

Lecture 23: Volume Rendering II

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Outline

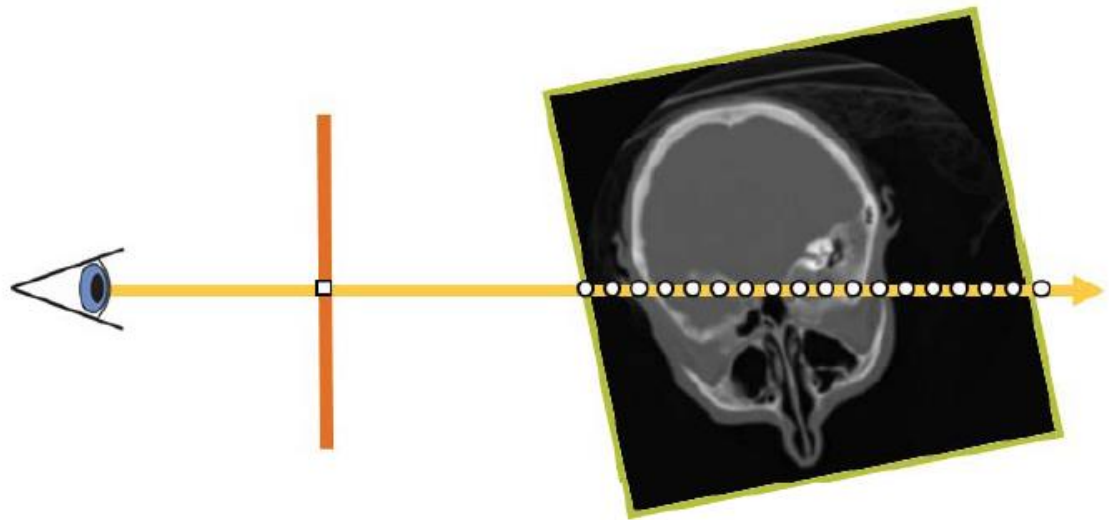
- Rendering methods
- Classification & transfer function
- Pre-integrated & isosurface volume rendering



Ray Casting Process

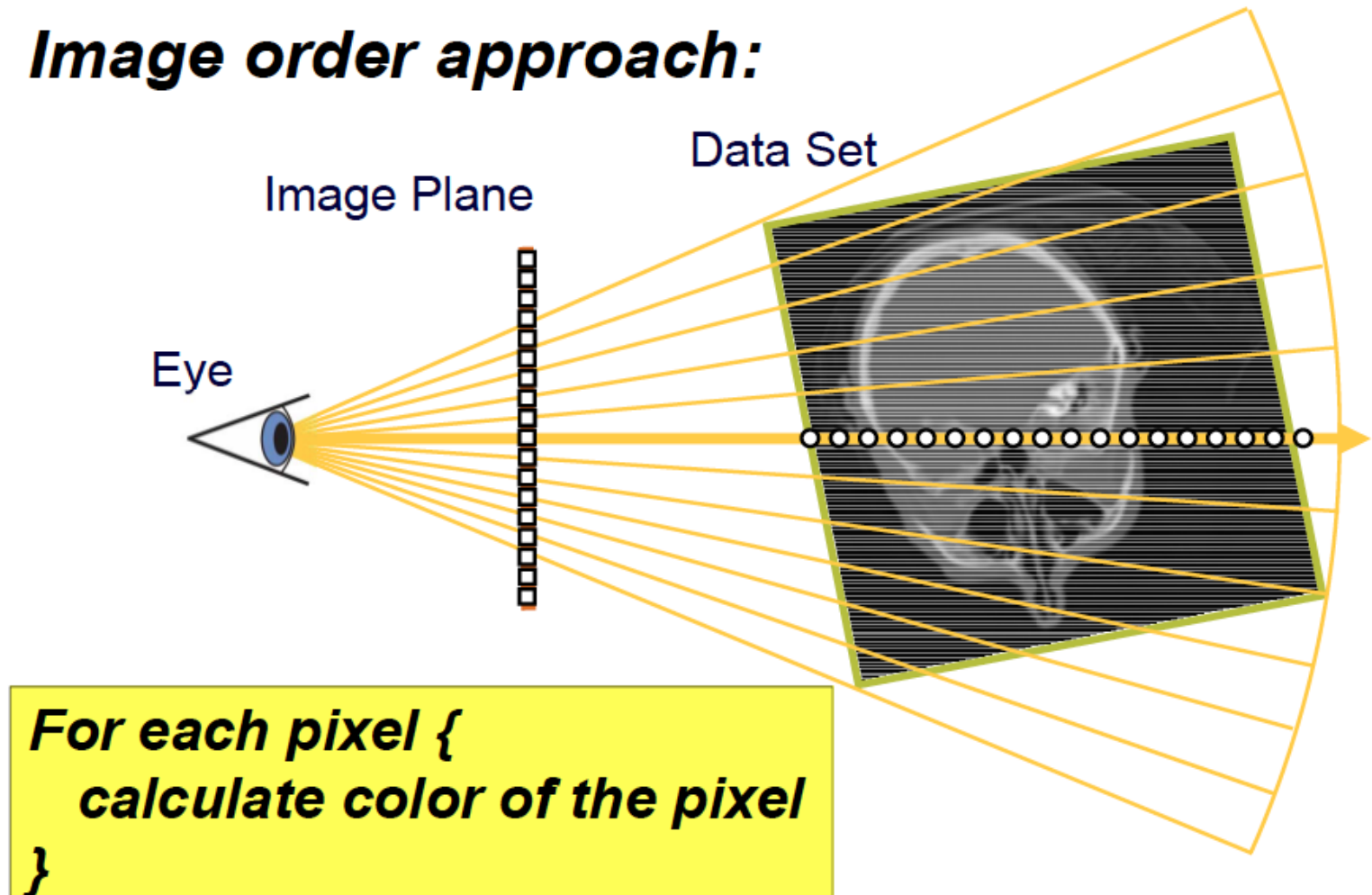
- Ray setup
- For every ray
 - Resample scalar value
 - Classification
 - Shading
 - Compositing

iterative sampling



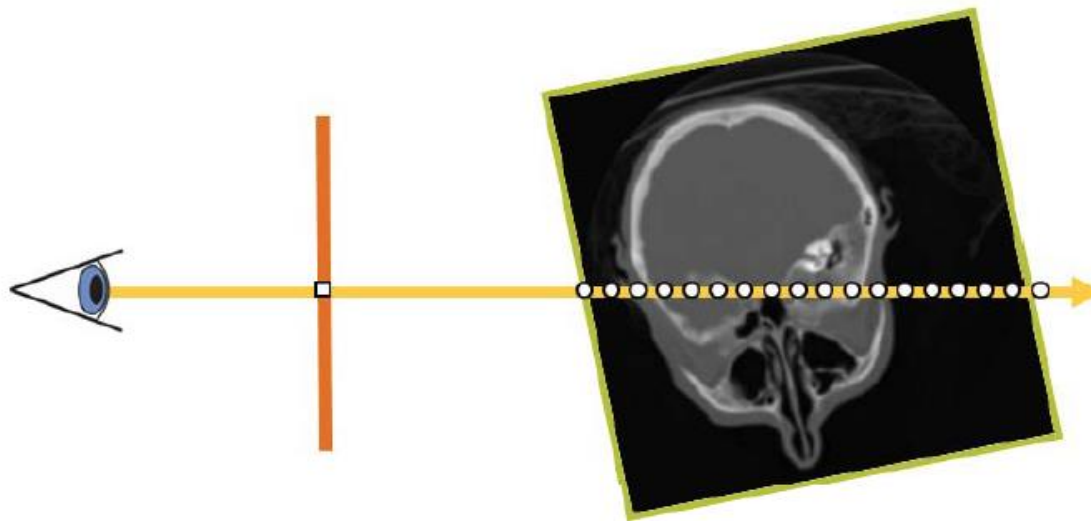
Volume Rendering

Image order approach:



Ray Setup

- Two approaches
 - Procedural ray/box intersection
 - Rasterize bounding box

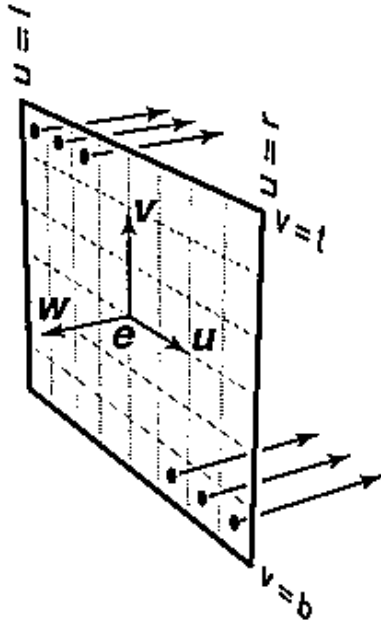


Procedural Ray Setup/Termination

- Fragment shader / CUDA kernel computes ray equation and bounding box intersection per pixel
 - Ray is defined by camera position and pixel location
- Pro : simple and self-contained
- Con : full computational load per pixel/fragment



