

Fehlerrechnungen

$$C_{th} = \frac{C_A m_A (T_A - T_M) + C_B m_B \cdot (T_B - T_M)}{T_M - T_B}$$

$$\left| \frac{\partial C_{th}}{\partial m_A} \right| \Delta m_A = \left| \frac{C_A \Delta m_A (T_A - T_M)}{T_M - T_B} \right|$$

$$\left| \frac{\partial C_{th}}{\partial m_B} \right| \Delta m_B = \left| \frac{C_B \Delta m_B (\cancel{T_B} - \cancel{T_M})}{\cancel{T_M} - \cancel{T_B}} \right| = C_B \Delta m_B$$

$$\left| \frac{\partial C_{th}}{\partial T_A} \right| \Delta T_A = \frac{C_A m_A \Delta T_A}{|T_M - T_B|}$$

$$\begin{aligned} \left| \frac{\partial C_{th}}{\partial T_B} \right| \Delta T_B &= \frac{\cancel{C_B m_B (T_M - T_B)} - (C_A m_A (T_A - \cancel{T_B}) + \cancel{C_B m_B (\cancel{T_B} - T_M)}) \cdot (-1)}{(T_M - T_B)^2} \\ &= \left| \frac{C_A m_A (T_A - T_B) \Delta T_B}{(T_M - T_B)^2} \right| \end{aligned}$$

$$\left| \frac{\partial C_{th}}{\partial T_M} \right| \Delta T_M = \left| \frac{-(C_A m_A + C_B m_B) \cdot (T_M - T_B) - (C_A m_A (T_A - T_M) + C_B m_B (T_B - T_M)) \cdot 1}{(T_M - T_B)^2} \right|$$

$$= \frac{C_A m_A (\cancel{T_M} - T_B + T_A - \cancel{T_M}) + C_B m_B (\cancel{T_M} - \cancel{T_B} + \cancel{T_B} - \cancel{T_M})}{(T_M - T_B)^2} \Delta T_M$$

$$= \left| \frac{C_A m_A (T_A - T_B)}{(T_M - T_B)^2} \right| \Delta T_M$$

$$C_A = \frac{(C_B m_B + C_H)(T_H - T_B)}{m_A (T_A - T_H)}$$

$$\left| \frac{\partial C_A}{\partial C_H} \right| \Delta C_H = \left| \frac{\Delta C_H (T_H - T_B)}{m_A (T_A - T_H)} \right|$$

$$\left| \frac{\partial C_A}{\partial m_A} \right| \Delta m_A = \left| \frac{C_A \Delta m_A}{m_A} \right|$$

$$\left| \frac{\partial C_A}{\partial m_B} \right| \Delta m_B = \left| \frac{C_B \Delta m_B (T_H - T_B)}{m_A (T_A - T_H)} \right|$$

$$\left| \frac{\partial C_A}{\partial T_A} \right| \Delta T_A = \left| \frac{C_A \Delta T_A}{(T_A - T_H)} \right|$$

$$\left| \frac{\partial C_A}{\partial T_B} \right| \Delta T_B = \left| \frac{C_A \Delta T_B}{(T_H - T_B)} \right|$$

$$\begin{aligned} \left| \frac{\partial C_A}{\partial T_H} \right| \Delta T_H &= (C_B m_B + C_H) \Delta T_H \cdot \frac{1 m_A (T_A - T_H) - (T_H - T_B) \cdot (-m_A)}{m_A^2} \\ &= (C_B m_B + C_H) \Delta T_H \cdot \frac{T_A - T_B}{m_A} \end{aligned}$$