

# Maximizing Network Connectivity for UAV Communications via Reconfigurable Intelligent Surfaces

Mohammed S. Al-Abiad, Mohammad Javad-Kalbasi, and Shahrokh Valaee

Department of Electrical and Computer Engineering, University of Toronto, Toronto, Canada

Email: mohammed.saif@utoronto.ca, mohammad.javadkalbasi@mail.utoronto.ca, valaee@ece.utoronto.ca

**Abstract**—It is anticipated that integrating unmanned aerial vehicles (UAVs) with reconfigurable intelligent surfaces (RISs), resulting in RIS-assisted UAV networks, will offer improved network connectivity against node failures for the beyond 5G networks. In this context, we utilize a RIS to provide path diversity and alternative connectivity options for information flow from user equipment (UE) to UAVs by adding more links to the network, thereby maximizing its connectivity. This paper employs the algebraic connectivity metric, which is adjusted by the reflected links of the RIS, to formulate the problem of maximizing the network connectivity in two cases. First, we consider formulating the problem for one UE, which is solved optimally using a linear search. Then, we consider the problem of a more general case of multiple UEs, which has high computational complexity. To tackle this problem, we formulate the problem of maximizing the network connectivity as a semi-definite programming (SDP) optimization problem that can be solved efficiently by polynomial time. In both cases, our proposed solutions find the best combination between UE(s) and UAVs through the RIS. As a result, it tunes the phase shifts of the RIS to direct the signals of the UEs to the appropriate UAVs, thus maximizing the network connectivity. Simulation results are conducted to assess the performance of the proposed solutions compared to the existing solutions.

**Index Terms**—Network connectivity, algebraic connectivity, RIS-assisted UAV communications, graph theory.

## I. Introduction

UAVs are expected to have a remarkable impact on the economy by 2026 with a global market value of US\$59.2 billion, making the incorporation of UAVs critical in beyond 5G networks [?]. One of the unique features of UAV-assisted communication is improved network connectivity by establishing line-of-sight (LoS) connections with UEs [?]. Meanwhile, RIS is a promising technique that is integrated with UAVs to further improve network connectivity [?], in particular, let networks experience deep fade. In this context, RISs can be leveraged to provide path diversity and alternative connectivity solutions for information flow from UEs to UAVs in RIS-assisted UAV networks.

The prime concern of UAV communications is that UAV nodes are prone to failure due to several reasons, such as limited energy, hardware failure, or targeted failure

in the case of battlefield surveillance systems. Such UAV failures cause network disintegration, and consequently, information flow from UEs to a fusion center through UAVs can be severely impacted. Hence, it is crucial to always keep the network connected, which was addressed in the literature by adding more backhaul links to the network, e.g., [?]. In spite of recent advances in wireless sensor networks, most of the existing studies consider routing solutions with the focus more on extending the battery lifetime of sensor nodes. These works define network connectivity as network lifetime, in which the first node or all the nodes have failed [?], [?]. However, none of the aforementioned works has ever explicitly considered the exploitation of RISs to add more reflected links for improving network connectivity. Different from works [?], [?] that focused on routing solutions, this paper focuses on designing a more connected RIS-assisted UAV network that enables information flow from the UEs to the UAVs even if some of the UAVs have failed.

The algebraic connectivity [?], also called the Fiedler metric or the second smallest eigenvalue of the Laplacian matrix representing a graph, is a metric that measures how well a graph is connected. In the literature, such metric is usually associated with network connectivity [?], [?], [?]. In [?], the authors maximized the algebraic connectivity by positioning the UAV to maximize the connectivity of small-cells backhaul network. A more general study in [?] proposed different network maintenance algorithms to maximize the connectivity of wireless sensor networks. Since the algebraic connectivity is a good measure of how connected the graph is, the more edges that exist between the UEs and the UAVs, the more resilient network can be designed without being disconnected due to node failures [?], [?]. To this end, this paper aims to utilize the RIS to add link redundancy to the network and tune the RIS phase shift configurations to direct UEs' signals to appropriate UAVs, so that the connectivity of RIS-assisted UAV networks is maximized. To the best of our knowledge, the problem of maximizing the network connectivity in RIS-assisted UAV networks has not been studied before in the literature.

