

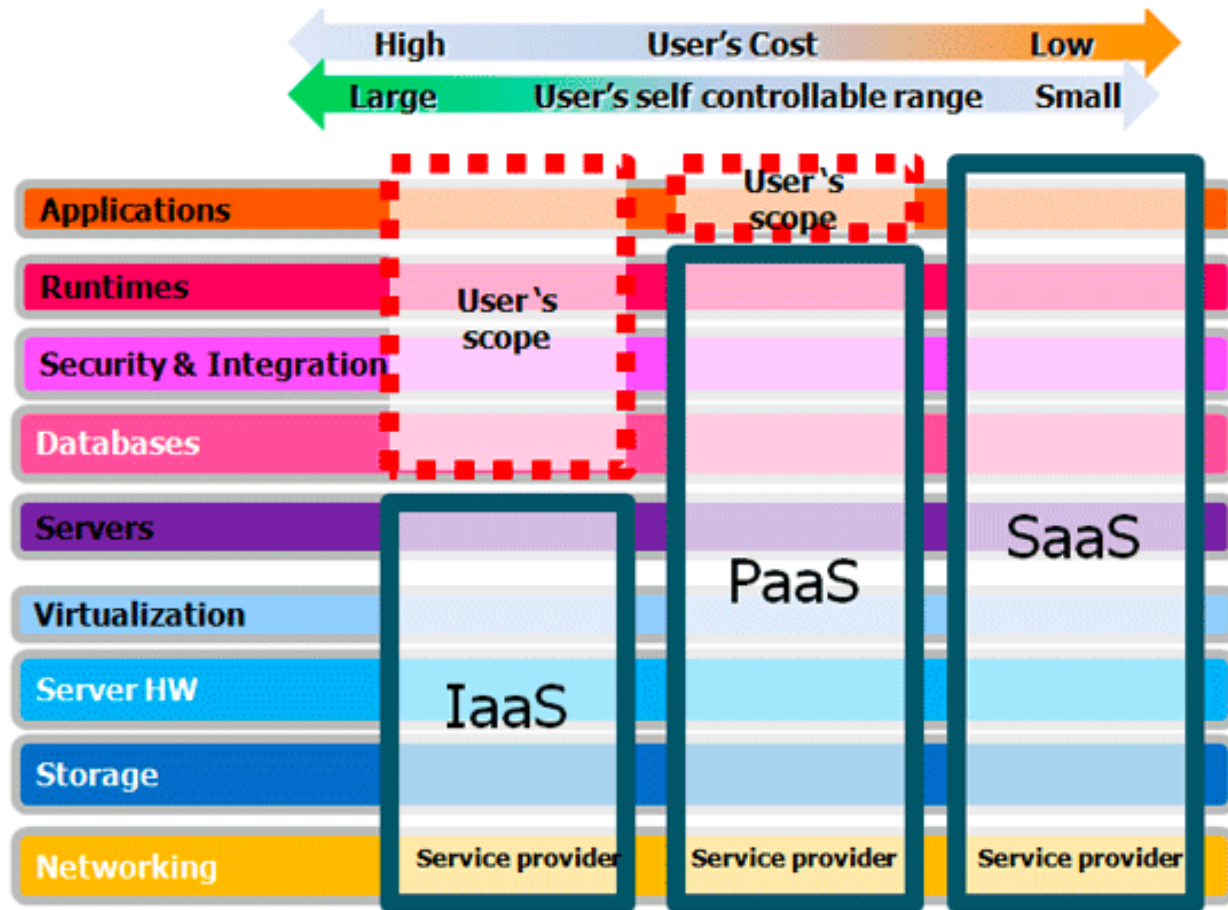
Object-Oriented Programming

Programming Project #2

郭建志

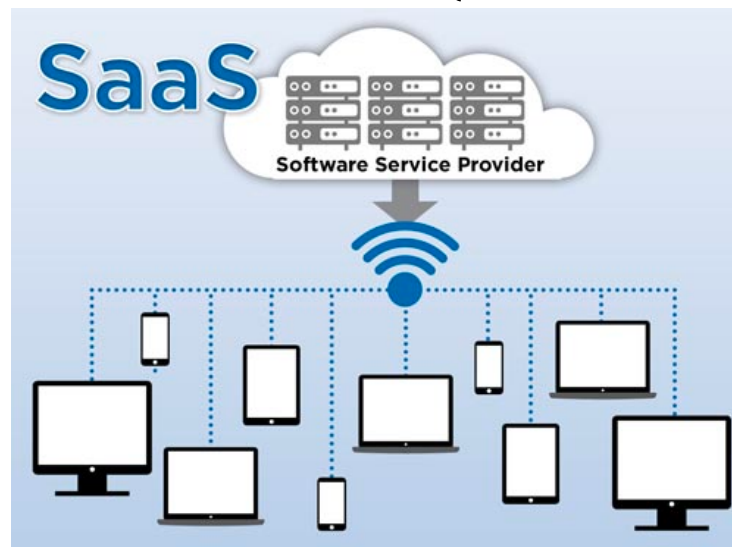
Background

- Cloud services can be broadly divided into main three models
- Infrastructure-as-a-Service (**IaaS**)
- Platform-as-a-Service (**PaaS**)
- Software-as-a-Service (**SaaS**)



