

Fig. 11. (a) Uplink RSMA without user pairing and (b) Uplink RSMA with user pairing.

reduce the computational complexity. Then the optimization variables are changed from decoding order and power allocation to bandwidth allocation and power allocation, by making use of the fact that the optimal decoding order of two users can be determined.

In this letter, we optimize the uplink RSMA with the objective of minimizing the maximum latency. Since the optimal decoding order is difficult to find, user pairing is employed to reduce the computational complexity. Then the optimization variables are changed from decoding order and power allocation to bandwidth allocation and

II. SYSTEM MODEL AND PROBLEM FORMULATION

We derive the closed-form expressions for power and bandwidth allocation, by making use of the fact that the optimal decoding order of two users can be determined. Without loss of generality, this letter considers a single input single output (SISO) uplink RSMA transmission as shown in Fig. 11, which contains a base station (BS) and N users. The channel gain from the user n to BS is denoted by h_n . Using RSMA uplink transmission, the information x_n of user n is divided into x_{n1} and x_{n2} . The message received by BS can be expressed as $y_{BS} = \sum_{n=1}^N \sum_{j=1}^2 \sqrt{h_n} \cdot x_{nj} + n_0$, where n_0 denotes additive Gaussian white noise. After SIC is performed at BS, the rate of x_{nj} can be expressed as $r_{nj} = B \log_2(1 + \frac{p_{nj}}{\sum_{\{(n',j') \in \mathcal{N} \mid \pi_{n',j'} > \pi_{n,j}\}} h_{n'} p_{n',j'} + \sigma^2 B})$, where B is

the bandwidth, p_{nj} is the transmission power allocated to x_{nj} , π_{nj} is the decoding order of x_{nj} , and σ^2 is the power spectral density of the Gaussian noise. So the transmission rate of user n can be expressed as $r_n = \sum_{j=1}^2 r_{nj}$, and the transmission latency can be written as $t_n = PL_n/r_n$, where PL_n is the package length of user n . In some automatic control systems, the BS needs to obtain information from all users before making control decisions, so we build the following optimization problem to minimize the maximum transmission latency.

Without loss of generality, this letter considers a single input single output (SISO) uplink RSMA transmission as shown in Fig. 11, which contains a base station (BS) and N users. The channel gain from the user n to BS is denoted by h_n . Using RSMA uplink transmission, the information of user n is divided into x_{n1} and x_{n2} . The message received by BS can be expressed as $y_{BS} = \sum_{n=1}^N \sum_{j=1}^2 \sqrt{h_n} \cdot x_{nj} + n_0$, where n_0 denotes additive Gaussian white noise. After SIC is performed at BS, the rate of x_{nj} can be expressed as $r_{nj} = B \log_2(1 + \frac{p_{nj}}{\sum_{\{(n',j') \in \mathcal{N} \mid \pi_{n',j'} > \pi_{n,j}\}} h_{n'} p_{n',j'} + \sigma^2 B})$, where B is

the bandwidth, p_{nj} is the transmission power allocated to x_{nj} , π_{nj} is the decoding order of x_{nj} , and σ^2 is the power spectral density of the Gaussian noise. So the transmission rate of user n can be expressed as $r_n = \sum_{j=1}^2 r_{nj}$, and the transmission latency can be written as $t_n = PL_n/r_n$, where PL_n is the package length of user n . In some automatic control systems, the BS needs to obtain information from all users before making control decisions, so we build the following optimization problem to minimize the maximum transmission latency.

