

# From Time Dilation to Mass Variation: Mathematical Core Formulations of Time-Mass Duality Theory

Johann Pascher

March 29, 2025

## Zusammenfassung

This work presents the essential mathematical formulations of time-mass duality theory, focusing on the fundamental equations and their physical interpretations. The theory establishes a duality between two complementary descriptions of reality: the standard view with time dilation and constant rest mass, and the T0 model with absolute time and variable mass. Central to this framework is the intrinsic time  $T(x) = \frac{\hbar}{\max(mc^2, \omega)}$ , which enables a unified treatment of massive particles and photons. The mathematical formulations include modified Lagrangian densities that emphasize emergent gravitation and energy-loss redshift in a static universe.

## Inhaltsverzeichnis

<b>1</b>	<b>Introduction to Time-Mass Duality</b>	<b>2</b>
1.1	Relationship to the Standard Model . . . . .	2
<b>2</b>	<b>Emergent Gravitation from the Intrinsic Time Field</b>	<b>2</b>
<b>3</b>	<b>Mathematical Foundations: Intrinsic Time</b>	<b>2</b>
<b>4</b>	<b>Modified Derivative Operators</b>	<b>3</b>
<b>5</b>	<b>Modified Field Equations</b>	<b>3</b>
<b>6</b>	<b>Modified Lagrangian Density for the Higgs Field</b>	<b>3</b>
<b>7</b>	<b>Modified Lagrangian Density for Fermions</b>	<b>3</b>
<b>8</b>	<b>Modified Lagrangian Density for Gauge Bosons</b>	<b>3</b>
<b>9</b>	<b>Complete Total Lagrangian Density</b>	<b>3</b>
<b>10</b>	<b>Cosmological Implications</b>	<b>3</b>
<b>11</b>	<b>Derivation of <math>\beta_T</math> in the T0 Model</b>	<b>4</b>

# 1 Introduction to Time-Mass Duality

The time-mass duality theory proposes an alternative framework:

1. Standard View:  $t' = \gamma_{\text{Lorentz}} t$ ,  $m_0 = \text{const.}$
2. T0 Model:  $T_0 = \text{const.}$ ,  $m = \gamma_{\text{Lorentz}} m_0$

## 1.1 Relationship to the Standard Model

The T0 model extends the Standard Model with:

1. Intrinsic Time Field:  $T(x) = \frac{\hbar}{\max(mc^2, \omega)}$
2. Higgs Field:  $\Phi$  with dynamic mass coupling
3. Fermion Fields:  $\psi$  with Yukawa coupling
4. Gauge Boson Fields:  $A_\mu$  with  $T(x)$  interaction

## 2 Emergent Gravitation from the Intrinsic Time Field

**Theorem 2.1** (Emergence of Gravitation). *Gravitation arises from gradients of the intrinsic time field:*

$$\nabla T(x) = -\frac{\hbar}{m^2 c^2} \nabla m \quad (1)$$

with the modified potential:

$$\Phi(r) = -\frac{GM}{r} + \kappa r, \quad \kappa \approx 4.8 \times 10^{-11} \text{ m/s}^2 \quad (2)$$

*Beweis.* From  $T(x) = \frac{\hbar}{mc^2}$  for massive particles:

$$\nabla T(x) = -\frac{\hbar}{m^2 c^2} \nabla m \quad (3)$$

With  $m(\vec{r}) = m_0(1 + \frac{\Phi_g}{c^2})$ :

$$\nabla m = \frac{m_0}{c^2} \nabla \Phi_g \quad (4)$$

Thus:

$$\nabla T(x) \approx -\frac{\hbar}{m_0 c^4} \nabla \Phi_g \quad (5)$$

□

## 3 Mathematical Foundations: Intrinsic Time

**Theorem 3.1** (Intrinsic Time).

$$T(x) = \frac{\hbar}{\max(mc^2, \omega)} \quad (6)$$

## 4 Modified Derivative Operators

**Definition 4.1** (Modified Derivative). The modified covariant derivative in the T0 model is:

$$\partial_\mu \Psi + \Psi \partial_\mu T(x) = \partial_\mu \Psi + \Psi \partial_\mu T(x) \quad (7)$$

## 5 Modified Field Equations

**Theorem 5.1** (Modified Schrödinger Equation).

$$i\hbar T(x) \frac{\partial}{\partial t} \Psi + i\hbar \Psi \frac{\partial T(x)}{\partial t} = \hat{H} \Psi \quad (8)$$

## 6 Modified Lagrangian Density for the Higgs Field

**Theorem 6.1** (Higgs Lagrangian Density). *The Lagrangian density of the Higgs field with coupling to  $T(x)$  is:*

$$\begin{aligned} \mathcal{L}_{Higgs-T} = & |T(x)(\partial_\mu + igA_\mu)\Phi + \Phi \partial_\mu T(x)|^2 + \frac{1}{2} \partial_\mu T(x) \partial^\mu T(x) - V(T(x), \Phi), \\ & T(x)(\partial_\mu + igA_\mu)\Phi + \Phi \partial_\mu T(x) = T(x)(\partial_\mu + igA_\mu)\Phi + \Phi \partial_\mu T(x) \end{aligned} \quad (9)$$

