R-4.5

Draw the recursion trace for the execution of function PuzzleSolve(3, S, U) (Code Fragment 4.14), where S is empty and $U = \{a, b, c, d\}$

```
U = \{a, b, c, d\}; S = ""; k = 3
for e in array: first iteration of {a, b, c, d}
- e = a
- k = 3
- add a to S
- S = a
- remove a from U
- U = \{b, c, d\}
- k! = 1
- recursive call(3 - 1, a, {b, c, d})
     - for e in array: first iteration of {b, c, d}
         - e = b
         - k = 2
         - add b to S
         -S = ab
         - remove b from U
         - U = \{c, d\}
         - k! = 1
         recursive call (2 - 1, ab, {c, d})
              - for e in array: first iteration of {c, d}
                  -e=c
                  - k = 1
                  - add c to S
                  -S = abc
                  - remove c from U
                  - U = \{d\}
                  - k == 1
                  - solve puzzle
                      - return solution if solved, otherwise continue
                  remove c from S
                  -S = ab
                  - add c to U
                  - U = \{d, c\}

    complete for loop

             - for e in array: second and last iteration of {c, d}
                  -e=d
                  - k = 1
                  - add d to S
```

```
-S = abd
             - remove d from U
             - U = \{c\}
             - solve puzzle
                 - return if solved, otherwise continue

    remove d from S

             -S = ab
             - add d to U
             - U = \{c, d\}

    complete for loop

    break because iteration of {c, d} complete

- for e in array: second iteration of {b, c, d}
    -e=c
    - k = 2
    - add c to S
    -S = ac
    - remove c from U
    - U = \{b, d\}
    - k! = 1
    recursive call (2 - 1 , ac, {b, d}
        - for e in array: first iteration of {b, d}
             - e = b
             - k = 1
             - add b to S
             -S = acb
             - remove b from U
             - U = \{d\}
             - k == 1
             - solve puzzle

    return solution if solved, otherwise continue

             - remove b from S
             -S = ac
             - add b to U
             - U = \{d, b\}

    complete for loop

    for e in array second and last iteration of {b, d}

             - e = d

    follow same pattern ....

             - complete for loop
        - break because iteration of {b, d} complete
- for e in array: third and last iteration of {b, c, d}
    -e=d
    - k = 2

    follow same pattern

    recursive call (2 - 1, ad, {b, c}
        - same pattern

    complete for loop
```

- same pattern
 - complete for loop
- break because iteration of {b, c} complete
- break because iteration of {b, c, d} complete

for e in array: second iteration of {a, b, c, d}

continue pattern

... continue pattern until parent for loop complete.