Without loss of generality, this letter considers a single input single output (SISO) uplink RSMA transmission as shown in Fig. 11, which contains a base station (BS) and N users. The channel gain from the user n to BS is denoted by h_n . Using RSMA uplink transmission, the information of user n is divided into x_{n1} and x_{n2} . The message received by BS can be expressed as $y_{BS} = \sum_{n=1}^N \sum_{j=1}^2 \sqrt{h_n} \cdot x_{nj} + n_0$, where n_0 denotes additive Gaussian white noise. After SIC is performed at BS, the rate of x_{nj} can be expressed as $r_{nj} = B \log_2(1 + \frac{p_{nj}}{\sum_{\{(n',j') \in \mathcal{N} \mid \pi_{n',j'} > \pi_{n,j}\}} h_{n'} p_{n',j'} + \sigma^2 B})$, where B is

the bandwidth, p_{nj} is the transmission power allocated to x_{nj} , π_{nj} is the decoding order of x_{nj} , and σ^2 is the power spectral density of the Gaussian noise. So the transmission rate of user n can be expressed as $r_n = \sum_{j=1}^2 r_{nj}$, and the transmission latency can be written as $t_n = PL_n/r_n$, where PL_n is the package length of user n . In some automatic control systems, the BS needs to obtain information from all users before making control decisions, so we build the following optimization problem to minimize the maximum transmission latency.

$$\begin{aligned} \mathbf{P1}: \quad & \min_{\pi, p} \max_n t_n \\ \text{s.t.} \quad & p_{nj} > 0, 1 \leq n \leq N, j \in [1, 2]; \\ \mathbf{P2}: \quad & \min_{\pi, p} \tau \\ & \pi \in \Pi; \\ \text{s.t.} \quad & r_n \geq \frac{2PL_n}{\sum_{j=1}^2 p_{nj}}, 1 \leq n \leq N, j \in [1, 2]; \\ & p_{nj} > 0, 1 \leq n \leq N, j \in [1, 2]; \end{aligned} \quad \begin{aligned} (1) \\ (1a) \\ (1b) \\ (2a) \\ (2b) \end{aligned}$$

where $p = [p_{11}, p_{12}, p_{21}, \dots, p_{N2}]$, Π denotes all possible orders of decoding and P_n^{\max} is the maximum transmission power of user n . $\sum_{j=1}^2 p_{nj} \leq P_n^{\max}, 1 \leq n \leq N$;

Using τ to denote the upper bound of latency for all users, we have $t_n \leq \tau, 1 \leq n \leq N$. Then problem $\mathbf{P1}$ can be transformed into:

$$\begin{aligned} \mathbf{P2}: \quad & \min_{\pi, p} \tau \\ & \pi \in \Pi; \\ \text{s.t.} \quad & r_n \geq \frac{2PL_n}{\sum_{j=1}^2 p_{nj}}, 1 \leq n \leq N, j \in [1, 2]; \\ & p_{nj} > 0, 1 \leq n \leq N, j \in [1, 2]; \end{aligned} \quad \begin{aligned} (2a) \\ (2b) \end{aligned}$$

where $p = [p_{11}, p_{12}, p_{21}, \dots, p_{N2}]$, Π denotes all possible orders of decoding and P_n^{\max} is the maximum transmission power of user n . $\sum_{j=1}^2 p_{nj} \leq P_n^{\max}, 1 \leq n \leq N$;

Using τ to denote the upper bound of latency for all users, we have $t_n \leq \tau, 1 \leq n \leq N$. Then problem $\mathbf{P1}$ can be transformed into:

The decoding order π in problem $\mathbf{P2}$ is a discrete variable, and the condition (2a) is in the form of the sum of two logarithmic functions. We can exhaust π and use the successive convex approximation (SCA) algorithm to transform condition (2a) into a convex form to find the approximate solution. However, the decoding order set Π contains $(2N)!/2^N$ elements, which means that the complexity of the algorithm using the exhaustive method will become extremely high as the number of users increases. Existing studies have determined the optimal decoding order of RSMA transmissions for two users [?], so we consider pairing every two users to reduce the complexity of the algorithm.

As shown in part (b) of Fig. 11, suppose all users are paired into M pairs, and each pair contains two users. According to the simulation test, since the change of channel gain is much larger than package length, the performance of pairing mainly depends on the channel gains, so this pairing is performed according to the order of channel gains [?]. The channel gain of the k -th user in the m -th pair to the BS is denoted by $h_k^m, k \in [1, 2], 1 \leq m \leq M$. Research [?] shows that uplink RSMA transmission of two users can achieve all rate regions by splitting the information of only one user. Without loss of generality, suppose the message of the first user in each pair is split into two parts x_{11}^m and x_{12}^m , and the message of the second user is not split, the optimal decoding order at the BS is $\pi_{11}^m, \pi_{12}^m, \pi_{21}^m, \pi_{22}^m$.

