```
term variable
\boldsymbol{x}
      type variable
\alpha
T
      type
      coercion variable
c
t
                                                        term
                                                            variable
                  \lambda(x:\tau) \Rightarrow t
                                                            abstraction
                  \lambda\{\alpha:\kappa\}\Rightarrow t
                                                            type abstraction
                  \lambda \{c: \tau_1 \sim \tau_2\} \Rightarrow t
                                                            coercion abstraction
                                                            application
                  t [\tau]
                                                            type application
                  t \sim [\gamma]
                                                            coercion application
                  t:\tau
                                                            type annotation
                  t \triangleright \gamma
                                                            coercion
                                                  S
                                                            parenthesis
                  (t)
v
                                                        value
                  \lambda(x:\tau) \Rightarrow t
                                                            abstraction
                                                       kind
\kappa
         ::=
                                                           \operatorname{star}
                                                           kind arrow
                  \kappa_1 \to \kappa_2
                                                  S
                                                           parenthesis
                                                        type
                                                            type variable
                  T
                                                            type
                                                            arrow
                 \{\tau_1 \sim \tau_2\} \to \tau_3\lambda(\alpha : \kappa), \tau
                                                            coercion arrow
                                                            operator abstraction
                  \forall (\alpha : \kappa), \tau
                                                            forall
                                                            operator application
                  \tau_1 \tau_2
                                                  S
                                                            parenthesis
                  (\tau)
                                                        coercion proof term
                                                            variable
                  \operatorname{\mathbf{refl}} 	au
                                                            reflexivity
                                                            symmetry
                  \operatorname{\mathbf{sym}} \gamma
                                                            composition
                  \gamma_1 \circ \gamma_2
                  \gamma_1 \rightarrow \gamma_2
                                                            arrow introduction
                  \{\tau_1 \sim \tau_2\} \to \gamma
                                                            coercion arrow introduction
                  \lambda(\alpha:\kappa),\gamma
                                                            operator abstraction introduction
                  \forall (\alpha : \kappa), \gamma
                                                            forall introduction
                                                            application introduction
                  \gamma_1 \gamma_2
                                                            left elimination
                  left \gamma
                                                            right elimination
                  \mathbf{right}\,\gamma
                                                  S
                  (\gamma)
                                                            parenthesis
Γ
                                                        typing environment
                                                            empty
```

variable

 $\Gamma, x : \tau$

$[\alpha \mapsto \tau_1]\tau_2 \rhd \tau_3$ Type substitution

$\Gamma \vdash t : \tau$ Typing rules

$$\frac{x:\tau\in\Gamma}{\Gamma\vdash x:\tau}\quad\text{T-VAR}$$

$$\frac{\Gamma,x:\tau_1\vdash t:\tau_2}{\Gamma\vdash\tau_1:*}$$

$$\frac{\Gamma\vdash\lambda(x:\tau_1)\Rightarrow t:\tau_1\to\tau_2}{\Gamma\vdash\lambda(x:\tau_1)\Rightarrow t:\tau_1\to\tau_2}\quad\text{T-Abs}$$

$$\frac{\Gamma,\alpha:\kappa\vdash t:\tau}{\alpha\notin\Gamma}$$

$$\frac{\alpha\notin\Gamma}{\Gamma\vdash\lambda\{\alpha:\kappa\}\Rightarrow t:\forall(\alpha:\kappa),\tau}\quad\text{T-TYAbs}$$

$$\frac{\Gamma,c:\tau_1\sim\tau_2\vdash t:\tau_3}{\Gamma\vdash\lambda\{c:\tau_1\sim\tau_2\}\Rightarrow t:\{\tau_1\sim\tau_2\}\to\tau_3}\quad\text{T-CAbs}$$

$$\frac{\Gamma\vdash t_1:\tau_2\to\tau_1}{\tau_2\equiv\tau_2'}$$

$$\frac{\Gamma\vdash t_2:\tau_2'}{\Gamma\vdash t_1\;t_2:\tau_1}\quad\text{T-App}$$

 $\Gamma \vdash \gamma : \tau_1 \sim \tau_2$ Coercion typing

$$\begin{array}{ll} \frac{c:\tau_1 \sim \tau_2 \in \Gamma}{\Gamma \vdash c:\tau_1 \sim \tau_2} & \text{C-VAR} \\ \\ \overline{\Gamma \vdash \mathbf{refl} \, \tau:\tau \sim \tau} & \text{C-Refl} \\ \\ \frac{\Gamma \vdash \gamma:\tau_2 \sim \tau_1}{\Gamma \vdash \mathbf{sym} \, \gamma:\tau_1 \sim \tau_2} & \text{C-Sym} \end{array}$$

