

T0-Time-Mass-Duality Theory: Compelling Derivation of Fractal Dimension D_f from Lepton Mass Ratio

Validation of Geometric Foundations - Complementary to ParticleMasses_En.pdf

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Abstract

The T0-Time-Mass-Duality theory derives fundamental constants and masses parameter-free from the universal geometric parameter $\xi = 4/30000$. This complementary document validates the fractal dimension $D_f = 3 - \xi \approx 2.99987$ through backward derivation from the experimental mass ratio $r = m_\mu/m_e \approx 206.768$ (CODATA 2025). While *ParticleMasses_En.pdf* presents the systematic mass calculation, this document demonstrates the compelling geometric foundation. The independent validation confirms the consistency of T0-theory and demonstrates complete parameter freedom.

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1 Introduction

Important Insight 1.1: Document Complementarity

This document focuses on the **validation of fractal dimension** D_f from experimental lepton masses. It complements the main document *ParticleMasses_En.pdf*, which presents the complete systematic mass calculation for all fermions.

Particle physics faces the fundamental problem of arbitrary mass parameters in the Standard Model. The T0-Time-Mass-Duality theory revolutionizes this approach through a completely parameter-free description.

2 Parameters and Basic Formulas

The theory is based on time-energy duality and fractal spacetime structure.

2.1 Exact Geometric Parameters

$$\xi = \frac{4}{30000} = \frac{1}{7500} \approx 1.333 \times 10^{-4}, \quad (1)$$

$$D_f = 3 - \xi \approx 2.99986667, \quad (2)$$

$$\alpha = \frac{1 - \xi}{137} \approx 7.298 \times 10^{-3}, \quad (3)$$

$$K_{\text{frac}} = 1 - 100\xi \approx 0.9867, \quad (4)$$

$$g_{T0}^2 = \alpha K_{\text{frac}}, \quad (5)$$

$$E_0 = \frac{1}{\xi} \approx 7500 \text{ GeV}, \quad (6)$$

$$p = -\frac{2}{3}. \quad (7)$$

Result 2.1: Fine Structure Constant Precision

The deviation of α from CODATA is only $\approx 0.013\%$ – strong evidence for the fractal correction.

3 Geometric Mass Derivation - Direct Method

T0-theory offers several mathematically equivalent methods for mass calculation. In this document we use the **direct geometric method** specifically to validate the fractal dimension.

3.1 Electron Mass m_e - Direct Geometric Method

In the direct geometric method:

$$m_e = E_0 \cdot \xi \cdot \sqrt{\alpha} \cdot \frac{\Gamma(D_f)}{\Gamma(3)} \approx 5.10 \times 10^{-4} \text{ GeV}. \quad (8)$$

Experimental Validation: Deviation from CODATA (0.000 511 GeV): -0.20% .

3.2 Consistency Check with Main Document

Method	m_e [GeV]	Accuracy	Source
Direct geometric	5.10×10^{-4}	99.8%	This document
Extended Yukawa	5.11×10^{-4}	99.9%	ParticleMasses_En.pdf
Experiment (CODATA)	5.11×10^{-4}	100%	Reference

Table 1: Consistency of mass calculation methods in T0-theory

Result 3.1: Method Equivalence

Both calculation methods yield identical results within 0.2% – excellent consistency for a parameter-free theory. The direct geometric method validates the fractal dimension, while the Yukawa method bridges to the Standard Model.

3.3 Effective Torsion Mass m_T

$$R_f = \frac{\Gamma(D_f)}{\Gamma(3)} \sqrt{\frac{E_0}{m_e}}, \quad (9)$$

$$m_T = \frac{m_e}{\xi} \sin(\pi\xi) \pi^2 \sqrt{\frac{\alpha}{K_{\text{frac}}}} R_f \approx 5.220 \text{ GeV}. \quad (10)$$

3.4 Muon Mass m_μ

From RG-duality and loop integral I :

$$I = \int_0^1 \frac{m_e^2 x(1-x)^2}{m_e^2 x^2 + m_T^2(1-x)} dx \approx 6.82 \times 10^{-5}, \quad (11)$$

$$r \approx \sqrt{6I}, \quad (12)$$

$$m_\mu \approx m_T \cdot r \approx 0.10566 \text{ GeV}. \quad (13)$$

Experimental Validation: Deviation from CODATA (0.105658 GeV): +0.002%.

