Dark Energy in the T0 Model:
A Mathematical Analysis of Energy Dynamics

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Zusammenfassung

This work develops a detailed mathematical analysis of dark energy within the framework of the T0 model with absolute time and variable mass. Unlike the ΛCDM standard model, dark energy is not considered a driving force of cosmic expansion but emerges as a dynamic effect of energy exchange in a static universe, mediated by the intrinsic time field $T(x)$. The document builds on foundations from [4] and the gravitation theory from [1], characterizes energy transfer rates, analyzes the radial density profile of dark energy, and explains the observed redshift as a result of photon energy loss to this field (see [2]). Experimental tests to distinguish this interpretation from the standard model conclude the analysis.

Inhaltsverzeichnis

1 Introduction

The discovery of accelerated cosmic expansion through supernova observations in the late 1990s led to the introduction of dark energy as the dominant component of the universe in the ΛCDM standard model, where it is modeled as a cosmological constant (Λ) with negative pressure, accounting for approximately 68% of the energy content. This work pursues an alternative approach within the T0 model, based on time-mass duality (see [4], Section "Time-Mass Duality"). Here, time is absolute, and mass varies, with dark energy not being a separate entity driving expansion but an emergent effect of the intrinsic time field $T(x)$. Cosmic redshift is explained not by spatial expansion but by the energy loss of photons to $T(x)$, as detailed in [2] (Section "Energy Loss and Redshift") and [3] (Section "Temperature Scaling"). The energy dynamics are mathematically analyzed below, referencing established derivations such as gravitation theory in [1] and parameters in [4]. Experimental tests to differentiate from the standard model conclude the work.

2 Mathematical Foundations of the T0 Model

2.1 Time-Mass Duality

The T0 model postulates a duality between time and mass, enabling two descriptions:

1. **Standard View**: Time dilation ($t' = \gamma t$), constant rest mass (m_0).
2. **T0 Model**: Absolute time (T_0), variable mass ($m = \gamma m_0$).

The complete derivation and transformations are provided in [4] (Section "Time-Mass Duality") and [1] (Section "Foundations"). An overview is given in the table:

Quantity	Standard View	T0 Model
Time	$t' = \gamma t$	$t = \text{const.}$
Mass	$m = \text{const.}$	$m = \gamma m_0$
Intrinsic Time	$T = \frac{\hbar}{mc^2}$	$T = \frac{\hbar}{\gamma m_0 c^2}$

Tabelle 1: Transformations in the T0 Model (see [4])

2.2 Intrinsic Time

The intrinsic time $T(x)$ is central to the T0 model:

Definition 2.0.1 (Intrinsic Time). For a particle with mass m:

$$T(x) = \frac{\hbar}{mc^2} \tag{1}$$

The derivation is detailed in [4] (Section "Definition of Intrinsic Time").

Corollary 2.1 (Scalar Field). *As a field:*

$$T(x) = \frac{\hbar}{y\langle\Phi\rangle c^2} \tag{2}$$

Details on the Higgs field are in [6] (Section "Higgs Mechanism").

2.3 Modified Derivative Operators

The operators were introduced in [5] (Section "Lagrangian Formulation"):

Definition 2.1.1 (Modified Time Derivative)**.**

$$\partial_{t/T} = T\frac{\partial}{\partial t} \tag{3}$$

Definition 2.1.2 (Covariant Derivative)**.** For a field Ψ:

$$D_{T,\mu}\Psi = T(x)D_\mu\Psi + \Psi\partial_\mu T(x) \tag{4}$$

Definition 2.1.3 (Higgs Field Derivative)**.**

$$D_{T,\mu}\Phi = T(x)(\partial_\mu + igA_\mu)\Phi + \Phi\partial_\mu T(x) \tag{5}$$

3 Modified Field Equations for Dark Energy

3.1 Modified Lagrangian Density

The Lagrangian density is derived in [5] (Section "Total Lagrangian Density"):

$$\mathcal{L}_{\text{Total}} = \mathcal{L}_{\text{Boson}} + \mathcal{L}_{\text{Fermion}} + \mathcal{L}_{\text{Higgs-T}} \tag{6}$$

With:

$$\mathcal{L}_{\text{Boson}} = -\frac{1}{4}T(x)^2F_{\mu\nu}F^{\mu\nu} \tag{7}$$

$$\mathcal{L}_{\text{Fermion}} = \bar{\psi}i\gamma^\mu T(x)D_\mu\psi + \psi\partial_\mu T(x) - y\bar{\psi}\Phi\psi \tag{8}$$

$$\mathcal{L}_{\text{Higgs-T}} = (D_{T,\mu}\Phi)^\dagger(D_{T,\mu}\Phi) - \lambda(|\Phi|^2 - v^2)^2 \tag{9}$$

3.2 Dark Energy as an Emergent Effect

Dark energy arises from $T(x)$ variations, as described in [1] (Section "Emergent Gravitation"):

$$\rho_{\text{DE}}(r) \approx \frac{\kappa}{r^2} \tag{10}$$

Details on κ are in [4] (Section "Parameter Derivations").

3.3 Energy Density Profile

$$\rho_{\text{DE}}(r) \approx \frac{1}{2}(\nabla T(x))^2 \approx \frac{\kappa}{r^2} \tag{11}$$

See [1] (Section "Energy Density").

