

$$= 3 \times 3 \times 3 \times 3 \times 3 =$$

243 . The base 3 appears 5 times in the repeated multiplication , because the exponent is 5 . Here , 3 is the base , 5 is the exponent , and 243 is the power or , more specifically , the fifth power of 3 , 3 raised to the fifth power , or 3 to the power of 5 .

The word " raised " is usually omitted , and very often " power " as well , so 3⁵ is typically pronounced " three to the fifth " or " three to the five " . The exponentiation bⁿ can be read as b raised to the n th power , or b raised to the power of n , or b raised by the exponent of n , or most briefly as b to the n .

Exponentiation may be generalized from integer exponents to more general types of numbers .

Integer exponents

The exponentiation operation with integer exponents requires only elementary algebra .

Positive integer exponents

Formally , powers with positive integer exponents may be defined by the initial condition

and the recurrence relation

From the associativity of multiplication , it follows that for any positive integers m and n ,

Zero exponent

Any nonzero number raised by the exponent 0 is 1 ; one interpretation of such a power is as an empty product . The case of 0⁰ is discussed below .

Negative exponents

The following identity holds for an arbitrary integer n and nonzero b :

Raising 0 by a negative exponent is left undefined .

The identity above may be derived through a definition aimed at extending the range of exponents to negative integers .

For non zero b and positive n , the recurrence relation from the previous subsection can be rewritten as

By defining this relation as valid for all integer n and nonzero b , it follows that

and more generally for any nonzero b and any nonnegative integer n ,

This is then readily shown to be true for every integer n .

Combinatorial interpretation

For nonnegative integers n and m , the power n^m is the number of functions from a set of m elements to a set of n elements (see cardinal exponentiation) . Such functions can be represented as m ^{tuples} from an n ^{element set} (or as m ^{letter words} from an n ^{letter alphabet}) .

Identities and properties

The following identities hold for all integer exponents , provided that the base is non zero :

<formula>