In this paper, we address this problem by employing the concept of algebraic connectivity [?] of a graph in network

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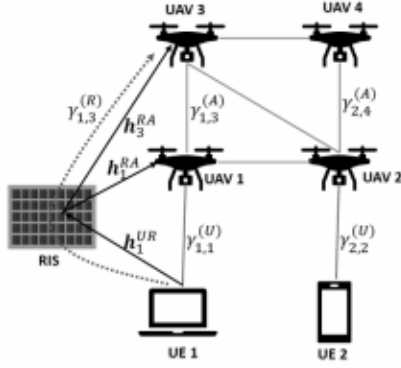


Fig. 1: A typical RIS-assisted UAV network with one RIS, 2 UEs, and 4 UAVs.

connectivity, then we consider two problems. First, we formulate the problem of UE and UAV RIS and solve it optimally via a line search. Then, we formulate the problem of generating a set of UEs and RIS links. This is the solving a hop graph problem, optimally solving it is computationally prohibitive since computing the connectivity of the network for each work for edge possibility that connects the UEs through UAVs and the RIS. To solve this problem, we adjust the connectivity of the original graph network by the candidate edges between UAVs and RIS. Then, we reformulate the problem of maximizing the network connectivity as a graph coloring (SDP) problem. This problem can be efficiently solved efficiently in polynomial time. In proposed section, we compare the performance of the proposed solutions with the existing solutions.

## II. System Model and Network Connectivity

### A. System Model

We consider a RIS-assisted UAV network with a set of UAVs, one RIS, and multiple UEs that represent ground users, sensors, etc. An example of the considered network is shown in Fig. 1. The sets of UAVs and UEs are denoted as  $\mathcal{A} = \{1, 2, \dots, A\}$  and  $\mathcal{U} = \{1, 2, \dots, U\}$ , respectively, where  $A$  is the cardinality of the set  $\mathcal{A}$ . All UEs and UAVs are equipped with single antennas. The  $A$  UAVs fly and hover over assigned locations at a fixed flying altitude and connect  $U$  UEs with the fusion center. The locations of the UAVs, UEs, and the RIS are assumed to be fixed. We assume that all channels follow a quasi-static flat-fading model and thus remain constant over one time slot. The RIS is installed with a certain altitude  $z_R$ . Let  $(x_R, y_R)$  be the 2D location of the RIS,  $(x_a, y_a, z_a)$  be the 3D location of the  $a$ -th UAV, and  $(x_u, y_u)$  be the 2D location of the  $u$ -th UE, respectively. The distances between the  $u$ -th UE

and the RIS and between the RIS and the  $a$ -th UAV are denoted by  $d_{u,R}^{UR}$  and  $d_{a,R}^{RA}$ , respectively.

Due to their altitude, UAVs can have good connectivity to UEs. However, UEs may occasionally experience deep fade. To overcome this problem and further improve network connectivity, we propose to utilize a RIS to impose link redundancy to the RIS-assisted UAV network. As such, the network becomes more resilient against node failures by providing path diversity and alternative connectivity options between UEs and UAVs. The RIS is equipped with a controller and  $M_r \times M_c$  passive reflecting units (PRUs) to form a uniform passive array (UPA). Each column of the UPA has  $M_r$  PRUs with an equal spacing of  $d_c$  meters (m) and each row of the UPA consists of  $M_c$  PRUs with an equal spacing of  $d_r$  m. These PRUs can add indirect links between UEs and UAVs with adjustable phase shifts. The phase-shift matrix of the RIS is modeled as the diagonal matrix  $\Theta = \text{diag}(e^{j\theta_1}, \dots, e^{j\theta_2}, \dots, e^{j\theta_M})$ , where  $\theta_m \in [0, 2\pi)$ , for  $m = \{1, \dots, M\}$  and  $M = M_r \times M_c$ .

