```
term variable
\boldsymbol{x}
      type variable
\alpha
T
      type constructor
      coercion variable
c
t
           ::=
                                                        _{\text{term}}
                                                            variable
                   \lambda(x:\tau) \Rightarrow t
                                                            abstraction
                   \lambda\{\alpha:\kappa\}\Rightarrow t
                                                            type abstraction
                   \lambda\{c: \tau_1 \sim \tau_2\} \Rightarrow t
                                                            coercion abstraction
                                                            application
                    t [\tau]
                                                            type application
                    t \sim [\gamma]
                                                            coercion application
                                                            type annotation
                                                            coercion
                                                        kind
\kappa
                                                            star
                                                            kind arrow
                   \kappa_1 \to \kappa_2
                                                        type
                                                            type variable
                                                            type constructor
                                                            \equiv (\rightarrow) \ \tau_1 \ \tau_2
                    \{\tau_1 \sim \tau_2\} \to \tau_3  \lambda(\alpha:\kappa), \tau 
                                                            coercion arrow
                                                            operator abstraction
                   \forall (\alpha : \kappa), \tau
                                                            universal quantification
                                                            operator application
                                                        coercion proof term
           ::=
                                                            variable
                   \operatorname{\mathbf{refl}} \tau
                                                            reflexivity
                                                            symmetry
                   \operatorname{sym} \gamma
                                                            composition
                   \gamma_1 \circ \gamma_2
                                                             \equiv (\rightarrow) \gamma_1 \gamma_2 \text{ where } (\rightarrow) : \text{refl } (\rightarrow)
                    \gamma_1 \rightarrow \gamma_2
                   \{\gamma_1 \sim \gamma_2\} \to \gamma_3
                                                            coercion arrow introduction
                   \lambda(\alpha:\kappa),\gamma
                                                            operator abstraction introduction
                   \forall (\alpha : \kappa), \gamma
                                                            universal quantification introduction
                                                            application introduction
                   \gamma_1 \gamma_2
                   left \gamma
                                                            left elimination
                   \mathbf{right} \, \gamma
                                                            right elimination
Γ
                                                         typing environment
                   Ø
                                                            empty
                   \Gamma, x : \tau
                                                            variable
                   \Gamma, T : \kappa
                                                            type constructor
                                                            type variable
                                                            coercion variable
                                                        typed value
tv
                   \lambda(x:\tau) \Rightarrow t
\lambda\{\alpha:\kappa\} \Rightarrow tv
                                                            abstraction
```

type abstraction

 $\frac{\Gamma \vdash \gamma : \tau_2 \sim \tau_1}{\Gamma \vdash \mathbf{sym} \ \gamma : \tau_1 \sim \tau_2} \quad \text{C\_Sym}$ 

 $\frac{\Gamma \vdash \gamma_1 : \tau_1 \sim \tau_2 \qquad \tau_2 \equiv \tau_2' \qquad \Gamma \vdash \gamma_2 : \tau_2' \sim \tau_3}{\Gamma \vdash \gamma_1 \circ \gamma_2 : \tau_1 \sim \tau_3} \quad \text{C-COMP}$ 

 $\Gamma \vdash \tau : \kappa$  Kinding rules

$$\frac{\alpha : \kappa \in \Gamma}{\Gamma \vdash \alpha : \kappa} \quad \text{K-VAR}$$

$$\frac{T : \kappa \in \Gamma}{\Gamma \vdash T : \kappa} \quad \text{K-TypeConstr}$$

$$\frac{\alpha \notin \Gamma \qquad \Gamma, \alpha : \kappa_1 \vdash \tau : \kappa_2}{\Gamma \vdash (\lambda(\alpha : \kappa_1), \tau) : \kappa_1 \to \kappa_2} \quad \text{K-Abs}$$

$$\frac{\Gamma \vdash \tau_1 : \kappa_2 \to \kappa_1 \qquad \Gamma \vdash \tau_2 : \kappa_2}{\Gamma \vdash \tau_1 \tau_2 : \kappa_1} \quad \text{K-App}$$

$$\frac{\Gamma \vdash \tau_1 : \kappa \qquad \Gamma \vdash \tau_2 : \kappa \qquad \Gamma \vdash \tau_3 : *}{\Gamma \vdash (\{\tau_1 \sim \tau_2\} \to \tau_3) : *} \quad \text{K_-CArrow}$$

$$\frac{\alpha \notin \Gamma \qquad \Gamma, \alpha : \kappa \vdash \tau : *}{\Gamma \vdash (\forall (\alpha : \kappa), \tau) : *} \quad \text{K_-Forall}$$

