The Selective Disclosure of Evidence

An Experiment

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Motivation

In many settings, agents communicate by disclosing *selected* evidence:

- *Journalists* select which facts to report in their articles
- *Managers* select which results to discuss in performance reports
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A pervasive force in communication, e.g., a principal source of news media bias

("filtering," Gentzkow et al. '14)

This Paper

A comprehensive experimental study on **selective disclosure**

We build on a small theoretical literature that studies disclosure of noisy evidence

Milgrom ('81, Bell), Fishman and Hagerty ('90, QJE), Di Tillio et al ('21, Ecma)

Our model generates rich comparative statics in N and K, e.g.,

- Which evidence do senders disclose?
- How much information do they transmit to receivers?
- Do receivers account the selection in the evidence they see?

These comparative statics inform a novel experimental design, and provide a rigorous test of the theory

Outline

1. Model

2. Equilibrium and Testable Predictions

3. Experimental Design

4. Results

model

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from Milgrom (1981)

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Receiver observes the message and takes an action $a \in A$

Payoffs

Given state θ and action a,

- Receiver's payoff is $u(\theta, a) = -(a - \theta)^2$ wants to guess the state
- Sender's payoff is $v(\theta, a) = a$ higher actions preferred

Discussion

Sender does not choose N, i.e., available evidence is **exogenous**

If $K = N$, the sender can disclose **all** her available evidence if so she wants

If $K < N$, sender can cherry pick which evidence to disclose

– $K < N$ captures exogenous communication constraints

Changes in K and N generate rich testable predictions, which we use as a test of the theory

equilibrium

Equilibrium

Our analysis focuses on pure-strategy **PBEs** (as in Okuno-Fujiwara et al., '90, *Restud*)

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We refine the equilibrium set using **neologism proofness**, Farrel ('93, *GEB*) adapted to our setting with verifiable information

Under this refinement, our game admits a **unique** equilibrium outcome

Equilibrium

More formally, we focus on a natural class of sender's strategies:

Definition

A sender's strategy is **maximally selective** if, given the available signals, she discloses the K-highest ones.

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Proposition 1

There exists a PBE in which the sender plays a maximally selective strategy

(Milgrom 1981)

Moreover, the outcome it induces is unique in the class of neologism-proof PBEs

Informativeness

Main outcome of interest is the **informativeness** the equilibrium strategies

- I.e., how effectively sender and receiver communicate

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We measure informativeness as the **correlation** btw θ and a, denoted by $\mathcal{I} = Corr(\theta, a)$ as in Lizzeri, Frechette, Perego ('22, Ecma)

Main Comparative Statics

Rich predictions regarding how informativeness changes in K and N

Proposition 2

Fixing N, Equilibrium informativeness increases in K

Fixing K, equilibrium informativeness can increase for small N but eventually decreases to zero as $N \to \infty$

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see also Fishman and Hagerty ('90, QJE),
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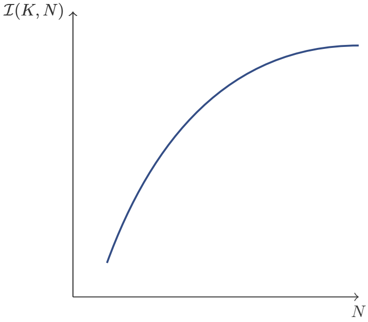

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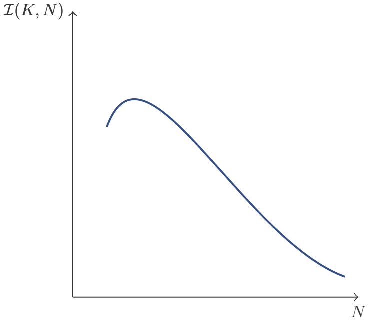


experiment

Experimental Design

Binary state: θ_L and θ_H, equal probability

Four possible signals $S = \{A, B, C, D\}$

Information structure f:

	Signal			
State	A	B	C	D
θ_L	10%	20%	25%	45%
θ_H	45%	25%	20%	10%

Receiver's action $a \in [0, 1]$, which makes it equivalent to a belief elicitation task

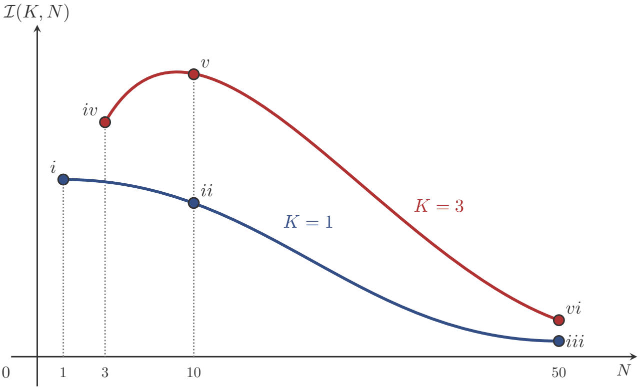
implemented using BSR (Hossain and Okui, '13 *Restud*) Details

Treatments

We vary K and N as follows:

	$N = 1$	$N = 3$	$N = 10$	$N = 50$
$K = 1$	✓	·	✓	✓
$K = 3$	·	✓	✓	✓

Main Comparative Statics



Experimental Details

- Undergrad population Columbia and NYU: Spring, Summer, Fall 2023
- 420 subjects, between-subject design
- 6 treatments
- 4 sessions per treatment
- 30 rounds per session, random rematching
- 17.5 subjects per sessions on average
- Average payout $30 per subject
- Fixed roles

User Interface: $N = 10$ and $K = 3$

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Round 7 of 30: Guessing Stage **You are the Receiver**

Reminder:

If the secret Urn is **Yellow**, this is the probability of each ball being drawn:

A	B	C	D
10 %	20 %	25 %	45 %

If the secret Urn is **Red**, this is the probability of each ball being drawn:

A	B	C	D
45 %	25 %	20 %	10 %

The Sender had 10 available balls and they could disclose 3 or less. This is the Sender's message:

A A B

Use the slider below to indicate your Guess of how likely it is that the secret Urn is Red.