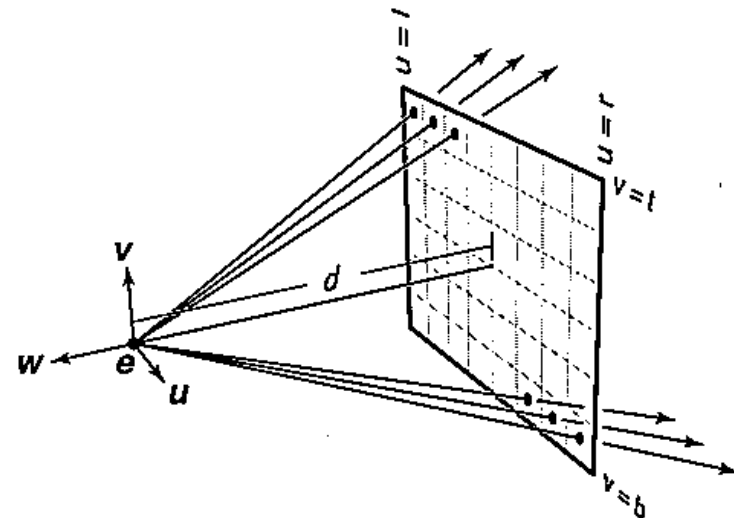
Procedural Ray Setup/Termination



Orthogonal view

Ray direction : $-\mathbf{w}$

Ray origin : $\mathbf{e} + u\mathbf{u} + v\mathbf{v}$



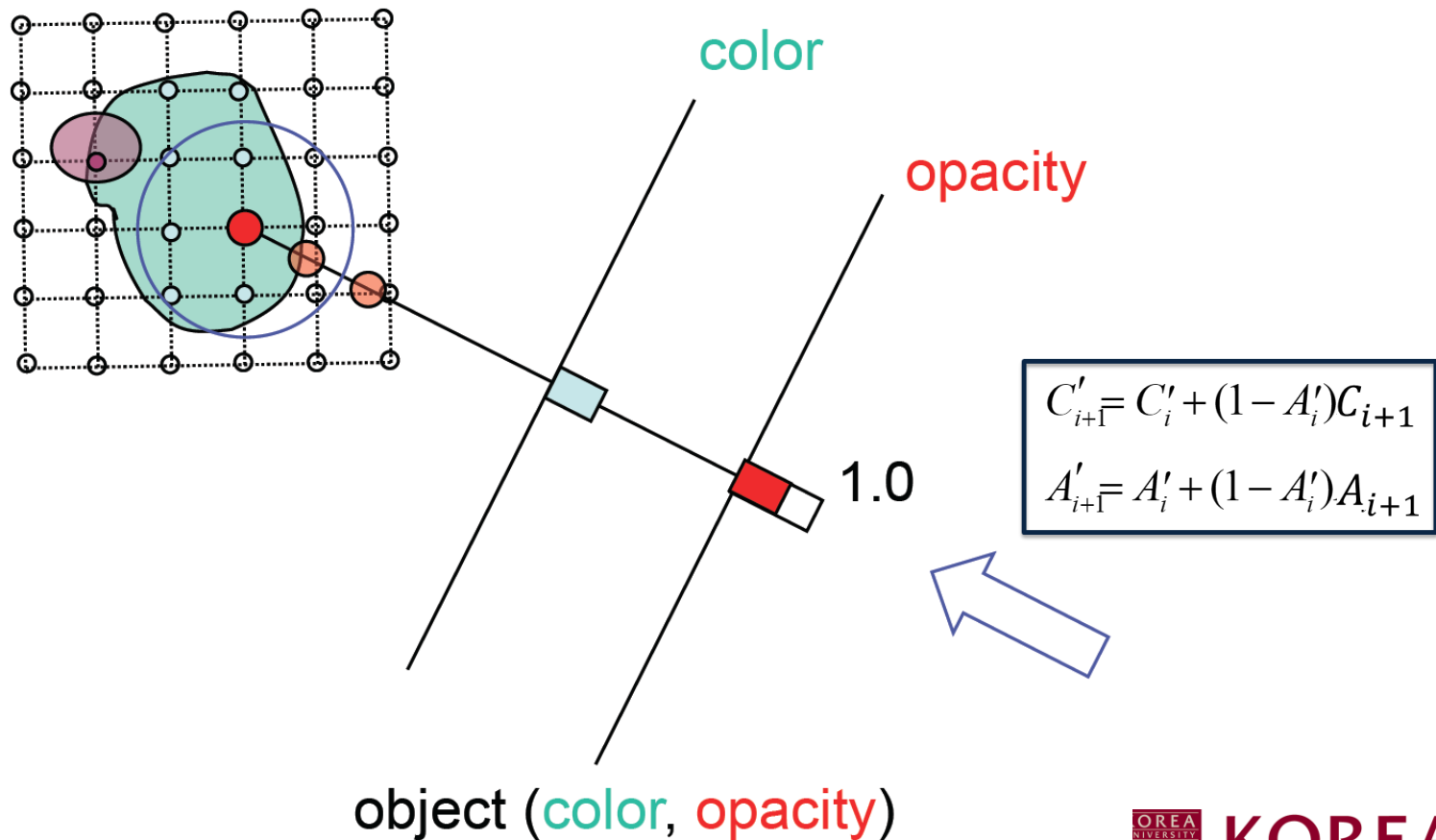
Perspective view

Ray direction : $-d\mathbf{w} + u\mathbf{u} + v\mathbf{v}$

Ray origin : \mathbf{e}

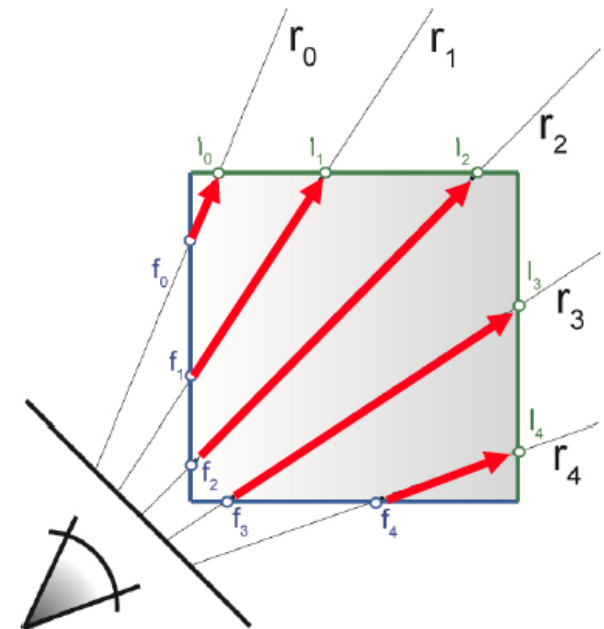
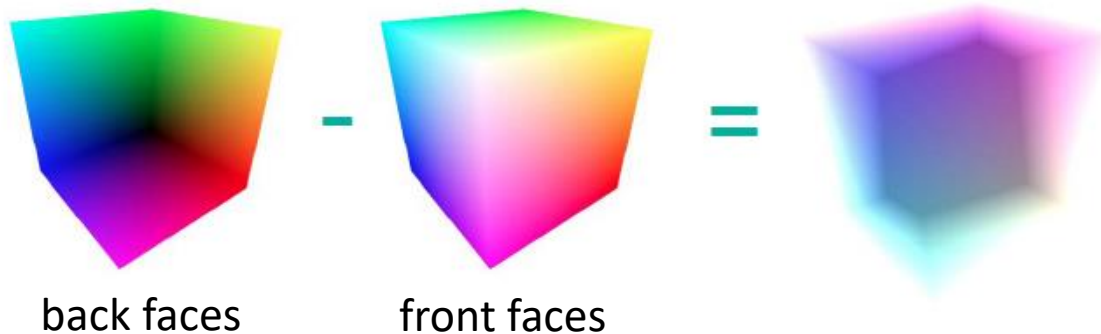
Procedural Ray Setup/Termination

- Trilinear interpolation, front-to-back



Rasterization-Based Ray Setup

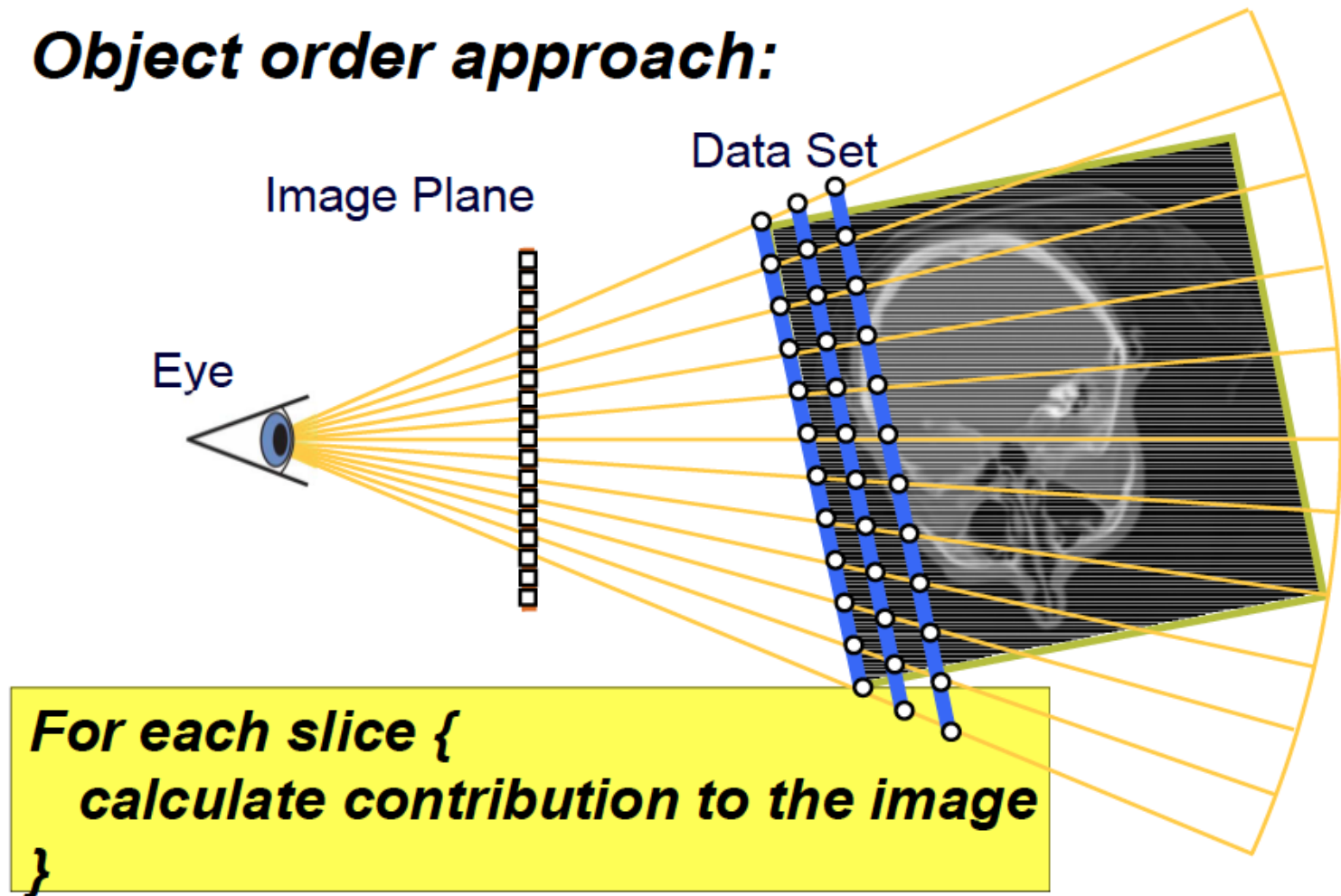
- Rasterize bounding box
 - Fragment == ray
 - Render front / back faces separately
 - Rasterization gives location
 - Subtraction gives direction



Identical for orthogonal & perspective projection!

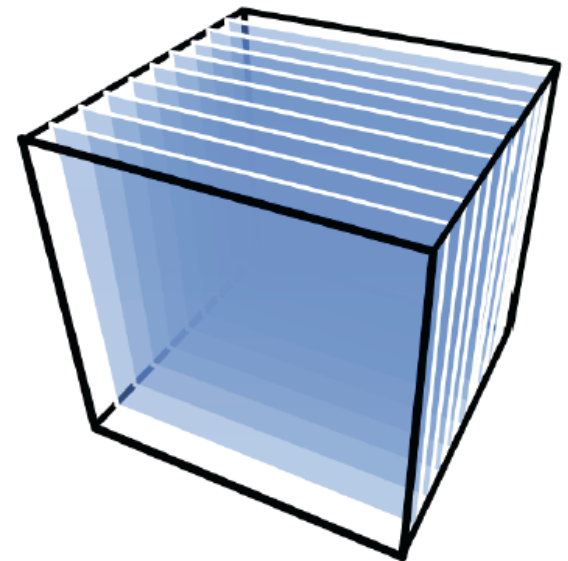
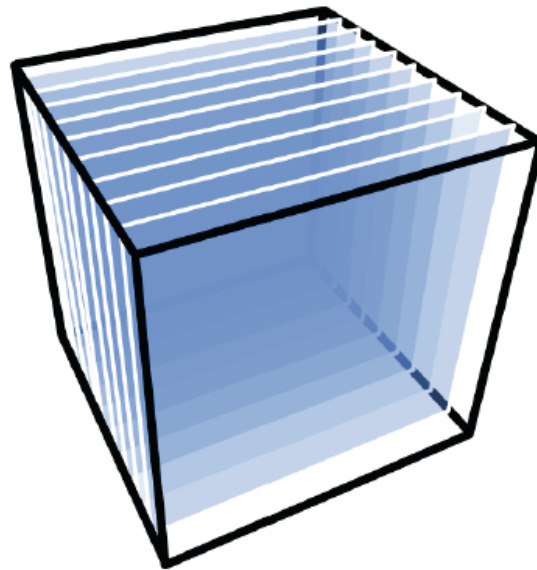
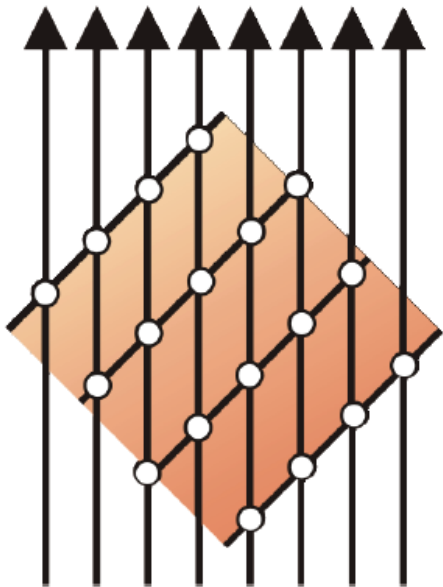
Volume Rendering

Object order approach:



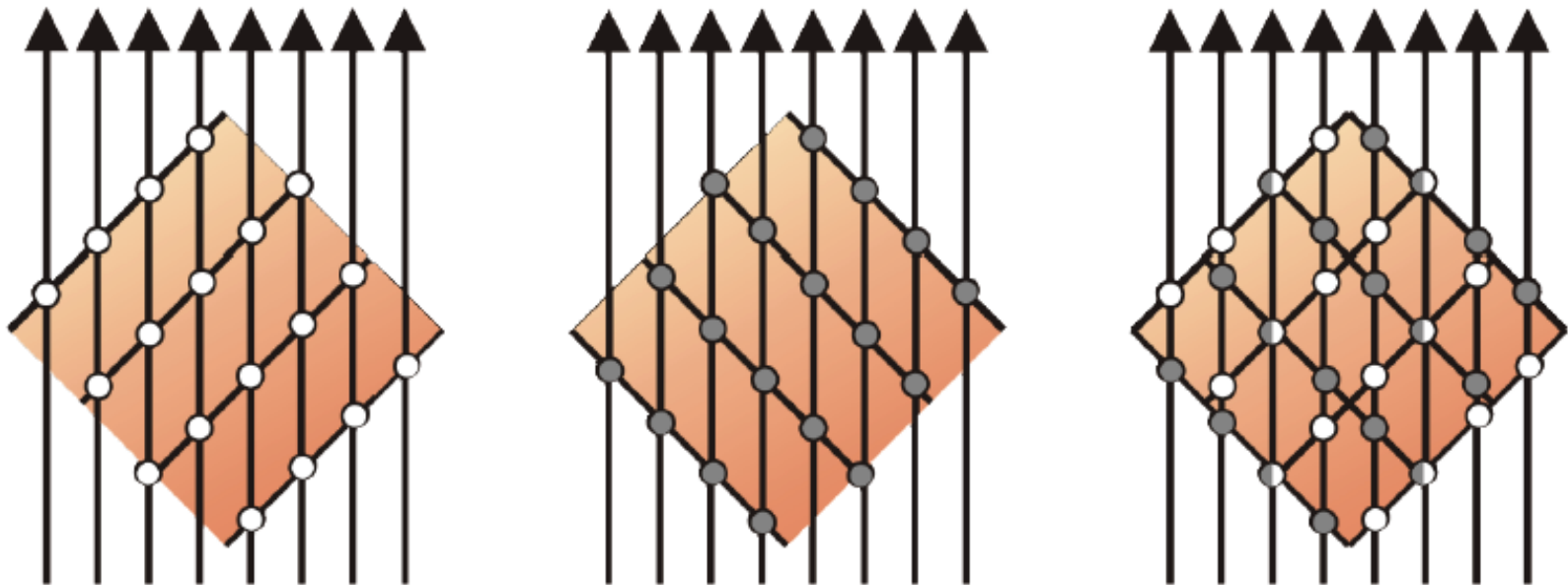
2D Texture Slices

- Object-aligned slices, back-to-front
- Three stacks of 2D textures (x - y , y - z , z - x)
- Bilinear interpolation



