# Cluster Difference Imaging Photometric Survey (CDIPS) II. TOI837: A Validated Saturn-Sized Planet in IC 2602

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#### **ABSTRACT**

We report the discovery of TOI 837.01 and its validation as a transiting planet. We characterize the system using data from the NASA TESS mission, the ESA Gaia mission, photometry from El Sauce and ASTEP400, and spectroscopy from CHIRON, FEROS, and Veloce. We find that TOI 837 is a T=9.9 G0 dwarf in the open cluster IC 2602. The star and planet are therefore  $35^{+11}_{-5}$  million years old. The planet is warm (P=8.3 d) and slightly smaller than Jupiter. Combining the transit photometry with a prior on the stellar parameters derived from the cluster color-magnitude diagram, we find that the transits are grazing with  $b=0.93\pm0.01$  and  $R_p=0.79\pm0.07\,R_{\rm Jup}$ . From radial velocity monitoring, we limit the minimum mass to less than  $1.20\,M_{\rm Jup}$  ( $3\sigma$ ). Grazing transits are a cause for concern, as they are usually indicative of astrophysical false positive scenarios. Our follow-up data show that such scenarios are highly unlikely. Our combined multi-color photometry, high-resolution imaging, and radial velocities rule out hierarchical eclipsing binary scenarios. Background eclipsing binary scenarios, though limited by speckle imaging, formally remain a 0.2% possibility. TOI 837.01 is therefore a validated adolescent exoplanet. Further observations of its stellar obliquity, atmosphere, and mass should confirm its planetary nature beyond doubt, and could improve our understanding of how the physical and orbital properties of exoplanets change in time.

*Keywords:* Exoplanets (498), Transits (1711), Exoplanet evolution (491), Stellar ages (1581), Young star clusters (1833)

# 1. INTRODUCTION

Over the first 100 million years of their lives, exoplanet systems are expected to undergo major physical and dynamical changes. For a typical Sun-like star, the protoplanetary disk disperses within roughly 1–10 million years (Mamajek 2009; Dullemond & Monnier 2010; Williams & Cieza 2011). Gas giants presumably finish accreting before the end of disk dispersal (Pollack et al. 1996). While rocky planets may fully form within only a few million years (Dauphas & Pourmand 2011), they can also undergo significant growth over the next 10–100 million years through giant impacts (*e.g.*, Kleine et al. 2009; König et al. 2011; Morbidelli et al. 2012; Raymond et al. 2014). The Moon, for instance, may have formed from debris ejected during a collision between the proto-Earth and a planetesimal during Earth's first 100 million years (Cameron & Ward 1976; Canup & Asphaug 2001).

A number of other processes are expected to shape young exoplanets. Planets with gaseous envelopes are thought to shrink as they contract and as their atmospheres undergo photoevaporation (*e.g.*, Fortney et al. 2007; Owen & Wu 2013; Fulton et al. 2017). The relative importance of contraction and photoevaporation is set by the planetary mass, as well as the radiation environment. The effectiveness of photoevaporation can be inferred from observations of planetary winds in the metastable 1083 nm He line (Spake et al. 2018; Oklopčić & Hirata 2018; Mansfield et al. 2018).

Beyond physical changes, dynamical changes are expected in the semi-major axes, eccentricities, and stellar obliquities of young planets. When the gas disk is present, the planetary semi-major axis is thought to change in step with the viscous evolution of the disk (Lin et al. 1996). High-eccentricity migration processes including planet-planet scattering, secular chaos, and Kozai-Lidov oscillations can also occur (*e.g.*, Chatterjee et al. 2008; Lithwick & Wu 2014; Fabrycky & Tremaine 2007). The circularization timescale is thought to be such that for any giant planets that migrated early, their orbits should circularize within 100 million years (Zahn 1977).

Finding and studying systems undergoing these evolutionary changes is a major goal in contemporary exoplanet research. To identify stars younger than say 1 Gyr, a number of direct and indirect methods are available (Soderblom 2010). The traditional approach is to isochronally age-date coeval groups of stars, hereafter "clusters" (e.g., Lada & Lada 2003; Zuckerman & Song 2004; Krumholz et al. 2019). Young field stars can also be identified using age indicators such as stellar rotation periods, the abundance of photospheric lithium, and chromospheric diagnostics such as calcium emission and broadband UV emission. Studies by for instance David et al. (2018) and G. Zhou et al. (2020, submitted) have combined these methods for individual field stars. Many of the latter methods were summarized by Mamajek & Hillenbrand (2008), and have since been calibrated by e.g., Irwin & Bouvier (2009); Barnes et al. (2015); Meibom et al. (2015); Angus et al. (2015) and Curtis et al. (2019b) for stellar rotation, Žerjal et al. (2017) for chromospheric activity, and e.g., Elliott et al. (2016); Berger et al. (2018) and Žerjal et al. (2019) for lithium abundances.

A few dozen planets in clusters have been detected, and fewer still have been closely characterized. Despite the challenges of starspot-induced radial velocity (RV) variations, RV surveys found success in the Hyades, NGC 2523, Praesepe, and M 67 (Sato et al. 2007; Lovis & Mayor 2007; Quinn et al. 2012; Malavolta et al. 2016; Brucalassi et al. 2017). RV surveys of highly active pre-main sequence stars in Taurus also led to the youngest hot Jupiters yet reported (Donati et al. 2016; Johns-Krull et al. 2016; Biddle et al. 2018; Flagg et al. 2019).

The transit method was comparatively slow to catch up. Early deep transit searches of open clusters by many groups did not yield definitive planet detections (Mochejska et al. 2005, 2006; Burke et al. 2006; Aigrain et al. 2007; Irwin et al. 2007; Miller et al. 2008; Pepper et al. 2008; Hartman et al. 2009). These searches were typically sensitive to planets larger than Jupiter, on  $\lesssim$  3 day orbital periods. Hot Jupiter occurrence rate limits were derived at the  $\lesssim$  5% level (*e.g.*, Burke et al. 2006; Hartman et al. 2009). The modern 0.5-1% occurrence rate suggests that these early transit surveys needed a greater data volume, at higher precision for detection to be possible (Mayor et al. 2011; Wright et al. 2012; Howard et al. 2012; Petigura et al. 2018).

Kepler observed a large enough number of stars with sufficient baseline and precision to detect transiting planets in open clusters: Kepler-66b and 67b, in the gigayear-old NGC 6811 (Borucki et al. 2010; Meibom et al. 2013). Though a broken reaction wheel ended the prime Kepler mission, the repurposed K2 (Howell et al. 2014) switched between fields along the ecliptic every quarter-year, and was able to observe far more clusters and young stars.

The discoveries made by K2 through its surveys of Taurus, the Hyades, Praesepe, and Upper Sco were a major inspiration for the present work (*e.g.*, Mann et al. 2016a; Obermeier et al. 2016; Mann et al. 2017; Vanderburg et al. 2018; Ciardi et al. 2018; Livingston et al. 2018; Mann et al. 2018; Rizzuto et al. 2018; Livingston et al. 2019). Observations with K2

convincingly showed that at least some close-in planets must form within about 10 Myr (Mann et al. 2016b; David et al. 2016). They also led to the first hints that young planets may in fact be qualtiatively different from their field counterparts. For instance, based on its observed mass, radius, and UV environment, the 700 Myr K2-100b is probably actively losing its atmosphere, and should become a bare rocky planet over the next few hundred Myr (Mann et al. 2017; Barragán et al. 2019). The four transiting planets in V1298 Tau (23 Myr) are also likely to be actively photoevaporating, and could represent a precursor to Kepler's compact multiple systems (David et al. 2019a,b).

With the aim of advancing the young planet census, we have been using data from the TESS spacecraft (Ricker et al. 2015) to perform a Cluster Difference Imaging Photometric Survey (CDIPS; Bouma et al. 2019). Our targets in this survey are candidate young stars that have been reported in the literature. At the time writing, of order  $6\times10^5$  light curves from the first year of TESS observations have been reduced, and are available at MAST¹ through DOI.ORG/10.17909/T9-AYD0-K727. Searching these light curves yielded the candidate transiting planet, TOI 837.01, that is the subject of this analysis.

The transits of TOI 837.01 are grazing, which is a cause for concern. Particularly for a target near the galactic plane  $(b = -5.8^{\circ})$ , background eclipsing binaries are a major source of astrophysical false positives (*e.g.*, Sullivan et al. 2015, Figure 30). Our follow-up data show that this and related scenarios are unlikely to the degree that we can "validate" the planet, *i.e.*, rule that its probability of being an astrophysical false positive is negligibly small. We considered this result worth reporting because of the planet's youth.

Section 2 describes the identification of the candidate, and the follow-up observations collected. Section 3 combines these data to assess the system's false positive probability, and validates TOI 837.01 as a planet. Section 4 presents our knowledge of the cluster (Section 4.1), the star (Section 4.2) and the planet (Section 4.3). We conclude by discussing avenues for confirmation and improved characterization in Section 5.

# 2. IDENTIFICATION AND FOLLOW-UP OBSERVATIONS

## 2.1. TESS Photometry

TOI 837 was observed by TESS from 26 March 2019 until 20 May 2019, during the tenth and eleventh sectors of science operations (Ricker et al. 2015). The star was designated TIC 460205581 in the TESS Input Catalog (Stassun et al. 2018, 2019). Pixel data for an  $11 \times 11$  array surrounding the star were averaged and saved at 2-minute cadence. The  $2048 \times 2048$  image from the entire CCD was also averaged into 30-minute stacks, and saved as a "full frame image" (FFI).

<sup>&</sup>lt;sup>1</sup> ARCHIVE.STSCI.EDU/HLSP/CDIPS

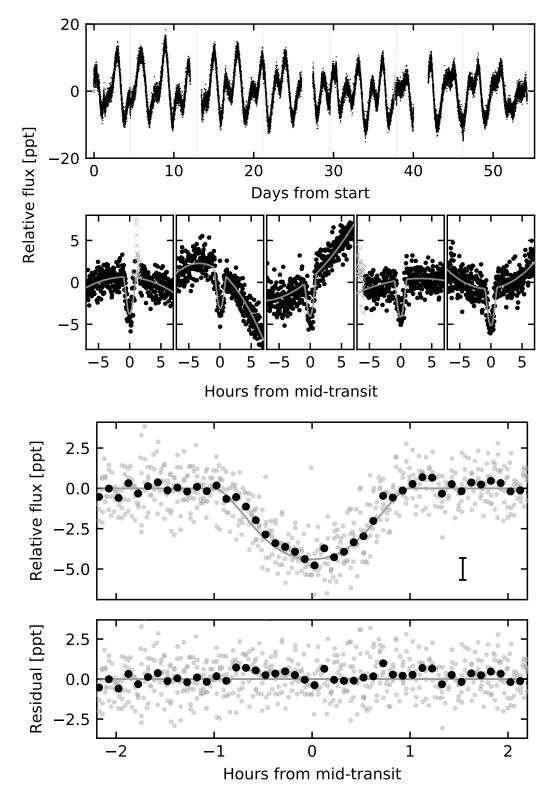


Figure 1. TESS light curve of TOI 837. Top: PDCSAP median-subtracted relative flux at 2-minute sampling in units of parts-per-thousand ( $\times 10^{-3}$ ). Starspot-induced variability is the dominant signal; flares are shown with gray crosses. Dashed lines indicate the five transits observed by TESS over Sectors 10 and 11. Middle: Zoomed windows of individual transits. Gray lines are the best-fit transit model, which includes a local quadratic trend in each window. Bottom: Phase-folded TESS transit. Gray points are 2-minute PDCSAP flux measurements with the local spot-induced variation removed. Black points are binned to 6-minute intervals. The black error-bar shows the median uncertainty for the black points. The gray line is the best-fit model to the combined TESS and ground-based data (Table 3).

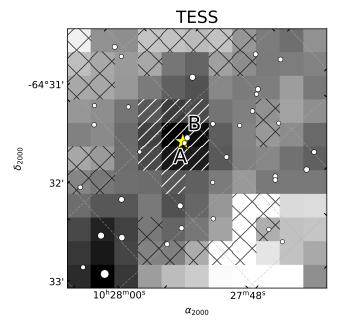


Figure 2. Scene of TOI 837. Mean TESS image of TOI 837 over Sector 10, with a logarithmic grayscale. The yellow star is the position of TOI 837. White circles are resolved Gaia sources with T < 16 (brighter stars are larger). The black X and white / hatches show the apertures used to measure the background and target star flux, respectively. Dashed lines of constant declination and right ascension are shown. Two stars of interest are "Star A" and "Star B", which were eventually excluded as being possible sources of the transits.