The successful communications between the UEs and the RIS are measured using the distance threshold  $D_o$ , i.e., the  $u$ -th UE is connected to the RIS with distance  $d_{u,R}^{(R)}$  if  $d_{u,R}^{(R)} \leq D_o$ . The communications between the UEs and UAVs/RIS are assumed to occur over different time slots (i.e., time multiplexing access) to avoid interference among the scheduled UEs. Therefore, we assume that only one UE is transmitting in each time slot to reduce interference. Considering the interference among the different scheduled UEs to the RIS and the UAVs is left for future work.

Since this paper focuses on the network connectivity from data link-layer viewpoint, we abstract the physical layer factors and consider a model that relies only on the distance between the nodes. Therefore, we model only the large scale fading and ignore the small scale fading. To quantify the UEs transmission to the UAVs and the RIS, we use the signal-to-noise ratio (SNR). For the  $u$ -th UE, SNR is defined as follows [?]

$$\gamma_{u,a}^{(U)} = \frac{d_{u,a}^{-\alpha} p}{N_0}, \quad (1)$$

where  $d_{u,a}$  is the distance between the  $u$ -th UE and the  $a$ -th UAV,  $p$  is the transmit power of the  $u$ -th UE, which is maintained fixed for all the UEs,  $N_0$  is the additive white Gaussian noise (AWGN) variance, and  $\alpha$  is the path loss exponent that depends on the transmission environment.

UAVs hover at high altitudes, thus we reasonably assume that they maintain LoS channel between each other. The path loss between the  $a$ -th and the  $a'$ -th UAVs can be expressed as

$$\Gamma_{a,a'} = 20 \log \left( \frac{4\pi f_c d_{a,a'}}{c} \right), \quad (2)$$

where  $d_{a,a'}$  is the distance between the  $a$ -th UAV and the  $a'$ -th UAV,  $f_c$  is the carrier frequency, and  $c$  is light



speed. The SNR in dB between the  $a$ -th UAV and the  $a'$ -th UAV is  $\gamma_{a,a'}^{(A)} = 10 \log P - \Gamma_{a,a'} - 10 \log N_0$ , where  $P$  is the transmit power of the  $a$ -th UAV, which is maintained fixed for all the UAVs. Note that the SNR of the  $u$ -th UE determines whether it has a successful connection to the corresponding UAV  $a$ . In other words, the  $a$ -th UAV is assumed to be within the transmission range of the  $u$ -th UE if  $\gamma_{u,a}^{(U)} \geq \gamma_0^{\text{UE}}$ , where  $\gamma_0^{\text{UE}}$  is the minimum SNR threshold for the communication links between the UEs and the UAVs. Similarly, we assume that UAV  $a$  and UAV  $a'$  have a successful connection provided that  $\gamma_{a,a'}^{(A)} \geq \gamma_0^{\text{UAV}}$ , where  $\gamma_0^{\text{UAV}}$  is the minimum SNR threshold for the communication links between the UAVs.

Since the RIS is deployed in the higher altitude, the signal propagation of UE-to-RIS link is adopted to be a simple yet reasonably accurate LoS channel model [?]. The LoS channel vector between the  $u$ -th UE and the RIS is given by [?]

$$\mathbf{h}_u^{\text{UR}} = \sqrt{\frac{\beta_0}{(d_u^{\text{UR}})^2}} \bar{\mathbf{h}}_u^{\text{UR}}, \quad (3)$$

where  $d_u^{\text{UR}}$  is the distance between the  $u$ -th UE and the RIS,  $\beta_0$  denotes the path loss at the reference distance  $d_{\text{ref}} = 1$  m, and  $\bar{\mathbf{h}}_u^{\text{UR}}$  represents the array response component which can be denoted by

$$\bar{\mathbf{h}}_u^{\text{UR}} = \begin{bmatrix} 1, e^{-j\frac{2\pi d}{\lambda} \phi_u^{\text{UR}} \varphi_u^{\text{UR}}}, \dots, e^{-j\frac{2\pi d}{\lambda} (M_r-1) \phi_u^{\text{UR}} \varphi_u^{\text{UR}}} \end{bmatrix}^T \\ \otimes \begin{bmatrix} 1, e^{-j\frac{2\pi d}{\lambda} \phi_u^{\text{UR}} \varphi_u^{\text{UR}}}, \dots, e^{-j\frac{2\pi d}{\lambda} (M_c-1) \phi_u^{\text{UR}} \varphi_u^{\text{UR}}} \end{bmatrix}^T,$$