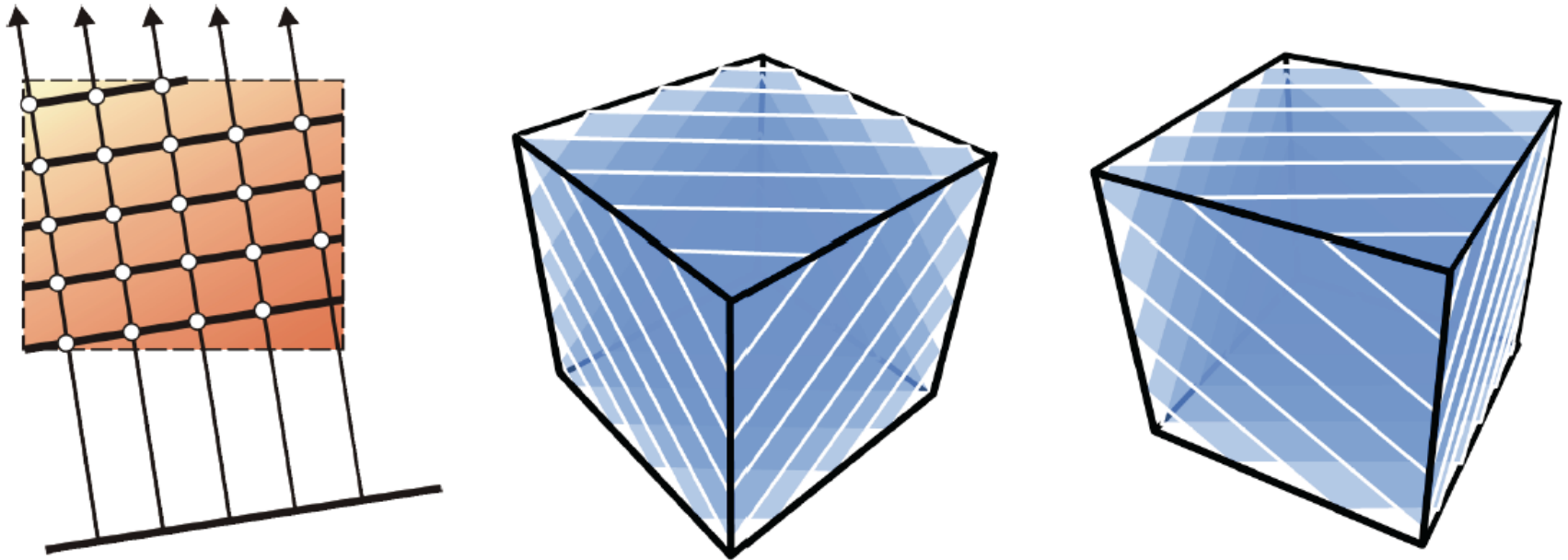
2D Texture Slices

- Artifacts when stack is viewed close to 45 degrees
 - Location of sampling points may change abruptly



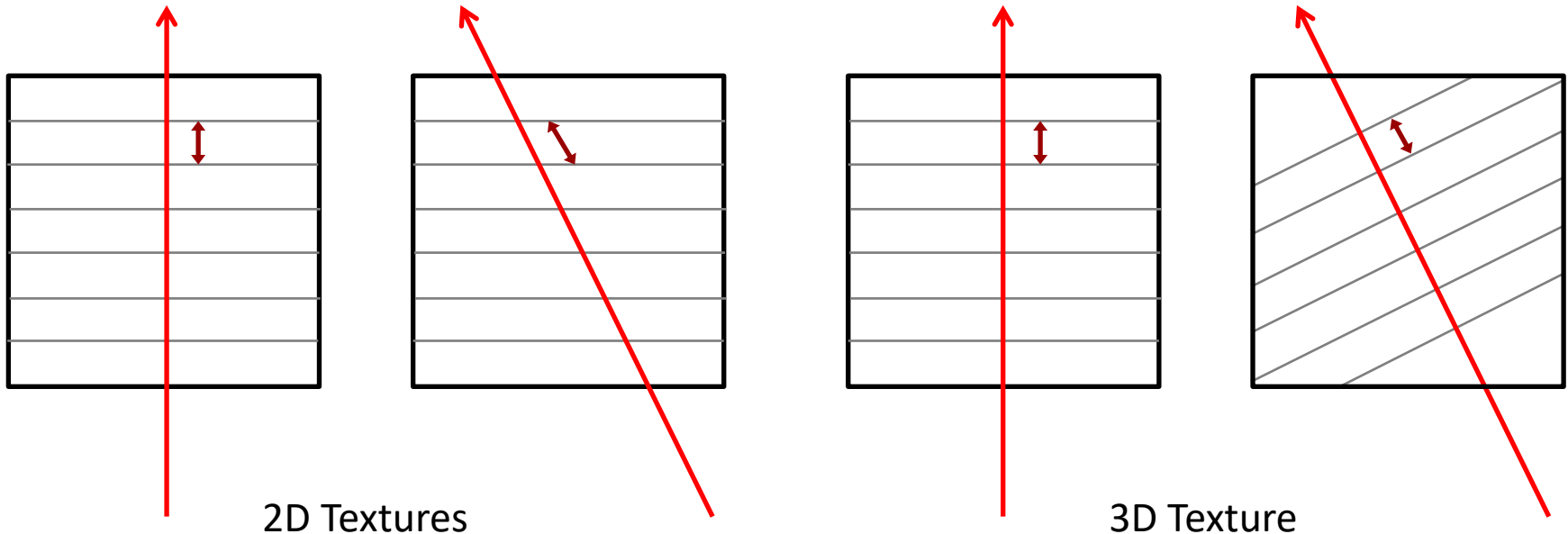
3D Textures

- View-aligned slices, back-to-front
- Single 3D texture
- Trilinear interpolation = better image quality



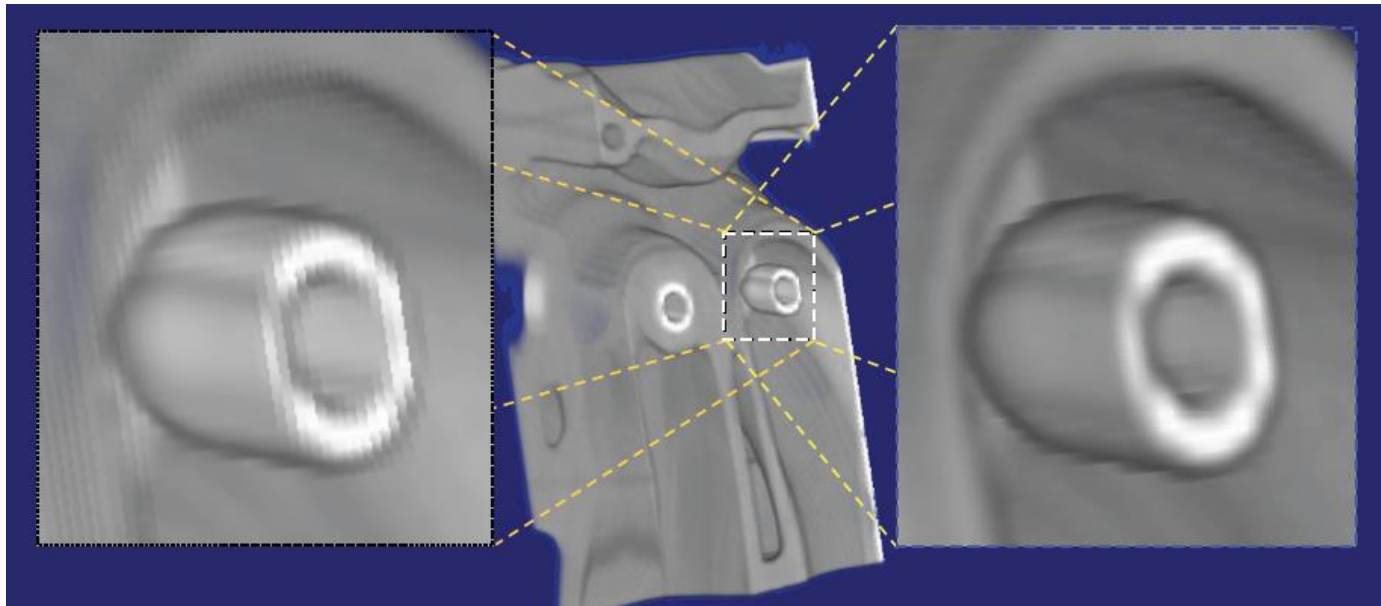
3D Textures

- Constant Euclidean distance between slices along a ray when view direction is changed



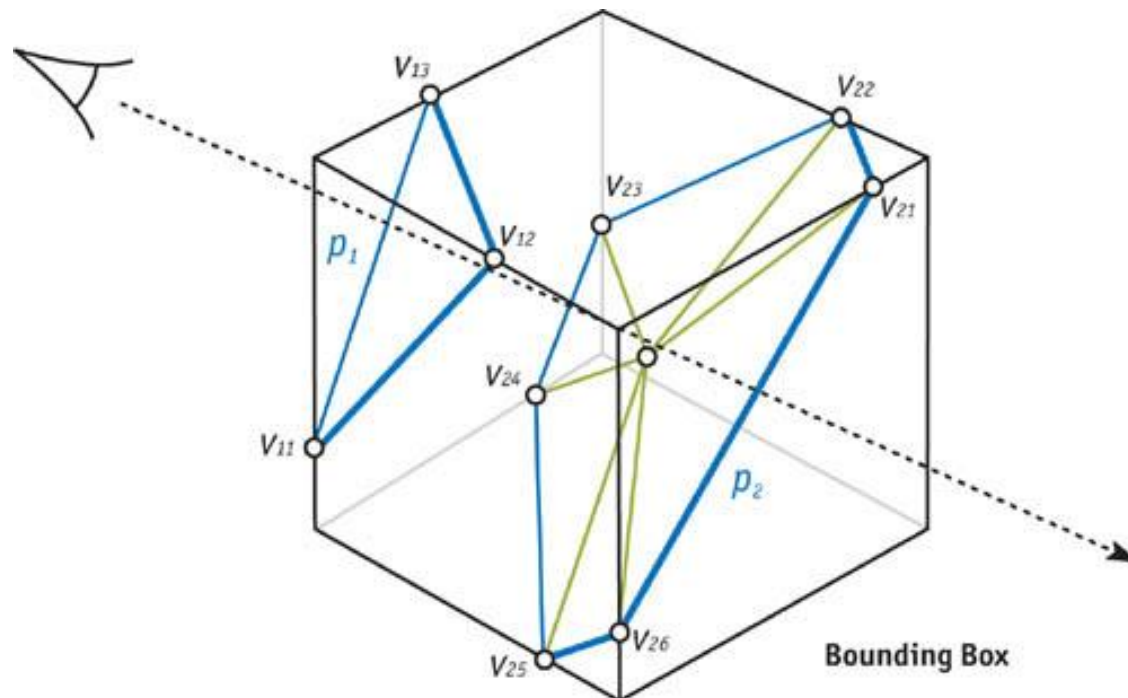
3D Texture

- No artifacts due to inappropriate viewing angles
- Increasing sampling rate is easy with 3D tex.
 - Use more slices

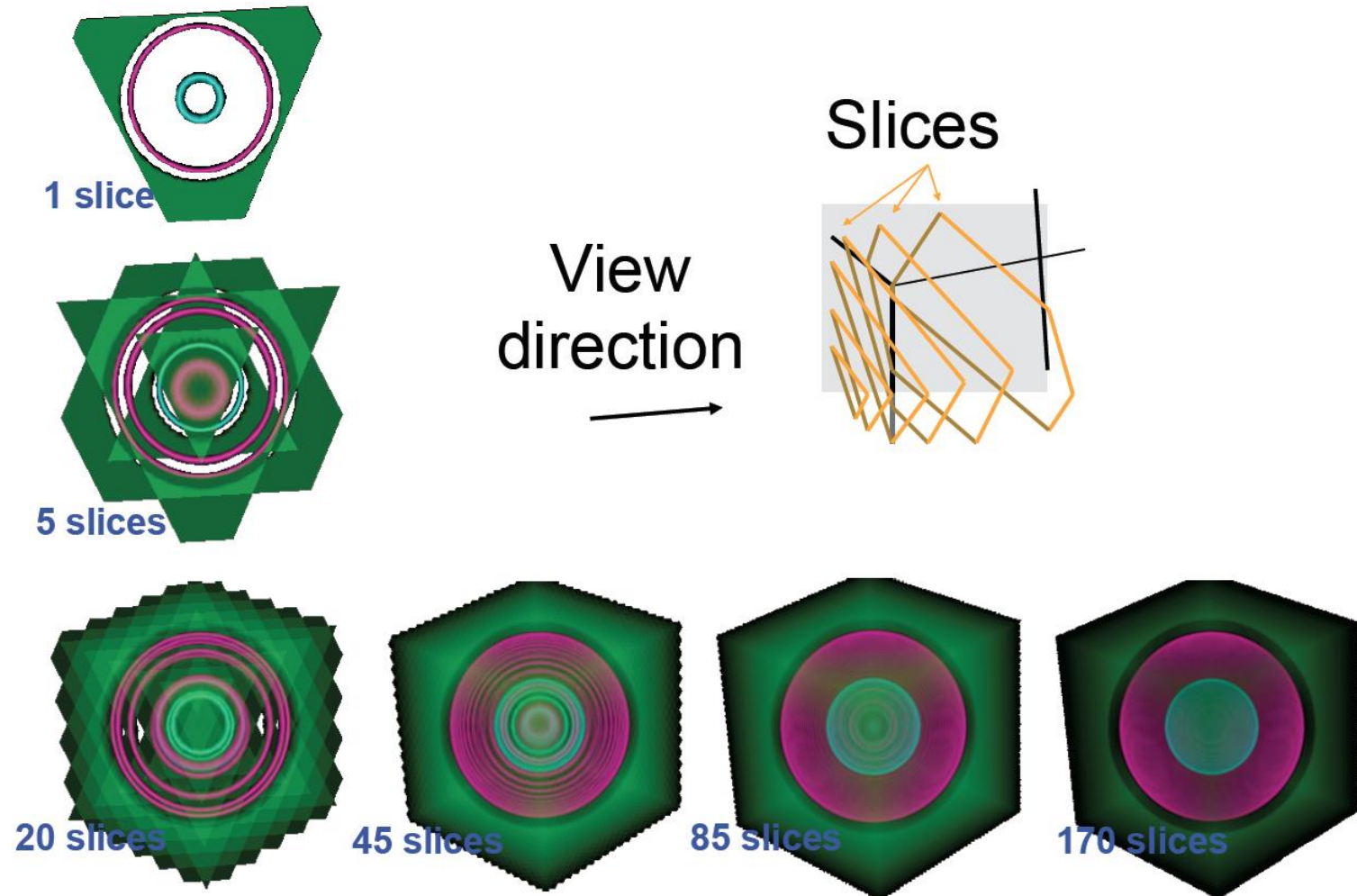


Proxy Geometry

- Plane-bbox intersection & tessellation with center point



Rendering Quality



Classification

- User defines look of the data by
 - Change per-voxel color and transparency
 - How? : **transfer function**



