CSC148 term test #2, L0101/L0301

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Three questio	ns:
Q1:	/ 5
Q2:	/ 6
Q3:	/ 9

1. (5 pts) Consider a post-order traversal, i.e. visiting each node in post-order, of a Binary Search Tree, with the act function defined as;

```
def act(node):
    print(node.value, end=' ') # prints all on the same line
```

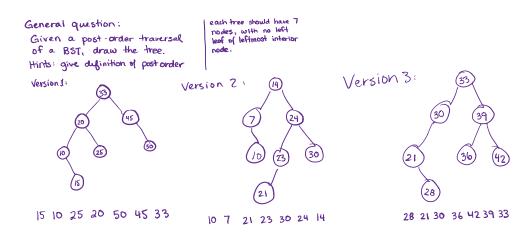
Recall that for a BST, a postorder traversal first visits the left subtree in postorder, then the right subtree in postorder, and finally the root.

Draw a representation of a Binary Search Tree that would produce the following output when traversed as described above.

```
15 10 25 20 50 45 33
```

Hint: Recall that both postorder traversals and the Binary Search Tree property are defined recursively, so that they apply at the root of the main tree and of each subtree...

sample solution: Below are solutions for all three test versions (9/10 a.m., 1 p.m., 6 p.m.)



Use the recursive definitions of both postorder traversals and the BST property to help.

2. (6 pts) Read the definition of class Tree below, from module tree. Notice that a Tree's children is a list of 0 or more Tree objects, and does not contain any None objects. Also, the only functions or methods you may rely are on are below.

Implement function count_at_depth on the next page. You may implement helper functions, if you wish, or implement it as one function.

```
class Tree:
   A bare-bones Tree ADT that identifies the root with the entire tree.
   def __init__(self, value=None, children=None):
       Create Tree self with content value and 0 or more children
       @param Tree self: this tree
       Oparam object value: value contained in this tree
       @param list[Tree] children: possibly-empty list of children
       Ortype: None
       self.value = value
       # copy children if not None
       self.children = children.copy() if children is not None else []
   def __str__(self, indent=0):
       Produce a user-friendly string representation of Tree self,
       indenting each level as a visual clue.
       Oparam Tree self: this tree
       Oparam int indent: amount to indent each level of tree
       Ortype: str
       >>> t = Tree(17)
       >>> print(t)
       17
       >>> t1 = Tree(19, [t, Tree(23)])
       >>> print(t1)
       19
          17
       >>> t3 = Tree(29, [Tree(31), t1])
       >>> print(t3)
       29
          19
              17
              23
       root_str = indent * " " + str(self.value)
       return '\n'.join([root_str] +
                         [c.__str__(indent + 3) for c in self.children])
```

```
from tree import Tree
def count_at_depth(t, d):
    """ Return the number of nodes at depth d of t.
    Oparam Tree t: tree to explore --- cannot be None
    Oparam int d: depth to report from, non-negative
    Ortype: int
    >>> t = Tree(17, [Tree(0), Tree(1, [Tree(4)]), Tree(2, [Tree(5)]), Tree(3)])
    >>> print(t)
    17
        0
        1
        2
           5
        3
    >>> count_at_depth(t, 0)
    >>> count_at_depth(t, 1)
    >>> count_at_depth(t, 2)
    >>> count_at_depth(t, 5)
    11 11 11
    # Hint: Any node that is at depth d from t is at depth d-1 from t's children.
sample solution(s): All three versions below.
        if d < 0:
           return 0
        elif d == 0:
            return 1
            return sum([count_at_depth(c, d - 1)
                       for c in t.children
                       if c is not None])
    def sum_at_depth(t, d):
        """ Return the sum of node values at depth d of t.
        Assume that node values are integers and that there are no
        None values in any list of children in t or its descendants.
        Oparam Tree t: tree to explore, cannot be None
```

```
Oparam int d: depth to report from, non-negative
    Ortype: int
    >>> t = Tree(17, [Tree(0), Tree(1, [Tree(4)]), Tree(2, [Tree(5)]), Tree(3)])
    >>> print(t)
    17
       1
       2
       3
    >>> sum_at_depth(t, 0)
    >>> sum_at_depth(t, 1)
    >>> sum_at_depth(t, 2)
   >>> count_at_depth(t, 5)
    0
    .....
    if d == 0:
        return t.value
    else:
        return sum([sum_at_depth(c, d - 1)
                    for c in t.children
                    if c is not None])
def concatenate_at_depth(t, d):
    """ Return the concatenation of node values at depth d of t.
    Assume that node values are strings and that there are no
    None values in any list of children in t or its descendants.
    Oparam Tree t: tree to explore, cannot be None
    Oparam int d: depth to report from, non-negative
    Ortype: str
    \Rightarrow t = Tree("a", [Tree("b"), Tree("c", [Tree("d")]), Tree("e", [Tree("f")]), Tree("g")])
    >>> print(t)
       b
          f
       g
    >>> concatenate_at_depth(t, 0)
    'na'
    >>> concatenate_at_depth(t, 1)
    'bceg'
    >>> concatenate_at_depth(t, 2)
    df'
    >>> concatenate_at_depth(t, 5)
    ....
    if d == 0:
```

3. (9 pts) Read the declaration of the LinkedList and LinkedListNode classes below, from module node. Notice that we use property and _get_value to make sure the values of these LinkedListNodes are immutable: they cannot be changed after initialization!

