

Quantifying Controversy on Social Media

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Which topics spark the most heated debates on social media? Identifying those topics is not only interesting from a societal point of view but also allows the filtering and aggregation of social media content for disseminating news stories. In this article, we perform a **systematic methodological study of controversy detection by using the content and the network structure of social media**.

Unlike previous work, rather than studying controversy in a single hand-picked topic and using domain-specific knowledge, we take a general approach to **study topics in any domain**. Our approach to quantifying controversy is based on a graph-based three-stage pipeline, which involves (i) **building a conversation graph about a topic**, (ii) **partitioning the conversation graph to identify potential sides of the controversy**, and (iii) **measuring the amount of controversy from characteristics of the graph**.

We perform an extensive comparison of controversy measures, different graph-building approaches, and data sources. We use both controversial and non-controversial topics on Twitter, as well as other external datasets. We find that our new random-walk-based measure outperforms existing ones in capturing the intuitive notion of controversy and show that content features are vastly less helpful in this task.

CCS Concepts: • **Information systems** → **Social networking sites**; *Social networks*; • **Human-centered computing** → *Social networks*; • **Applied computing** → *Sociology*;

Additional Key Words and Phrases: Controversy, polarization, echo chambers, filter bubble, twitter

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1 INTRODUCTION

Given their widespread diffusion, online social media have become increasingly important in the study of social phenomena such as peer influence, framing, bias, and controversy. Ultimately, we would like to understand how users perceive the world through the lens of their social media feed. However, before addressing these advanced application scenarios, we first need to focus on the fundamental yet challenging task of distinguishing whether a topic of discussion is controversial.

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Our work is motivated by interest in observing controversies at societal level, monitoring their evolution, and possibly understanding which issues become controversial and why.

The study of controversy in social media is not new; there are many previous studies aimed at identifying and characterizing controversial issues, mostly around political debates [1, 10, 39, 40] but also for other topics [27]. And while most recent articles have focused on Twitter [10, 27, 39, 40], controversy in other platforms, such as blogs [1] and opinion fora [2], has also been analyzed.

However, most previous articles have **severe limitations**. First, the **majority of previous studies focus on controversy regarding political issues** and, in particular, are centered around long-lasting major events, such as elections [1, 10]. More crucially, most previous works can be characterized as **case studies**, where controversy is identified in a single carefully curated dataset, collected using ample domain knowledge and auxiliary domain-specific sources (e.g., an extensive list of hashtags regarding a major political event, or a list of left-leaning and right-leaning blogs).

We aim to overcome these limitations. **We develop a framework to identify controversy regarding topics in any domain (e.g., political, economical, or cultural), and without prior domain-specific knowledge about the topics in question.** Within the framework, we quantify the controversy associated with each topic and thus compare different topics to find the most controversial ones. Having a framework with these properties allows us to deploy a system in the wild and is valuable for building real-world applications.

To enable such a versatile framework, we work with topics that are defined in a lightweight and domain-agnostic manner. Specifically, when focusing on Twitter, a topic is specified as a text query. For example, “#beefban” is a special keyword (a “hashtag”) that Twitter users employed in March 2015 to signal that their posts referred to a decision by the Indian government about the consumption of beef meat in India. In this case, the query “#beefban” defines a topic of discussion, and the related activity consists of all posts that contain the query or other closely related terms and hashtags, as explained in Section 4.1.

We represent a topic of discussion with a conversation graph. In such a graph, vertices represent users, and edges represent conversation activity and interactions, such as *posts*, *comments*, *mentions*, or *endorsements*. Our working hypothesis is that it is possible to analyze the conversation graph of a topic to reveal how controversial the topic is. In particular, we expect the conversation graph of a controversial topic to have a *clustered structure*. This hypothesis is based on the fact that a controversial topic entails different sides with opposing points of view, and individuals on the same side tend to endorse and amplify each other’s arguments [1, 2, 10].

Our main contribution is to **test this hypothesis**. We achieve this result by studying a large number of candidate features, based on the following *aspects* of activity: (i) *structure of endorsements*, i.e., who agrees with whom on the topic; (ii) *structure of the social network*, i.e., who is connected with whom among the participants in the conversation; (iii) *content*, i.e., the keywords used in the topic; and (iv) *sentiment*, i.e., the tone (positive or negative) used to discuss the topic. Our study shows that all features, except from content-based ones, are useful in detecting controversial topics, to different extents. Particularly for Twitter, we find endorsement features (i.e., retweets) to be the most useful.

The extracted features are then used to compute the **controversy score** of a topic. We offer a systematic definition and provide a thorough evaluation of measures to quantify controversy. We employ a broad range of topics, both controversial and non-controversial, on which we evaluate several measures, either defined in this article or coming from the literature [27, 40]. We find that one of our newly proposed measures, based on *random walks*, is able to discriminate controversial topics with great accuracy. In addition, it also generalizes well as it agrees with previously defined measures when tested on datasets from existing work. We also find that the *variance* of the sentiment expressed on a topic is a reliable indication of controversy.

The approach to quantifying controversy presented in this article can be condensed into a three-stage pipeline: (i) building a *conversation graph* among the users who contribute to a topic, where edges signify that two users are in some form of agreement, (ii) identifying the potential sides of the controversy from the graph structure or the textual content, and (iii) quantifying the amount of controversy in the graph.

The rest of this article is organized as follows. Section 2 discusses how this work fills gaps in the existing literature. Subsequently, Section 3 provides a high-level description of the pipeline for quantifying controversy of a topic, while Sections 4, 5, and 6 detail each stage. Section 7 shows how to extend the controversy measures from topics to users who participate in the discussion. We report the results of an extensive empirical evaluation of the proposed measures of controversy in Section 8. Section 9 extends the evaluation to a few measures that do not fit the pipeline. We conclude in Section 10 with a discussion on possible improvements and directions for future work, as well as lessons learned from carrying out this study.

2 RELATED WORK

Analysis of controversy in online news and social media has attracted considerable attention, and a number of articles have provided very interesting case studies. In one of the first articles, Adamic and Glance [1] study the link patterns and discussion topics of political bloggers, focusing on blog posts about the U.S. presidential election of 2004. They measure the degree of interaction between liberal and conservative blogs and provide evidence that conservative blogs are linking to each other more frequently and in a denser pattern. These findings are confirmed by the more recent study of Conover et al. [10], who also study controversy in political communication regarding congressional midterm elections. Using data from Twitter, Conover et al. [10] identify a highly segregated partisan structure (present in the retweet graph but not in the mention graph), with limited connectivity between left- and right-leaning users. In another recent work related to controversy analysis in political discussion, Mejova et al. [39] identify a significant correlation between controversial issues and the use of negative affect and biased language.

The articles mentioned so far study controversy in the political domain and provide case studies centered around long-lasting major events, such as presidential elections. In this article, we aim to identify and quantify controversy for any topic discussed in social media, including short-lived and ad-hoc ones (for example, see the topics in Table 2). The problem we study has been considered by previous work, but the methods proposed so far are, to a large degree, domain specific.

The work of Conover et al. [10], discussed above, employs the concept of modularity and graph partitioning to verify (but not quantify) controversy structure of graphs extracted from discussion of political issues on Twitter. In a similar setting, Guerra et al. [27] propose an alternative graph-structure measure. Their measure relies on the analysis of the boundary between two (potentially) polarized communities and performs better than modularity. Differently from these studies, our contribution consists in providing an extensive study of a large number of measures, including the ones proposed earlier, and demonstrating clear improvement over those. We also aim at quantifying controversy in diverse and in-the-wild settings rather than carefully curated domain-specific datasets.

In a recent study, Morales et al. [40] quantify polarity via the propagation of opinions of influential users on Twitter. They validate their measure with a case study from Venezuelan politics. Again, our methods are not only more general and domain agnostic, but they provide more intuitive results. In a different approach, Akoglu [2] proposes a polarization metric that uses signed bipartite opinion graphs. The approach differs from ours as it relies on the availability of this particular type of data, which is not as readily available as social-interaction graphs.

Similarly to the articles discussed above, in our work we quantify controversy based on the graph structure of social interactions. In particular, we assume that controversial and polarized

Table 1. Summary of Related Work for Identifying/Quantifying Controversial Topics

Paper	Identifying	Quantifying	Content	Network
Choi et al. [8]	✓		✓	
Popescu and Pennacchiotti [45]	✓		✓	
Mejova et al. [39]	✓		✓	
Klenner et al. [33]	✓		✓	
Tsytsarau et al. [49]	✓		✓	
Dori-Hacohen and Allan [14]	✓		✓	
Jang et al. [29]	✓		✓	
Conover et al. [10]	✓			✓
Coletto et al. [9]	✓			✓
Akoglu [2]	✓			✓
Amin et al. [3]	✓			✓
Guerra et al. [27]	✓	✓		✓
Morales et al. [40]	✓	✓		✓
Garimella et al. [20]	✓	✓		✓



Fig. 1. Block diagram of the pipeline for computing controversy scores.

topics induce graphs with clustered structure, representing different opinions and points of view. This assumption relies on the concept of “echo chambers,” which states that opinions or beliefs stay inside communities created by like-minded people, who reinforce and endorse the opinions of each other. This phenomenon has been quantified in many recent studies [4, 18, 26].

