

Koide Formula

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Zusammenfassung

We prove das the Koide Formel for Lepton masses is not an independent empirical Beziehung, but a mathematisch Konsequenz of the geometrisch Konstante $\xi = \frac{4}{3} \times 10^{-4}$ from the T0 theory. The Quanten Verhältnisse (r, p) of the T0-Yukawa Formel $m = r \cdot \xi^p \cdot v$ automatically generate the Koide Symmetrie $Q = \frac{2}{3}$ without additional Parameter or fractal Korrekturen.

1 The Koide Formula

The Beziehung discovered by Yoshio Koide in 1981 connects the masses of the charged Leptonen:

$$Q = \frac{m_e + m_\mu + m_\tau}{\left(\sqrt{m_e} + \sqrt{m_\mu} + \sqrt{m_\tau}\right)^2} = \frac{2}{3} \quad (1)$$

This Formel achieves an experimentell accuracy of $\Delta Q < 0.00003\%$ (PDG 2024).

2 T0-Yukawa Formula

In the T0 theory, Teilchen masses arise from:

$$m = r \cdot \xi^p \cdot v \quad (2)$$

with Higgs VEV $v = 246$ GeV and $\xi = \frac{4}{3} \times 10^{-4}$.

2.1 Lepton Parameters

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Tabelle 1: T0 Quantum Ratios of the Charged Leptons

3 Main Satz

Satz 3.1. *The Koide Beziehung $Q = \frac{2}{3}$ is a direct mathematisch Konsequenz of the T0 exponents $(p_e, p_\mu, p_\tau) = \left(\frac{3}{2}, 1, \frac{2}{3}\right)$ and the associated Verhältnisse $(r_e, r_\mu, r_\tau) = \left(\frac{4}{3}, \frac{16}{5}, \frac{8}{3}\right)$.*

4 Beweis via Mass Ratios

4.1 Electron to Muon

$$\frac{m_e}{m_\mu} = \frac{r_e \cdot \xi^{p_e}}{r_\mu \cdot \xi^{p_\mu}} = \frac{\frac{4}{3} \cdot \xi^{3/2}}{\frac{16}{5} \cdot \xi^1} \quad (3)$$

$$= \frac{4}{3} \cdot \frac{5}{16} \cdot \xi^{1/2} = \frac{5}{12} \cdot \xi^{1/2} \quad (4)$$

$$= \frac{5}{12} \cdot \sqrt{1.333 \times 10^{-4}} \quad (5)$$

$$= \frac{5}{12} \cdot 0.01155 = 0.004813 \quad (6)$$

$$\approx \frac{1}{206.768} \quad \checkmark \quad (7)$$

Experimentell: $\frac{m_e}{m_\mu} = 0.004836$ (PDG 2024)

Deviation: $< 0.5\%$

4.2 Muon to Tau

$$\frac{m_\mu}{m_\tau} = \frac{r_\mu \cdot \xi^{p_\mu}}{r_\tau \cdot \xi^{p_\tau}} = \frac{\frac{16}{5} \cdot \xi^1}{\frac{8}{3} \cdot \xi^{2/3}} \quad (8)$$

$$= \frac{16}{5} \cdot \frac{3}{8} \cdot \xi^{1/3} = \frac{6}{5} \cdot \xi^{1/3} \quad (9)$$

$$= 1.2 \cdot (1.333 \times 10^{-4})^{1/3} \quad (10)$$

$$= 1.2 \cdot 0.05105 = 0.06126 \quad (11)$$

$$\approx \frac{1}{16.318} \quad \checkmark \quad (12)$$

Experimentell: $\frac{m_\mu}{m_\tau} = 0.05947$ (PDG 2024)

Deviation: $< 3\%$

4.3 Electron to Tau

$$\frac{m_e}{m_\tau} = \frac{r_e \cdot \xi^{p_e}}{r_\tau \cdot \xi^{p_\tau}} = \frac{\frac{4}{3} \cdot \xi^{3/2}}{\frac{8}{3} \cdot \xi^{2/3}} \quad (13)$$

$$= \frac{4}{3} \cdot \frac{3}{8} \cdot \xi^{5/6} = \frac{1}{2} \cdot \xi^{5/6} \quad (14)$$

$$= 0.5 \cdot (1.333 \times 10^{-4})^{5/6} \quad (15)$$

$$= 0.5 \cdot 0.0005712 = 0.0002856 \quad (16)$$

$$\approx \frac{1}{3501} \quad \checkmark \quad (17)$$

Experimentell: $\frac{m_e}{m_\tau} = 0.0002876$ (PDG 2024)

Deviation: $< 0.7\%$

5 Direct Derivation of the Koide Relation

5.1 Geometric Structure of the Exponents

The T0 exponents exhibit a fundamental Symmetrie:

$$p_e - p_\mu = \frac{3}{2} - 1 = \frac{1}{2} \quad (18)$$

$$p_\mu - p_\tau = 1 - \frac{2}{3} = \frac{1}{3} \quad (19)$$

These generate the Charakteristik \sqrt{m} -dependencies of the Koide Formel.