Your Guess: 10

Submit

results

Outline

Progression of our analysis:

- Which evidence do senders disclose?
- How informative is it?
- How do receivers respond to it?

result 1

(which evidence is disclosed)

Which Evidence is Disclosed?

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  sender can be more selective with larger sample

- If K increases, evidence disclosed should become **less** favorable

  held to higher a standard, sender needs to be less selective

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To test this, we compute the **GPA** of each message ($A \rightsquigarrow 4$, $B \rightsquigarrow 3$, etc) and study how it changes in N and K

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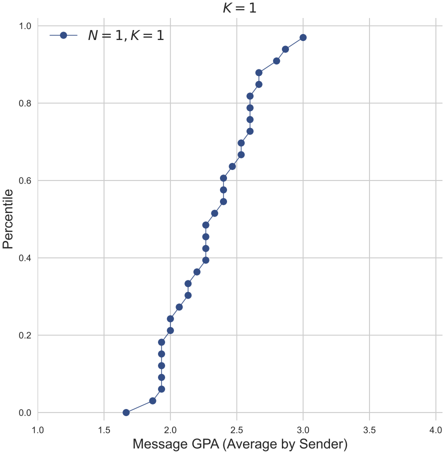

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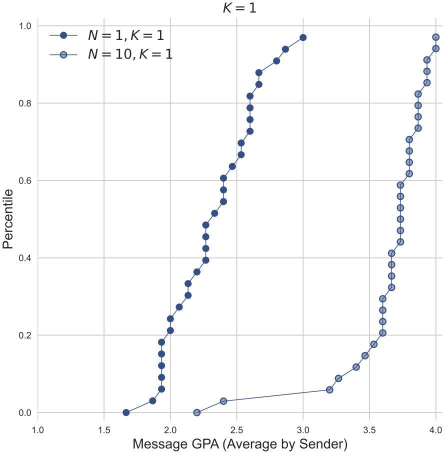

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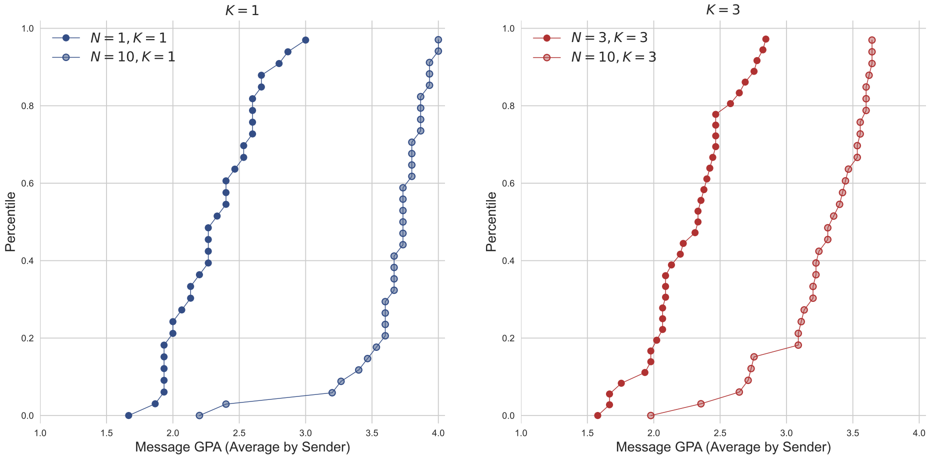

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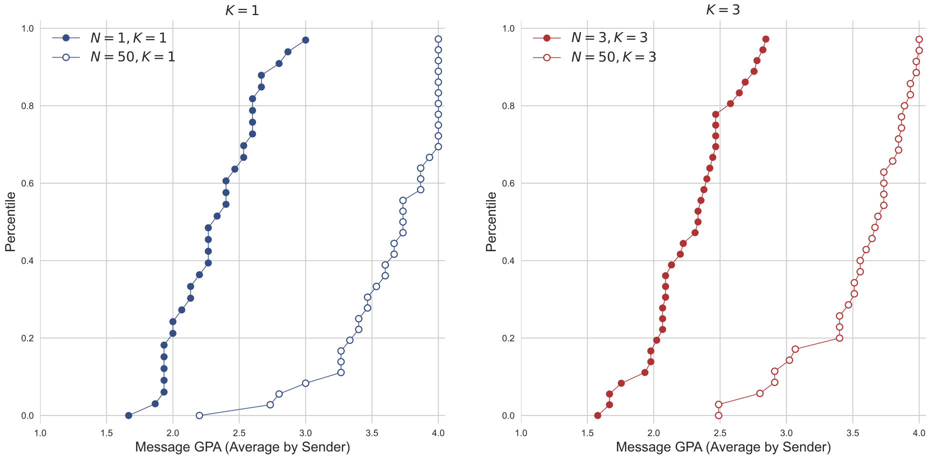

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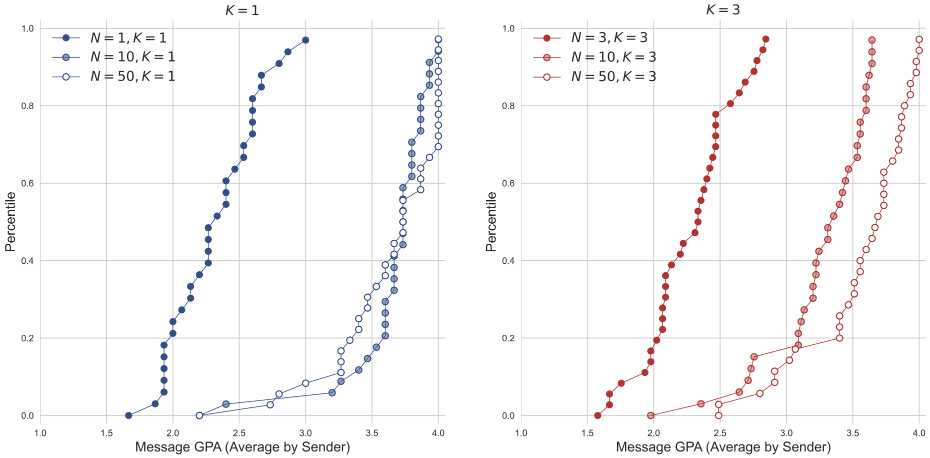