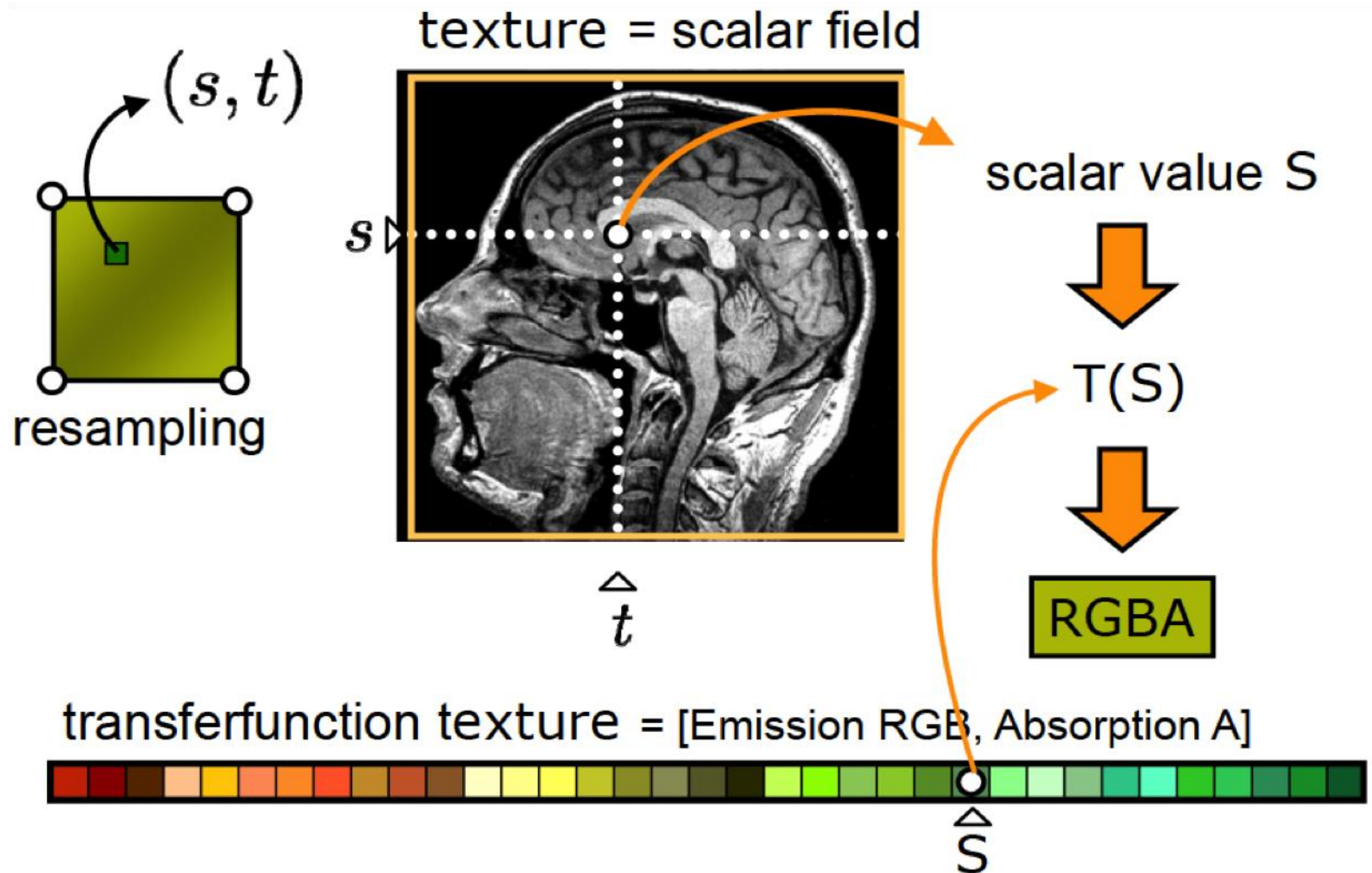
Transfer Function

- Input volume contains only scalar value
- Transfer function T maps scalar to vector
 - (R,G,B) : color or emission
 - A : absorption

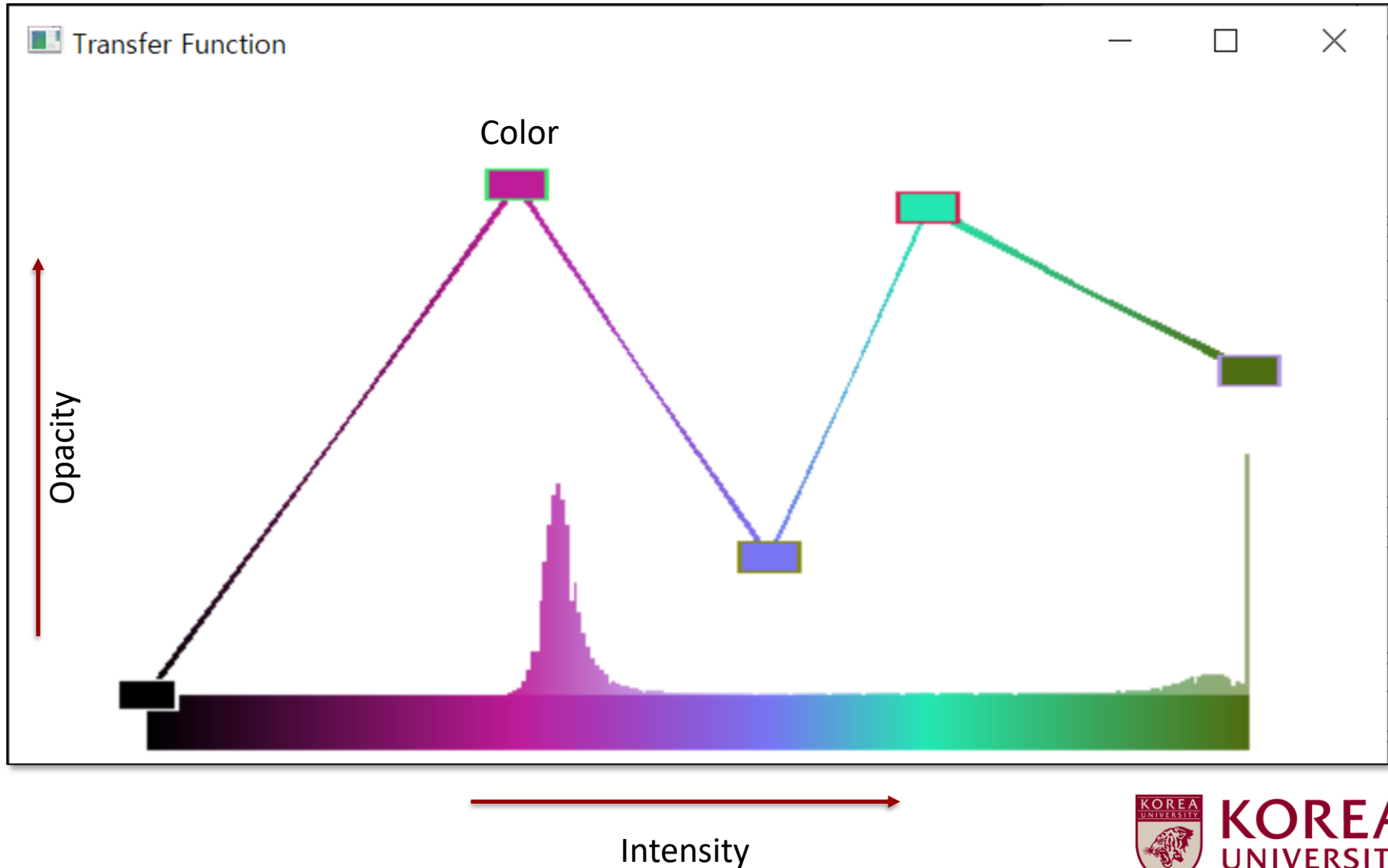
$$T(S) = (R, G, B, A)$$



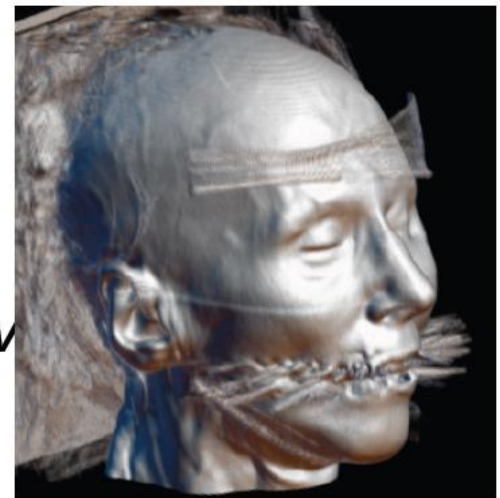
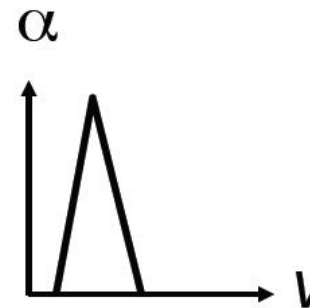
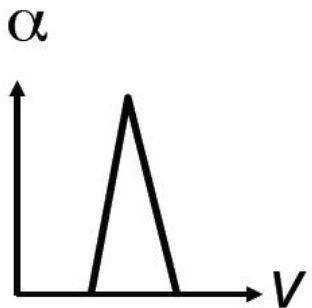
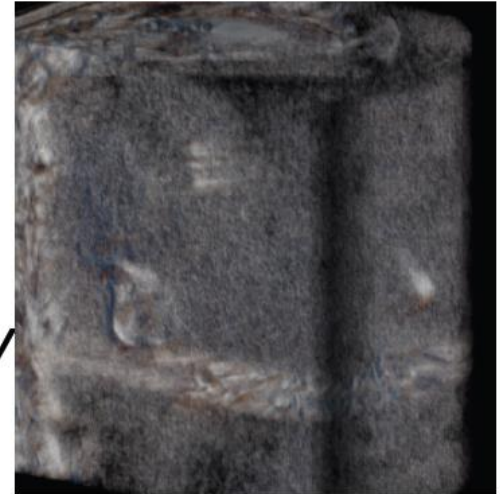
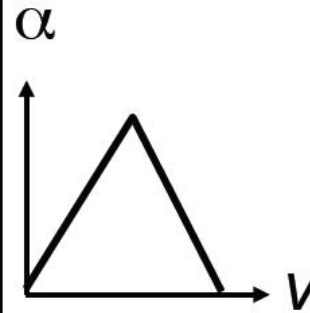
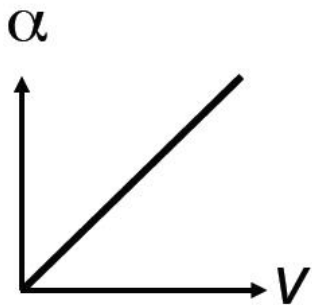
Transfer Function Application



1D Transfer Function Example

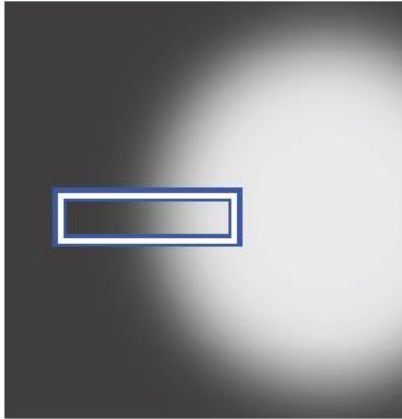


Setting Transfer Function is Hard!