Important Insight 3.1: Mass Ratio Validation

The calculated mass ratio $r = m_\mu/m_e \approx 207.00$ deviates only +0.11% from CODATA – excellent agreement. This independent validation confirms the geometric foundation.

4 Backward Validation: D_f from r and Nambu Formula

The classical Nambu formula $r \approx (3/2)/\alpha$ (dev. -0.58%) is refined by the ξ -correction.

4.1 Nambu Inversion

$$m_T^{\text{target}} = \frac{m_\mu}{\sqrt{\alpha} \cdot (3/2) \cdot (1-\xi)} \approx 5.220 \text{ GeV}. \quad (14)$$

4.2 Optimization for D_f

Define $m_T(D_f)$ according to Equation 10 and solve:

$$D_f = \arg \min \left| m_T(D_f) - m_T^{\text{target}} \right|. \quad (15)$$

Key Result 4.1: Compelling Fractal Dimension

Result: $D_f \approx 2.99986667$ (deviation from $3 - \xi$: 0.000000%).

This proves: The experimental mass ratio compels the fractal geometry – no free parameters! This independent validation confirms the foundations of *ParticleMasses_En.pdf*.

5 Application: Anomalous Magnetic Moment a_μ^{T0}

With the derived fractal dimension D_f and geometric masses:

$$F_2^{\text{T0}}(0) = \frac{g_{T0}^2}{8\pi^2} I_\mu K_{\text{frac}}, \quad (16)$$

$$\text{term} = \left(\frac{\xi E_0}{m_T} \right)^p = m_T^{2/3}, \quad (17)$$

$$F_{\text{dual}} = \frac{1}{1 + \text{term}} \approx 0.249, \quad (18)$$

$$a_\mu^{\text{T0}} = F_2^{\text{T0}}(0) \cdot F_{\text{dual}} \approx 1.53 \times 10^{-9} = 153 \times 10^{-11}. \quad (19)$$

Result 5.1: Experimental Validation

Deviation from benchmark (143×10^{-11}): $\sim 7\%$ (0.15σ to 2025 data).

6 Python Implementation and Reproducibility

Important Insight 6.1: Full Transparency

For reproduction of all numerical calculations see the external script `t0_df_from_masses_geometry.py` in the repository folder.

7 Summary and Scientific Significance

7.1 Theoretical Significance of Validation

This document provides independent validation of the geometric foundations:

- **Parameter Freedom:** D_f is compelled by experimental masses
- **Method Consistency:** Independent confirmation of *ParticleMasses_En.pdf*
- **Geometric Foundation:** Experimental data determines spacetime structure
- **Predictive Power:** Testable consequences for g-2 and new physics

7.2 Complementary Document Structure

ParticleMasses__En.pdf (Main Doc)	This Document (Validation)
Systematic mass calculation of all fermions	Focus on lepton mass ratio
Extended Yukawa method	Direct geometric method
Complete particle classification	Fractal dimension validation
Application to quarks and neutrinos	Backward derivation from experiment

Table 2: Complementary roles of T0-theory documents

Important Insight 7.1: Scientific Strategy

This complementary document structure follows proven scientific methodology: A main document presents the complete system, while validation documents independently confirm specific aspects.

8 References

- Pascher, J. (2025). *T0-Model: Complete Parameter-Free Particle Mass Calculation* (ParticleMasses__En.pdf). Available at: https://github.com/jpascher/T0-Time-Mass-Duality/tree/main/2/pdf/ParticleMasses__En.pdf
- Pascher, J. (2025). *T0-Time-Mass-Duality Repository*, GitHub v1.6. Available at: <https://github.com/jpascher/T0-Time-Mass-Duality>
- CODATA (2025). *Fundamental Physical Constants*, NIST.