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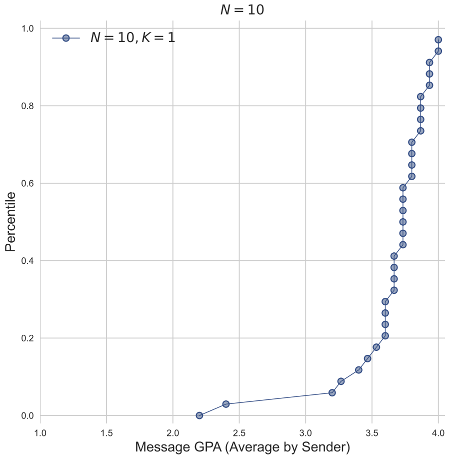

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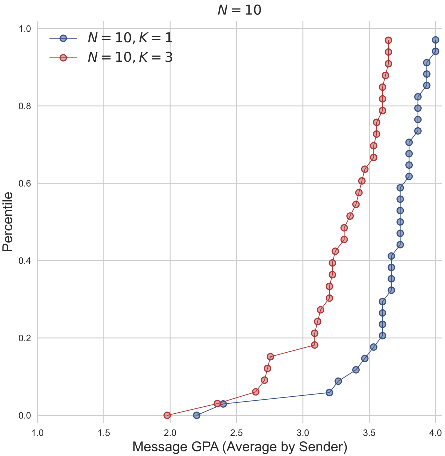

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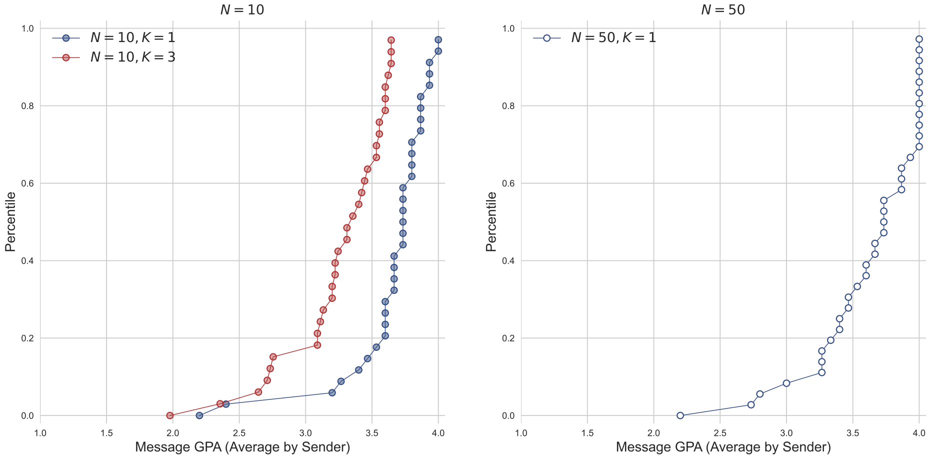

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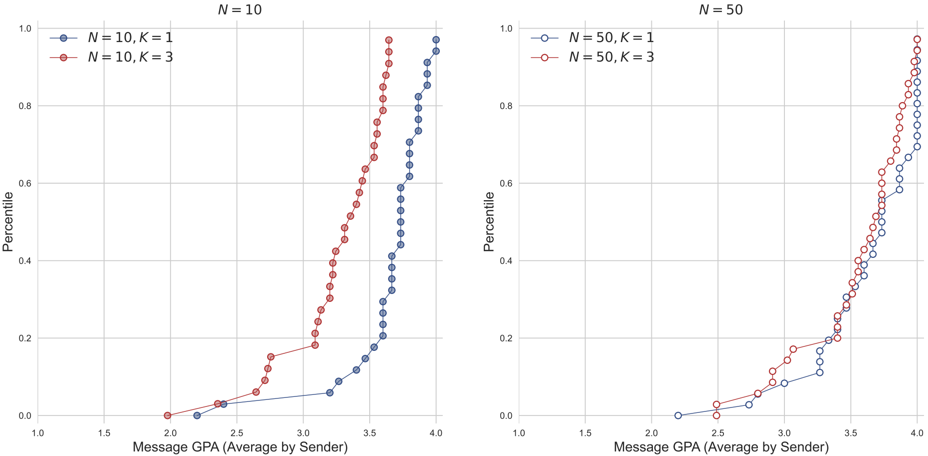

Which Evidence is Disclosed?

Robustness:

- Theoretical predictions Appendix
- Average treatment effects, statistical tests Appendix
- Raw data Appendix

Summary of Result 1

Result 1. Senders selectively disclose the available evidence in ways that are consistent with the key qualitative predictions of the theory

Theory is held to a high standard:

- FOSD rankings are a rather demanding test for the theory
- Contrasting signs reduce scope for alternative explanations

result 2

(informativeness)

How Much Information is Transmitted?

Previous result documents that senders engage in selective disclosure:

Question 2: What are the consequences of this selection on how much information is transmitted?

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We measure **informativeness** as the correlation between the state θ and the guess a induced by the sender' strategy

Appendix

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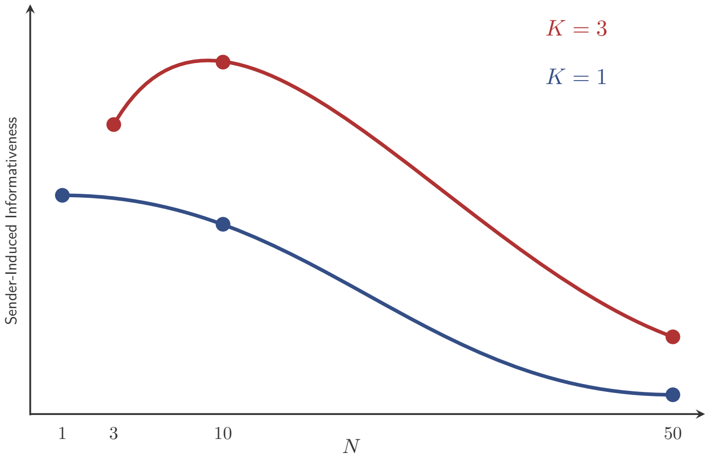