A different direction for quantifying controversy, followed by Choi et al. [8] and Mejova et al. [39], relies on text and sentiment analysis. Both studies focus on language found in news articles. In our case, since we are mainly working with Twitter, where text is short and noisy, and since we are aiming at quantifying controversy in a domain-agnostic manner, text analysis has its limitations. Nevertheless, we experiment with incorporating content features in our approach.

A summary of related work categorized along different dimensions is presented in Table 1. As we mention above, most existing work to date tries to *identify* controversial topics as case studies on a particular topic, either using content or networks of interactions. Our work is one of the few that *quantifies* the degree of controversy using language and domain-independent methods. Section 8 shows that our method outperforms existing ones [27, 40].

Finally, our findings on controversy have several potential applications on news-reading and public-debate scenarios. Quantifying controversy can provide a basis for analyzing the “news diet” of readers [34, 35], offering the chance of better information by providing recommendations of contrarian views [41], deliberating debates [16], and connecting people with opposing views [15, 25].

3 PIPELINE

Our approach to measuring controversy is based on a systematic way of characterizing social media activity. We employ a pipeline with three stages, namely *graph building*, *graph partitioning*, and *controversy measure*, as shown in Figure 1. The final output of the pipeline is a value that measures

how controversial a topic is, with higher values corresponding to higher degree of controversy. We provide a high-level description of each stage here and more details in the sections that follow.

3.1 Building the Graph

The purpose of this stage is to build a *conversation graph* that represents activity related to a single *topic* of discussion. In our pipeline, a topic is operationalized as a set of related hashtags (details in Section 4.1), and the social media activity related to the topic consists of those items (e.g., posts) that match this set of hashtags. For example, the query might consist simply of a keyword, such as “#ukraine,” in which case the related activity consists of all tweets that contain that keyword, or related tags such as #kyiv and #stoprussianaggression. Even though we describe textual queries in standard document-retrieval form, in principle queries can take other forms, as long as they are able to induce a graph from the social media activity (e.g., RDF queries or topic models).

Each item related to a topic is associated with one user who generated it, and we build a graph where each user who contributed to the topic is assigned to one vertex. In this graph, an edge between two vertices represents *endorsement*, *agreement*, or *shared point of view* between the corresponding users. Section 4 details several ways to build such a graph.

3.2 Partitioning the Graph

In the second stage, the resulting conversation graph is fed into a *graph partitioning* algorithm to extract *two* partitions (we defer considering multi-sided controversies to further study). Intuitively, the two partitions correspond to two disjoint sets of users who possibly belong to different sides in the discussion. In other words, the output of this stage answers the following question: “Assuming that users are split into two sides according to their point of view on the topic, which are these two sides?” Section 5 describes this stage in further detail. If indeed there are two sides which do not agree with each other—a controversy—then the two partitions should be loosely connected to each other, given the semantic of the edges. This property is captured by a measure computed in the third and final stage of the pipeline.

3.3 Measuring Controversy

The third and last stage takes as input the graph built by the first stage and partitioned by the second stage and computes the value of a *controversy measure* that characterizes how controversial the topic is. Intuitively, a controversy measure aims to capture how well separated the two partitions are. We test several such measures, including ones based on random walks, betweenness centrality, and low-dimensional embeddings. Details are provided in Section 6.

4 GRAPH BUILDING

This section provides details about different approaches to build graphs from raw data. We use posts on Twitter to create our datasets.¹ Twitter is a natural choice for the problem at hand, as it represents one of the main fora for public debate in online social media and is often used to report news about current events. Following the procedure described in Section 3.1, we specify a set of queries (indicating topics) and build one graph for each query. We choose a set of topics that is balanced between controversial and non-controversial ones to test for both false positives and false negatives.

We use Twitter hashtags as *queries*. Users commonly employ hashtags to indicate the topic of discussion their posts pertain to. Then, we define a *topic* as the set of hashtags related to the given query. Among the large number of hashtags that appear in the Twitter stream, we consider those

¹From the full Twitter firehose stream.

that were trending during the period from February 27 to June 15, 2015. By manual inspection we find that most trending hashtags are not related to controversial discussions [19].

We first manually pick a set of 10 hashtags that we know represent *controversial* topics of discussion. All hashtags in this set have been widely covered by mainstream media and have generated ample discussion, both online and offline. Moreover, to have a dataset that is balanced between controversial and non-controversial topics, we sample another set of 10 hashtags that represent *non-controversial* topics of discussion. These hashtags are related mostly to “soft news” and entertainment but also to events that, while being impactful and dramatic, did not generate large controversies (e.g., #nepal and #germanwings). In addition to our intuition that these topics are non-controversial, we manually check a sample of tweets, and we are unable to identify any clear instance of controversy.²

As a first step, we now describe the process of expanding a single hashtag into a set of related hashtags that define the topic. The goal of this process is to broaden the definition of a topic and ultimately improve the coverage of the topic itself.

4.1 From Hashtags to Topics

In the literature, a topic is often defined by a single hashtag. However, this choice might be too restrictive in many cases. For instance, the opposing sides of a controversy might use different hashtags, as the hashtag itself is loaded with meaning and used as a means to express their opinion. Using a single hashtag may thus miss part of the relevant posts.

To address this limitation, we extend the definition of topic to be more encompassing. Given a *seed* hashtag, we define a topic as a set of related hashtags, which co-occur with the seed hashtag. To find related hashtags, we employ (and improve on) a recent clustering algorithm tailored for the purpose [17].

Feng et al. [17] develop a simple measure to compute the similarity between two hashtags, which relies on co-occurring words and hashtags. The authors then use this similarity measure to find closely related hashtags and define clusters. However, this simple approach presents one drawback, in that very popular hashtags such as #ff or #follow co-occur with a large number of hashtags. Hence, directly applying the original approach results in extremely noisy clusters. Since the quality of the topic affects critically the entire pipeline, we want to avert this issue and ensure minimal noise is introduced in the expanded set of hashtags.

Therefore, we improve the basic approach by taking into account and normalizing for the popularity of the hashtags. Specifically, we compute the document frequency of all hashtags on a random 1% sample of the Twitter stream³ and normalize the original similarity score between two hashtags by the inverse document frequency. The similarity score is formally defined as

$$\text{sim}(h_s, h_t) = \frac{1}{1 + \log(df(h_t))} (\alpha \cos(W_s, W_t) + (1 - \alpha) \cos(H_s, H_t)), \quad (1)$$

where h_s is the seed tag; h_t is the candidate tag; W_x and H_x are the sets of words and hashtags that co-occur with hashtag h_x , respectively; \cos is the cosine similarity between two vectors; df is the document frequency of a tag; and α is a parameter that balances the importance of words compared to hashtags in a post.

By using the similarity function in Equation (1), we retrieve the top- k most similar hashtags to a given seed. The set of these hashtags along with the initial seed defines the topic for the given

²Code and networks used in this work are available at <http://github.com/gvrkiran/controversy-detection>.

³From the Twitter Streaming API <https://dev.twitter.com/streaming/reference/get/statuses/sample>.



Fig. 2. Sets of related hashtags for the topics (a) #baltimoreriots and (b) #netanyahuspeech.

seed hashtag. The topic is used as a filter to get all tweets that contain at least one of the hashtags in the topic. In our experiments, we use $\alpha = 0.3$ (as proposed by Feng et al. [17]) and $k = 20$.

Figure 2 shows the top-20 most similar hashtags for two different seeds: (a) #baltimoreriots, which identifies the discussion around the Baltimore riots against police violence in April 2015 and (b) #netanyahuspeech, which identifies the discussion around Netanyahu’s speech at the U.S. congress in March 2015. By inspecting the sets of hashtags, it is possible to infer the nature of the controversy for the given topic, as both sides are represented. For instance, the hashtags #istandwithisrael and #shutupbibi represent opposing sides in the discussion raised by Netanyahu’s speech. Both hashtags are recovered by our approach when #netanyahuspeech is provided as the seed hashtag. It is also clear why using a single hashtag is not sufficient to define a topic: The same user is not likely to use both #safespaceforriot and #segregatenow, even though the two hashtags refer to the same event (#baltimoreriots).

4.2 Data Aspects

For each topic, we retrieve all tweets that contain one of its hashtags and that are generated during the observation window. We also ensure that the selected hashtags are associated with a large-enough volume of activity. Table 2 presents the final set of seed hashtags, along with their description and the number of related tweets.⁴ For each topic, we build a graph G where we assign a vertex to each user who contributes to it and generate edges according to one of the following four approaches, which capture different *aspects* of the data source.

1. Retweet graph. Retweets typically indicate endorsement.⁵ Users who retweet signal endorsement of the opinion expressed in the original tweet by propagating it further. Retweets are not constrained to occur only between users who are connected in Twitter’s social network, but users are allowed to retweet posts generated by any other user.

We select the edges for graph G based on the retweet activity in the topic: An edge exists between two users u and v if there are at least *two* ($\tau = 2$) retweets between them that use the hashtag, irrespective of direction. We remark that, in preliminary experimentation with this approach, building the retweet graph with a threshold $\tau = 1$ did not produce reliable results. We presume that a single retweet on a topic is not enough of a signal to infer endorsement. Using $\tau = 2$ retweets as threshold

⁴We use a hashtag in Russian, #Марш, which we refer to as #russia_march henceforth, for convenience.

