IRS-Enabled Covert and Reliable Communications: How Many Reflection Elements are Required?

Manlin Wang[†], Bin Xia[†], Yao Yao[†], Zhiyong Chen[†] and Jiangzhou Wang[‡]

†Department of Electronic Engineering, Shanghai Jiao Tong University, Shanghai, China

†School of Engineering, University of Kent, Canterbury, U.K.

Email: †{wangmanlin, bxia, sandyyao, zhiyongchen}@sjtu.edu.cn, *j.z.wang@kent.ac.uk

Abstract—Short-packet communications are applied to various scenarios where transmission covertness and reliability are crucial due to the open wireless medium and finite blocklength. Although intelligent reflection surface (IRS) has been widely utilized to enhance transmission covertness and reliability, the question of how many reflection elements at IRS are required remains unanswered, which is vital to system design and practical deployment. The inherent strong coupling exists between the transmission covertness and reliability by IRS, leading to the question of intractability. To address this issue, the detection error probability at the warder and its approximation are derived first to reveal the relation between covertness performance and the number of reflection elements. Besides, to evaluate the reliability performance of the system, the decoding error probability at the receiver is also derived. Subsequently, the asymptotic reliability performance in high covertness regimes is investigated, which provides theoretical predictions about the number of reflection elements at IRS required to achieve a decoding error probability close to 0 with given covertness requirements. Furthermore, Monte-Carlo simulations verify the accuracy of the derived results for detection (decoding) error probabilities and the validity of the theoretical predictions for reflection elements. Moreover, results show that more reflection elements are required to achieve high reliability with tighter covertness requirements, longer blocklength and higher transmission rates.

Index Terms—Covert and reliable transmission, short-packet communications, intelligent reflecting surface

I. Introduction

The fifth generation of mobile standards expands its focus into massive machine-type communication (mMTC) and ultra-reliable low-latency communication (uRLLC) [?]. In addition to transmission throughput, reliability and latency, transmission security is also essential in these scenarios since vast amounts of confidential information are transferred over an open wireless medium.

To ensurehighly ranssissions exactly, to vert communicational has been readised ensured ensurements and the remains a local readised ensurements and the remains a local readised ensurements. The information-theoretic limits of covert communications were established in [?] first. Subsequently, extra uncertainty sources have been utilized to further enhance covert capacity, such as the full-duplex receiver and the collaborative jammer. In addition, to tackle the resource-consuming issue, intelligent reflection surface (IRS) has emerged as a cutting-edge technology for covert communications [?].

Recently, massive efforts have been devoted to exploiting the performance gain by IRS in covert communications. By jointly optimizing the phase shifts at IRS and beamformers at the transmitter, favorable communication environments were established for covert communication in [?], [?]. Based on the above system, the transmission probability was also optimized in [?], and full-duplex technology was combined in [?]. Furthermore, IRS-assisted covert communications were extended to relaying networks [?], non-orthogonal multiple access systems [?] and unmanned aerial vehicle assisted systems [?].

Noteworthily, in many mMTC and uRLLC applications such as industrial automation and remote surgery, stringent latency and high transmission reliability are also mandatory requirements, where short-packet communication is required to minimize the transmission latency. However, the above existing works [?], [?], [?], [?], [?], [?], [?] focus on the system design based on Shannon information-theoretic framework with infinite blocklength assumptions, and they ignore the transmission reliability constraints. Thus, the analytical method and results obtained by these works are ineffective and cannot be directly applied to short-packet transmission where both covertness and reliability are required. However, it is imperative to reveal the benefit brought by IRS for short-packet communications to guarantee transmission covertness and reliability. More specifically, the question of how many reflection elements at IRS are required to achieve covert and reliable transmission is critical for practical system deployment and is still an open issue.

To address this issue, in this paper, an IRS-enabled short-packet communication system against a multiantenna warder is considered, and the number of required reflection elements is provided to guarantee transmission covertness and reliability. Specifically, to evaluate the system covertness and reliability performance, the average detection error probability at the warder and the average decoding error probability at the receiver are derived. Besides, to facilitate system analysis, concise approximation expression for detection error probability is also proposed in high covertness scenarios. Furthermore, we give a quantitative answer to the question that how many reflection elements are required to achieve a decoding error probability close to 0 with given covertness requirements

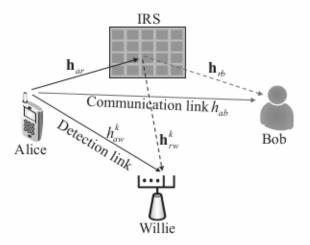


Fig. 1. IRS-enabled short-packet communication system against a multi-antenna warder.

even if the number of antennas at the warder is infinite. Finally, the analytical results are justified by the Monte-Carlo simulations, and the impacts of system parameters on the system performance are illustrated, which provides some insights for practical system design.