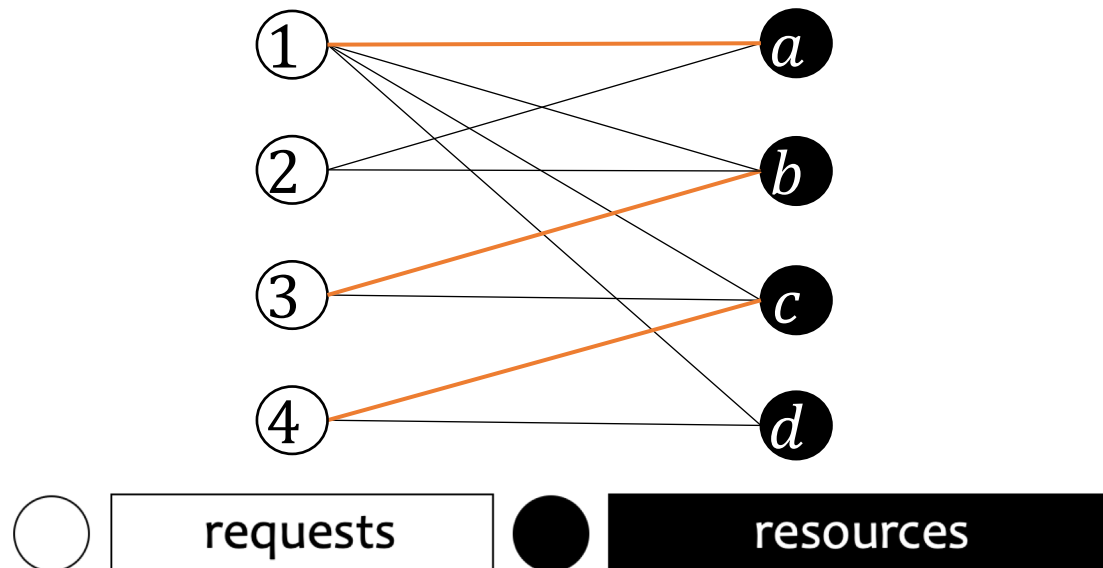
Background

- Service providers have resources (such as virtual infrastructures, virtual platform, service software) and users request the resources for services
- For example, Google constructs data centers and maintain the hardware and software to provide the mail service for users (i.e., Gmail)