⁵We do not consider ‘quote retweets’ (retweet with a comment added) in our analysis.

Table 2. Datasets Statistics: Hashtag, Sizes of the Follow and Retweet Graphs, and Description of the Event

Hashtag	# Tweets	Retweet graph		Follow graph		Description and collection period (2015)
		V	E	V	E	
#beefban	422908	21590	30180	9525	204332	Government of India bans beef, Mar 2–5
#nemtsov	371732	43114	77330	17717	155904	Death of Boris Nemtsov, Feb 28–Mar 2
#netanyahuspeech	1196215	122884	280375	49081	2009277	Netanyahu’s speech at U.S. Congress, Mar 3–5
#russia_march	317885	10883	17662	4844	42553	Protests after death of Boris Nemtsov (“march”), Mar 1–2
#indiasdaughter	776109	68608	144935	38302	131566	Controversial Indian documentary, Mar 1–5
#baltimoreriots	1989360	289483	432621	214552	690944	Riots in Baltimore after police kills a black man, Apr 28–30
#indiana	972585	43252	74214	21909	880814	Indiana pizzeria refuses to cater gay wedding, Apr 2–5
#ukraine	514074	50191	91764	31225	286603	Ukraine conflict, Feb 27–Mar 2
#gunsense	1022541	30096	58514	17335	841466	Gun violence in U.S., Jun 1–30
#leadersdebate	2099478	54102	136290	22498	1211956	Debate during the U.K. national elections, May 3
#sxsw	343652	9304	11003	4558	91356	SXSW conference, Mar 13–22
#1dfamheretostay	501960	15292	26819	3151	20275	Last OneDirection concert, Mar 27–29
#germanwings	907510	29763	39075	2111	7329	Germanwings flight crash, Mar 24–26
#mothersday	1798018	155599	176915	2225	14160	Mother’s day, May 8
#nepal	1297995	40579	57544	4242	42833	Nepal earthquake, Apr 26–29
#ultralive	364236	9261	15544	2113	16070	Ultra Music Festival, Mar 18–20
#FF	408326	5401	7646	3899	63672	Follow Friday, Jun 19
#jurassicworld	724782	26407	32515	4395	31802	Jurassic World movie, Jun 12–15
#wcw	156243	10674	11809	3264	23414	Women crush Wednesdays, Jun 17
#nationalkissingday	165172	4638	4816	790	5927	National kissing day, Jun 19

The top group represents controversial topics, while the bottom one represents non-controversial ones.

proves to be a good tradeoff between high selectivity (which hinders analysis) and noise reduction. The resulting size for each retweet graph is listed in Table 2.

In an earlier version of this work [20], when building a conversation graph for a single hashtag, we created an edge between two vertices only if there were “at least two retweets per edge” (in either direction) between the corresponding pair of users. When defining topics as sets of hashtags, there are several ways to generalize this filtering step. The simplest approach considers “two of any” in the set of hashtags that defines the topic. However, this approach is too permissive and results in an overly inclusive graph, with spurious relationships and a high level of noise. Instead, we opt to create an edge between two nodes only if there are at least two retweets for any given

hashtag between the corresponding pair of users. In other words, the resulting conversation graph for the topic is the union of the retweet graphs for each hashtag in the topic, considered (and filtered) separately.

2. Follow graph. In this approach, we build the follow graph induced by a given hashtag. We select the edges for graph G based on the social connections between Twitter users *who employ the given hashtag*: An edge exists between users u and v if u follows v or vice versa. We stress that the graph G built with this approach is topic specific, as the edges in G are constrained to connections between users who discuss the topic that is specified as input to the pipeline.

The rationale for using this graph is based on an assumption of the presence of homophily in the social network, which is a common trait in this setting. To be more precise, we expect that *on a given topic* people will agree more often than not with people they follow and that for a controversial topic this phenomenon will be reflected in well-separated partitions of the resulting graph. Note that using the entire social graph would not necessarily produce well-separated partitions that correspond to single topics of discussion, as those partitions would be “blurred” by the existence of additional edges that are due to other reasons (e.g., offline social connections).

On the practical side, while the retweet information is readily available in the stream of tweets, the social network of Twitter is not. Collecting the follower graph thus requires an expensive crawling phase. The resulting graph size for each follow graph is listed in Table 2.

3. Content graph. We create the edges of graph G based on whether users post instances of the same content. Specifically, we experiment with the following three variants: create an edge between two vertices if the users (i) use the same hashtag, other than the ones that defines the topic, (ii) share a link to the same URL, or (iii) share a link with the same URL domain (e.g., cnn.com is the domain for all pages on the website of CNN).

4. Hybrid content and retweet graph. We create edges for graph G according to a state-of-the-art process that blends content and graph information [46]. Concretely, we associate each user with a vector of frequencies of mentions for different hashtags. Subsequently, we create edges between pairs of users whose corresponding vectors have high cosine similarity and combine them with edges from the retweet graph, built as described above. For details, we refer the interested reader to the original publication [46].

5 GRAPH PARTITIONING

As previously explained, we use a graph partitioning algorithm to produce two partitions on the conversation graph. To do so, we rely on a state-of-the-art off-the-shelf algorithm, METIS [32]. Figure 3 displays the two partitions returned for some of the topics on their corresponding retweet and follow graphs (Figures 3(a)–(d) and Figures 3(e)–(h), respectively).⁶ The partitions are depicted in blue or red. The graph layout is produced by Gephi’s ForceAtlas2 algorithm [28] and is based solely on the structure of the graph, not on the partitioning computed by METIS. Only the largest connected component is shown in the visualization, though in all the cases the largest connected component contains more than 90% of nodes.

From an initial visual inspection of the partitions identified on retweet and follow graphs, we find that the partitions match well with our intuition of which topics are controversial (the partitions returned by METIS are well separated for controversial topics). To make sure that this initial assessment of the partitions is not an artifact of the visualization algorithm we use, we try other layouts offered by Gephi. In all cases we observe similar patterns. We also manually sample and

⁶Other topics show similar trends.

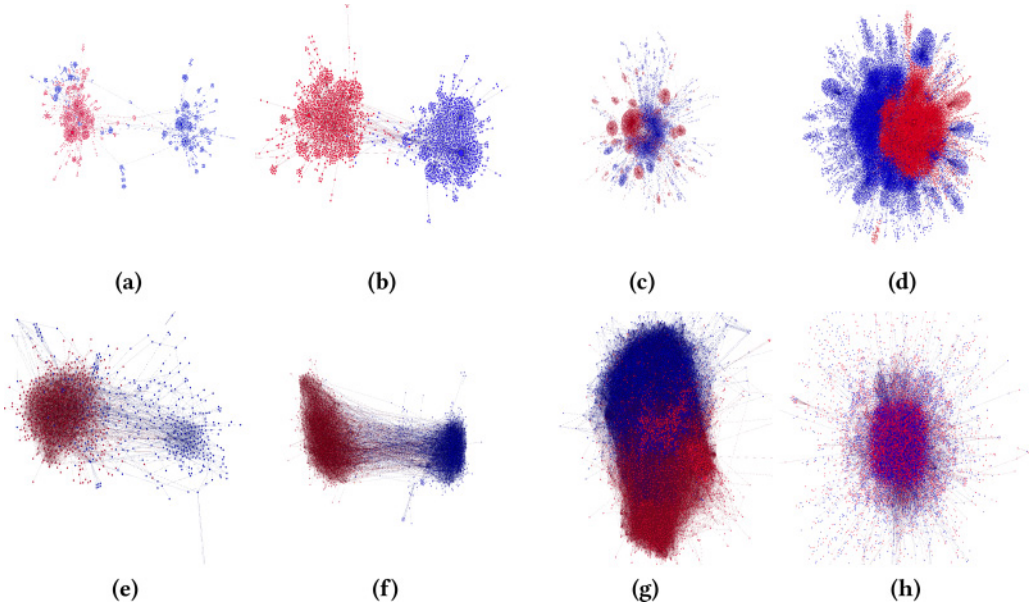


Fig. 3. Sample conversation graphs with retweet (top) and follow (bottom) aspects (visualized using the force-directed layout algorithm in Gephi). The left side is controversial, ((a) and (e)) #beefban and ((b) and (f)) #russia_march, while the right side is non-controversial, ((c) and (g)) #sxsw and ((d) and (h)) #germanwings. Only the largest connected component is shown.

check tweets from the partitions to verify the presence of controversy. While this anecdotal evidence is hard to report, indeed the partitions seem to capture the spirit of the controversy.⁷

On the contrary, the partitions identified on content graphs fail to match our intuition. All three variants of the content-based approach lead to sparse graphs and highly overlapping partitions, even in cases of highly controversial issues. The same pattern applies for the hybrid approach, as shown in Figure 4. We also try a variant of the hybrid graph approach with vectors that represent the frequency of different URL domains mentioned by a user, with no better results. We thus do not consider these approaches to graph building any further in the remainder of this article.

Finally, we try graph partitioning algorithms of other types. Besides METIS (cut based), we test spectral clustering, label propagation, and affiliation-graph-based models. The difference among these methods is not significant; however, from visual inspection METIS generates the cleanest partitions.

