Lecture 18: Hierarchical Models

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Outline

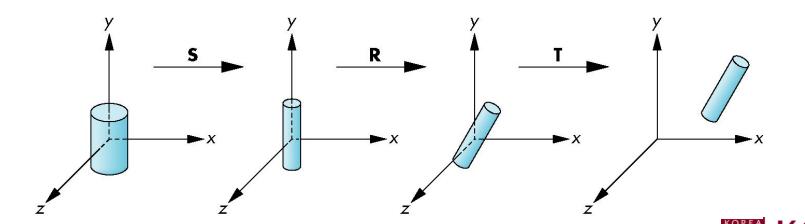
- Limitations of linear modeling
- Hierarchical modeling
- Tree-structured modeling and traversal





Instance Transformation

- Start with a prototype object (a symbol)
- Each appearance of the object in the model is an instance
 - Can have different scale, orient, position
 - Defines instance transformation



Symbol-Instance Table

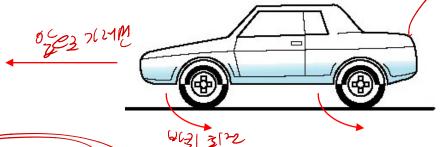
 Can store a model by assigning a number to each symbol and storing the parameters for the instance transformation

	Object.			
	Symbol	Scale	Rotate	Translate
Same symbol Different instance	1 2 3 1	s _x , s _y , s _z	$\theta_{x'} \theta_{y'} \theta_{z}$	d _x , d _y , d _z



Relationships in Car Model

- Symbol-instance table does not show relationships between parts of model 2 collection of models
- Consider model of car
 - Chassis + 4 identical wheels
 - Two symbols



 Rate of forward motion determined by rotational speed of wheels



Structure Through Function Calls

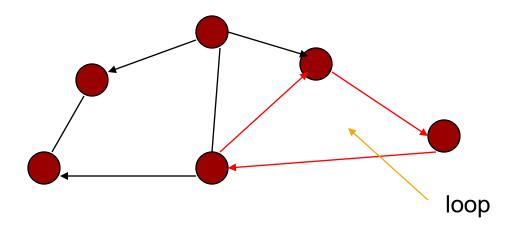
```
car(speed)
{
    chassis()
    wheel(right_front);
    wheel(left_front);
    wheel(right_rear);
    wheel(left_rear);
}
```

- Fails to show relationships well
- Look at problem using a graph



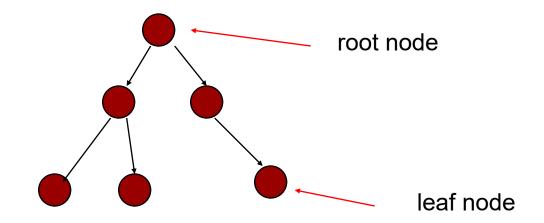
Graphs

- Set of nodes and edges (links)
- Edge connects a pair of nodes
 - Directed or undirected
- Cycle: directed path that is a loop



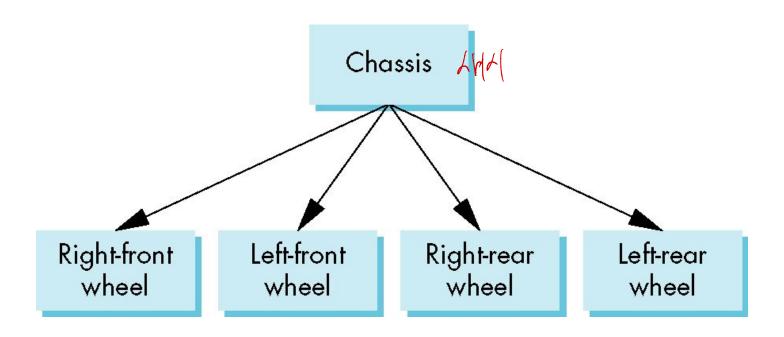


- Graph in which each node (except the root) has exactly one parent node
 - May have multiple children
 - Leaf or terminal node: no children