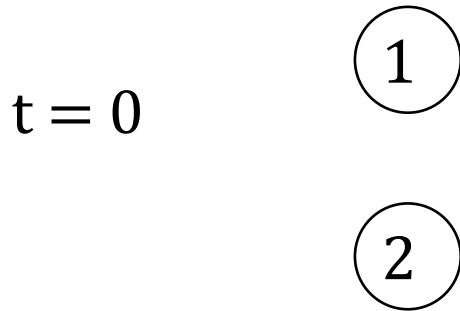
Background

- Resource allocation can be modeled as a bipartite matching problem
- But resource allocation is usually **dynamic**
- Some request arrives and some resources are released at a time



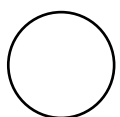
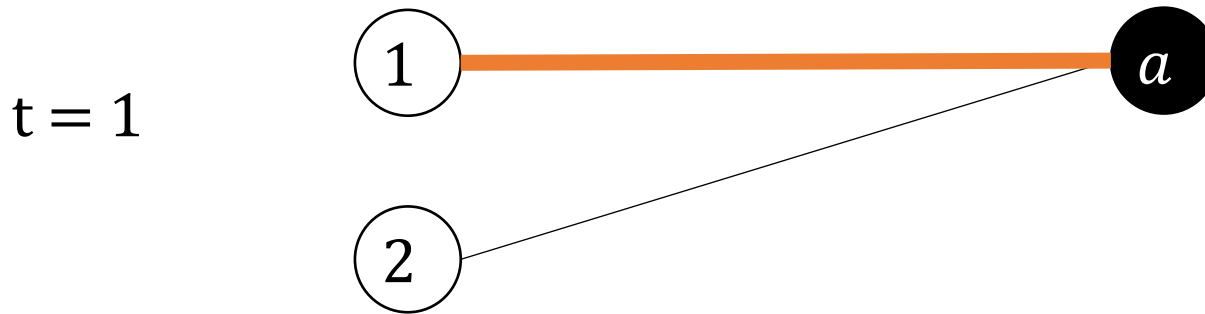
Online Bipartite Matching Problem (BMP)

- Consider a scenario, where some request arrives and some resources are released at a time:

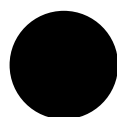


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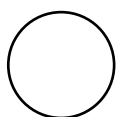
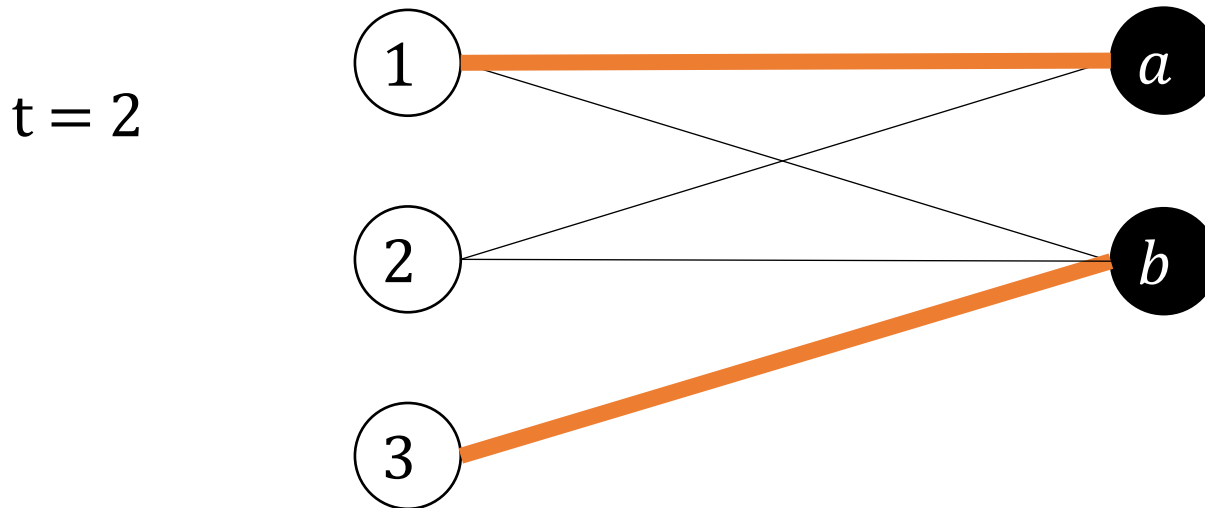
requests