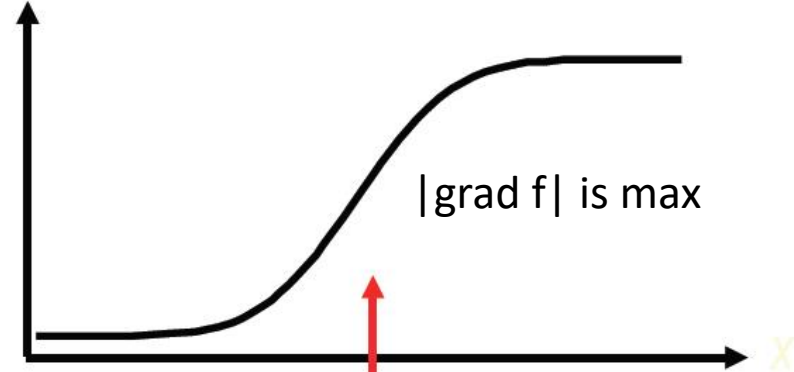


Finding Edges

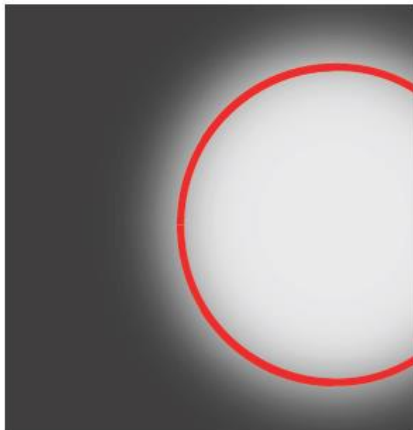
“Where’s the edge?”



$$v = f(x)$$



“ here’s the edge ”

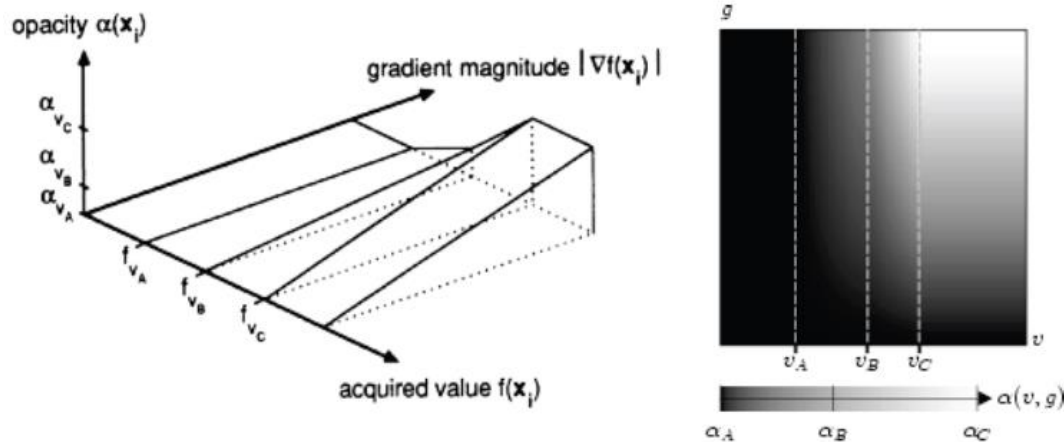
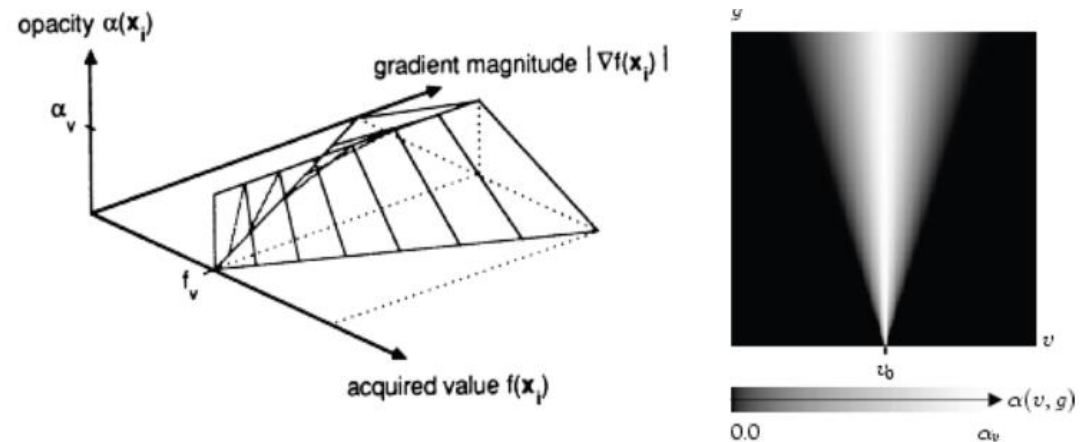


Result: edge pixels



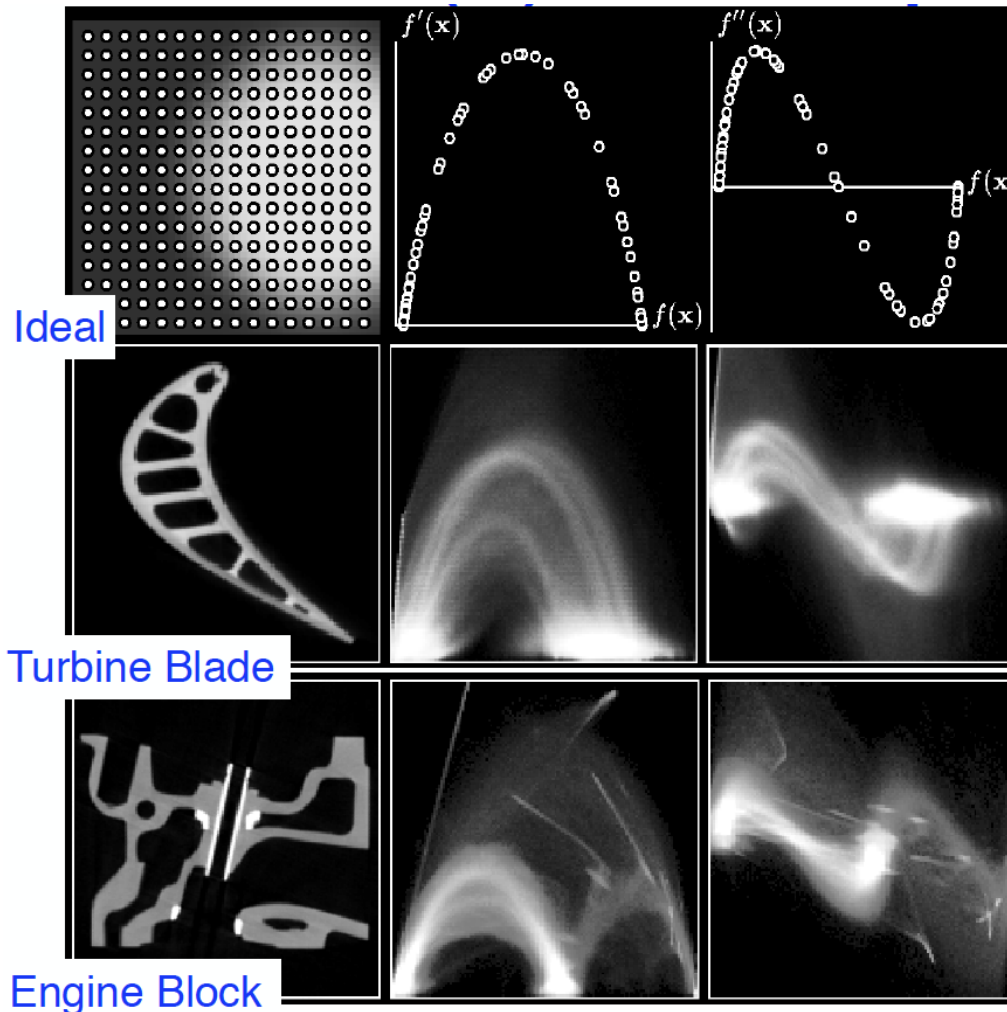
2D Transfer Function

- Assign opacity from data value and $|\text{grad } f|$

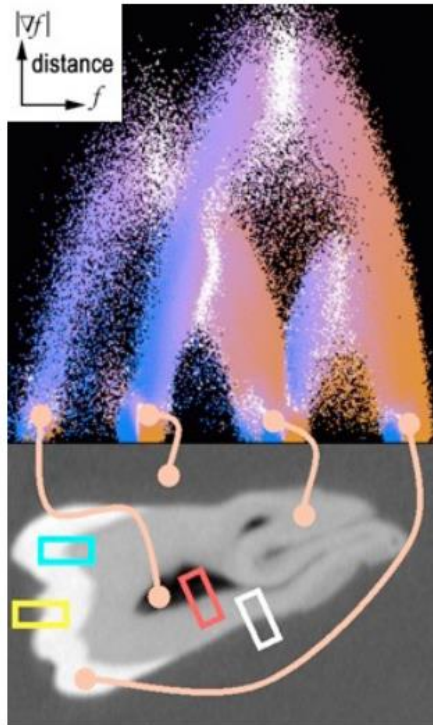


2D Scatter Plot

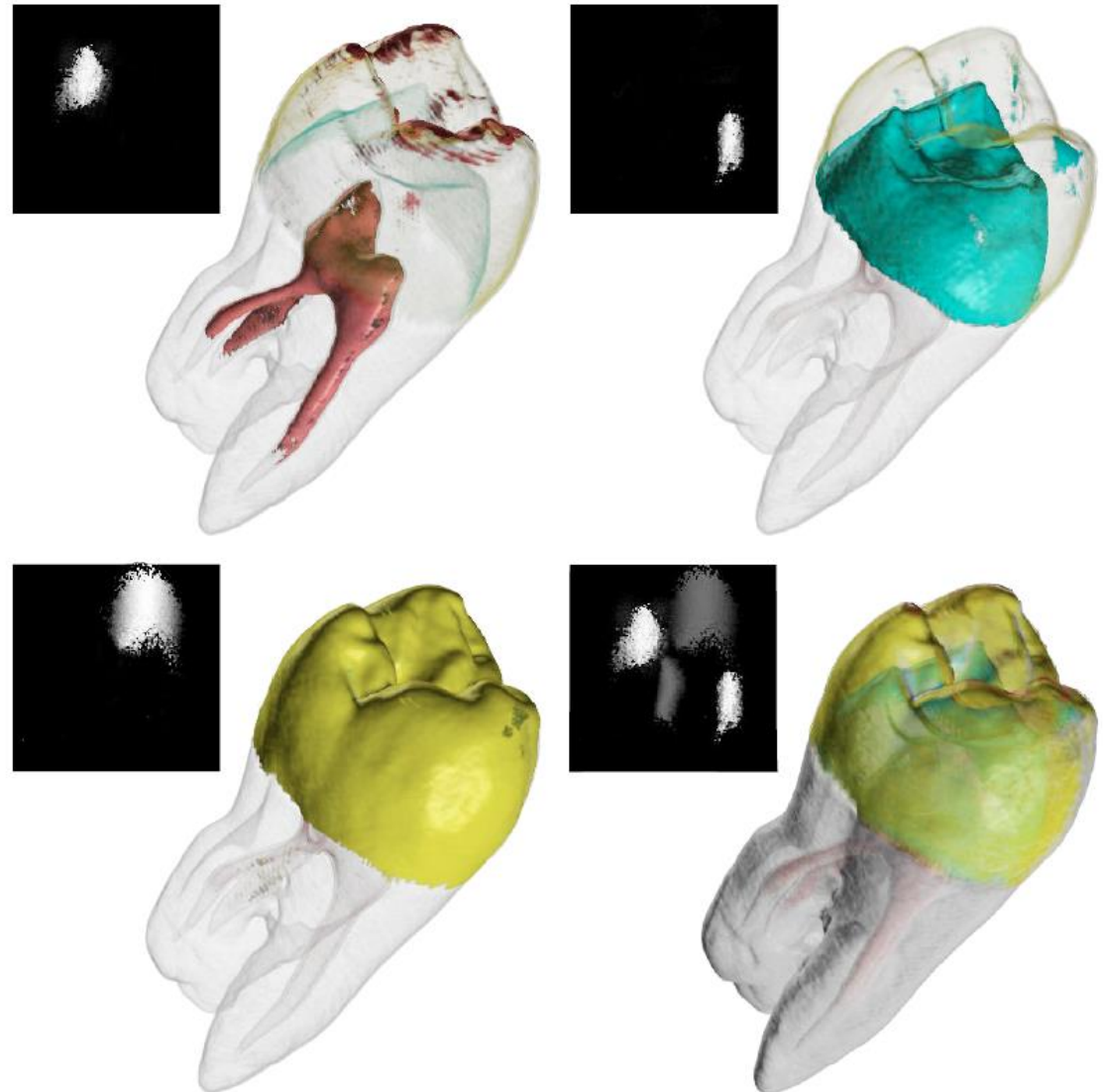
- Project histogram volume to 2D scatterplots