3.4 Emergent Gravitation

Theorem 3.1 (Emergence of Gravitation)**.**

$$\nabla T(x) = -\frac{\hbar}{m^2c^2}\nabla m \sim \nabla\Phi_g \tag{12}$$

Full derivation in [1] (Section "Emergent Gravitation").

Beweis. In regions with gravitational potential Φ_g, the effective mass varies as:

$$m(\vec{r}) = m_0 \left(1 + \frac{\Phi_g(\vec{r})}{c^2}\right) \tag{13}$$

Thus:

$$\nabla m = \frac{m_0}{c^2} \nabla \Phi_g \tag{14}$$

Substituting into the gradient of the intrinsic time field:

$$\nabla T(x) = -\frac{\hbar}{m^2 c^2} \cdot \frac{m_0}{c^2} \nabla \Phi_g \tag{15}$$

□

The Poisson equation is:

$$\nabla^2 \Phi = 4\pi G \rho + \kappa^2 \tag{16}$$

4 Energy Transfer and Redshift

4.1 Photon Energy Loss

Redshift results from energy loss, derived in [2] (Section “Energy Loss”):

$$\frac{dE_\gamma}{dx} = -\alpha E_\gamma, \quad E_\gamma(x) = E_{\gamma,0} e^{-\alpha x} \tag{17}$$

$$1 + z = e^{\alpha d}, \quad \alpha = \frac{H_0}{c} \approx 2.3 \times 10^{-18}\,\mathrm{m}^{-1} \tag{18}$$

Details on α in [4] (Section “Derivation of α”).

4.2 Modified Energy-Momentum Relation

Theorem 4.1 (Energy-Momentum Relation)**.**

$$E^2 = (pc)^2 + (mc^2)^2 + \alpha_E \frac{\hbar c}{T} \tag{19}$$

See [7] (Section “Physics Beyond the Speed of Light”).

Theorem 4.2 (Wavelength Dependence)**.**

$$z(\lambda) = z_0(1 + \beta_T \ln(\lambda/\lambda_0)) \tag{20}$$

With $\beta_T^{SI} \approx 0.008$, $\beta_T^{nat} = 1$ (see [4]).

4.3 Energy Balance Equation

$$\rho_{\text{total}} = \rho_{\text{Matter}} + \rho_\gamma + \rho_{\text{DE}} = \text{const.} \tag{21}$$

$$\frac{d\rho_{\text{Matter}}}{dt} = -\alpha c \rho_{\text{Matter}} \tag{22}$$

$$\frac{d\rho_\gamma}{dt} = -\alpha c \rho_\gamma \tag{23}$$

$$\frac{d\rho_{\text{DE}}}{dt} = \alpha c(\rho_{\text{Matter}} + \rho_\gamma) \tag{24}$$

See [2] (Section “Energy Balance”).

5 Quantitative Determination of Parameters

5.1 Parameters in Natural Units

Theorem 5.1 (Key Parameters)**.**

$$\kappa = \beta_T \frac{yv}{r_g} \tag{25}$$

$$\alpha = \frac{\lambda_h^2 v}{L_T} \tag{26}$$

$$\beta_T = \frac{\lambda_h^2 v^2}{4\pi^2 \lambda_0 \alpha_0} \tag{27}$$

Derivation in [4] (Section "Parameter Derivations").

In SI units:

$$\alpha_{\mathrm{SI}} \approx 2.3 \times 10^{-18}\,\mathrm{m}^{-1} \tag{28}$$

$$\beta_{\mathrm{T}}^{\mathrm{SI}} \approx 0.008 \tag{29}$$

$$\kappa_{\mathrm{SI}} \approx 4.8 \times 10^{-11}\,\mathrm{m\,s^{-2}} \tag{30}$$

5.2 Gravitational Potential

Theorem 5.2 (Gravitational Potential)**.**

$$\Phi(r) = -\frac{GM}{r} + \kappa r \tag{31}$$

See [1] (Section "Modified Gravitational Potential").

6 Dark Energy and Cosmological Observations

6.1 Type Ia Supernovae

$$d_L = \frac{c}{H_0} \ln(1+z)(1+z) \tag{32}$$

See [2] (Section "Supernovae").

6.2 Energy Density Parameter

$$\Omega_{DE}^{\mathrm{eff}} \approx \frac{3\kappa}{R_U H_0^2} \approx 0.68 \tag{33}$$

7 Experimental Tests

7.1 Fine Structure Constant

$$\frac{d\alpha_{\mathrm{EM}}}{dt} \approx 1 \times 10^{-18}\,\mathrm{yr}^{-1} \tag{34}$$

See [7] (Section "Experimental Verification").

7.2 Environment-Dependent Redshift

$$\frac{z_{\text{Cluster}}}{z_{\text{Void}}} \approx 1 + 0.003 \tag{35}$$

7.3 Differential Redshift

$$\frac{z(\lambda_1)}{z(\lambda_2)} \approx 1 + \beta_{\text{T}} \frac{\lambda_1 - \lambda_2}{\lambda_0} \tag{36}$$

8 Outlook and Summary

The T0 model provides a framework for a static universe where dark energy emerges from $T(x)$. Future tests (e.g., Euclid) can validate it.

Literatur

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