6 CONTROVERSY MEASURES

This section describes the controversy measures used in this work. For completeness, we describe both those measures proposed by us (Sections 6.1, 6.3, 6.4) as well as the ones from the literature that we use as baselines (Sections 6.5, 6.6).

⁷For instance, of these two tweets for #netanyahuspeech from two users on opposing sides, one is clearly supporting the speech <https://t.co/OVeWB4XqIg>, while the other highlights the negative reactions to it <https://t.co/v9RdPudrrC>.

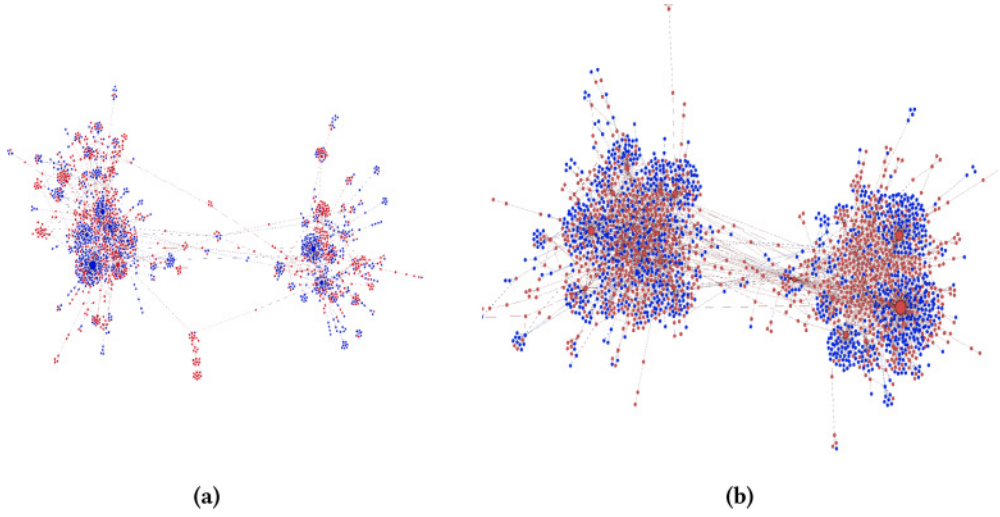


Fig. 4. Partitions obtained for (a) #beefban snf (b) #russia_march by using the hybrid graph building approach. The partitions are more noisy than those in Figures 3(a) and (b).

6.1 Random Walk

This measure uses the notion of random walks on graphs. It is based on the rationale that, in a controversial discussion, there are authoritative users on both sides, as evidenced by a large degree in the graph. The measure captures the intuition of how likely a random user on either side is to be exposed to authoritative content from the opposing side.

Let $G(V, E)$ be the graph built by the first stage and its two partitions X and Y , ($X \cup Y = V$, $X \cap Y = \emptyset$) identified by the second stage of the pipeline. We first distinguish the k highest-degree vertices from each partition. High degree is a proxy for authoritativeness, as it means that a user has received a large number of endorsements on the specific topic. Subsequently, we select one partition at random (each with probability 0.5) and consider a random walk that starts from a random vertex in that partition. The walk terminates when it visits any high-degree vertex (from either side).

We define the Random Walk Controversy (RWC) measure as follows. “Consider two random walks, one ending in partition X and one ending in partition Y , RWC is the difference of the probabilities of two events: (i) both random walks started from the partition they ended in and (ii) both random walks started in a partition other than the one they ended in.” The measure is quantified as

$$RWC = P_{XX}P_{YY} - P_{YX}P_{XY}, \quad (2)$$

where P_{AB} , $A, B \in \{X, Y\}$ is the conditional probability

$$P_{AB} = \Pr[\text{start in partition } A \mid \text{end in partition } B]. \quad (3)$$

The aforementioned probabilities have the following desirable properties: (i) they are not skewed by the size of each partition, as the random walk starts with equal probability from each partition, and (ii) they are not skewed by the total degree of vertices in each partition, as the probabilities are conditional on ending in either partition (i.e., the fraction of random walks ending in each partition is irrelevant). RWC is close to one when the probability of crossing sides is low and close to zero when the probability of crossing sides is comparable to that of staying on the same side.

6.2 An Efficient Variant of the Random Walk Controversy Score

The most straightforward way to compute *RWC* is via Monte Carlo sampling. We use this approach in an earlier version of this work [20], with samples of 10,000 random walks. Nevertheless, collecting a large number of samples is computationally intensive and leads to slow evaluation of *RWC*. In this section, we propose a variant of *RWC* defined as a special case of a *random walk with restart*, thus leading to a much more efficient computation. This variant can handle cases where the random walker gets stuck (i.e., dangling vertices) by using restarts. This feature is important for two reasons: (i) Retweet graphs (one of our main considerations in this article) are inherently directed, hence the direction of endorsement should be taken into account, and (ii) since these directed graphs are very often starlike, there are a few authoritative users who generate information that spreads through the graph. Our previous Monte Carlo sampling does not take into consideration such graph structure, and the direction of information propagation, as the random walk process needs to be made ergodic for the sampling process to function.

To define the proposed variant of *RWC*, we assume there are two sides for a controversy, defined as two disjoint sets of vertices X and Y . In the original definition of the measure, we start multiple random walks from random vertices on either side, which terminate once they reach a high-degree vertex. For this variant of *RWC*, random walks do not terminate; rather they *restart* once they reach a high-degree vertex.

More formally, we consider two instances of a random walk with restart (RWR), based on whether they start (and restart) from X (start = X) or Y (start = Y). When start = X , the RWR has a restart vector uniformly distributed over X and zero for vertices in Y (the situation is symmetric for start = Y). Moreover, the random walk runs on a modified graph with all outgoing edges from high-degree vertices removed. This modification transforms the high-degree vertices into dangling vertices, hence forcing the random walk to restart once it reaches one of these vertices.⁸

To formally define this variant of *RWC*, let P_1 and P_2 be the stationary distributions of the RWR obtained for start = X and start = Y , respectively. We consider the conditional probability $Pr[\text{start} = A \mid \text{end} = B^+]$ that the random walk had started on side $A \in \{X, Y\}$, given that at some step at steady state it is found in one of the high-degree vertices of side $B \in \{X, Y\}$ (denoted as B^+). We thus consider the following four probabilities:

$$P_{X,X^+} = Pr[\text{start} = X \mid \text{end} = X^+] = \frac{\frac{|X|}{|V|} \sum_{v \in X^+} P_1(v)}{\frac{|X|}{|V|} \sum_{v \in X^+} P_1(v) + \frac{|Y|}{|V|} \sum_{v \in X^+} P_2(v)}, \quad (4)$$

$$P_{X,Y^+} = Pr[\text{start} = X \mid \text{end} = Y^+] = \frac{\frac{|X|}{|V|} \sum_{v \in Y^+} P_1(v)}{\frac{|X|}{|V|} \sum_{v \in Y^+} P_1(v) + \frac{|Y|}{|V|} \sum_{v \in Y^+} P_2(v)}, \quad (5)$$

$$P_{Y,Y^+} = Pr[\text{start} = Y \mid \text{end} = Y^+] = \frac{\frac{|Y|}{|V|} \sum_{v \in Y^+} P_2(v)}{\frac{|X|}{|V|} \sum_{v \in Y^+} P_1(v) + \frac{|Y|}{|V|} \sum_{v \in Y^+} P_2(v)}, \quad (6)$$

$$P_{Y,X^+} = Pr[\text{start} = Y \mid \text{end} = X^+] = \frac{\frac{|Y|}{|V|} \sum_{v \in X^+} P_2(v)}{\frac{|X|}{|V|} \sum_{v \in X^+} P_1(v) + \frac{|Y|}{|V|} \sum_{v \in X^+} P_2(v)}. \quad (7)$$

Notice that for the probabilities above we have

$$Pr[\text{start} = X \mid \text{end} = X^+] + Pr[\text{start} = Y \mid \text{end} = X^+] = 1$$

⁸To compute the stationary distribution of the random walks, we use the implementation of Personalized PageRank from NetworkX, retrieved from https://networkx.github.io/documentation/latest/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html.

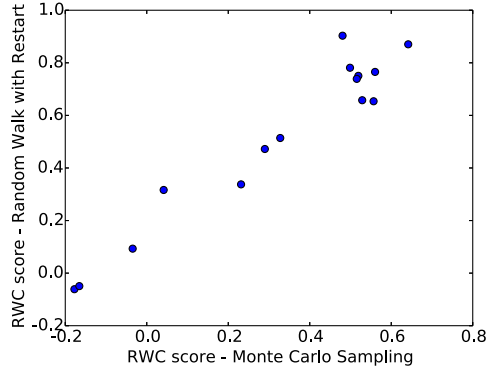


Fig. 5. Comparison between *RWC* scores computed via Monte Carlo sampling and those computed via RWR. Pearson's $r = 0.96$.

and

$$Pr[\text{start} = X \mid \text{end} = Y^+] + Pr[\text{start} = Y \mid \text{end} = Y^+] = 1,$$

as we ought to. The variant of the *RWC* score can be now defined as

$$RWC = P_{XX^+}P_{YY^+} - P_{XY^+}P_{YX^+}, \quad (8)$$

which, like the original version, intuitively captures the difference in the probability of staying on the same side and crossing the boundary.

