Problem Set 1

JP

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```
set.seed(082421)
# creating 5 different categories, with different amounts of time they show up in the data
categories = rep(letters[1:5], times = c(5, 4, 6, 8, 7))

# 30 observations with the mean and standard deviation
test_scores = rnorm(n = 30, mean = 7.14, sd = 2.16)

# Making the categories act like categories rather than numerical values
categories = as.factor(categories)

# Observations (be careful R is case sensitive)
N = 30
```

I will do this two ways

Using the numerical values and then using the objects approach

Frequencies

```
# get the frequencies of all the categories
table(categories)

## categories
## a b c d e
## 5 4 6 8 7

# Frequency & Percentage of A
5/30

## [1] 0.1666667

(5/30)*100
## [1] 16.66667
```

```
# Frequency & Percentage of B
4/30
## [1] 0.1333333
(4/30)*100
## [1] 13.33333
# Frequency & Percentage of C
## [1] 0.2
(6/30)*100
## [1] 20
# Frequency & Percentage of D
## [1] 0.2666667
(8/30) *100
## [1] 26.66667
\# Frequency \ensuremath{\mathfrak{G}} Percentage of \ensuremath{E}
7/30
## [1] 0.2333333
(7/30) *100
## [1] 23.33333
\textit{\# cumulative frequencies of categories A \& B}
(5/30) + (4/30)
## [1] 0.3
# another option is to do the calculations above and then just add up the frequency of A with the frequ
.167 + .133
```

[1] 0.3

```
# To get the cumlative percentage of all 5 categories
(5/30)*100 + (4/30)*100 + (6/30)*100 + (8/30)*100 + (7/30)*100
## [1] 100
# you can also use the calculations above to add up all the percentages
16.667 + 13.333 + 20 + 26.667 + 23.333
## [1] 100
Frequencies using objects
freq_a \leftarrow 5/N
freq_a
## [1] 0.1666667
# Percent of category A
percent_a <- freq_a*100</pre>
percent_a
## [1] 16.66667
freq_b <- 4/N
freq_b
## [1] 0.1333333
percent_b <- freq_b*100</pre>
percent_b
## [1] 13.33333
freq_c \leftarrow 6/N
freq_c
## [1] 0.2
percent_c <- freq_c*100</pre>
percent_c
## [1] 20
freq_d <- 8/N</pre>
freq_d
## [1] 0.2666667
```

```
percent_d \leftarrow freq_d*100
percent_d
## [1] 26.66667
freq_e <- 7/N
freq_e
## [1] 0.2333333
percent_e <- freq_e*100</pre>
percent_e
## [1] 23.33333
# cumulative frequency of A & B
freq_ab = freq_a + freq_b
freq_ab
## [1] 0.3
# To get the cumlative percentage of all 5 categories
total_percent = percent_a + percent_b + percent_c + percent_d + percent_e
total_percent
## [1] 100
# Just a way to combine all the percentages together to see in one place
cbind(percent_a, percent_b, percent_c, percent_d, percent_e)
        percent_a percent_b percent_c percent_d percent_e
## [1,] 16.66667 13.33333
                                   20 26.66667 23.33333
# find the mode
table(categories)
## categories
## a b c d e
## 5 4 6 8 7
# which value occurs most often
```

Getting the Median Two ways

```
sort(test_scores)
```

```
## [1] 1.979125 3.537262 3.566831 4.282318 4.396029 4.506466 4.977139
## [8] 5.668250 5.895740 6.085677 6.436928 6.440507 6.589584 6.821120
## [15] 7.060384 7.212301 7.288768 7.816361 7.868345 7.869582 8.239301
## [22] 8.691209 8.845786 8.924377 9.383258 9.407202 10.668180 10.949238
## [29] 12.055448 12.588050
#look for the middle value or in this case the 15th and 16th observations
# 7.060384 & 7.212301 and then divide by 2
(7.06 + 7.21)/2
## [1] 7.135
# find the median
sort(test_scores)
## [1] 1.979125 3.537262 3.566831 4.282318 4.396029 4.506466 4.977139
## [8] 5.668250 5.895740 6.085677 6.436928 6.440507 6.589584 6.821120
## [15] 7.060384 7.212301 7.288768 7.816361 7.868345 7.869582 8.239301
## [22] 8.691209 8.845786 8.924377 9.383258 9.407202 10.668180 10.949238
## [29] 12.055448 12.588050
sort(test_scores)[15:16]
## [1] 7.060384 7.212301
get_median = (7.06 + 7.21)/2
get_median
## [1] 7.135
median(test_scores)
## [1] 7.136343
```

Getting the Mean Two Ways

[1] 216.09

```
# look at test scores first in order for lowest to highest
sort(test_scores)

## [1] 1.979125 3.537262 3.566831 4.282318 4.396029 4.506466 4.977139

## [8] 5.668250 5.895740 6.085677 6.436928 6.440507 6.589584 6.821120

## [15] 7.060384 7.212301 7.288768 7.816361 7.868345 7.869582 8.239301

## [22] 8.691209 8.845786 8.924377 9.383258 9.407202 10.668180 10.949238

## [29] 12.055448 12.588050

# Now let's get the sum

1.98 + 3.54 + 3.57 + 4.28 + 4.40 + 4.51 + 4.98 + 5.67 + 5.90 + 6.09 + 6.44 + 6.44 + 6.59 + 6.82 + 7.06
```