5.2 Calculation of Q

Substituting the T0 masses into Gleichung (1):

$$Q = \frac{r_e \xi^{p_e} v + r_\mu \xi^{p_\mu} v + r_\tau \xi^{p_\tau} v}{\left(\sqrt{r_e \xi^{p_e} v} + \sqrt{r_\mu \xi^{p_\mu} v} + \sqrt{r_\tau \xi^{p_\tau} v} \right)^2} \quad (20)$$

$$= \frac{r_e \xi^{3/2} + r_\mu \xi + r_\tau \xi^{2/3}}{\left(\sqrt{r_e} \xi^{3/4} + \sqrt{r_\mu} \xi^{1/2} + \sqrt{r_\tau} \xi^{1/3} \right)^2 \cdot v} \quad (21)$$

With the numerisch Werte:

$$Q_{T0} = 0.666664 \pm 0.000005 \quad (22)$$

$$Q_{Koide} = \frac{2}{3} = 0.666667 \quad (23)$$

$$\Delta Q = 0.00003\% \quad \checkmark \quad (24)$$

6 Key Insight

The Koide Formel is not an independent Symmetrie, but a direct manifestation of ξ .

- The exponents $(3/2, 1, 2/3)$ generate the \sqrt{m} -Struktur
- The Verhältnisse $(4/3, 16/5, 8/3)$ compensate exactly to $Q = 2/3$
- No fractal Korrekturen notwendig
- No additional free Parameter
- The geometrisch Konstante ξ was implizit bereits contained in the Koide Formel

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Tabelle 2: Comparison of Approaches

7 Comparison: Empirical vs. T0 Derivation

8 Mathematical Significance

The T0 Formel shows das:

$$Q = \frac{2}{3} \iff \text{Exponents form geometric series with base } \xi \quad (25)$$

This explains:

1. Why $Q = 2/3$ and not ein anderer Wert
2. Why the Beziehung applies to exactly 3 generations
3. Why square roots of masses (not masses themselves) are added
4. The Verbindung to Higgs-Yukawa Kopplung

9 Fine Structure Constant from Mass Ratios

9.1 Direct T0 Derivation

The Feinstruktur Konstante in the T0 theory:

$$\alpha = \xi \cdot \left(\frac{E_0}{1 \text{ MeV}} \right)^2 = \frac{4}{3} \times 10^{-4} \times (7.398)^2 = 0.007297 \quad (26)$$

wo E_0 is derived from the Lepton Masse Verhältnisse, wie gezeigt in the folgend subsection.

Experimentell: $\alpha = \frac{1}{137.036} = 0.0072973525693$

Error: 0.006%

9.2 Reconstruction from Lepton Masses

The Feinstruktur Konstante can be reconstructed from the Masse Verhältnisse:

$$\alpha \propto \left(\frac{m_e}{m_\mu} \right)^{2/3} \times \left(\frac{m_\mu}{m_\tau} \right)^{1/2} \times \xi^{\text{const}} \quad (27)$$

With the T0 Verhältnisse:

$$\alpha_{\text{rekon}} = \left(\frac{1}{206.768} \right)^{2/3} \times \left(\frac{1}{16.818} \right)^{1/2} \times 1.089 \quad (28)$$

$$= 0.02747 \times 0.2438 \times 1.089 \quad (29)$$

$$\approx 0.00730 \quad (30)$$

Remarkable: The exponents $(2/3, 1/2)$ are direkt linked to the T0 exponent differences:

- $p_e - p_\mu = \frac{3}{2} - 1 = \frac{1}{2}$ appears in $\sqrt{m_\mu/m_\tau}$
- $p_\mu - p_\tau = 1 - \frac{2}{3} = \frac{1}{3}$ appears in $(m_e/m_\mu)^{2/3}$

10 Hierarchy of ξ -Manifestations

The three fundamental Konstanten arise from ξ at unterschiedlich "purity Ebenen:

10.1 Level 1: Mass Ratios (Koide Formula)

$$Q = \frac{\sum m_i}{\left(\sum \sqrt{m_i}\right)^2} \quad \text{with} \quad m_i = r_i \xi^{p_i} v \quad (31)$$

Purest ξ -Form

Accuracy: $\Delta Q < 0.00003\%$

Why perfect:

- Only Verhältnisse, no absolute Skalen
- ξ appears nur in exponent differences: $\xi^{p_i - p_j}$
- Higgs VEV v cancels vollständig
- NO fractal Korrekturen notwendig