To verify that the new variant of the score works as expected, we compare it to the original version of the score (obtained via Monte Carlo sampling). The results are shown in Figure 5, from which it can be clearly seen that the new variant is almost identical to the original one. However, for the datasets considered in this work, we found empirically that this algorithm based on random walk with restart is up to 200 times faster compared to the original Monte Carlo algorithm.

6.3 Betweenness

Let us consider the set of edges $C \subseteq E$ in the cut defined by the two partitions X, Y . This measure uses the notion of edge betweenness and how the betweenness of the cut differs from that of the other edges. Note that the cut here refers to the partitioning obtained using METIS, as described in Section 3. Recall that the betweenness centrality $bc(e)$ of an edge e is defined as

$$bc(e) = \sum_{s \neq t \in V} \frac{\sigma_{s,t}(e)}{\sigma_{s,t}}, \quad (9)$$

where $\sigma_{s,t}$ is the total number of shortest paths between vertices s, t in the graph and $\sigma_{s,t}(e)$ is the number of those shortest paths that include edge e .

The intuition here is that if the two partitions are well-separated, then the cut will consist of edges that bridge *structural holes* [7]. In this case, the shortest paths that connect vertices of the two partitions will pass through the edges in the cut, leading to high betweenness values for edges in C . On the other hand, if the two partitions are not well separated, then the cut will consist of *strong ties*. In this case, the paths that connect vertices across the two partitions will pass through one of the many edges in the cut, leading to betweenness values for C similar to the rest of the graph.

Given the distributions of edge betweenness on the cut and the rest of the graph, we compute the KL divergence d_{KL} of the two distributions by using kernel density estimation to compute the

PDF and sampling 10,000 points from each of these distributions (with replacement). We define the Betweenness Centrality Controversy (BCC) measure as

$$BCC = 1 - e^{-d_{KL}}, \quad (10)$$

which assumes values close to zero when the divergence is small and close to 1 when the divergence is large.

6.4 Embedding

This measure is based on a low-dimensional embedding of graph G produced by Gephi's ForceAtlas2 algorithm [28] (the same algorithm used to produce the plots in Figures 3 and 4). According to Noack [43], a force-directed embedding also maximizes modularity. Based on this observation, the two-dimensional layouts produced by this algorithm indicate a layout with maximum modularity.

Let us consider the two-dimensional embedding $\phi(v)$ of vertices $v \in V$ produced by ForceAtlas2. Given the partition X, Y produced by the second stage of the pipeline, we calculate the following quantities:

- d_X and d_Y , the average embedded distance among pairs of vertices in the same partition, X and Y , respectively;
- d_{XY} , the average embedded distance among pairs of vertices across the two partitions X and Y .

Inspired by the Davies-Bouldin (DB) index [12], we define the Embedding Controversy measure EC as

$$EC = 1 - \frac{d_X + d_Y}{2d_{XY}}. \quad (11)$$

EC is close to 1 for controversial topics, corresponding to better-separated graphs and thus to higher degree of controversy and close to zero for non-controversial topics.

6.5 Boundary Connectivity

This controversy measure was proposed by Guerra et al. [27] and is based on the notion of boundary and internal vertices. Let $u \in X$ be a vertex in partition X ; u belongs to the *boundary* of X iff it is connected to at least one vertex of the other partition Y , and it is connected to at least one vertex in partition X that is not connected to any vertex of partition Y . Following this definition, let B_X, B_Y be the set of boundary vertices for each partition and $B = B_X \cup B_Y$ the set of all boundary vertices. By contrast, vertices $I_X = X - B_X$ are said to be the *internal* vertices of partition X (similarly for I_Y). Let $I = I_X \cup I_Y$ be all internal vertices in either partition. The reasoning for this measure is that if the two partitions represent two sides of a controversy, then boundary vertices will be more strongly connected to internal vertices than to other boundary vertices of either partition. This intuition is captured in the formula

$$GMCK = \frac{1}{|B|} \sum_{u \in B} \frac{d_i(u)}{d_b(u) + d_i(u)} - 0.5, \quad (12)$$

where $d_i(u)$ is the number of edges between vertex u and internal vertices I , while $d_b(u)$ is the number of edges between vertex u and boundary vertices B . Higher values of the measure correspond to higher degrees of controversy.

6.6 Dipole Moment

This controversy measure was presented by Morales et al. [40] and is based on the notion of *dipole moment* that has its origin in physics. Let $R(u) \in [-1, 1]$ be a polarization value assigned to vertex $u \in V$. Intuitively, extreme values of R (close to -1 or 1) correspond to users who belong most clearly to either side of the controversy. To set the values $R(u)$, we follow the process described in the original article [40]: We set $R = \pm 1$ for the top-5% highest-degree vertices in each partition X and Y and set the values for the rest of the vertices by label propagation. Let n^+ and n^- be the number of vertices V with positive and negative polarization values, respectively, and ΔA the absolute difference of their normalized size $\Delta A = \left| \frac{n^+ - n^-}{|V|} \right|$. Moreover, let gc^+ (gc^-) be the average polarization value among vertices n^+ (n^-) and set d as half their absolute difference, $d = \frac{|gc^+ - gc^-|}{2}$. The dipole moment controversy measure is defined as

$$MBLB = (1 - \Delta A)d. \quad (13)$$

The rationale for this measure is that if the two partitions X and Y are well separated, then label propagation will assign different extreme (± 1) R -values to the two partitions, leading to higher values of the $MBLB$ measure. Note also that larger differences in the size of the two partitions (reflected in the value of ΔA) lead to decreased values for the measure, which takes values between zero and 1.

7 CONTROVERSY SCORES FOR USERS

The previous sections present measures to quantify the controversy of a conversation graph. In this section, we propose two measures to quantify the controversy of a single user in the graph. We denote this score as a real number that takes values in $[-1, 1]$, with 0 representing a neutral score and ± 1 representing the extremes for each side. Intuitively, the controversy score of a user indicates how “biased” the user is towards a particular side on a topic. For instance, for the topic “abortion,” pro-choice/pro-life activist groups tweeting consistently about abortion would get a score close to $-1/+1$ while average users who interact with both sides would get a score close to zero. In terms of the positions of users on the retweet graph, a neutral user would lie in the “middle,” retweeting both sides, where as a user with a high controversy score lies exclusively on one side of the graph.

RWC^{user} : The first proposed measure is an adaptation of RWC . As input, we are given a user $u \in V$ in the graph and a partitioning of the graph into two sides, defined as disjoint sets of vertices X and Y . We then consider a random walk that starts—and restarts—at the given user u . Moreover, as with RWC , the high-degree vertices on each side (X^+ and Y^+) are treated as dangling vertices; whenever the random walk reaches these vertices, it teleports to vertex u with probability 1 in the next step. To quantify the controversy of u , we ask how often the random walk is found on vertices that belong to either side of the controversy. Specifically, for each user u , we consider the conditional probabilities $Pr[\text{start} = u \mid \text{end} = X^+]$ and $Pr[\text{start} = u \mid \text{end} = Y^+]$ and estimate them by using the power iteration method. Assuming that user u belongs to side X of the controversy (i.e., $u \in X$), their controversy is defined as

$$RWC^{user}(u, X) = \frac{Pr[\text{start} = u \mid \text{end} = X^+]}{Pr[\text{start} = u \mid \text{end} = X^+] + Pr[\text{start} = u \mid \text{end} = Y^+]}. \quad (14)$$

Expected hitting time: The second proposed measure is also random-walk based but defined on the expected number of steps to hit the high-degree vertices on either side. Intuitively, a vertex is assigned a score of higher absolute value (closer to 1 or -1) if, compared to other vertices in the graph, it takes a very different time to reach a high-degree vertex on either side (X^+ or Y^+).

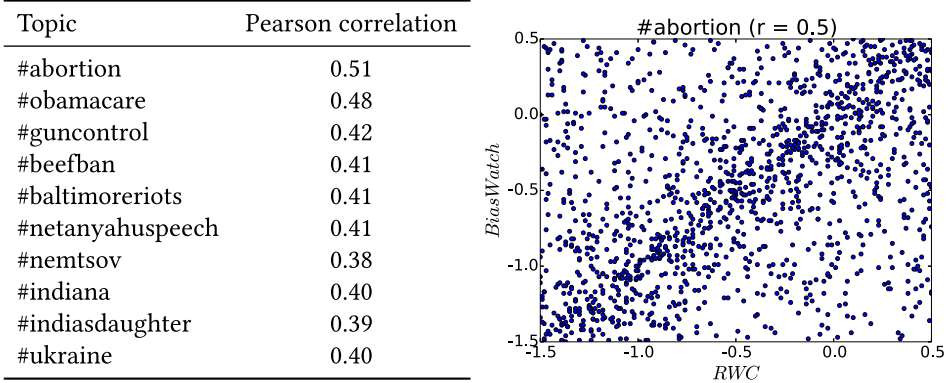


Fig. 6. (Left) Pearson's r between the scores obtained by our algorithm (Expected hitting time) and BiasWatch. (Right) Sample scatter plot for #abortion.