## 7 Modified Lagrangian Density for Fermions

**Theorem 7.1** (Fermion Lagrangian Density).

$$\mathcal{L}_{Fermion} = \bar{\psi} i \gamma^\mu (\partial_\mu \psi + \psi \partial_\mu T(x)) - y \bar{\psi} \Phi \psi \quad (10)$$

## 8 Modified Lagrangian Density for Gauge Bosons

**Theorem 8.1** (Gauge Boson Lagrangian Density).

$$\mathcal{L}_{Boson} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \frac{1}{2} \partial_\mu T(x) \partial^\mu T(x) \quad (11)$$

## 9 Complete Total Lagrangian Density

**Theorem 9.1** (Total Lagrangian Density).

$$\mathcal{L}_{Total} = \mathcal{L}_{Boson} + \mathcal{L}_{Fermion} + \mathcal{L}_{Higgs-T} + \mathcal{L}_{intrinsic}, \quad \mathcal{L}_{intrinsic} = \frac{1}{2} \partial_\mu T(x) \partial^\mu T(x) - V(T(x)) \quad (12)$$

## 10 Cosmological Implications

The T0 model has the following implications:

- Modified Gravitational Potential:  $\Phi(r) = -\frac{GM}{r} + \kappa r$ ,  $\kappa \approx 4.8 \times 10^{-11} \text{ m/s}^2$
- Cosmic Redshift:  $1 + z = e^{\alpha d}$ ,  $\alpha \approx 2.3 \times 10^{-28} \text{ m}^{-1}$
- Wavelength Dependence:  $z(\lambda) = z_0(1 + \beta_T \ln(\lambda/\lambda_0))$ ,  $\beta_T \approx 0.008$  (SI units)

## 11 Derivation of $\beta_T$ in the T0 Model

The parameter  $\beta_T$  describes the coupling of the intrinsic time field  $T(x)$  to physical phenomena such as wavelength-dependent redshift. In the T0 model,  $\beta_T$  is precisely derived as:

$$\beta_T = \frac{\lambda_h^2 v^2}{16\pi^3} \cdot \frac{1}{m_h^2} \cdot \frac{1}{\xi} \quad (13)$$

where  $\lambda_h$  is the Higgs self-coupling,  $v$  is the Higgs vacuum expectation value,  $m_h$  is the Higgs mass, and  $\xi \approx 1.33 \times 10^{-4}$  is a dimensionless parameter defining the characteristic length scale  $r_0 = \xi \cdot l_P$  ( $l_P$ : Planck length). In natural units,  $\beta_T = 1$  holds, representing an exact theoretical prediction derived directly from the model parameters, as detailed in [11]. A comprehensive derivation and discussion of this parameter can be found in [11].

## Literatur

- [1] Pascher, J. (2025). [Time as an Emergent Property in Quantum Mechanics: A Connection Between Relativity, Fine-Structure Constant, and Quantum Dynamics](#). March 23, 2025.
- [2] Pascher, J. (2025). [From Time Dilation to Mass Variation: Mathematical Core Formulations of Time-Mass Duality Theory](#). March 29, 2025.
- [3] Pascher, J. (2025). [Dynamic Mass of Photons and Its Implications for Nonlocality in the T0 Model](#).
- [4] Pascher, J. (2025). [The Necessity of Extending Standard Quantum Mechanics and Quantum Field Theory](#). March 27, 2025.
- [5] Pascher, J. (2025). [Mass Variation in Galaxies: An Analysis in the T0 Model with Emergent Gravitation](#). March 30, 2025.
- [6] Pascher, J. (2025). [Mathematical Formulation of the Higgs Mechanism in Time-Mass Duality](#). March 28, 2025.
- [7] Pascher, J. (2025). [Field Theory and Quantum Correlations: A New Perspective on Instantaneity](#). March 28, 2025.
- [8] Pascher, J. (2025). [Compensatory and Additive Effects: An Analysis of Measurement Differences Between the T0 Model and the  \$\Lambda\$ CDM Standard Model](#). April 2, 2025.
- [9] Pascher, J. (2025). [Real Consequences of Reformulating Time and Mass in Physics: Beyond the Planck Scale](#). March 24, 2025.
- [10] Pascher, J. (2025). [Energy as a Fundamental Unit: Natural Units with  \$\alpha\_{EM} = 1\$  in the T0 Model](#). March 26, 2025.
- [11] Pascher, J. (2025). [Unified Unit System in the T0 Model: The Consistency of  \$\alpha = 1\$  and  \$\beta = 1\$](#) . April 5, 2025.
- [12] Pascher, J. (2025). [Adjustment of Temperature Units in Natural Units and CMB Measurements](#). April 2, 2025.
- [13] Pascher, J. (2025). [Time-Mass Duality Theory \(T0 Model\): Derivation of Parameters  \$\kappa\$ ,  \$\alpha\$ , and  \$\beta\$](#) . April 4, 2025.
- [14] Pascher, J. (2025). [Emergent Gravitation in the T0 Model: A Comprehensive Derivation](#). April 1, 2025.