

= 2 rounds to determine the winner , a tournament of 32 teams requires  $\log_2 32 = 5$  rounds , etc . In this case , for n players / teams where n is not a power of 2 ,  $\log_2 n$  is rounded up since it is necessary to have at least one round in which not all remaining competitors play . For example ,  $\log_2 6$  is approximately 2.585 , which rounds up to 3 , indicating that a tournament of 6 teams requires 3 rounds ( either two teams sit out the first round , or one team sits out the second round ) . The same number of rounds is also necessary to determine a clear winner in a Swiss round-robin system tournament .

=== Photography ===

In photography , exposure values are measured in terms of the binary logarithm of the amount of light reaching the film or sensor , in accordance with the Weber - Fechner law describing a logarithmic response of the human visual system to light . A single stop of exposure is one unit on a base-2 logarithmic scale . More precisely , the exposure value of a photograph is defined as

where N is the f-number measuring the aperture of the lens during the exposure , and t is the number of seconds of exposure .

Binary logarithms ( expressed as stops ) are also used in densitometry , to express the dynamic range of light sensitive materials or digital sensors .

== Calculation ==

=== Conversion from other bases ===

An easy way to calculate  $\log_2 n$  on calculators that do not have a  $\log_2$  function is to use the natural logarithm ( ln ) or the common logarithm ( log or  $\log_{10}$  ) functions , which are found on most scientific calculators . The specific change of logarithm base formulae for this are :

or approximately

=== Integer rounding ===

The binary logarithm can be made into a function from integers and to integers by rounding it up or down . These two forms of integer binary logarithm are related by this formula :

The definition can be extended by defining . Extended in this way , this function is related to the number of leading zeros of the 32-bit unsigned binary representation of x ,  $\text{nlz}(x)$  .

The integer binary logarithm can be interpreted as the zero-based index of the most significant 1 bit in the input . In this sense it is the complement of the find first set operation , which finds the index of the least significant 1 bit . Many hardware platforms include support for finding the number of leading zeros , or equivalent operations , which can be used to quickly find the binary logarithm . The `fls` and `flsl` functions in the Linux kernel and in some versions of the `libc` software library also compute the binary logarithm ( rounded up to an integer , plus one ) .

=== Iterative approximation ===

For a general positive real number , the binary logarithm may be computed in two parts . First , one computes the integer part , ( called the characteristic of the logarithm ) . This reduces the problem to one where the argument of the logarithm is in a restricted range , the interval [ 1 , 2 ) , simplifying the second step of computing the fractional part ( the mantissa of the logarithm ) . For

any  $x > 0$  , there exists a unique integer  $n$  such that  $2^n \leq x < 2^{n+1}$  , or equivalently  $1 \leq 2^{-n}x < 2$  . Now the integer part of the logarithm is simply  $n$  , and the fractional part is  $\log_2 ( 2^{-n}x )$  . In other words :

<formula>

For normalized floating point numbers , the integer part is given by the floating point exponent , and for integers it can be determined by performing a count leading zeros operation .

The fractional part of the result is  $\log_2 y$  , and can be computed iteratively , using only elementary multiplication and division . The algorithm for computing the fractional part can be described in pseudocode as follows :