A retirement planner and withdrawal optimization model

Introduction:

What is the problem we are concerned with here?

For most of us the amount we are able to build up for our retirement is less than what we would like. This creates challenges for us in our retired years. In order to make the most of what we are able to do with these funds we look to our financial advisors. The financial community has understood for a long time that the specific withdrawal patterns can make a significant impact on the amount available to us and how long our funds will last.

One of the first articles I read[[1]](#footnote-1) along these lines discussed 15 separate withdrawal strategies, chief among them is the Common Rule (CR) and its comparison with the winner, starting with withdrawals from a Tax Deferred account up to your level of deductions first (TDD) strategy variant. The common rule, simply stated, is to withdraw from after tax accounts first, then the tax deferred accounts and finally the tax free accounts. The idea is to allow as much growth as possible in accounts sheltering that growth. TDD on the other hand shuffles the order to start with some portion of the tax deferred accounts, followed by after tax accounts, next the tax free accounts and finally the rest from the tax deferred accounts. Here the idea is to withdraw the amount equal to the level of deductions from the tax deferred account effectively withdrawing taxable money tax free. Additionally this lowers the amount that will have to be withdrawn starting at age 70 ½ for the Required Minimum Distribution (RMD) required by the IRS, which may prevent some creeping into higher tax brackets caused by the RMD. The paper finds TDD outperforms CR by $400K more remaining and paying $225K less taxes when starting with $2M (IRA 70%, After Tax Account 20%, Roth 10%) and a $50K yearly withdrawal.

A primary tool for their work as discussed in their paper was a Linear Programming (LP) model that fully accounted for tax implications. However, they do not go into the details of the model. Thankfully, there is a substantial example[[2]](#footnote-2) from 1994 that can serve as a guide for those of us not completely comfortable with LP models.

The main focus in the above work is on where to withdraw funds for each period of retirement in order to get the most from what you have. Another line of thinking that is even more important is focused on how much to withdraw while ensuring your funds do not run out. The 4% rule[[3]](#footnote-3) seems to have been the first systematic approach to this line of thinking and is well worth the read. The basic idea is to withdraw 4% of your funds the first year of retirement. Each subsequent year, increase the 4% by the previous year’s inflation rate. In many cases (dare I say most) following this advice will leave a substantial amount for the estate. In a few cases (have some examples for this) however it may still fail to fund the retirement in its entirety.

Looking to improve the guidance for where to make withdrawals while also ensuring funds will last throughout retirement has pushed LP models forward to be use for retirement planning and year to year execution as with 3-PEAT.[[4]](#footnote-4) ---Now what to say ---

(Give refs and examples…) and a later ref

Current environment and the rules that govern it:

In order for such models to be useful they must take into account current tax laws and the special nature of retirement accounts, their laws and rules. All of these are regularly modified and updated each year so the models also need to be updated to continue to be accurate. Let’s look at each area of the models will have to address.

Ordinary Income Tax: Ordinary income tax includes taxes for earned income. The 2017 tax code defines 7 tax brackets progressing from a 10% marginal rate up to a 39.6% marginal rate. The actual bracket definitions vary depending on filing status: single, married filed jointly, married filing separately… The IRS defines deductions and exemptions allowed from the income to reach a taxable income amount. These deductions can be complicated so the IRS also defines a Standard Deduction and personal exemptions which is also dependent on filing status.

Capital Gains Tax: Capital gains tax is the return on capital investments that have been purchased and held for a year or more before selling to recoup the investment and any gain or loss. Such gains from items not held for a year or more are taxed as ordinary income. The 2017 tax code defines three capital gains tax brackets from a 0% marginal rate up to a 20% marginal rate. As with ordinary tax brackets, these vary depending on filing status. High earners also pay a Medicare Net Investment Income tax of 3.8% with threshold amounts that are not indexed to inflation.