Notation: Vectors and matrices are denoted by boldface lowercase and uppercase letters, respectively. \mathbf{A}^T and \mathbf{A}^H denote the transpose and conjugate transpose of \mathbf{A} , respectively. $diag(\mathbf{p})$ denotes a diagonal matrix whose diagonal elements consist of the elements in the vector \mathbf{p} . $\|\cdot\|$ and $|\cdot|$ denote the Frobenius norm and the absolute value, respectively. $\mathcal{CN}(\mu, \mathbf{\Sigma})$ denotes the complex Gaussian distribution with mean μ and covariance $\mathbf{\Sigma}$. $\Pr(\cdot)$ denotes the probability of an event. $Q(x) = \int_x^\infty \frac{1}{\sqrt{2\pi}} \exp\left(-t^2/2\right) dt$ denotes the Q-function. $\Gamma(n) = (n-1)!$ denotes the Gamma function, $\gamma(n,x) = \int_0^x e^{-t}t^{n-1}dt$ denotes the lower incomplete Gamma function, and $\Gamma(n,x) = \int_x^\infty e^{-t}t^{n-1}dt$ denotes the upper incomplete Gamma function.

II. Signal and Channel Model

As shown in Fig. 1, a covert communication scenario is considered, where the transmitter (Alice) desires to deliver messages to the receiver (Bob) while keeping a multi-antenna wazdder(WWlill)c)nawawoofthe transmissionisAlice Alid Bohda Bobsameaksune deptippe depitipactingle within Willich ike a Willieds to showed tipped within Wedawtehn W., Antel R. S. swith M. Sruffection reflection is edephtyed deplayed this stransmission.

In one transmission round, Alice transmits n covert signals $x[i] \sim \mathcal{CN}(0, P_a)$, $i \in \{1, ..., n\}$ to Bob, where P_a denotes the transmit power at Alice. Willie collects n received signals to detect whether the transmission happens or not. We denote the additive white Gaussian noise (AWGN) at Bob and Willie as $n_b[i] \sim \mathcal{CN}(0, \sigma_b^2)$ and $\mathbf{n}_w[i] \sim \mathcal{CN}(\mathbf{0}, \sigma_w^2\mathbf{I})$, where σ_b^2 and σ_w^2 are the noise variances at Bob and Willie, respectively.

The wireless channels from Alice to Bob (h_{ab}) , from Alice to the k-th antenna of Willie $(h_{aw,k})$, from Alice

to IRS (\mathbf{h}_{ar}) , from IRS to Bob (\mathbf{h}_{rb}) , and from IRS to the k-th antenna of Willie $(\mathbf{h}_{rw,k})$ are subject to the quasi-static Rayleigh fading [?]. The channel coefficients remain constant during one transmission round, and are independently and identically distributed (i.i.d.) among different rounds. Specifically, $h_{ab} \sim CN(0, \lambda_{ab})$, $h_{aw,k} \sim$ $CN(0, \lambda_{aw})$, $\mathbf{h}_{ar} \sim CN(\mathbf{0}, \lambda_{ar}\mathbf{I})$, $\mathbf{h}_{rb} \sim CN(\mathbf{0}, \lambda_{rb}\mathbf{I})$, and $\mathbf{h}_{rw,k} \sim \mathcal{CN}(\mathbf{0}, \lambda_{rw}\mathbf{I})$. The instantaneous channel state information (CSI) of legitimate links (including the Alice-Bob link and Alice-IRS-Bob link) is assumed available at IRS by channel estimation [?]. In addition, since Willie does not cooperate with Alice, only statistical CSI of warder-related links (including the Alice-IRS-Willie link and Alice-Willie link) can be estimated at Alice through the local oscillator power inadvertently leaked from the receiver radio frequency frontend signal [?]. Besides, the instantaneous CSI of warder-related links is assumed available at Willie from the worst perspective for covert communication.

III. Covertness Performance Analysis

To detect the presence of covert communications, Willie must distinguish between the following two hypotheses

$$\mathbf{y}_{w}[i] = \begin{cases} \mathbf{n}_{w}[i], & \mathcal{H}_{0} \\ \mathbf{h}_{w}x[i] + \mathbf{n}_{w}[i], & \mathcal{H}_{1} \end{cases}$$
(1)

where \mathcal{H}_0 and \mathcal{H}_1 denote the null hypothesis that Alice does not transmit and the alternative hypothesis that Alice transmits, respectively. $\mathbf{y}_w[i]$ is the received signal at Willie, and $\mathbf{h}_w = [h_{w,1}, \dots, h_{w,N_w}]^T$ is the equivalent channel from Alice to Willie, where $h_{w,k} = h_{aw,k} + \mathbf{h}_{rw,k}^H \Theta \mathbf{h}_{ar}, k \in \{1, \dots, N_w\}$. $\Theta = diag\left(e^{j\theta_1}, \dots, e^{j\theta_{N_r}}\right)$ is the reflection matrix at IRS, where $\theta_i \in [0, 2\pi), i \in \{1, \dots, N_r\}$ denotes the phase of i-th reflection element.

