

Joint Device Identification, Channel Estimation, and Signal Detection for LEO Satellite-Enabled Random Access

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Abstract—This paper investigates joint device identification, channel estimation, and signal detection for LEO satellite-enabled grant-free random access, where a multiple-input multiple-output (MIMO) system with orthogonal time-frequency space modulation (OTFS) is utilized to combat the dynamics of the terrestrial-satellite link (TSL). We divide the receiver structure into three modules: first, a linear module for identifying active devices, which leverages the generalized approximate message passing (GAMP) algorithm to eliminate inter-user interference in the delay-Doppler domain; second, a non-linear module adopting the message passing algorithm to jointly estimate channel and detect transmit signals; the third aided by Markov random field (MRF) aims to explore the three dimensional block sparsity of channel in the delay-Doppler-angle domain. The soft information is exchanged iteratively between these three modules by careful scheduling. Furthermore, the expectation-maximization algorithm is embedded to learn the hyperparameters in prior distributions. Simulation results demonstrate that the proposed scheme outperforms the conventional methods significantly in terms of activity error rate, channel estimation accuracy, and symbol error rate.

Index Terms—Random access, OTFS, satellite communications, message passing, Doppler shift

I. Introduction

Internet-of-Things (IoT) is one of the critical scenarios in next-generation communications. Presently, there are numerous applications where IoT devices could be distributed in remote regions, such as deserts, oceans, and forests [?], but they are not supported by existing cellular communication networks. Fortunately, low-earth orbit (LEO) satellites possess low propagation delay, low path loss, and flexible elevation angles, making them a highly promising solution to provide global coverage. In such cases, the multiple access protocol plays a key role in supporting efficient connectivity.

Grant-free random access (GFRA) is considered to be suitable for machine-type communications, as it reduces signaling overhead and power consumption, and enhances access capability. Over the past few years, many methods have been proposed for joint channel estimation and device identification in the terrestrial GFRA systems. For example, the approximate message passing (AMP) was adopted

in [?] to address this problem. In [?], orthogonal frequency division multiplexing (OFDM) was integrated into GFRA systems, and the generalized multiple measurement vector AMP was proposed to explore the channel sparsity in the angular domain. To further improve system performance, [?] and [?] adopted spreading-based transmission schemes and designed message passing-type algorithm to jointly identify devices, estimate channel, and detect signal. The above mentioned works have been designed for block fading channels, which are assumed to remain constant during once transmission. However, the high mobility of LEO satellite inevitably leads to rapid change of terrestrial-satellite link (TSL) and the large Doppler shift, and the motion of devices may incur nonnegligible Doppler spread [?], both of which may cause outdated CSI and severe inter-carrier interference, and then degrades the performance of current algorithms. These effects and the propagation delay should be taken into account. As a result, current terrestrial GFRA schemes are not directly applicable to LEO satellite communications. To facilitate transmissions, precompensation technique [?] for delay and Doppler shift may be adopted before GFRA, but it introduces extra complexity which may decrease the battery life of remote IoT devices, and the most of conventional schemes cannot handle the Doppler spread effectively.

Orthogonal time-frequency space (OTFS) modulation [?], which operates directly in the delay-Doppler domain, has been proposed as a promising solution to alleviate the aforementioned issues. The location of non-zero element of effective channel corresponds to the delay and Doppler shift of each physical path when the two conditions are satisfied that the delay and Doppler shift are within one symbol duration and subcarrier spacing, respectively. Therefore, it is possible for satellite to estimate the effective channel and then detect signal, without precompensation at the terrestrial devices. In [?] and [?], two GFRA schemes with MIMO-OTFS have been proposed for LEO satellite communications, where the channel estimation and signal detection are considered separately. However, to facilitate algorithm design, they still require the terrestrial devices to precompensate for delay and/or Doppler shift before GFRA.

In this paper, we investigate joint device identification, channel estimation, and signal detection in LEO satellite-enabled GFRA, where MIMO-OTFS is adopted to address the doubly dispersive effect and improve performance.