The following is an analysis for the m -th pair of users. According to the simulation test, since the change of channel gain is much larger than package length, the performance of pairing mainly depends on the channel gains, so this pairing is performed according to the order of channel gains [?]. The channel gain of the k -th user in the m -th pair to the BS is denoted by $h_k^m, k \in [1, 2], 1 \leq m \leq M$. Research [?] shows that uplink RSMA transmission of two users can achieve all rate regions by splitting the information of only one user. Without loss of generality, suppose the message of the first user in each pair is split into two parts x_{11}^m and x_{12}^m , and the message of the second user is not split, the optimal decoding order at the BS is $\pi_{11}^m, \pi_{12}^m, \pi_{21}^m, \pi_{22}^m$.

where α_{12}^m is the bandwidth allocation factor with $\alpha_{11}^m + \alpha_{12}^m + \alpha_{21}^m + \alpha_{22}^m = 1$. The following is an analysis for the m -th pair of users. According to the simulation test, since the change of channel gain is much larger than package length, the performance of pairing mainly depends on the channel gains, so this pairing is performed according to the order of channel gains [?]. The channel gain of the k -th user in the m -th pair to the BS is denoted by $h_k^m, k \in [1, 2], 1 \leq m \leq M$. Research [?] shows that uplink RSMA transmission of two users can achieve all rate regions by splitting the information of only one user. Without loss of generality, suppose the message of the first user in each pair is split into two parts x_{11}^m and x_{12}^m , and the message of the second user is not split, the optimal decoding order at the BS is $\pi_{11}^m, \pi_{12}^m, \pi_{21}^m, \pi_{22}^m$.

where α_{12}^m is the bandwidth allocation factor with $\alpha_{11}^m + \alpha_{12}^m + \alpha_{21}^m + \alpha_{22}^m = 1$. The following is an analysis for the m -th pair of users. According to the simulation test, since the change of channel gain is much larger than package length, the performance of pairing mainly depends on the channel gains, so this pairing is performed according to the order of channel gains [?]. The channel gain of the k -th user in the m -th pair to the BS is denoted by $h_k^m, k \in [1, 2], 1 \leq m \leq M$. Research [?] shows that uplink RSMA transmission of two users can achieve all rate regions by splitting the information of only one user. Without loss of generality, suppose the message of the first user in each pair is split into two parts x_{11}^m and x_{12}^m , and the message of the second user is not split, the optimal decoding order at the BS is $\pi_{11}^m, \pi_{12}^m, \pi_{21}^m, \pi_{22}^m$.

The optimization of the power and decoding order in **P2** can be translated into the optimization of the bandwidth and power allocation in **P3** as follows:

$$h_1^m p_{12}^m, \quad (5)$$

P3: $\min_{\alpha_m} \tau$ s.t. $\alpha_m \leq 1, P_k^m \leq P_K^m, \sum_{m=1}^M \alpha_m \leq 1, \alpha_m \in [0, 1], P_k^m \in [0, P_K^m], \tau \leq \tau_{\max}$ (6)

where α_m is the bandwidth allocation factor with $\sum_{m=1}^M \alpha_m \leq 1$, P_k^m and P_K^m are the power allocated to x_{11}^m , x_2^m and x_{12}^m respectively. So the rate of user 1 in m -th pair is $r_{11}^m = \alpha_m \log_2(1 + \frac{P_k^m}{\tau})$ and the transmission latency of user k in the m -th pair is $t_k^m = PL_k^m / r_k^m$, where PL_k^m is the package length of user k in the m -th pair.