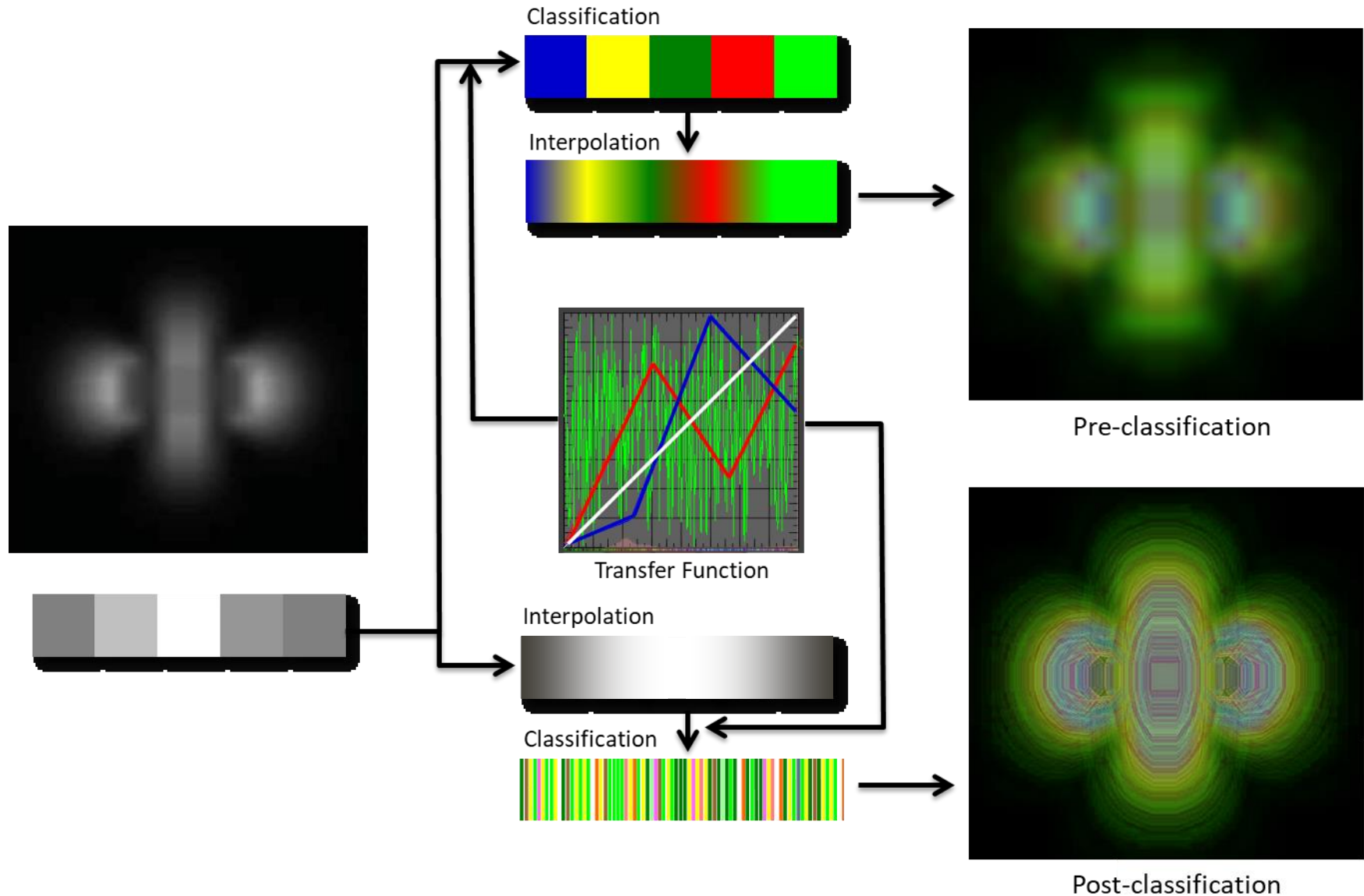
2D Transfer Function



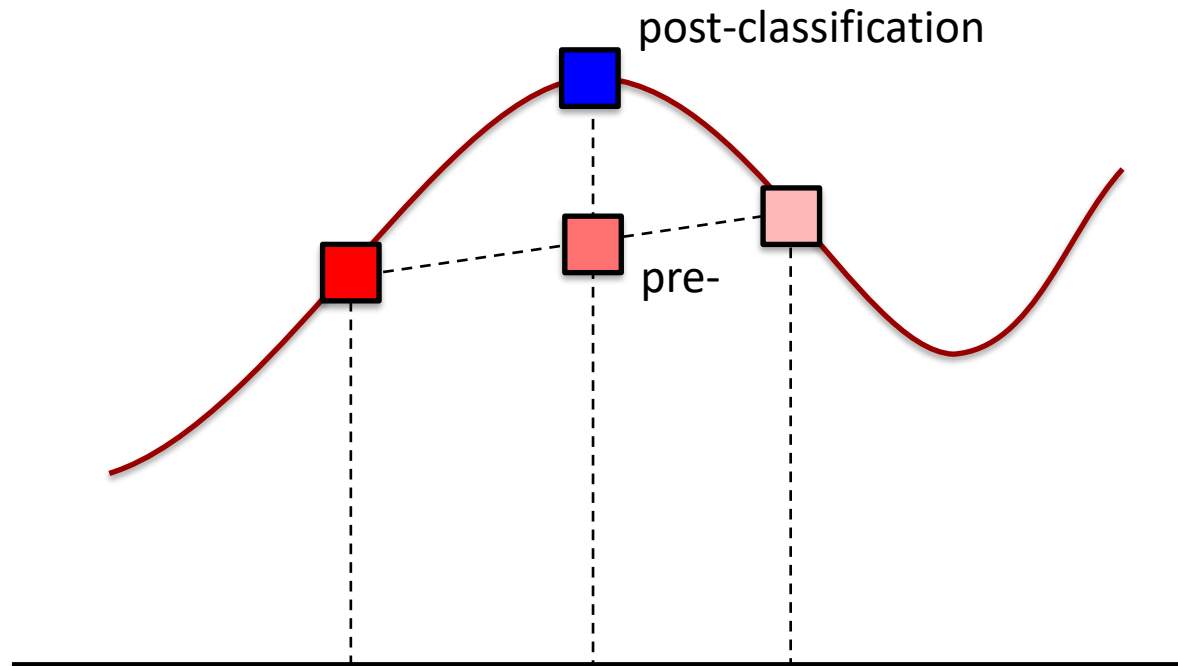
Mostly accurate
isolation of all
material
boundaries



Type of Classification



Pre- vs. Post-classification



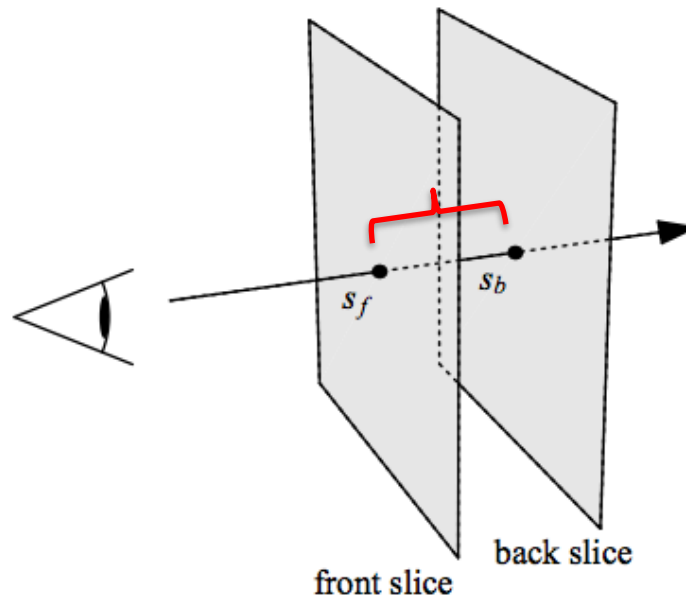
Pre- vs. Post-classification

- Pre-
 - Classification can be done only once = fast
 - Low quality
- Post-
 - Classification must be done per sample = slow
 - High-quality
- Similar to Gouraud vs. Phong shading!



Pre-integrated Volume Rendering

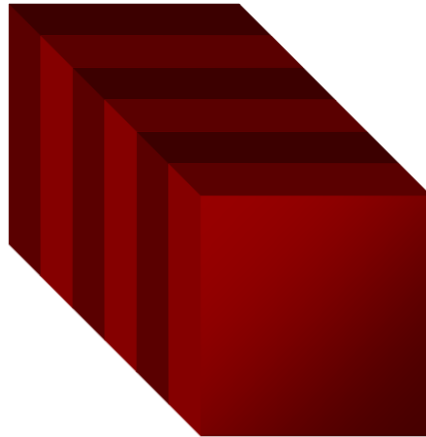
- Idea
 - Linear interpolation of scalar values within a slap
 - Constant length of a slap : L
 - Pre-compute integral along a ray in a slab



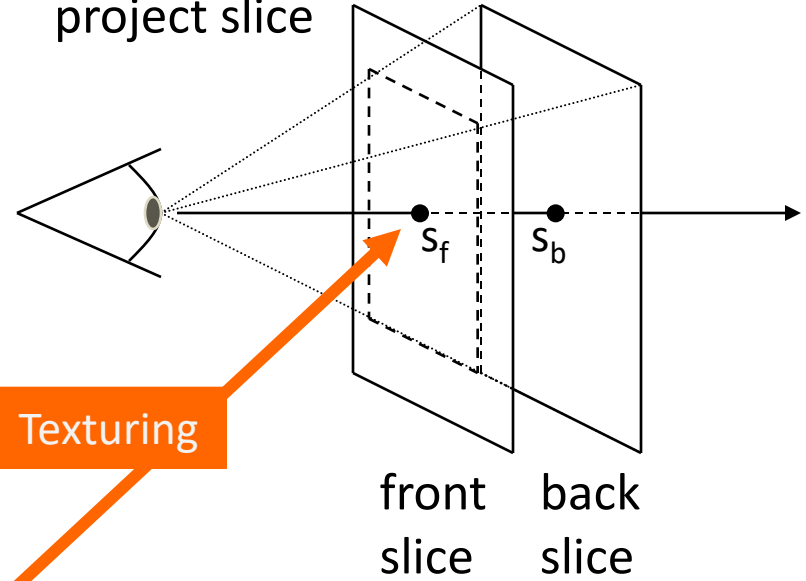
slice-by-slice



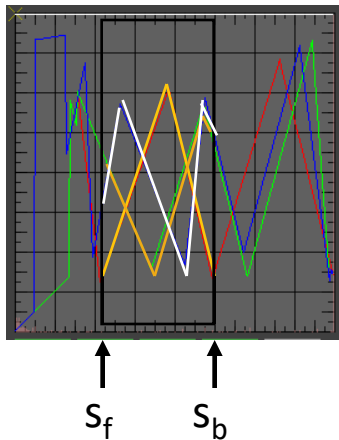
slab-by-slab



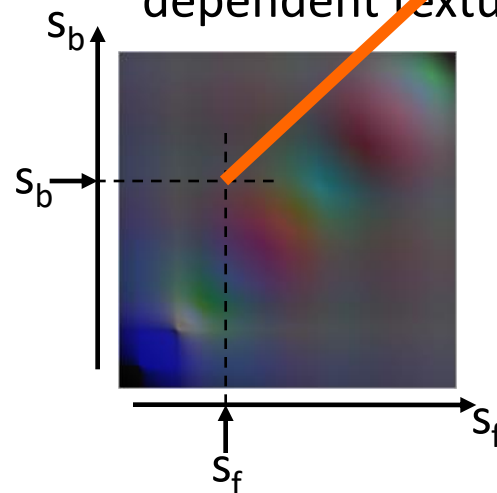
project slice



pre-integrate all possible combinations



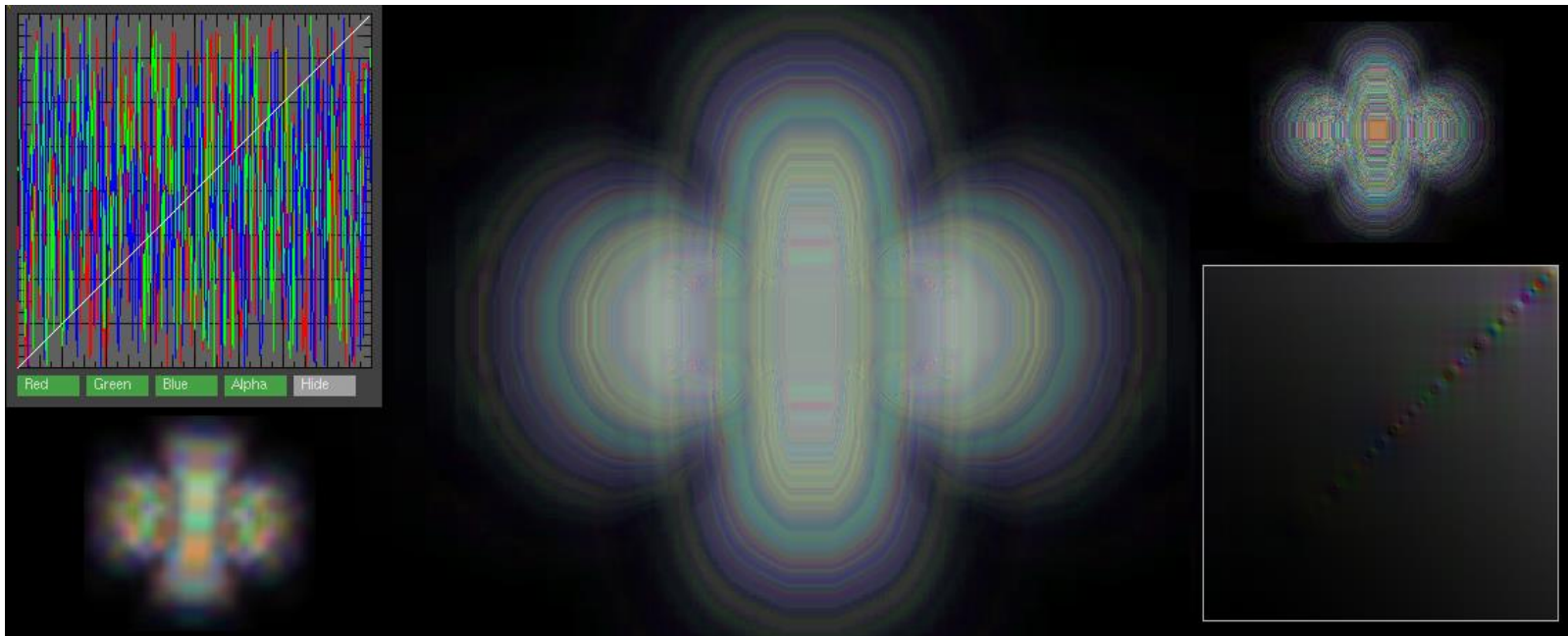
fetch integral from dependent texture

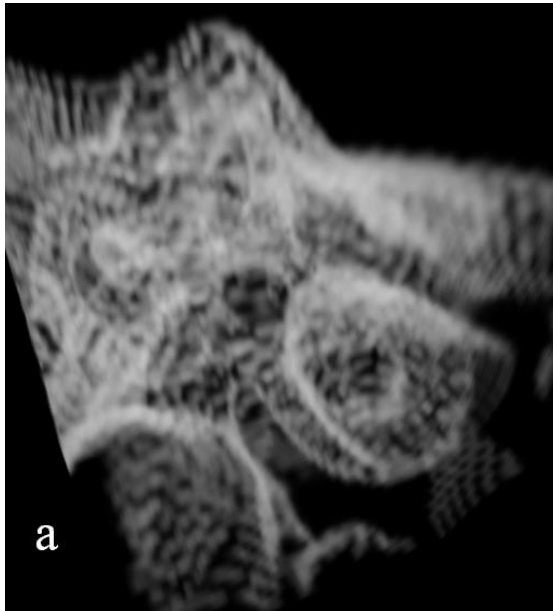


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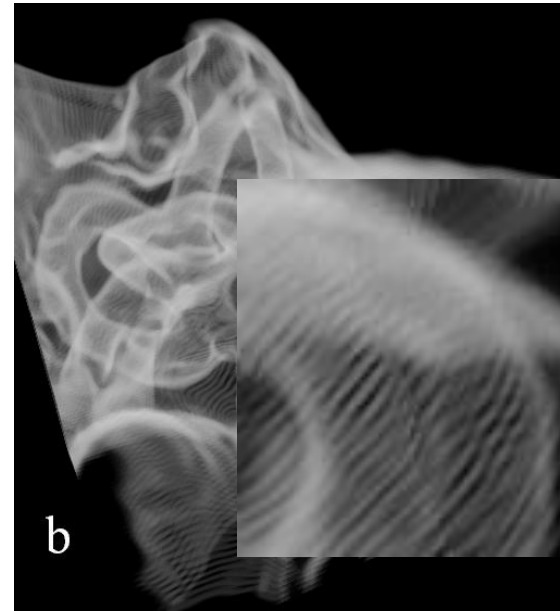
Pre-integrated Volume Rendering