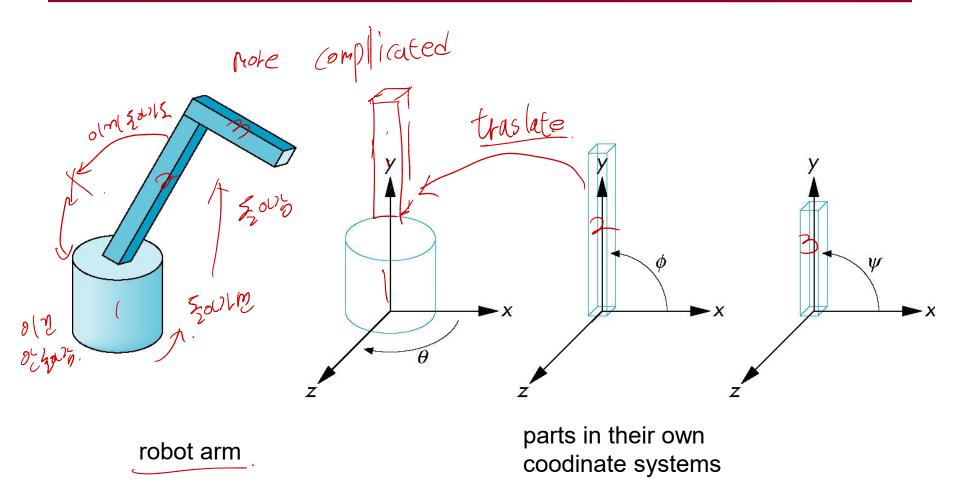


Tree Model of Car





Robot Arm





Articulated Models

Robot arm is an example of an articulated model

Parts connected at joints

- Can specify state of model by

giving all joint angles

Tipel 3/3 17
3/3/5.



Relationships in Robot Arm

- Base rotates independently
 - Single angle determines position
- Lower arm attached to base
 - Its position depends on rotation of base
 - Must also translate relative to base and rotate about connecting joint
- Upper arm attached to lower arm
 - Its position depends on both base and lower arm
 - Must translate relative to lower arm and rotate about joint connecting to lower arm



Required Matrices

- Rotation of base: \mathbf{R}_{b}
 - Apply $\mathbf{M} = \mathbf{R}_{b}$ to base
- Translate lower arm <u>relative</u> to base: Tu Height. Base.
- Rotate lower arm around joint: \mathbf{R}_{lu}
 - Apply $\mathbf{M} = \mathbf{R}_{b} \mathbf{T}_{lu} \mathbf{R}_{lu}$ to lower arm
- Translate upper arm <u>relative</u> to lower arm: T_{uu}
- Rotate upper arm around joint: \mathbf{R}_{uu}
 - Apply $\mathbf{M} = \mathbf{R}_b \mathbf{T}_{lu} \mathbf{R}_{lu} \mathbf{T}_{uu} \mathbf{R}_{uu}$ to upper arm (700 of upper arm).

OpenGL Code for Robot Arm

```
mat4 ctm;
robot arm()
    ctm = RotateY(theta);
    base();
    ctm *= Translate(0.0, h1, 0.0);
    ctm *= RotateZ(phi);
    lower arm();
    ctm *= Translate(0.0, h2, 0.0);
    ctm *= RotateZ(psi);
    upper arm();
```



Tree Model of Robot Arm

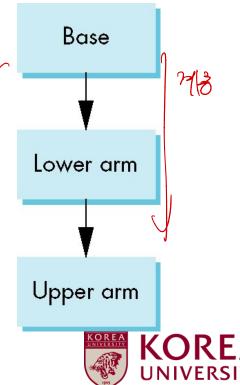
Note code shows relationships between parts of model

