

## Assignment - 2

1

a) The screw axes  $S_i$  in  $\{0\}$  are

$$\begin{array}{l}
 \{0\} \quad \begin{array}{cc} \omega_i & V_i \\ (0, 0, 0) & (0, 0, 0) \end{array} \\
 \{1\} \quad \begin{array}{cc} (0, 0, 1) & (0, 0, 0) \end{array} \\
 \{2\} \quad \begin{array}{cc} (0, 0, 1) & (l_1, 0, 0) \end{array} \\
 \{3\} \quad \begin{array}{cc} (0, 0, 1) & (d_1 + l_2, 0, 0) \end{array} \\
 \{b\} \quad \begin{array}{cc} (0, 0, 0) & (0, 0, 1) \end{array}
 \end{array}
 \quad \left| \begin{array}{l} z, \text{ Axis} \\ M = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & l_1 + l_2 \\ 0 & 0 & 1 & d_1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \end{array} \right.$$

The screw axes in  $\{b\}$  are

$$\begin{array}{l}
 \{b\} \quad \begin{array}{cc} \omega_i & V_i \\ (0, 0, 0) & (0, 0, 1) \end{array} \\
 \{3\} \quad \begin{array}{cc} (0, 0, 1) & (0, 0, 0) \end{array} \\
 \{2\} \quad \begin{array}{cc} (0, 0, 1) & (-l_2, 0, 0) \end{array} \\
 \{1\} \quad \begin{array}{cc} (0, 0, 1) & (-d_1 - l_2, 0, 0) \end{array} \\
 \{0\} \quad \begin{array}{cc} (0, 0, 0) & (-l_1 - l_2, 0, 0) \end{array}
 \end{array}$$

b) The final answer obtained using matlab is

$$T = \begin{bmatrix} 1 & 0 & 0 & -1 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



②

(a) The screw axes for the RRP robot are

$$\begin{array}{ll} \{1\} & (0, 0, 1) \\ \{2\} & (1, 0, 0) \\ \{3\} & (0, 0, 1) \end{array}$$

By inspection  $M = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 3 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \text{--- (1)}$

The forward kinematics completed are,

when  $\theta = (90, 90, 1)$  the forward kinematics are

$$T(\theta) = e^{[S_2]\theta} e^{[S_1]\theta} e^{[S_3]\theta} M$$

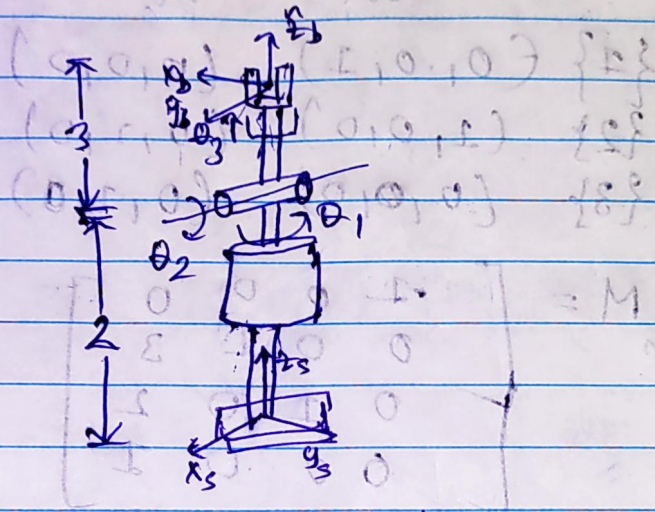
Evaluating this expression in matlab gives

$$T(\theta) = \begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 6 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



④

The Space Jacobian for this configuration is the screw axes when the robot is in the configuration



for  $J_s(\theta)$ :  $\omega_i \cdot v_i$

$$\begin{aligned} \{1\} & (0, 0, 1) \quad (0, 0, 0) \\ \{2\} & (0, 1, 0) \quad (-2, 0, 0) \\ \{3\} & (0, 0, 1) \quad (0, 0, 1) \end{aligned}$$

$$J_s(\theta) = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

⑤ The forward kinematics at  $\theta = (90, 90, 1)$  in the body frame are



$w_i$ 

$$V_i = \vec{q} \times \vec{w}$$

$$\{1\} \quad (0, 1, 0) \quad (3, 0, 0)$$

$$\{2\} \quad (-1, 0, 0) \quad (0, 3, 0)$$

$$\{3\} \quad (0, 0, 0) \quad (0, 0, 1)$$

The forward kinematics computed on matlab are  $\theta = (90, 90, 1)$

$$T(\theta) = M e^{TB_1 \theta_1} e^{TB_2 \theta_2} e^{TB_3 \theta_3}$$

$$T(\theta) = \begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \text{for } M \text{ in (2)}$$