The optimization of the power and decoding order in **P2** can be translated into the optimization of the bandwidth and power allocation in **P3** as follows:

III. RESOURCE ALLOCATION ALGORITHM FOR (6a)

PAIRED RSMA

$$p_{kj}^m > 0, 1 \leq m \leq M, k, j \in [1, 2]; \quad (6b)$$

Since the expression of transmission rate is a monotonically increasing function of power and bandwidth, we can use contradiction to prove that the optimal solution of **P3** is obtained when and only when all users have the same latency, i.e., $t_1^1 : t_2^1 : t_2^2 : \dots : t_2^M = P_{kmax}^1 : 1 \leq m \leq M$. In other words, the ratio of optimized rates is $r_1^1 : r_2^1 : r_2^2 : \dots : r_2^M = PL_1^1 : PL_2^1 : PL_2^2 : \dots : PL_2^M$. Thus, the rates of two users in the same pair have $r_2^m = \frac{PL_2^m}{PL_1^m} r_1^m$.

Fig. ?? shows the achievable rate region for two users using DSMA transmission when the decoding order is x^m, x^m and

RSMA transmission, when the decoding order is x_{11}^m, x_2^m and x_{12}^m . Since the expression of the region can be reached, a monotonically increasing power allocation is required. For the last AB, the power allocation is. Since the bandwidth, we can use contradiction to prove that the optimal solution of P3 is obtained when and only when all users have the same listen. 2 has the maximum rate as $r_2^M = 1 : 1 : 1 : \dots : 1$, in other words, the ratio of optimized rates is $r_1^1 : r_2^1 : r_1^2 : \dots : r_2^M = PL_1^{\frac{P_m}{\sigma^2 B_{\text{max}}}} : PL_2^{\frac{P_m}{\sigma^2 B_{\text{max}}}} : PL_1^{\frac{P_m}{\sigma^2 B_{\text{max}}}} : \dots : PL_2^{\frac{P_m}{\sigma^2 B_{\text{max}}}}$. Thus, the rates of two users in the same pair have $r_3^m = \frac{P_m}{D_1^m} r_1^m$.

Fig. 77 shows the achievable rate region for two users using RSMA with transmission order 1 and decoding order is 2. The sum rate of the two user is:

For the line AB, the power allocation is:

$$r_1^m + 0 \leq p_{11}^m \leq P_{1\max}^m, \quad p_{12}^m = 0, \quad \frac{h_1^m P_{1\max}^m}{\sigma^2 \beta_{2,m}} \leq p_{2\max}^m. \quad (16)$$

$$p_{11}^m = 0, r_2^m p_{12}^m B \alpha_m P_m^m \log_2 \left(1 + \frac{h^m P_m^m}{\sigma^2 B \alpha_m} \right) \leq (P_m^m)_{\max}, \quad (18)$$

For the line BC, the power allocation is:

$$x_1^m = B\alpha_m \log_2(1 + \frac{n_1^{\text{max}} P_{\text{max}}}{2\beta_1 B \alpha_m}). \quad (12)$$

$$p_{11}^m + p_{12}^m = P_{1max}^m, \quad p_{21}^m + p_{22}^m = P_{2max}^m, \quad (9)$$

According to the above analysis, the optimal power allocation of problem P3 is the intersection of line $r_m^m = \frac{PL_m^m}{PL_1^m} r_1^m$ and the mfc region. As shown in Fig. 7, the intersection point may exist three cases.

For the The CD, the optimal allocation is, according to (??), (??), (??) and (6a), we have:

$$p_{11}^m = 0, \quad p_{12}^m = P_{1max}^m, \quad 0 \leq p_2^m \leq P_{2max}^m, \quad (11)$$

$$\text{User 1 has the DoF maximum rate as: } \frac{h_2^m P_{2\max}}{\sigma^2 B \alpha_{AB}^m} = \frac{PL_2^m}{\tau}, \quad (13)$$

$$r_{\alpha_m}^{m,AB} = \frac{r_{\alpha_m}^{m,AB}}{(2^{\frac{r_{\alpha_m}^{m,AB}}{B\alpha_m}} - 1)(h_2^2 P_{2max}^2 + \alpha_m^2 B\alpha_m^{AB})} \quad (12)$$

