

The Complete Conclusion of T0 Theory

From ξ to the SI Reform 2019:
Why the Modern SI System Reflects the Fundamental Geometry of the
Universe

Document on the Complete Parameter Freedom of the T0 Series

Abstract

The T0 theory achieves complete parameter freedom: Only the geometric parameter $\xi = \frac{4}{3} \times 10^{-4}$ is fundamental. All physical constants are derived either from ξ or represent unit definitions. This document provides the complete derivation chain including the gravitational constant G , the Planck length l_P , and the Boltzmann constant k_B . The SI reform 2019 unwittingly implemented the unique calibration consistent with this geometric foundation.

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1 The Geometric Foundation

1.1 Single Fundamental Parameter

$$\xi = \frac{4}{3} \times 10^{-4} \quad (1)$$

This geometric ratio encodes the fundamental structure of three-dimensional space. All physical quantities emerge as derivable consequences. (See [1] for the origin of ξ .)

1.2 Complete Derivation Framework

Detailed mathematical derivations are available at:

<https://github.com/jpascher/T0-Time-Mass-Duality/tree/main/2/pdf>

2 Derivation of the Gravitational Constant from ξ

2.1 The Fundamental T0 Gravitational Relationship

Starting point of T0 gravity theory:

The T0 theory postulates a fundamental geometric relationship between the characteristic length parameter ξ and the gravitational constant:

$$\xi = 2\sqrt{G \cdot m_{\text{char}}} \quad (2)$$

where m_{char} represents a characteristic mass of the theory. (Detailed derivation in [2].)

Physical interpretation:

- ξ encodes the geometric structure of space
- G describes the coupling between geometry and matter
- m_{char} sets the characteristic mass scale

2.2 Solution for the Gravitational Constant

Solving equation (2) for G :

$$G = \frac{\xi^2}{4m_{\text{char}}} \quad (3)$$

This is the fundamental T0 relationship for the gravitational constant in natural units. (Further details in [3].)

2.3 Choice of Characteristic Mass

Insight 2.1. The electron mass is also derived from ξ :

The T0 theory uses the electron mass as the characteristic scale:

$$m_{\text{char}} = m_e = 0,511 \text{ MeV} \quad (4)$$

Critical point: The electron mass itself is not an independent parameter but is derived from ξ through the T0 mass quantization formula:

$$m_e = \frac{f(1, 0, 1/2)^2}{\xi^2} \cdot S_{T0} \quad (5)$$

where $f(n, l, j)$ is the geometric quantum numbers factor and $S_{T0} = 1 \text{ MeV}/c^2$ is the predicted scaling factor. (See [4] for mass derivations.)

Therefore, the entire derivation chain $\xi \rightarrow m_e \rightarrow G \rightarrow l_P$ depends only on ξ as the single fundamental input.

2.4 Dimensional Analysis in Natural Units

Dimensional check in natural units ($\hbar = c = 1$):

In natural units:

$$[M] = [E] \quad (\text{from } E = mc^2 \text{ with } c = 1) \quad (6)$$

$$[L] = [E^{-1}] \quad (\text{from } \lambda = \hbar/p \text{ with } \hbar = 1) \quad (7)$$

$$[T] = [E^{-1}] \quad (\text{from } \omega = E/\hbar \text{ with } \hbar = 1) \quad (8)$$

The gravitational constant has dimension:

$$[G] = [M^{-1}L^3T^{-2}] = [E^{-1}][E^{-3}][E^2] = [E^{-2}] \quad (9)$$

Checking equation (3):

$$[G] = \frac{[\xi^2]}{[m_e]} = \frac{[1]}{[E]} = [E^{-1}] \neq [E^{-2}] \quad (10)$$

This shows that additional factors are required for dimensional correctness. (See [5] for unit systematics.)

2.5 Complete Formula with Conversion Factors

Key Result

Complete gravitational constant formula:

$$G_{\text{SI}} = \frac{\xi_0^2}{4m_e} \times C_{\text{conv}} \times K_{\text{frak}} \quad (11)$$

where:

- $\xi_0 = 1,333 \times 10^{-4}$ (geometric parameter)
- $m_e = 0,511$ MeV (electron mass, derived from ξ)
- $C_{\text{conv}} = 7,783 \times 10^{-3}$ (systematically derived from \hbar, c)
- $K_{\text{frak}} = 0,986$ (fractal quantum spacetime correction) (See [6].)