- High-quality as post-classification, fast rendering as pre-classification
- Cons : pre-integrated table must be updated when transfer function is changed = use GPU for speed up

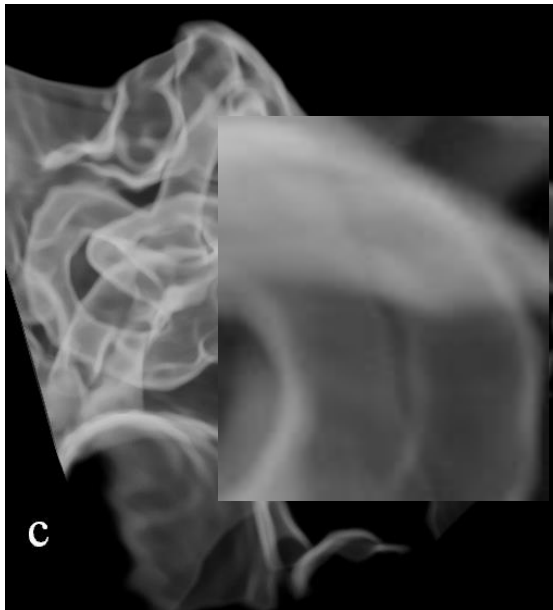




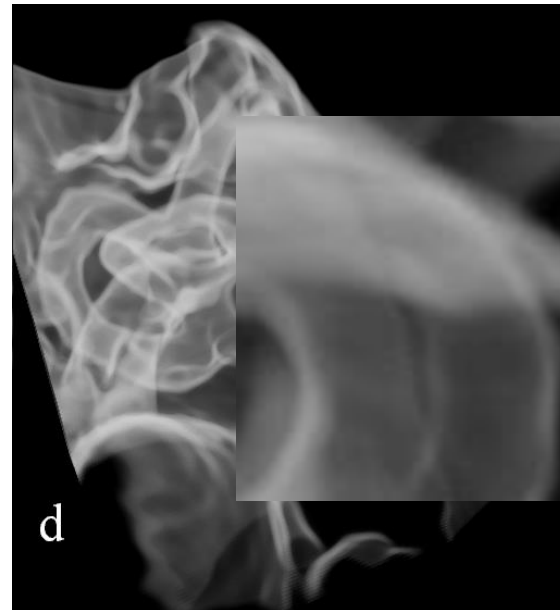
128 slices
pre-
classification



128 slices
post-
classification



284 slices
post-
classification



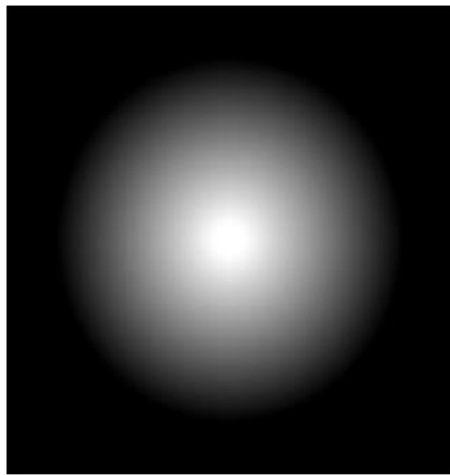
128 slices
pre-integrated



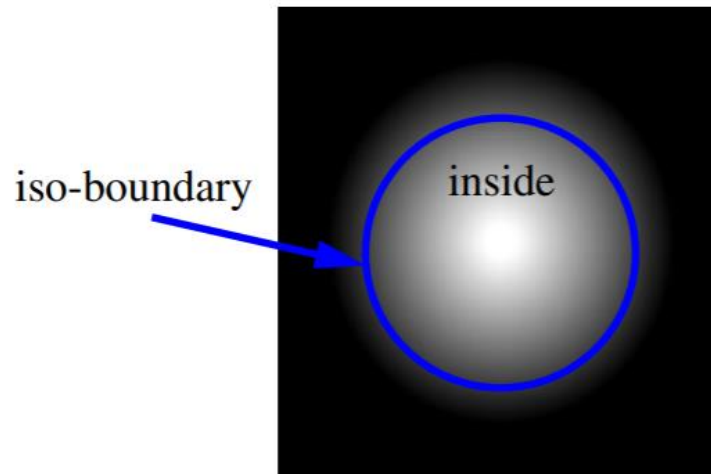
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Isosurface Volume Rendering

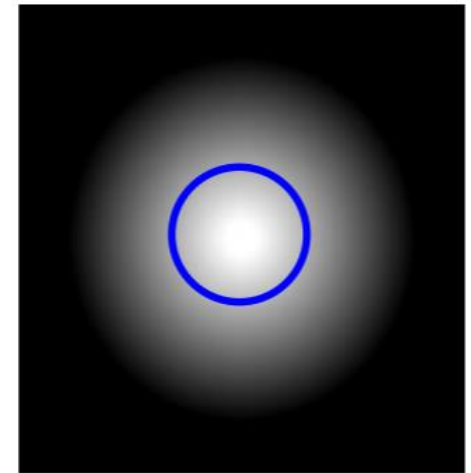
- Voxels are separated as inside or outside
 - Iso-value is where the contour/boundary located