The TESS project detected the transits in the 2-minute data and the community was alerted on 17 June 2019. While our CDIPS FFI light curves also showed the transits, the 2-minute data had better sampling cadence, and so we opted to use the Presearch Data Conditioning (PDC) light curve with the default aperture for our analysis (Smith et al. 2012; Stumpe et al. 2014; Jenkins et al. 2016; Smith et al. 2016).

Figure 1 shows the data. The dominant modulation induced by starspots coming into and out of view has a peak-to-peak amplitude of about 2.3%, and a period of about 3 days. The dips suggestive of a grazing transiting planet recur roughly every 8 days, and have a depth of about 0.4%. A few flares are visible. A phase-folded view of the TESS transits with starspot variability removed is shown in Figure 1. Our fitting procedure for the models shown in these plots is described in Section 4.3.

#### 2.2. Gaia Astrometry and Imaging

Between 25 July 2014 and 23 May 2016, the ESA Gaia satellite measured about 300 billion centroid positions of 1.6 billion stars. The positions, proper motions, and parallaxes of the brighest 1.3 billion were calculated for the second data release (DR2) (Gaia Collaboration et al. 2016; Lindegren et al. 2018; Gaia Collaboration et al. 2018). TOI 837 was assigned the Gaia DR2 identifier 5251470948229949568, and had 276 "good" astrometric observations. Its brightness was

measured in the *G*, *Rp*, and *Bp* bands of the Radial Velocity Spectrometer (Cropper et al. 2018; Evans et al. 2018).

The Gaia imaging, reduced to its point-source catalog, provides the initial context for analyzing the TESS data. Stars brighter than T=16, as queried from the Gaia DR2 source catalog, are shown with white circles in Figure 2, overlaid on the TESS image. Given its galactic latitude of  $b=-6^{\circ}$ , it is not surprising that the field of TOI 837 is crowded. The resolved stars that were of immediate concern for our false positive analysis were as follows.

- TOI 837  $\equiv$  TIC 460205581 (T = 9.9). The target star.
- Star A  $\equiv$  TIC 847769574 (T=14.6), 2.3" west. The proper motions and parallax of this star imply it is comoving with TOI 837 and that the two stars are separated by  $6.6 \pm 0.1$  pc. Star A is therefore likely an IC 2602 member, but unlikely to be a bound binary compnaion.
- Star B  $\equiv$  TIC 460205587 (T = 13.1), 5.4" north. The Gaia parallax implies this is a giant background star.

An additional source, TIC 847769581, is 4.9'' from the target, but too faint (T = 18.8) to be the source of the observed transit signal.

The Gaia DR2 data for Star A seems poorly behaved. While Star A has G = 15.1, and Bp = 14.9, no Rp magnitude is reported. Correspondingly, no RUWE<sup>2</sup> value is available. We suspect that the photometric failure to produce an Rp magnitude as well as its poor astrometric fit are due to blending with TOI 837.

At the  $\approx 1'$  resolution of the TESS data, if either Star A or Star B were eclipsing binaries, they could be the sources of the transit signal. A detailed analysis of ground-based seeing-limited photometry was necessary to assess and rule out this possibility (Section 2.4).

# 2.3. High-Resolution Imaging

To determine if any fainter point sources existed closer to TOI 837 inside of Gaia's point-source detection limits, we acquired high-resolution speckle images. We then searched the autocorrelation functions of these images for peaks indicative of nearby companions.

The observations of TOI 837 were initially acquired by Ziegler et al. (2020) as part of the Southern Astrophysical Research (SOAR) TESS Survey using the High Resolution Camera (HRCam; Tokovinin 2018). The HRCam *I*-band filter is described by Tokovinin (2018). The points in Figure 4 show the resulting measured 5- $\sigma$  detectable contrasts. The lines are linear smoothing fits between the regimes of the diffraction limit, the "knee" at  $\approx 0.2$ ", and the slow decrease until  $\approx 1.5$ ", beyond which the speckle patterns become de-correlated. Star A (TIC 847769574) was detected

<sup>&</sup>lt;sup>2</sup> See the Gaia DPAC technical note GAIA-C3-TN-LU-LL-124-01, http://www.rssd.esa.int/doc\_fetch.php?id=3757412, 2020-07-08.

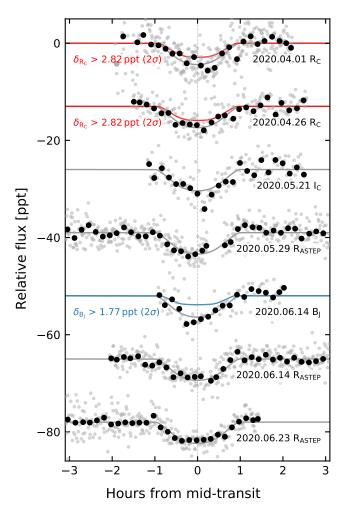


Figure 3. Ground-based follow-up photometry. The data were acquired using the 0.36m at El Sauce and the 0.40m ASTEP400 at Dome C. Black points are binned to 10-minute intervals. The gray line is the best-fit model to the combined TESS and ground-based data. Models show  $2\sigma$  lower limits on the transit depths in the Cousins-R and Johnson-B bandpasses used to rule out specific false positive scenarios (see Section 3.1.5).

at the expected location and brightness contrast, and no additional companions were found. Star B was not detected; with a separation of 5.4'' from TOI 837, it fell outside the field of view.

## 2.4. Ground-based Time-Series Photometric Follow-up

We obtained ground-based seeing-limited time series photometric observations of TOI 837 bracketed around the times of transit. These observations confirmed that the transits occurred on-target to within  $\approx 2''$ , and that they were achromatic. Both features are essential for our ability to eliminate false-positive scenarios.

# 2.4.1. El Sauce 0.36m

Acquisition and reduction—We observed four transits with the 0.36m at Observatario El Sauce, located in the Río Hurtado

Valley in Chile, and operated by co-author P. Evans. The observations were obtained in Cousins-R band on the nights of 1 April 2020 and 26 April 2020, Cousins-I band on the night of 21 May 2020, and Johnson-B band on the night of 14 June 2020. The final 14 June transit began shortly after twilight.

We scheduled our transit observations using the TESS Transit Finder, which is a customized version of the Tapir software package (Jensen 2013). The photometric data were calibrated and extracted using AstroImageJ (Collins et al. 2017). Comparison stars of similar brightness were used to produce the final light curves, each of which showed a roughly 4ppt dip near the expected transit time. The data are reported in Table 4 and plotted in Figure 3.

Custom aperture analysis—Based solely on the TESS data, both Star A and Star B were possible sources of blended eclipsing binary signals. The typical FWHM for stars in the El Sauce observations was  $\approx 2.3''$ , with a variance of  $\approx 0.2''$ . Star B is resolved in the 0.36m images; Star A is not.

To rule out blend scenarios with the ground-based photometry, we produced light curves centered on TOI 837 with circular apertures of radii ranging from 0.7" to 5.1". We did not detect any statistically significant variation in the depth of the transits with aperture size. Two lines of evidence rule out Star B as the eclipsing source: first, the transits were detected in the smallest apertures. Second, we made light curves with 2.1" apertures centered on Star B, and they did not show the transit.

To assess the possibility that Star A is an eclipsing body, we created light curves with a custom set of circular apertures with radii of 2.1" and positions ranging from Star A (2.3" west of TOI 837) to 2.3" east of TOI 837. We did not detect any variation of the transit depth along this line of light curves. The apertures east of TOI 837 exclude over 90% of the flux from Star A. The eclipse on Star A would therefore need to have depth greater than unity to produce the observed eclipse depth. We therefore interpret the lack of asymmetry between the western-most (centered on Star A) and eastern-most (furthest from Star A) light curves as conclusive evidence that TOI 837 is the source of the transit signal to within  $\approx 2.0''$ . To verify self-consistency, we checked that the maximum dilution from Star A ( $\approx 1\%$ ) is less than the uncertainty of the transit depth measurements  $(\approx 15\%)$ , and so the lack of variation of transit depth with aperture location is consistent with TOI 837 being the source of transits.

### 2.4.2. ASTEP400

We observed three transits with the 0.40m ASTEP telescope at the Concordia base on the Antarctic Plateau (Daban et al. 2010). Concordia base is operated jointly by the French and Italian polar institutes, IPEV and PNRA. Its position on the Antarctic Plateau at lat 75.06°S, long 123.3°E allows it to take advantage of the continuous night during Austral winter. The weather is of photometric quality for about two-thirds of each winter (Crouzet et al. 2018).

ASTEP is equipped with a FLI Proline science camera with a KAF-16801E, 4096 × 4096 front-illuminated CCD. The camera has an image scale of 0.93 arcsec pixel<sup>-1</sup> resulting in a 1° × 1° corrected field of view. The focal instrument dichroic plate splits the beam into a blue wavelength channel for guiding, and a non-filtered red science channel roughly matching a Cousins-R transmission curve (Abe et al. 2013; Mékarnia et al. 2016). The images were processed on-site using an automated aperture photometry pipeline based on the daophot package of the IDL astronomy user's library (Landsman 1995).

TOI 837 was observed with ASTEP on 12 May 2020, 29 May 2020, 14 June 2020, and 23 June 2020 (UT) with a cadence of 50s (exposure time of 25s, readout and processed overhead of 25s). Except for 12 May, our observations were conducted under stable weather conditions, with clear skies, temperatures of about  $-70^{\circ}$ C, and wind speeds inferior to 5 ms<sup>-1</sup>. Due to their poor quality, we exclude from the analysis all data collected on May 12. We found that the optimal calibrated light curves of TOI 837 correspond to an 11 pixel (10 arcsec) and 14 pixel (12 arcsec) radius aperture for observations carried out on June and May, respectively. The data are reported in Table 4, and are plotted in Figure 3.

# 2.5. Spectroscopic Follow-up

Reconaissance spectroscopic follow-up is an essential step in vetting planet candidates. Medium to high-resolution spectra enable physical characterization of the star and therefore planet. Reducing multiple spectra to a radial velocity time-series can enable planet mass measurements, and also set limits on the mass of any nearby companions. Finally, if there are close or bright companions, reconaissance spectra can also reveal the presence of a secondary set of stellar lines.

# 2.5.1. SMARTS 1.5m / CHIRON

We acquired nine spectra using CHIRON at the SMARTS 1.5m telescope at Cerro Tollo Inter-American Observatory, Chile (Tokovinin et al. 2013). Six met our signal-to-noise requirements for radial velocity measurements and stellar parameter extraction. We used CHIRON in its image slicer configuration, yielding a spectral resolution of  $\approx 79,000$  across 415–880 nm.

George TODO: please describe the formal secondary line search in more depth in this paragraph We searched for secondary lines in the CHIRON spectra by cross-correlating against a **template of some kind**. This rules out lines with flux ratios of  $\approx 2\%$ , if the lines are well-separated in velocity. To derive the star's physical parameters, we cross-correlated the template against **something**, and used the **nameofcode**. We measured the radial velocities through a least-squares deconvolution of the observed spectra against the same synthetic template. The resulting velocities are given in Table 5, and shown in Figure 4.

# 2.5.2. *FEROS*

We acquired 13 spectra using the FEROS echelle spectrograph, mounted on the MPG 2.2m telescope at the European

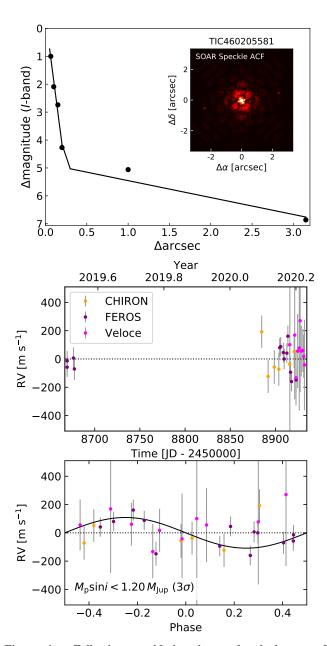


Figure 4. Following speckle-imaging and velocimetry of TOI 837. *Top:* SOAR HRCam contrast limits derived from point-source injection-recovery experiments. Star A ( $\Delta T = 4.7, 2.3''$  west) is detected in the autocorrelation function, and is also a resolved Gaia source. It is co-moving with TOI 837, and its parallax and on-sky position imply that it is physically separated from TOI 837 by  $6.6 \pm 0.1\,\mathrm{pc}$ . *Middle:* Radial velocity (RV) measurements, with best-fit instrument offsets and jitter terms included. The expected scatter from starspots based on  $v\sin i$  and the photometric modulation amplitude is of order  $300\mathrm{m\,s^{-1}}$ . *Bottom:* RV measurements phased to the orbital ephemeris of TOI 837.01. The planet is not detected. The black line shows a circular Keplerian orbit representing the  $3\sigma$  upper mass limit.

Soutern Observatory in La Sille, Chile (Kaufer et al. 1999). FEROS has a resolution of  $\approx 48,000$  across a spectra range of 350–920 nm. It has a remarkably high efficiency of  $\approx 20\%$ .