Considering the worst perspective for covert communication, when Willie knows the instantaneous CSI and the reflection coefficients at IRS, the maximum ratio combiner can be adopted as an optimal detector [?]

$$T = \frac{1}{n} \sum_{i=1}^{n} |\mathbf{h}_{w}^{H} \mathbf{y}_{w}[i]|^{2} \underset{D_{0}}{\overset{D_{1}}{\geqslant}} \tau^{*}, \qquad (2)$$

where T is the average power of each received signal at Willie, D_1 and D_0 denote the binary decisions that infer whether Alice transmits or not, respectively. In addition, τ^* denotes the optimal detection threshold, which is given by [?], [?]

$$\tau^* = \frac{\sigma_w^2 \left(\sigma_w^2 + \|\mathbf{h}_w\|^2 P_a\right)}{P_a} \ln \left(1 + \frac{\|\mathbf{h}_w\|^2 P_a}{\sigma_w^2}\right). \quad (3)$$

Suppose there is no prior knowledge for Willie about when Alice will transmit. The prior probability of either hypothesis is equal. Mathematically, the detection error probability ξ at Willie is defined as $\xi = \Pr(D_1 \mid \mathcal{H}_0) +$ $\Pr(D_0 \mid \mathcal{H}_1)$, where $\Pr(D_1 \mid \mathcal{H}_0)$ denotes the false alarm probability, and $\Pr(D_0 \mid \mathcal{H}_1)$ denotes the missed detection probability [?]. Thus, the minimum detection error probability ξ^* , with optimal detection threshold τ^* . is expressed as [?]

$$\xi\left(\tau^{*}\right) = \Pr\left(T > \tau^{*}|H_{0}\right) + \Pr\left(T < \tau^{*}|H_{1}\right)$$

$$= 1 - \frac{1}{\Gamma(n)} \left(\gamma\left(n, \frac{n\tau^{*}}{\|\mathbf{h}_{w}\|^{2}\sigma_{w}^{2}}\right) - \gamma\left(n, \frac{n\tau^{*}}{\|\mathbf{h}_{w}\|^{2}\sigma_{w}^{2} + \|\mathbf{h}_{w}\|^{4}P_{a}}\right)\right). \tag{4}$$

Since Alice only knows the statistical CSI of warderrelated links, the average detection error probability with statistical CSI is adopted as the covertness performance of the system.

Theorem 1. The average detection error probability at Willie with optimal detection threshold can be derived as

$$\begin{split} & \overline{\xi}(\tau^*) = 1 - \frac{\pi}{B\Gamma(n)} \sum_{b=1}^{B} \left[\gamma \left(n, \frac{n \left(\sigma_w^2 + \tan \theta_b P_a \right)}{\tan \theta_b P_a} \ln \left(\frac{\sigma_w^2 + \tan \theta_b P_a}{\sigma_w^2} \right) \right) \right. \\ & \left. - \gamma \left(n, \frac{n\sigma_w^2}{\tan \theta_b P_a} \ln \left(\frac{\sigma_w^2 + \tan \theta_b P_a}{\sigma_w^2} \right) \right) \right] \frac{\sqrt{\theta_b \left(\frac{\pi}{2} - \theta_b \right)} f(\tan \theta_b)}{\cos^2 \theta_b}, \end{split}$$
(5)

where B is the parameter of Gaussian-Chebyshev Quadrature, $\theta_b = \frac{\pi}{4} \left(1 + \cos \frac{(2b-1)\pi}{2B} \right)$, and $f(x) = \frac{e^{-\frac{x}{\lambda_w}} x^{N_w-1}}{\lambda_w^{N_w} \Gamma(N_w)}$ with $\lambda_w = \lambda_{aw} + N_r \lambda_{rw} \lambda_{ar}$.

Proof. We denote $X_k = \mathbf{h}_{rw,k}^H \boldsymbol{\Theta} \mathbf{h}_{ar}$, which approximately follows the complex Gaussian distribution, i.e., $X_k \sim \mathcal{CN}\left(0, N_r \lambda_{rw} \lambda_{ar}\right)$, when N_r is sufficiently large [?]. The tightness of this approximation is validated by [?] and Section VI even N_r is relatively small. Thus, $\|\mathbf{h}_w\|^2$ follows the Gamma distribution with the probability density function (PDF) $f(x) = \frac{e^{-\frac{1}{\lambda_w}} x^{N_w-1}}{\lambda_w^{N_w} \Gamma(N_w)}$ [?]. By substituting (??) into (??), the average detection error probability can be expressed as

$$\begin{split} & \overline{\xi} \left(\tau^* \right) \! = \! 1 \! - \! \int \limits_0^\infty \! \left[\gamma \! \left(n, n \left(\frac{\sigma_w^2}{x P_a} \! + \! 1 \right) \ln \! \left(1 \! + \! \frac{x P_a}{\sigma_w^2} \right) \right) \right. \\ & \left. - \gamma \! \left(n, \frac{n \sigma_w^2}{x P_a} \ln \! \left(1 \! + \! \frac{x P_a}{\sigma_w^2} \right) \right) \right] \frac{f(x)}{\Gamma \left(n \right)} dx. \end{split} \tag{6}$$

By substituting $x = \tan \theta$ into (??) and applying Gaussian-Chebyshev Quadrature into the above integral expression [?], (??) can be obtained, and the proof is completed. \square

Due to the complicated form of (??), it is intractable to guide the system design. To address this issue, we derive a tractable approximation of the detection error probability as follows.