cross-section of a smooth sphere

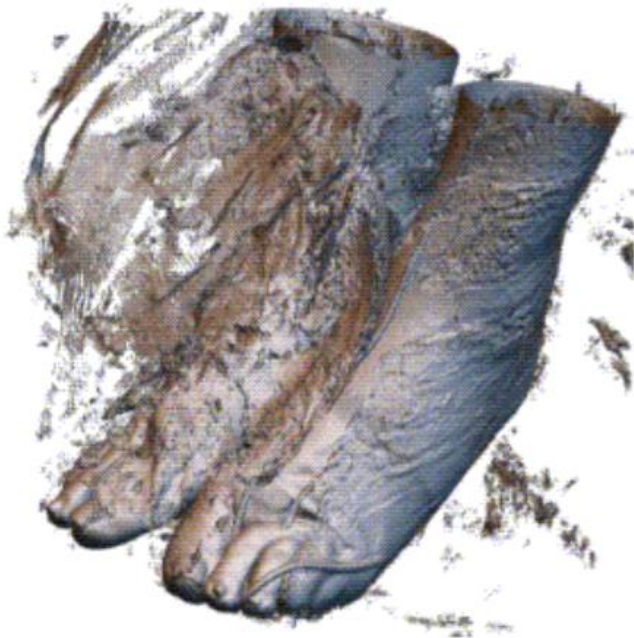


iso-value = 50
will render a large sphere



iso-value = 200
will render a small sphere

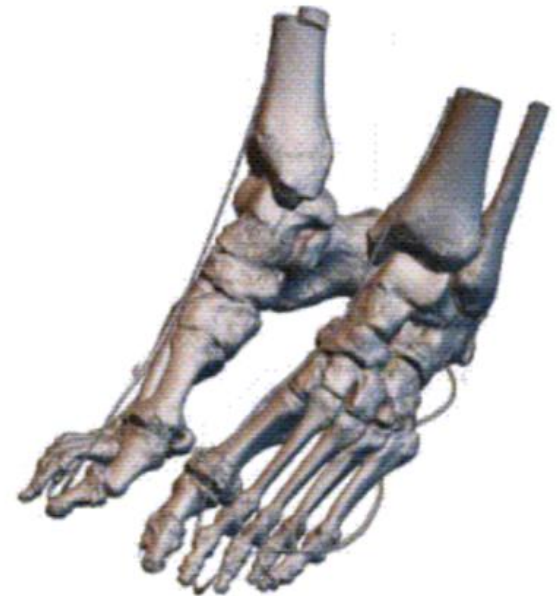
Example of Isosurface Volren



iso-value = 30



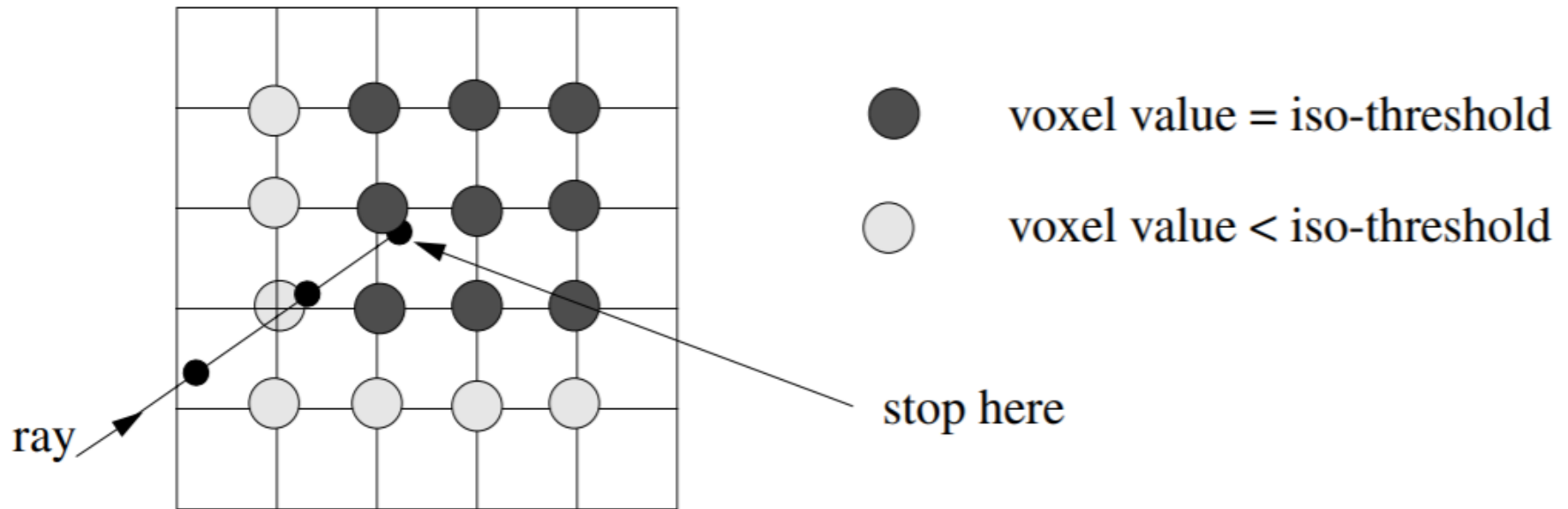
iso-value = 80



iso-value = 200

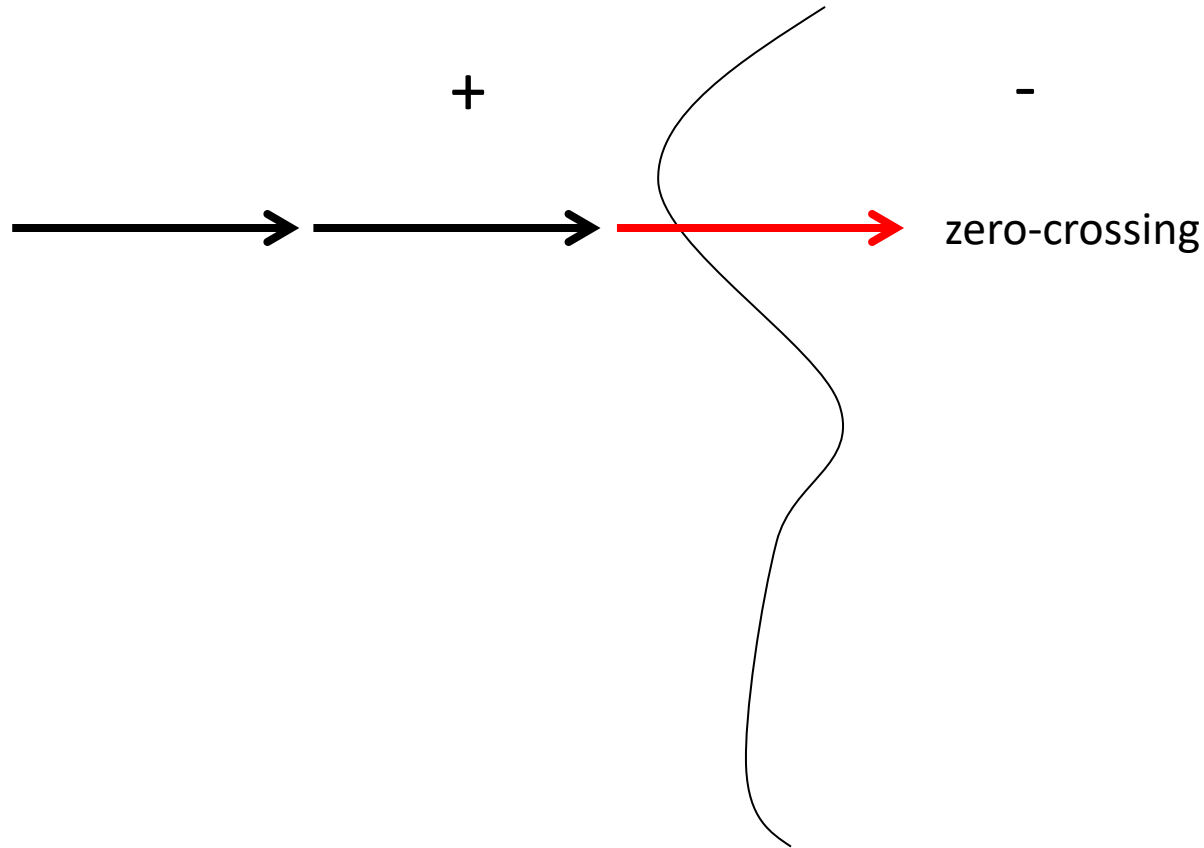
Algorithm

- Marching along ray until reach zero-crossing



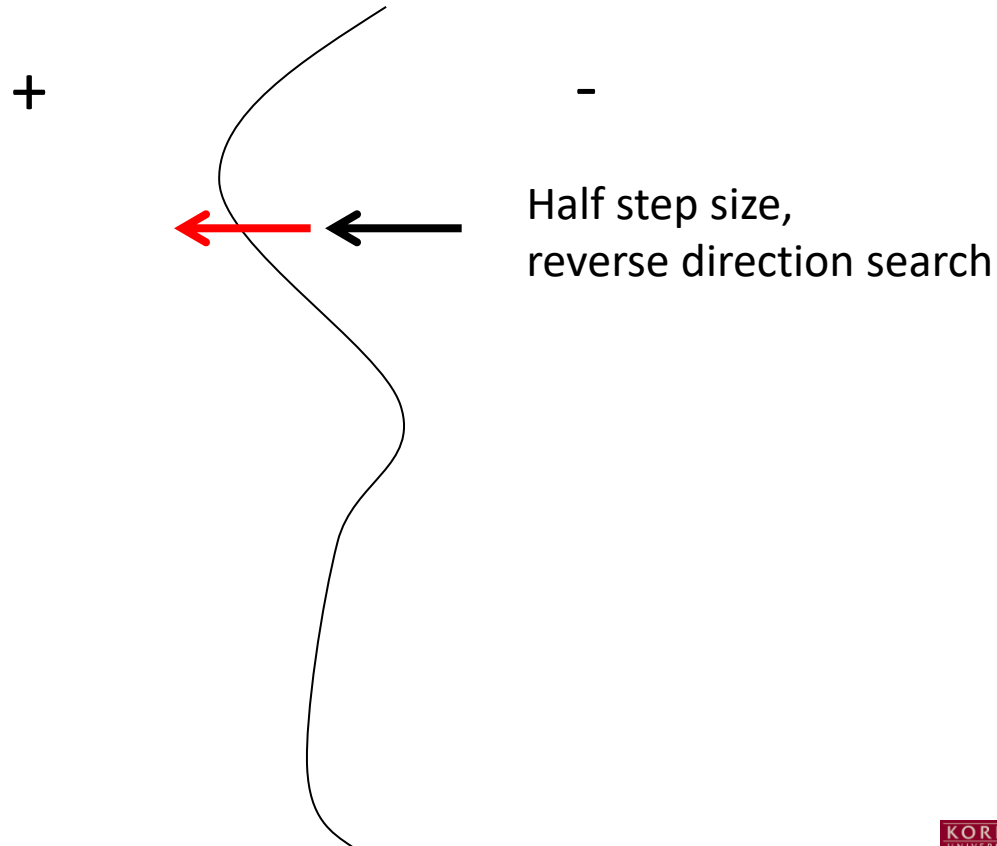
Algorithm

- Iterative root finding



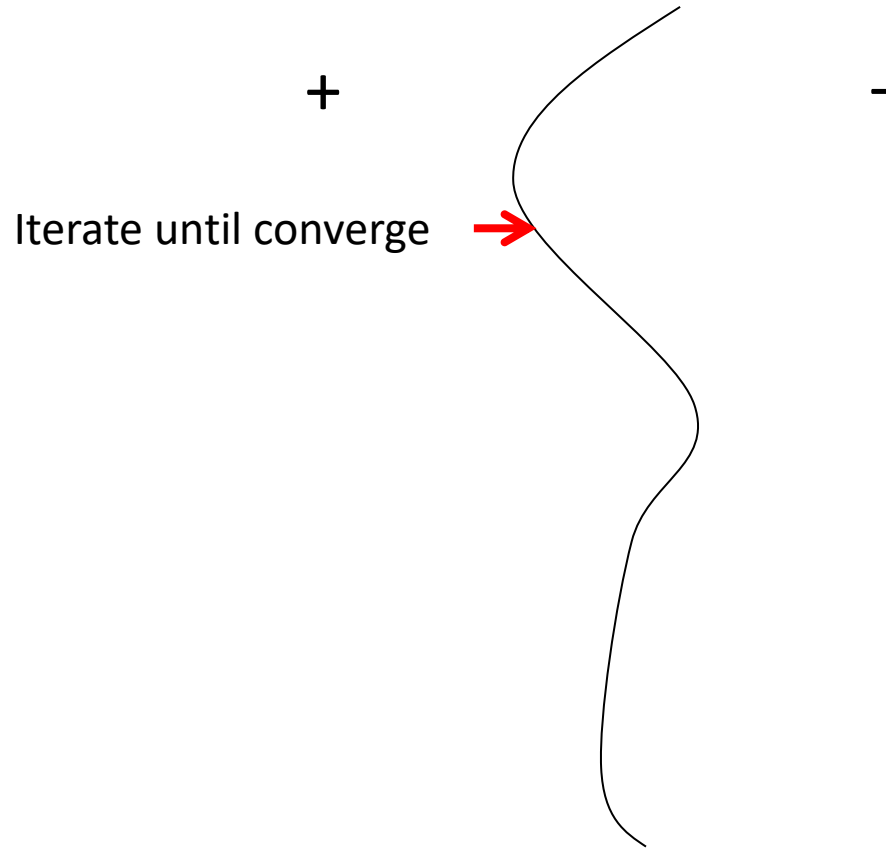
Algorithm

- Iterative root finding



Algorithm

- Iterative root finding



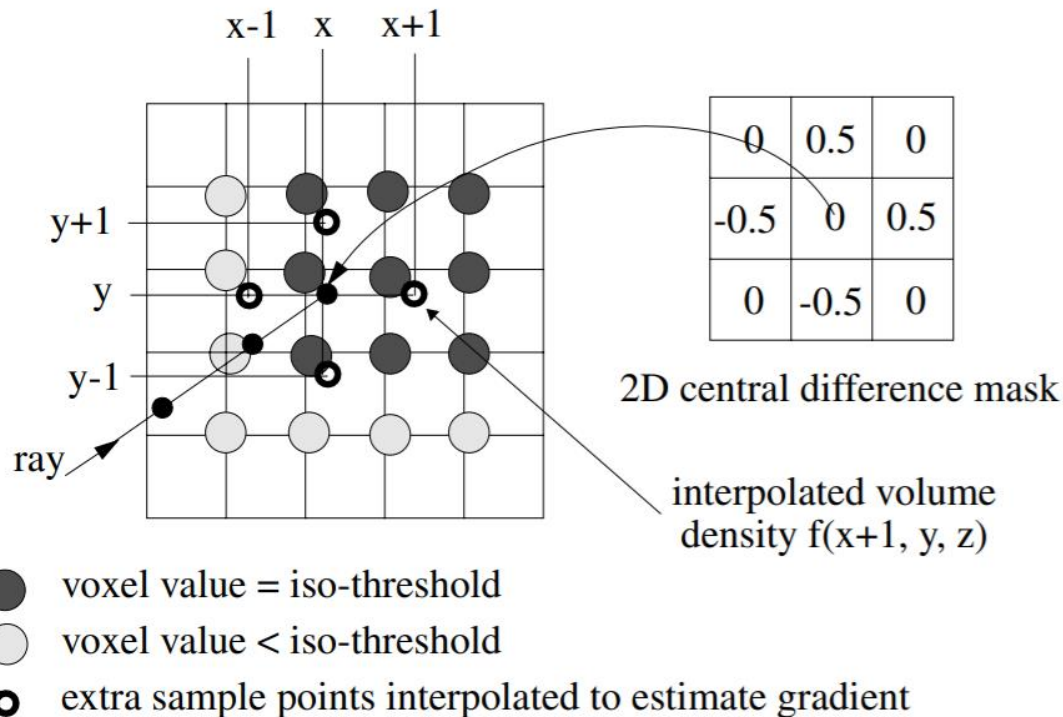
Algorithm

- Compute gradient vector

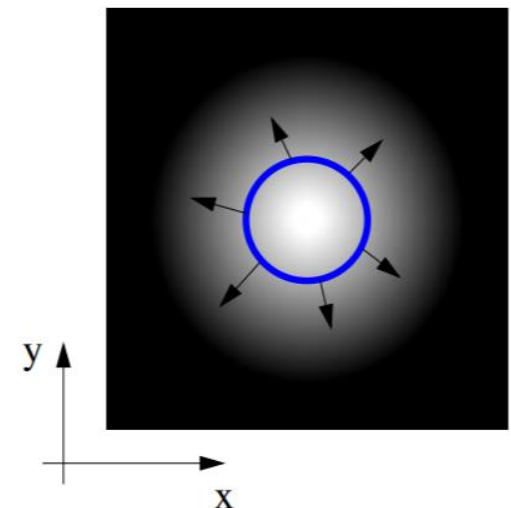
$$g_x = \frac{f(x-1, y, z) - f(x+1, y, z)}{2}$$

$$g_y = \frac{f(x, y-1, z) - f(x, y+1, z)}{2}$$

$$g_z = \frac{f(x, y, z-1) - f(x, y, z+1)}{2}$$

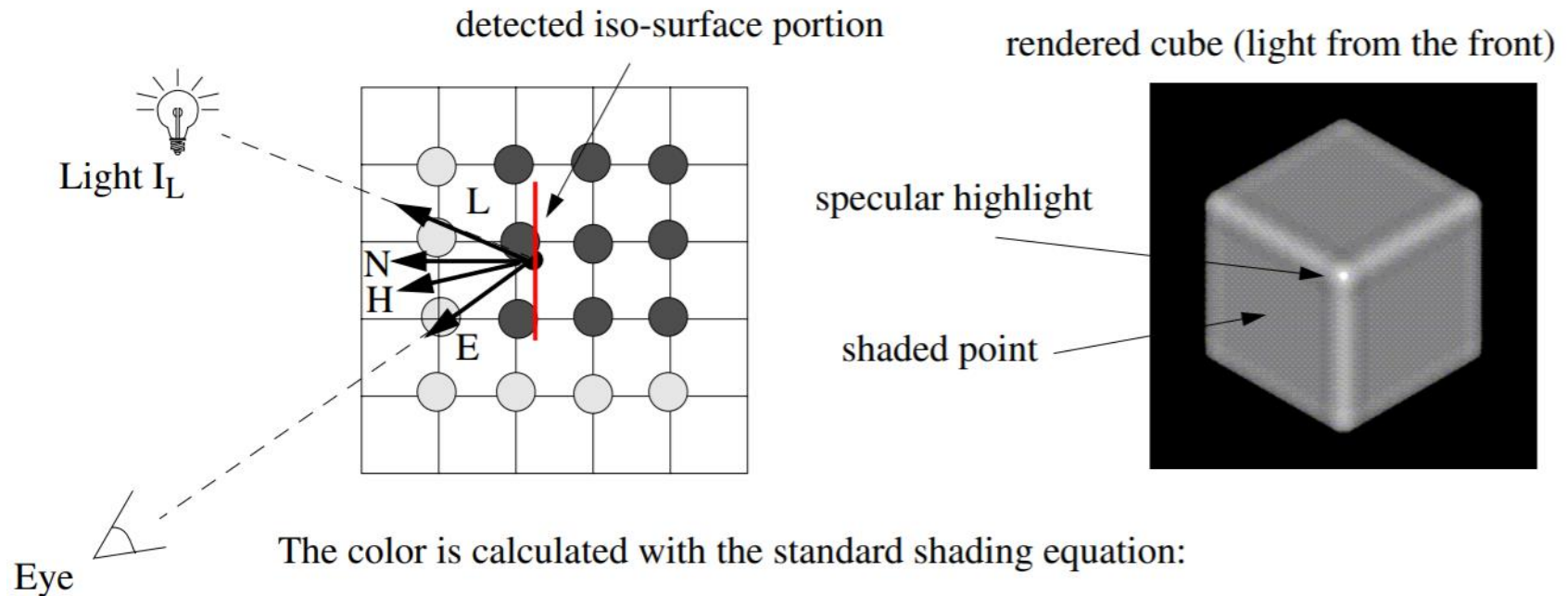


the x and y component
of the gradient vector
for the smooth sphere



Algorithm

- Use any illumination model (e.g., Phong)



The color is calculated with the standard shading equation:

$$C = C_{obj} (k_a I_A + k_d I_L N \cdot L) + k_s I_L (H \cdot N)^{ns}$$

Questions?



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