

## homework\_problem\_set\_2

JP

9/1/2021

$$s_x^2 = \frac{\Sigma(X - \bar{X})^2}{N - 1}$$

$$s_x = \sqrt{\frac{\Sigma(X - \bar{X})^2}{N - 1}}$$

```
# get the sum
4.377026 + 8.628671 + 6.403844 + 10.191558 + 4.452261 + 7.848496 + 12.25767 + 7.950580 + 9.182271 + 0.7
```

```
## [1] 71.99798
```

```
# sum is 71.99798
```

```
# get the mean
71.99798/10
```

```
## [1] 7.199798
```

```
# mean is 7.199798
```

```
# get the deviates
4.377026 - 7.199798 # -2.822772
```

```
## [1] -2.822772
```

```
8.628671 - 7.199798 # 1.428873
```

```
## [1] 1.428873
```

```
6.403844 - 7.199798 # -0.795954
```

```
## [1] -0.795954
```

```
10.191558 - 7.199798 # 2.99176
```

```
## [1] 2.99176
```

```
4.452261 - 7.199798 # -2.747537
```

```
## [1] -2.747537
```

```
7.848496 - 7.199798 # 0.648698
```

```
## [1] 0.648698
```

```
12.25767 - 7.199798 # 5.057872
```

```
## [1] 5.057872
```

```
7.950580 - 7.199798 # 0.750782
```

```
## [1] 0.750782
```

```
9.182271 - 7.199798 # 1.982473
```

```
## [1] 1.982473
```

```
0.705607 - 7.199798 # -6.494191
```

```
## [1] -6.494191
```

```
# square the deviates  
(-2.822772)^2
```

```
## [1] 7.968042
```

```
(1.428873)^2
```

```
## [1] 2.041678
```

```
(-0.795954)^2
```

```
## [1] 0.6335428
```

```
(2.99176)^2
```

```
## [1] 8.950628
```

```
(-2.747537)^2
```

```
## [1] 7.54896
```

```
(0.648698)^2
```

```
## [1] 0.4208091
```

```
(5.057872)^2
```

```
## [1] 25.58207
```

```
(0.750782)^2
```

```
## [1] 0.5636736
```

```
(1.982473)^2
```

```
## [1] 3.930199
```

```
(-6.494191)^2
```

```
## [1] 42.17452
```

```
# get the sum of the squared deviates
```

```
7.968042 + 2.041678 + 0.6335428 + 8.950628 + 7.54896 + 0.4208091 + 25.58207 + 0.5636736 + 3.930199 + 42.17452
```

```
## [1] 99.81412
```

```
# numerator is 99.81412
```

```
# denominator is 10 - 1
```

```
10-1
```

```
## [1] 9
```

```
# denominator is 9
```

```
# get the variance
```

```
99.81412/9
```

```
## [1] 11.09046
```

```
# variance is 11.09046
```

```
# standard deviation is the variance squared
```

```
sqrt(11.09046)
```

```
## [1] 3.330234
```

```
# sd is 3.330234
```

```
# double check our work
```

```
sd(numbers)
```

```
## [1] 3.330235
```

```
# pretty close
```

$$s_x^2 = \frac{\sum X^2 - \frac{(\sum X)^2}{N}}{N - 1}$$

$$s_x = \sqrt{\frac{\sum X^2 - \frac{(\sum X)^2}{N}}{N - 1}}$$

```
numbers
```

```
## [1] 4.377026 8.628671 6.403844 10.191558 4.452261 7.848496 12.257677
```

```
## [8] 7.950580 9.182271 0.705607
```

```
4.377026 + 8.628671 + 6.403844 + 10.191558 + 4.452261 + 7.848496 + 12.25767 + 7.950580 + 9.182271 + 0.705607
```

```
## [1] 71.99798
```

```
# sum is 71.99798
```

```
71.99798^2
```

```
## [1] 5183.709
```

```
# squared sum of x is 5183.709
```

```
5183.709/10
```

```
## [1] 518.3709
```

```
# 518.3709 is the value after dividing by N
```

```
4.377026^2 + 8.628671^2 + 6.403844^2 + 10.191558^2 + 4.452261^2 + 7.848496^2 + 12.25767^2 + 7.950580^2 + 9.182271^2 + 0.705607^2
```

```
## [1] 618.1851
```

```
# sum of squared Xs is 618.1851
```

```
618.1851 - 518.3709
```

```
## [1] 99.8142
```

```
# numerator is 99.8142
```

```
# denominator is  $N - 1$   
10-1
```

```
## [1] 9
```

```
99.8142/9
```

```
## [1] 11.09047
```

```
# variance is 11.09047
```

```
sqrt(11.09047)
```

```
## [1] 3.330236
```

```
# sd is 3.330236
```

```
sd(numbers)
```

```
## [1] 3.330235
```