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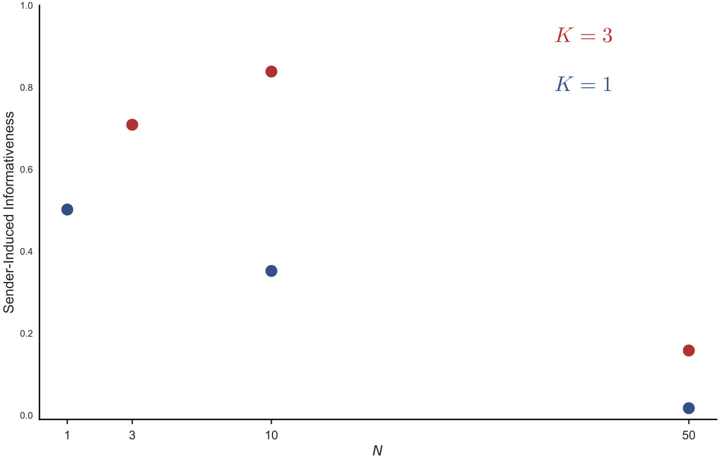

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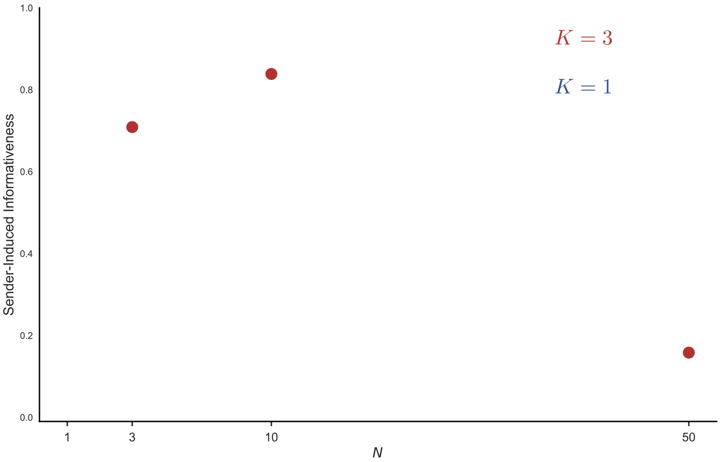

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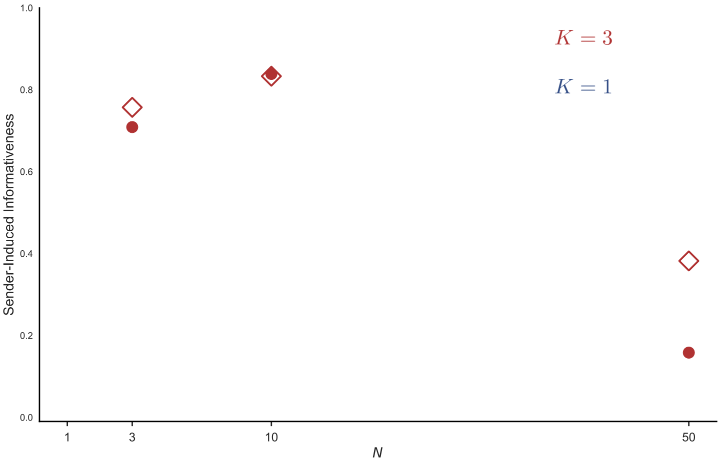

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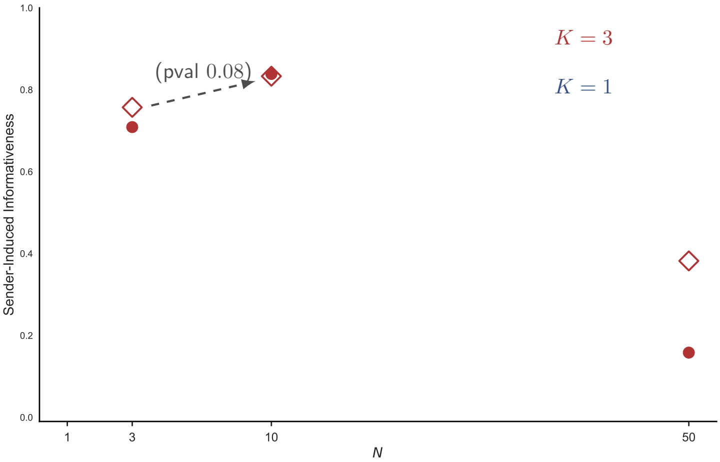

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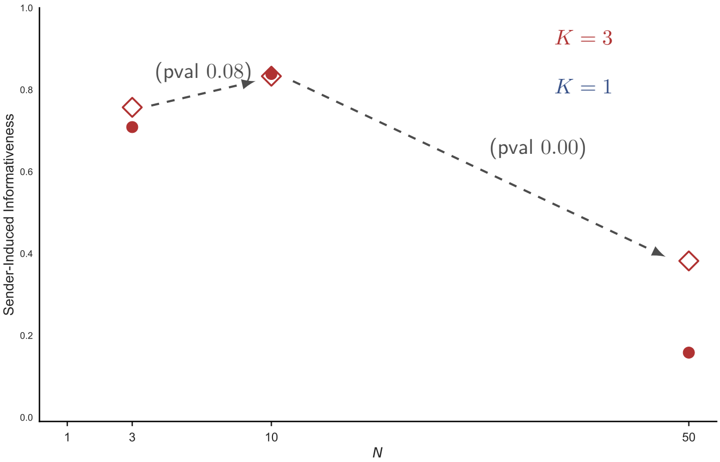