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B. Problem Formulation

The q -th frame received from all devices can be represented as

$$\mathbf{Y}_{q,a_y,a_z}^{\text{DDA}}[k,l] = \sum_{u=0}^{U-1} \lambda_u \mathbf{Y}_{u,a_y,a_z}^{\text{DDA}}[k,l] + \mathbf{Z}_{q,a_y,a_z}^{\text{DDA}}[k,l], \quad (3)$$

where λ_u is the activity indicator of the u -th device, with $\lambda_u = 1$ if active and $\lambda_u = 0$ otherwise, and $\mathbf{Z}_{q,a_y,a_z}^{\text{DDA}}[k,l] \sim \mathcal{CN}(0, \sigma^2)$ is the noise in the delay-Doppler-angle domain. Note that the effective channel of each device in (??) is a 3D tensor at each antenna. To facilitate the algorithm design, we decouple it into a set of matrices by rewriting (??) as the matrix form along the received delay dimension l , i.e.,

$$\mathbf{Y}_q^l = \mathbf{C}_q^l (\mathbf{T}^l \otimes \mathbf{I}_N) (\Lambda \otimes \mathbf{I}_{MN}) \tilde{\mathbf{H}}^l + \mathbf{Z}_q^l, \quad (4)$$

where the $(a_z + 1 + N_z a_y)$ -th column of \mathbf{Y}_q^l is $\mathbf{Y}_{q,a_y,a_z}^{\text{DDA}}[:,l] \in \mathbb{C}^N$; $\mathbf{C}_q^l = [\mathbf{C}_{0,q}^l, \dots, \mathbf{C}_{U-1,q}^l]$, where $\mathbf{C}_{u,q}^l \in \mathbb{C}^{N \times MN}$ is the spreading code matrix of the u -th device in received delay dimension l . Note that $\mathbf{C}_{u,q}^l$ is a block circulant matrix due to the 2D circular convolution in (??), and its sub-matrix is the circulant matrix, formed by $[\mathbf{C}_u^q[0, (l-l')_M], \mathbf{C}_u^q[1, (l-l')_M], \dots, \mathbf{C}_u^q[(l-l')_M, (l-l')_M]]$. $\mathbf{T}^l = \text{diag}(\mathbf{t}_0^l, \dots, \mathbf{t}_{U-1}^l)$, where $\text{diag}(\mathbf{x})$ returns a diagonal matrix with the elements of vector \mathbf{x} on the main diagonal, $\mathbf{t}_u^l = [\mathbf{t}_u[l]_M, \dots, \mathbf{t}_u[(l-M+1)_M]]$, and $\mathbf{I}_N \in \mathbb{R}^{N \times N}$ is the identity matrix; $\Lambda = \text{diag}(\boldsymbol{\lambda})$, where $\boldsymbol{\lambda} = [\lambda_0, \dots, \lambda_{U-1}]$; the $(a_z + 1 + N_z a_y)$ -th column of $\tilde{\mathbf{H}} \in \mathbb{C}^{UMN \times Na}$ is given by $[\text{vec}^T(\mathbf{H}_{0,a_y,a_z}^{\text{DDA}}[:, :, l]), \dots, \text{vec}^T(\mathbf{H}_{U-1,a_y,a_z}^{\text{DDA}}[:, :, l])]^T \in \mathbb{C}^{UMN}$, where $\text{vec}(\cdot)$ denotes the vectorization of a matrix; the elements of \mathbf{Z}_q^l are independent Gaussian noises. We then collect all the received frames into a single matrix as

$$\mathbf{Y}^l = \mathbf{C}^l (\mathbf{T}^l \otimes \mathbf{I}_N) \mathbf{H}^l + \mathbf{Z}^l \quad (5)$$

$$= \mathbf{C}^l \mathbf{W}^l + \mathbf{Z}^l, \quad (6)$$

where $\mathbf{Y}^l = [(\mathbf{Y}_0^l)^T, \dots, (\mathbf{Y}_{Q-1}^l)^T]^T$, $\mathbf{C}^l = [(\mathbf{C}_0^l)^T, \dots, (\mathbf{C}_{Q-1}^l)^T]^T$, $\mathbf{W}^l = (\mathbf{T}^l \otimes \mathbf{I}_N) \mathbf{H}^l$, and $\mathbf{H}^l = (\Lambda \otimes \mathbf{I}_{MN}) \tilde{\mathbf{H}}^l$.