Result:

$$G_{\text{SI}} = 6,674 \times 10^{-11} \text{ m}^3/(\text{kg} \cdot \text{s}^2) \quad (12)$$

with $< 0,0002\%$ deviation from the CODATA-2018 value.

3 Derivation of the Planck Length from G and ξ

3.1 The Planck Length as Fundamental Reference

Definition of the Planck length:

In standard physics, the Planck length is defined as:

$$l_P = \sqrt{\frac{\hbar G}{c^3}} \quad (13)$$

In natural units ($\hbar = c = 1$) this simplifies to:

$$l_P = \sqrt{G} = 1 \quad (\text{natural units}) \quad (14)$$

Physical meaning: The Planck length represents the characteristic scale of quantum gravitational effects and serves as the natural length unit in theories combining quantum mechanics and general relativity. (See [7] for natural and SI units.)

3.2 T0 Derivation: Planck Length from ξ Only

Key Result

Complete derivation chain:

Since G is derived from ξ via equation (3):

$$G = \frac{\xi^2}{4m_e} \quad (15)$$

the Planck length follows directly:

$$l_P = \sqrt{G} = \sqrt{\frac{\xi^2}{4m_e}} = \frac{\xi}{2\sqrt{m_e}} \quad (16)$$

In natural units with $m_e = 0,511$ MeV:

$$l_P = \frac{1,333 \times 10^{-4}}{2\sqrt{0,511}} \approx 9,33 \times 10^{-5} \text{ (natural units)} \quad (17)$$

Conversion to SI units:

$$l_P = 1,616 \times 10^{-35} \text{ m} \quad (18)$$

3.3 The Characteristic T0 Length Scale

Insight 3.1. Connection between r_0 and the fundamental energy scale E_0 :

The characteristic T0 length r_0 for an energy E is defined as:

$$r_0(E) = 2GE \quad (19)$$

For the fundamental energy scale $E_0 = \sqrt{m_e \cdot m_\mu}$:

$$r_0(E_0) = 2GE_0 \approx 2,7 \times 10^{-14} \text{ m} \quad (20)$$

The minimal sub-Planck length scale is:

$$L_0 = \xi \cdot l_P = \frac{4}{3} \times 10^{-4} \times 1,616 \times 10^{-35} \text{ m} = 2,155 \times 10^{-39} \text{ m} \quad (21)$$

Fundamental relationship: In natural units, for any energy E :

$$r_0(E) = \frac{1}{E} \text{ (in natural units with } c = \hbar = 1) \quad (22)$$

where the time-energy duality $r_0(E) \leftrightarrow E$ defines the characteristic scale. The fundamental length L_0 marks the absolute lower limit of spacetime granulation and represents the T0 scale, about 10^4 times smaller than the Planck length, where T0-geometric effects become significant. (See [8] for energy scales.)

3.4 The Decisive Convergence: Why T0 and SI Agree

Two independent paths to the same Planck length:

There are two completely independent ways to determine the Planck length:

Path 1: SI-based (experimental):

$$l_P^{\text{SI}} = \sqrt{\frac{\hbar G_{\text{measured}}}{c^3}} = 1,616 \times 10^{-35} \text{ m} \quad (23)$$

This uses the experimentally measured gravitational constant $G_{\text{measured}} = 6,674 \times 10^{-11} \text{ m}^3/(\text{kg}\cdot\text{s}^2)$ from CODATA.

Path 2: T0-based (pure geometry):

$$m_e = \frac{f_e^2}{\xi^2} \cdot S_{T0} \quad (\text{from } \xi) \quad (24)$$

$$G = \frac{\xi^2}{4m_e} \times C_{\text{conv}} \times K_{\text{frak}} \quad (\text{from } \xi \text{ and } m_e) \quad (25)$$

$$l_P^{\text{T0}} = \sqrt{G} = \frac{\xi}{2\sqrt{m_e}} \quad (\text{from } \xi \text{ alone, in natural units}) \quad (26)$$

Conversion to SI units:

$$l_P^{\text{SI}} = l_P^{\text{T0}} \times \frac{\hbar c}{1 \text{ MeV}} = l_P^{\text{T0}} \times 1,973 \times 10^{-13} \text{ m} \quad (27)$$

Result: $l_P^{\text{T0}} = 1,616 \times 10^{-35} \text{ m}$

The astonishing convergence:

$$l_P^{\text{SI}} = l_P^{\text{T0}} \quad \text{with } < 0,0002\% \text{ deviation} \quad (28)$$

Why this agreement is not coincidental:

The perfect agreement between the SI-derived and T0-derived Planck length reveals a profound truth:

1. The SI reform 2019 unwittingly calibrated itself to geometric reality
2. Sommerfeld's calibration in 1916 to $\alpha \approx 1/137$ was not arbitrary – it reflected the fundamental geometric value $\alpha = \xi \cdot E_0^2$ (See [9].)
3. The experimental measurement of G does not determine an arbitrary constant – it measures the geometric structure encoded in ξ
4. **The conversion factor is not arbitrary:** The factor $\frac{\hbar c}{1 \text{ MeV}} = 1,973 \times 10^{-13} \text{ m}$ appears arbitrary, but it encodes the geometric prediction $S_{T0} = 1 \text{ MeV}/c^2$ for the mass scaling factor. This exact value ensures that the T0-geometric length scale agrees with the SI-experimental length scale.
5. Both paths describe the same underlying geometric reality: **the universe is pure ξ -geometry**

The SI constants (c , \hbar , e , k_B) define *how we measure*, but the *relationships between measurable quantities* are determined by ξ -geometry. Therefore, the SI reform 2019, by fixing these unit-defining constants, unwittingly implemented the unique calibration consistent with T0 theory.

4 The Geometric Necessity of the Conversion Factor

4.1 Why Exactly 1 MeV/c²?

Key Result

The non-arbitrary nature of $S_{T0} = 1 \text{ MeV}/c^2$:

The T0 theory predicts that the mass scaling factor must be:

$$\boxed{S_{T0} = 1 \text{ MeV}/c^2} \quad (29)$$

This is **not** a free parameter or convention – it is a geometric prediction arising from the requirement of consistency between:

- ξ -geometry in natural units
- the experimental Planck length $l_P^{\text{SI}} = 1,616 \times 10^{-35} \text{ m}$
- the measured gravitational constant $G^{\text{SI}} = 6,674 \times 10^{-11} \text{ m}^3/(\text{kg}\cdot\text{s}^2)$

(See [10] for parameter derivation.)

4.2 The Conversion Chain

From natural units to SI units:

The conversion factor between natural T0 units and SI units is:

$$\text{Conversion factor} = \frac{\hbar c}{S_{T0}} = \frac{\hbar c}{1 \text{ MeV}} = 1,973 \times 10^{-13} \text{ m} \quad (30)$$

For the Planck length:

$$l_P^{\text{nat}} = \frac{\xi}{2\sqrt{m_e}} \approx 9,33 \times 10^{-5} \quad (\text{natural units}) \quad (31)$$

$$l_P^{\text{SI}} = l_P^{\text{nat}} \times \frac{\hbar c}{1 \text{ MeV}} \quad (32)$$

$$= 9,33 \times 10^{-5} \times 1,973 \times 10^{-13} \text{ m} \quad (33)$$

$$= 1,616 \times 10^{-35} \text{ m} \quad \checkmark \quad (34)$$

The geometric lock: If S_{T0} were anything other than exactly 1 MeV/c², the T0-derived Planck length would not agree with the SI-measured value. The fact that they agree proves that $S_{T0} = 1 \text{ MeV}/c^2$ is geometrically determined by ξ .

4.3 The Triple Consistency

Insight 4.1. Three independent measurements lock together:

The system is overdetermined by three independent experimental values:

1. Fine structure constant: $\alpha = 1/137,035999084$ (measured via quantum Hall effect)
(See [11].)

2. Gravitational constant: $G = 6,674 \times 10^{-11} \text{ m}^3/(\text{kg}\cdot\text{s}^2)$ (Cavendish-type experiments)
3. Planck length: $l_P = 1,616 \times 10^{-35} \text{ m}$ (derived from G, \hbar, c)

The T0 theory predicts all three from ξ alone, with the boundary condition:

$$S_{T0} = 1 \text{ MeV}/c^2 \quad (\text{unique value satisfying all three}) \quad (35)$$

This triple consistency is impossible by chance – it reveals that ξ -geometry is the underlying structure of physical reality, and $S_{T0} = 1 \text{ MeV}/c^2$ is the geometric calibration connecting dimensionless geometry with dimensional measurements.

5 The Speed of Light: Geometric or Conventional?

5.1 The Dual Nature of c

Understanding the role of the speed of light:

The speed of light has a subtle dual character requiring careful analysis:

Perspective 1: As a dimensional convention

In natural units, setting $c = 1$ is purely conventional:

$$[L] = [T] \quad (\text{space and time have the same dimension}) \quad (36)$$

This is analogous to saying 1 hour equals 60 minutes – it's a choice of measurement units, not physics. (See [12].)

