

$= 1$  if  $m$  is even . Thus the set of rational numbers  $q$  for which  $(-1)^q = 1$  is dense in the rational numbers , as is the set of  $q$  for which  $(-1)^q = -1$  . This means that the function  $(-1)^q$  is not continuous at any rational number  $q$  where it is defined .  
 On the other hand , arbitrary complex powers of negative numbers  $b$  can be defined by choosing a complex logarithm of  $b$  .

= = Irrational exponents = = =

If  $a$  is a positive algebraic number , and  $b$  is a rational number , it has been shown above that  $ab$  is algebraic . This remains true even if one accepts any algebraic number for  $a$  , with the only difference that  $ab$  may take several values ( see below ) , all algebraic . Gelfond - Schneider theorem provides some information on the nature of  $ab$  when  $b$  is irrational ( that is not rational ) . It states :  
 If  $a$  is an algebraic number different from 0 and 1 , and  $b$  an irrational algebraic number , then all the values of  $ab$  are transcendental numbers ( that is , not algebraic ) .

= = Complex exponents with positive real bases = =

= = Imaginary exponents with base  $e$  = = =