Lemma 1. In high covertness scenarios with moderate blocklength (such as $n \geq 50$), the average detection error probability at Willie can be approximated as

$$\bar{\xi}(\tau^*) \approx 1 - \sqrt{\frac{n}{2\pi}} \frac{N_w P_a \lambda_w}{\sigma_w^2}$$
. (7)

Proof. The detection error probability (??) is approximated as

$$\xi\left(\tau^*\right) \stackrel{(a)}{\approx} 1 - \frac{e^{-n}n^n}{\Gamma\left(n\right)} \frac{P_a \|\mathbf{h}_w\|^2}{\sigma_w^2} \stackrel{(b)}{\approx} 1 - \sqrt{\frac{n}{2\pi}} \frac{P_a \|\mathbf{h}_w\|^2}{\sigma_w^2}, (8)$$

where step (a) is obtained by the linear approximation in high covertness scenarios [?], and step (b) is due to $\lim_{n\to\infty} \frac{e^{-n}n^n}{\Gamma(n)} = \sqrt{\frac{n}{2\pi}}$ with relative error less than 2×10^{-3} when $n \ge 50$.

Thus, the average detection error probability is derived as

$$\bar{\xi}\left(\tau^{*}\right) \approx \int_{0}^{\frac{\sigma_{w}^{2}}{P_{a}}} \sqrt{\frac{2\pi}{n}} \left(1 - \sqrt{\frac{n}{2\pi}} \frac{P_{a}x}{\sigma_{w}^{2}}\right) f(x) dx = 1 - \sqrt{\frac{n}{2\pi}} \frac{N_{w}P_{a}\lambda_{w}}{\sigma_{w}^{2}} + g_{1}(P_{a}),$$
where $g_{1}\left(P_{a}\right) = \sqrt{\frac{n}{2\pi}} \frac{\lambda_{w}P_{a}}{\Gamma(N_{w})\sigma_{w}^{2}} \Gamma\left(N_{w} + 1, \frac{\sigma_{w}^{2}}{\lambda_{w}P_{a}} \sqrt{\frac{2\pi}{n}}\right) - \frac{1}{\Gamma(N_{w})} \Gamma\left(N_{w}, \frac{\sigma_{w}^{2}}{\lambda_{w}P_{a}} \sqrt{\frac{2\pi}{n}}\right),$ which can be ignored compared with other terms due to $\lim_{P_{a} \to 0} \frac{g_{1}(P_{a})}{P_{a}} = 0.$

The concise expression (??) implies that the $\bar{\xi}(\tau^*)$ is linear to \sqrt{n} , N_w and P_a in high covertness scenarios, facilitating the performance analysis in Section V. Besides, the tightness of (??) is also validated in Section VI.

IV. Reliability Performance Analysis

When Alice transmits, the received signal at Bob is

$$y_b[i] = (h_{ab} + \mathbf{h}_{rb}^H \Theta \mathbf{h}_{ar}) x[i] + n_b[i].$$
 (10)

Based on the received signal (??), Bob can decode the messages. However, the decoding error can not be ignored due to finite blocklength, which is given by [?]

$$\delta \left(\gamma_b\right) = Q \left(\frac{\ln 2\sqrt{n} \left(\log_2 \left(1 + \gamma_b\right) - R\right)}{\sqrt{1 - \left(\gamma_b + 1\right)^{-2}}} \right), \quad (11)$$

where $\gamma_b = |h_{ab} + \mathbf{h}_{rb}^H \boldsymbol{\Theta} \mathbf{h}_{ar}|^2 P_a / \sigma_b^2$ denotes the received SNR at Bob, and R is the transmission rate measured by bits per channel use (bpcu). Since the decoding error probability (??) is affected by fading channels, the average decoding error probability $\overline{\delta}$ is adopted to evaluate the reliability performance.

IRS can adjust its reflection coefficients at each transmission round to maximize γ_b, where the optimal phase is given by θ^{*}_i = arg (h_{ab}) + arg (h_{rb,i}) − arg (h_{ar,i}), h_{ar,i} and h_{rb,i} denote the channel from Alice to the *i*-th element at IRS, and from the *i*-th element to Bob, respectively. Thus, the instantaneous SNR can be expressed as γ_b = X²P_a/σ²_b where X = |h_{ab}| + ∑^{N_r}_{i=1} |h_{rb,i}| |h_{ar,i}|. According to [?, Lemma 1], X can be approximated by a generalized Gamma distribution with PDF f_X(x) = β^αx^{α-1}e^{-βx}/Γ(α), where α = Ψ²/Φ, β = Ψ/Φ, Ψ = α_d/β_d + N_rα_r/β_r, Φ = (7) α_d/β²_d + N_rα_r/β²_r, α_d = π/4−π, β_d = (2√π)/(N_{ab}), α_r = π²/(16−π²)

and $\beta_r = \frac{4\pi}{(16-\pi^2)\sqrt{\lambda_{ar}\lambda_{rb}}}$. Then, the PDF of γ_b is derived

