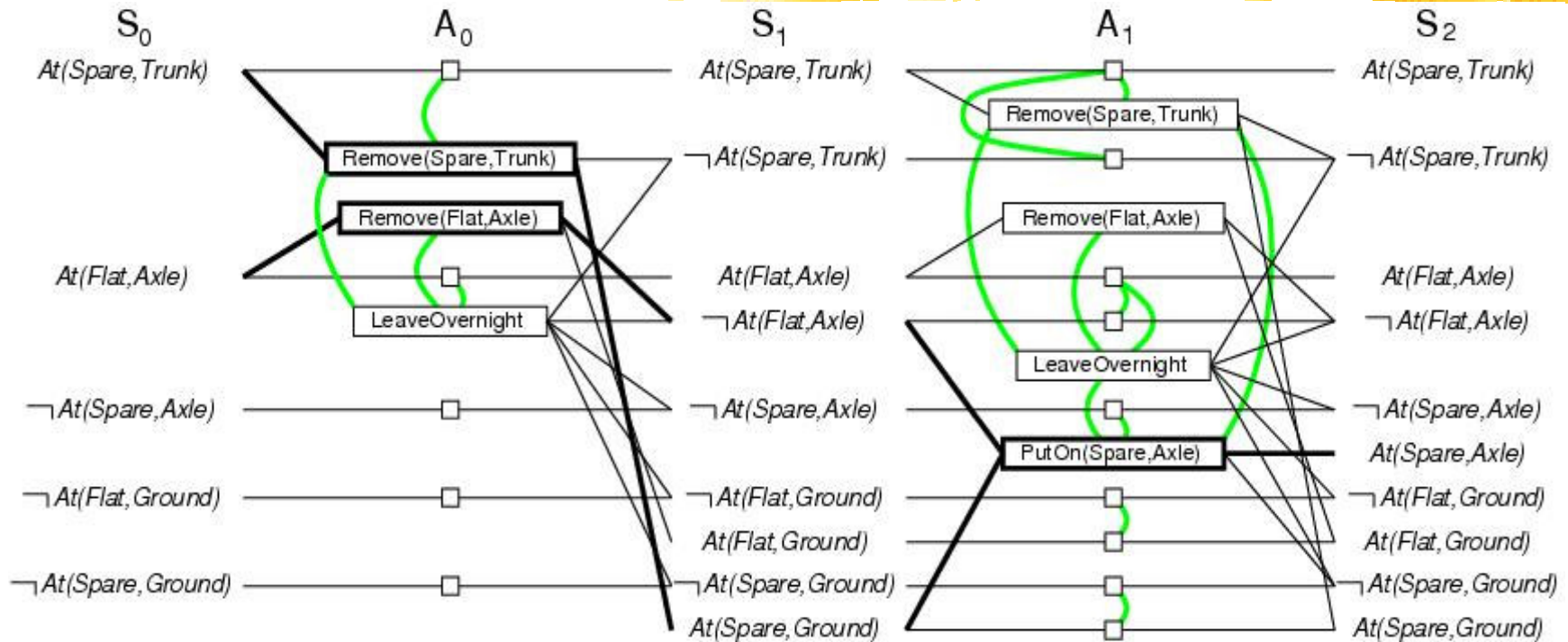


# GRAPHPLAN example



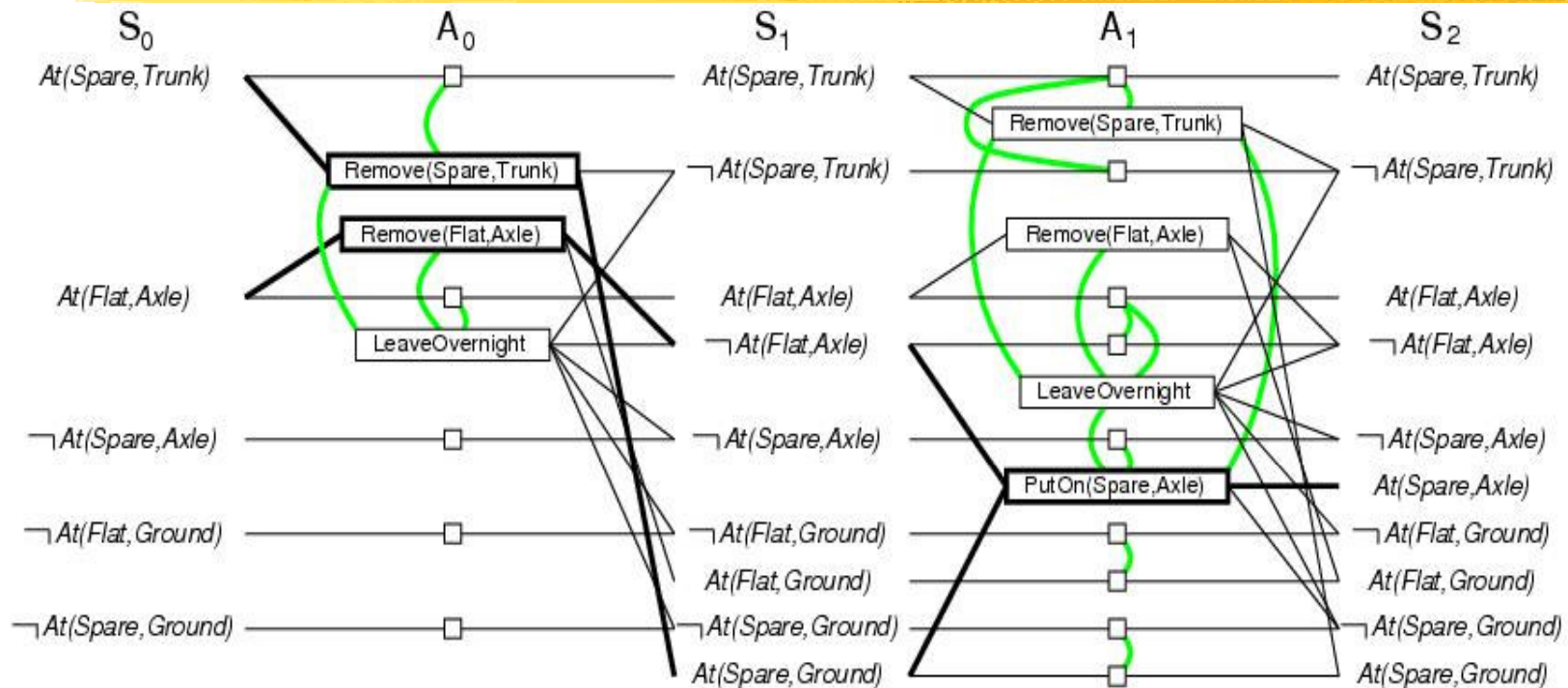
- EXPAND-GRAPH also looks for mutex relations
  - Inconsistent effects
    - E.g.  $Remove(Spare, Trunk)$  and  $LeaveOverNight$
  - Interference
    - E.g.  $Remove(Flat, Axle)$  and  $LeaveOverNight$
  - Competing needs
    - E.g.  $PutOn(Spare, Axle)$  and  $Remove(Flat, Axle)$
  - Inconsistent support
    - E.g. in  $S_2$ ,  $At(Spare, Axle)$  and  $At(Flat, Axle)$

# GRAPHPLAN example



- In  $S_2$ , the goal literal exists and is not mutex with any other
  - Solution might exist and EXTRACT-SOLUTION will try to find it
- EXTRACT-SOLUTION can use Boolean CSP to solve the problem or a search process:
  - Initial state = last level of PG and goal goals of planning problem
  - Actions = select any set of non-conflicting actions that cover the goals in the state
  - Goal = reach level  $S_0$  such that all goals are satisfied
  - Cost = 1 for each action.

# GRAPHPLAN example



- Termination? YES
- PG are monotonically increasing or decreasing:
  - Literals increase monotonically
  - Actions increase monotonically
  - Mutexes decrease monotonically
- Because of these properties and because there is a finite number of actions and literals, every PG will eventually level off !

# Analysis of planning approach



- Planning is an area of great interest within AI
  - Search for solution
  - Constructively prove a existence of solution
- Biggest problem is the combinatorial explosion in states.
- Efficient methods are under research
  - E.g. divide-and-conquer