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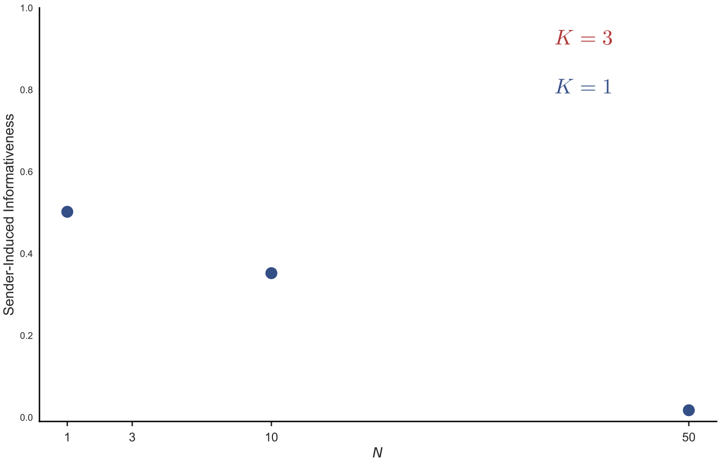

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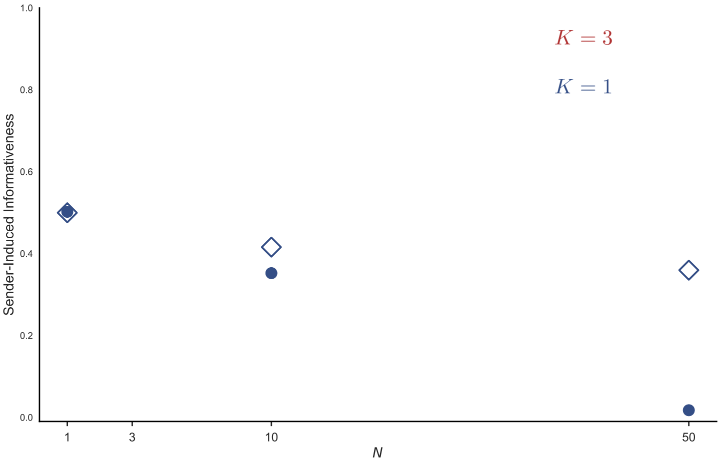

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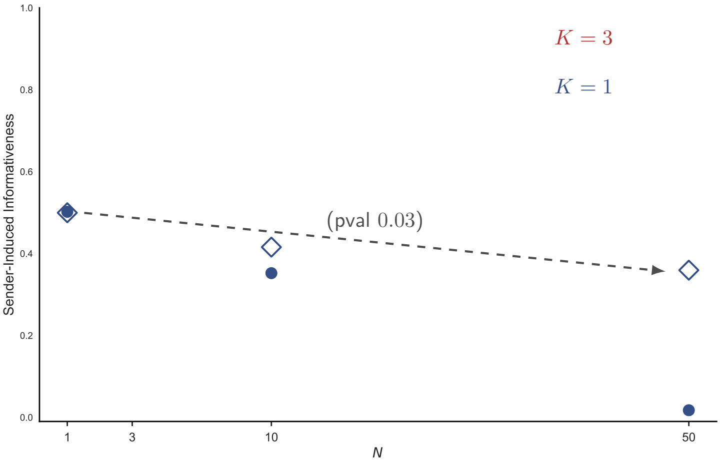

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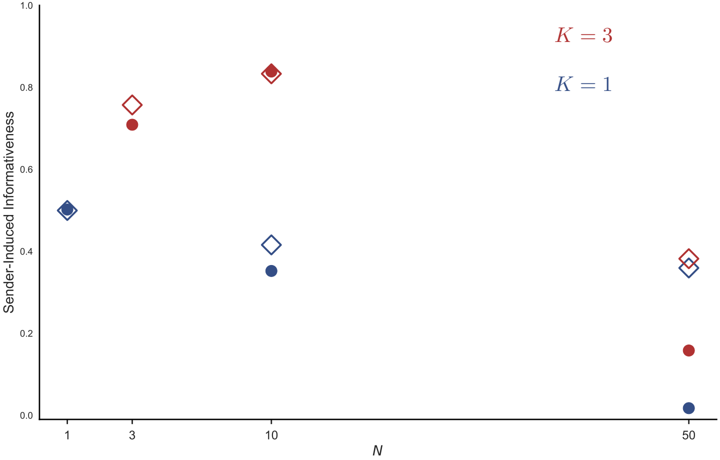

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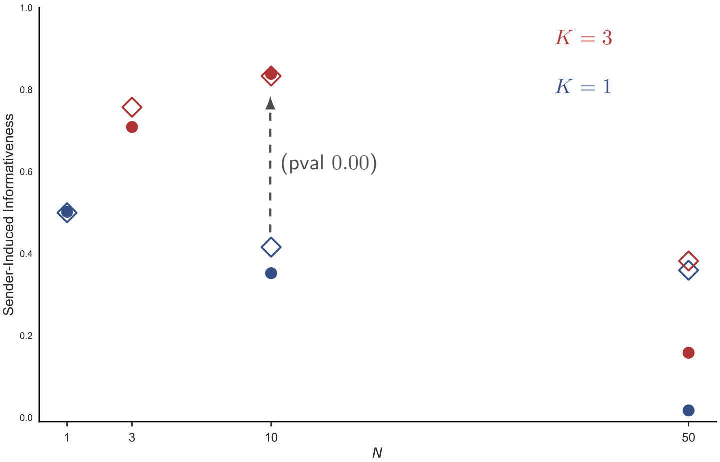

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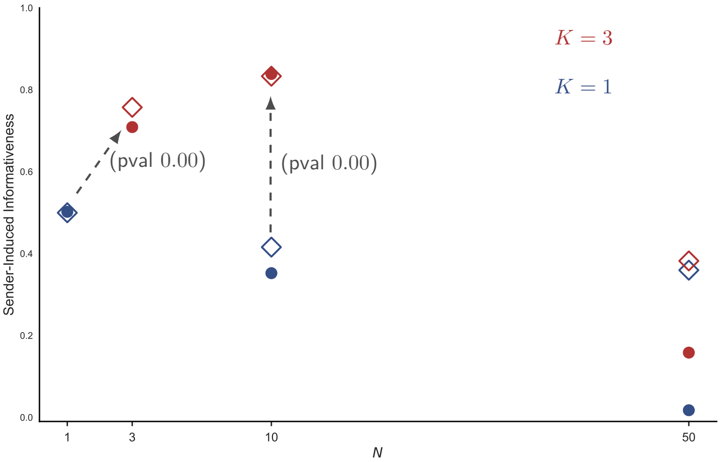