On page 7 implement the function reverse_list. You may create new local names (variables) to refer to existing nodes (if you need to), but you may not create any new objects (LinkedLists, LinkedListNodes, or Python lists, etc.).

```
class LinkedListNode:
   Node to be used in linked list
   === Attributes ===
   @param LinkedListNode next_: successor to this LinkedListNode
   Oparam object value: data this LinkedListNode represents
   def __init__(self, value, next_=None):
        Create LinkedListNode self with data value and successor next_.
       @param LinkedListNode self: this LinkedListNode
        Oparam object value: data of this linked list node
       @param LinkedListNode|None next_: successor to this LinkedListNode.
       Ortype: None
       self._value, self.next_ = value, next_
   def _get_value(self):
       # to show value
       return self._value
   # no way to set value!
   value = property(_get_value)
   def __str__(self):
        ....
       Return a user-friendly representation of this LinkedListNode.
        @param LinkedListNode self: this LinkedListNode
       Ortype: str
       >>> n = LinkedListNode(5, LinkedListNode(7))
       >>> print(n)
       5 -> 7 ->|
       s = "{} ->".format(self.value)
       current_node = self.next_
       while current_node is not None:
           s += " {} ->".format(current_node.value)
            current_node = current_node.next_
       assert current_node is None, "unexpected non_None!!!"
       s += "|"
       return s
```

```
class LinkedList:
   Collection of LinkedListNodes
   === Attributes ==
   @param: LinkedListNode front: first node of this LinkedList
   @param LinkedListNode back: last node of this LinkedList
   Oparam int size: number of nodes in this LinkedList
                       a non-negative integer
   def __init__(self):
       Create an empty linked list.
       @param LinkedList self: this LinkedList
       Ortype: None
       self.front, self.back, self.size = None, None, 0
   def __str__(self):
       .....
       Return a human-friendly string representation of
       LinkedList self.
       @param LinkedList self: this LinkedList
       >>> lnk = LinkedList()
       >>> print(lnk)
       I'm so empty...
       if self.front is None:
           assert self.back is None and self.size is 0, "ooooops!"
           return "I'm so empty..."
       else:
           return str(self.front)
   def prepend(self, value):
       Insert value before LinkedList self.front.
       @param LinkedList self: this LinkedList
       @param object value: value for new LinkedList.front
       Ortype: None
       >>> lnk = LinkedList()
       >>> lnk.prepend(0)
       >>> lnk.prepend(1)
       >>> lnk.prepend(2)
       >>> str(lnk.front)
       '2 -> 1 -> 0 ->|'
       >>> lnk.size
       3
       new_node = LinkedListNode(value, self.front)
       self.front = new_node
       if self.size == 0:
           self.back = new_node
       self.size += 1
```

```
from node import LinkedList, LinkedListNode
```

```
def reverse_list(list_):
    """ Reverse the order of the nodes in list_.
    @param list_ LinkedList: linked list to modify
    Ortype: None
    >>> lnk = LinkedList()
    >>> lnk.prepend(1)
    >>> lnk.prepend(3)
    >>> lnk.prepend(5)
    >>> print(lnk)
    5 -> 3 -> 1 ->|
    >>> reverse_list(lnk)
    >>> print(lnk)
    1 -> 3 -> 5 ->|
    11 11 11
    # Hint: draw pictures.
sample solution(s): All three versions below...
     def reverse_list(list_, arg=None):
        current = list_.front
        prev = None
        tail = list_.front
        while current:
            next_ = current.next_
            current.next_ = prev
            prev = current
            current = next_
            # Or in one line:
            # current.next_, current, prev = prev, current.next_, current
        list_.front, list_.back = prev, tail
    def reverse_list_to_value(list_, value):
        """ Does not update size, discards other nodes. """
        current = list_.front
        prev = None
        tail = list_.front
        while current and (prev is None or prev.value != value):
            next_ = current.next_
            current.next_ = prev
            prev = current
            current = next_
            # Or in one line:
            # current.next_, current, prev = prev, current.next_, current
```

```
list_.front, list_.back = prev, tail
def reverse_list_after_value(list_, value):
    """ Does not update size, discards other nodes. """
   current = list_.front
   while current and current.value != value:
       current = current.next_
   if current:
       prev = None
       tail = current
       while current:
           next_ = current.next_
           current.next_ = prev
           prev = current
           current = next_
           # Or in one line:
           # current.next_, current, prev = prev, current.next_, current
       list_.front, list_.back = prev, tail
```