

$$1. c(t) = 10 - 12.5 \cdot e^{-1.2t} \cdot \sin(1.6t + 53.1^\circ)$$

$$= 10 [1 - 1.25 e^{-1.2t} \cdot \sin(1.6t + 53.1^\circ)]$$

由于系统为二阶系统, 故  $\frac{1}{\sqrt{1-\xi^2}} = 1.25$ ,  $\xi \omega_n = 1.2$ ,

$$\omega_d = 1.6, \theta = 53.1^\circ$$

解得  $\xi = 0.6$ ,  $\omega_n = 2$

$$\sigma_p = e^{-\pi/\sqrt{1-\xi^2}} \times 100\% = 9.48\%$$

$$t_p = \frac{\pi}{\omega_d} = 1.96s$$

$$\text{设误差限 } \Delta = 0.05, t_s = \frac{3}{\omega_n \xi} = 2.5s$$

$$\text{设 } \Delta = 0.02, t_s = \frac{4}{\omega_n \xi} = 3.33s$$

(1).  
2. 系统传递函数  $M(s) = \frac{G(s)}{1 + K_f G(s)} = \frac{\frac{K_i K_a K_m}{R_f s(Js + f)}}{1 + \frac{K_i K_a K_m K_f}{R_f s(Js + f)}}$

$$= \frac{K_i K_a K_m}{R_f J s^2 + R_f f s + K_i K_a K_m K_f}$$

$$= \frac{6000}{s^2 + 10s + 6000}$$

系统为二阶系统,  $\omega_n^2 = 6000$ ,  $2\xi\omega_n = 10$ , 得  $\omega_n = 77.46$ ,  $\xi = 0.0645$

$$\theta = \arccos \xi = 86.3^\circ, \omega_d = \omega_n \sqrt{1-\xi^2} = 77.30$$

$$\theta(t) = 1 - \frac{1}{\sqrt{1-\xi^2}} e^{-\xi \omega_n t} \sin(\omega_d t + \theta) = 1 - 1.002 e^{-5t} \sin(77.3t + 86.3^\circ)$$

(2). 系统的特征方程为:  $s^2 + 10s + 6000 = 0$ , 劳斯表如下:

$$\begin{array}{cc|c} s^2 & 1 & 6000 \end{array}$$

$$\begin{array}{cc|c} s & 10 & \end{array}$$

$$\begin{array}{cc|c} s^0 & 6000 & \end{array}$$

系统稳定

$$\theta_d(t) = 0, n(t) = 1(t) \text{ 时}, N(s) = \frac{1}{s}$$

$$E(s) = -K_f \theta(s) = -K_f \frac{-\frac{R(s)}{N(s)} \cdot \frac{1}{s(Js+f)}}{1 + \frac{K_a K_m K_f}{R_f s(Js+f)}} N(s) = \frac{1}{s(0.1s^2 + s + 600)}$$

$$e_{ss} = \lim_{s \rightarrow 0} s E(s) = \frac{1}{600}$$

$$(3). n(t) = 0, \theta_d(t) = t, t > 0 \text{ 时}, R(s) = \frac{1}{s^2}$$

$$e_{ss} = \lim_{s \rightarrow 0} s \frac{R(s)}{1 + G(s)H(s)} = \lim_{s \rightarrow 0} \frac{0.1s + 1}{0.1s^2 + s + 600} = \frac{1}{600}$$