## Range

```
data_example <- tibble(Maximum = c(81, 41, 80, 71, 100, 4, 39, 71, 60, 38),  
                        Minimum = c(50, 2, 34, 10, 9, 0, 12, 5, 50, 3))
```

```
data_example
```

```
## # A tibble: 10 x 2  
##   Maximum Minimum  
##   <dbl>   <dbl>  
## 1     81     50  
## 2     41      2  
## 3     80     34  
## 4     71     10  
## 5    100      9  
## 6      4      0  
## 7     39     12  
## 8     71      5  
## 9     60     50  
## 10    38      3
```

## z-Score

$$z = \frac{X - \bar{X}}{S_X}$$

```
get_z <- tibble(single_obs = c(8, 10, 23, 23, 30, 53, 40, 57, 27, 8),
                 mean = c(10, 15, 17, 24, 34, 45, 36, 50, 41, 4),
                 sd = c(2.1, 3.1, 1.4, 3, 1.2, .2, .9, .47, .16, .67))

get_z
```

```
## # A tibble: 10 x 3
##   single_obs mean    sd
##   <dbl> <dbl> <dbl>
## 1      8    10  2.1
## 2     10    15  3.1
## 3     23    17  1.4
## 4     23    24  3
## 5     30    34  1.2
## 6     53    45  0.2
## 7     40    36  0.9
## 8     57    50  0.47
## 9     27    41  0.16
## 10     8     4  0.67
```

## Raw Score From z-Score

$$X = (z)(S_X) + \bar{X}$$

```
get_raw <- tibble(z = c(1, 2, 3, -3, -2, -1, 1.4, 1.6, -2.4, -3),
                  mean = c(10, 15, 17, 24, 34, 45, 36, 50, 41, 4),
                  sd = c(2.1, 3.1, 1.4, 3, 1.2, .2, .9, .47, .16, .67))

get_raw
```

```
## # A tibble: 10 x 3
##       z mean    sd
##   <dbl> <dbl> <dbl>
## 1  1     10  2.1
## 2  2     15  3.1
## 3  3     17  1.4
## 4 -3     24  3
## 5 -2     34  1.2
## 6 -1     45  0.2
## 7  1.4    36  0.9
## 8  1.6    50  0.47
## 9 -2.4    41  0.16
## 10 -3     4  0.67
```

## Standard Error of the Mean

$$\sigma_{\bar{X}} = \frac{\sigma_X}{\sqrt{N}}$$

```
get_sample_distribution <- tibble(ind_mean = c(10, 15, 17, 24, 34, 45, 36, 50, 41, 4),
  mu = c(12, 16, 14, 22, 30, 40, 32, 54, 43, 8),
  sigma_x = c(3, 2, 4, 1.4, .2, .6, .7, .1, 2.4, 2.9), #this is not sig
  N = c(10, 12, 14, 16, 20, 24, 11, 8, 15, 10))

get_sample_distribution
```

```
## # A tibble: 10 x 4
##   ind_mean    mu sigma_x     N
##   <dbl> <dbl>   <dbl> <dbl>
## 1      10     12      3      10
## 2      15     16      2      12
## 3      17     14      4      14
## 4      24     22     1.4     16
## 5      34     30     0.2     20
## 6      45     40     0.6     24
## 7      36     32     0.7     11
## 8      50     54     0.1      8
## 9      41     43     2.4     15
## 10      4      8     2.9     10
```

$$z = \frac{\bar{X} - \mu}{\sigma_{\bar{X}}}$$

```
get_sample_distribution
```

```
## # A tibble: 10 x 4
##   ind_mean    mu sigma_x     N
##   <dbl> <dbl>   <dbl> <dbl>
## 1      10     12      3      10
## 2      15     16      2      12
## 3      17     14      4      14
## 4      24     22     1.4     16
## 5      34     30     0.2     20
## 6      45     40     0.6     24
## 7      36     32     0.7     11
## 8      50     54     0.1      8
## 9      41     43     2.4     15
## 10      4      8     2.9     10
```

## Let's Try Variance & SD Together Now

```
set.seed(090221)
```

```
numbers = rnorm(n = 10, mean = 4.14, sd = 1.11)
```

```
N = 10
```

```
numbers
```

```
## [1] 5.060850 3.865486 3.521444 3.571518 4.629313 4.115526 4.492806 4.364263
```

```
## [9] 5.067677 2.977059
```