We used the dedicated instrument pipeline to extract 1-dimensional, wavelength calibrated spectra. To measure radial velocities, **Rafael/Paula TODO: what procedure was used? What software packages?**. The velocities are given in Table 5, and shown in Figure 4.

#### 2.5.3. *Veloce*

We acquired 34 spectra over 10 visits of TOI 837 using the Veloce spectrograph, mounted on the AAT 4.0m telescope at Siding Spring Observatory near Coonabarabran, Australia (Gilbert et al. 2018). In the "Rosso" instrument-mode, Veloce provides coverage from 600–950 nm at a spectral resolution of  $\approx 80,000$ .

Many of the exposures were taken in average or poor seeing conditions, when fiber-to-fiber cross-contamination on the IFU-style fiber feed is strongest. To reduce the spectra to velocities, we cross-correlated against a high S/N template of  $\delta$  Pavonis. The velocity RMS seen across each visit was hundreds of meters per second, likely due to uncorrected fiber-to-fiber cross-contamination. For analysis purposes, we averaged across each visit, and set the velocity uncertainties to be the standard deviation of the per-visit exposures. The velocities are given in Table 5, and shown in Figure 4.

#### 3. ELIMINATION OF FALSE POSITIVE SCENARIOS

Validating a transiting planet means statistically arguing that the data are much more likely to be explained by a planet than by an astrophysical false positive. The concept of validation has been developed and calibrated by *e.g.*, Torres et al. (2011); Morton (2012); Díaz et al. (2014); Santerne et al. (2015); Morton et al. (2016) and Giacalone & Dressing (2020). "Validation" is different from "confirmation", which means that there is overwhelming evidence that the transits *must* be explained by a planet, through elimination of all false positive scenarios and determination that the planety's mass is in the substellar regime.

Assuming an eclipse has been localized to the target star, potential false positive scenarios include eclipses of a background binary (BEB), eclipses of a hierarchical system bound to the primary star (HEB), and the possibility that the eclipses are simply caused by a stellar companion, rather than a planetary one (EB).

Figure 5 provides a visual summary of the possible astrophysical false positive scenarios, as well as our ability to rule them out based on our combined photometry, velocimetry, and imaging. In this Section we describe each constraint in turn, and then present a calculation using VESPA (Morton 2012) to demonstrate that the probability TOI 837 is an astrophysical false positive is small enough to formally validate it as a planet.

### 3.1. Constraints on False Positive Scenarios

3.1.1. Transit Depth

In HEB and BEB scenarios, the flux from TOI 837 and the true eclipsing binary host blend together, and reduce the "true" eclipse depth  $\delta_{\text{true}}$  to the observed depth  $\delta_{\text{obs}}$ :

$$\delta_{\text{obs}} = \delta_{\text{true}} \frac{F_{\text{comp}}}{F_{\text{total}}},\tag{1}$$

where the total system flux and the flux from only the companion ("comp") binary are labeled appropriately. The requirement that the eclipse is produced by fusion-powered stars and that  $\delta_{\text{true}} < 0.5$  translates to a bound on the faintest possible blended companion system:

$$\Delta m < -\frac{5}{2} \log_{10} \left( \frac{0.5}{\delta_{\text{obs}}} \right). \tag{2}$$

For TOI 837 (T = 9.93), this implies that any stellar companion invoked to explain the transit depth must be brighter than T = 15.07. In Figure 5, we set the spatial limit to 2" based on the precision at which we have localized the transits using seeing-limited ground-based photometry.

If the transit were box-shaped, this argument could be extended to even more restrictive depths (*e.g.*, Seager & Mallén-Ornelas 2003; Vanderburg et al. 2019; Rizzuto et al. 2020) Since the transits of TOI 837 are grazing, the second and third contact points do not occur, and the shape of the transit is not restrictive.

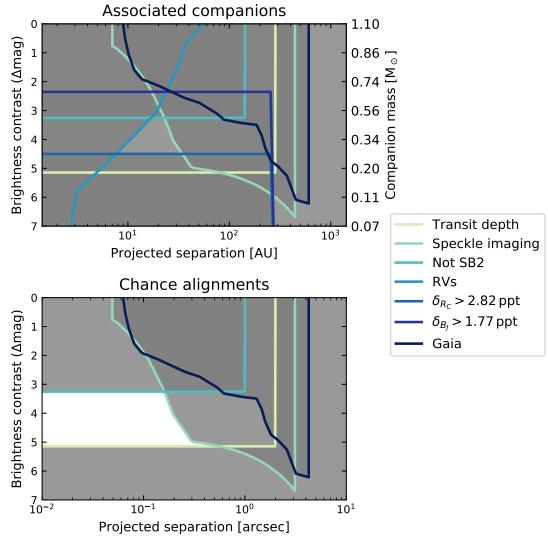
## 3.1.2. Speckle Imaging

The contrast limits obtained through the SOAR *I*-band speckle imaging (Section 2.3) are shown in Figure 5. While "Star A" was detected in the SOAR images, our ground-based photometry rules it out as a possible source of the eclipse signal (Section 2.4). To convert the remaining contrast constraints to limits on the masses of bound companions, we used the Baraffe et al. (2003) models for sub-stellar mass objects and the MIST models for stellar mass objects (Paxton et al. 2011, 2013, 2015; Dotter 2016; Choi et al. 2016). We assumed that the system age was 35 Myr, so that companions would be at a plausible state of contraction.

To convert from theoretical effective temperatures and bolometric luminosities to expected magnitudes in instrumental bandpasses, we made the simplying assumption that all sources had blackbody spectra. Using the theoretical stellar parameters and the measured transmission functions (Tokovinin 2018), we then calculated the apparent magnitudes of stellar companions of different masses, and interpolated to produce the scale shown on the upper-right in Figure 5.

#### 3.1.3. Not SB2

As described in Section 2.5.1, we searched the CCFs of the CHIRON spectra to determine whether TOI 837 is double-lined. For a stellar companion well-separated in velocity, this typically reveals companions with flux-fractions  $F_2/F_1 \gtrsim 2\%$ . For plotting purposes, in Figure 5 we have assumed a flux-fraction limit of 5% ( $\Delta$ mag  $\approx 3.25$ ).



**Figure 5. Astrophysical false positive scenarios.** *Top*: for bound companions (EB and HEB scenarios), *Bottom*: for unassociated companions along the same line of sight (BEB scenarios). Each constraint is described in Section 3.1. Gray regions are ruled out by at least one constraint.

3.1.4. RVs

The combined radial velocities from FEROS, CHIRON, and Veloce can be used to detect massive bound companions orbiting TOI 837. We searched for the presence of planetary and stellar-mass companions using radvel (Fulton et al. 2018). We assumed circular orbits, and performed two sets of fits.

For the first fit, we assumed a restrictive prior on the period and time of periapse, using the known ephemeris from the transit. We then fitted for the semi-amplitude, instrument offsets, and jitter parameters. This yielded a non-detection of the planet's orbit. The corresponding  $3-\sigma$  (99.7<sup>th</sup> percentile) upper limit on  $M_{\rm p} \sin i$  is  $1.20 M_{\rm Jup}$ . The data and corresponding model are shown in Figure 4.

The above exercise ruled out the possibility that the observed eclipses are caused by a stellar-mass object orbiting TOI 837. The lack of a linear trend in the radial velocities, particularly in the FEROS data, further constrains the pres-

ence of a hierarchical binary system. To derive limits for this second possibility, we placed a wide log-uniform prior on the semi-amplitude and period (log K [ms<sup>-1</sup>]  $\sim \mathcal{U}(1,10^5)$ , log P [days]  $\sim \mathcal{U}(0.1,10^{15})$ ). We then fitted for the semi-amplitude, period, time of conjunction, instrument offsets, and jitter parameters. We converted the resulting posterior in period and semi-amplitude to minimum mass and semi-major axis assuming Kepler's third law. The resulting  $3\sigma$  limits are shown in Figure 5.

# 3.1.5. Multicolor Photometry

Multicolor photometry and HEB scenarios—The most plausible HEB scenarios for TOI 837 involve pairs of eclipsing M dwarfs (Figure 5). Eclipses of such stars are much redder than eclipses of the G-dwarf TOI 837. Limits on whether the transit depth decreases in bluer bandpasses can therefore rule out some HEB scenarios.

We fitted for the observed depths in different bandpasses using a similar machinery as described in Section 4.3. We fitted each ground-based transit individually for the planet-to-star size ratio, the impact parameter, and a local quadratic trend (the ephemeris was assumed from an initial fit of only the TESS data). The corresponding  $2-\sigma$  limits on the transit depths in Cousins-R and Johnson-B band light curves were 2.82 and 1.77 ppt, respectively, and are shown in Figure 3. Particularly in our Johnson-B light curve, the transit depth is correlated with the mean and linear slope of the light curve: a smaller depth is allowed if the data are fitted with a larger linear slope and a larger mean. Our quoted limits marginalize over these correlations, and the depth measurement itself is nearly Gaussian.

To determine what classes of HEB are eliminated by these limits, we performed the following calculation. We assumed that each system was composed of the primary (TOI 837), plus a tertiary companion eclipsing a secondary companion every 8.3 days. For secondary masses ranging from 0.07 to  $1.10\,M_{\odot}$ , and mass ratios  $(M_3/M_2)$  from 0.1 to 1, we then calculated the observed maximal eclipse depth caused by Star 3 eclipsing Star 2 in each observed bandpass. As before, we interpolated between mass, effective temperature, and radius assuming the MIST isochrones for a 35 Myr old system, and also assumed that each source had a blackbody spectrum. We used the transmission functions from the SVO filter profile service<sup>3</sup>. For a typical HEB system (e.g.,  $M_2 = M_3 = 0.2 M_{\odot}$ ), the bluest optical bandpasses produced eclipses roughly 10 times shallower than in TESS-band, because the M-dwarf blackbody function turns over at much redder wavelengths than the G-dwarf blackbody (Wien's law).

For a fixed secondary mass, we then asked whether any tertiary companions existed for which the maximal expected eclipse depth could have been larger than the observed depth. In cases for which the answer was yes, we could not rule out such hierarchical eclipsing binary systems. Conversely, we ruled out systems for which at fixed secondary mass no tertiary mass could enable eclipses of the necessary depth (in  $R_C$ -band, or in  $B_J$ -band). The  $R_C$ -band limit corresponded to a secondary mass limit of  $M_2 > 0.27 M_{\odot}$ , and the  $B_J$ -band corresponded to a stronger limit of  $M_2 > 0.70 M_{\odot}$ .

Multicolor photometry and BEB scenarios—While the above constraints rule out HEBs, certain configurations of BEB systems (e.g., a background G2V+K6V binary) can produce blue eclipses while remaining undetected along the line of sight. Such scenarios are constrained by the lack of an observed secondary eclipse, and therefore require either eccentric orbits to avoid secondary eclipses, or else a background twin binary system at double the orbital period. The only way to definitively rule out such scenarios is to prove that the loss of light is from the target star, for instance by detecting the Rossiter-McLaughlin effect during a transit, and confirming that the spectroscopic transit is consistent with the photometric transit.

The "Gaia" curve in Figure 5 combines both point-source detections from imaging, and sources that show an astrometric excess. The curve was interpolated from Figure 4 of Rizzuto et al. (2018). TOI 837 has a RUWE statistic of 1.022, indicative that there are no obviously present astometric companions. The UWE statistic (square-root of the reduced astrometric  $\chi^2$ ) is 1.38, which is consistent with stars of similar brightness and color (Lindegren et al. 2018, Appendix A).

# 3.1.7. Patient Imaging

Archival SERC-J and AAO-SES plates are available for the TOI 837 field<sup>4</sup>. These plates were acquired in 1982 and 1992, respectively. For high proper motion stars archival imagery can be used to detect slowly moving background stars that might be an astrophysical false-positive source (*e.g.*, Huang et al. 2018, Vanderburg et al. 2019). However TOI 837 has only moved  $\approx 0.7''$  between 1982 and present, in comparison to the  $\approx 2.0''$  FWHM of the target on the plates. We therefore cannot resolve it with great confidence from background sources not already resolved through more modern imaging.

# 3.2. False positive probability

The constraints on false-positive scenarios summarized in Figure 5 rule out the possibilities that i) the eclipses are caused by a star orbiting TOI 837, ii) the eclipses are caused by hierarchical blends, and iii) the eclipses are caused by neighboring stars outside  $\approx 2''$ . The only scenario not formally ruled out is a background eclipsing binary. A simple (fallacious) argument on the a priori probability of background blends follows from counting statistics. The local density of T < 15.1 stars around TOI 837, found by counting from TIC8, is  $3.7 \times 10^{-4} \, \mathrm{arcsec^{-2}}$ . Therefore within the relevant  $\approx 0.3''$  radius not excluded by the SOAR HRCam contrast curve, for a randomly selected star we would expect  $1.0 \times 10^{-4}$  potential T < 15.1 contaminants, which appears small.