where  $\phi_u^{\text{UR}}, \varphi_u^{\text{UR}}$ , and  $\psi_u^{\text{UR}}$  are related to the sine and cosine terms of the vertical and horizontal angles-of-arrival (AoAs) at the RIS [?], and given by  $\phi_u^{\text{UR}} = \frac{y_u - y_R}{\sqrt{(x_u - x_R)^2 + (y_u - y_R)^2}}$ ,  $\varphi_u^{\text{UR}} = \frac{x_R - x_u}{\sqrt{(x_u - x_R)^2 + (y_u - y_R)^2}}$ ,  $\psi_u^{\text{UR}} = \frac{z_R}{d_u^{\text{UR}}}$ ,  $\lambda$  is the wavelength, and  $T$  denotes transpose. On the other hand, the RIS and UAVs are deployed in the higher altitudes, thus the reflected signal propagation of the RIS-to-UAV link typically occurs in clear airspace where the obstruction or reflection effects diminish. The LoS channel vector between the RIS and the  $a$ -th UAV is given by

$$\mathbf{h}_a^{\text{RA}} = \sqrt{\frac{\beta_0}{(d_a^{\text{RA}})^2}} \bar{\mathbf{h}}_a^{\text{RA}}, \quad (4)$$

where  $d_a^{\text{RA}}$  is the distance between the RIS and the  $a$ -th UAV, and  $\bar{\mathbf{h}}_a^{\text{RA}}$  represents the array response component which can be denoted by

$$\bar{\mathbf{h}}_a^{\text{RA}} = \begin{bmatrix} 1, e^{-j\frac{2\pi d}{\lambda} \phi_a^{\text{RA}} \varphi_a^{\text{RA}}}, \dots, e^{-j\frac{2\pi d}{\lambda} (M_r-1) \phi_a^{\text{RA}} \varphi_a^{\text{RA}}} \end{bmatrix}^T \\ \otimes \begin{bmatrix} 1, e^{-j\frac{2\pi d}{\lambda} \phi_a^{\text{RA}} \varphi_a^{\text{RA}}}, \dots, e^{-j\frac{2\pi d}{\lambda} (M_c-1) \phi_a^{\text{RA}} \varphi_a^{\text{RA}}} \end{bmatrix}^T,$$

where  $\phi_a^{\text{RA}}, \varphi_a^{\text{RA}}$ , and  $\psi_a^{\text{RA}}$  are related to the sine and cosine terms of the vertical and horizontal angles-of-departure (AoDs) from the RIS to the  $a$ -th UAV [?], and respectively given by  $\phi_a^{\text{RA}} = \frac{y_R - y_a}{\sqrt{(x_R - x_a)^2 + (y_R - y_a)^2}}$ ,  $\varphi_a^{\text{RA}} = \frac{x_R - x_a}{\sqrt{(x_R - x_a)^2 + (y_R - y_a)^2}}$ , and  $\psi_a^{\text{RA}} = \frac{z_R - z_a}{d_a^{\text{RA}}}$ .

Given the aforementioned channel models, the concatenated channel for the UE-RIS-UAV link between the  $u$ -th UE and the  $a$ -th UAV through the RIS is given by  $\mathbf{h}_{u,a}^{\text{URA}} = (\mathbf{h}_a^{\text{RA}})^H \mathbf{\Theta} \mathbf{h}_u^{\text{UR}}$  [?]. Accordingly, the SNR of the reflected link between the  $u$ -th UE and the  $a$ -th UAV through the RIS can be written as  $\gamma_{u,a}^{(R)} = \frac{p|\mathbf{h}_{u,a}^{\text{URA}}|^2}{N_0}$  [?]. For successful connection between UE  $u$  and UAV  $a$  via RIS  $r$ ,  $\gamma_{u,a}^{(R,r)} \geq \gamma_0^{\text{RIS}}$ , where  $\gamma_0^{\text{RIS}}$  is the minimum SNR threshold for the communication links between the UEs and the UAVs via the RISs.