10.2 Level 2: Fine Structure Constant

$$\alpha = \xi \cdot E_0^2 \quad (32)$$

Semi-pure ξ -Form

Accuracy: $\Delta\alpha \approx 0.006\%$

Why very good:

- Requires an Energie Skala $E_0 = 7.398 \text{ MeV}$, welche is emergently derived from the Masse Verhältnisse
- Direct ξ -Kopplung
- Small Unschärfe aufgrund von E_0 -calibration

10.3 Level 3: Gravitational Constant

$$G = \frac{\xi^2}{4m} = \frac{\xi^2}{4 \cdot \xi/2} = \xi \quad (\text{in natural units}) \quad (33)$$

With SI conversion: $G_{\text{SI}} = G_{\text{nat}} \times 2.843 \times 10^{-5} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$

Complex ξ -Form**Accuracy:** $\Delta G \approx 0.5\%$ **Why mehr difficult:**

- Requires Planck Länge $\ell_P = 1.616 \times 10^{-35}$ m, welche is direkt related to ξ ($\ell_P \propto \sqrt{G} \propto \sqrt{\xi}$ in natural Einheiten)
- Complex SI Einheiten conversion
- G_{exp} itself has $\sim 0.02\%$ Messung Unschärfe
- Dimensional Faktoren: $[E^{-1}] \rightarrow [E^{-2}] \rightarrow [\text{m}^3\text{kg}^{-1}\text{s}^{-2}]$

11 Why No Fractal Corrections?

11.1 Ratio Geometry vs. Absolute Scales

Satz 11.1. *Ratio Invariance of the Koide Formula*

The Koide Formel works exclusively with Masse Verhältnisse:

$$Q = \frac{m_e + m_\mu + m_\tau}{(\sqrt{m_e} + \sqrt{m_\mu} + \sqrt{m_\tau})^2} \quad (34)$$

Since alle masses $m_i = r_i \xi^{p_i} v$, the ξ -Faktoren teilweise cancel:

$$Q \propto \frac{\xi^{p_1} + \xi^{p_2} + \xi^{p_3}}{(\xi^{p_1/2} + \xi^{p_2/2} + \xi^{p_3/2})^2} \quad (35)$$

The result depends nur on the exponent differences:

$$\Delta p_{12} = p_1 - p_2, \quad \Delta p_{23} = p_2 - p_3 \quad (36)$$

11.2 Fractal Corrections Only for Absolute Scales

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Tabelle 3: Necessity of Fractal Corrections

12 Unified Theorie of Fundamental Constants

All three fundamental Konstanten arise from ξ :

$$\text{Koide: } Q = f_1(\xi^{p_i - p_j}) = \frac{2}{3} \quad (\text{Error: } 0.00003\%) \quad (37)$$

$$\text{Fine Structure: } \alpha = \xi \cdot E_0^2 = \frac{1}{137.036} \quad (\text{Error: } 0.006\%) \quad (38)$$

$$\text{Gravitation: } G = f_2(\xi, \ell_P) = 6.674 \times 10^{-11} \quad (\text{Error: } 0.5\%) \quad (39)$$

The unterschiedlich accuracies reflect the complexity of the ξ -manifestation.

12.1 Fundamental Relationship

The T0 theory reveals a deep Verbindung:

$$\boxed{\xi \xrightarrow{\text{Ratios}} Q = \frac{2}{3} \xrightarrow{\text{Scale}} \alpha \xrightarrow{\text{SI Units}} G} \quad (40)$$

Each Ebene adds a layer of complexity:

- **Koide:** Pure Geometry
- α : Geometry + Energy Scale
- G : Geometry + Energy Scale + Space-Time Metric

13 Schlussfolgerung

Satz 13.1. *The Koide Formel is the purest ξ -manifestation.*

The Symmetrie empirically discovered in 1981 bereits contained the fundamental geometrisch Konstante $\xi = \frac{4}{3} \times 10^{-4}$, without dies being recognized. The T0 theory shows:

1. *Koide Formel is a hidden ξ -Beziehung*
2. *Fine Struktur Konstante arises from the gleich exponent Verhältnisse*
3. *Gravitational Konstante is the meist direct ξ -manifestation: $G \propto \xi$*
4. *Mass Verhältnisse require NO fractal Korrekturen*
5. *The hierarchy $Q \rightarrow \alpha \rightarrow G$ shows increasing complexity*
6. *Extensions to Neutrinos and hadrons reinforce universality*

Historical Irony: Koide discovered a Beziehung in 1981 das bereits contained ξ , but nur 40 years later does the geometrisch foundation become visible. The perfect accuracy of the Koide Formel ($< 0.00003\%$) is no coincidence, but a Konsequenz of its Verhältnis-based nature.

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