The reason the above statement is an insufficient argument against BEBs is that TOI 837 is not a randomly selected star—it was selected because it shows eclipses. Given a foreground star that shows eclipses, the probability of a background star being present is much greater than for an arbitrary foreground star. The relevant populations need to be modelled at the Monte Carlo level. We opt to use VESPA to perform this population modelling (Morton 2012, 2015b).

VESPA calculates the false positive probability for a transit signal as

$$FPP = 1 - P_{pl}, \tag{3}$$

where in our case the probability that the signal comes from a planet,  $P_{\rm pl}$ , is given by

$$P_{\rm pl} = \frac{\mathcal{L}_{\rm pl} \pi_{\rm pl}}{\mathcal{L}_{\rm pl} \pi_{\rm pl} + \mathcal{L}_{\rm BEB} \pi_{\rm BEB}},\tag{4}$$

<sup>3.1.6.</sup> *Gaia* 

<sup>&</sup>lt;sup>3</sup> http://svo2.cab.inta-csic.es/theory/fps/

<sup>4</sup> https://archive.stsci.edu/cgi-bin/dss\_form

where  $\mathcal{L}_i$  is the model likelihood for the planet and BEB scenarios, and  $\pi_i$  is the model prior. The terms labelled as "BEB" usually include other false positive scenarios (HEBs and EBs), but our followup data have excluded these possibilities. The priors are evaluated using a combination of galactic population synthesis (Girardi et al. 2005), binary star statistics (Raghavan et al. 2010), and specific planet occurrence rates (Morton 2012, Section 3.4). The likelihoods are evaluated by forward-modelling a representative population of eclipsing bodies for model class, in which each population member has a particular trapezoidal eclipse depth, total duration, and ingress duration. The likelihood is then calculated by multiplying the probability distribution function of simulated population's shape parameters with the posterior probability of the actual observed eclipse shape.

We ran VESPA<sup>5</sup>, and directly incorporated our constraints of the SOAR I-band contrast curve and a non-detection of secondary eclipses with a depth set at roughly twice the limits from the SPOC vetting report (0.1%). We verified that changing the secondary eclipse depth limit did not significantly affect the results. We set the maximum aperture radius at 2", based on our ground-based photometry. Incorporating the constraints from Figure 5, our nominal false positive probability analysis excluded EB and HEB scenarios. This yielded an FPP of 0.21% for TOI 837.01, sufficient for formal validation as a planet (Morton 2012). We did not incorporate our constraint that TOI 837 is not double-lined, which rules out an additional portion of BEB parameter space. Had we not acquired multicolor ground-based photometry, and been unable to exclude HEB scenarios, the FPP would have risen to 8%. Since the transits are achromatic (Figure 3), particularly in Johnson-B band, we can rule out HEB scenarios.

One potential caveat in our approach is that VESPA uses a galactic population synthesis to model the sight-line. Since TOI 837 is in the foreground of IC 2602 (see Section 4.2), for roughly 25 pc behind the sightline to the star, the number of background stars is higher than VESPA would predict due to the presence of the cluster. To quantify the importance of this effect, we assessed the sky-plane density of potential contaminants by counting stars brighter than T = 15.07 within 0.5 degrees of TOI 837 (Stassun et al. 2019). We then compared this density against sightlines rotated in galactic longitude towards and away from the galactic center. Within  $\pm 10^{\circ}$  in galactic longitude, the sky-plane density of stars fluctuated at the level of  $\approx 15\%$ , with a local maximum a few degrees away from TOI 837, towards the center of IC 2602. The overall density also slowly increased towards the galactic center. We therefore do not expect this consideration to significantly alter our FPP calculation.

#### 4. SYSTEM MODELLING

4.1. The Cluster

4.1.1. Physical Characteristics

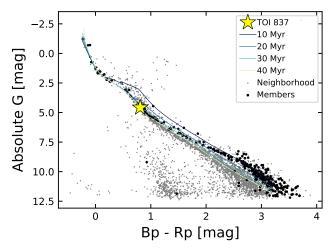


Figure 6. Hertzsprung-Russell diagram of TOI 837 and members of IC 2602. Members (black circles) were identified by Cantat-Gaudin et al. (2018). Gray circles are non-member stars within 5 standard deviations of the mean IC 2602 right ascension, declination, and parallax. G denotes Gaia broadband magnitudes, Bp Gaia blue, and Rp Gaia red. MIST isochrones (colored lines) fit the upper main sequence well, but diverge from the data for  $M_{\star} \lesssim 0.7 M_{\odot}$ . This is a known problem with PMS models (see Section 4.1.2).

The IC 2602 cluster is about 150pc from the Earth, and is near the galactic plane with  $(l,b) \approx (289.6^{\circ}, -5.0^{\circ})$  (Cantat-Gaudin et al. 2018). It is also sometimes called the  $\theta$  Carinae cluster, after its brightest member. While IC 2602 is close to the Lower Centaurus Crux subgroup of the Scorpio-Centaurus OB2 association in both position and proper motion space, its older age and clear kinematic separation indicate that it is a distinct stellar population (de Zeeuw et al. 1999; Damiani et al. 2019).

Reliable ages reported for IC 2602 range from 30–46 Myr. We have collected ages reported over the years in Table 1. The Li depletion boundary technique yields slightly older absolute ages than isochrone fitting (Dobbie et al. 2010; Randich et al. 2018). Rather than redetermine the age of the cluster and add another line to the table, we simply adopt an absolute age range for TOI 837 of 30–46 Myr.

Reported mean metallicity values [Fe/H] for the cluster range between slightly super-solar  $(0.04 \pm 0.01)$ , Baratella et al. 2020) and slightly sub-solar  $(-0.02 \pm 0.02)$ , Netopil et al. 2016). The extinction E(B-V) is rather low, with reported values ranging from 0.03 to 0.07 (e.g., Randich et al. 2018).

Kinematically, IC 2602 seems to be supervirial, in the sense that the observed stellar velocity dispersion is larger than the value expected if it were in virial equilibrium by about a factor of two (Bravi et al. 2018). Damiani et al. (2019) also reported evidence for the ongoing evaporation of IC 2602, in the form of a diffuse  $\approx 10^{\circ}$  halo of young stars around the central density cusps. A gyrochronological study of these stars could confirm that these stars are truly coeval with the cluster.

<sup>&</sup>lt;sup>5</sup> We used VESPA-0.6 and isochrones-1.2.2.

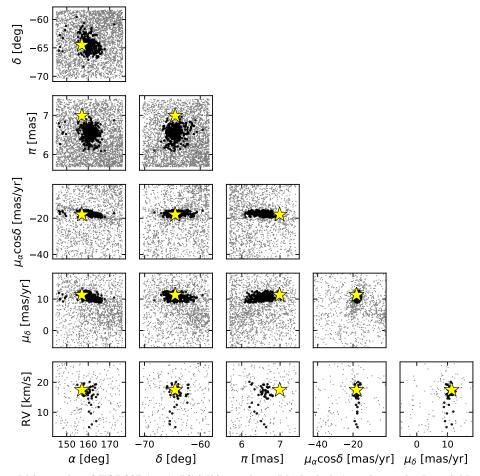


Figure 7. Positions and kinematics of TOI 837 (star), IC 2602 members (black circles), and stars in the neighborhood (gray circles). Members were identified by Cantat-Gaudin et al. (2018).  $\alpha$  denotes right ascension,  $\delta$  declination,  $\pi$  parallax,  $\mu_{\delta}$  and  $\mu_{\alpha}$  proper motion in each equatorial direction, and RV radial velocity reported by Gaia DR2. The RVs are for unblended spectra of bright stars ( $G \lesssim 12$ ). The proper motion projection ( $\mu_{\delta}$  vs.  $\mu_{\alpha}$  cos  $\delta$ ) highlights incompleteness in the membership selection function.

## 4.1.2. HR Diagram

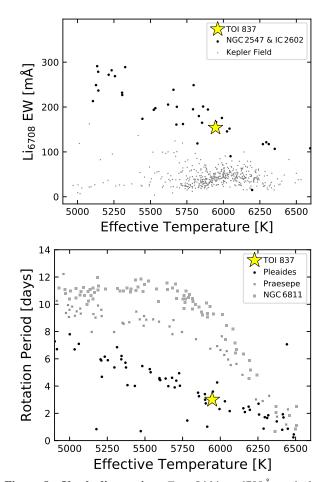
Figure 6 shows a Hertzsprung-Russell diagram of TOI 837, the IC 2602 cluster, and the "neighborhood" of spatially nearby stars. Stars labelled as "cluster members" are those reported by Cantat-Gaudin et al. (2018) based on Gaia DR2 positions, proper motions, and parallaxes. We included candidate members with formal membership probability exceeding 10%. Most members appear to be young and coeval. TOI 837 is in its expected position relative to the other members along the cluster isochrone. This photometrically limits the presence of binary companions in the TOI 837 system, to within perhaps half the brightness ( $\approx$  0.75 magnitudes) of the target star.

Figure 6 suggests that the membership census of IC 2602 is incomplete. We defined the reference "neighborhood" as the group of at most 10<sup>4</sup> randomly selected non-member stars within 5 standard deviations of the mean IC 2602 right ascension, declination, and parallax. We queried Gaia DR2 for these stars using astroquery (Ginsburg et al. 2018). Many low-mass stars appear above the main sequence, even though they were not identified as 5-dimensional kinematic

members through the unsupervised Cantat-Gaudin et al. (2018) membership assignment process.

Figure 6 also compares the data to the MIST isochrones (Choi et al. 2016). We used the web-interace<sup>6</sup> to interpolate isochrones at 10, 20, 30, and 40 million years. We assumed solar metallicity, and a fixed extinction value of  $A_V = 0.217$  (Randich et al. 2018). The 30 and 40 Myr models align well with the data for stars with masses ranging from roughly  $0.7-7M_{\odot}$ . The PMS K and M dwarf models are bluer than observed in the Gaia photometry. This discrepancy was noted and discussed at length by Choi et al. (2016). The most plausible explanation seems to be that strong magnetic fields in low-mass pre-main-sequence stars inhibit convection and produce a high filling factor of starspots (e.g., Stauffer et al. 2003; Feiden & Chaboyer 2013). To conserve flux, the stellar radius expands, and the star becomes cooler than a 1-dimensional model would predict.

<sup>&</sup>lt;sup>6</sup> http://waps.cfa.harvard.edu/MIST/interp\_isos.html, 2020-07-08



**Figure 8. Youth diagnostics.** *Top:* Lithium 6708Å equivalent widths for TOI 837, field stars, and young open clusters. The field star sample is drawn from Kepler planet hosts, and was measured by Berger et al. (2018) using Keck-HIRES. The young open clusters members were surveyed by Randich et al. (2018) using the UVES and GIRAFFE spectrographs at the ESO VLT. Randich et al. (2018) found lithium depletion boundary ages for these clusters of 37.7<sup>+5.7</sup><sub>-4.8</sub> Myr (NGC 2547) and 43.7<sup>+4.3</sup><sub>-3.9</sub> Myr (IC 2602). *Bottom:* Rotation periods for TOI 837 and selected open clusters. The Pleiades (120Myr), Praesepe (670Myr), and NGC 6811 (1000Myr) are shown. Their rotation periods were measured by Rebull et al. (2016); Douglas et al. (2017, 2019), and Curtis et al. (2019a), respectively.

#### 4.2. The Star

#### 4.2.1. Membership of TOI 837 in IC 2602

TOI 837 has been reported as a member of IC 2602 by many independent investigators (*e.g.*, Kharchenko et al. 2013; Oh et al. 2017; Cantat-Gaudin et al. 2018; Damiani et al. 2019; Kounkel & Covey 2019). The simplest way to verify the membership is through inspection of the Gaia DR2 position and kinematics. Figure 7 shows the six-dimensional positions and kinematics of TOI 837, IC 2602 members, and nearby stars. The "neighborhood" is defined as in Figure 6.

The axes limits for the right ascension, declination, and parallax dimensions are set by being within 5 standard deviations of the mean IC 2602 right ascension, declination, and parallax. The axes limits for the proper motion and radial velocity dimensions are set at the 25<sup>th</sup> and 75<sup>th</sup> percentiles, in order to give a sense of the population's distribution, while excluding outliers. The radial velocities suffer the greatest incompleteness due to the current  $G \approx 12$  magnitude limit of the Gaia DR2 data processing.

Figure 7 provides strong evidence that TOI 837 is a member of IC 2602. The only dimension that could lead to some worry is the parallax, as TOI 837 is one of the closest IC 2602 members reported by Cantat-Gaudin et al. (2018). Fortunately, there are independent means of verifying the star's youth.