Specifically, for each vertex $u \in V$ in the graph, we consider a random walk that starts at u and estimate the expected number of steps l_u^X before the random walk reaches any high-degree vertex in X^+ . Considering the distribution of values of l_u^X across all vertices $u \in V$, we define $\rho^X(u)$ as the fraction of vertices $v \in V$ with $l_v^X < l_u^X$. We define $\rho^Y(u)$ similarly. Obviously, we have $\rho^X(u), \rho^Y(u) \in [0, 1)$. The controversy score of a user is then defined as

$$\rho(u) = \rho^X(u) - \rho^Y(u) \in (-1, 1). \quad (15)$$

Following this definition, a vertex that, compared to most other vertices, is very close to high-degree vertices X^+ will have $\rho^X(u) \approx 1$; and if the same vertex is very far from high-degree vertices Y^+ , it will have $\rho^Y(u) \approx 0$, leading to a controversy score $\rho(u) \approx 1 - 0 = 1$. The opposite is true for vertices that are far from X^+ but close to Y^+ , leading to a controversy score $\rho(u) \approx -1$.

7.1 Comparison with BiasWatch

BiasWatch [37] is a recently proposed, lightweight approach to compute controversy scores for users on Twitter. At a high level, the BiasWatch approach consists of the following steps:

- (1) Hand pick a small set of seed hashtags to characterize the two sides of a controversy (e.g., #prochoice vs. #prolife);
- (2) Expand the seed set of hashtags based on co-occurrence;
- (3) Use the two sets of hashtags, identify strong partisans in the graph (users with high controversy score);
- (4) Assign controversy scores to other users via a simple label propagation approach.

We compare the controversy scores obtained by our approaches to the ones obtained by BiasWatch⁹ on two sets of datasets: tweets matching the hashtags (i) #obamacare, #guncontrol, and #abortion, provided by Lu et al. [37], and (ii) the datasets in Table 2. We compute the Pearson correlation between our measure based on Expected hitting time and BiasWatch; the results are shown in Figure 6. We omit the comparison with RWC^{user} scores as they are almost identical to the ones by BiasWatch.

⁹For BiasWatch, we use parameters $\mu_1 = 0.1$, $\mu_2 = 0.4$, optimization method "COBYLA," cosine similarity threshold 0.4, and 10 nearest neighbors for hashtag extension.

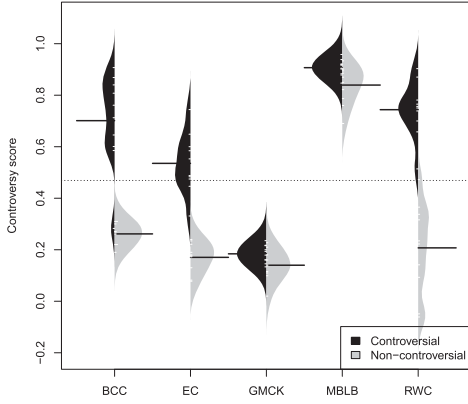


Fig. 7. Controversy scores on *retweet* graphs of various controversial and non-controversial datasets.

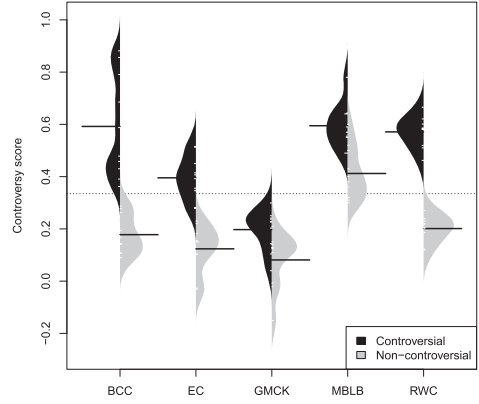


Fig. 8. Controversy scores on *follow* graphs of various controversial and non-controversial datasets.

The authors also provide datasets that contain human annotations for controversy score (in the range $[-2,2]$) for 500 randomly selected users. We discretize our controversy scores to the same range and compute the five-category Fleiss' κ value. The κ value is 0.35, which represents a “fair” level of agreement, according to Landis and Koch [36].

Our approach thus provides results that are similar to the state-of-the-art approach. Our method also has two advantages over the BiasWatch measure: (i) Even though we do not make use of any content information in our measure, we perform at par; and (ii) RWC^{user} provides an intuitive extension to our RWC measure. Given this unified framework, it is possible to design ways to reduce controversy, e.g., by connecting opposing views [21, 22], and such a unified formulation can help us define principled objective functions to approach these tasks.

8 EXPERIMENTS

In this section, we report the results of the various configurations of the pipeline proposed in this article. As previously stated, we omit results for the content and hybrid graph building approaches presented in Section 4, as they do not perform well. We instead focus on the retweet and follow graphs and test all the measures presented in Section 6 on the topics described in Table 2. In addition, we test all the measures on a set of external datasets used in previous studies [1, 10, 27] to validate the measures against a known ground truth. Finally, we use an evolving dataset from Twitter collected around the death of Venezuelan president Hugo Chavez [40] to show the *evolution* of the controversy measures in response to high-impact events.

To avoid potential overfitting, we use only eight graphs as testbed during the development of the measures, half of them controversial (beefban, nemtsov, netanyahu, russia_march) and half non-controversial (sxsw, germanwings, onedirection, ultralive). This procedure resembles a 40/60% train/test split in traditional machine learning applications.¹⁰

8.1 Twitter Hashtags

Figure 7 and Figure 8 report the scores computed by each measure for each of the 20 hashtags on the retweet and follow graph, respectively. Each figure shows a set of beanplots,¹¹ one for each

¹⁰A demo of our controversy measures can be found at <https://users.ics.aalto.fi/kiran/controversy>.

¹¹A beanplot is an alternative to the boxplot for visual comparison of univariate data among groups.

Table 3. Results on External Datasets

Dataset	V	E	C?	RWC	BCC	EC	GMCK	MLB
Political blogs	1222	16714	✓	0.42	0.53	0.49	0.18	0.45
Twitter politics	18470	48053	✓	0.77	0.79	0.62	0.28	0.34
Gun control	33254	349782	✓	0.70	0.68	0.55	0.24	0.81
Brazil soccer	20594	82421	✓	0.67	0.48	0.68	0.17	0.75
Karate club	34	78	✓	0.11	0.64	0.51	0.17	0.11
Facebook university	281	4389	✗	0.35	0.26	0.38	0.01	0.27
NYC teams	95924	176249	✗	0.34	0.24	0.17	0.01	0.19

The C? column indicates whether the previous study considered the dataset controversial (ground truth).

measure. Each beanplot shows the estimated probability density function for a measure computed on the topics, the individual observations are shown as small white lines in a one-dimensional scatter plot, and the median as a longer black line. The beanplot is divided into two groups, one for controversial topics (left/dark) and one for non-controversial ones (right/light). A larger separation of the two distributions indicates that the measure is better at capturing the characteristics of controversial topics. For instance, this separation is fundamental when using the controversy score as a feature in a classification algorithm.

Figures 7 and 8 clearly show that *RWC* is the best measure on our datasets. *BCC* and *EC* show varying degrees of separation and overlap, although *EC* performs slightly better as the distributions are more concentrated, while *BCC* has a very wide distribution. The two baselines *GMCK* and *MLB* instead fail to separate the two groups. Especially on the retweet graph, the two groups are almost indistinguishable.

For all measures, the median score of controversial topics is higher than for non-controversial ones. This result suggests that both graph building methods, retweet and follow, are able to capture the difference between controversial and non-controversial topics. Given the broad range of provenience of the topics covered by the dataset, and their different characteristics, the consistency of the results is very encouraging.

8.2 External Datasets

We have shown that our approach works well on a number of datasets extracted in-the-wild from Twitter. But how well does it generalize to datasets from different domains?

We obtain a comprehensive group of datasets kindly shared by authors of previous works: *Political blogs*, links between blogs discussing politics in the U.S. [1]; *Twitter politics*, Twitter messages pertaining to the 2010 midterm election in U.S. [10]; and the following five graphs used in the study that introduced *GMCK* [27]: (a) *Gun control*, retweets about gun control after the shooting at the Sandy Hook school; (b) *Brazil soccer*, retweets about two popular soccer teams in Brazil; (c) *Karate club*, the well-known social network in Reference [50]; (d) *Facebook university*, a social graph among students and professors at a Brazilian university; and (e) *NYC teams*, retweets about two New York City sports teams.

Table 3 shows a comparison of the controversy measures under study on the aforementioned datasets.¹² For each dataset, we also report whether it was considered controversial in the original article, which provides a sort of “ground truth” to evaluate the measures against.

¹²The datasets provided by Guerra et al. [27] are slightly different from the ones used in the original article because of some irreproducible filtering used by the authors. We use the datasets provided to us verbatim.

All the measures are able to distinguish controversial graphs to some extent, in the sense that they return higher values for the controversial cases. The only exception is Karate club. Both *RWC* and *MBLB* report low controversy scores for this graph. It is possible that the graph is too small for such random-walk-based measures to function properly. Conversely, *BCC* is able to capture the desired behavior, which suggests that shortest-path and random-walk-based measures might have a complementary function.