$$f_{\gamma_b}(t) = \frac{\beta^{\alpha} e^{-\beta \sqrt{\frac{\sigma_b^2 t}{P_a}}}}{2\Gamma(\alpha) t} \left(\frac{\sigma_b^2 t}{P_a}\right)^{\frac{\alpha}{2}}, \quad (12)$$

and the average decoding error probability can be derived as

$$\begin{split} \bar{\delta} &= \int\limits_{0}^{\infty} \delta\left(t\right) f_{\gamma_{I}}(t) dt \stackrel{(a)}{\approx} \int\limits_{\varpi - \frac{1}{2\nu}}^{\varpi + \frac{1}{2\nu}} \nu F_{\gamma_{I}}(t) dt \\ &= \frac{\gamma \left(\alpha, \beta \sqrt{\frac{\sigma_{L}^{2}}{P_{a}} \left(\varpi - \frac{1}{2\nu}\right)}\right)}{\Gamma\left(\alpha\right)} + g(\varpi + \frac{1}{2\nu}) - g(\varpi - \frac{1}{2\nu}), \end{split} \tag{13}$$

where step (a) is due to linear approximation of Q-function [?], $\varpi = 2^R - 1$, $\nu = \sqrt{\frac{n}{2\pi(4^R - 1)}}$, $F_{\gamma_b}(t) = \frac{1}{\Gamma(\alpha)} \gamma \left(\alpha, \beta \sqrt{\frac{\sigma_b^2 t}{P_a}}\right)$ and $g(t) = \frac{\nu P_a}{\Gamma(\alpha)\beta^2 \sigma_b^2} \Gamma \left(\alpha + 2, \beta \sqrt{\frac{\sigma_b^2 t}{P_a}}\right) - \frac{(2\varpi\nu + 1)}{2\Gamma(\alpha)} \Gamma \left(\alpha, \beta \sqrt{\frac{\sigma_b^2 t}{P_a}}\right)$.

V. Theoretical Predictions about Required Reflection Elements

In this section, the reliability performance is derived under the covertness requirement $\overline{\xi}(\tau^*) \ge 1 - \varepsilon$, where ε is predetermined value to evaluate the covertness level. Besides, we provide the theoretical predictions about the number of reflection elements required to achieve a decoding error probability close to 0 with given covertness requirements.

On the one hand, $\bar{\xi}(\tau^*)$ decreases with N_r as shown in (??), which implies that the allowed transmit power P_a also decreases with N_r to meet the covertness requirement $\bar{\xi}(\tau^*) \geq 1 - \varepsilon$. On the other hand, $\bar{\delta}$ decreases with N_r and P_a as shown in (??). Therefore, the reliability guarantee by IRS is unclear but crucial, and the question that how many reflection elements are required to achieve a decoding error probability close to 0 with covertness requirements is significative.

To address this issue, we first derive the reliability performance in high covertness scenarios when $N_r \to \infty$ as follows.

Theorem 2. When $N_r \to \infty$, the achievable average decoding error probability with given ε in high covertness scenarios is

$$\lim_{N_r \to \infty} \overline{\delta} = \begin{cases} 1, & r_{rw} < r_1 \\ \frac{(2\varpi\nu + 1)}{2} - \sqrt{\frac{2\pi}{n}} \frac{\pi^2 \varepsilon \sigma_w^2 \lambda_{rb} \nu r_{rw}}{16\sigma_b^2 \lambda_{rw}}, & r_1 \leqslant r_{rw} < r_2 \\ 0, & r_2 \leqslant r_{rw} \end{cases}$$
(14)

where $r_{rw} = \lim_{N_r \to \infty} \frac{N_r}{N_w}$ denotes the ratio of the number of reflection elements at IRS to that of antennas at Willie, $r_1 = \sqrt{\frac{n}{2\pi}} \frac{16\lambda_{rw}\sigma_b^2}{\pi^2\lambda_{rb}\varepsilon\sigma_w^2} \left(\varpi - \frac{1}{2\nu}\right)$ and $r_2 = \sqrt{\frac{n}{2\pi}} \frac{16\lambda_{rw}\sigma_b^2}{\pi^2\lambda_{rb}\varepsilon\sigma_w^2} \left(\varpi + \frac{1}{2\nu}\right)$.

TABLE I Achievable Decoding Error Probability

Element Number	$N_w, N_r \rightarrow \infty$	$N_w, N_r \rightarrow \infty$	$N_w, N_r \rightarrow \infty$
	$r_{rw} < r_1$	$r_1 \leq r_{rw} < r_2$	$r_2 \leq r_{rw}$
$\bar{\delta}$	1	(??)	0
Element Number	$N_w \rightarrow \infty$	$N_r \rightarrow \infty$	$N_r, N_w,$
	N_r , finite	N_w , finite	finite
$\bar{\delta}$	1	0	(??)

Proof. See Appendix ??.