According to the above analysis, the optimal power allocation of problem P3 is the intersection of line BC and the intersection point is on BC, and according to (??), (??) and (6a), rate region. As shown in Fig. ??,

the intersection point may exist three cases: $PL_1^m + PL_2^m$
 Case 1: If the intersection point is on AB, and according
 to ((?), ((?), ((?) and (6a), we have: (15)

$$\frac{B\alpha_m^{AB}}{p_{12}^m} \log_2 \left(\frac{h_2^m P_{2max}^{Pm}}{B\alpha_m^{AB}} \right) \sigma^2 \frac{P I_m^{BC}}{B\alpha_m^{BC}}, \quad (13)$$

The r_{12}^m can be obtained by taking p_{12}^m into (??), then r_{12}^m (14)
 $PL_1^m/\tau - r_{12}^m$, and according to (??) we can obtain p_{11}^m :

Case 2: The intersection point is on BC, and according to (??), (??), (??) and (6a)

$$p_{12}^m = \frac{\frac{p_1}{2} - \frac{p_2}{2} \frac{B_0}{B_m} - \frac{1}{2} (h_1^m p_{12}^m + h_1^m p_{12}^m + \sigma^2 B a_m^{BC})}{1 - \frac{B_0}{B_m}}, \quad (17)$$

Case 3: The intersection point is on CD, and according to (??), (??) and (6a):

$$P_{\text{case 3}}^{BC} = \frac{h_1^m P_{1max}^m + h_2^m P_{2max}^m}{\sigma^2 B a_m} = \frac{PL_1^m + PL_2^m}{\gamma} \quad (15)$$

$$B\alpha_m^{CD} \log_2 \left(\frac{h_1^m P_{m,1max}}{h_2^m P_{m,2max} B\alpha_m^{CD}} \right) \sigma^2 B\alpha_m^{BC}, \quad (18)$$

$$P_{12}^m = \frac{PL_2^m}{(P_{\text{B-CD}} + PL_2^m)(2^{\frac{\tau_{\text{B-CD}}}{m}} - 1)} - \frac{h_1^m}{2^{\frac{\tau_{\text{B-CD}}}{m}}}, \quad (16)$$

The $p_{12}^m = \frac{(2^{1-\alpha_m} - 1)(h_1^m P_{12}^{max} + \sigma^2 B \alpha_m^m)}{h_2^m P_{12}^m + \sigma^2 B \alpha_m^m}$ (19) can be obtained by taking p_{12}^m into (??), then $r_1^m = PL^m/\tau - r_2^m$, and according to (??) we can obtain p_{11}^m . According to (??), (??) and (??), the expression of p_{11}^m, α_m^{BC} and α_m^{CD} are given in (??), (??) and (??). Where $W(\cdot)$ is the Lambert-W function which satisfies $W(xe^x) = x$. Note that the Lambert-W function has multiple solutions here, and the appropriate solution should be chosen.

With the closed-form expressions for \mathbf{G}_m and \mathbf{a}_m according to (33)–(35), we can solve the problem **P3** by the bisection method. For each given τ , a set of α_m^{AB} , α_m^{BC} and α_m^{CD} can be calculated according to (22), (23) and (24), and the power allocation corresponding to each case can be obtained by (25), (26) and (27), and then the condition (6d) is used to judge which case occurs. The specific algorithm is shown in Algorithm 1.

According to eq. (3f), Algorithm 1 (7n), each expression of $\check{c}_{n,m}^{AB}$, $\check{c}_{n,m}^{BC}$, $\check{c}_{n,m}^{CD}$ satisfies the power constraint (6d) which introduces the complexity of $\mathcal{O}(M \log_2(1/\epsilon))$ at (7f), (7g) and (7h).² In addition, the complexity of the for loop is multiplied with $\log_2(1/\epsilon)$ at (7f).³ So the total complexity of Algorithm 1 is $\mathcal{O}(M \log_2(1/\epsilon))$.