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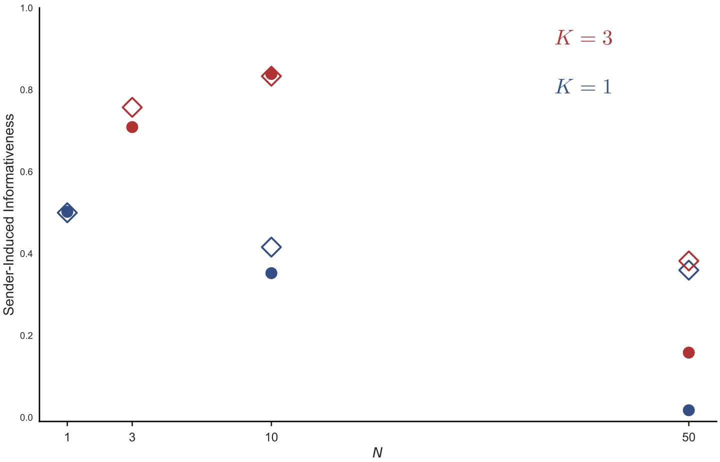

Summary of Result 2

Array of contrasting predictions sets high bar for the theory

Result 2. Informativeness changes in ways that is consistent with the key qualitative predictions of the theory

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Result 2. Informativeness changes in ways that is consistent with the key qualitative predictions of the theory

Overall, as a force in communication, selective disclosure seems behaviorally descriptive

Yet, our results also reveal substantial **quantitative** deviations

- Senders transmit (weakly) more information than it is predicted. That is, they **overcommunicate**

result 3

(overcommunication)

Explaining Overcommunication

This finding is at odds with existing experimental literature on disclosure

e.g., Forsythe, Isaac and Palfrey ('89, Rand), Jin and Leslie ('03, QJE), Jin, Luca, and Martin ('22, AEJ: Micro), Lizzeri, Frechette, Perego ('22, Ecma)

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- These papers consistently find that senders **undercommunicate**
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- They offer empirical support to policies that mandate disclosure in the marketplace

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Question 3. Then why do we observe **overcommunication**?

Explaining Overcommunication

In our setting, full unraveling is not an equilibrium:

Why?

- Informativeness is always predicted to be interior $\mathcal{I} \in (0, 1)$
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- It allows theoretical predictions to fail from both directions: **over** and **under** communication)

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Our findings suggest that **undercommunication** is not a robust behavioral feature in disclosure games

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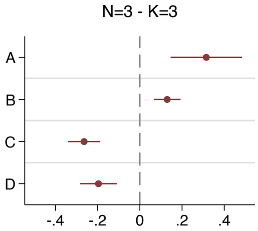
To illustrate, we estimate an OLS regression model:

details

$$\text{Prob}(s \text{ is disclosed}) = \alpha + \beta_s \cdot \theta + \gamma \cdot X + \varepsilon$$

where X is a set of regressors that controls for senders' available evidence

Explaining Overcommunication



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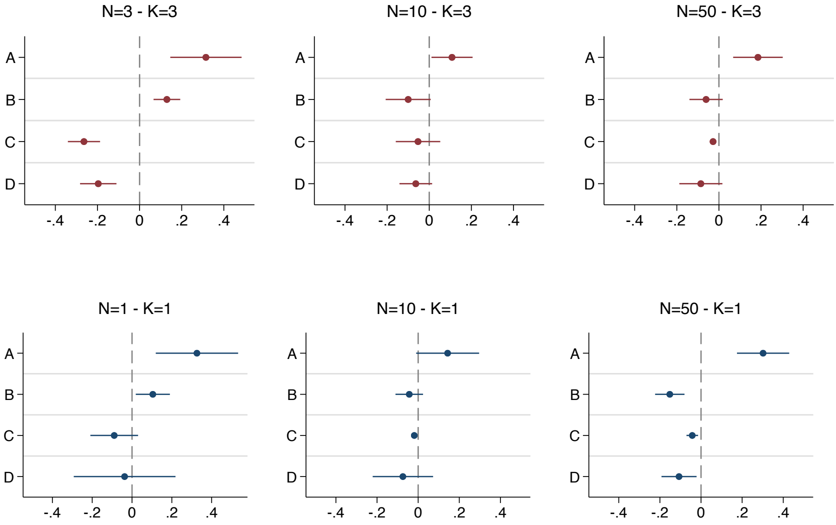

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Also: effects on GPA

Result 3. Senders exhibit a form of **deception aversion**

Sender can't lie in our setting. Yet, some actively avoid being deceptive, by disclosing evidence that is congruent with underlying state Sobel, 2023, *JPE*

State-dependent behavior makes senders' strategies more informative than they should

result 4

(receivers' beliefs)

Do Receivers Account for Selection?

The previous results have established that (modulo overcommunication) the evidence receivers see is **endogenously selected**

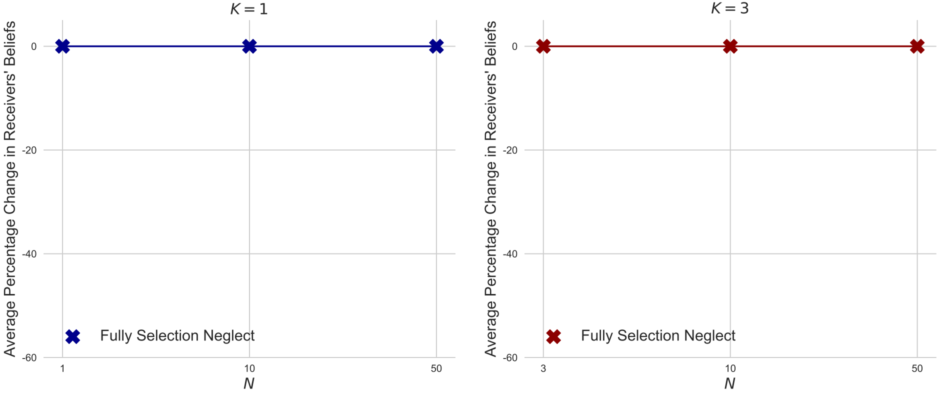
Question 4. To what extent do receivers account this selection in their responses?