Company Managed Retirement Plans: 401(k), 403(b), 457(b)…, Pensions, ???? (401K… fall into what I will call a Tax Deferred Retirement Account (TDRA))

Individual Retirement Accounts (IRA): IRAs are also TDRAs but not managed by an employer. It has a limit to the yearly contribution that is the minimum of the defined maximum contribution level and your actual ordinary income. The defined maximum contribution is shared between all IRA and Roth IRA accounts. For 2017 it is $5,500 with a $1,000 catchup adder if you are over 50 years old. The yearly contribution to an IRA account is tax deductible (i.e., pretax) in most cases but higher earners are subject to a graduated scale till no deduction is allowed. No contributions are allowed after age 70.

IRA withdrawals before age 59 ½ are both taxed and receive a 10% tax penalty for early withdrawal. Withdrawals made after 59 ½ are taxed as ordinary income with no additional penalty. Once the IRA account owner reaches age 70 ½ they are required to withdraw a Required Minimum Distribution (RMD). The RMD is the sum of all the owners IRA account balances divided by their life expectancy as defined by the IRS. If the RMD is not withdrawn the portion remaining will be taxed at 50% (excise tax). (Need to explain in more detail)

Roth IRA: A Roth IRA is not a TDRA. Contributions to a Roth IRA are made with after tax money. The advantage they provide is that the profits made in a Roth IRA are never taxed. As mentioned above a maximum yearly contribution is shared between all your IRA and Roth IRA accounts. However, the maximum that can be contributed to a Roth IRA starts to be restricted based on filing status to the point that no contributions can be made for the highest earners.

Roth IRA withdrawals of contributions (as opposed to profits/gains) have no restrictions. Withdrawals of profits/gains on the other hand, taken before age 59 ½ or before your oldest Roth IRA account has been in place for 5 years will result in the profits being taxed as ordinary income and if before age 59 ½ a 10% penalty tax. After age 59 ½ there will be no penalty and after your oldest Roth account is 5 years old there will be no taxes. Withdrawal from a Roth IRA are defined by the IRS to be in the following order:[[5]](#footnote-5) first contributions then conversions (oldest conversions first) finally profits. Because of this ordering of withdrawal funds it is often the case that withdrawals that are made before 59 ½ and / or before the oldest Roth account is 5 still do not require any tax or penalty to be paid.

TDRA to Roth Conversions: no yet.

Estate Taxes:

Model Assumptions:

* The standard deduction is assumed along with a personal exemption
* All withdrawals from the investment account are taxed based on gains only and are assumed long term capital gains
  + Fraction gains needs improvement
* The percent of Social Security income that is subject to tax varies by income, here we assume the maximum percentage of 85%
* Not including the Medicare Net Investment Income tax
* All IRA contributions are with pretax money, this ignores deduction limits at the high end
* Roth withdrawals never incur tax on profits but do incur a penalty before age 59 ½ on the full amount
* Roth account contributions up to the personal maximum but I think I am allowing a joint max to be deposited into a single account (TODO: do I need to change/fix this?)
* No Roth contribution restrictions based on income levels are modeled
* Roth 5 year restriction is assumed to be passed
* RMD table all use the same which assumes the spouses are within 10 years age of each other

(Currently all Roth documentation and modeling is suspect and need double checking)

Discuss each of the laws as Ragsdale does (about a paragraph or so each)

* Contribution (We ignore company retirement contributions…)
* Early withdrawal
  + IRA, 401K…
  + Roth (a good source with good links for the 2 five year rules is: https://www.kitces.com/blog/understanding-the-two-5-year-rules-for-roth-ira-contributions-and-conversions/ )
* Minimum distribution
* Tax method
* Estate tax

Now, what about the model and its mathematical representation?

A little background may be required at this point. Linear Programming (LP) is a mathematical technique for optimization. The name was chosen prior to the wide spread use and development of software and the programming involved to create it. Rather, when using LP we define an object function to be optimized, a set of real valued variables to be determined, and a set of constraint expressions that set requirements on the optimal solution. This gives us everything we need to set up and solve our matrix expression:

(0)

Where x is our vector of variables, each row of A is represents a constraint such that when this row is multiplied by x the corresponding element of b appears on the Right Hand Side (RHS) of the expression. Once the problem has been defined in this manor, expression (0) can be solved for the optimal value of the object function (variable vector) c, ct is the transpose of c. With that out of the way, let’s move on.

