```
term variable
\boldsymbol{x}
      type variable
\alpha
T
      type
      coercion variable
c
t
                                                        term
                                                            variable
                  \lambda(x:\tau) \Rightarrow t
                                                            abstraction
                  \lambda\{\alpha:\kappa\}\Rightarrow t
                                                            type abstraction
                  \lambda \{c: \tau_1 \sim \tau_2\} \Rightarrow t
                                                            coercion abstraction
                                                            application
                  t [\tau]
                                                            type application
                  t \sim [\gamma]
                                                            coercion application
                  t:\tau
                                                            type annotation
                  t \triangleright \gamma
                                                            coercion
                                                  S
                                                            parenthesis
                  (t)
v
                                                        value
                  \lambda(x:\tau) \Rightarrow t
                                                            abstraction
                                                        kind
\kappa
         ::=
                                                            \operatorname{star}
                                                            kind arrow
                  \kappa_1 \to \kappa_2
                                                  S
                                                            parenthesis
                                                        type
                                                            type variable
                  T
                                                            type
                                                            arrow
                 \{\tau_1 \sim \tau_2\} \leadsto \tau_3\lambda(\alpha : \kappa), \tau
                                                            coercion arrow
                                                            operator abstraction
                  \forall (\alpha : \kappa), \tau
                                                            forall
                                                            operator application
                  \tau_1 \tau_2
                                                  S
                                                            parenthesis
                  (\tau)
                                                        coercion proof term
                                                            variable
                  \operatorname{\mathbf{refl}} 	au
                                                            reflexivity
                                                            symmetry
                  \operatorname{\mathbf{sym}} \gamma
                                                            composition
                  \gamma_1 \circ \gamma_2
                  \gamma_1 \rightarrow \gamma_2
                                                            arrow introduction
                  \{\tau_1 \sim \tau_2\} \leadsto \gamma
                                                            coercion arrow introduction
                  \lambda(\alpha:\kappa),\gamma
                                                            operator abstraction introduction
                  \forall (\alpha : \kappa), \gamma
                                                            forall introduction
                                                            application introduction
                  \gamma_1 \gamma_2
                                                            left elimination
                  left \gamma
                                                            right elimination
                  \mathbf{right}\,\gamma
                                                  S
                  (\gamma)
                                                            parenthesis
Γ
                                                        typing environment
                                                            empty
```

variable

 $\Gamma, x : \tau$ 

 $| \Gamma, T : \kappa$  abstract type  $| \Gamma, \alpha : \kappa$  type variable  $| \Gamma, c : c_1 \sim c_2$  coercion variable

## $[\alpha \mapsto \tau_1]\tau_2 \rhd \tau_3$ Type substitution

## $|\Gamma \vdash t : \tau|$ Typing rules

$$\frac{x:\tau\in\Gamma}{\Gamma\vdash x:\tau}\quad \text{T_-VAR}$$

$$\frac{\Gamma,x:\tau_1\vdash t:\tau_2}{\Gamma\vdash\tau_1:*}$$

$$\frac{\Gamma\vdash \lambda(x:\tau_1)\Rightarrow t:\tau_1\to\tau_2}{\Gamma\vdash \lambda(x:\tau_1)\Rightarrow t:\tau_1\to\tau_2}\quad \text{T_-Abs}$$

$$\frac{\Gamma\vdash t_1:\tau_2\to\tau_1}{\Gamma\vdash t_1:t_2:\tau_1}\quad \text{T_-APP}$$

$$\frac{\Gamma,\alpha:\kappa\vdash t:\tau}{\alpha\notin\Gamma}$$

$$\frac{\alpha\notin\Gamma}{\Gamma\vdash\lambda\{\alpha:\kappa\}\Rightarrow t:\forall(\alpha:\kappa),\tau}\quad \text{T_-TYAbs}$$

$$\frac{\Gamma\vdash t:\forall(\alpha:\kappa),\tau_2}{\Gamma\vdash\tau_1:\kappa}$$

$$\frac{[\alpha\mapsto\tau_1]\tau_2\rhd\tau_2'}{\Gamma\vdash t:\tau_2}\quad \text{T_-TYAPP}$$

$$\frac{\Gamma\vdash t:\tau_2}{\Gamma\vdash t:\tau_2}$$

$$\frac{\tau_1\equiv\tau_2}{\Gamma\vdash (t:\tau_1):\tau_1}\quad \text{T_-Annot}$$

## $\Gamma \vdash \tau : \kappa$ Kinding

$$\frac{\alpha:\kappa\in\Gamma}{\Gamma\vdash\alpha:\kappa}\quad \text{K_-VAR}$$
 
$$\frac{T:\kappa\in\Gamma}{\Gamma\vdash T:\kappa}\quad \text{K_-ABSTYPE}$$
 
$$\frac{\Gamma,\alpha:\kappa_1\vdash\tau:\kappa_2}{\Gamma\vdash\lambda(\alpha:\kappa_1),\tau:\kappa_1\to\kappa_2}\quad \text{K_-ABS}$$
 
$$\frac{\Gamma\vdash\tau_1:\kappa_2\to\kappa_1}{\Gamma\vdash\tau_2:\kappa_2}\quad \text{K_-APP}$$
 
$$\frac{\Gamma\vdash\tau_1:*}{\Gamma\vdash\tau_1:*}\quad \text{K_-APP}$$
 
$$\frac{\Gamma\vdash\tau_1:*}{\Gamma\vdash\tau_1\to\tau_2:*}\quad \text{K_-ARROW}$$
 
$$\frac{\Gamma,\alpha:\kappa\vdash\tau:*}{\Gamma\vdash\tau_1\to\tau_2:*}\quad \text{K_-FORALL}$$

## $\tau_1 \equiv \tau_2$ Type equivalence

 $[x \mapsto v]t_1 \rhd t_2$  substitution

$$\overline{[x \mapsto v]x \triangleright v}$$
 Subst\_Var1

 $|t_1 \longrightarrow t_2|$  Evaluation

$$\frac{t_2 \longrightarrow t_2'}{t_1 t_2 \longrightarrow t_1 t_2'} \quad \text{E-APP1}$$

$$\frac{t_1 \longrightarrow t_1'}{t_1 v \longrightarrow t_1' v} \quad \text{E-APP2}$$

$$[x \mapsto v]t \rhd t'$$

$$\frac{t' \longrightarrow t''}{(\lambda(x : \tau) \Rightarrow t) v \longrightarrow t''} \quad \text{E-APPABS}$$

$$\frac{t \longrightarrow t'}{\lambda\{\alpha : \kappa\} \Rightarrow t \longrightarrow t'} \quad \text{E-TABS}$$

$$\frac{t \longrightarrow t'}{\lambda\{c : \tau_1 \sim \tau_2\} \Rightarrow t \longrightarrow t'} \quad \text{E-CABS}$$

$$\frac{t \longrightarrow t'}{t \ [\tau] \longrightarrow t'} \quad \text{E-TAPP}$$

$$\frac{t \longrightarrow t'}{t \sim [\gamma] \longrightarrow t'} \quad \text{E-CAPP}$$

$$\frac{t \longrightarrow t'}{t : \tau \longrightarrow t'} \quad \text{E-ANNOT}$$

$$\frac{t \longrightarrow t'}{t \longrightarrow t'} \quad \text{E-COERCE}$$

Definition rules: 51 good 0 bad Definition rule clauses: 106 good 0 bad