

$= g ( \frac{r^2}{k} )$  , since  $\omega^2 =$

$k \omega^2$  . For example , let the path of the first particle be an ellipse

$\langle \text{formula} \rangle$

where A and B are constants ; then , the path of the second particle is given by

$\langle \text{formula} \rangle$

$=$  = Orbital precession  $=$  =

If k is close , but not equal , to one , the second orbit resembles the first , but revolves gradually about the center of force ; this is known as orbital precession ( Figure 3 ) . If k is greater than one , the orbit precesses in the same direction as the orbit ( Figure 3 ) ; if k is less than one , the orbit precesses in the opposite direction .

Although the orbit in Figure 3 may seem to rotate uniformly , i.e. , at a constant angular speed , this is true only for circular orbits . If the orbit rotates at an angular speed  $\omega$  , the angular speed of the second particle is faster or slower than that of the first particle by  $\omega$  ; in other words , the angular speeds would satisfy the equation  $\omega^2$

$= \omega_1 + \omega$  . However , Newton 's theorem of revolving orbits states that the angular speeds are related by multiplication :  $\omega^2 =$

$k \omega_1^2$  , where k is a constant . Combining these two equations shows that the angular speed of the precession equals  $\omega = ( k \omega_1^2 ) \omega_1$  . Hence ,  $\omega$  is constant only if  $\omega_1$  is constant . According to the conservation of angular momentum ,  $\omega_1$  changes with the radius r

$\langle \text{formula} \rangle$

where m and  $L_1$  are the first particle 's mass and angular momentum , respectively , both of which are constant . Hence ,  $\omega_1$  is constant only if the radius r is constant , i.e. , when the orbit is a circle . However , in that case , the orbit does not change as it precesses .

$=$  = Illustrative example : Cotes 's spirals  $=$  =