We model the considered RIS-assisted UAV network as an undirected graph  $\mathcal{G}(\mathcal{V}, \mathcal{E})$ , where  $\mathcal{V} = \{v_1, v_2, \dots, v_V\}$  is the set of nodes (i.e., UAVs and UEs) in the network,  $\mathcal{E} = \{e_1, e_2, \dots, e_E\}$  is the set of all edges.  $V = |\mathcal{U} \cup \mathcal{A}| = |\mathcal{V}|$  and  $E = |\mathcal{E}|$  are the numbers of vertices and edges in the graph, respectively. The graph  $\mathcal{G}$  implies that all the links in the network are bidirectional, i.e., a node  $v$  is able to reach node  $v'$ , and vice versa. The edge between any two nodes is created based on a typical SNR threshold.

## B. Network Connectivity

For an edge  $e_k$ ,  $1 \leq k \leq E$ , that connects two nodes  $\{v_n, v_m\} \in \mathcal{V}$ , let  $\mathbf{a}_k$  be a vector, where the  $n$ -th and  $m$ -th elements in  $\mathbf{a}_k$  are given by  $a_{k,n} = 1$  and  $a_{k,m} = -1$ , respectively, and zero otherwise. The incidence matrix  $\mathbf{A} \in \mathbf{R}^{V \times E}$  of a graph  $\mathcal{G}$  is the matrix with the  $k$ -th column given by  $\mathbf{a}_k$ . Hence, in undirected graph  $\mathcal{G}(\mathcal{V}, \mathcal{E})$ , the Laplacian matrix  $\mathbf{L}$  is an  $V$  by  $V$  matrix, which is defined as follows [?]:

$$\mathbf{L} = \mathbf{A} \mathbf{A}^T = \sum_{k=1}^E \mathbf{a}_k \mathbf{a}_k^T, \quad (5)$$

where the entries of  $\mathbf{L}$  are given as follows:

$$L(n, m) = \begin{cases} D_{v_n} & \text{if } v_n = v_m, \\ -1 & \text{if } (v_n, v_m) \in \mathcal{E} \\ 0 & \text{otherwise} \end{cases} \quad (6)$$

where  $n, m \in \{1, 2, \dots, V\}$  are the indices of the nodes, and  $D_{v_n}$  is the degree of node  $v_n$ , which represents the number of all its neighboring nodes.

In network connectivity, algebraic connectivity, also called the Fiedler metric or the second smallest eigenvalue [?], measures how well a graph  $\mathcal{G}$  that has the associated Laplacian matrix  $\mathbf{L}$  is connected. From its name, this metric is usually denoted as  $\lambda_2(\mathbf{L})$ . The motivation of  $\lambda_2(\mathbf{L})$  to be used as a network connectivity metric comes from the following two main reasons [?]. First,  $\lambda_2(\mathbf{L}) > 0$  if and only if  $\mathcal{G}$  is connected, i.e.,  $\mathcal{G}$  is only one connected graph. It is worth mentioning that when  $\lambda_2(\mathbf{L}) = 0$ , the graph is disconnected in which at least one of its vertices is unreachable from any other vertices in the graph. Second,  $\lambda_2(\mathbf{L})$  is monotone increasing in the edge set, i.e., if  $\mathcal{G}_1 = (V, E_1)$  and  $\mathcal{G}_2 = (V, E_2)$  and  $E_1 \subseteq E_2$ , then  $\lambda_2(\mathbf{L}_2) \geq \lambda_2(\mathbf{L}_1)$ . This implies that  $\lambda_2(\mathbf{L})$  qualitatively represents the connectivity of a graph in the sense that

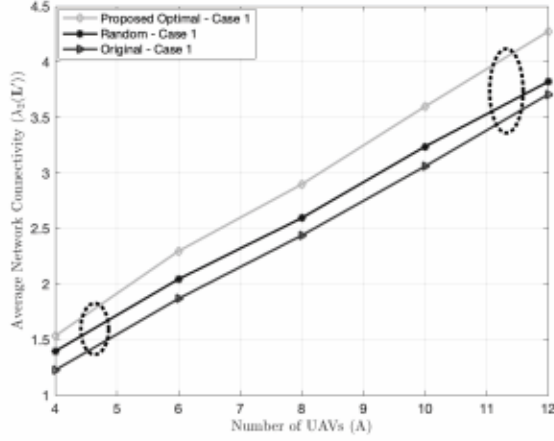


Fig. 2: The average network connectivity  $\lambda_2(\mathbf{L}')$  of case 1 versus the number of UAVs  $A$ .

