COMP 140: Stock Prediction (Writeup)

Due on October 11, 2017 at $8{:}00~\mathrm{PM}$

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1 Recipe

The inputs of the markov_chain() function are a sequence of numbers assigned to the variable data (corresponding to the bins 0-3) and a number greater than or equal to 1 assigned to the variable order, representing the order of the desired markov chain. The function outputs an n^{th} order markov chain, where n = order represented as a mapping between n-tuples (corresponding to the previous n states) and a mapping between integers (representing a certain possible next state) and real numbers between 0 and 1 (representing the probability of reaching the corresponding state). ***Note that the notation f(x) will be used throughout this assignment to refer to the value that x maps to under the mapping f.***

```
1: procedure MARKOV_CHAIN(data, order)
 2:
        model \leftarrow \text{empty mapping}
        arr \leftarrow \text{empty sequence of integers}
 3:
        index \leftarrow -1
 4:
        for all element \in data do
 5:
            index \leftarrow index + 1
 6:
 7:
            if index < order then
                arr \leftarrow arr + element
 8:
            else
 9:
                tup \leftarrow tuple with elements of arr
10:
                if tup is not in the domain of model then
11:
                    model(tup) \leftarrow \text{empty mapping between integers and real-valued probabilities}
12:
                end if
13:
                if tup is not in the domain of model then
14:
                    model(tup)(element) \leftarrow 0
15:
                end if
16:
                model(tup)(element) \leftarrow model(tup)(element) + 1
17:
                arr \leftarrow arr + element
18:
                remove first element of arr
19:
            end if
20:
        end for
21:
        for all n-tuples entry in the domain of model do
22:
            total \leftarrow 0.0
23:
            for all integers state in the domain of model(entry) do
24:
                total \leftarrow total + model(entry)(state)
25:
            end for
26:
            for all integers state in the domain of model(entry) do
27:
                model(entry)(state) \leftarrow model(entry)(state)/total
28:
            end for
29:
        end for
30:
        return model
31:
32: end procedure
```

The predict function takes the following as inputs: markov model, model, represented as a mapping between tuples and mappings between integer valued states and real-valued probabilities; a sequence of integers, prev, representing the previous states with length n where n is the order of the markov model, model; an integer, num, representing the number of future states to predict. The predict function outputs a sequence of integers of length num, representing the predicted states for the next num days.

```
1: procedure PREDICT(model, last, num)
        prev \leftarrow \text{copy of } last
 2:
 3:
        predicted \leftarrow \text{empty sequence of integers}
        index \leftarrow -1
 4:
        while index < num do
 5:
            next \leftarrow 0
 6:
            tup \leftarrow tuple with elements of last
 7:
            if tup is not in the domain of model then
 8:
                 next \leftarrow random integer between 0 and 3, inclusive
 9:
            else
10:
                 entry \leftarrow model(tup)
11:
                total \leftarrow 0
12:
                random\_number \leftarrow random real value between 0 and 1
13:
                for all integers state in the domain of entry do
14:
                     total \leftarrow total + entry(key)
15:
                    \mathbf{if} \ random\_number <= total \ \mathbf{then}
16:
                         next \leftarrow key
17:
                         break
18:
                    end if
19:
                end for
20:
            end if
21:
            predicted \leftarrow predicted + next
22:
            prev \leftarrow prev + next
23:
            remove first element of prev
24:
        end while
25:
        return predicted
26:
27: end procedure
```

2 Discussion

Discuss the results of the experiments you ran in 4.B (be sure to include the results). In particular, discuss the following questions:

- 1. What is the order of the model that works best for each stock/index? If the orders are not the same, discuss why that might be the case.
- 2. Which stock/index can you predict with the lowest error? Based on the plots of the day-to-day change in stocks and the histogram of bins, can you guess why that stock/index is easiest to predict?
- 3. Given that we have divided the day-to-day price change into 4 bins, how many possible states are there in an n^{th} order Markov chain for predicting the change in stock price?
- 4. The training data we gave you covers two years of data, with 502 data points per stock/index. Is that enough data that it is possible to see all possible states in an n^{th} order Markov chain? What are the constraints on n? How do you think it would affect the accuracy of the model if there were not enough data?

Solution

- 1. The model predicts with the least error for stock FSLR with order 5, for stock GOOG with order 1, and for stock DJIA with order 3. This is likely since highly volatile stocks require higher order markov models in order to predict accurately, as low order markov models would be skewed by noise; only as order increases does the impact of noise decrease. Thus, since FSLR is more volatile than DJIA which is more volatile than GOOG (based on daily change and variations in the bin histogram), it is logical that the model for FSLR required a higher order than that for DJIA which required a higher order than that for GOOG.
- 2. GOOG is predicted with the lowest error, since it is the most stable of the three stocks given. GOOG has the most homogenous bin histogram as well as the least volatile daily change. As such, since stability implies predictability, a given state for GOOG is likely to be similar to the previous state, which is easily predictable by a markov model.
- 3. Since the model is of order n, a state is represented by a tuple with n values, where each value has 4 possibilities. Thus, there are 4^n possible states.
- 4. There is theoretically enough data to see all possible states in a 3^{rd} order Markov chain, but not for a 5^{th} order markov chain. Thus, for $n \leq \frac{\log 502}{\log 4} \approx 4$ we can see all possible states. Without enough data, the model would be inaccurate since it would predict certain next states with high certainty based off of insufficient empirical data, leading to false confidence.