

Assignment - 2

1

(a) The screw axes S_i in $\{0\}$ are

$$\begin{array}{l}
 \{0\} \quad \begin{array}{cc} \omega_i & V_i \\ (0, 0, 0) & (0, 0, 0) \end{array} \\
 \{1\} \quad \begin{array}{cc} (0, 0, 1) & (0, 0, 0) \end{array} \\
 \{2\} \quad \begin{array}{cc} (0, 0, 1) & (l_1, 0, 0) \end{array} \\
 \{3\} \quad \begin{array}{cc} (0, 0, 1) & (d_1 + l_2, 0, 0) \end{array} \\
 \{b\} \quad \begin{array}{cc} (0, 0, 0) & (0, 0, 1) \end{array}
 \end{array}
 \quad \left| \begin{array}{l} z, \text{ Axis} \\ M = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & l_1 + l_2 \\ 0 & 0 & 1 & d_1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \end{array} \right.$$

The screw axes in $\{b\}$ are

$$\begin{array}{l}
 \{b\} \quad \begin{array}{cc} \omega_i & V_i \\ (0, 0, 0) & (0, 0, 1) \end{array} \\
 \{3\} \quad \begin{array}{cc} (0, 0, 1) & (0, 0, 0) \end{array} \\
 \{2\} \quad \begin{array}{cc} (0, 0, 1) & (-l_2, 0, 0) \end{array} \\
 \{1\} \quad \begin{array}{cc} (0, 0, 1) & (-d_1 - l_2, 0, 0) \end{array} \\
 \{0\} \quad \begin{array}{cc} (0, 0, 0) & (-l_1 - l_2, 0, 0) \end{array}
 \end{array}$$

(b) The final answer obtained using matlab is

$$T = \begin{bmatrix} 1 & 0 & 0 & -1 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

②

(a) The screw axes for the RRP robot are

$$\begin{array}{ll} \{1\} & (0, 0, 1) \\ \{2\} & (1, 0, 0) \\ \{3\} & (0, 0, 1) \end{array}$$

By inspection $M = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 3 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \text{--- (1)}$

The forward kinematics completed are,

when $\theta = (90, 90, 1)$ the forward kinematics are

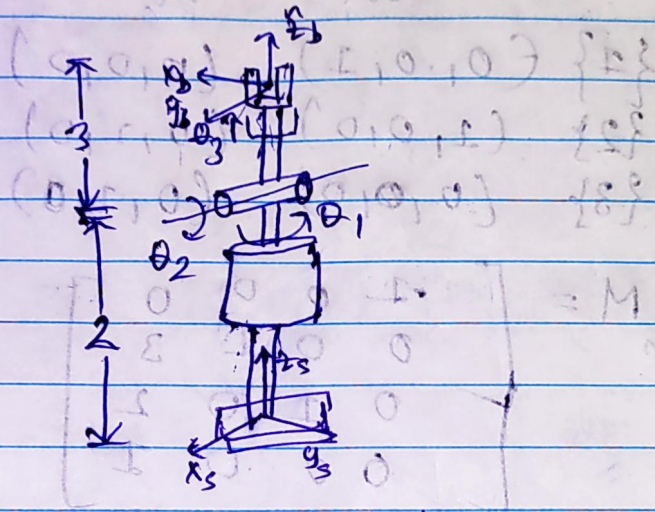
$$T(\theta) = e^{[S_2]\theta} e^{[S_1]\theta} e^{[S_3]\theta} M$$

Evaluating this expression in matlab gives

$$T(\theta) = \begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 6 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

④

The Space Jacobian for this configuration is the screw axes when the robot is in the configuration



for $J_s(\theta)$: $\omega_i \cdot v_i$

$$\begin{aligned} \{1\} & (0, 0, 1) \quad (0, 0, 0) \\ \{2\} & (0, 1, 0) \quad (-2, 0, 0) \\ \{3\} & (0, 0, 0) \quad (0, 0, 1) \end{aligned}$$

$$J_s(\theta) = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

⑤ The forward kinematics at $\theta = (90, 90, 1)$ in the body frame are

ω_i

$$V_i = \vec{q} \times \vec{\omega}$$

$$\{1\} \quad (0, 1, 0) \quad (3, 0, 0)$$

$$\{2\} \quad (-1, 0, 0) \quad (0, 3, 0)$$

$$\{3\} \quad (0, 0, 0) \quad (0, 0, 1)$$

The forward kinematics computed on matlab are $\theta = (90, 90, 1)$

$$T(\theta) = M e^{TB_1 \theta_1} e^{TB_2 \theta_2} e^{TB_3 \theta_3}$$

$$T(\theta) = \begin{bmatrix} 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \text{for } M \text{ in (2)}$$

The space Jacobian J_b is

$$J_b(\theta) \begin{matrix} \omega_i & V_i \\ \{1\} & (0, 0, 1) & (0, 0, 0) \\ \{2\} & (-1, 0, 0) & (0, 3, 0) \\ \{3\} & (0, 0, 0) & (0, 0, 1) \end{matrix}$$

$$\therefore J_b(\theta) = \begin{bmatrix} 0 & -1 & 0 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

⑧ Member of Project
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