Can change "look" of parts easily without altering relationships

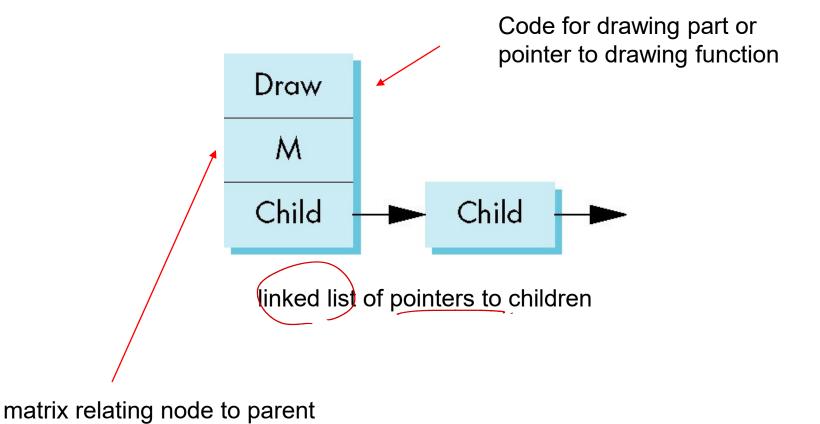
• Simple example of tree model

• Want a general node structure

for nodes



Possible Node Structure





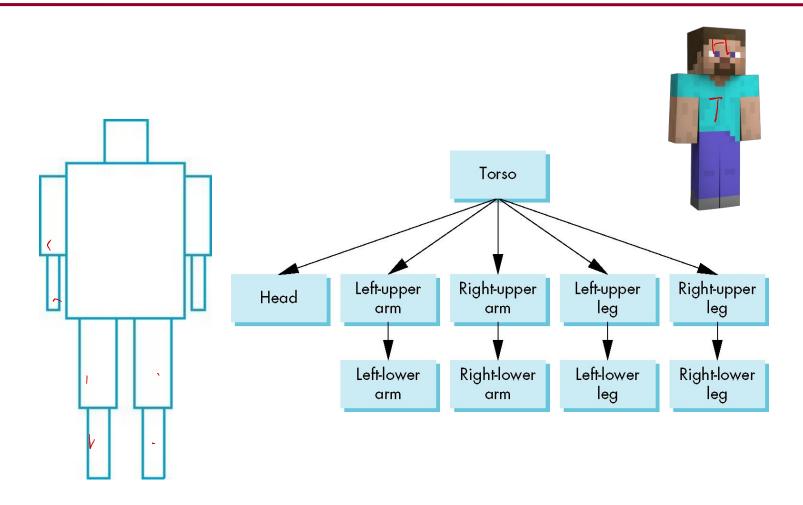
Generalizations

rot predofined

- Need to deal with multiple children
 - How do we represent a more general tree?
 - How do we traverse such a data structure?
- Animation
 - How to use dynamically?
 - Can we create and delete nodes during execution?



Humanoid Figure



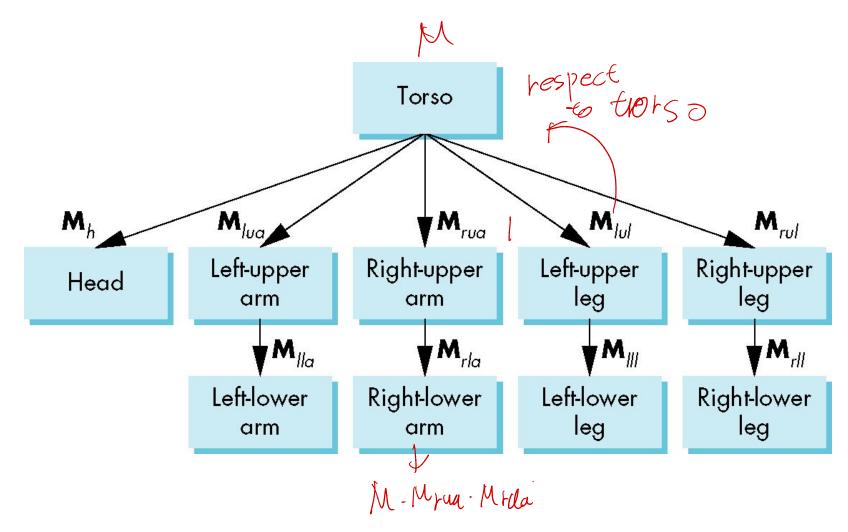


Building the Model

- Can build a simple implementation using quadrics: ellipsoids and cylinders
- Access parts through functions
 - torso()
 - -left_upper_arm()
- Matrices describe position of node <u>with respect</u>
 <u>to</u> its parent
 - $-M_{lla}$ positions left lower arm with respect to left upper arm



Tree with Matrices





Transformation Matrices

• There are 10 relevant matrices

main tors

- M positions and orients entire figure through the torso which is the root node
- $-\mathbf{M}_{h}$ positions head with respect to torso
- $-M_{lua}, M_{rua}, M_{lul}, M_{rul}$ position arms and legs with respect to torso
- $-M_{lla}, M_{rla}, M_{lll}, M_{rll}$ position lower parts of limbs with respect to corresponding upper limbs



Display and Traversal

- Display of the tree requires a graph traversal
 - Visit each node once
 - Display function at each node that describes the part associated with the node, applying the correct transformation matrix for position and orientation
- Traversal
 - Explicit traversal
 - Recursive tree traversal



Explicit Traversal

- Set model-view matrix to M and draw torso
- Set model-view matrix to \mathbf{MM}_{lua} and draw left-upper arm
- For left-lower arm need $\mathbf{M}\mathbf{M}_{lua}\mathbf{M}_{lla}$ and so on
- We can use the matrix stack to store previous matrices as we traverse the tree



Traversal Code

Ady Silve Is

```
figure() {
    PushMatrix()
                                   save present model-view matrix
    torso();
                                   update model-view matrix for head
    Rotate (...);
    head (); Head 29/04
                                    recover original model-view matrix
    PopMatrix();
    PushMatrix();
                                        save it again
    Translate(...);
                              ( Lat wing
                                       update model-view matrix
    Rotate (...);
                                       for left upper arm
    left upper arm()
    PopMatrix();
                                      recover and save original
                                      model-view matrix again
    PushMatrix();
```

rest of code



Analysis

- The code describes a particular tree and a particular traversal strategy
 - Can we develop a more general approach?
- Note that the sample code does not include state changes, such as changes to colors
 - May also want to use a PushAttrib and
 PopAttrib to protect against unexpected state changes affecting later parts of the code