Theorem 2 gives the theoretical predictions about the number of reflection elements required to achieve high-reliability performance $(\bar{\delta} \to 0)$ with $N_w \to \infty$. Specifically, when $N_r \geq r_2 N_w$, the decoding error probability approaches 0. However, when $N_r < r_1 N_w$, the decoding error probability approaches 1. Besides, when $r_1 N_w \leq N_r < r_2 N_w$, the decoding error probabilities approach values between 0 and 1. Moreover, it shows that the covertness requirements ε , the blocklength n and the transmission rate R all affect the critical factors r_1 and r_2 . Specifically, the tighter the covert requirement, the longer the blocklength and the higher the transmission rate, the more reflection elements are required to guarantee high-reliability performance.

When the number of reflection elements at IRS (antennas at Willie) is finite, the decoding error probability can be obtained by substituting the maximum allowed transmit power $P_a = \sqrt{\frac{2\pi}{n}} \frac{\sigma_w^2 \varepsilon}{N_w \lambda_w}$ by (??) into (??). Finally, we summarize the achievable reliability of IRS-enabled short-packet communication systems under covertness requirements in Table I.

VI. Numerical Simulation

In this section, numerical results are provided to evaluate the performance of IRS-enabled short-packet communications. For illustration, we assume that Alice, Bob, Willie, and the IRS are located at (0,0), (10m,0), (12m,-5m), and (10m,1m) in a two-dimensional plane, respectively. The fadidg gapaneters are expressoresed $_{ij}$ as $\mathcal{B}_{0}\left(\frac{d_{i,j}}{d_{0}}\right)\beta_{0}\left(\frac{d_{i,j}}{d_{0}}\right) \stackrel{\alpha_{i,j}}{\in} \{ab, ar, r\{ab, ar, rb\}, aw\}$ rereduly. the odistance distance between between i marks ji $dnd=j \cdot 1 (tn)=isl$ (the ise februare feliation ordinated θ_0 and 30 (dB) -30 (dB) and the order of the februare -30 (dB) -30ploweregainwert bei refer theer distance. Astdore, iA tide coatis thus perponents expit heats with $\alpha_{i}\alpha_{ar} == 2\alpha_{sa}^{2}\alpha_{ab} + 2\alpha_{bab} =$ $\partial_{\alpha 5w} \alpha_{\overline{r}b} = 3.52 \alpha_s \text{Besides}, \text{By}^2 \text{sides} \alpha_w^2 \sigma_b^2 = 660_w^2 \text{ (dBm)} 60 R \text{ (dBm)}.$ Pope (f). 2u(dpx (i) 2001. All=t B00sinAullatthonsine sultation resented are sobtained do voltairagding vovavel againg anwel realizations el realizations 2 (a) and (b), the impacts of the transmit polyerFigs. the avarage ble teltion parts of obability sand average ode odding verage probability areoin vastlightidity Frond Figra 2e (le)codfingaerrobepsebabthiat atheincustigatwdtlFrom Figrical (si)nulations, behavioral the pression (\$2) and therical robations expression (123) coincide or (21) if the then hypprofere flection expression is ???) lattively demailers with the Mumil 6: Front Cigor (b) neit to ais belatevoly, banathes results

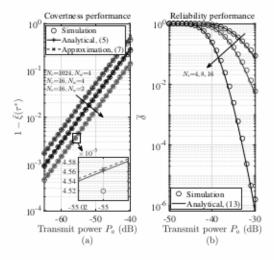


Fig. 2. The average detection error probability and decoding error probability versus the transmit power.

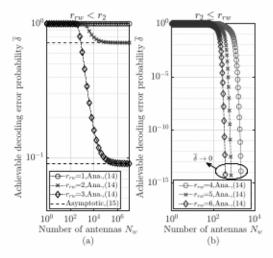


Fig. 3. The achievable decoding error probability versus the number of antennas at Willie.

∂btail@dPbyr(i? F)igr ② close ito chosbeobteintellabyt humesidal shtalatibhs, (even aife teles entrobers of obtfaictibh yelement ic is selant luctives nelle suith the Alumber Infadell citio in the electricis (dlatóvichg) nearbus polo babilit ies4 dbcradsictivit.ht hP, d et ed tiNu street dinge energy is bebelived bleeWillie (Bob) Pwhend IRS isinequipped ewithymione ceffect ibu Wilhien (BoThesheresIRtS isalidatepted veithltangive neffe Section difficultsplyings threathe publicated lappeoiding tions in 39c and IMP) implying adopted as opowerd nespeared mediabili (9?) eaform (3.6); ecametrics adopt 6d their ventrisen essdandial gilithesser formance metrics due to their Eigesisen(es) and (lg)tthesimpacts of the number of antenfrags.and(areflection) elebrentspontstor decoding berrof and baháki tyuad e influestiga telepuda te ohe thervies cyding "Anai" deplote ility assults sobitaited where? the It waves by ishen Athaë tlenote with bys(ill's) tehtdited byas(ill) ptiticannes bye(ill's) tehtdited byas(ill) ptiticannes bye(ill's) flig., play ulter day. Strectfinally framasiving 50(a), oitesalty be seen fliat $N_r \rightarrow \text{lowlfspecifically}$, from Fig. 6, (and if earl be 10 \overline{e}) thlatn $\delta r_1 \rightarrow <1$ rwhen $3r \leq r_2 = <3 d_1$. Bekidesanfroin—Fig.×51($|5|^2$,