Interestingly, while the Political blogs dataset is often considered a gold standard for polarization and division in online political discussions, all the measures agree that it presents only a moderate level of controversy. Conversely, the Twitter politics dataset is clearly one of the most controversial across all measures. This difference suggests that the measures are more geared towards capturing the dynamics of controversy as it unfolds on social media, which might differ from more traditional blogs. For instance, one such difference is the *cost* of an endorsement: placing a link on a blog post arguably consumes more mental resources than clicking on the retweet button.

For the Gun control dataset, Guerra et al. need to manually distinguish three different partitions in the graph: gun rights advocates, gun control supporters, and moderates. Our pipeline is able to find the two communities with opposing views (grouping together gun control supporters and moderates, as suggested in the original study) without any external help. All measures agree with the conclusions drawn in the original article that this topic is highly controversial.

Note that even though, from the results in Table 3, *RWC*, *BCC*, and *EC* appear to outperform each other, this is not the case. These methods are not comparable, meaning that a score of 0.5 for *RWC* is not the same as a 0.5 for *BCC*. The insight we can draw from these results is that our methods are able to discern a controversial topic from a non-controversial one consistently, irrespective of the domain, and are able to do so more reliably than existing methods (*GMCK* and *MBLB*).

8.3 Evolving Controversy

We have shown that our approach also generalizes well to datasets from different domains. But in a real deployment the measures need to be computed continuously, as new data arrives. How well does our method work in such a setting? And how do the controversy measures evolve in response to high-impact events?

To answer these questions, we use a dataset from the study that introduced *MBLB* [40]. The dataset comprises Twitter messages pertaining to political events in Venezuela around the time of the death of Hugo Chavez (February–May 2013). The authors built a retweet graph for each of the 56 days around the day of the death (one graph per day).

Figure 9 shows how the intensity of controversy evolves according to the measures under study (which occurs on day D). The measure proposed in the original article, *MBLB*, which we use as “ground truth,” shows a clear decrease of controversy on the day of the death, followed by a progressive increase in the controversy of the conversation. The original interpretation states that on the day of the death a large amount of people, also from other countries, retweeted news of the event, creating a single global community that got together at the shock of the news. After the death, the ruling and opposition parties entered into a fiery discussion over the next elections, which increased the controversy.

All the measures proposed in this work show the same trend as *MBLB*. Both *RWC* and *EC* follow very closely the original measure (Pearson correlation coefficients r of 0.944 and 0.949, respectively), while *BCC* shows a more jagged behavior in the first half of the plot ($r = 0.743$), due to the discrete nature of shortest paths. All measures, however, present a dip on day D, an increase in controversy in the second half, and another dip on day D+20. Conversely, *GMCK* reports an almost constant moderate value of controversy during the whole period ($r = 0.542$),

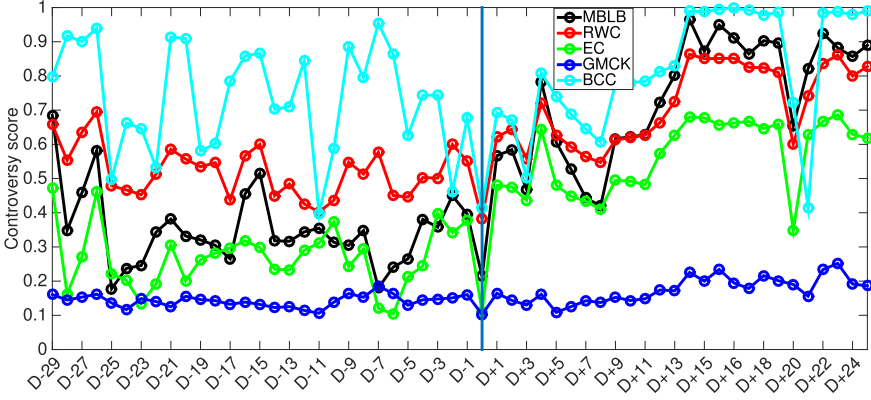


Fig. 9. Controversy scores on 56 retweet graphs from Morales et al. Day D (indicated by the blue vertical line) indicates the announcement of the death of president Hugo Chavez.

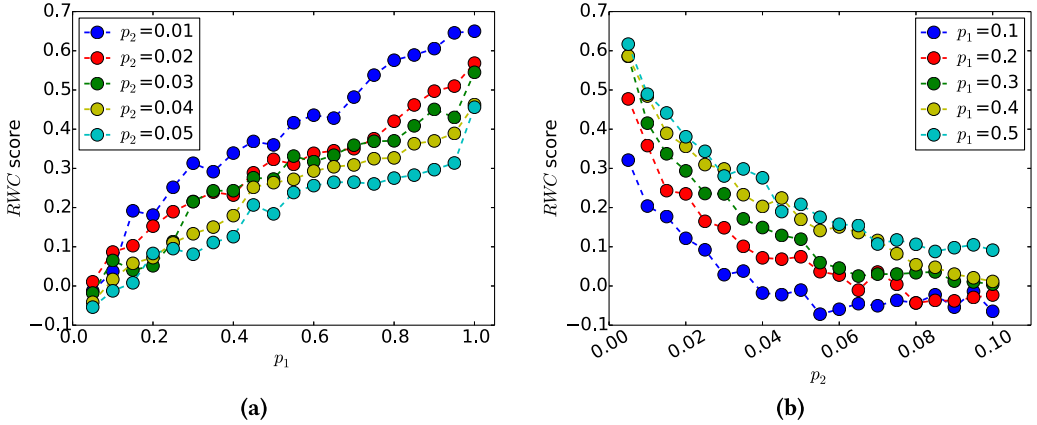


Fig. 10. *RWC* scores for synthetic Erdős-Rényi graphs planted with two communities. p_1 is the intra-community edge probability, while p_2 is the inter-community edge probability.

with barely noticeable peaks and dips. We conclude that our measures generalize well also to the case of evolving graphs and behave as expected in response to high-impact events.

8.4 Simulations

Given that *RWC* is the best-performing score among the ones in this study, we focus our attention solely on it henceforth. To measure the robustness of the *RWC* score, we generate random Erdős-Rényi graphs with varying community structure and compute the *RWC* score on them. Specifically, to mimic community structure, we plant two separate communities with intra-community edge probability p_1 . That is, p_1 defines how dense these communities are within themselves. We then add random edges between these two communities with probability p_2 . Therefore, p_2 defines how connected the two communities are. A higher value of p_1 and a lower value of p_2 create a clearer two-community structure.

Figure 10 shows the *RWC* score for random graphs of 2000 vertices for two different settings: plotting the score as a function of p_1 while fixing p_2 (Figure 10(a)) and vice versa (Figure 10(b)).

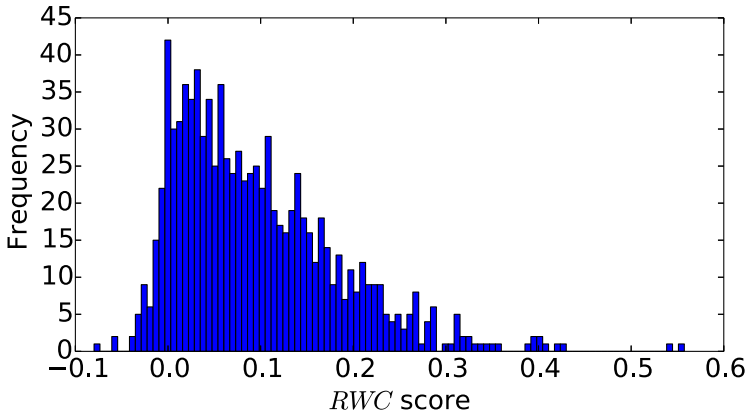


Fig. 11. Frequency of *RWC* scores for hashtags trending from June to September 2015.

The *RWC* score reported is the average over 10 runs. We observe a clear pattern: the *RWC* score increases as we increase the density within the communities and decreases as we add noise to the community structure. The effects of the parameters is also expected, for a given value of p_1 , a smaller value of p_2 generates a larger *RWC* score, as the communities are more well separated. Conversely, for a given value of p_2 , a larger value of p_1 generates a larger *RWC* scores, as the communities are denser.

8.5 Controversy Detection in the Wild

In most of the experiments presented so far, we hand-picked known topics that are controversial and showed that our method is able to separate them from the non-controversial topics. To check whether our system works in a real-world setting, we deploy it in the wild to explore actual topics of discussion on Twitter and detect the ones that are controversial. More specifically, we obtain daily trending hashtags (both U.S. and worldwide) on the platform for a period of three months (June 25–September 19, 2015). Then, we obtain all tweets that use these hashtags and create retweet graphs (as described in Section 4). Finally, we apply the *RWC* measure on these conversation graphs to identify controversial hashtags.

The results can be explored in our online demo [19].¹³ To mention a few examples, our system was able to identify the following controversial hashtags:

- #whosiburningblackchurches (score 0.332): a hashtag about the burning of predominantly black churches.¹⁴
- #communityshield (score 0.314): discussion between the fans of two sides of a soccer game.¹⁵
- #nationalfriedchickenday (score 0.393): a debate between meat lovers and vegetarians about the ethics of eating meat.