General Tree Data Structure

- Need a data structure to represent tree and an algorithm to traverse the tree
- We will use a left-child right sibling structure
 - Uses linked lists

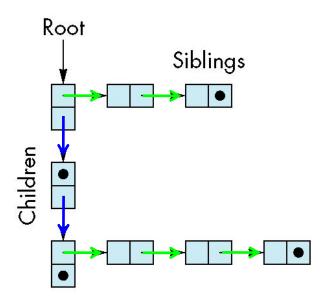
like binary tree

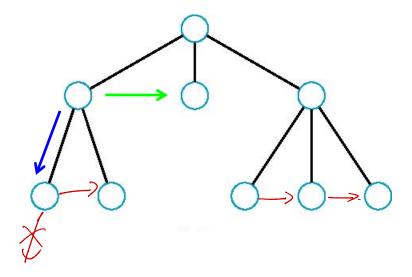
- Each node in data structure has two pointers
 - Left: next child node



Left-Child Right-Sibling Tree

• Blue: child, Green: sibling







Tree Node Structure

- At each node we need to store
 - Pointer to sibling
 - Pointer to child
 - Pointer to a function that draws the object represented by the node
 - Homogeneous coordinate matrix to multiply on the right of the current model-view matrix



Definition of treenode

```
typedef struct treenode
   mat4 m;
   void (*f) (); Junction pointer.
   struct treenode *sibling;
   struct treenode *child;
} treenode;
```



Example: torso and head nodes

```
treenode torso node, head node, lua node, ...;
torso node.m = RotateY(theta[0]);
torso node.f = torso;
torso node.sibling = NULL;
torso node.child = &head node;
        ナツラ、の場かいまりからり
head node.m = translate(0.0,
  TORSO HEIGHT+0.5*HEAD HEIGHT,
  0.0) * \overline{R}otateX (theta[1]) * RotateY (theta[2]);
head node.f = head;
head node.sibling = &lua node;
head node.child = NULL;
```



Notes

- The position of figure is determined by II joint angles stored in theta[11] AZ MAN ONUMBER
- Animate by changing the angles and redisplaying
- We form the required per-node matrix using Rotate and Translate
 - Because the matrix is formed using the modelview matrix, we may want to first push original model-view matrix on matrix stack



Recursive Traversal (Preorder)

```
Dreotder traversal.
void traverse(treenode* node)
   if (node==NULL) return;
   mvstack.push (model_view); Cutterf & Cate
   model_view = model_view*node->m; & apply whatever node->f();) in H & They &
   node->f();) 한거 또 경영은
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop(); -) return to current state forgot.
   if(node->sibling!=NULL) traverse(node->sibling);
                                                MBX
```

1. Depth first traversal

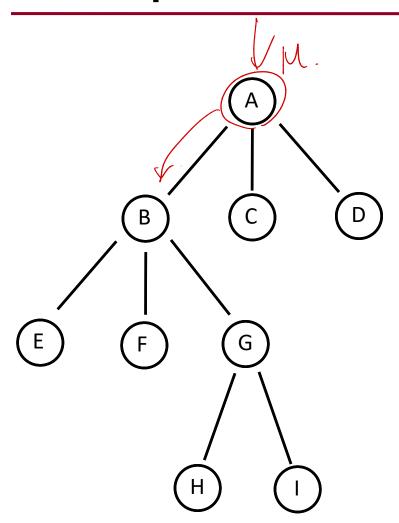
2. Sibling's transformation only depends on its parent)

Child 2012 14307 33540101-34

Childrenon/

अहर छन्थेरत.





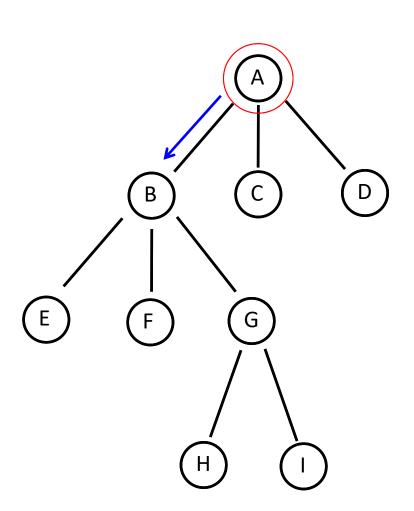
```
void traverse(treenode* node)
{
   if(node==NULL) return;
   mvstack.push(model_view);
   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}
```

Current Matrix: I (Identity)

