# Time-Mass Duality Theory (T0 Model) Derivation of Parameters $\kappa$ , $\alpha$ and $\beta$

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#### Abstract

This document presents a complete theoretical analysis of the central parameters in the Time-Mass Duality Theory (T0 Model):

- 1. Fundamental derivations in natural units ( $\hbar=c=G=1$ )
- 2. Conversion to SI units for experimental predictions
- 3. Microscopic justification of the correlation length  $L_T$
- 4. Perturbative derivation of  $\beta$  via Feynman diagrams

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#### 1 Introduction

The T0 Model postulates a duality between temporal and mass-based descriptions of physical processes. The key parameters are:

- $\kappa$ : Modification of gravitational potential  $\Phi(r) = -\frac{GM}{r} + \kappa r$
- $\alpha$ : Photon energy loss rate  $(1 + z = e^{\alpha r})$
- $\beta$ : Wavelength dependence of redshift  $(z(\lambda) = z_0(1 + \beta \ln(\lambda/\lambda_0)))$

### 2 Introduction

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### 3 Derivation of $\kappa$

# 3.1 Natural units ( $\hbar = c = G = 1$ )

$$\kappa = \beta \frac{yv}{r_g}, \quad r_g = \sqrt{\frac{M}{a_0}}$$

where:

- y: Yukawa coupling (dimensionless)
- $v \approx 246$  GeV: Higgs vacuum expectation value

#### 3.2 SI units

$$\kappa_{\rm SI} = \beta \frac{yvc^2}{r_g^2} \approx 4.8 \times 10^{-11} \text{ m/s}^2$$

# 4 Derivation of $\alpha$

4.1 Natural units ( $\hbar = c = G = 1$ )

$$\alpha = \frac{\lambda_h^2 v}{L_T}, \quad L_T \sim \frac{M_{\rm Pl}}{m_h^2 v}$$

where:

•  $\lambda_h \approx 0.13$ : Higgs self-coupling

•  $L_T \approx 10^{26}$  m: Cosmic correlation length

4.2 SI units

$$\alpha_{\rm SI} = \frac{\lambda_h^2 vc^2}{L_T} \approx 2.3 \times 10^{-18}~{\rm m}^{-1}$$

### 5 Derivation of $\beta$

5.1 Natural units ( $\hbar = c = G = 1$ )

$$\beta = \frac{\lambda_h^2 v^2}{4\pi^2 \lambda_0 \alpha_0}$$

where:

•  $\lambda_0 \approx 500$  nm: Reference wavelength

•  $\alpha_0 = \alpha$  (as above)

### 5.2 Feynman diagram analysis



#### 5.3 Perturbative result

$$\beta = \frac{(2\pi)^4 m_h^2}{16\pi^2 v^4 y^2 M_{\rm Pl}^2 \lambda_0^4 \alpha_0} \approx 0.008$$

5.4 Experimental consequences

$$z(\lambda) = z_0 \left( 1 + 0.008 \ln \frac{\lambda}{\lambda_0} \right)$$

Detectable with JWST ( $\Delta z/z \sim 10^{-4}$ ).

# 6 Summary

| Parameter | Natural form   | SI value                            |
|-----------|--|-------------------------------------|
| $\kappa$  | $\beta \frac{yv}{r_a}$   | $4.8 \times 10^{-11} \text{ m/s}^2$ |
| $\alpha$  | $\frac{\lambda_h^2 \overset{\circ}{v}}{L_T}$                               | $2.3\times 10^{-18}~{\rm m}^{-1}$   |
| $\beta$   | $\frac{(2\pi)^4 m_h^2}{16\pi^2 v^4 y^2 M_{\rm Pl}^2 \lambda_0^4 \alpha_0}$ | 0.008                               |

# Appendix: Detailed Explanations

### 6.1 Microscopic justification of $L_T$

• Higgs fluctuations:

$$\langle \delta \Phi(x) \delta \Phi(0) \rangle \sim \frac{m_h}{16\pi^2 M_{\rm Pl}} e^{-m_h|x|}$$

• Microscopic scale:

$$L_h = \frac{1}{m_h} \approx 1.58 \times 10^{-9} \text{ m}$$

• Cosmic scale:

$$L_T \sim \frac{M_{\rm Pl}}{m_h^2 v} \approx 6.3 \times 10^{27}~{\rm m}$$

### 6.2 Dimensional analysis

In natural units ( $\hbar = c = G = 1$ ):

- $[m_h] = [v] = E = L^{-1}$
- $[M_{\rm Pl}] = E = L^{-1}$
- $\bullet \ \ [\alpha]=L^{-1},\, [\kappa]=L^{-2}$
- $[\beta] = 1$  (dimensionless)