 $|\Gamma \vdash \tau : \kappa|$ Kinding

$$\frac{\alpha:\kappa\in\Gamma}{\Gamma\vdash\alpha:\kappa}\quad \text{K_-VAR}$$

$$\frac{T:\kappa\in\Gamma}{\Gamma\vdash T:\kappa}\quad \text{K_-AbsType}$$

$$\frac{\Gamma,\alpha:\kappa_1\vdash\tau:\kappa_2}{\Gamma\vdash\lambda(\alpha:\kappa_1),\tau:\kappa_1\to\kappa_2}\quad \text{K_-Abs}$$

$$\frac{\Gamma\vdash\tau_1:\kappa_2\to\kappa_1}{\Gamma\vdash\tau_2:\kappa_2}\quad \text{K_-App}$$

$$\frac{\Gamma\vdash\tau_1:\kappa}{\Gamma\vdash\tau_1:\kappa}\quad \text{K_-App}$$

$$\frac{\Gamma\vdash\tau_1:\kappa}{\Gamma\vdash\tau_1:\kappa}\quad \text{K_-Arrow}$$

$$\frac{\Gamma\vdash\tau_1:\kappa}{\Gamma\vdash\tau_1:\kappa}\quad \text{K_-Arrow}$$

$$\frac{\Gamma\vdash\tau_1:\kappa}{\Gamma\vdash\tau_2:\kappa}\quad \text{K_-Arrow}$$

$$\frac{\Gamma\vdash\tau_1:\kappa}{\Gamma\vdash\tau_2:\kappa}\quad \text{K_-CArrow}$$

$$\frac{\Gamma\vdash\tau_1:\kappa}{\Gamma\vdash\tau_2:\kappa}\quad \text{K_-CArrow}$$

$$\frac{\Gamma,\alpha:\kappa\vdash\tau:*}{\Gamma\vdash\forall(\alpha:\kappa),\tau:*}\quad \text{K_-Forall}$$

 $\tau_1 \equiv \tau_2$ Type equivalence

 $[x \mapsto v]t_1 \rhd t_2$ substitution

$$\frac{[x \mapsto v]x \triangleright v}{[x_1 \mapsto v]x_2 \triangleright x_2} \quad \text{SUBST_VAR2}$$

$$\frac{[x \mapsto v]\lambda(x : \tau) \Rightarrow t \triangleright \lambda(x : \tau) \Rightarrow t}{[x_1 \mapsto v]\lambda(x : \tau) \Rightarrow t} \quad \text{SUBST_ABS1}$$

$$\frac{[x_1 \mapsto v]t_1 \triangleright t_2}{[x_1 \mapsto v]\lambda(x_2 : \tau) \Rightarrow t_1 \triangleright \lambda(x_2 : \tau) \Rightarrow t_2} \quad \text{SUBST_ABS2}$$

$$\frac{[x \mapsto v]t_1 \triangleright t_2}{[x \mapsto v]\lambda\{\alpha : \kappa\} \Rightarrow t_1 \triangleright \lambda\{\alpha : \kappa\} \Rightarrow t_2} \quad \text{SUBST_TABS}$$

$$\frac{[x \mapsto v]t_1 \triangleright t_2}{[x \mapsto v]\lambda\{c : \tau_1 \sim \tau_2\} \Rightarrow t_2} \quad \text{SUBST_CABS}$$

$$\frac{[x \mapsto v]t_1 \triangleright t_2'}{[x \mapsto v]t_2 \triangleright t_2'} \quad \text{SUBST_CABS}$$

$$\frac{[x \mapsto v]t_1 \rhd t_2}{[x \mapsto v]t_1 \ [\tau] \rhd t_2 \ [\tau]} \quad \text{Subst_TApp}$$

$$\frac{[x \mapsto v]t_1 \rhd t_2}{[x \mapsto v]t_1 \sim [\gamma] \rhd t_2 \sim [\gamma]} \quad \text{Subst_CApp}$$

$$\frac{[x \mapsto v]t_1 \rhd t_2}{[x \mapsto v]t_1 : \tau \rhd t_2 : \tau} \quad \text{Subst_Annot}$$

$$\frac{[x \mapsto v]t_1 \rhd t_2}{[x \mapsto v]t_1 \rhd t_2} \quad \text{Subst_Coerce}$$

$$\frac{[x \mapsto v]t_1 \rhd t_2}{[x \mapsto v]t_1 \blacktriangleright \gamma \rhd t_2 \blacktriangleright \gamma} \quad \text{Subst_Coerce}$$

$t_1 \longrightarrow t_2$ Evaluation

$$\frac{t_2 \longrightarrow t_2'}{t_1 t_2 \longrightarrow t_1 t_2'} \quad \text{E_APP1}$$

$$\frac{t_1 \longrightarrow t_1'}{t_1 v \longrightarrow t_1' v} \quad \text{E_APP2}$$

$$[x \mapsto v]t \rhd t'$$

$$\frac{t' \longrightarrow t''}{(\lambda(x : \tau) \Rightarrow t) v \longrightarrow t''} \quad \text{E_APPABS}$$

$$\frac{t \longrightarrow t'}{\lambda\{\alpha : \kappa\} \Rightarrow t \longrightarrow t'} \quad \text{E_TABS}$$

$$\frac{t \longrightarrow t'}{\lambda\{c : \tau_1 \sim \tau_2\} \Rightarrow t \longrightarrow t'} \quad \text{E_CABS}$$

$$\frac{t \longrightarrow t'}{t \ [\tau] \longrightarrow t'} \quad \text{E_TAPP}$$

$$\frac{t \longrightarrow t'}{t \sim [\gamma] \longrightarrow t'} \quad \text{E_CAPP}$$

$$\frac{t \longrightarrow t'}{t : \tau \longrightarrow t'} \quad \text{E_ANNOT}$$

$$\frac{t \longrightarrow t'}{t : \tau \longrightarrow t'} \quad \text{E_ANNOT}$$

$$\frac{t \longrightarrow t'}{t \longrightarrow \tau} \quad \text{E_COERCE}$$

Definition rules: 60 good 0 bad Definition rule clauses: 135 good 0 bad