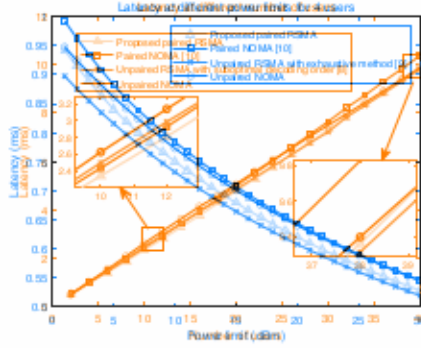


Fig. 4. Latency performance for different total number of users when the power limit $P_{\max} = 23$ dBm.

TABLE I

Comparison of the computational complexity of each scheme

Since the algorithmic complexity of the exhaustive method grows exponentially as the total number of users increases,

Schemes	Simulation time				
	$N = 4$	$N = 10$	$N = 20$	$N = 30$	$N = 40$
Proposed paired RSMA	0.068 s	0.095 s	0.106 s	0.141 s	0.131 s
Unpaired RSMA with exhaustive method	3447.5 s	-	-	-	-
Unpaired RSMA with suboptimal decoding order	1.783 s	7.378 s	19.002 s	36.117 s	74.457 s
Unpaired NOMA	4.084 s	4.515 s	5.737 s	7.589 s	10.113 s
Paired NOMA	4.084 s	4.515 s	5.737 s	7.589 s	10.113 s

we choose a suboptimal decoding order [19] to compare the latency performance at different total number of users in Fig. 22 and the power limit is set to $P_{\max} = 23$ dBm. It can be seen that RSMA always outperforms NOMA, regardless of paired or unpaired. In addition, the paired schemes are more advantageous when the total number of users is small, and as the total number of users increases, the performance of the unpaired schemes will outperform the paired schemes due to the fact that more number of users means more number of pairs and therefore less bandwidth is allocated to each pair.

Overall, the proposed paired-based RSMA resource allocation algorithm greatly reduces the complexity and achieves similar performance to unpaired RSMA. To further evaluate the benefits of the proposed algorithm in terms of computational complexity, Table II gives the simulation time for each scheme at different total number of users. For unpaired RSMA, the algorithmic complexity introduced by the exhaustive method grows exponentially as the total number of users increases, so user pairing is introduced and a low complexity resource allocation algorithm based on user pairing is proposed to minimize the maximum transmission latency. However, the complexity of unpaired uplink RSMA to confirm the optimal decoding order exponentially increases, so there is a trade-off between computational complexity and transmission performance. The optimal power allocation scheme is determined by judging which one satisfies the power constraint. Results show that the proposed low-complexity algorithm based on user pairing significantly reduces the user complexity and also achieves similar performance to unpaired uplink RSMA.

TABLE I

COMPARISON OF THE COMPUTATIONAL COMPLEXITY OF EACH SCHEME

Schemes	Simulation time				
	$N = 4$	$N = 10$	$N = 20$	$N = 30$	$N = 40$
Proposed paired RSMA	0.068 s	0.095 s	0.106 s	0.141 s	0.131 s
Unpaired RSMA with exhaustive method	3447.5 s	-	-	-	-
Unpaired RSMA with suboptimal decoding order	1.783 s	7.378 s	19.002 s	36.117 s	74.457 s
Paired NOMA	4.084 s	4.515 s	5.737 s	7.589 s	10.113 s
Unpaired NOMA	4.084 s	4.515 s	5.737 s	7.589 s	10.113 s

a closed-form expression for power and bandwidth allocation, and achieves similar performance to unpaired RSMA with a very low complexity.

The results demonstrate that the proposed user pairing-based power allocation algorithm achieves good performance with significantly reduced computational complexity. As the total number of users increases, the performance of the proposed algorithm decreases due to the total bandwidth limitation, and the computational complexity of the unpaired uplink RSMA to confirm the optimal decoding order exponentially increases, so there is a trade-off between computational complexity and transmission performance.