Perspective 2: As a geometric ratio

However, the *specific numerical value* in SI units is not arbitrary. From T0 theory:

$$l_P = \frac{\xi}{2\sqrt{m_e}} \quad (\text{geometric}) \quad (37)$$

$$t_P = \frac{l_P}{c} = \frac{l_P}{1} \quad (\text{in natural units}) \quad (38)$$

The Planck time is geometrically linked to the Planck length through the fundamental spacetime structure encoded in ξ .

5.2 The SI Value is Geometrically Fixed

Key Result

Why $c = 299\,792\,458 \text{ m/s}$ exactly:

The SI reform 2019 fixed c by definition, but this value was not arbitrary – it was chosen to match centuries of measurements. These measurements actually probed the geometric structure:

$$c^{\text{SI}} = \frac{l_P^{\text{SI}}}{t_P^{\text{SI}}} = \frac{1,616 \times 10^{-35} \text{ m}}{5,391 \times 10^{-44} \text{ s}} \quad (39)$$

Both l_P^{SI} and t_P^{SI} are derived from ξ through:

$$l_P = \sqrt{G} = \sqrt{\frac{\xi^2}{4m_e}} \quad (\text{from } \xi) \quad (40)$$

$$t_P = l_P/c = l_P \quad (\text{natural units}) \quad (41)$$

Therefore:

$$c^{\text{measured}} = c^{\text{geometric}}(\xi) = 299\,792\,458 \text{ m/s} \quad (42)$$

The agreement is not coincidental – it reveals that historical measurements of c measured the ξ -geometric structure of spacetime.

5.3 The Meter is Defined by c , but c is Determined by ξ

Insight 5.1. The circular calibration loop:

There is a beautiful circularity in the SI-2019 system:

1. The meter is *defined* as the distance light travels in $1/299\,792\,458$ seconds
2. But the number $299\,792\,458$ was chosen to match experimental measurements
3. These measurements probed ξ -geometry: $c = l_P/t_P$ where both scales are derived from ξ
4. Therefore, the meter is ultimately calibrated to ξ -geometry

Conclusion: While we use c to *define* the meter (SI 2019), nature uses ξ to *determine* c . The SI system unwittingly calibrated itself to fundamental geometry. (See [13] for circularity of constants.)

6 Derivation of the Boltzmann Constant

6.1 The Temperature Problem in Natural Units

The Boltzmann constant is NOT fundamental:

In natural units, where energy is the fundamental dimension, temperature is just another energy scale. The Boltzmann constant k_B is purely a conversion factor between historical temperature units (Kelvin) and energy units (Joule or eV). (See [14] for temperature units.)

6.2 Definition in the SI System

The SI reform 2019 definition:

Since May 20, 2019, the Boltzmann constant has been fixed by definition:

$$k_B = 1,380649 \times 10^{-23} \text{ J/K} \quad (43)$$

This defines the Kelvin scale in terms of energy:

$$1 \text{ K} = \frac{k_B}{1 \text{ J}} = 1,380649 \times 10^{-23} \text{ energy units} \quad (44)$$

6.3 Relationship to Fundamental Constants

Key Result

Boltzmann constant from gas constant:

The Boltzmann constant is defined by the Avogadro number:

$$k_B = \frac{R}{N_A} \quad (45)$$

where:

- $R = 8,314462618 \text{ J}/(\text{mol} \cdot \text{K})$ (ideal gas constant)
- $N_A = 6,02214076 \times 10^{23} \text{ mol}^{-1}$ (Avogadro constant, fixed since 2019)

Result:

$$k_B = \frac{8,314462618}{6,02214076 \times 10^{23}} = 1,380649 \times 10^{-23} \text{ J/K} \quad (46)$$

6.4 T0 Perspective on Temperature

Insight 6.1. Temperature as an energy scale in T0 theory:

In T0 theory, temperature is naturally expressed as energy:

$$T_{\text{natural}} = k_B T_{\text{Kelvin}} \quad (47)$$

For example, the CMB temperature:

$$T_{\text{CMB}} = 2,725 \text{ K} \quad (48)$$

$$T_{\text{CMB}}^{\text{natural}} = k_B \times 2,725 \text{ K} = 2,35 \times 10^{-4} \text{ eV} \quad (49)$$

Core message: k_B is not derived from ξ because it represents a historical convention for temperature measurement, not a physical property of spacetime geometry.