#### 4.2.2. Rotation

As stars get older, their rotation rates incrementally slow due to magnetic braking Weber & Davis (1967); Skumanich (1972). One way to verify the youth of TOI 837 is by comparing its rotation period to other stars with known ages.

We measured the rotation period from the PDCSAP light curve using the Lomb-Scargle periodogram implemented in astropy (Lomb 1976; Scargle 1982; VanderPlas & Ivezić 2015). We fitted the light curve without masking out the transits or flares, as these represent a small fraction of the overall time series. To derive the uncertainty on the best period, we fitted a gaussian to the dominant peak, after first ensuring that we had oversampled the initial frequency grid. This gave a rotation period of  $P_{\rm rot} = 2.987 \pm 0.056 \,\mathrm{d}$  when allowing for a single Fourier terms in the periodogram model, and  $P_{\rm rot} = 3.004 \pm 0.053 \,\mathrm{d}$  when allowing for two Fourier terms. As the second model provides a better fit to the data, we adopt the second measurement.

As we will discuss in Section 4.2.4, we measured the star's radius by combining the spectroscopic effective temperature with a broadband photometry SED fit. We would expect, combining our  $R_{\star}$  and  $P_{\rm rot}$  measurements, that the equatorial velocity v of the star would be  $17.67 \pm 0.32 \, {\rm km \, s^{-1}}$ . Our spectroscopically measured  $v \sin i$  from CHIRON,  $17.48 \pm 0.15 \, {\rm km \, s^{-1}}$  agrees reasonably well with this expectation.

The star is clearly a rapid rotator. Figure 8 compares its rotation period with rotation periods that have been measured in a number of well-studied open clusters. TOI 837 seems to be gyrochronologically coeval with the Pleiades sequence. This is not to say that TOI 837 is "Pleaides-aged", because the observed scatter in the rotation-period diagram for the first 10–100 Myr is quite high (see Figure 9 of Rebull et al. 2020). Instead, we interpret the rotation period as evidence to support the claim that TOI 837 is younger than ~ 500 Myr.

## 4.2.3. *Lithium*

Lithium depletion for early G-dwarfs like TOI 837 requires hundreds of megayears (Soderblom et al. 2014). This is because their convective envelopes are shallow, and so transport of photospheric lithium to the hot core takes place over diffusive timescales, rather than convective timescales. Nonetheless, comparison of early G-dwarfs in the field to *e.g.*, 600 Myr old Hyads has shown that the depletion does indeed happen over many gigayears (Berger et al. 2018).

The spectra of TOI 837 all show the 6708 Å lithium doublet in absorption. Opting to use our FEROS spectra because of their high S/N, we measured the line's equivalent width (EW) to be  $154 \pm 9\,\text{mÅ}$ . Figure 8 compares this EW to stars in the field, and other young open cluster members. The field star measurements were collected by Berger et al. (2018); we show their reported lithium detections with S/N > 3. The young open cluster members were selected for the presence of lithium, as described by Randich et al. (2018). The measured TOI 837 Li EW is much larger than observed for field stars, and is consistent with lithium absorption seen in stars with similar colors in sub-100 Myr moving groups.

#### 4.2.4. Stellar Parameters

Select properties of TOI 837 from the literature and our analysis are presented in Table 2. We calculated the stellar parameters using two different approaches.

In "Method 1", we measured spectroscopic parameters from each of the CHIRON spectra (Section 2.5.1). We then calculated the stellar radius and reddening following Stassun et al. (2017). We first derived the bolometric flux by combining available broadband magnitudes from Gaia, Tycho-2, APASS, 2MASS, and WISE. We then fitted the SED with the Kurucz (2013) stellar atmopshere models, and summed to find  $F_{\text{bol}}$ . When fitting the atmosphere model, we varied the extinction ( $A_V$ ) and the overall normalization. This procedure yielded  $A_V = 0.20 \pm 0.03$ , which agrees with the average from the IC 2602 isochrone fits of Randich et al. (2018). Combining the spectroscopic effective temperature, bolometric flux, and Gaia distance, we determined the stellar radius using the Stefan-Boltzmann law. Combining this radius with the spectroscopic log g also yields a stellar mass.

In "Method 2", we simply used the observed location of TOI 837 in the HR diagram and interpolated against the 40 Myr isochrone. This method leverages the relative location of TOI 837 within the narrow IC 2602 isochrone to derive precise, theoretically self-consistent constraints on all of the stellar parameters. Although this approach would fail for a low-mass star, TOI 837 is above the stellar masses where the Gaia photometry and isochrone models begin to diverge.

Method 1 yielded a stellar mass that seemed to be high relative to the observed CHIRON effective temperature  $(1.21M_{\odot}$  to 5946 K, with relative uncertainties of a few percent on each). To avoid poorly understood systematics, we adopted the stellar parameters from Method 2, and report them in Table 2.

#### 4.3. The Planet

We fitted the available time-series photometry of TOI 837.01 as follows. For the PDCSAP light curve, we first eliminated points that had quality flags corresponding to any of bits  $\{3,4,6,8,11,12\}$ . This excluded cadences affected by coarse spacecraft pointing, reaction wheel desaturation events, manual flags, cosmic ray hits, and straylight

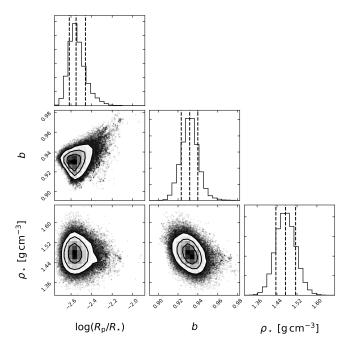


Figure 9. Posterior probabilities of impact parameter, planet-to-star size ratio, and stellar density. The planet-to-star size ratio corresponds to a planet size between  $0.65 R_{\text{Jup}}$  and  $0.91 R_{\text{Jup}}$  ( $3^{\text{rd}}$ – $97^{\text{th}}$  percentile). This plot was made using corner (Foreman-Mackey 2016).

from the Earth or Moon being present. Inspecting the data, we also manually excluded the two flares shown in Figure 1. We then trimmed the TESS data to windows of  $\pm 7\,\mathrm{hr}$  centered on each transit.

Our joint model for the TESS and ground-based data was an Agol et al. (2019) transit with physical and orbital parameters shared across all transit windows, plus a local quadratic trend allowed within each window. Select parameters and priors are listed in Table 3. In brief, we fitted for the shared stellar parameters ( $\log g$ ,  $R_{\star}$ ,  $u_0$ ,  $u_1$ ), and the shared planetary parameters ( $t_0$ , P, b,  $\log(R_p/R_{\star})$ ). There were also three free trend parameters for each of the twelve transits to account for the rotational variability. This yielded a total of 44 free parameters, of which 8 have physical relevance, and 36 are nuisance parameters. To keep the table at a manageable length, we only report the physically relevant parameters and derived quantities.

We fitted the model using PyMC3 (Salvatier et al. 2016; Theano Development Team 2016). For the exoplanet transit, we used the exoplanet code (Foreman-Mackey et al. 2020). After initializing each model with the parameters of the maximum *a posteriori* model, we assumed a Gaussian likelihood, and sampled using PyMC3's gradient-based No-U-Turn Sampler (Hoffman & Gelman 2014). We used  $\hat{R}$  as our convergence diagnostic (Gelman & Rubin 1992).

While alternative approaches are available for simultaneously fitting space and ground based photometry (in addition to radial velocimetry), we opted for this approach because *i*) the radial velocimetry on its own did not show ev-

idence for a planetary signal, *ii*) we expected that this approach would provide the best measurement of the planetary ephemeris, which is key for follow-up efforts, and *iii*) the assumption of identical limb-darkening across all bandpasses seemed justified by the level of precision in the ground-based data. The assumption of a constant radius across all bandpasses was tested by independently fitting each ground-based transit while letting the planetary radius float (Section 3.1.5). The transit depths did not significantly change between different bandpasses.

The posteriors from this procedure are given in Table 3. The transit is grazing. In the absence of a strong prior on the stellar density, the grazing geometry would hinder our ability to infer the planet-to-star size ratio. However, our priors on the stellar parameters from the cluster isochrone fit are strong enough that we can derive two-sided limits on the planet-to-star size ratio. The relevant posterior probabilities are shown in Figure 9.

## 5. DISCUSSION

TOI 837 joins a number of other young planetary systems reported from TESS, including DS Tuc Ab, HIP 67522b, TOI 1726, and AU Mic b (Newton et al. 2019; Zhou et al. 2019; Montet et al. 2019; Rizzuto et al. 2020; Mann et al. 2020; Plavchan et al. 2020; Palle et al. 2020; Addison et al. 2020; Martioli et al. 2020; Hirano et al. 2020). Unlike these planets, TOI 837.01 is validated but not yet confirmed.

The easiest path towards definitively confirming whether TOI 837 is a planet will be a Rossiter-McLaughlin (RM) measurement. Detection of an RM signal consistent with the photometric transit would rule out BEB and HEB scenarios, as it would imply that the eclipsing object is bound to the target star. Combined with our non-detection of the planet's mass from radial velocity monitoring, this would confirm that TOI 837.01 is a planet.

The maximum amplitude of the Rossiter-McLaughlin anomaly is (Gaudi & Winn 2007)

$$\Delta V_{\rm RM} \approx f_{\rm LD} \cdot \delta \cdot v \sin i \cdot \sqrt{1 - b^2} \approx 14 \,\mathrm{m \, s^{-1}},$$
 (5)

for

$$f_{\rm LD} = 1 - c_1 (1 - \mu) - c_2 (1 - \mu)^2,$$
 (6)

where  $\mu \approx (1-b^2)^{1/2}$ , and for calculation purposes we assumed b = 0.95 and used stellar and transit parameters from Tables 2 and 3. Although challenging, for a 1.84 hr transit of a V = 10.6 star, a detection could be achieved with modern spectrographs. The next viable total transit windows from Chile occur in January and February of 2021; there are also a few visible per season from other southern locations.

The Rossiter-McLaughlin approach is more likely to yield short-term success than a direct mass measurement because of the RV noise expected to be induced by stellar rotation. The photometric amplitude induced by starspots on TOI 837 is  $\approx 2\%$ . The spot-induced RV variation expected over the course of the  $\approx 3\,\mathrm{d}$  rotation period can then be estimated

by multiplying the photometric amplitude and spectroscopic equatorial velocity. This gives  $\sigma_{RV,rot}\approx 300\,\mathrm{m\,s^{-1}}$ , and is consistent with the scatter we observe in our radial velocities from FEROS. Detecting a planet's Doppler signal in these regimes is challenging, and requires a significant amount of data and care in signal extraction (Barragán et al. 2019). The Rossiter-McLaughlin measurement avoids the majority of this issue because the transit occurs over a much shorter duration than a single stellar rotation period.

If the RM measurements prove that the planet is real, a campaign to measure the mass timed to coincide with TESS sectors 36 and 37 (*i.e.*, from late March to late May of 2021) would significantly ease the extraction of the planetary Doppler signal. The reason is that the radial velocities, activity indicators, and photometry could then be modeled simultaneously, which would greatly constrain a Gaussian process model for the spot-induced RV signal.

#### **ACKNOWLEDGMENTS**

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*Software:* astrobase (Bhatti et al. 2018), AstroImageJ (Collins et al. 2017), astropy (Astropy Collaboration et al. 2018), astroquery (Ginsburg et al. 2018), cdips-pipeline (Bhatti et al. 2019) corner (Foreman-Mackey 2016), exoplanet (Agol et al. 2019) exoplanet (Foreman-Mackey et al. 2020), and its dependencies (Agol et al. 2019; Kipping 2013; Luger et al. 2019; Theano Development Team 2016). IDL Astronomy User's Library (Landsman 1995), IPython (Pérez & Granger 2007), isochrones (Morton 2015a), lightkurve (Lightkurve Collaboration et al. 2018), matplotlib (Hunter 2007), MESA (Paxton et al. 2011, 2013, 2015) numpy (Walt et al. 2011), pandas (McKinney 2010), pyGAM (Servén et al. 2018), PyMC3 (Salvatier et al. 2016), radvel (Fulton et al. 2018), scipy (Jones et al. 2001), tesscut (Brasseur et al. 2019), VESPA (Morton 2012, 2015b), webplotdigitzer (Rohatgi 2019), wotan (Hippke et al. 2019).

Facilities: Astrometry: Gaia (Gaia Collaboration et al. 2016, 2018). Imaging: Second Generation Digitized Sky Survey, SOAR (HRCam; Tokovinin 2018). Spectroscopy: CTIO1.5m (CHIRON; Tokovinin et al. 2013), MPG2.2m (FEROS; Kaufer et al. 1999), AAT (Veloce; Gilbert et al. 2018). Photometry: ASTEP:0.40m (ASTEP400), El Sauce:0.356m, TESS (Ricker et al. 2015).

