# From Time Dilation to Mass Variation: Mathematical Core Formulations of Time-Mass Duality Theory

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#### Zusammenfassung

This work presents the essential mathematical formulations of time-mass duality theory, focusing on the fundamental equations and their physical interpretations. The theory establishes a duality between two complementary descriptions of reality: the standard view with time dilation and constant rest mass, and the T0 model with absolute time and variable mass. Central to this framework is the intrinsic time  $T(x) = \frac{\hbar}{\max(mc^2,\omega)}$ , which enables a unified treatment of massive particles and photons. The mathematical formulations include modified Lagrangian densities that emphasize emergent gravitation and energy-loss redshift in a static universe.

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## 1 Introduction to Time-Mass Duality

The time-mass duality theory proposes an alternative framework:

- 1. Standard View:  $t' = \gamma_{\text{Lorentz}}t$ ,  $m_0 = \text{const.}$
- 2. To Model:  $T_0 = \text{const.}, m = \gamma_{\text{Lorentz}} m_0$

#### 1.1 Relationship to the Standard Model

The T0 model extends the Standard Model with:

- 1. Intrinsic Time Field:  $T(x) = \frac{\hbar}{\max(mc^2,\omega)}$
- 2. Higgs Field:  $\Phi$  with dynamic mass coupling
- 3. Fermion Fields:  $\psi$  with Yukawa coupling
- 4. Gauge Boson Fields:  $A_{\mu}$  with T(x) interaction

## 2 Emergent Gravitation from the Intrinsic Time Field

**Theorem 2.1** (Emergence of Gravitation). Gravitation arises from gradients of the intrinsic time field:

$$\nabla T(x) = -\frac{\hbar}{m^2 c^2} \nabla m \tag{1}$$

with the modified potential:

$$\Phi(r) = -\frac{GM}{r} + \kappa r, \quad \kappa \approx 4.8 \times 10^{-11} \, \text{m/s}^2 \tag{2}$$

Beweis. From  $T(x) = \frac{\hbar}{mc^2}$  for massive particles:

$$\nabla T(x) = -\frac{\hbar}{m^2 c^2} \nabla m \tag{3}$$

With  $m(\vec{r}) = m_0(1 + \frac{\Phi_g}{c^2})$ :

$$\nabla m = \frac{m_0}{c^2} \nabla \Phi_g \tag{4}$$

Thus:

$$\nabla T(x) \approx -\frac{\hbar}{m_0 c^4} \nabla \Phi_g \tag{5}$$

#### 3 Mathematical Foundations: Intrinsic Time

Theorem 3.1 (Intrinsic Time).

$$T(x) = \frac{\hbar}{\max(mc^2, \omega)} \tag{6}$$

#### 4 Modified Derivative Operators

**Definition 4.1** (Modified Derivative). The modified covariant derivative in the T0 model is:

$$\partial_{\mu}\Psi + \Psi \partial_{\mu}T(x) = \partial_{\mu}\Psi + \Psi \partial_{\mu}T(x) \tag{7}$$

## 5 Modified Field Equations

Theorem 5.1 (Modified Schrödinger Equation).

$$i\hbar T(x)\frac{\partial}{\partial t}\Psi + i\hbar\Psi\frac{\partial T(x)}{\partial t} = \hat{H}\Psi$$
 (8)

## 6 Modified Lagrangian Density for the Higgs Field

**Theorem 6.1** (Higgs Lagrangian Density). The Lagrangian density of the Higgs field with coupling to T(x) is:

$$\mathcal{L}_{Higgs-T} = |T(x)(\partial_{\mu} + igA_{\mu})\Phi + \Phi\partial_{\mu}T(x)|^{2} + \frac{1}{2}\partial_{\mu}T(x)\partial^{\mu}T(x) - V(T(x), \Phi),$$

$$T(x)(\partial_{\mu} + igA_{\mu})\Phi + \Phi\partial_{\mu}T(x) = T(x)(\partial_{\mu} + igA_{\mu})\Phi + \Phi\partial_{\mu}T(x) \quad (9)$$

#### 7 Modified Lagrangian Density for Fermions

Theorem 7.1 (Fermion Lagrangian Density).

$$\mathcal{L}_{Fermion} = \bar{\psi}i\gamma^{\mu}(\partial_{\mu}\psi + \psi\partial_{\mu}T(x)) - y\bar{\psi}\Phi\psi \tag{10}$$

## 8 Modified Lagrangian Density for Gauge Bosons

Theorem 8.1 (Gauge Boson Lagrangian Density).

$$\mathcal{L}_{Boson} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \frac{1}{2} \partial_{\mu} T(x) \partial^{\mu} T(x)$$
(11)

#### 9 Complete Total Lagrangian Density

Theorem 9.1 (Total Lagrangian Density).

$$\mathcal{L}_{Total} = \mathcal{L}_{Boson} + \mathcal{L}_{Fermion} + \mathcal{L}_{Higgs-T} + \mathcal{L}_{intrinsic}, \quad \mathcal{L}_{intrinsic} = \frac{1}{2} \partial_{\mu} T(x) \partial^{\mu} T(x) - V(T(x)) \quad (12)$$

## 10 Cosmological Implications

The T0 model has the following implications:

- Modified Gravitational Potential:  $\Phi(r) = -\frac{GM}{r} + \kappa r$ ,  $\kappa \approx 4.8 \times 10^{-11} \, \text{m/s}^2$
- Cosmic Redshift:  $1+z=e^{\alpha d},\ \alpha\approx 2.3\times 10^{-28}\,\mathrm{m}^{-1}$
- Wavelength Dependence:  $z(\lambda) = z_0(1 + \beta_T \ln(\lambda/\lambda_0)), \beta_T \approx 0.008$  (SI units)

## 11 Derivation of $\beta_T$ in the T0 Model

The parameter  $\beta_{\rm T}$  describes the coupling of the intrinsic time field T(x) to physical phenomena such as wavelength-dependent redshift. In the T0 model,  $\beta_{\rm T}$  is precisely derived as:

$$\beta_{\rm T} = \frac{\lambda_h^2 v^2}{16\pi^3} \cdot \frac{1}{m_h^2} \cdot \frac{1}{\xi} \tag{13}$$

where  $\lambda_h$  is the Higgs self-coupling, v is the Higgs vacuum expectation value,  $m_h$  is the Higgs mass, and  $\xi \approx 1.33 \times 10^{-4}$  is a dimensionless parameter defining the characteristic length scale  $r_0 = \xi \cdot l_P$  ( $l_P$ : Planck length). In natural units,  $\beta_T = 1$  holds, representing an exact theoretical prediction derived directly from the model parameters, as detailed in [11]. A comprehensive derivation and discussion of this parameter can be found in [11].

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