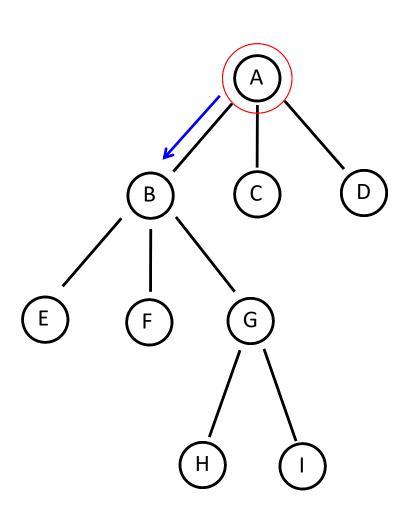
Matrix Stack:









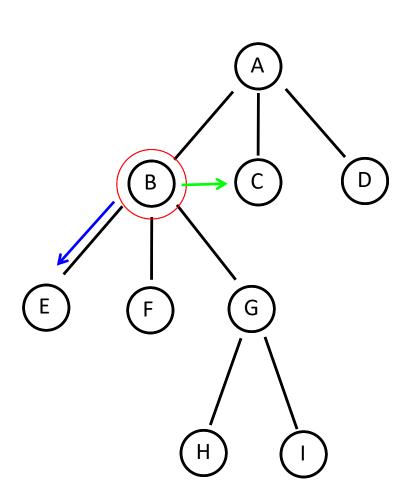


```
void traverse(treenode* node)
{
   if(node==NULL) return;
   mvstack.push(model_view);
   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}
```

Current Matrix: A

Matrix Stack: I



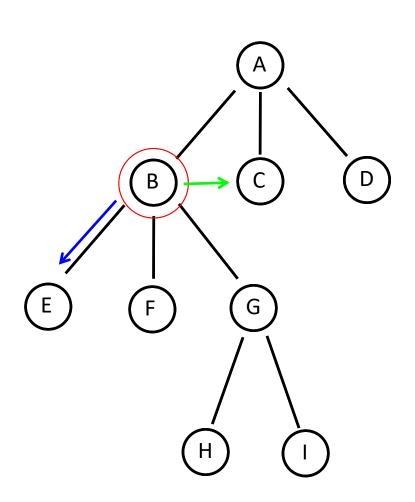


```
void traverse(treenode* node)
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   if(node==NULL) return;
   mvstack.push(model_view);
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   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}
```

Current Matrix: A

Matrix Stack: I, A

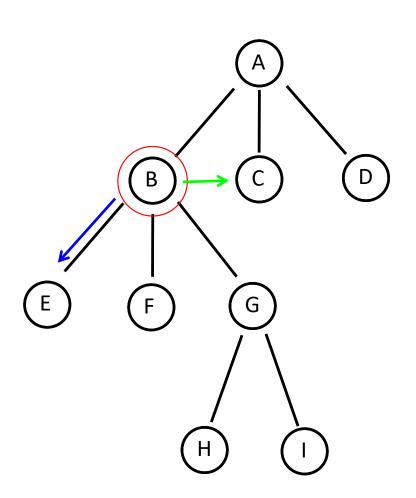




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   if(node->sibling!=NULL) traverse(node->sibling);
}
```

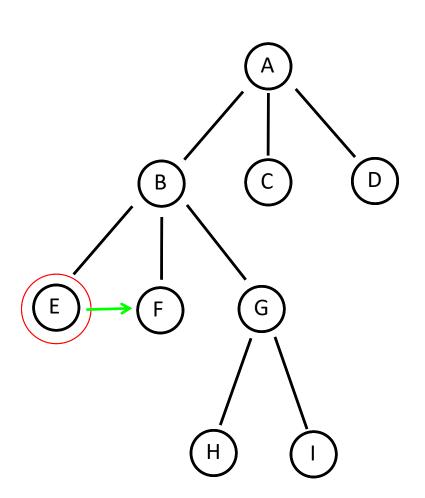
Current Matrix: AB





```
void traverse(treenode* node)
   if(node==NULL) return;
  mvstack.push(model view);
   model view = model view*node->m;
   node->f();
   if (node->child!=NULL) traverse (node->child);
   model view = mvstack.pop();
   if (node->sibling!=NULL) traverse (node->sibling);
         Current Matrix: AB
         Matrix Stack: I, A
                          Top.
```

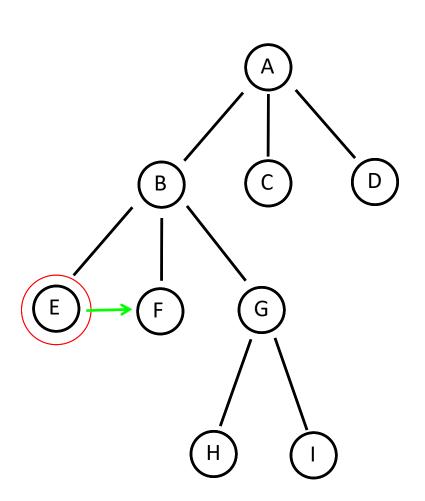




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   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}

Current Matrix: AB
```