Table 1. Previously reported ages for the open cluster IC 2602.

Method	Age [Myr]	Reference
MSTO isochrone	36.3	Mermilliod (1981)
PMS+MSTO isochrone	$30 \pm 5$	Stauffer et al. (1997)
Isochrone (a)	67.6	Kharchenko et al. (2005)
Isochrone (b)	221	Kharchenko et al. (2013)
Isochrone	67.6	van Leeuwen (2009)
LDB (c)	$46^{+6}_{-5}$	Dobbie et al. (2010)
MSTO isochrone (d)	41 - 46	David & Hillenbrand (2015)
MSTO isochrone (e)	37 - 43	David & Hillenbrand (2015)
Li selection + isochrone	$43.7^{+4.3}_{-3.9}$	Bravi et al. (2018)
Isochrone (f)	$30^{+9}_{-7}$	Randich et al. (2018)
LDB	$43.7_{-3.9}^{+4.3}$	Randich et al. (2018)
Isochrone	$35.5^{+0.8}_{-1.6}$	Bossini et al. (2019)
Isochrone	$35.5^{+14.6}_{-10.4}$	Kounkel & Covey (2019)

NOTE— MSTO  $\equiv$  main sequence turn-off. PMS  $\equiv$  pre-main-sequence. LDB  $\equiv$  lithium depletion boundary. (a) Based on location in HR diagram of just two stars. (b) Notes major age change since Kharchenko et al. (2005). (c) Dobbie et al. (2010) performed a dedicated study of the LDB in IC 2602. Comparing to early isochronal ages, they write their age is "consistent with the general trend delineated by the Pleiades,  $\alpha$ -Per, IC 2391, and NGC 2457, whereby the LDB age is 120-160 per cent of the estimates derived using more traditional techniques" such as isochrone fitting. (d) Using Ekström et al. (2012) evolutionary models. (e) Using PARSEC evolutionary models (Bressan et al. 2012). (f) Averaged across PROSECCO, PARSEC, MIST models in  $(J, H, K_s)$  and  $(J, H, K_s, V)$  planes.

Table 2. Literature and Measured Properties for TOI 837

Other identifiers TIC 460205581 GAIADR2 5251470948229949568 Parameter Description Value Source Right Ascension (hh:mm:ss)... 10:28:08.95  $\delta_{J2015.5}$ ..... Declination (dd:mm:ss)..... -64:30:18.76 l<sub>J2015.5</sub> . . . . . . Galactic Longitude (deg) . . . . . 288.2644 1  $b_{J2015.5}$ ...... Galactic Latitude (deg)...... -5.7950 1 V . . . . . . Johnson V mag. . . . . . . . . . . . 10.635  $\pm$  0.020 Rp...... Gaia Rp mag..... 9.887 $\pm$ 0.020 T...... TESS mag. ..... 9.9322±0.006  $J \dots \dots 2MASS \ J \ mag \dots 9.392 \pm 0.030$ 3 H..... 2MASS H mag. . . . . 9.108  $\pm$  0.038 3  $K_S$ ...... 2MASS  $K_S$  mag...... 8.933  $\pm$  0.026 3  $8.875 \pm 0.021$ 4 W3 . . . . . . WISE3 mag. . . . . . . . . 8.875  $\pm$  0.020 4  $8.936 \pm N/A$ in RA (mas yr<sup>-1</sup>) in DEC (mas yr<sup>-1</sup>) .....  $17.44 \pm 0.64^{\dagger}$ RV ..... Systemic radial velocity ( $km s^{-1}$ )  $v \sin i_{\star} \dots$  Rotational velocity (km s<sup>-1</sup>)  $17.48\pm0.15$ 5 [Fe/H]..... Metallicity .....  $-0.065 \pm 0.035$ 5  $T_{\text{eff}}$  ..... Effective Temperature (K)  $6047 \pm 40$ 6  $\log g_{\star}$  ...... Surface Gravity (cgs) .....  $4.467 \pm 0.010$ 6 Li EW . . . . . 6708Å Equiv. Width (mÅ) . . . .  $154 \pm 9$ *P*<sub>rot</sub> . . . . . Rotation period (d) . . . . . . .  $3.004 \pm 0.053$ 8 Adopted stellar age (Myr) . . . . 30-46 9 Age Spec. Type . . . Spectral Type . . . . . . . . . . . . G0V 5  $R_{\star}$  ...... Stellar radius  $(R_{\odot})$  ......  $1.022 \pm 0.015$ 6  $M_{\star}$  ...... Stellar mass  $(R_{\odot})$  .....  $1.118 \pm 0.011$ 6 A<sub>V</sub>..... Interstellar reddening (mag)... 10  $0.20 \pm 0.03$ 

NOTE—† Systemic RV uncertainty is the standard deviation of single-transit radial velocities, as quoted in Gaia DR2. Provenances are: <sup>1</sup>Gaia Collaboration et al. (2018), <sup>2</sup>Stassun et al. (2019), <sup>3</sup>Skrutskie et al. (2006), <sup>4</sup>Wright et al. (2010), <sup>5</sup>CHIRON spectra, <sup>6</sup>Method 2 (cluster isochrone, Section 4.2.4), <sup>7</sup>FEROS spectra, <sup>8</sup>TESS light curve, <sup>9</sup>IC 2602 ages from isochrone & lithium depletion analyses (Section 4.1.1), <sup>10</sup>Method 1 (photometric SED fit, Section 4.2.4).