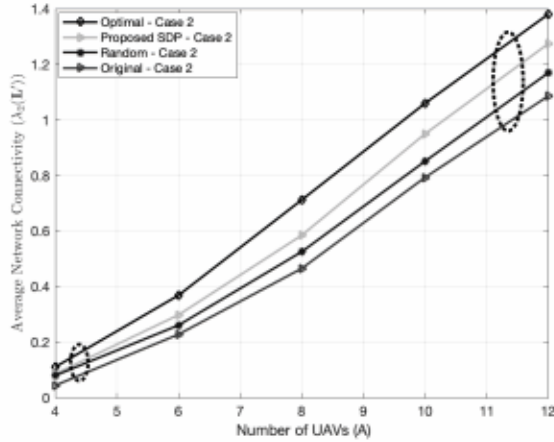


Fig. 3: The average network connectivity  $\lambda_2(\mathbf{L}')$  of case 2 versus the number of UAVs  $A$ .

of 20 m,  $M = 100$ ,  $d_r = 5$  cm,  $d_c = 5$  cm,  $\beta_0 = 10^{-6}$ ,  $N_0 = -130$  dBm, the altitude of the UAVs is 50 m,  $f_c = 3 \times 10^9$  Hz,  $c = 3 \times 10^8$  m/s,  $\alpha = 4$ ,  $p = 1$  watt,  $P = 5$  watt,  $\gamma_0^{(U)} = 85$  dB, and  $\gamma_0^{(A)} = 80$  dB. Unless specified otherwise,  $A = 7$ ,  $U = 10$ , and  $\gamma_0^{(\text{RIS})} = 30$  dB.

For the sake of numerical comparison, the proposed schemes are compared with the following schemes: 1) original benchmark scheme without RIS deployment, 2) random scheme that selects a random link to connect the UE to one of the UAVs through the RIS. For completeness of our work, we also compare the proposed SDP scheme of case 2 with the optimal scheme that is considered as a performance upper bound since it searches over all the possible links between the UEs and the UAVs. In the simulations, the network connectivity is calculated over 500 iterations, and the average value is presented. In each iteration, we change the locations of the UEs and the UAVs.

In Figs. 2 and 3, we show the average network connectivity versus the number of UAVs  $A$  for both cases. For

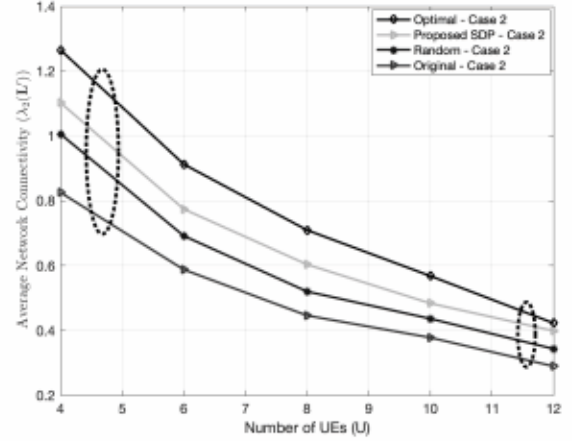


Fig. 4: The average network connectivity  $\lambda_2(\mathbf{L}')$  versus the number of UEs  $U$ .