V. CONCLUSION

In this letter, to address the requirement of maximum latency among all users in some automatic control scenarios, we propose a resource allocation algorithm for uplink RSMA to minimize the maximum transmission latency. However, the complexity of uplink RSMA to confirm the optimal decoding order grows exponentially with the total number of users, so user pairing is introduced and a low-complexity resource allocation algorithm based on user pairing is designed to transform the optimization of power and decoding order into the optimization of power and bandwidth allocation. The achievable rate region of two-user uplink RSMA is first analyzed, and the closed-form expressions of three possible values of the optimal power and bandwidth allocation are derived. Then the maximum latency τ is determined by the bisection method, and for each given τ , the corresponding three power and bandwidth allocations are derived. The optimal power allocation scheme is determined by judging which one satisfies the power constraint. Results show that the proposed low-complexity algorithm based on user pairing significantly reduces the user complexity and also achieves similar performance to unpaired uplink RSMA.

V. Conclusion

In this letter, to address the requirement of maximum latency among all users in some automatic control scenarios, we propose a resource allocation algorithm for uplink RSMA to minimize the maximum transmission latency. However, the complexity of unpaired uplink RSMA to confirm the optimal decoding order grows exponentially with the total number of users, so user pairing is introduced and a low-complexity resource allocation algorithm based on user pairing is designed to transform the optimization of power and decoding order into the optimization of power and bandwidth allocation. The achievable rate region of two-user uplink RSMA is first analyzed, and

REFERENCES

- [1] V. Poor, "Rate-Splitting Multiple Access: Fundamentals, Survey, and Future Research Trends," in *IEEE Communications Surveys & Tutorials*, vol. 24, no. 4, pp. 2073–2126, Fourthquarter 2022, doi: 10.1109/COMST.2022.3192012.
- [2] Y. Liang, B. Zhao, and Y. Li, "Rate-Splitting Multiple Access: A Survey," in *IEEE Communications Surveys & Tutorials*, vol. 24, no. 4, pp. 2073–2126, Fourthquarter 2022, doi: 10.1109/COMST.2022.3192012.

the closed-form expressions of the possible values of the optimal power and bandwidth allocation are derived. Then the maximum latency τ is determined by the bisection method and for each given τ , the corresponding three power and bandwidth allocations are derived. The optimal power allocation scheme is determined by judging which one satisfies the power constraint. Results show that the proposed low-complexity algorithm based on user pairing significantly reduces the user complexity and also achieves similar performance to an unpaired uplink RSMA.