**Table 3.** Best-fit transit model priors and posteriors.

Parama								
6/0	Param.	Unit	Prior	Median	Mean	Std. Dev.	3%	97%
$   \log R_p/R_r   =   U(-4.605;0.000)   2.55384   2.24233   0.0086   0.0945   0.9474   u_1                                      $		d	N(8.3249; 0.1000)	8.3248764	8.3248763	0.0000155	8.3248471	8.3249057
$   \log R_p/R_r   =   U(-4.605;0.000)   2.55384   2.24233   0.0086   0.0945   0.9474   u_1                                      $	$t_0^{(1)}$	d	$\mathcal{N}(1574.273800; 0.1000)$	1574.2725293	1574.2725235	0.0005870	1574.2713802	1574.2735879
$a_1$   $a_1$   $a_2$   $a_3$   $a_4$   $a_5$   $a_5$		_	$\mathcal{U}(-4.605; 0.000)$	-2.55384	-2.54233	0.08209	-2.68504	-2.39643
a <sub>2</sub> -         (2)         0.086         0.096         0.383         0.562         0.773           R,         R <sub>O</sub> 7(1.022;0.015)         1.022         1.022         0.015         0.0393         1.048           log g         cgs         N/(1.00;0.01)         0.985         0.9985         0.0001         0.9984         0.9987           a <sub>CTESS</sub> -         N/(1.00;0.01)         0.0004         0.0003         0.0010         0.0003           a <sub>CTESS</sub> -         N/(1.00;0.01)         1.0088         1.0088         0.0013         0.0023         -0.024         -0.0140           a <sub>CTESS</sub> -         N/(1.00;0.01)         1.0088         1.0088         0.0001         1.0087         1.0080           a <sub>CTESS</sub> -         N/(1.00;0.01)         0.0138         0.0018         0.0003         -0.0144         -0.0492         0.0001         0.095         -0.0132           a <sub>CTESS</sub> -         N/(1.00;0.01)         0.0156         0.0156         0.0056         0.0001         0.0901         0.0013           a <sub>CTESS</sub> -         N/(1.00;0.01)         0.0013         0.0013         0.0015         0.0015           a <sub>CTESS</sub> -	b	-	$\mathcal{U}(0; 1 + R_{\rm p}/R_{\star})$	0.932	0.9321	0.0086	0.9145	0.9474
$R_{\bullet}$ $R_{\odot}$ $T(1,022,0.015)$ $1.022$ $1.025$ $0.015$ $0.993$ $1.049$ log $g$ cgs $V(1.000,01)$ $0.9985$ $0.0001$ $0.9984$ $0.9985$ $a_{17888}$ $a^{-1}$ $U(-0.05;0.05)$ $0.0004$ $0.0003$ $0.0010$ $0.0003$ $a_{27888}$ $a^{-1}$ $U(-0.05;0.05)$ $0.0182$ $0.0182$ $0.0003$ $0.0010$ $0.0003$ $a_{27888}$ $a^{-1}$ $U(-0.05;0.05)$ $0.0138$ $0.0013$ $0.0003$ $0.0144$ $0.0138$ $a_{17888}$ $a^{-1}$ $U(-0.05;0.05)$ $0.0138$ $0.0013$ $0.0003$ $0.0144$ $0.0132$ $a_{17888}$ $a^{-2}$ $U(-0.05;0.05)$ $0.0156$ $0.0156$ $0.0001$ $0.9990$ $0.9999$ $a_{17888}$ $a^{-2}$ $U(-0.05;0.05)$ $0.0156$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$	$u_1$	_	(2)	0.558	0.584	0.360	0.	1.169
log g	$u_2$	_	(2)	0.086	0.096	0.383	-0.562	0.773
αlters         -         N(1.00;0.01)         0.9985         0.9985         0.0001         0.9984         0.9987           αlters         σ²         U(-0.05;0.05)         -0.0004         -0.0004         0.0003         -0.0010         0.0000           αlters         σ²         U(-0.05;0.05)         -0.0182         -0.0182         0.0003         -0.0010         1.0089           αlters         -         N(1.00;0.01)         1.0088         1.0088         0.0001         1.0087         1.0089           αlters         σ²         U(-0.05;0.05)         -0.0138         -0.0138         0.0003         -0.0145         -0.0479           αστεss         σ²         U(-0.05;0.05)         0.0156         0.0156         0.0003         0.0150         0.0163           αστεss         σ²         U(-0.05;0.05)         0.0234         0.0233         0.0024         0.0188         0.0278           αστεss         σ²         V(-0.05;0.05)         0.0221         0.0211         0.0001         1.0011         1.0013         0.0004         0.014         0.0022           αυτεss         σ²         V(-0.05;0.05)         0.0021         0.0021         0.0001         0.0004         0.004         0.0028         0.0147	$R_{\star}$	$R_{\odot}$	T(1.022; 0.015)	1.022	1.022	0.015	0.993	1.049
a):TESS $d^{-1}$ $U(-0.05;0.05)$ $-0.0004$ $-0.0003$ $-0.0010$ $0.0003$ a):TESS $d^{-1}$ $U(-0.05;0.05)$ $-0.0182$ $-0.0182$ $0.0023$ $-0.0120$ $-0.0140$ a0;TESS $ V(-0.05;0.05)$ $-0.0138$ $-0.0188$ $0.0003$ $-0.0144$ $-0.0132$ a1;TESS $d^{-1}$ $U(-0.05;0.05)$ $-0.0138$ $-0.0138$ $0.0003$ $-0.0144$ $-0.0132$ a2;TESS $d^{-1}$ $U(-0.05;0.05)$ $0.0156$ $0.0156$ $0.0003$ $0.0150$ $0.0163$ a2;TESS $d^{-1}$ $U(-0.05;0.05)$ $0.0234$ $0.0233$ $0.0024$ $0.0163$ a2;TESS $d^{-1}$ $U(-0.05;0.05)$ $0.0214$ $0.0233$ $0.0024$ $0.01163$ a1;TESS $d^{-1}$ $U(-0.05;0.05)$ $0.0021$ $0.0021$ $0.0004$ $0.0004$ $0.0014$ $0.0014$ a1;TESS $d^{-1}$ $U(-0.05;0.05)$ $0.0021$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ <td><math>\log g</math></td> <td>cgs</td> <td><math>\mathcal{N}(4.467; 0.010)</math></td> <td>4.467</td> <td>4.467</td> <td>0.009</td> <td>4.450</td> <td>4.485</td>	$\log g$	cgs	$\mathcal{N}(4.467; 0.010)$	4.467	4.467	0.009	4.450	4.485
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$a_{0:TESS}$		$\mathcal{N}(1.00; 0.01)$	0.9985	0.9985	0.0001	0.9984	0.9987
		$d^{-1}$	$\mathcal{U}(-0.05; 0.05)$	-0.0004	-0.0004	0.0003	-0.0010	0.0003
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	$a_{2:TESS}$	$d^{-2}$	$\mathcal{U}(-0.05; 0.05)$	-0.0182	-0.0182	0.0023	-0.0224	-0.0140
$a_{1,TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $-0.0138$ $-0.0138$ $-0.0007$ $-0.05$ $-0.0132$ $a_{2,TESS}$ $a_{1}$ $U(-0.05;0.05)$ $-0.0494$ $-0.0492$ $0.0007$ $-0.05$ $-0.0175$ $a_{1,TESS}$ $a_{1}$ $U(-0.05;0.05)$ $0.0156$ $0.0156$ $0.0003$ $0.0150$ $0.0163$ $a_{2,TESS}$ $a_{2}^{2}$ $U(-0.05;0.05)$ $0.0234$ $0.0233$ $0.0024$ $0.0188$ $0.0273$ $a_{1,TESS}$ $a_{2}^{2}$ $U(-0.05;0.05)$ $0.0021$ $0.0021$ $0.0004$ $0.0014$ $0.0024$ $a_{1,TESS}$ $a_{1}^{2}$ $U(-0.05;0.05)$ $0.0021$ $0.0021$ $0.0004$ $0.0014$ $0.0014$ $a_{1,TESS}$ $a_{1}^{2}$ $U(-0.05;0.05)$ $0.0015$ $0.0004$ $0.0022$ $0.0014$ $0.0003$ $0.0009$ $0.0022$ $a_{2,TESS}$ $a_{1}^{2}$ $U(-0.05;0.05)$ $0.0015$ $0.0015$ $0.0003$ $0.0009$ $0.0022$ $a_{2,TESS}$ $a_{1}^{2}$		_	$\mathcal{N}(1.00; 0.01)$	1.0088	1.0088	0.0001	1.0087	1.0089
$a_{2,TESS}$ $d^2$ $U(-0.05;0.05)$ $-0.0494$ $-0.0492$ $0.0007$ $-0.05$ $-0.0499$ $a_{1,TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0156$ $0.0156$ $0.0003$ $0.0150$ $0.0163$ $a_{2,TESS}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0234$ $0.0233$ $0.0024$ $0.0188$ $0.0278$ $a_{0,TESS}$ $ N(1.00;0.01)$ $1.0013$ $1.0013$ $0.0004$ $0.0141$ $0.0029$ $a_{0,TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0021$ $0.0021$ $0.0004$ $0.0014$ $0.0014$ $0.0022$ $a_{0,TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0004$ $0.0004$ $0.0014$ $0.0044$ $0.0022$ $0.0004$ $0.0014$ $0.0004$ $0.0014$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0003$ $0.0009$ $0.0005$ $0.0035$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$ $0.0004$		$d^{-1}$	$\mathcal{U}(-0.05; 0.05)$	-0.0138	-0.0138	0.0003	-0.0144	-0.0132
$a_{0,TESS}$ - $\mathcal{N}(1,00;0.01)$ 0.9992         0.9991         0.0901         0.9990         0.9993 $a_{1,TESS}$ $d^{-2}$ $\mathcal{U}(-0.05;0.05)$ 0.0156         0.0156         0.0003         0.0150         0.0163 $a_{2,TESS}$ $d^{-2}$ $\mathcal{U}(-0.05;0.05)$ 0.0021         0.0021         0.0001         1.0011         1.0015 $a_{1,TESS}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ 0.0021         0.0021         0.0004         0.014         0.0022 $a_{0,TESS}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ 0.0094         0.0094         0.0004         0.0147         -0.0042 $a_{0,TESS}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ 0.0015         0.0015         0.0001         0.9905         0.9908 $a_{1,TESS}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ 0.0015         0.0015         0.0003         0.0007         0.0022 $a_{1,TESS}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ 0.0014         0.0044         0.0023         0.00271         0.0357 $a_{0,Sauce}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ 0.0319         0.0264         0.0198         0.0120		$d^{-2}$	$\mathcal{U}(-0.05; 0.05)$	-0.0494	-0.0492	0.0007	-0.05	-0.0479
$a_{1:TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0156$ $0.0156$ $0.0003$ $0.0180$ $0.0278$ $a_{2:TESS}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0234$ $0.0233$ $0.0024$ $0.0188$ $0.0278$ $a_{1:TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0021$ $0.0021$ $0.0004$ $0.0014$ $0.0014$ $a_{1:TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0021$ $0.0004$ $0.0004$ $0.0014$ $0.0002$ $a_{2:TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0015$ $0.0003$ $0.0009$ $0.0001$ $0.9905$ $0.9905$ $0.9905$ $0.0003$ $0.0009$ $0.0003$ $0.0009$ $0.0001$ $0.9995$ $0.0001$ $0.9993$ $0.9995$ $0.0001$ $0.9993$ $0.9997$ $0.0001$ $0.9993$ $0.9997$ $0.0001$ $0.9993$ $0.9997$ $0.0001$ $0.9993$ $0.9997$ $0.0001$ $0.9993$ $0.9997$ $0.0001$ $0.9993$ $0.9993$ $0.9993$ $0.9993$ $0.9993$ $0.9993$		_	$\mathcal{N}(1.00; 0.01)$	0.9992	0.9992	0.0001	0.9990	0.9993
$a_{2,TESS}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0234$ $0.0233$ $0.0024$ $0.0188$ $0.0278$ $a_{0,TESS}$ - $V(1.00;0.01)$ $1.0013$ $1.0013$ $0.0001$ $1.0011$ $1.0015$ $a_{1,TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0021$ $0.0021$ $0.0004$ $0.0028$ $-0.0147$ $-0.0042$ $a_{0,TESS}$ - $V(1.00;0.01)$ $0.9996$ $0.0001$ $0.9995$ $0.9998$ $a_{1,TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0015$ $0.0003$ $0.0009$ $0.9998$ $a_{1,TESS}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0314$ $0.0015$ $0.0003$ $0.0029$ $0.0021$ $0.0033$ $0.0021$ $0.0039$ $0.0001$ $0.0999$ $0.0001$ $0.0999$ $0.0001$ $0.0999$ $0.0001$ $0.0999$ $0.0001$ $0.0999$ $0.0001$ $0.0999$ $0.0001$ $0.0999$ $0.0001$ $0.0999$ $0.0001$ $0.0006$ $0.0006$ $0.0006$ $0.0006$ $0.0006$ $0.$		$d^{-1}$	$\mathcal{U}(-0.05; 0.05)$	0.0156	0.0156	0.0003	0.0150	0.0163
$a_{OTESS}$ - $\mathcal{N}(1.00; 0.01)$ 1.0013         1.0013         0.0001         1.0011         1.0015 $a_{ITESS}$ $a^{-2}$ $\mathcal{U}(-0.05; 0.05)$ 0.0021         0.0021         0.0004         0.0014         0.0029 $a_{OTESS}$ $a^{-2}$ $\mathcal{U}(-0.05; 0.05)$ 0.0001         0.9906         0.0001         0.9905         0.9908 $a_{ITESS}$ $a^{-1}$ $\mathcal{U}(-0.05; 0.05)$ 0.0015         0.0003         0.0009         0.0022 $a_{2TESS}$ $a^{-2}$ $\mathcal{U}(-0.05; 0.05)$ 0.0014         0.0014         0.0023         0.0071         0.055 $a_{0.5succ}$ $a^{-1}$ $\mathcal{U}(-0.05; 0.05)$ 0.0044         0.004         0.0023         0.008         0.006 $a_{0.5succ}$ $a^{-1}$ $\mathcal{U}(-0.05; 0.05)$ 0.0314         0.0044         0.0023         0.008         0.006 $a_{0.5succ}$ $a^{-1}$ $\mathcal{U}(-0.05; 0.05)$ 0.0319         0.0264         0.0198         0.0120         0.05 $a_{0.5succ}$ $a^{-1}$ $\mathcal{U}(-0.05; 0.05)$ 0.0314         0.0041         0.0023         0.001         0.0996		$d^{-2}$	$\mathcal{U}(-0.05; 0.05)$	0.0234	0.0233	0.0024	0.0188	0.0278
$a_{1:TESS}$ $d^{-1}$ $U(-0.05; 0.05)$ $0.0021$ $0.0021$ $0.0004$ $0.0004$ $0.0014$ $0.0014$ $a_{2:TESS}$ $d^{-2}$ $U(-0.05; 0.05)$ $0.0094$ $0.0004$ $0.0028$ $-0.0147$ $0.0042$ $a_{0:TESS}$ $d^{-1}$ $U(-0.05; 0.05)$ $0.0015$ $0.0001$ $0.9905$ $0.9906$ $a_{1:TESS}$ $d^{-1}$ $U(-0.05; 0.05)$ $0.0014$ $0.0015$ $0.0003$ $0.0009$ $0.0022$ $a_{2:TESS}$ $d^{-2}$ $U(-0.05; 0.05)$ $0.0314$ $0.0314$ $0.0023$ $0.0271$ $0.0357$ $a_{0:Sauce}$ $ N(1.00; 0.01)$ $0.9995$ $0.9995$ $0.0001$ $0.9993$ $0.9997$ $a_{0:Sauce}$ $d^{-1}$ $U(-0.05; 0.05)$ $0.0319$ $0.0264$ $0.0198$ $-0.0120$ $0.05$ $a_{0:Sauce}$ $d^{-1}$ $U(-0.05; 0.05)$ $0.0331$ $0.0264$ $0.0198$ $0.0011$ $0.0038$ $a_{0:Sauce}$ $d^{-1}$ $U(-0.05; 0.05)$ $0.0367$				1.0013	1.0013	0.0001	1.0011	1.0015
$a_{2,TESS}$ $d^2$ $U(-0.05;0.05)$ $-0.0094$ $-0.0094$ $0.0028$ $-0.0147$ $-0.0042$ $a_{0,TESS}$ $ N(1.00;0.01)$ $0.9906$ $0.9906$ $0.0001$ $0.9905$ $0.9908$ $a_{1,TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0015$ $0.0013$ $0.0023$ $0.0271$ $0.0357$ $a_{0,Sauce}$ $ N(1.00;0.01)$ $0.9995$ $0.9995$ $0.0001$ $0.9993$ $0.9997$ $a_{1,Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ $0.004$ $-0.004$ $0.0023$ $0.008$ $0.0006$ $a_{2,Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0319$ $0.0264$ $0.0103$ $0.0012$ $0.006$ $a_{1,Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0319$ $0.0264$ $0.0198$ $0.0001$ $0.9996$ $0.0001$ $0.0996$ $0.0001$ $0.0996$ $0.0001$ $0.0006$ $0.0001$ $0.0006$ $0.0003$ $0.001$ $0.0003$ $0.001$ $0.0003$ $0.001$ $0.0006$ <		$d^{-1}$		0.0021		0.0004	0.0014	0.0029
$a_{0,TESS}$ - $N(1.00;0.01)$ 0.9906         0.9906         0.0001         0.9905         0.9908 $a_{1,TESS}$ $d^{-1}$ $U(-0.05;0.05)$ 0.0015         0.0015         0.0003         0.0009         0.0022 $a_{2,TESS}$ $d^{-2}$ $U(-0.05;0.05)$ 0.0314         0.0314         0.0023         0.0271         0.0357 $a_{0,Sauce}$ $ N(1.00;0.01)$ 0.9995         0.9995         0.0001         0.9993         0.9997 $a_{1,Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ 0.0044         -0.004         0.0023         -0.008         0.0006 $a_{2,Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ 0.0319         0.0264         0.0198         -0.0120         0.05 $a_{0,Sauce}$ $ N(1.00;0.01)$ 0.9998         0.0001         0.9996         1.0 $a_{1,Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ 0.0367         0.0323         0.0156         0.0033         0.05 $a_{2,Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ 0.0007         0.0029         0.0001         0.9996         1.0001 $a_{1,Sauce}$		$d^{-2}$			-0.0094	0.0028		-0.0042
$a_{1:TESS}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0015$ $0.0015$ $0.0003$ $0.0009$ $0.0022$ $a_{2:TESS}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0314$ $0.0023$ $0.0271$ $0.0357$ $a_{0:Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ $0.004$ $-0.004$ $0.0023$ $-0.098$ $0.0006$ $a_{2:Sauce}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0319$ $0.0264$ $0.0128$ $-0.008$ $0.0006$ $a_{2:Sauce}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0319$ $0.0264$ $0.0198$ $-0.0120$ $0.05$ $a_{0:Sauce}$ $ N(1.00;0.01)$ $0.9998$ $0.9998$ $0.0001$ $0.9996$ $1.001$ $a_{1:Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0367$ $0.0323$ $0.0156$ $0.0033$ $0.056$ $a_{2:Sauce}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0071$ $0.0007$ $0.0029$ $0.0063$ $0.0048$ $a_{2:Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0071$ $0.0046$ $0.027$				0.9906	0.9906	0.0001	0.9905	0.9908
$a_{2:TESS}$ $d^2$ $U(-0.05; 0.05)$ $0.0314$ $0.0314$ $0.0023$ $0.0271$ $0.0357$ $a_{0:Sauce}$ - $V(1.00; 0.01)$ $0.9995$ $0.9995$ $0.0001$ $0.9993$ $0.9997$ $a_{1:Sauce}$ $d^{-1}$ $U(-0.05; 0.05)$ $0.004$ $-0.004$ $0.0023$ $-0.008$ $0.0006$ $a_{2:Sauce}$ $d^2$ $U(-0.05; 0.05)$ $0.0319$ $0.0264$ $0.0198$ $-0.0120$ $0.05$ $a_{0:Sauce}$ - $V(1.00; 0.01)$ $0.9998$ $0.9998$ $0.0001$ $0.9996$ $1.$ $a_{1:Sauce}$ $d^{-1}$ $U(-0.05; 0.05)$ $0.0367$ $0.0323$ $0.0156$ $0.0033$ $0.05$ $a_{0:Sauce}$ - $V(1.00; 0.01)$ $0.9999$ $0.9999$ $0.0001$ $0.9996$ $1.0001$ $a_{1:Sauce}$ $d^{-1}$ $U(-0.05; 0.05)$ $0.0071$ $0.0046$ $0.0276$ $-0.0412$ $0.0048$ $a_{2:Sauce}$ $d^{-1}$ $U(-0.05; 0.05)$ $0.0071$ $0.0066$ <		$d^{-1}$						
$a_{0.\text{Sauce}}$ - $\mathcal{N}(1.00;0.01)$ 0.9995         0.9995         0.0001         0.9993         0.9997 $a_{1.\text{Sauce}}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ 0.004         0.004         0.0023         -0.008         0.0006 $a_{2.\text{Sauce}}$ $d^{-2}$ $\mathcal{U}(-0.05;0.05)$ 0.0319         0.0264         0.0198         -0.0120         0.05 $a_{0.\text{Sauce}}$ - $\mathcal{N}(1.00;0.01)$ 0.9998         0.9998         0.0001         0.9996         1. $a_{1.\text{Sauce}}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ 0.0367         0.0323         0.0156         0.0033         0.05 $a_{0.\text{Sauce}}$ - $\mathcal{N}(1.00;0.01)$ 0.9999         0.9999         0.0001         0.9996         1.0001 $a_{1.\text{Sauce}}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ 0.0007         -0.0007         0.0029         -0.0063         0.0048 $a_{2.\text{Sauce}}$ $d^{-2}$ $\mathcal{U}(-0.05;0.05)$ 0.0071         0.0046         0.0276         -0.0412         0.0496 $a_{0.\text{Sauce}}$ - $\mathcal{N}(1.00;0.01)$ 0.9996         0.9996         0.0002         0.9991		$d^{-2}$	$\mathcal{U}(-0.05; 0.05)$	0.0314	0.0314	0.0023	0.0271	0.0357
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			$\mathcal{N}(1.00; 0.01)$					
$a_{2:\text{Sauce}}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0319$ $0.0264$ $0.0198$ $-0.0120$ $0.05$ $a_{0:\text{Sauce}}$ - $N(1.00;0.01)$ $0.9998$ $0.9998$ $0.0001$ $0.9996$ $1.$ $a_{1:\text{Sauce}}$ $d^{-1}$ $U(-0.05;0.05)$ $-0.0004$ $-0.0003$ $0.0021$ $-0.0041$ $0.0033$ $a_{2:\text{Sauce}}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0367$ $0.0323$ $0.0015$ $0.0033$ $0.005$ $a_{1:\text{Sauce}}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0007$ $-0.0007$ $0.0029$ $-0.0063$ $0.0048$ $a_{2:\text{Sauce}}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0071$ $0.0046$ $0.0276$ $-0.0412$ $0.0496$ $a_{0:\text{Sauce}}$ $ N(1.00;0.01)$ $0.9996$ $0.9996$ $0.0002$ $0.9991$ $1.$ $a_{1:\text{Sauce}}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0066$ $0.9996$ $0.0002$ $0.0079$ $0.0175$ $a_{2:\text{Sauce}}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0022$ </td <td></td> <td><math>d^{-1}</math></td> <td></td> <td>-0.004</td> <td>-0.004</td> <td>0.0023</td> <td></td> <td>0.0006</td>		$d^{-1}$		-0.004	-0.004	0.0023		0.0006
$a_{0:Sauce}$ - $\mathcal{N}(1.00;0.01)$ 0.9998         0.9998         0.0001         0.9996         1. $a_{1:Sauce}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ -0.0004         -0.0003         0.0021         -0.0041         0.0038 $a_{2:Sauce}$ $d^{-2}$ $\mathcal{U}(-0.05;0.05)$ 0.0367         0.0323         0.0156         0.0033         0.05 $a_{0:Sauce}$ - $\mathcal{N}(1.00;0.01)$ 0.9999         0.9999         0.0001         0.9996         1.0001 $a_{1:Sauce}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ 0.0007         -0.0007         0.0029         -0.0063         0.0048 $a_{2:Sauce}$ $d^{-2}$ $\mathcal{U}(-0.05;0.05)$ 0.0071         0.0046         0.0276         -0.0412         0.0498 $a_{0:Sauce}$ - $\mathcal{N}(1.00;0.01)$ 0.9996         0.0902         0.9991         1. $a_{1:Sauce}$ $d^{-1}$ $\mathcal{U}(-0.05;0.05)$ 0.0051         0.0050         0.0069         -0.0079         0.0175 $a_{2:Sauce}$ $d^{-2}$ $\mathcal{U}(-0.05;0.05)$ 0.0066         0.0046         0.0281         -0.0418         0.0496		$d^{-2}$	$\mathcal{U}(-0.05; 0.05)$	0.0319	0.0264	0.0198	-0.0120	0.05
$a_{1.Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ $-0.0004$ $-0.0003$ $0.0021$ $-0.0041$ $0.0038$ $a_{2.Sauce}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0367$ $0.0323$ $0.0156$ $0.0033$ $0.05$ $a_{0.Sauce}$ $ N(1.00;0.01)$ $0.9999$ $0.9999$ $0.0001$ $0.9996$ $1.0001$ $a_{1.Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0007$ $0.0007$ $0.0029$ $-0.0043$ $0.0448$ $a_{2.Sauce}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0071$ $0.0046$ $0.0226$ $0.0412$ $0.0496$ $a_{0.Sauce}$ $ N(1.00;0.01)$ $0.9996$ $0.9996$ $0.0002$ $0.9991$ $1.$ $a_{1.Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0051$ $0.0050$ $0.0069$ $-0.0079$ $0.0175$ $a_{2.Sauce}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0066$ $0.0046$ $0.0021$ $0.9994$ $0.9998$ $a_{1.Satre}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0022$ $0.002$	a <sub>0:Sauce</sub>		$\mathcal{N}(1.00; 0.01)$	0.9998	0.9998	0.0001	0.9996	1.
$a_{2:Sauce}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0367$ $0.0323$ $0.0156$ $0.0033$ $0.05$ $a_{0:Sauce}$ - $\mathcal{N}(1.00;0.01)$ $0.9999$ $0.9999$ $0.0001$ $0.9996$ $1.0001$ $a_{1:Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0071$ $0.0046$ $0.0276$ $-0.0412$ $0.0496$ $a_{0:Sauce}$ - $\mathcal{N}(1.00;0.01)$ $0.9996$ $0.9996$ $0.0002$ $0.9991$ $1.$ $a_{1:Sauce}$ $d^{-1}$ $U(-0.05;0.05)$ $0.0051$ $0.0050$ $0.0069$ $-0.0079$ $0.0175$ $a_{2:Sauce}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0066$ $0.0046$ $0.0069$ $-0.0079$ $0.0175$ $a_{2:Sauce}$ $d^{-2}$ $U(-0.05;0.05)$ $0.0066$ $0.0046$ $0.0021$ $0.0019$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$ $0.0049$		$d^{-1}$		-0.0004	-0.0003	0.0021	-0.0041	0.0038
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		$d^{-2}$	$\mathcal{U}(-0.05; 0.05)$	0.0367	0.0323	0.0156	0.0033	0.05
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			$\mathcal{N}(1.00; 0.01)$	0.9999	0.9999	0.0001	0.9996	1.0001
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			$\mathcal{U}(-0.05; 0.05)$	-0.0007		0.0029	-0.0063	0.0048
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$d^{-2}$	$\mathcal{U}(-0.05; 0.05)$	0.0071	0.0046	0.0276	-0.0412	0.0496
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			$\mathcal{N}(1.00; 0.01)$	0.9996	0.9996	0.0002	0.9991	1.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$d^{-1}$	$\mathcal{U}(-0.05; 0.05)$	0.0051	0.0050	0.0069	-0.0079	0.0175
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$d^{-2}$	$\mathcal{U}(-0.05; 0.05)$	0.0066	0.0046	0.0281	-0.0418	0.0496
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			$\mathcal{N}(1.00; 0.01)$	0.9996	0.9996	0.0001	0.9994	0.9998
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$d^{-1}$	$\mathcal{U}(-0.05; 0.05)$	0.0022	0.0022	0.0007	0.0010	0.0035
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$d^{-2}$	$\mathcal{U}(-0.05; 0.05)$	0.0074	0.0075	0.0076	-0.0064	0.0222
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		_	$\mathcal{N}(1.00; 0.01)$	1.	1.	0.0001	0.9998	1.0002
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$d^{-1}$	$\mathcal{U}(-0.05; 0.05)$	0.0043	0.0043	0.0010	0.0024	0.0062
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				0.0174	0.0171	0.0151	-0.0105	0.0447
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		_	$\mathcal{N}(1.00; 0.01)$	0.9993	0.9993	0.0001	0.9991	0.9995
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		$d^{-1}$		-0.0075			-0.0105	-0.0044
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$d^{-2}$						
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		_						
$R_{\rm p}$ $R_{\rm Jup}$ -     0.77     0.79     0.07     0.67     0.90 $a/R_{\star}$ -     -     17.54     17.54     0.15     17.25     17.83 $\cos i$ -     -     0.05     0.05     0.0     0.05     0.05 $T_{14}$ hr     -     1.97     1.97     0.05     1.88     2.07		$g cm^{-3}$	_					
$a/R_{\star}$ 17.54 17.54 0.15 17.25 17.83 $\cos i$ 0.05 0.05 0.0 0.05 0.05 $T_{14}$ hr - 1.97 1.97 0.05 1.88 2.07			_					
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-	-	_					
$T_{14}$ hr – 1.97 1.97 0.05 1.88 2.07		_	_					
		hr	_					
		hr	_	0.28	0.29			