 $\tau_1 \equiv \tau_2$  Type equivalence

$$\frac{\tau \equiv \tau}{\tau \equiv \tau} \quad \text{EQ\_REFL}$$

$$\frac{\tau_2 \equiv \tau_1}{\tau_1 \equiv \tau_2} \quad \text{EQ\_SYM}$$

$$\frac{\tau_1 \equiv \tau_2 \qquad \tau_2 \equiv \tau_3}{\tau_1 \equiv \tau_3} \quad \text{EQ\_TRANS}$$

$$\frac{\tau_1 \equiv \tau_3}{\alpha \equiv \alpha} \quad \text{EQ\_VAR}$$

$$\overline{T \equiv T} \quad \text{EQ-TypeConstr}$$

$$\underline{\tau_1 \equiv \tau_1'} \quad \tau_2 \equiv \tau_2' \quad \tau_3 \equiv \tau_3' \quad \text{EQ-CArrow}$$

$$(\{\tau_1 \sim \tau_2\} \to \tau_3) \equiv (\{\tau_1' \sim \tau_2'\} \to \tau_3') \quad \text{EQ-CArrow}$$

$$\underline{\tau_1 \equiv \tau_2} \quad \text{EQ-Forall}$$

$$\underline{\forall (\alpha : \kappa), \tau_1 \equiv \forall (\alpha : \kappa), \tau_2} \quad \text{EQ-Abs}$$

$$\underline{\tau_1 \equiv \tau_2} \quad \text{EQ-Abs}$$

$$\underline{\tau_1 \equiv \tau_1'} \quad \tau_2 \equiv \tau_2' \quad \text{EQ-App}$$

$$\underline{\tau_1 \equiv \tau_1'} \quad \tau_2 \equiv \tau_1' \tau_2' \quad \text{EQ-App}$$

$$\underline{(\alpha \mapsto \tau_2] \ \tau_1 \rhd \tau_1'} \quad \text{EQ-AppAbs}$$

 $t \longrightarrow tv$  Operational semantics

$$\frac{t_2 \longrightarrow tv_2}{t_1 t_2 \longrightarrow tv_3} \qquad \text{E-APP1}$$

$$\frac{t \longrightarrow tv_1}{t tv_2 \longrightarrow tv_3} \qquad \text{E-APP2}$$

$$\frac{t \mapsto tv_1] \ t \rhd t' \qquad t' \longrightarrow tv_2}{(\lambda(x:\tau) \Rightarrow t) \ tv_1 \longrightarrow tv_2} \qquad \text{E-APPABS}$$

$$\frac{t \longrightarrow tv}{(\lambda\{\alpha:\kappa\} \Rightarrow t) \longrightarrow (\lambda\{\alpha:\kappa\} \Rightarrow tv)} \qquad \text{E-TABS}$$

$$\frac{t \longrightarrow tv}{(\lambda\{c:\tau_1 \sim \tau_2\} \Rightarrow t) \longrightarrow (\lambda\{c:\tau_1 \sim \tau_2\} \Rightarrow tv)} \qquad \text{E-CABS}$$

$$\frac{t \longrightarrow tv}{t \ [\tau] \longrightarrow tv \ [\tau]} \qquad \text{E-TAPP}$$

$$\frac{[\alpha \mapsto \tau] \ t \rhd t' \qquad t' \longrightarrow tv}{(\lambda\{\alpha:\kappa\} \Rightarrow t) \ [\tau] \longrightarrow tv} \qquad \text{E-TAPPABS}$$

$$\frac{t \longrightarrow tv}{(\lambda\{\alpha:\kappa\} \Rightarrow t) \ [\tau] \longrightarrow tv} \qquad \text{E-TAPPABS}$$

 $|tv \longrightarrow v|$  type erasure

$$\frac{tv \longrightarrow v}{(\lambda\{\alpha:\kappa\} \Rightarrow t) \longrightarrow t} \quad \text{ERASE\_ABS}$$

$$\frac{tv \longrightarrow v}{(\lambda\{\alpha:\kappa\} \Rightarrow tv) \longrightarrow v} \quad \text{ERASE\_TABS}$$

$$\begin{array}{c} tv \longrightarrow v \\ \hline (\lambda\{c:\tau_1 \sim \tau_2\} \Rightarrow tv) \longrightarrow v \\ \hline (tv\mid \tau|) \longrightarrow v \\ \hline (tv\mid \tau|)$$

$$\frac{[x \mapsto tv] \ t_1 \rhd t_2}{[x \mapsto tv] \ (t_1 \ [\tau]) \rhd (t_2 \ [\tau])} \quad \text{Subst\_TApp}$$

$$\frac{[x \mapsto tv] \ t_1 \rhd t_2}{[x \mapsto tv] \ (t_1 \sim [\gamma]) \rhd (t_2 \sim [\gamma])} \quad \text{Subst\_CApp}$$

$$\frac{[x \mapsto tv] \ t_1 \rhd t_2}{[x \mapsto tv] \ (t_1 : \tau) \rhd (t_2 : \tau)} \quad \text{Subst\_Annot}$$

$$\frac{[x \mapsto tv] \ t_1 \rhd t_2}{[x \mapsto tv] \ (t_1 \triangleright \tau) \rhd (t_2 \triangleright \tau)} \quad \text{Subst\_Coerce}$$

 $[\alpha \mapsto \tau] \ t_1 \rhd t_2$ 

substitution of type variable in term

Definition rules: 80 good 3 bad Definition rule clauses: 153 good 3 bad