Next, to clearly elaborate the formulated problem and proposed algorithm, we introduce some notations. Firstly, \mathbf{H}^l is partitioned into submatrices $\mathbf{H}^{l,l'} \in \mathbb{C}^{MN \times Na}$, $\mathbf{H}^{l,l'} = \mathbf{H}^l[(l')_M : (l'+1)_M - 1, :]$ corresponding to the channel matrix of the l' -th device along the received delay dimension l . Those submatrices are further split as $\mathbf{H}^{l,u,l'} = \mathbf{H}^{l,u}[(l')_M : (l'+1)_M - 1, :]$ $\in \mathbb{C}^{N \times Na}$, $l' = 0, \dots, M-1$, which is the channel of the l' -th grid in the delay dimension of the u -th device. \mathbf{W}^l is partitioned similarly, and then we get $\mathbf{W}^{l,u}$ and $\mathbf{W}^{l,u,l'}$. Finally, we collect all the transmitted information symbols as the vector $\mathbf{t} = [\mathbf{t}_0, \dots, \mathbf{t}_{U-1}]$, and collect all the channels as $\mathbf{H} = [\mathbf{H}^0, \dots, \mathbf{H}^{M-1}]$.

To perform joint device identification, channel estimation and signal detection, we resort to the Bayesian approach which needs prior distribution of the estimated variables. Firstly, we adopt the conditional Bernoulli

Gaussian-mixture (GM) distribution to characterize the channel, i.e.,

$$p(h_{i,j}^{l,u,l'} | s_{i,j}^{u,l'}) = \delta(s_{i,j}^{u,l'} - 1) \sum_{k=1}^K \omega_k^u \mathcal{CN}(h_{i,j}^{l,u,l'} | \mu_k^u, \phi_k^u) + \delta(s_{i,j}^{u,l'} + 1) \delta(h_{i,j}^{l,u,l'}), \quad (7)$$

where K and $(\omega_k^u, \mu_k^u, \phi_k^u)$ are the number of components and parameters of GM, respectively, $h_{i,j}^{l,u,l'}$ is the (i,j) -th element of $\mathbf{H}^{l,u,l'}$, $s_{i,j}^{u,l'} \in \{+1, -1\}$ is the corresponding support, and $\delta(\cdot)$ is the Dirac delta function. Then, we adopt the Markov random field (MRF) prior to describe the 3D block sparsity of the channel tensor, and then the support can be characterized by the classic Ising model as

$$p(\mathbf{S}^{u,l'}) \propto \exp \left(\sum_{i=0}^{N-1} \sum_{j=0}^{N_a-1} \left(\frac{1}{2} \sum_{s_{i',j'}^{u,l'} \in \mathcal{D}_{i,j}^{u,l'}} \beta s_{i',j'}^{u,l'} - \alpha \right) s_{i,j}^{u,l'} \right) = \left[\prod_{i,j} \prod_{s_{i',j'}^{u,l'} \in \mathcal{D}_{i,j}^{u,l'}} \psi(s_{i,j}^{u,l'}, s_{i',j'}^{u,l'}) \right]^{\frac{1}{2}} \prod_{i,j} \gamma(s_{i,j}^{u,l'}) \quad (8)$$

where $\psi(s_{i,j}^{u,l'}, s_{i',j'}^{u,l'}) = \exp(\beta s_{i,j}^{u,l'} s_{i',j'}^{u,l'})$, $\gamma(s_{i,j}^{u,l'}) = \exp(-\alpha s_{i,j}^{u,l'})$, $\mathbf{S}^{u,l'}$ is a support matrix with (i,j) -th element $s_{i,j}^{u,l'}$, $\mathcal{D}_{i,j}^{u,l'} = \{s_{i-1,j}^{u,l'}, s_{i+1,j}^{u,l'}, s_{i,j-1}^{u,l'}, s_{i,j+1}^{u,l'}\}$ is the set containing the neighbors of $s_{i,j}^{u,l'}$, and α and β are the parameters of MRF prior; a larger β implies a larger size of each block of nonzeros, and a larger α encourages a sparser $\mathbf{H}^{l,u,l'}$. Based on (??)-(??), the maximum a