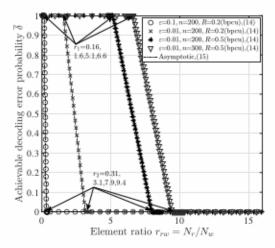


Fig. 4. The achievable decoding error probability versus the ratio r_{rw} .

ithean r be seen $\pm h3.t < \bar{\delta}r_2 \rightarrow 0.1.s$ Belsides, $\bar{\delta}$ from 1 Fig. 4. 5w(be), it_{ru}can 4b5, 6e≥nr₄hat3 d. These results averify the accuracy of The 6r 5n 6 3: which 3 give Eltere the outsice invelicions which af TelastreyuN3, velifiektigiveslehrenbecatetiRS predictigired lfat dededsing eNorreflebaloilitikentenapptokRS Ore required for delndFig.e4:otherdnabálitéeofosustemaglanameters on the debodbig, etrothopiohabilityofareyshevestigzaed; tewhere the dembler of carten pass ha Wittie and Offi viestage bedse cultifrat the nesults:byf (AR):renascadeWiltle theOfsytoptotic ones that The Besidesbit (22) bei seede twiththee casyntates irequiselyent?): Bardidyst etn: a_{1} arbenseters t_{1} t_{2} t_{3} t_{4} t_{5} t_{6} t_{1} t_{2} t_{3} t_{4} t_{5} t_{6} t_{6} tand is described by $r_{P}(R)$ although the filter of the t₁6a(31b)₂, when it call anges (from hanges of 0.01, 0.016) (Dally) to (16) (3hh)ngwhérom dh6n(8e3)fitom5.0.1(7.9)0.0the6iuRibhrlynges from th2n(bescfrom 0.5 (Bpc)u) o In. addition when rb) changes from (521 (6569)) to (656 (6964)), When dit ich anges from (2009) froi300.1These) results demonstrate that angre frefrect266 elera00ts Tares required the achieve deigh at eliability effection with etightere coveutness tre quitierne ritig lhighiab thitus (dission) vaites tageliteoregeventhoeksleregitli; ewhitets, phighidest iausightss for the practical system colesign, which provides insights for the practical system design VII. Conclusion

In this paper, we have provided the theoretical prediction absorpther required enprobled the flettion etchements lite giverant out other transition of well-ability reflection and entend RS gnabled eshorteptoket another link litigarer fronthis ceind, IRSe deaddid no bear to pay to be bility untic Willie. His these ender it be dead tiden bear to pay to be bility untic Willie. His these ender it be dead tiden evaluating the absorption of a calibrate where a consist of proximating the absorption of a calibrate for the analysis of proximation of the consistency of the proximation of the consistency of the calibrate of the consistency of

Evaluate Monace Grarby of analytical bresults cand phevioleidity of athetetheoretical cyroflicitidusic Simulation desigl teal haive shows the three steady paradictions ($\varepsilon Sim R$) as ignificantly affect showerthized systemb gracefune fields (on releft) enga, if which judges files the systemedlesignber of refelction elements, which guides the system design.

Appendix A ProfipreThiorem 2

In high covertness see national section $\mathbb{R}^2 \to \infty$, the allowed transhigh powert neiths given os overthrass -requirement lowers transmit power excith given covertness requirement ε is $\frac{P_{\psi,\pi^{\pm}}}{2\pi}$, $\frac{1}{N_r} \frac{N_r N_s \sqrt{3-\lambda_{ar}}}{N_r N_s \sqrt{3-\lambda_{ar}}}$. Besides, when $N_r \to \infty$, ε ε ε ε $\frac{1}{N_r} \frac{N_r N_s \sqrt{3-\lambda_{ar}}}{N_r N_s \sqrt{3-\lambda_{ar}}}$. By substituting the allowed $\frac{4V-\pi^2}{6}$ power-and $\frac{16-\pi^24\sqrt{\lambda_a-\lambda_{rb}}}{4\sqrt{\lambda_b}\sqrt{\kappa}}$ approximations into (allowed transhtaipower and above approximations into (??), we can obtain

where
$$f_{2}(t) = \frac{\gamma}{2(16\pi^{2})} \left(\frac{N_{r}\pi^{2}}{16\pi^{2}}, \frac{4\pi}{(16\pi^{2})^{2}}, \frac{N_{r}N_{r}N_{w}\lambda_{r}w}{\lambda_{r}N_{w}\lambda_{r}w} - \frac{(2\varpi\nu+1)}{(2\varpi\nu+1)}\right) - \frac{\gamma}{16\pi^{2}} \left(\frac{N_{r}\pi^{2}}{N_{r}N_{w}\lambda_{r}w}, \frac{N_{r}N_{w}\lambda_{r}w}{\lambda_{r}w} - \frac{(2\varpi\nu+1)}{2}\right) - \frac{\gamma}{2}$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi + \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi - \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi - \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi - \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi - \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi - \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right), \qquad (15)$$

$$\times \left(f_{3}\left(\varpi - \frac{1}{2\nu}\right) - f_{3}\left(\varpi - \frac{1}{2\nu}\right)\right$$