Note— $T_{13}$  is ill-defined for a grazing transit.  $\mathcal{U}$  denotes a uniform distribution,  $\mathcal{N}$  a normal distribution, and  $\mathcal{T}$  a truncated normal bounded between zero and an upper limit much larger than the mean. (1) To convert TESS mid-transit time from BTJD to BJD<sub>TDB</sub>, add 2,457,000. (2) Uninformative quadratic limb-darkening prior from Kipping (2013), implemented by Foreman-Mackey et al. (2020). The precision achieved in the ground-based data did not appear to necessitate using bandpass-dependent limb-darkening coefficients. For comparison, the Claret (2017) parameters for the appropriate  $T_{\rm eff}$  and  $\log g$  in TESS-band would have been  $(u_1, u_2) = (0.3249, 0.235)$ .

Table 4. TOI 837 photometry.

Time [BJD <sub>TDB</sub> ]	Rel. Flux	Rel. Flux Err.	Instrument
2451234.12345	1.00	0.01	TESS

NOTE— Table 4 is published in its entirety in a machine-readable format. An example entry is shown for guidance regarding form and content

Table 5. TOI 837 radial velocities.

Time [BJD <sub>TDB</sub> ]	RV [m s <sup>-1</sup> ]	$\sigma_{\rm RV}~[{\rm ms}^{-1}]$	Instrument
8669.533150	-57.80	27.50	FEROS
8669.540450	-13.90	29.40	FEROS
8676.506930	6.70	37.80	FEROS
8677.519150	-70.30	44.60	FEROS
8884.787630	240.00	28.00	CHIRON
8891.891180	-76.00	37.00	CHIRON
8898.735330	-10.00	43.00	CHIRON
8903.725760	-25.00	38.00	CHIRON
8904.739930	80.10	24.50	FEROS
8905.793630	88.00	21.70	FEROS
8908.762520	45.30	28.30	FEROS
8909.702140	0.00	31.80	FEROS
8912.606750	41.30	24.10	FEROS
8913.740580	161.10	37.30	FEROS
8915.762170	10.00	33.00	CHIRON
8916.714540	-93.50	33.60	FEROS
8917.765720	-159.70	24.80	FEROS
8920.706100	99.00	32.00	CHIRON
8922.845800	-148.30	54.90	FEROS
8915.924027	37.51	725.91	Veloce
8921.284950	105.90	453.19	Veloce
8922.733572	-195.92	195.63	Veloce
8924.583708	-7.65	262.32	Veloce
8926.365810	14.28	442.64	Veloce
8927.318146	207.04	505.19	Veloce
8928.559780	-7.28	180.24	Veloce
8930.324059	-2.60	152.02	Veloce
8931.293091	-45.68	152.94	Veloce
8932.065206	-105.60	319.82	Veloce

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