The space Jacobian  $J_b$  is

$$J_b(\theta) \begin{matrix} w_i & v_i \\ \{1\} & (0, 0, 1) & (0, 0, 0) \\ \{2\} & (-1, 0, 0) & (0, 3, 0) \\ \{3\} & (0, 0, 0) & (0, 0, 1) \end{matrix}$$

$$\therefore J_b(\theta) = \begin{bmatrix} 0 & -1 & 0 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

⑧ Member of Project  
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```
% Assignment 2 - Question 1, Forward Kinematics
```

```
clear all;
```

```
%lengths
```

```
l0 = 1;
```

```
l1 = 1;
```

```
l2 = 1;
```

```
%M
```

```
M = [1, 0, 0, 0;  
      0, 1, 0, l1+l2;  
      0, 0, 1, l0;  
      0, 0, 0, 1];
```

```
%Screw Axes
```

```
S1 = [0,0,1,0,0,0];  
S2 = [0,0,1,l1,0,0];  
S3 = [0,0,1,l1+l2,0,0];  
S4 = [0,0,0,0,0,1];  
Slist = [S1', S2', S3', S4'];
```

```
%Body Axes
```

```
B1 = [0,0,1,-(l1+l2),0,0];  
B2 = [0,0,1,-l2,0,0];  
B3 = [0,0,1,0,0,0];  
B4 = [0,0,0,0,0,1];  
Blist = [B1', B2', B3', B4'];
```

```
%thetalist
```

```
thetalist = [0;pi/2;-pi/2;1];
```

```
%Configuration Space frame
```

```
Ts = FKinSpace(M,Slist,thetalist);
```

```
%Configuration Body Frame
```

```
Tb = FKinBody(M,Blist,thetalist);
```

```
% OUTPUT
```

```
% Ts =
```

```
%  
%      1      0      0     -1  
%      0      1      0      1  
%      0      0      1      2  
%      0      0      0      1  
%  
%
```

```
% Tb =
```

```
%  
%      1      0      0     -1  
%      0      1      0      1  
%      0      0      1      2  
%      0      0      0      1  
%
```

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```
% Assignment 2 - Question 2, Forward Kinematics
```

```
clear all;
```

```
%M
```

```
M = [-1, 0, 0, 0;  
      0, 0, 1, 3;  
      0, 1, 0, 2;  
      0, 0, 0, 1];
```

```
%Screw Axes w,v
```

```
S1 = [0,0,1, 0,0,0];  
S2 = [1,0,0, 0,2,0];  
S3 = [0,0,0, 0,1,0];
```

```
Slist = [S1',S2',S3'];
```

```
%Body Axes
```

```
B1 = [0,1,0,3,0,0];  
B2 = [-1,0,0,0,3,0];  
B3 = [0,0,0,0,0,1];
```

```
Blist = [B1',B2',B3'];
```

```
%thetalist
```

```
thetalist = [pi/2;pi/2;1];
```

```
%Configuration Space frame
```

```
Ts = FKinSpace(M,Slist,thetalist);
```

```
%Configuration Body Frame
```

```
Tb = FKinBody(M,Blist,thetalist);
```

```
% OUTPUT:
```

```
%
```

```
%
```

```
% Tb =
```

```
%
```

```
%   -0.0000    1.0000   -0.0000   -0.0000  
%   -1.0000   -0.0000    0.0000    0.0000  
%         0    0.0000    1.0000    6.0000  
%         0         0         0     1.0000
```

```
%
```

```
%
```

```
% Ts =
```

```
%
```

```
%   -0.0000    1.0000   -0.0000   -0.0000  
%   -1.0000   -0.0000    0.0000    0.0000  
%         0    0.0000    1.0000    6.0000  
%         0         0         0     1.0000
```

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