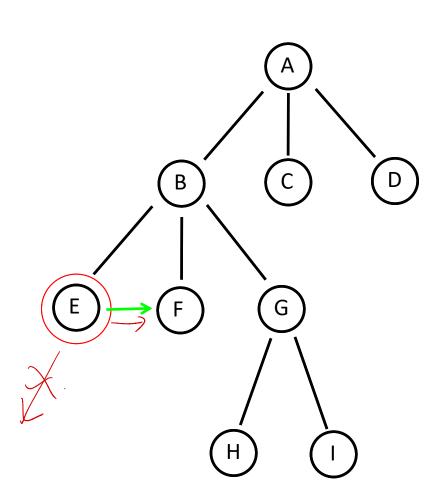




```
void traverse(treenode* node)
{
   if(node==NULL) return;
   mvstack.push(model_view);
   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}
```

Current Matrix: ABE

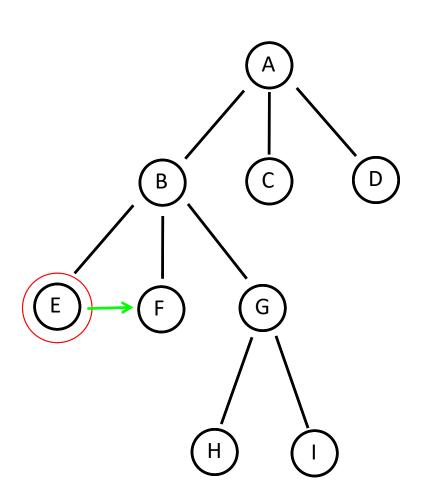




```
void traverse(treenode* node)
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   if(node==NULL) return;
   mvstack.push(model_view);
   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}

Current Matrix: ABE
```

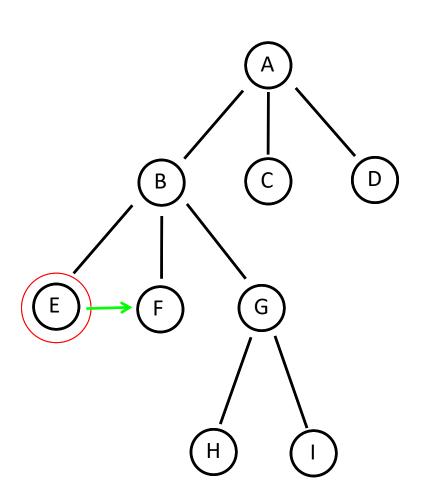




```
void traverse(treenode* node)
{
   if(node==NULL) return;
   mvstack.push(model_view);
   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}
```

Current Matrix: AB

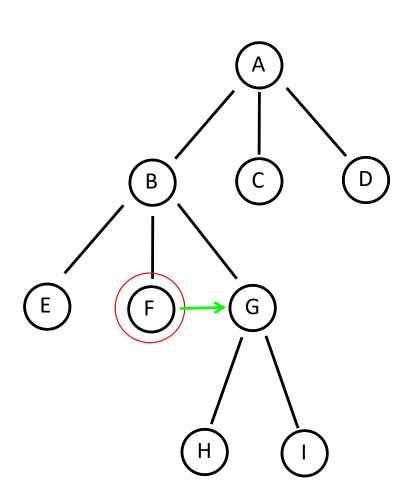




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}
```

Current Matrix: AB

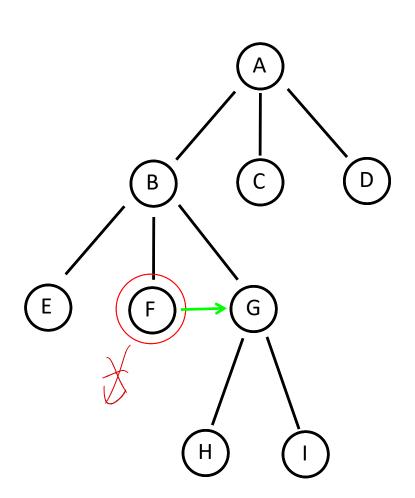




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   node->f();
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   if(node->sibling!=NULL) traverse(node->sibling);
}
```