OK, so we are looking at a new object function as well as the original we got from Ragsdale. In the Ragsdale model the overall effect of the mode was to optimize for the largest Estate possible. To get it to work on optimizing the way funds are removed from the various accounts it needs a desired spending amount. Without this, the model will not remove any funds from any account that is not required, like the RMD (Require Minimum Distribution). If we are not inclined to maximize our final estate, but would rather maximize the funds we can spend each year we need to emphasize the yearly spending component for the object function. With such an object function we might want to specify a maximum spending level, above which we’d rather keep the funds in the estate. Let’s start with the new (experimental) object function (S1) and then we will rewrite the Ragsdale object function as a variant (R1):

(S1)

(R1)

The idea here is that we want to maximize the spendable (si) dollars across the retirement years. For Ragsdale we also want to maximize the remaining account balances. However, we don’t want to require that all the available account balances is use up in cases where we set a maximum spending amount. So, in both the cases we define the object function to include both the sum of the yearly spendable amount and the sum of the account balances at the end of the period times a discount rate for each account (DjA). For (S1) though we include a “balancer” to lower the significance of the final balances in the optimization such that spendable funds will be favored. The balancer is using a heuristic of dividing by the sum of the initial account balances. The account discount rate is applied to the final balances to suggest the value of the balance given how the account is taxed; TDRA at 0.85, ROTH at 1.0, and the after tax investment account at 0.9. Finally we want to put pressure on our tax brackets in such a way as to force, as much as possible, the ordinary taxable funds into the lowest brackets first. We do this by subtracting all the brackets for every year with the higher brackets having higher values (higher btk).

Accounts in nl are not homogenies, there is up to one account per person for the TDRA and RothIRA type accounts and one after tax account. The account types include:

1. Tax Deferred Retirement Accounts (TDRA) including 401(k), traditional IRA and similar plans (one per person),
2. Roth Retirement Accounts (RothIRA) including after tax contributions to 401(k) and similar as well as Roth IRAs (one per person) and
3. After Tax Retirement Savings/Investing Accounts (ATRSI) (shared).

Note: This model uses one account for each type of account for each person such that the balance and withdrawals for the model account represent the sum of the balances / withdrawals for any number of accounts of that type. One sticky point here is when, for example, a 401(k) contains both tax deferred and after tax contributions. In this case the balance must be split and added to the correct account types.

To summarize, the objective specified by expression (S1) attempts to maximize the spendable amounts (si) and to a lesser degree remaining balances (bij) while helping to reinforce the proper filling of the tax brackets. Similarly, (R1) does the same while emphasizing the remaining account balances more.

The spendable amount (si) is the sum of all withdrawals (wij) minus any penalty for early withdrawal (pij) plus Social Security (SSi) and other income (oi) minus special expenses (ei), income tax (xik subject to tk) and capital gains tax (yil subject to tcgl) as well as money deposited back into the investment account (Dij). The following constraint is used to assign the spendable amount to si.

(2)

In the above expression the tkxik where tk monotonically increases with each bracket should force the funds into the lowest brackets first. However, in practice it does not always do so which is the reason we added the btkxik to the (S1) and (R1) above; this gives it a little more of a nudge.

In general we want allowable spending to increase with inflation and to remain steady year to year so we have the following constraint:

(3)

Questions to address (a bit obsolete): Maximizing the after tax yearly income and the TDRA balances at the end may have issues, is this really what I want? Maybe maximize include while keeping estate a certain level? Or meeting an include amount while maximizing the estate? How to handle the estate taxes. I’ve dropped them in the above.