Moreover, based on our experience with our system, most hashtags that are reported as trending on Twitter concern topics that are not controversial. Figure 11 shows the histogram of the *RWC*

¹³<https://users.ics.aalto.fi/kiran/controversy/table.php>.

¹⁴<https://erlc.com/article/explainer-whoisburningblackchurches>.

¹⁵https://en.wikipedia.org/wiki/2015_FA_Community_Shield.

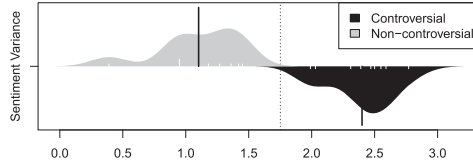


Fig. 12. Sentiment variance controversy score for controversial and non-controversial topics.

score over the 924 trending hashtags we collected. A majority of these hashtags have an *RWC* score around zero.

9 CONTENT

In this section, we explore alternative approaches to measuring controversy that use only the content of the discussion rather than the structure of user interactions. As such, these methods do not fit in the pipeline described in Section 3. The question we address is “does content help in measuring the controversy of a topic?” In particular, we test two types of features extracted from the content. The first is a typical IR-inspired bag-of-words representation. The second involves sentiment-related features, extracted with Natural language processing (NLP) tools.

9.1 Bag of Words

We take as input the raw content of the social media posts—in our case, the tweets pertaining to a specific topic. We represent each tweet as a vector in a high-dimensional space composed of the words used in the whole topic, after standard preprocessing used in IR (lowercasing, stopword removal, stemming). Following the lines of our main pipeline, we group these vectors in two clusters by using CLUTO [31] with cosine distance.

The underlying assumption is that the two sides, while sharing the use of the hashtag for the topic, use different vocabularies in reference to the issue at hand. For example, for #beefban, a side may be calling for “freedom” while the opposing one for “respect.” We use KL divergence as a measure of distance between the vocabularies of the two clusters, and the I2 measure [38] of clustering heterogeneity.

We use an unpaired Wilcoxon rank-sum test at the $p = 0.05$ significance level, but we are unable to reject the null hypothesis that there is no difference in these measures between the controversial and non-controversial topics. Therefore, there is not enough signal in the content representation to discern between controversial and non-controversial topics with confidence. This result suggests that the bag-of-words representation of content is not a good basis for our task. It also agrees with our earlier attempts to use content to build the graph used in the pipeline (see Section 4, which suggests that using content for the task of quantifying controversy might not be straightforward).

9.2 Sentiment Analysis

Next, we resort to NLP techniques for sentiment analysis to analyze the content of the discussion. We use SentiStrength [48] trained on tweets to give a sentiment score in $[-4, 4]$ to each tweet for a given topic. In this case, we do not try to cluster tweets by their sentiment. Rather, we analyze the difference in distribution of sentiment between controversial and non-controversial topics.

While it is not possible to say that controversial topics are more positive or negative than non-controversial ones, we can detect a difference in their variance. Indeed, controversial topics have a higher variance than non-controversial ones, as shown in Figure 12. Controversial ones have a variance of at least 2, while non-controversial ones have a variance of at most 1.5.

Table 4. Summary of Various Graph Building and Controversy Measures Tried

Graphs	Retweet
	Follow
	Content
	Mention
	Hybrid (content + retweet, mention + retweet)
Measures	Random Walk
	Edge Betweenness
	Embedding
	Boundary Connectivity
	Dipole Moment
	Cut-based Measures (conductance, cut ratio)
	Sentiment Analysis
	Modularity
	SPID

Methods that worked reliably are in bold.

In practice, the “tones” with which controversial topics are debated are stronger, and sentiment analysis is able to detect this. While this signal is clear, it is not straightforward to incorporate it into the measures based on graph structure. Moreover, this feature relies on technologies that do not work reliably for languages other than English and hence cannot be applied for topics such as #russia_march.

10 DISCUSSION

The task we tackle in this work is certainly not an easy one, and this study has some limitations, which we discuss in this section. We also report a set of negative results that we produced while coming up with the measures presented. We believe these results will be very useful in steering this research topic towards a fruitful direction. Table 4 provides a summary of the various graph building strategies and controversy measures we tried for quantifying controversy.

10.1 Limitations

Twitter only. We present our findings mostly on datasets coming from Twitter. While this is certainly a limitation, Twitter is one of the main venues for online public discussion and one of the few for which data are available. Hence, Twitter is a natural choice. In addition, our measures generalize well to datasets from other social media and the Web.

Choice of data. We manually pick the controversial topics in our dataset, which might introduce bias. In our choice, we represent a broad set of typical controversial issues coming from religious, societal, racial, and political domains. Unfortunately, ground truths for controversial topics are hard to find, especially for ephemeral issues. However, the topics are unanimously judged controversial by the authors. Moreover, the hashtags represent the intuitive notion of controversy that we strive to capture, so human judgement is an important ingredient we want to use.

Overfitting. While this work presents the largest systematic study on controversy in social media so far, we use only 20 topics for our main experiment. Given the small number of examples, the risk of overfitting our measures to the dataset is real. We reduce this risk by using only 40% of the

topics during the development of the measures. Additionally, our measures agree with previous independent results on external datasets, which further decreases the likelihood of overfitting.

Reliance on graph partitioning. Our pipeline relies on a graph partitioning stage, whose quality is fundamental for the proper functioning of the controversy measures. Given that graph partitioning is a hard but well-studied problem, we rely on off-the-shelf techniques for this step. A measure that bypasses this step entirely is highly desirable, and we report a few unsuccessful attempts in the next subsection.

Multisided controversies. Not all controversies involve only two sides with opposing views. Some times discussions are multifaceted, or there are three or more competing views on the field. The principles behind our measures neatly generalize to multisided controversies. However, in this case, the graph partitioning component needs to automatically find the optimal number of partitions. We defer experimental study of such cases to an extended version of this article.

Evaluation. Defining what is controversial/polarized can be subjective. There are many ways to define what is controversial, depending on the context, subject, and field of study, e.g., see Reference [6] for around a dozen ways to define polarization. Our evaluation is based on our intuitive labelling that a topic is controversial/polarized. This might not always be true, but given that the alternative is to hand-label/survey the thousands of users, we presume that this assumption is reasonable for developing methods that can be adapted to large scale systems.

10.2 Negative Results

We briefly review a list of methods that failed to produce reliable results and were discarded early in the process of refining our controversy measures.

Mentions graph. Conover et al. [10] rely on the mention graph in Twitter to detect controversies. However, in our dataset the mention graphs are extremely sparse given that we focus on short-lived events. Merging the mentions into the retweet graph does not provide any noticeable improvement.

Previous studies have also shown that people retweet similar ideologies but mention across ideologies [5]. We exploit this intuition by using correlation clustering for graph partitioning, with negative edges for mentions. Alas, the results are qualitatively worse than those obtained by METIS.

Cuts. Simple measures such as size of the cut of the partitions do not generalize across different graphs. Conductance (in all its variants) also yields poor results. Prior work identifies controversies by comparing the structure of the graph with randomly permuted ones [10]. Unfortunately, we obtain equally poor results by using the difference in conductance with cuts obtained by METIS and by random partitions.

Community structure. Good community structure in the conversation graph is often understood as a sign that the graph is polarized or controversial. However, this is not always the case. We find that both assortativity and modularity (which have been previously used to identify controversy) do not correlate with the controversy scores and are not good predictors for how controversial a topic is. The work by Guerra et al. [27] presents clear arguments and examples of why modularity should be avoided.

Partitioning. As already mentioned, bypassing the graph partitioning to compute the measure is desirable. We explore the use of the all pairs expected hitting time computed by using SimRank [30]. We compute the SPID (ratio of variance to mean) of this distribution, however results are mixed.

10.3 Conclusions

In this article, we performed the first large-scale systematic study for quantifying controversy in social media. We have shown that previously used measures are not reliable and demonstrated that controversy can be identified both in the retweet and topic-induced follow graph. We have also shown that simple content-based representations do not work in general, while sentiment analysis offers promising results.

Among the measures we studied, the random-walk-based *RWC* most neatly separates controversial topics from non-controversial ones. Besides, our measures gracefully generalize to datasets from other domains and previous studies.

This work opens several avenues for future research. First, it is worth exploring alternative approaches and testing additional features, such as following a generative-model-based approach or exploiting the temporal evolution of the discussion of a topic [23].

From the application point of view, the controversy score can be used to generate recommendations that foster a healthier “news diet” on social media. Given the ever-increasing impact of polarizing figures in our daily politics and the rise in polarization in the society [13, 24], it is important to not restrict ourselves to our own “bubbles” or “echo chambers” [44, 47]. Our methods for identifying controversial topics can be used as building blocks for designing such systems to reduce controversy on social media [21, 22] by connecting social media users with content outside their own bubbles.

Finally, polarization by itself may not be a wholly negative phenomenon. Several studies [11, 42] argue that a democracy needs deliberation, and polarization enables such a deliberation to happen in the public, to a certain extent, thus informing people about the issues and arguments from different sides. Given such a setting, it is of paramount importance to understand to what extent a discussion is polarized, so that things do not spiral out of control or create isolated echo chambers. Our article contributes methods that are useful in this setting and enables measuring the degree of polarization of a topic in a domain-agnostic fashion.

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