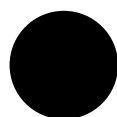
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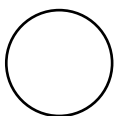
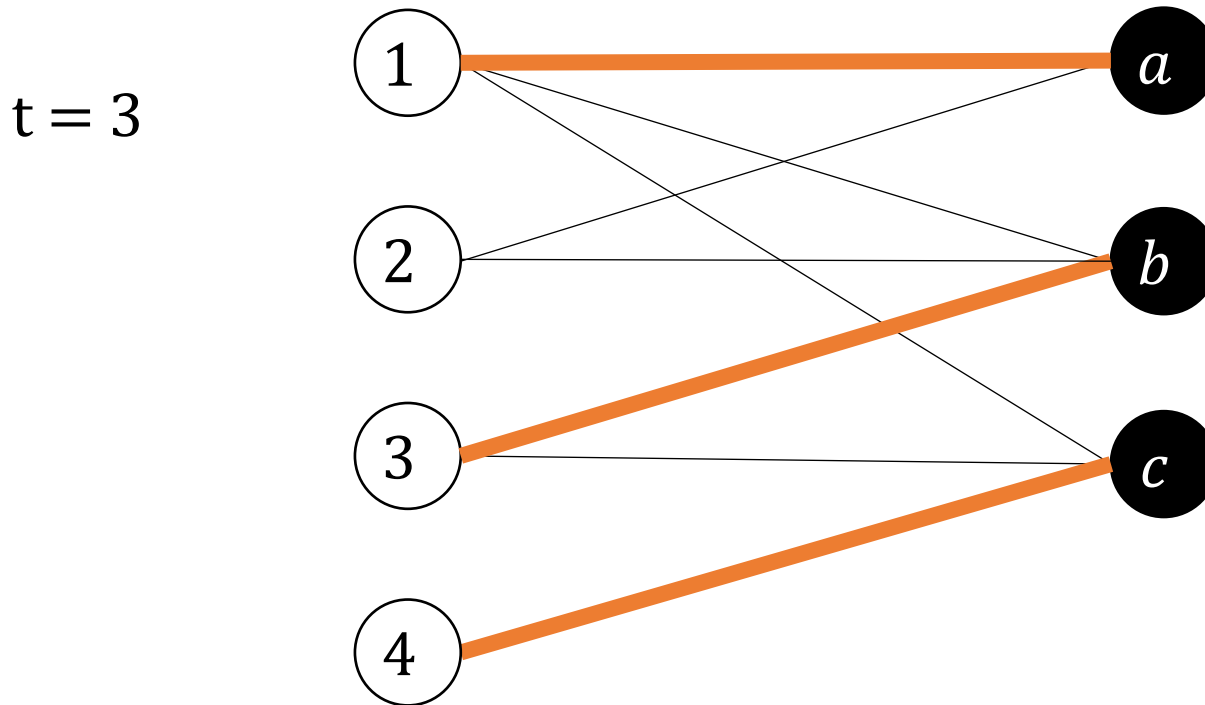
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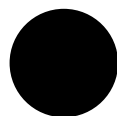