- [6] S. A. Tegos, P. D. Diamantoulakis and G. K. Karagiannidis, "On the Performance of Uplink Rate-Splitting Multiple Access," in *IEEE Communications Letters*, vol. 26, no. 3, pp. 523-527, March 2022, doi: 10.1109/LCOMM.2022.3142102.
- [7] O. Abbasi and H. Yanikomeroglu, "Transmission Scheme, Detection and Power Allocation for Uplink User Cooperation With NOMA and RSMA," in *IEEE Transactions on Wireless Communications*, vol. 22, no. 1, pp. 223-232, Oct. 2022, doi: 10.1109/LCOMM.2022.3192012.
- [8] M. Katwe, K. Singh, B. Clerckx and C. -P. Li, "Rate Splitting Multiple Access for Sum-Rate Maximization in IRS Aided Uplink Communications," in *IEEE Transactions on Wireless Communications*, vol. 22, no. 4, pp. 2246-2261, April 2023, doi: 10.1109/TWC.2022.3210338.
- [9] Z. Yang, M. Chen, W. Saad, W. Xu and M. Shikh-Bahaei, "Sum-Rate Maximization of Uplink Rate-Splitting Multiple Access (RSMA) Communication," in *IEEE Transactions on Mobile Computing*, vol. 21, no. 7, pp. 2596-2609, 1 July 2022, doi: 10.1109/TMC.2020.3037374.
- [10] Z. Ding, P. Fan and H. V. Poor, "Impact of User Pairing on 5G Nonorthogonal Multiple-Access Downlink Transmissions," in *IEEE Transactions on Vehicular Technology*, vol. 65, no. 8, pp. 6010-6023, Aug. 2016, doi: 10.1109/TVT.2015.2480766.
- [11] B. Rimoldi and R. Urbanke, "A rate-splitting approach to the gaussian multiple-access channel," in *IEEE Transactions on Information Theory*, vol. 42, no. 4, pp. 364-375, 1996.
- [12] S. Boyd and L. Vandenberghe, *Convex Optimization*. Cambridge, U.K.: Cambridge Univ. Press, 2004.
- [1] A. Maira, C. D'Azavedo, C. D'Azavedo and B. Clerckx, "Rate-Splitting Multiple Access for 6G," Part 1: Principles, Applications and Future Works," in *IEEE Communications Letters*, vol. 26, no. 1, pp. 171-185, Jan. 2023, doi: 10.1109/TWC.2022.3195532.
- [2] M. Katwe, K. Singh, B. Clerckx and C. -P. Li, "Rate Splitting Multiple Access for Sum-Rate Maximization in IRS Aided Uplink Communications," in *IEEE Transactions on Wireless Communications*, vol. 22, no. 4, pp. 2246-2261, April 2023, doi: 10.1109/TWC.2022.3210338.
- [3] Z. Yang, M. Chen, W. Saad, W. Xu and M. Shikh-Bahaei, "Sum-Rate Maximization of Uplink Rate-Splitting Multiple Access (RSMA) Communication," in *IEEE Transactions on Mobile Computing*, vol. 21, no. 7, pp. 2596-2609, 1 July 2022, doi: 10.1109/TMC.2020.3037374.
- [4] H. Liu, P. Fan, K. S. R. Kumar and H. V. Poor, "Rate-Splitting Multiple Access Downlink Transmissions," in *IEEE Transactions on Vehicular Technology*, vol. 65, no. 8, pp. 6010-6023, Aug. 2016, doi: 10.1109/TVT.2015.2480766.
- [5] C. Sun, H. Lin, S. Yan, T. A. Tsiptsis and J. Yuan, "Joint Receive and Passive Beamforming Optimization for RIS-Assisted Uplink RSMA Systems," in *IEEE Wireless Communications Letters*, doi: 10.1109/LWC.2023.3266883.
- [6] S. A. Tegos, P. D. Diamantoulakis and G. K. Karagiannidis, "On the Performance of Uplink Rate-Splitting Multiple Access," in *IEEE Communications Letters*, vol. 26, no. 3, pp. 523-527, March 2022, doi: 10.1109/LCOMM.2022.3142102.
- [7] O. Abbasi and H. Yanikomeroglu, "Transmission Scheme, Detection and Power Allocation for Uplink User Cooperation With NOMA and RSMA," in *IEEE Transactions on Wireless Communications*, vol. 22, no. 1, pp. 471-485, Jan. 2023, doi: 10.1109/TWC.2022.3195532.
- [8] M. Katwe, K. Singh, B. Clerckx and C. -P. Li, "Rate Splitting Multiple Access for Sum-Rate Maximization in IRS Aided Uplink Communications," in *IEEE Transactions on Wireless Communications*, vol. 22, no. 4, pp. 2246-2261, April 2023, doi: 10.1109/TWC.2022.3210338.
- [9] Z. Yang, M. Chen, W. Saad, W. Xu and M. Shikh-Bahaei, "Sum-Rate Maximization of Uplink Rate-Splitting Multiple Access (RSMA) Communication," in *IEEE Transactions on Mobile Computing*, vol. 21, no. 7, pp. 2596-2609, 1 July 2022, doi: 10.1109/TMC.2020.3037374.
- [10] Z. Ding, P. Fan and H. V. Poor, "Impact of User Pairing on 5G Nonorthogonal Multiple-Access Downlink Transmissions," in *IEEE Transactions on Vehicular Technology*, vol. 65, no. 8, pp. 6010-6023, Aug. 2016, doi: 10.1109/TVT.2015.2480766.
- [11] B. Rimoldi and R. Urbanke, "A rate-splitting approach to the gaussian multiple-access channel," in *IEEE Transactions on Information Theory*, vol. 42, no. 2, pp. 364-375, 1996.
- [12] S. Boyd and L. Vandenberghe, *Convex Optimization*. Cambridge, U.K.: Cambridge Univ. Press, 2004.