a small number of UAVs in Figs. 2 and 3, the proposed optimal and SDP schemes offer a slight performance gain in terms of network connectivity compared to the original and the random schemes. This is because our proposed schemes have a few options of links, where the RIS can direct the signal of the UE to a few number of UAVs. However, when the number of UAVs increases, the proposed schemes smartly selects an effective UE-RIS-UAV link that significantly maximizes the network connectivity. It is noted that  $\lambda_2(\mathbf{L}')$  of all schemes increases with the number of UAVs since adding more connected nodes to the network increases the number of edges which increases the network connectivity. It is also noted that the values of  $\lambda_2(\mathbf{L}')$  in Fig. 3 are smaller than the values of  $\lambda_2(\mathbf{L}')$  in Fig. 2 for all the UAVs configurations. This is reasonably because the number of unconnected nodes that represent the UEs in Fig. 3 of case 2, i.e.,  $U = 10$ , is larger than those of Fig. 2 of case 1, which is one UE. This makes the network of case 2 less connected (i.e., more UE nodes and no links between them), thus low network connectivity in Fig. 3. When  $A > 8$  in Fig. 3, the average network connectivity of all the schemes increases significantly with  $A$ , which follows the same behaviour of Fig. 2 that is  $A > U$ .

In Fig. 4, we plot the network connectivity versus the number of UEs  $U$  for case 2. From Fig. 4, we can see that the proposed SDP outperforms the original and the random schemes in terms of network connectivity. Notably, the network connectivity of all the schemes decreases as the number of UEs increases, since adding more unconnected UEs may result in a sparse graph with low network connectivity.

In Fig. 5, we show the impact of the SNR threshold  $\gamma_0^{(\text{RIS})}$  on the network connectivity for case 2. For small SNR threshold, all the links between the UEs and the UAVs through the RIS can satisfy this SNR threshold, thus many alternative links between the potential UE and



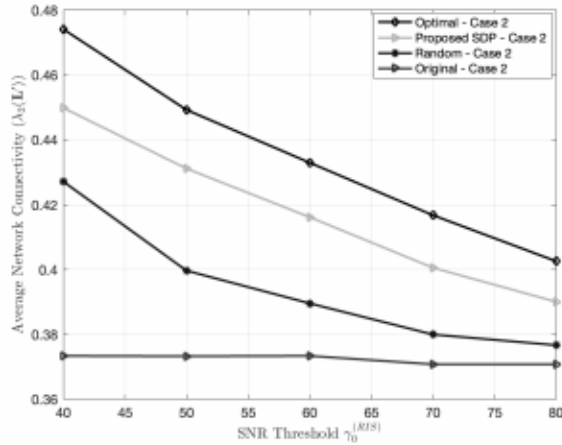


Fig. 5: The average network connectivity  $\lambda_2(\mathbf{L}')$  versus SNR threshold  $\gamma_0^{(RIS)}$  in dB.

the UAVs to select to maximize the network connectivity. On the other hand, for high RIS SNR threshold, a few UE-RIS-UAV links can satisfy such high SNR threshold, thus the network connectivity of all the schemes is degraded, and it becomes close to the original scheme, which does not get affected by changing  $\gamma_0^{(RIS)}$ .

It is worth remarking that while the random scheme adds a random link to the network, the original scheme does not add a link. The proposed solutions balance between the aforementioned aspects by judiciously selecting an effective link, between a UE and a UAV, that maximizes the network connectivity. This utilizes the benefits of the cooperation between an appropriate scheduling algorithm design and RIS phase shift configurations. Compared to the optimal scheme, our proposed SDP has a certain degradation in network connectivity that comes as the achieved polynomial computational complexity as compared to the high complexity of the optimal scheme that is in the order of  $\mathcal{O}(4E'V^3/3)$  [?].

## VI. Conclusion

In this paper, we proposed a novel joint UE-UAV scheduling and RIS phase shift optimization for achieving connected and resilient RIS-assisted UAV networks. We leveraged the RIS to add more links to the network by opportunistically reflecting the signal of the UE to the appropriate UAV such that the network connectivity is maximized. The problem of maximizing the network connectivity was formulated in two cases of a single UE and multiple UEs, and optimal and efficient SDP solutions were proposed for the two problem cases, respectively. Simulation results showed that both the proposed schemes result in improved network connectivity as compared to the existing solutions. Such promising performance gain can be significantly improved for the case of multiple RISs, which will be pursued in our future work.

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