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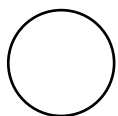
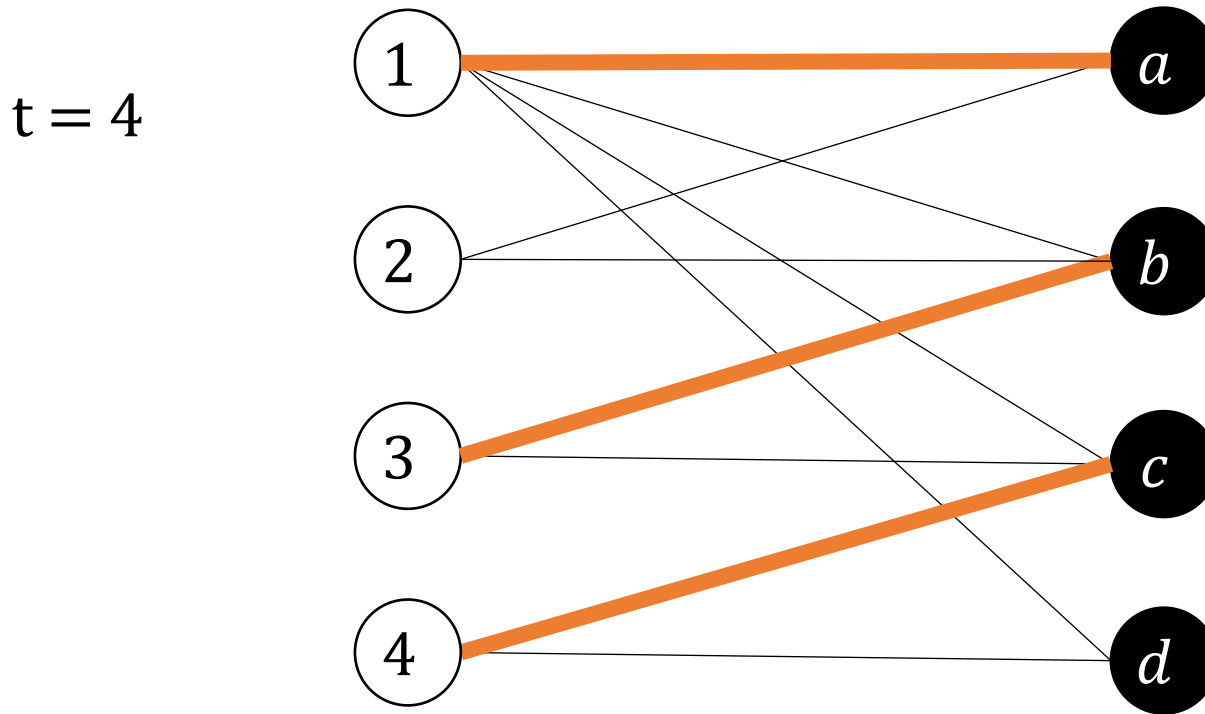
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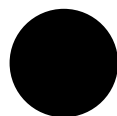
