

2) (1) $1\forall x(Fx \rightarrow Gx \wedge Hx)$	S
(2) $2.\exists xFx$	S
(3) $3.Fa$	S
(1) $4.Fa \rightarrow Ga \wedge Ha$	$E\forall 1$
(1)(3) $5.Ga \wedge Ha$	Mpp3,4
(1)(3) $6.Ha$	$E\wedge 5$
(1)(3) $7.\exists xHx$	$I\exists 6$
(1)(2) $8.\exists xHx$	$E\exists 2,3,7$
3) (1) $1\forall x(Fx \vee Gx \rightarrow Hx)$	S
(2) $2.\exists x\sim Hx$	S
(3) $3.\sim Ha$	S
(1) $4.Fa \vee Ga \rightarrow Ha$	$E\forall 1$
(1)(3) $5.\sim(Fa \vee Ga)$	Mtt3,4
(1)(3) $6.\sim Fa \wedge \sim Ga$	L.Morgan5
(1)(3) $7.\sim Fa$	$E\wedge 6$
(1)(3) $8.\exists x\sim Fx$	$I\exists 7$
(1)(2) $9.\exists x\sim Fx$	$E\exists 2,3,8$
4) (1) $1\forall x(Fx \rightarrow \sim Gx)$	S
(2) $2.\exists x(Hx \wedge Gx)$	S
(3) $3.Ha \wedge Ga$	S
(1) $4.Fa \rightarrow \sim Ga$	$E\forall 1$
(3) $5.Ga$	$E\wedge 3$
(3) $6.Ha$	$E\wedge 3$
(1)(3) $7.\sim Fa$	Mtt4,5
(1)(3) $8.Ha \wedge \sim Fa$	$I\wedge 6,7$
(1)(3) $9.\exists x(Hx \wedge \sim Fx)$	$I\exists 8$
(1)(2) $10.\exists x(Hx \wedge \sim Fx)$	$E\exists 2,3,9$
5) (1) $1\exists x(Fx \wedge Gx)$	S
(2) $2.\forall x(Fx \rightarrow Hx)$	S
(3) $3.Fa \wedge Ga$	S
(2) $4.Fa \rightarrow Ha$	$E\forall 2$
(3) $5.Fa$	$E\wedge 3$
(3) $6.Ga$	$E\wedge 3$
(2)(3) $7.Ha$	Mpp4,5
(2)(3) $8.Ha \wedge Ga$	$I\wedge 6,7$
(2)(3) $9.\exists x(Hx \wedge Gx)$	$I\exists 8$
(1)(2) $10.\exists x(Hx \wedge Gx)$	$E\exists 1,3,9$