

$r(\theta) = r(\theta + 2\pi)$ the curve will be symmetrical about the horizontal ($0^\circ / 180^\circ$) ray, if $r(\theta) = r(\pi - \theta)$ it will be symmetric about the vertical ($90^\circ / 270^\circ$) ray, and if $r(\theta) = r(\theta + \pi)$ it will be rotationally symmetric by π clockwise and counterclockwise about the pole.

Because of the circular nature of the polar coordinate system, many curves can be described by a rather simple polar equation, whereas their Cartesian form is much more intricate. Among the best known of these curves are the polar rose, Archimedean spiral, lemniscate, limaçon, and cardioid.

For the circle, line, and polar rose below, it is understood that there are no restrictions on the domain and range of the curve.

=== Circle ===

The general equation for a circle with a center at (r_0, θ_0) and radius a is

$$r = r_0 \sec(\theta - \theta_0) \pm a$$

This can be simplified in various ways, to conform to more specific cases, such as the equation

$$r = r_0 \pm a$$

for a circle with a center at the pole and radius a .

When $r_0 = a$, or when the origin lies on the circle, the equation becomes

$$r = 2a \cos(\theta - \theta_0)$$

In the general case, the equation can be solved for r , giving

$$r = \frac{r_0 \pm a}{\cos(\theta - \theta_0)}$$

the solution with a minus sign in front of the square root gives the same curve.

=== Line ===

Radial lines (those running through the pole) are represented by the equation

$$\theta = \theta_0$$