$$\lim_{\substack{x \to \text{initr} < 1 \\ x \to \infty, r < 1}} f_4(x, r) = \lim_{\substack{x \to \text{initr} < 1 \\ x \to \infty, r < 1}} \int_{4}^{x} \frac{t_{x-1}^{x-1} e^{-t}}{\frac{t_{x-1}^{x} e^{-t}}{\Gamma(x)}} dt$$

$$\lim_{\substack{x \to \text{initr} < 1 \\ x \to \infty, r < 1}} \frac{(rx)_x^x e^{-rx}}{\frac{t^x}{2\Gamma(x)}} \stackrel{\text{(b)}}{\leqslant} \lim_{\substack{x \to \text{initr} < 1 \\ x \to \infty, r < 1}} \sqrt{\frac{x}{x} e^{x(1-r)} r^x} \stackrel{\text{(c)}}{\approx} 0}{\text{(16)}}$$

$$\lim_{\substack{x \to \text{initr} < 1 \\ x \to \infty, r < 1}} \frac{(rx)_x^x e^{-rx}}{\frac{t^x}{2\Gamma(x)}} \stackrel{\text{(b)}}{\leqslant} \lim_{\substack{x \to \text{initr} < 1 \\ x \to \infty, r < 1}} \sqrt{\frac{x}{2} e^{x(1-r)} r^x} \stackrel{\text{(c)}}{\approx} 0}{\text{(16)}}$$

where step (a) holds due to the convexity of $g_2(t) \equiv$ $t_x^{x-1}e^{-t}$ on $(0, r_x)$ with $r < 1, x \to \infty$; and $f_{22}(t)dt \le t$ $\frac{rx(g_2(0)+g_2(rx))}{g_2(rx)}$: Step (b) holds due to the asymptotic Property of Gamma function as $\lim_{x\to \infty} F(x) \leq e^{-x} x^{x-\frac{3}{2}} \sqrt{2\pi}$ by [?, (1:43)]: Step (e) holds due to time, $\sqrt{x}e^{x(1-x)}r^{x} \equiv 0$:

For the case with $r \equiv 1$, we can obtain that

$$\lim_{x \to \infty; r \equiv 1} f_4(x, r) \equiv 1 = \lim_{x \to \infty} \frac{F(x, x)}{F(x)} \stackrel{(2)}{=} \frac{1}{2}; \quad (17)$$

where step (a) holds since $\lim_{x \to \infty} \Gamma(x, x) = \sqrt{\frac{\pi}{2}} x^{x - \frac{1}{2}} e^{-x}$ according to the resurgence property of the incomplete Gamma function by [?, (1.2)] and the asymptotic property of Gamma function by [?, (1.43)].

For the case with $r \ge 1$, we can obtain that

$$1 - \lim_{x \to \infty, r > 1} f_4(x, r) = \lim_{x \to \infty, r > 1} \int_{rx}^{\infty} \frac{t^{x-1}e^{-t}}{\Gamma(x)} dt$$

$$\stackrel{(a)}{<} \lim_{x \to \infty} \frac{(rx)^x e^{-rx}}{\Gamma(x)} \stackrel{(b)}{<} \lim_{x \to \infty} \frac{\sqrt{x}r^x e^{x(1-r)}}{\sqrt{2\pi}} \stackrel{(c)}{=} 0,$$
(18)

where the step (a) holds since $g_3(t) = t^{x-1}e^{-t} < g_4(t) =$ $(rx)^{x+1}e^{-rx}t^{-2}$ for $t\geqslant rx, r>1, x\to\infty$, and $\int_{-\infty}^{\infty}t^{-2}dt=$ $\frac{1}{rx}$. Besides, steps (b) and (c) holds for the same reason as elaborated in the case with r < 1.

To sum, $\lim_{r \to 0} f_4(x, r) = 0$ with r < 1, $\lim_{r \to 0} f_4(x, r) = \frac{1}{2}$ with r = 1, and $\lim_{x \to \infty} f_4(x, r) = 1$ with r > 1. Similarly, we can obtain $\lim_{r \to \infty} f_5(x, r) = 0$ with r > 1, $\lim_{r \to \infty} f_5(x, r) = \frac{1}{2}$ with r = 1, and $\lim_{x \to \infty} f_5(x, r) = 1$ with r < 1.

By substituting $x=\frac{N_r\pi^2}{16-\pi^2}$ and $r=\frac{4}{\pi}\sqrt{\frac{N_w\lambda_{rw}\sigma_b^2}{N_r\lambda_{rb}\varepsilon\sigma_w^2}}\sqrt{\frac{n}{2\pi}}\left(\varpi+\frac{1}{2\nu}\right)\left(\frac{4}{\pi}\sqrt{\frac{N_w\lambda_{rw}\sigma_b^2}{N_r\lambda_{rb}\varepsilon\sigma_w^2}}\sqrt{\frac{n}{2\pi}}\left(\varpi-\frac{1}{2\nu}\right)\right)$ into $f_4(x,r)$ and $f_5(x,r)$, results in Theorem ?? are obtained.