To test this, we exploit the following prediction of the theory:

– Given any message, as N increases, receivers' beliefs about the state being high should decrease

We report the percentage change in receiver' beliefs averaged out across all messages and receivers

Do Receivers Account for Selection?



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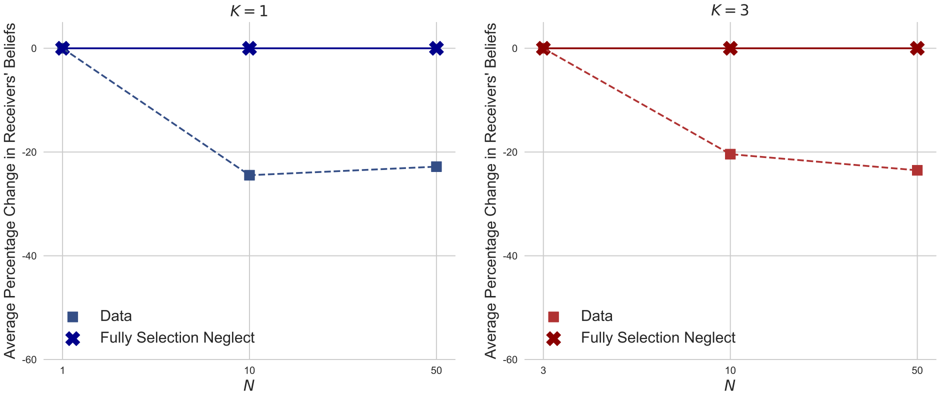

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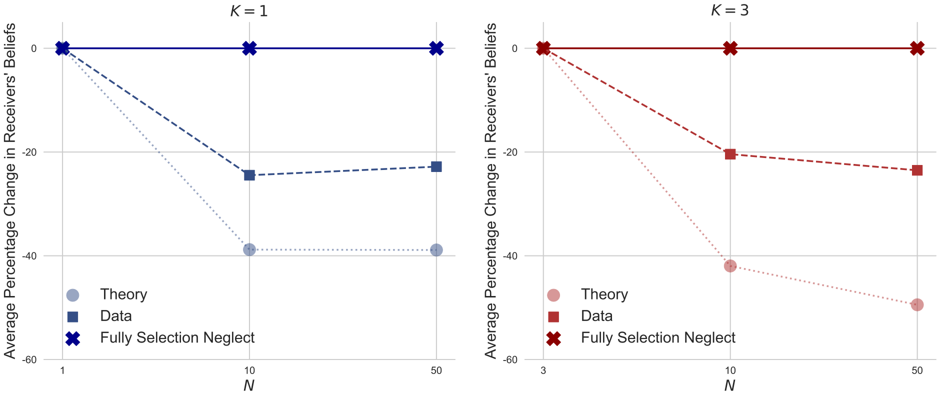

Summary of Result 4

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Recent literature has documented selection neglect in non-strategic settings, where selection is exogenous

Esponda, Vespa ('18, QE), Enke ('20, QJE), Barron, Huck, Jehiel (2023, AEJ:Micro)

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In progress: Identify receivers' "types"

result 5

(receivers' accuracy)

Do Receivers Account for Selection?

Question 5. The previous result focused on beliefs, but how costly are these mistakes in terms of payoffs?

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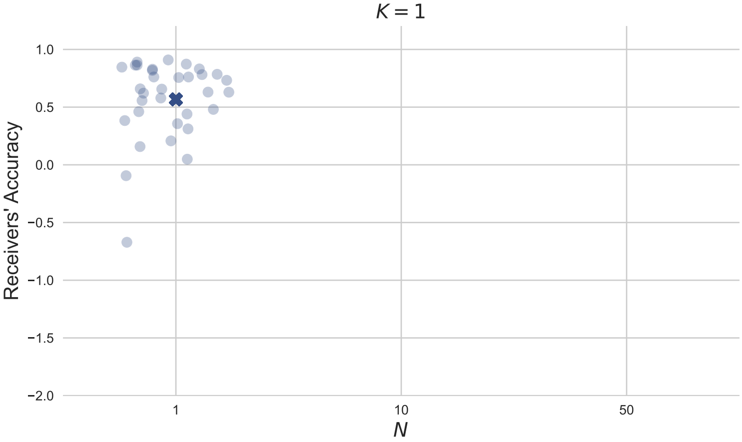
Define **accuracy** as the percentage of the payoff the receiver obtains relative to what a Bayesian would have obtained

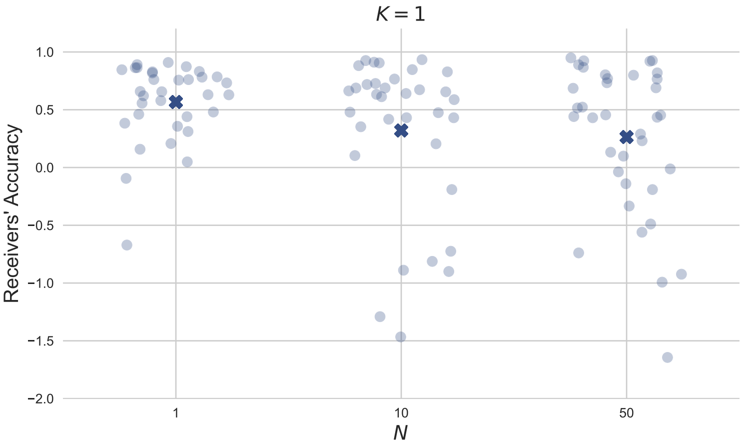
We normalize accuracy by the accuracy of receiver would obtain if she would behave at random