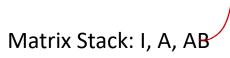
Current Matrix: AB



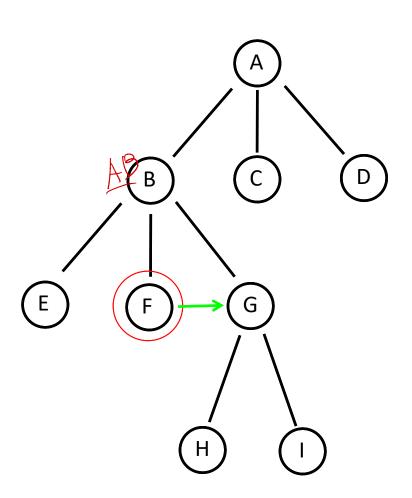


```
void traverse(treenode* node)
{
   if(node==NULL) return;
   mvstack.push(model_view);
   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}

Current Matrix(ABF)
```



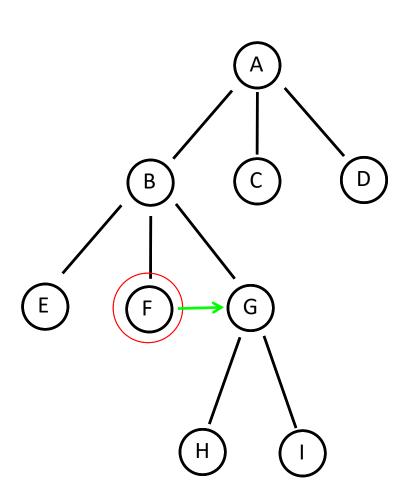




```
void traverse(treenode* node)
{
   if(node==NULL) return;
   mvstack.push(model_view);
   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}
```

Current Matrix AB

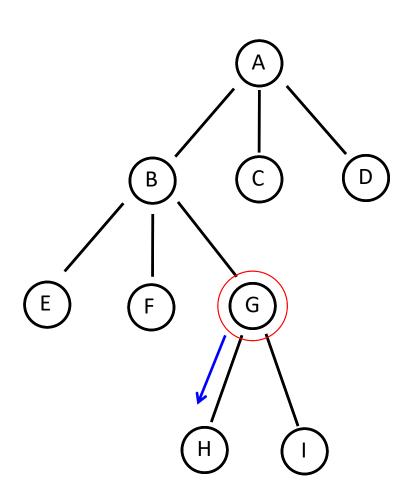




```
void traverse(treenode* node)
{
   if(node==NULL) return;
   mvstack.push(model_view);
   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
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```

Current Matrix: AB

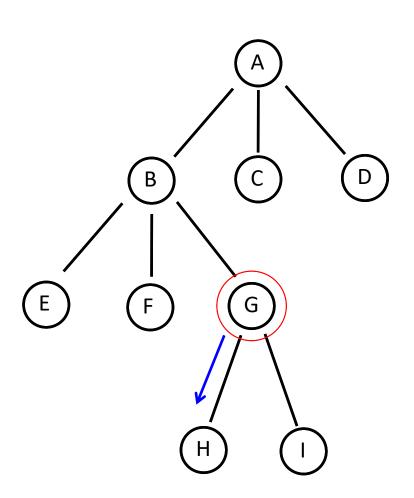




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   mvstack.push(model_view);
   model_view = model_view*node->m;
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}
```

Current Matrix: AB

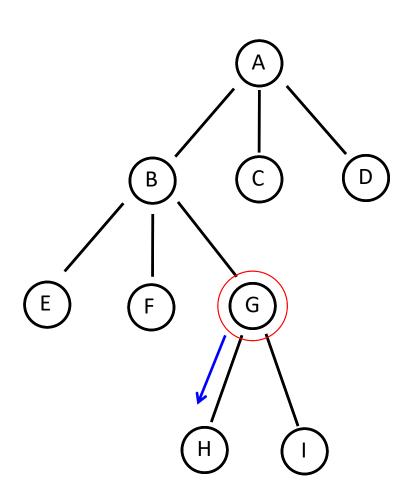




```
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   mvstack.push(model_view);
   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}
```

Current Matrix: ABG

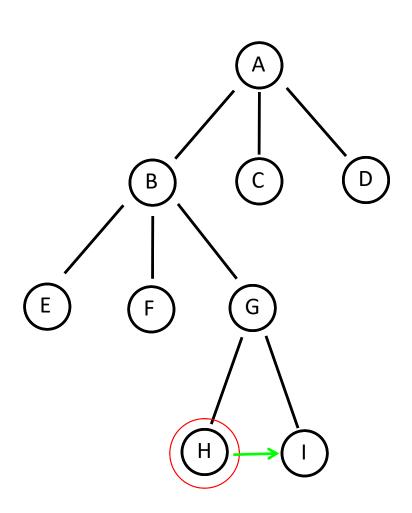




```
void traverse(treenode* node)
{
   if(node==NULL) return;
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   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}
```