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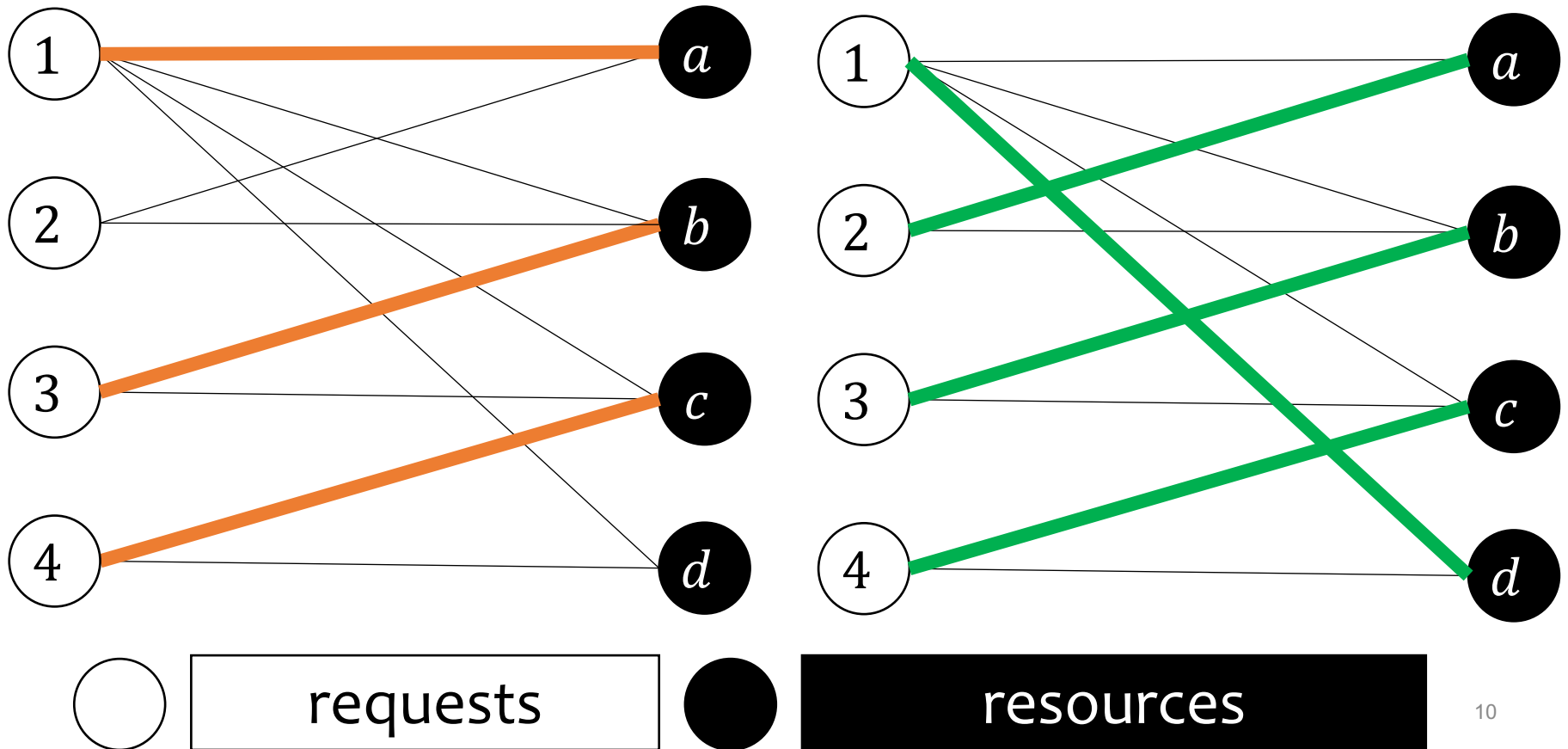
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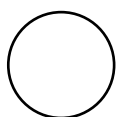
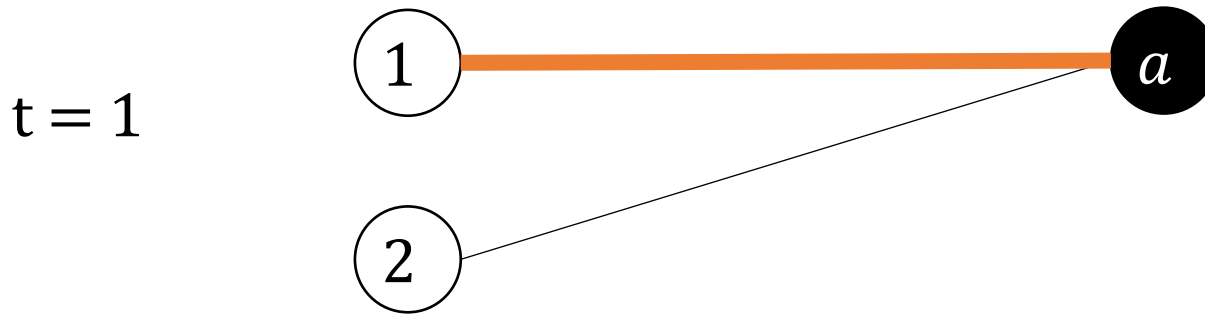
Online Bipartite Matching Problem (BMP)