(4)

An additional constraint will be given to allow for a minimum level of income per year. To this end we define expression (4) to ensure that each year’s spendable amount (si) is at least as much as the desired income (di) for every year in the modeled retirement period. This is only applicable with (R1) as (S1) will maximize the spendable amount and should surpass di whenever possible. When not possible the optimization will fail.

(5)

Similarly, we add a constraint for limiting the yearly spendable amount (si) to be less the some desired maximum (dmi). This constraint is only applicable with (S1) as (R1) will maximize for the ending balance and would find smaller spendable amounts independent of this constraint.

A number of constraints are required to constrain the objective function in expression (R1) and (S1) to optimal values while ensuring that IRS rules are followed and taxes and penalties are properly accounted for.

(6)

(7)

(8)

(9)

Deposits (Dij) to the all IRA and Roth accounts must not exceed either other income (oi) or the sum of the IRS defined maximum contribution(s) (mcir) as in (6). In addition, in the ‘married joint’ case we need to ensure that each person’s accounts do not exceed their personal maximums as in (7). On the other hand we want deposits to at least match the user specified contribution level (ucij) (8). We also need to ensure that no deposits are made to an IRA account after the owner is age 70 or above.

MAYBE: Add specific variables for IRA to Roth per owner conversions and not allow it to be done with deposits (Dij).

Another constraint required to meet IRS rules for Required Minimum Distribution (RMD).

(10)

Of the three account types, only the TDRA has an IRS requirement for a minimum require distribution (RMD). This requirement applies to all such accounts but the sum of the MRD can be withdrawn from each account, any one of the accounts or some combination of TDRA accounts as long as the full amount of the MRD is withdrawn from TDRA accounts for each account owner. To ensure withdrawals are at least as much as the IRS minimum required, equation (10), requires withdrawals, starting at age 70 (n70j), exceed the balance in the TDRA (bij) divided by an IRS defined life expectancy value (aij). N70j is the year in which the account owner for account j turns 70 years old. IRS requirement is the year they turn 70 ½ years old. aij is a life expectancy from the IRS tables that includes information of the owners age and the age of the spouse / beneficiary of the j account.

(11)

(12)

Equation (11) constrains the variable representing the amount of income in tax bracket k (xik) to take on an amount related to the total taxable income (the TDRA withdrawals (wij) minus deposits (Dij) and other taxable income, oti) minus the deductions (standard deduction and exemptions, sdi). Expression (2) forces income into the lowest possible brackets through the applied tax and need to be maximized. That is, tk is monotonically increasing as k increases in expression (2), which forces the xik in the lowest brackets to fill first. Expression (12) ensures that the xik portion of the income does not exceed the bracket amount (mik). Mik and sdi are inflation adjusted.

(13)

(14)

In the same manor (13, 14) fill the capital gains tax brackets (yil) with the non-basis fraction (fi) of the investment account (ATRSI) withdrawal (winAT). However, the capital gains tax bracket fill must start where the ordinary income bracket fill stopped and continue up from there. In order to do this we subtract the amounts in the tax brackets (xik) that overlap with the capital gains bracket from the size of the capital gains bracket.

(15)

Equation (15) ensures that the balance for each account at the beginning of the year (bi+1,j) is equal to the balance of the account at the start of the previous year (bij), minus the previous year’s withdrawals (wij) (modeled as being withdrawn at the beginning of the year) plus the deposits in the previous year (also modeled as occurring at the beginning of the year) times the return on the investment for the year at the rate of return (rij). This is somewhat pessimistic because withdrawals are usually not taken out in one transaction and optimistic as neither are deposits made at the beginning of the year but this is a small effect for our purposes here.

(16)

Expression (13) sets the beginning account balances to qj.

(17)

Finally, expression (14) constrains the model variables to be greater than or equal zero.

Transforming our model into a python implementation:

OK for our current work we will use the python scipy library, specifically the function scipy.optimize.linprog(). This requires the model to conform to the following template:

Object function: Minimize ct x

With constraints: A x <= b, and x >= 0

(need to zero base the indices)

Given this we transform our model expressions to match scipy template form as follows:

OK, as above we will first look at the new objective function followed by the Ragsdale objective function.