Current Matrix: ABG



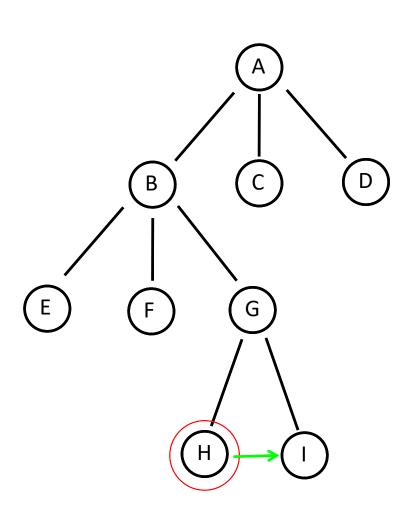


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   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}
```

Current Matrix: ABG

Matrix Stack: I, A, AB, ABG





```
void traverse(treenode* node)
{
   if(node==NULL) return;
   mvstack.push(model_view);
   model_view = model_view*node->m;
   node->f();
   if(node->child!=NULL) traverse(node->child);
   model_view = mvstack.pop();
   if(node->sibling!=NULL) traverse(node->sibling);
}
```

Current Matrix: ABGH

Matrix Stack: I, A, AB, ABG



Note

- Current matrix must be stored in a stack before updated by current node's matrix
- Current matrix is concatenation of parent node's matrices with mine
- Current matrix is only applied to children, not siblings
- We can push/pop attributes as well

Color rems 2021 x6.

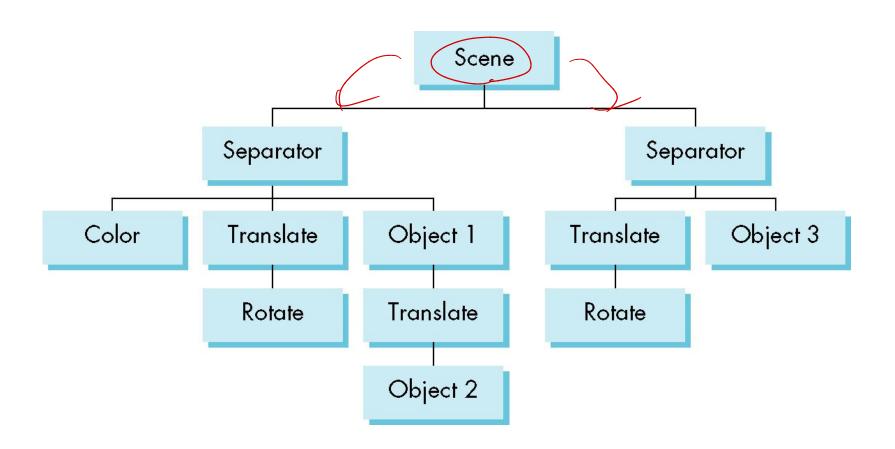


General Scene Descriptions

- In Humanoid figure model, we saw that
 - We could describe model either by tree or by equivalent code
 - We could write a generic traversal to display
- If we can represent all the elements of a scene (cameras, lights, materials, geometry) as nodes, we should be able to show them in a tree
 - Render scene by traversing this tree



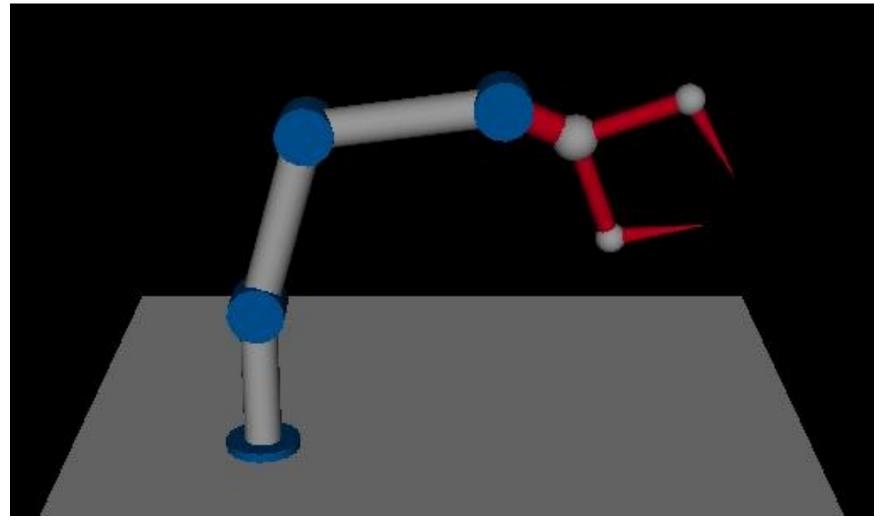
Scene Graph





Questions?







Questions?