- Compared with the offline optimal solution

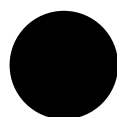


Hardness of the Online BMP

- If your algorithm is deterministic



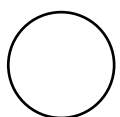
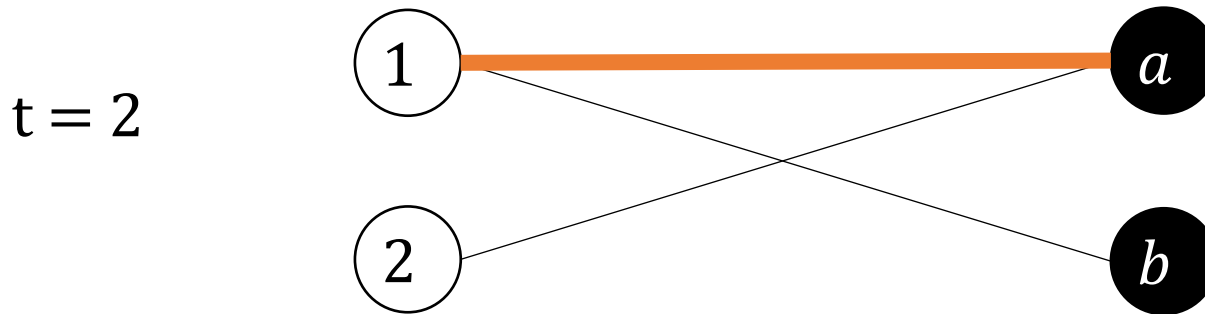
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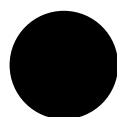
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Hardness of the Online BMP

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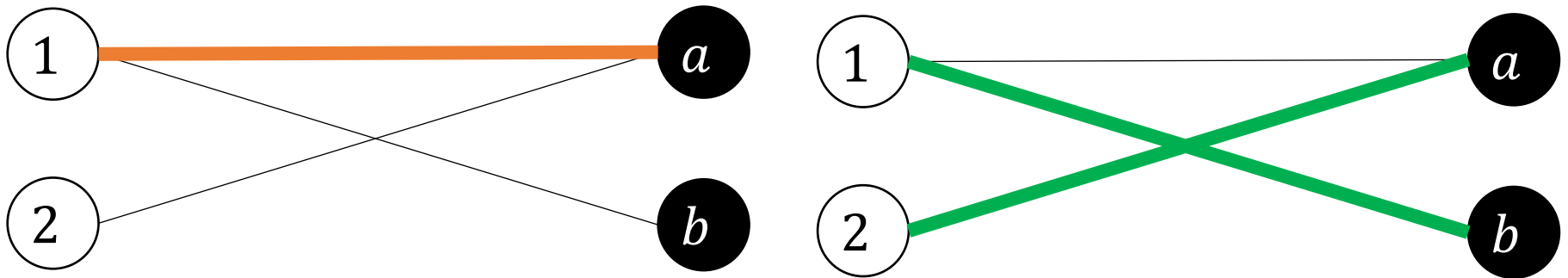
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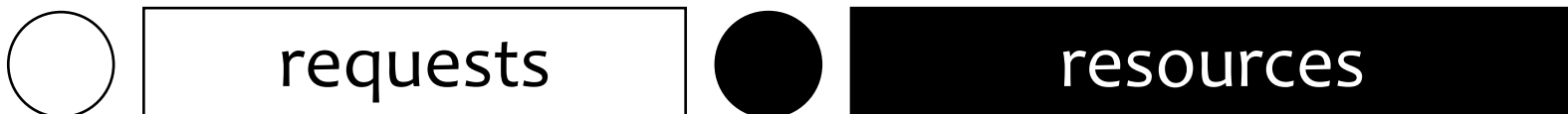
resources

Hardness of the Online BMP

- Compared with the offline optimal solution



- No deterministic algorithm can bound the ratio larger than $1/2$



Programming Project #2:

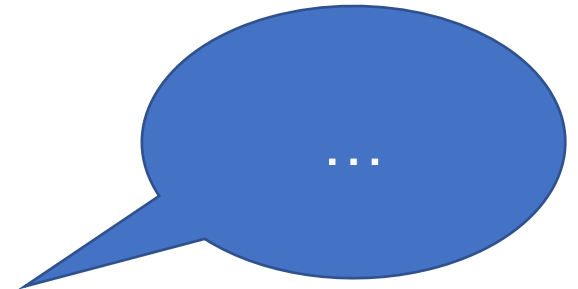
Online resource allocation

- Input:
 - # time slots
 - Time slot ID, # requests, # resources, request IDs, and resource IDs at the time slot
 - Number of edges and edges between a request ID and a resource ID at the time slot
- Procedure:
 - Assign the resource to a request at the time slot when the resource is released
- Output:
 - # assigned pairs
 - The time slot
- The grade is proportional to # assigned pairs

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騙我了嗎

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沒錯!

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- Implement a designated randomized algorithm

Programming Project #2:

Online resource allocation

- **Designated Algorithm:**

1. For each time slot:
2. Uniform-randomly assign a value in $[0, 1]$ for each arrival requests
3. Assign the available resource with the smallest ID to the unsatisfied request with the maximum random value
4. Repeat step 3 until there is no available resource
5. Go to step 1 for the next time slot

- **Note:**

1. Use default_random_engine and uniform_real_distribution
2. Let the random seed be a parameter of main function
3. Define classes Resource and Request, and use vector to store the objects of class Resource and Request
4. Generate new resource and request by push_back
5. Design static member variables and static member functions to count and get the number of satisfied requests

Programming Project #2:

Online resource allocation

// You need forward declaration

```
class Resource{
    int id;
    bool matched;
    int requestId;
public:
    // constructors...
    bool operator->* (Request &b){...}
    // ->* check whether both of them are un-matched.
    // If they are, then match them and return true;
    // otherwise, return false
    // accessor
};
class Request{
    int id;
    bool matched;
    int resourceId;
    double weight; // a random value, indicates the priority
public:
    // constructors...
    friend class Resource;
    // accessor
};
```

Discussion

- Why does the randomized algorithm work?
- What can be added to improve the performance?
- Discussion & bonus

Discussion

- Why does the randomized algorithm work?
- It can avoid **being stuck in the trap of adversary**
- Adversary: deliberately choose difficult data to maximize the gap between the generated solution and the offline optimum
- What can be added to improve the performance?
- Distribution of the input
- Discussion & bonus

Further Reading

- Randomized primal-dual analysis of RANKING for online bipartite matching, in SODA 2013
- Online stochastic matching beating $1-1/e$, in FOCS 2009
- ...
- 演算法頂尖研討會: STOC, FOCS, SODA...
- 一個字, 神

Input Sample: request.txt

Format:

#timeSlots

timeSlotID1	#requests	#resources
-------------	-----------	------------

requestID1	requestID2	...
------------	------------	-----

resourceID1	resourceID2	...
-------------	-------------	-----

#edges

edgeID1	requestID	resourceID
---------	-----------	------------

edgeID2	...
---------	-----

timeSlotID2...

之後揭曉，先自己設計input

Output Sample: result.txt

Format:

#satisfiedRequests

requestID resourceID

...

下次揭曉，用自己設計input產生答案

Input Sample: request.txt

Format:

3
0 5 2
0 1 2 3 4
0 1
3
0 3 0
1 0 1
2 4 1
1 1 1
5
2
2
3 0 2
4 4 2

2 3 3
6 7 8
3 4 5
9
5 0 3
6 1 3
7 3 3
8 6 3
9 8 3
10 5 4
11 2 5
12 4 5
13 5 5

Format:

#timeSlots
timeSlotID1 #requests #resources
requestID1 requestID2 ...
resourceID1 resourceID2 ...
#edges
edgeID1 requestID resourceID
edgeID2 ...
timeSlotID2...

Output Sample: result.txt

Format:

6
0 2
2 5
3 0
4 1
5 4
8 3

Format:

#satisfiedRequests
requestID resourceID
...

Note

- Deadline: 4/16 Tue
- 小老師deadline: 4/2 Tue (暫定)
- E-course
- **C++ Source code**
- Show a good programming style