

$$\textcircled{1} \lim_{x \rightarrow -3^+} \frac{x+2}{x+3} \rightsquigarrow \left( \lim_{x \rightarrow -3^+} x+2 \right) \cdot \left( \lim_{x \rightarrow -3^+} \frac{1}{x+3} \right)$$

$$-1 \cdot \frac{1}{0^++3} = -\infty$$

$$\textcircled{2} \lim_{x \rightarrow -3^-} \frac{x+2}{x+3} \rightsquigarrow \left( \lim_{x \rightarrow -3^-} x+2 \right) \cdot \left( \lim_{x \rightarrow -3^-} \frac{1}{x+3} \right)$$

$$(-1) \cdot \frac{1}{0^-+3} = +\infty$$

$$\textcircled{3} \lim_{x \rightarrow 3^+} \frac{\sqrt{x^2-9}}{x-3} \rightsquigarrow \lim_{x \rightarrow 3^+} \sqrt{x^2-9} \cdot \lim_{x \rightarrow 3^+} \frac{1}{x-3}$$

$$(\sqrt{0^+}) \cdot \left( \frac{1}{0^+} \right) = +\infty$$

$$4) \lim_{x \rightarrow 2} \frac{x^2-2x}{x^2-4x+4} \rightsquigarrow \frac{x(x-2)}{(x-2)(x+2)} \rightsquigarrow \frac{x}{x+2} = \frac{2}{-\infty} = -\infty$$

$$5) \lim_{y \rightarrow +\infty} \frac{2-3y^2}{5y^2+4y} \rightsquigarrow \lim_{y \rightarrow +\infty} \frac{2}{5y^2+4y} \cdot \lim_{y \rightarrow +\infty} -\frac{3y^2}{y(5+\frac{4}{y})}$$

$$\frac{-3}{5+\frac{4}{y}} \rightsquigarrow \boxed{\frac{-3}{5}}$$

$$6) \lim_{t \rightarrow +\infty} \frac{\sqrt{t}+t^2}{2t-t^2} \rightsquigarrow \frac{\sqrt{t}}{2t-t^2} + \frac{t^2}{2t-t^2} \rightsquigarrow \lim_{t \rightarrow +\infty} \frac{\sqrt{t}}{2t-t^2} \cdot \lim_{t \rightarrow +\infty} \frac{t^2}{2t-t^2}$$

$$\lim_{t \rightarrow +\infty} \frac{t^2}{t(2-\frac{1}{t})} \rightsquigarrow \frac{1}{(\frac{1}{t}-1)} = \boxed{-1}$$

$$07) \lim_{x \rightarrow +\infty} \frac{\sqrt{4x^2 - x}}{x+1} \cdot \frac{\sqrt{4x^2 - x}}{\sqrt{4x^2 - x}} \leadsto \frac{4x^2 - x}{(x+1)(\sqrt{4x^2 - x})} \leadsto \frac{x^2(4 - \frac{1}{x})}{x(1 + \frac{1}{x})(x\sqrt{4 - \frac{1}{x}})}$$

$$\frac{4 - \frac{1}{x}}{(1 + \frac{1}{x})(\sqrt{4 - \frac{1}{x}})} \leadsto \frac{4}{2} = \boxed{2}$$

$$8) \lim_{x \rightarrow \infty} \frac{\sqrt{4x^2 - x}}{x+1} \cdot \frac{\sqrt{4x^2 - x}}{\sqrt{4x^2 - x}} \leadsto \frac{4x^2 - x}{(x+1)(\sqrt{4x^2 - x})} \leadsto \frac{x^2(4 - \frac{1}{x})}{x(1 + \frac{1}{x})(x\sqrt{4 - \frac{1}{x}})}$$

$$\frac{4 - \frac{1}{x}}{(1 + \frac{1}{x})(\sqrt{4 - \frac{1}{x}})} \leadsto \frac{4}{2} = \boxed{2}$$

$$9) y = \frac{2x+1}{x-2} \leadsto \frac{x(2 + \frac{1}{x})}{x(1 - \frac{2}{x})} \leadsto \frac{2 + \frac{1}{x}}{1 - \frac{2}{x}}$$

$$\lim_{x \rightarrow \infty^+} \frac{2 + \frac{1}{x}}{1 - \frac{2}{x}} = \boxed{2} \quad / \quad \lim_{x \rightarrow \infty^-} \frac{2 + \frac{1}{x}}{1 - \frac{2}{x}} = \boxed{2} \leadsto \boxed{y=2} \text{ Horizontal}$$

$$x-2=0 \quad \boxed{x=2} \leadsto \lim_{x \rightarrow 2^-} \frac{2x+1}{x-2} = \frac{2x}{x-2} + \frac{1}{x-2} \leadsto \lim_{x \rightarrow 2^-} \frac{2x}{x-2} \rightarrow -\infty + \lim_{x \rightarrow 2^-} \frac{1}{x-2} \rightarrow -\infty$$

$$\lim_{x \rightarrow 2^-} \frac{2x+1}{x-2} = -\infty$$

$$\lim_{x \rightarrow 2^+} \frac{2x+1}{x-2} \leadsto \lim_{x \rightarrow 2^+} \frac{2x}{x-2} + \lim_{x \rightarrow 2^+} \frac{1}{x-2} = +\infty + +\infty = +\infty$$

$$\boxed{x=2} \text{ vertical}$$

$$10) y = \frac{3x^2 + x - 1}{x^2 + x - 2} \rightsquigarrow \frac{x^2(3 + \frac{1}{x} - \frac{1}{x^2})}{x^2(1 + \frac{1}{x} - \frac{2}{x^2})}$$

$$\lim_{x \rightarrow +\infty} \frac{3 + \frac{1}{x} - \frac{1}{x^2}}{1 + \frac{1}{x} - \frac{2}{x^2}} = \frac{3}{1} = 3 \quad / \quad \lim_{x \rightarrow -\infty} \frac{3 + \frac{1}{x} - \frac{1}{x^2}}{1 + \frac{1}{x} - \frac{2}{x^2}} = 3 \rightsquigarrow \boxed{y=3} \rightsquigarrow \text{Horizontal}$$

$$x^2 + x - 2 = 0 \rightsquigarrow (x-1)(x+2) = 0, \quad x=1, \quad x=-2$$

$$\lim_{x \rightarrow 1^-} \frac{3x^2 + x - 1}{x^2 + x - 2} \rightsquigarrow \frac{\lim_{x \rightarrow 1^-} 3x^2 + x - 1}{\lim_{x \rightarrow 1^-} (x-1)(x+2)} = \frac{3}{0^-} = -\infty$$

$$\lim_{x \rightarrow 1^+} \frac{3x^2 + x - 1}{x^2 + x - 2} \rightsquigarrow \frac{\lim_{x \rightarrow 1^+} 3x^2 + x - 1}{\lim_{x \rightarrow 1^+} (x-1)(x+2)} = \frac{3}{0^+} = +\infty$$

$$\lim_{x \rightarrow -2^-} \frac{3x^2 + x - 1}{x^2 + x - 2} \rightsquigarrow \frac{\lim_{x \rightarrow -2^-} 3x^2 + x - 1}{\lim_{x \rightarrow -2^-} (x-1)(x+2)} = \frac{9}{0^+} = +\infty$$

$$\lim_{x \rightarrow -2^+} \frac{3x^2 + x - 1}{x^2 + x - 2} \rightsquigarrow \frac{\lim_{x \rightarrow -2^+} 3x^2 + x - 1}{\lim_{x \rightarrow -2^+} (x-1)(x+2)} = \frac{9}{0^-} = -\infty$$