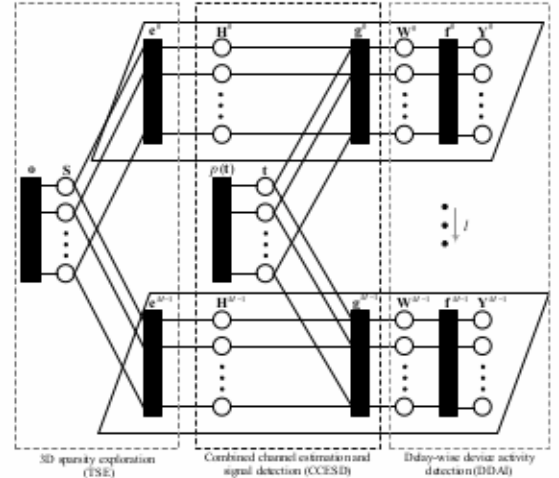


Fig. 1: Factor graph representation.

posteriori (MAP) estimate for $(\mathbf{W}, \mathbf{H}, \mathbf{t}, \mathbf{S})$ is given by

$$(\hat{\mathbf{W}}, \hat{\mathbf{H}}, \hat{\mathbf{t}}, \hat{\mathbf{S}}) = \arg \max_{(\mathbf{W}, \mathbf{H}, \mathbf{t}, \mathbf{S})} p(\mathbf{W}, \mathbf{H}, \mathbf{t}, \mathbf{S} | \mathbf{Y}), \quad (9)$$

where $\mathbf{Y} = [\mathbf{Y}^0, \dots, \mathbf{Y}^{M-1}]$, $\mathbf{W} = [\mathbf{W}^0, \dots, \mathbf{W}^{M-1}]$, \mathbf{S} is composed of $\mathbf{S}^{u,l'}$, and the posterior distribution is represented as

$$p(\mathbf{W}, \mathbf{H}, \mathbf{t}, \mathbf{S} | \mathbf{Y})$$

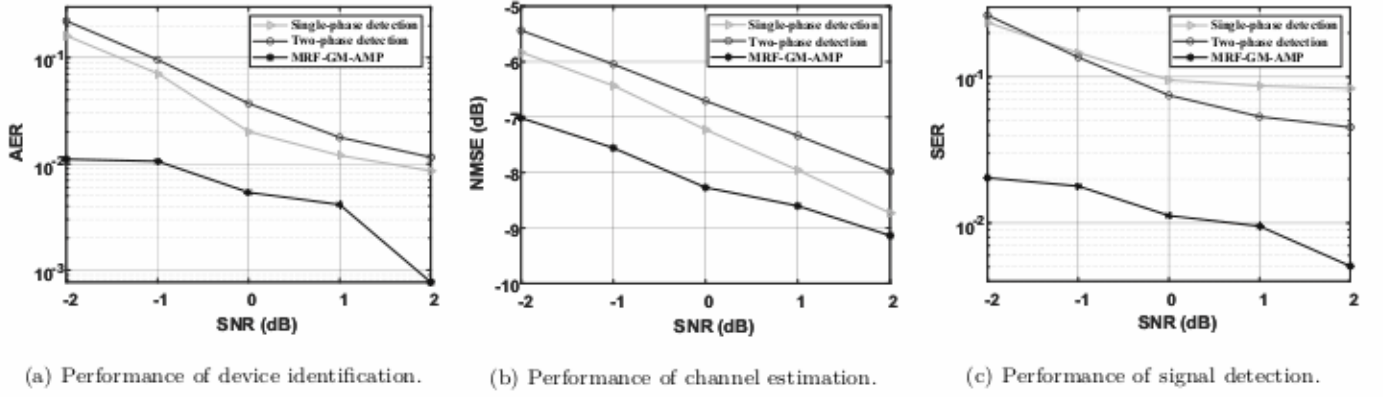


Fig. 2: Performance comparison between the single-phase detection, two-phase detection, and MRF-GM-AMP under different SNR values, where $U = 40$, $p_\lambda = 0.1$, and $N_y = N_z = 4$.

