

Homework 3: Agent Coordination and Reward Shaping

Due Oct 25, 2022 at 11:59 PM

Arthur's El Farol bar problem [2] is a perfect example of a congestion game. In this problem each agent i decides whether to attend a bar by predicting, based on its previous experience, whether the bar will be too crowded to be "rewarding" at that time, as quantified by a system reward G . The congestion game structure means that if most agents think the attendance will be low (and therefore choose to attend), the attendance will actually be high, and vice-versa.

For this assignment, we use a modified version of the bar problem where the N agents pick one out of K nights to attend the bar every week [1]. The system reward in any particular week is:

$$G(z) \equiv \sum_{k=1}^K x_k(z) e^{\frac{-x_k(z)}{b}}, \quad (1)$$

where $x_k(z)$ is the total attendance on night k , and b is a real-valued parameter representing the optimal number of people in the bar. The system dynamics are as follows:

Initialize: week $\leftarrow 0$

For week $<$ Time Limit

- Each agent chooses an action.
- Those actions lead to a system state.
- The system state leads to a system reward.
- Each agent receives a reward (i.e., agent reward) .
- week \leftarrow week + 1

Learning Agents: Each agent i keeps a K -dimensional vector of its estimates of the reward it would receive for taking each of those K actions (action-value learning). Each week, each agent i picks the night to attend based on sampling this vector.

Problem 1: Derive a simple local reward for this problem where each agent is rewarded based only on the night they chose. Discuss the alignment and sensitivity of this reward.

Problem 2: Derive a difference reward for each agent. What is a good counterfactual "action" c_i for this case? For at least two values of c_i , discuss the locality of the information and the alignment and sensitivity of the resulting difference rewards.

Problem 3: Perform a simulation for this problem with the following parameters:

- a) There are 20 agents in the system, $b=5$, and $k=7$.
- b) There are 50 agents in the system, $b=4$, and $k=6$.

Plot the performance of three agent rewards (G , difference, and local) and a histogram of sample attendance profiles. How do the rewards in Problems 1 and 2 perform in the two cases? Discuss the simulation results. The report should be in research paper format, and clearly describe your algorithms, results and analysis. You must use IEEE, AAMAS, or other similar conference citation styles. Please submit your report as a PDF, and submit your code in a separate zip file.

References

- [1] A. K. Agogino and K. Tumer, Analyzing and visualizing multiagent rewards in dynamic and stochastic environments, *Journal of Autonomous Agents and Multi Agent Systems*, 17:320–338, 2008.
- [2] W. B. Arthur. Complexity in economic theory: Inductive reasoning and bounded rationality. *The American Economic Review*, 84(2):406–411, May 1994.