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Large Scale Parallel Simulation of EPR Lineshape Spectra

Abstract: This experiment's aim is to measure the Zeeman effect's influence on the spectrum of a mercury light source exposed to magnetic field. Mercury's green 546nm and yellow 577nm spectral lines split into nine different components each, attributable to the *anomalous Zeeman effect*. Applying a quantum-mechanical theory originally designed for hydrogen-like atoms, we predict the spectral wavelength shifts of the much heavier element mercury and show experimentally the validity of our predictions within a certain tolerance level.

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1 Basics

What happens during EPR from a quite general point of view? We excite a certain system with an electromagnetic signal and measure the system's response. In other words, the system Φ uses the time-resolved input x(t) to generate output y(t):

$$y(x) = \Phi\{x(t)\}\tag{1}$$

If we assume the system to be linear

$$\Phi\{\alpha x_1(t) + \beta x_2(t)\} = \alpha y_1(t) + \beta y_2(t)$$
 (2)

and time-invariant

$$\Phi\{x(t-t_0)\} = y(t-t_0) \tag{3}$$

we can expand the input function in a series of some orthonormal basis set $g_k(t)$, or in some integral transform in the continuous limit with basis $g(\tau, t)$ and define the system completely by its set of responses to the basis functions:

$$x(t) = \sum_{k} \chi_k g_k(t) = \int_{-\infty}^{\infty} \chi(\tau) g(\tau, t) d\tau$$
 (4)

$$\Rightarrow \Phi x(t) = \sum_{k} \chi_k \Phi\{g_k(t)\} = \int_{-\infty}^{\infty} \chi(\tau) \Phi\{g(\tau, t)\} d\tau$$
 (5)

Using the definition of the Dirac delta function and applying our LTI (linear time-invariant) system

$$x(t) = \int_{-\infty}^{\infty} x(\tau)\delta(\tau - t)d\tau \tag{6}$$

$$\Rightarrow \Phi\{x(t)\} = \int_{-\infty}^{\infty} x(\tau) \Phi\{\delta(\tau - t)\} d\tau = \int_{-\infty}^{\infty} x(\tau) h(\tau - t) d\tau = x(t) * h(t)$$
 (7)

we find the system's output to be the convolution of the input wit its pulse response or free induction decay (FID) $h(t) = \Phi\{\delta(t)\}$. Furthermore, harmonics are eigenfunctions of LTI systems, and the frequency response or spectrum $H_{(\omega)}$ is just the Fourier transform of the system's FID:

$$\Phi\{e^{i\omega t}\} = \int_{-\infty}^{\infty} e^{i\omega t} h(\tau - t) d\tau = e^{i\omega t} \int_{-\infty}^{\infty} e^{i\omega(\tau - t)} h(\tau - t) d\tau = e^{i\omega t} \int_{-\infty}^{\infty} e^{i\omega(\tau)} h(\tau) d\tau = H(\omega) e^{i\omega t}$$
(8)

2 π -pulsed EPR

The mechanisms of EPR (Electron Paramegnetic Resonance), also called ESR (Electron Spin Resonance), work analogous to the mechanisms of NMR (Nuclear Magnetic Resonance). In diamagnetic materials, all electrons are spin-paired, making the magnetic dipole vanish, and enabling the system to be accessible by NMR. On the other hand, EPR experiments are suitable to investigate systems with unpaired electrons, which exhibit a non-zero electron spin. The basic idea is to perturb a spin system's equilibrium by a small pulsed oscillating magnetic field and record the emitted radiation during the relaxation process.

When we place a spin sytem inside a static magnetic field $\vec{B}_0 = B_0 \hat{z}$ and let it settle to equilibrium, due to Zeeman effect more electron spins are goint to align parallel to \vec{B}_0 than antiparallel, resulting in a net magnetization of the system. The pulse $\vec{B}_1 = B_1 \hat{x} e^{i(\vec{k} \cdot \vec{r} - \omega_1 t)} \cdot u(t_0 - t)$ linearly polarized in x-direction will tilt the electron spins and disturb the equilibrium in a way we are going to examine in the following:

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2.1 Spin Electron Hamiltonian

The Hamiltonian of an unpaired spin electron will exhibit several perturbation terms of different nature:

$$\mathcal{H} = \mathcal{H}_Z + \mathcal{H}_{HF} + \mathcal{H}_{CS} + \mathcal{H}_J + \mathcal{H}_D \tag{9}$$

- 1. Zeeman contribution \mathcal{H}_Z
- 2. Hyperfine interaction \mathcal{H}_{HF}

3 Spinach

The Matlab library Spinach supplies efficient methods for large-scale spin dynamics simulations. It consists of the kernel with the implementation of general spin dynamics simulation techniques and the user-land with a collection of different experiements to perform. Basically, the user prepares the description of a spin system, which is then translated by the kernel into the most efficient basis sets, superoperators, etc. The user-land decides how to deal with those objects, whether to apply a pre-established experiment, or whether to perform the kernel's simulation procedures manually. Though Spinach is able to simulate numerous kinds of experiments, in this work we are going to restrict ourselves to standard EPR experiments. For the π -pulsed EPR, the user-land readily provides the method pulse_acquire

References

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