(S1’)

(R1’)

(2’)

Pij == 0.1 for i <60,j<nl Otherwise pij ==0

(3a’)

(3b’)

(4’)

(5’)

(6’)

(7’)

(8’)

(9’)

Deposits to the IRA and roth accounts must not exceed any of these two: other income (oi), IRS define maximum contribution (mci). However they should a least match the user specified contribution level (ucij).

MAYBE: can add specific variables for IRA to Roth per owner conversions and not allow it to be done with deposits (Dij).

(10’)

(11’)

(12’)

(13a’)

(13b’)

(14’)

(15a’)

(15b’)

Bij supports an extra year

(16a’)

(16b’)

(17’)

To transform our model into the scipy equivalent we have only to use a few operations. To transform the object function, expression (R1’) or (S1’), we minimize the opposite of (R1) or (S1). The rest of the expressions are transformed by multiplying by minus one (-1) to change greater than or equal (≥) to less than or equal (≤), moving constants to the Right Hand Side (RHS) of the expression and doubling up equations to convert from equal (=) into two relations, one with greater than or equal (≤) and the other with less than or equal (≥) (properly transformed) to bring all constraints into standard form (i.e., A x ≤ b). In (11a’ and 11b’) we also multiplied out the c(bij – wij) to (cbij – cwij) to more closely match the matrix coding. Constraint (13a’ and 13b’) set the initial account balances to qj.

Model input specification:

The basis for the model input specification is the toml specification[[6]](#footnote-6) with its library. The basic format is sections of information ‘[‘ section name ‘]’ where section name can be a category followed by a ‘.’ and a dispriptive name. ‘#’ to the end of the line represents a comment. The global section has no section name header. The input information is represented by an assignment.

General model information (global section):

retirement\_type = 'joint' # defaults to joint, could be single, joint (married), ??? TODO

returns = 6 # defaults to 6.0, return rate of investments as a percent

inflation = 2.5 # defaults to 0, yearly inflation rate as a percent

#maximize = ‘PlusEstate’ # defaults to ‘Spending’, ‘PlusEstate’ maximizes the final estate.

# individual retiree info (one section per retiree, at least one will need an id)

[iam] or [iam.id] where id is some string that represents the retiree

age = 60 # retiree’s age

retire = 65 # age retiree will retire

through = 95 # age through which to plan

primary = true # if there are more than one retiree one should be designated as primary

# Social Security section must specify amount, FRA and an age range

[SocialSecurity] or [SocialSecurity.id] # if more than one retiree at least one needs an id (id should match retiree id)

amount = 31000 # $31,000 at Full Retirement Age (FRA); Assumes inflation, 85% taxed

FRA = 67

age = "68-"

# Income must specify amount (yearly), age range, whether to adjust for inflation, and if it is taxed

[income.mytaxfree] # income after retirement that does not involve retirement accounts

amount = 3000

age = "67-" # starts at age 67 and continue

inflation = false # Adjust for inflation

tax = false # count this as ordinary taxable income (true/false)

[income.rental\_1] # another income source

amount = 36000

age = "67-"

inflation = true

tax = true # count this as income tax

[income.rental\_2] # a third income source

amount = 2400

age = "67-"

inflation = true

tax = true # count this as income tax

# desire income section must define amount, age range, inflation adjustment and whether it is taxed

# desired income should be use in conjunction with ‘PlusEstate’

#[desired.income]

#amount = 45000 # per year

#age = "68-"

#inflation = true

#tax = true # count this as income tax

# max income section must define amount, age range, inflation adjusted

#[max.income]

#amount = 150000

#age = "68-"

#inflation = true

## sections for each account type, IRA and Roth types should have on per retiree as needed

## only one pre-tax account

## Each accounts must define the initial balance. Optionally, an investment return rate can be given

[IRA] or [IRA.id] # where id must match the retiree’s id who is the owner of the account

bal = 2000000

#rate = 7.25

maxcontrib = 00

# roth type accounts

[roth.spouse]

bal = 100000

maxcontrib = 000

# after tax savings/investment type accounts

[aftertax] # assumes joint ownership if multiple retirees

bal = 700000

basis = 400000 # for capital gains tax

Expression Key:

aij IRA life expectancy at age in year i for account j

Bcg Number of capital gains tax brackets

Bt Number of tax brackets

bij balance of account j in year i

di desired minimal before tax income

dmi desire maximal before tax income

Di deposits to investment account in year i (this may be expanded to other accounts pre retirement?)