```
# Now let's decide the sum of the scores by the number of observations
(1.98 + 3.54 + 3.57 + 4.28 + 4.40 + 4.51 + 4.98 + 5.67 + 5.90 + 6.09 + 6.44 + 6.44 + 6.59 + 6.82 + 7.06
## [1] 7.203
# 7.20 is the mean of our scores
# now getting the mean with objects
sort(test_scores)
## [1] 1.979125 3.537262 3.566831 4.282318 4.396029 4.506466 4.977139
## [8] 5.668250 5.895740 6.085677 6.436928 6.440507 6.589584 6.821120
## [15] 7.060384 7.212301 7.288768 7.816361 7.868345 7.869582 8.239301
## [22] 8.691209 8.845786 8.924377 9.383258 9.407202 10.668180 10.949238
## [29] 12.055448 12.588050
# look at how many observations we have
## [1] 30
# Now lets get the sum of the scores
sum_of_scores = sum(test_scores)
sum_of_scores
## [1] 216.0508
# get the mean
xbar = sum_of_scores/N
# could also look at it this way
xbar2 = sum_of_scores/30
xbar
## [1] 7.201692
xbar2
## [1] 7.201692
# we get the same mean
```

Now deviations

```
sort(test_scores)
```

```
## [1] 1.979125 3.537262 3.566831 4.282318 4.396029 4.506466 4.977139
## [8] 5.668250 5.895740 6.085677 6.436928 6.440507 6.589584 6.821120
## [15] 7.060384 7.212301 7.288768 7.816361 7.868345 7.869582 8.239301
## [22] 8.691209 8.845786 8.924377 9.383258 9.407202 10.668180 10.949238
## [29] 12.055448 12.588050
# look at how far students deviated from the average score by doing each one individually
1.98 - 7.20
## [1] -5.22
3.54 - 7.20
## [1] -3.66
3.57 - 7.20
## [1] -3.63
4.28 - 7.20
## [1] -2.92
4.40 - 7.20
## [1] -2.8
4.51 - 7.20
## [1] -2.69
4.98 - 7.20
## [1] -2.22
5.67 - 7.20
## [1] -1.53
5.90 - 7.20
## [1] -1.3
6.09 - 7.20
```

[1] -1.11

6.44 - 7.20## [1] -0.76 6.44 - 7.20## [1] -0.76 6.59 - 7.20## [1] -0.61 6.82 - 7.20 ## [1] -0.38 7.06 - 7.20 ## [1] -0.14 7.21 - 7.20 ## [1] 0.01 7.29 - 7.20## [1] 0.09 7.82 - 7.20 ## [1] 0.62 7.87 - 7.20 ## [1] 0.67 7.87 - 7.20## [1] 0.67 8.24 - 7.20 ## [1] 1.04 8.69 - 7.20 ## [1] 1.49

```
8.85 - 7.20
## [1] 1.65
8.92 - 7.20
## [1] 1.72
9.38 - 7.20
## [1] 2.18
9.41 - 7.20
## [1] 2.21
10.67 - 7.20
## [1] 3.47
10.95 - 7.20
## [1] 3.75
12.06 - 7.20
## [1] 4.86
12.59 - 7.20
## [1] 5.39
# now to get the sum of the deviations
(-5.22) + (-3.66) + (-3.63) + (-2.92) + (-2.8) + (-2.69) + (-2.22) + (-1.53) + (-1.3) + (-1.11) + (-.76)
## [1] 0.09
# remember to look at the test scores
sort(test_scores)
## [1] 1.979125 3.537262 3.566831 4.282318 4.396029 4.506466 4.977139
## [8] 5.668250 5.895740 6.085677 6.436928 6.440507 6.589584 6.821120
## [15] 7.060384 7.212301 7.288768 7.816361 7.868345 7.869582 8.239301
## [22] 8.691209 8.845786 8.924377 9.383258 9.407202 10.668180 10.949238
```

[29] 12.055448 12.588050

```
# lets remember what the mean was
xbar
## [1] 7.201692
# look at how far students deviated from the average score using the objects we created earlier
deviation = test_scores - xbar
deviation
## [1] -2.80566349 -3.66442975 -0.61210859 -0.76476402 -5.22256690 0.01060902
## [7] 5.38635782 0.61466928 -2.22455345 -0.76118503 -2.69522654 2.18156621
## [13] 1.48951665 0.66788945 2.20550951 1.03760910 -1.11601555 1.72268513
## [19] 1.64409340 3.74754569 -3.63486163 -0.38057177 4.85375559 0.08707613
## [25] 3.46648728 0.66665299 -0.14130830 -2.91937412 -1.30595174 -1.53344238
# look to see how far the worse test score was from the mean
sort(deviation)
## [1] -5.22256690 -3.66442975 -3.63486163 -2.91937412 -2.80566349 -2.69522654
## [7] -2.22455345 -1.53344238 -1.30595174 -1.11601555 -0.76476402 -0.76118503
## [13] -0.61210859 -0.38057177 -0.14130830 0.01060902 0.08707613 0.61466928
## [19] 0.66665299 0.66788945 1.03760910 1.48951665 1.64409340 1.72268513
## [25] 2.18156621 2.20550951 3.46648728 3.74754569 4.85375559 5.38635782
# getting the sum of the deviations
sum(deviation)
```

[1] 5.77316e-15