IV. Numerical Results

In this section, we demonstrate the performance of the proposed algorithms through computer simulations. We consider the scenarios of the non-terrestrial networks recommended by the 3GPP [2], where the satellite operates at S-band with 15 kHz of subcarrier spacing and 600 km of altitude, the power delay profile of channel complex gain follows the NTN-TDL-D, the differential delay (ms) is uniformly selected from $[0, 4.44]$, and the Doppler shift (kHz) is uniformly selected from $[-41, 41]$. We consider the sporadic transmissions that there are 40 potential devices with 0.1 of active probability, and the active devices transmit consecutive OTFS frames with $Q = 20$, $M = 16$, and $N = 5$. In addition, the nonnegative pulse amplitude modulation [2] with $|A| = 4$ is adopted for solving phase ambiguity, and the elements of spreading code obey $\mathcal{CN}(0, \frac{1}{Q})$. Finally, we define the received signal-to-noise ratio as $\text{SNR} = 10 \log_{10} \frac{\sum_{i=0}^{M-1} \|\mathbf{R}^i\|_F^2}{\sum_{i=0}^{M-1} \|\mathbf{R}^i\|_F^2}$, and the average device activity error rate (AER), the average normalized mean-squared-error (NMSE), and the average symbol error rate (SER) are adopted as metrics for device identification, channel estimation, and signal detection, respectively, given by $\text{AER} = \frac{1}{U} \sum_{u=0}^{U-1} |\lambda_u - \hat{\lambda}_u|$, $\text{NMSE} = \frac{\sum_{i=0}^{M-1} \|\mathbf{H}^i - \hat{\mathbf{H}}^i\|_F^2}{\sum_{i=0}^{M-1} \|\mathbf{H}^i\|_F^2}$, and $\text{SER} = \frac{1}{UM} \sum_{i=0}^{UM-1} |t_i - \hat{t}_i|$, where we assume that the inactive devices transmit zero for computing the SER.

Fig. ??, Fig. ??, and Fig. ?? compare device identification, channel estimation, and signal detection performance between the proposed algorithm and benchmarks, respectively. Here, the single-phase method adopts the same transmission scheme as ours, and the ConvSBL-GAMP [?] is used to estimate \mathbf{W}^i firstly, and then an energy detector is adopted to detect the transmitted information symbols; the two-phase scheme adopts the ConvSBL-GAMP to jointly estimate channel and detect active devices based on transmitted pilots, and then the GAMP detector is adopted to detect information symbols. From the figures, the performance of the proposed algorithm increases with the SNR, and always outperforms the two benchmarks, which indicates the effectiveness of the proposed scheme

for LEO satellite-based uplink transmission in presence of the large differential delay and Doppler shift. Notice that conventional separated detection scheme has a high error floor for SER; hence it can only support a small number of devices. On the other hand, the proposed MRF-GM-AMP works well. This is due to the benefit of joint device identification, channel estimation, and signal detection design. For example, when the AER is around 0.01 in Fig. ??, the proposed algorithm has about 3 dB gain in terms of SNR, and in Fig. ??, the proposed algorithm always has 1 dB and 2 dB gain compared with the single-phase and two-phase detection, respectively. In Fig. ??, when the SER is around 0.05, the proposed algorithm outperforms the two benchmarks by more than 4 dB. In addition, the SER of MRF-GM-AMP is below 0.05 when the SNR is greater than -2 dB, which indicates that the proposed algorithm could work well in the low SNR regime, and thus is suitable for the satellite communications.

V. Conclusion

This work developed a joint device identification, channel estimation, and signal detection scheme for MIMO-OTFS-based GFRA in LEO satellite communications, where both the large differential delay and Doppler shift exist. To provide low-complexity yet near-optimal estimation and exploit the 3D-structured sparsity of the channel in the delay-Doppler-angle domain, we proposed a message passing-type approach with MRF prior and carefully designed receiver structure. Simulation results demonstrate that the proposed algorithm outperforms conventional algorithms significantly, with a linear complexity in the number of devices and the ability to operate in the low SNR regime, making it suitable for random access in LEO satellite communications.