DjA The discount rate for the jth account

ei Special expenses that have a limited duration. These will not be counted as part of si

fi the capital gains fraction of investments (i.e., fraction that does not include the basis)

Flcg floor of the capital gains bracket l

i index for number of retirement years

inf inflation rate

j index for the number of accounts

k index for the tax brackets

l index for capital gains tax brackets

mik size of the kth tax bracket in year i

mcgil size of the lth capital gains bracket in year i

n Number of retirement years

n70,j year number that retiree owning the jth account is age 70 (i.e., primary retiree age 70 plus partner retiree age difference)

nl Number of accounts (i.e., number TDRA + number Roth+ aftertax accounts)

nAT Aftertax account index (when there is an aftertax account, nAT will equal nl)

oi Other income in the ith year

oti Other taxable income in the ith year (oti is a subset of oi)

pi the penalty cost of accessing a retirement account prior to age 60 (59½), Age <60 10% else 0%

pvi Present Value in year i

qj balance for account j at the start of retirement

rij rate of return for account j in year i

rcg capital gains tax rate (temp until cg tax brackets are working)

sdi Standard deduction in year i

si Spendable amount in year i

SSi Social Security income in year i

SSt Social Security faction that is taxable

tlcg marginal capital gains tax rate in bracket l

tk marginal tax rate in tax bracket k

wij withdrawal from account j in year i (j=1 TDRA, j=2 Roth, j=3 Investment)

xik ordinary taxable income in year i and bracket k

yil capital gains income in year i and bracket l

Consolidated Todos:

1. Create a case to use Aeq x == beq as well as Aub x <= bub
2. Add to this document a note in the proper place that states that inflation adjusted values assume the years of adjustment equal the number of years from start of retirement.
   1. So income or expense that is to be adjusted should be based on values at the time of retirement (e.g., enter income amount of 100 per year during retirement, will use 100 the first year of retirement, 100\*(1+inflation) for the second year or 100\*(1+inflation)^#yearsRetired )
   2. SS is an exception in that it is adjusted twice, once for the IRS adjustment depending on the start age vs. FRA and then for inflation as above.
   3. NEED TO ENSURE SS WORKS correct if it has already started (i.e., we are already retired)
3. Add to this document a note that income and expense info timelines tie back to the primary age line. That is, if [income.apt] include ‘62-‘ then the model will match this with the primary retiree’s 62 year and forward.

To Add:

* Experiment: what happens if I use 2x si rather than 1x ?
* MUST FIX. Like to enable the user to plug in a value for the standard deduction + exemptions.
* Should I assume any interest yields??? Currently it’s just capital gains
* Other taxes (Medicare tax, ???)
* What about fsic (social security tax?)
* Another problem with this is it DOES NOT ALLOW FOR A CHANGE IN THE BASIS while optimization is happening. Why is this important? Because, I want to be able to have excess withdrawals placed in ATRSI (bi3) which would need a corresponding change to the basis bmi this would require it to be a variable (not a constant) but I don’t think this method allows for variable to be multiplied. NEED TO VERIFY

To Do:

* Break out the consistency checking code into a separate file
* Make all output headings consistent and useful (uniform across the different ones (Taxable done the same everywhere))
* Convert the indices to zero based to match the python code
* Add selectable MRD tables (single, joint married, ???)
* Add state taxes
* ~~Add for retirement pre age 60 (TDRA 10% penalties, …)~~
  + Add a check box to not use this is an exception applies (add an attribute in the accountable?)
* Can the tax brackets be changed somehow to significantly lower the number of variables?
  + Want smaller / faster model
* Add checks to eliminate constraints where not needed
* New Auld model:
  + Add pre-retirement, how much to add to tIRA, tRoth, tSavings, tInvestments (use wayne scott or james welch jr style pre retirement; ws include in LP jw I don’t think does)
    - Add an output row for the current state (balances…) followed by the retirement rows, such as:
      * Current time row (input values)
      * Start row input values modified to match expected values at retirement
      * Year to year rows
      * End row with final state of the values
  + Input to optimize:
    - Add fRoth to the tax summary page in case of a 10% early withdrawal penalty
    - add a maximum spend rate (to for excess withdrawals into Roth accounts
    - ~~I think I will need to add two TDRA and two ROTH accounts to correctly handle joint where both have these accounts (RMD differ, timelines differ, SS differs)~~
    - Think about: if want to enable the model to deposit money in any of the account types the it has to be present whether or not its in the input file. Given this we could attach it to the primary retiree
      * Might help answer the question on whether a spouse should continue to contribute to IRA or Roth after another spouse retires
        + To add to the IRA you need to have taxable income of equal amount (not sure of the restriction for Roth)
    - Add version function and information (tag a commit for specific spots)
    - What mix for Investment account? (100% stock, stock bond mix?)
      * Capital gains taxes vs. interest vs. income tax
      * Currently assuming 100% -- But this is not most people or standard advice
    - Other sources of income include
      * illiquid assets (house)
        + will require an investment account to deposit the funds
      * reverse morgage
      * yield (is this interest? From?)
    - Like to optimize start year of SS
    - Short term savings goals (car, ….)
      * ORP use a list of time x amount tuples
      * Fplan has an expense vector from input (implementing this! Has model stability problems)
    - Emergency fund (6months – 1year, family emergencies,…)
    - Run for time prior to retirement
    - Break out SS husband and wife in print out
* Ability to run in simulation mode against a defined return rate for each year (ie., a portion of the historical S&P 500 record).
  + Compare against other strategies:
    - 4% initial amount forever, or with inflation, or adjust to 4% each year[[7]](#footnote-7) [[8]](#footnote-8) [[9]](#footnote-9)
    - CR
    - TDD
    - Autopilot (<http://www.marketwatch.com/story/theres-a-better-way-to-plan-retirement-withdrawals-2015-01-13?page=2> )
    - RMD all the way
* Like to be able to consider two peoples accounts more fully. That is to be able to determine things like:
  + When older retires and is withdrawing from TDRA does it make sense for the younger to continue to add money to the TDRA, maybe even enough money for the limit of both.

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2. Ragsdale, Cliff T., Andrew F. Seila, and Philip L. Little. 1994. “An Optimization Model for Scheduling Withdrawals from Tax-Deferred Retirement Accounts.” Financial Services Review 3, 2: 93–108. Retrieved from [www.twenty-first.com/pdf/RagsdaleAn\_Opt\_Model.pdf](http://www.twenty-first.com/pdf/RagsdaleAn_Opt_Model.pdf) [↑](#footnote-ref-2)
3. Bengen, William P (October 1994) Determining withdrawal rates using historical Data. Journal of Financial Planning Pages 171-180, Retrieved from: <http://www.retailinvestor.org/pdf/Bengen1.pdf> [↑](#footnote-ref-3)
4. Welch, James S Jr. A 3-Step Procedure for computing sustainable retirement savings withdrawals. Journal of Financial Planning 30 (8): 45-55. Retrieved from: <https://www.onefpa.org/journal/Pages/AUG17-A-3-Step-Procedure-for-Computing-Sustainable-Retirement-Savings-Withdrawals.aspx> [↑](#footnote-ref-4)
5. IRS 2017 publication 590b. [↑](#footnote-ref-5)
6. The toml specification is archived at: <https://github.com/toml-lang/toml> [↑](#footnote-ref-6)
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