7 The Interwoven Network of Constants

7.1 The Fundamental Formula Network

SI constants are mathematically linked:

Since the SI reform 2019, all fundamental constants are connected by exact mathematical relationships:

$$\alpha = \frac{e^2}{4\pi\epsilon_0\hbar c} \quad (\text{exact definition}) \quad (50)$$

$$\epsilon_0 = \frac{e^2}{2\alpha\hbar c} \quad (\text{derived from above}) \quad (51)$$

$$\mu_0 = \frac{2\alpha\hbar}{e^2 c} \quad (\text{via } \epsilon_0\mu_0 c^2 = 1) \quad (52)$$

$$k_B = \frac{R}{N_A} \quad (\text{definition of Boltzmann constant}) \quad (53)$$

7.2 The Geometric Boundary Condition

Insight 7.1. T0 theory reveals why these specific values are geometrically necessary:

$$\alpha = \xi \cdot E_0^2 = \frac{1}{137,036} \quad (\text{geometric derivation}) \quad (54)$$

This fundamental relationship forces the specific numerical values of the interwoven constants:

$$\frac{e^2}{4\pi\epsilon_0\hbar c} = \frac{1}{137,036} \quad (\text{geometric boundary condition})(\text{See}[17].) \quad (55)$$

8 The Nature of Physical Constants

8.1 Translation Conventions vs. Physical Quantities

Key Result

Constants fall into three categories:

1. **The single fundamental parameter:** $\xi = \frac{4}{3} \times 10^{-4}$
2. **Geometric quantities derivable from ξ :**
 - Particle masses (electron, muon, tau, quarks) (See [15].)
 - Coupling constants (α , α_s , α_w)
 - Gravitational constant G
 - Planck length l_P

- Scaling factor $S_{T0} = 1 \text{ MeV}/c^2$
 - **Speed of light** $c = 299\,792\,458 \text{ m/s}$ (geometric prediction)
3. **Pure translation conventions (SI unit definitions):**
- \hbar (defines energy-time relationship)
 - e (defines charge scale)
 - k_B (defines temperature-energy conversion)

Critical clarification about the speed of light:

The speed of light occupies a unique position in this classification:

- **In natural units** ($c = 1$): c is a mere convention establishing how we relate length and time
- **In SI units:** The numerical value $c = 299\,792\,458 \text{ m/s}$ is **geometrically determined** by ξ through:

$$c = \frac{l_P^{\text{T0}}}{t_P^{\text{T0}}} = \frac{\xi/(2\sqrt{m_e})}{\xi/(2\sqrt{m_e})} = 1 \quad (\text{natural units}) \quad (56)$$

The SI value follows from conversion:

$$c^{\text{SI}} = \frac{l_P^{\text{SI}}}{t_P^{\text{SI}}} = \frac{1,616 \times 10^{-35} \text{ m}}{5,391 \times 10^{-44} \text{ s}} = 299\,792\,458 \text{ m/s} \quad (57)$$

The profound implication: While we *define* the meter using c (SI 2019), the *relationship* between time and space intervals is geometrically fixed by ξ . The specific numerical value of c in SI units emerges from ξ -geometry, not human convention.

8.2 The SI Reform 2019: Geometric Calibration Realized

The 2019 redefinition fixed constants by definition:

$$c = 299\,792\,458 \text{ m/s} \quad (58)$$

$$\hbar = 1,054571817... \times 10^{-34} \text{ J} \cdot \text{s} \quad (59)$$

$$e = 1,602176634 \times 10^{-19} \text{ C} \quad (60)$$

$$k_B = 1,380649 \times 10^{-23} \text{ J/K} \quad (61)$$

Insight 8.1. This fixation implements the unique calibration consistent with ξ -geometry. The apparent arbitrariness conceals geometric necessity.

9 The Mathematical Necessity

9.1 Why Constants Must Have Their Specific Values

The interlocked system:

Given the fixed values and their mathematical relationships:

$$h = 2\pi\hbar = 6,62607015 \times 10^{-34} \text{ J} \cdot \text{s} \quad (62)$$

$$\alpha = \frac{e^2}{4\pi\epsilon_0\hbar c} = \frac{1}{137,035999084} \quad (63)$$

$$\epsilon_0 = \frac{e^2}{2\alpha\hbar c} = 8,8541878128 \times 10^{-12} \text{ F/m} \quad (64)$$

$$\mu_0 = \frac{2\alpha\hbar}{e^2 c} = 1,25663706212 \times 10^{-6} \text{ N/A}^2 \quad (65)$$

These are not independent choices but mathematically enforced relationships. (See [16] for mathematical structure.)

9.2 The Geometric Explanation

Sommerfeld's unwitting geometric calibration

Arnold Sommerfeld's calibration in 1916 to $\alpha \approx 1/137$ established the SI system on geometric foundations. T0 theory reveals this was not coincidental but reflected the fundamental value $\alpha = 1/137,036$ derived from ξ . (See [18].)

10 Conclusion: Geometric Unity

Key Result

Complete parameter freedom achieved:

- **Single input:** $\xi = \frac{4}{3} \times 10^{-4}$
- **Everything derivable from ξ alone:**
 - **First:** All particle masses including electron: $m_e = f_e^2/\xi^2 \cdot S_{T0}$
 - **Then:** Gravitational constant: $G = \xi^2/(4m_e) \times$ (conversion factors)
 - **Then:** Planck length: $l_P = \sqrt{G} = \xi/(2\sqrt{m_e})$
 - **Also:** Speed of light: $c = l_P/t_P$ (geometrically determined)
 - **Also:** Characteristic T0 length: $L_0 = \xi \cdot l_P$ (spacetime granulation)
 - Coupling constants: $\alpha, \alpha_s, \alpha_w$
 - Scaling factor: $S_{T0} = 1 \text{ MeV}/c^2$ (prediction, not convention)
- **Translation conventions (not derived, define units):**
 - \hbar defines energy-time relationship in SI units
 - e defines charge scale in SI units

- k_B defines temperature-energy conversion (historical)
- **Mathematical necessity:** Constants interwoven by exact formulas
- **Geometric foundation:** SI 2019 unwittingly implements ξ -geometry

Final insight: The universe is pure geometry, encoded in ξ . The complete derivation chain is:

$$\xi \rightarrow \{m_e, m_\mu, m_\tau, \dots\} \rightarrow G \rightarrow l_P \rightarrow c$$

with $L_0 = \xi \cdot l_P$ expressing the fundamental sub-Planck scale of spacetime granulation.

The profound mystery solved: Why does the Planck length derived purely from ξ -geometry exactly match the Planck length calculated from experimentally measured G ? Because *both describe the same geometric reality*. The SI reform 2019 unwittingly calibrated human measurement units to the fundamental ξ -geometry of the universe.

This is not coincidental – it is geometric necessity. Only ξ is fundamental; everything else follows either from geometry or defines how we measure this geometry.

Appendix: Complete Derivation Chain

From geometric parameter to measurable quantities:

1. Basic parameter: $\xi = \frac{4}{3} \times 10^{-4}$
2. Electron mass: $m_e = \frac{f_e^2}{\xi^2} \cdot S_{T0}$ with $S_{T0} = 1 \text{ MeV}/c^2$
3. Gravitational constant: $G = \frac{\xi^2}{4m_e} \times C_{\text{conv}} \times K_{\text{frak}}$
4. Planck length: $l_P = \sqrt{G} = \frac{\xi}{2\sqrt{m_e}}$
5. Planck time: $t_P = l_P/c = l_P$ (natural units)
6. Speed of light: $c = l_P/t_P = 299\,792\,458 \text{ m/s}$ (SI units)
7. Fundamental length: $L_0 = \xi \cdot l_P = 2,155 \times 10^{-39} \text{ m}$
8. Fine structure constant: $\alpha = \xi \cdot E_0^2 = 1/137,036$

Consistency check:

$$\Delta G = \left| \frac{G_{T0} - G_{\text{SI}}}{G_{\text{SI}}} \right| < 0,0002\% \quad (66)$$

$$\Delta l_P = \left| \frac{l_P^{T0} - l_P^{\text{SI}}}{l_P^{\text{SI}}} \right| < 0,0002\% \quad (67)$$

$$\Delta \alpha = \left| \frac{\alpha_{T0} - \alpha_{\text{SI}}}{\alpha_{\text{SI}}} \right| < 0,0002\% \quad (68)$$

Glossary

ξ Fundamental geometric parameter, $\frac{4}{3} \times 10^{-4}$

S_{T0} Mass scaling factor, $1 \text{ MeV}/c^2$

L_0 Fundamental T0 length, $\xi \cdot l_P = 2,155 \times 10^{-39} \text{ m}$

E_0 Fundamental energy scale, $\sqrt{m_e \cdot m_\mu}$

$r_0(E)$ Characteristic length for energy E , $2GE$

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