The theory predicts accuracy is equal to 1 in all treatments

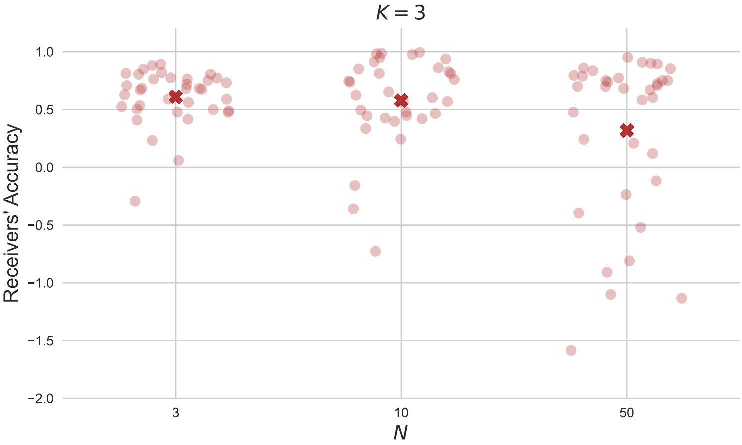
Receivers' Accuracy



Receivers' Accuracy



Receivers' Accuracy



Summary of Result 5

Result 5. Receivers become less accurate as N increases

This is puzzling especially if considering that the receiver' problem becomes "easier" as N increases

In progress: Is it selection neglect that drives this payoff losses?

conclusion

Conclusion

A comprehensive experimental study on **selective disclosure**

We exploit comparative statics to inform a novel experimental design

Our data corroborates the key qualitative predictions of the theory

- Validate **selective disclosure** as a force in communication models that is behaviorally descriptive

We detect two main *quantitative* deviations from the theory:

- A form of **deception aversion** in senders leads to **overcommunicate**
- We find evidence of a **selection neglect** in a strategic setting

The Selective Disclosure of Evidence

An Experiment

Agata Farina
NYU

Guillaume Fréchette
NYU

Alessandro Lizzeri
Princeton

Jacopo Perego
Columbia

thank you

Appendix

Related Literature: Theory

Closest theory papers:

- Milgrom (1981, Bell) – information unraveling
- Fishman and Hagerty (1990, QJE) – optimal amount of discretion
- Di Tillio, Ottaviani and Sorensen (2021, Ecma) – positive and negative effect of selection on information transmission

Richer settings (but less related):

- Glazer and Rubinstein (2004, Ecma; 2006, TE) – receiver's commitment
- Shin (2003, Ecma) – uncertainty about available evidence
- Dziuda (2011, JET) – uncertainty about sender's preferences
- Haghtalab et al. (2021) – no silence and partial congruence of preference

Related Literature: Experimental

Broader goals of studying communication in the lab:

- What scope for our comm theories if people are non-bayesian?
- Which communication biases are first order, and which are not?

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A puzzle in existing literature:

- **Disclosure:** Undercommunication, failure of unravelling. Forsythe, Isaac and Palfrey ('89, Rand), Jin and Leslie (2003, QJE), Jin, Luca and Martin (2022, AEJ: Micro)
- **Cheap Talk:** Overcommunication, lying aversion. Cai and Wang (2006, GEB), Blume, Lai and Lim (2020, Handbook)

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Our methodological approach: (from Frechette, Lizzeri and Perego (2022, Ecma))

- Test qualitative prediction of the theory in "hybrid" models that span cheap talk to disclosure

How Much Information is Transmitted?

Question: How informative are senders' strategies?

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Sender provides information — *Receiver processes information*

state θ $\rightsquigarrow$ message m $\longrightarrow$ guess a^B

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Question: How informative are senders' strategies?

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- The state θ
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$$\text{state } \theta \; \overset{\textit{Sender provides information}}{\rightsquigarrow} \; \text{message } m \; \xrightarrow{\textit{Receiver processes information}} \; \text{guess } a^B$$

We refer to $\text{Corr}(\theta, a^B)$ as the **sender-induced correlation**

Back

Richness

Theoretically, our setting differs from typical disclosure model because evidence structure is not "rich"

Evidence structure is rich if, for all θ, sender can send message that verifiably reveals θ

In our setting, evidence is noisy, and K and N are finite. No message can verifiably reveal θ

Richness drives unraveling results (Okuno-Fujiwara et al., 1990, *Restud*)

Strong assumption in many practical settings

Back

OLS Regression Model

We restrict attention to the observations in which s is available:

$$\text{Prob}(s \text{ is disclosed}) = \alpha + \beta_s \cdot \theta + \sum_{s \in S} \gamma_s \cdot \min\{k, \text{av}_s\} + \varepsilon$$

Senders' random effects; Standard errror clustered at the session level

Regressors $\{\min\{k, \text{av}_s\}\}_{s \in S}$ controls for senders available evidence

Results robust to controlling for set of available messages

Back

Some Notation: Strategies and Beliefs

Denote $\mathcal{M}$ the space of all messages

Sender's Strategy

pure and θ-independent

- $\sigma : \Omega^N \to \mathcal{M}$ s.t. $\sigma(\bar{s}) \in M(\bar{s})$, for all $\bar{s}$

where $M(\bar{s})$ is the space of available messages given $\bar{s}$

Receiver's Beliefs and Strategy

- $\mu : \mathcal{M} \to \Delta(S^N)$
- $a : \mathcal{M} \to \Delta(A)$

Given μ, receiver's optimal strategy given by

$$a(m) = \mathbb{E}(\theta|m) = \sum_{\bar{s}} \mu(\bar{s}|m)\mathbb{E}(\theta|\bar{s}) \qquad \forall\, m$$

Sequential Equilibrium

A **Sequential Equilibrium** is a pair (σ^*, μ^*) s.t.

1. For all $\bar{s} \in \Omega^N$, $\sigma^*(\bar{s}) \in M(\bar{s})$ and

$$\sum_{\bar{s}'} \mu^*(\bar{s}'|\sigma^*(\bar{s}))\mathbb{E}(\theta|\bar{s}') \geq \sum_{\bar{s}'} \mu^*(\bar{s}'|m')\mathbb{E}(\theta|\bar{s}') \qquad m' \in M(\bar{s})$$

2. For all m, supp $\mu^*(\cdot|m) \subseteq C(m) = \{\bar{s} \in S^N : m \in M(\bar{s})\}$. In particular, if $m \in \sigma^*(S^N)$,

$$\mu^*(\bar{s}|m) = q(\bar{s}|{\sigma^{\star}}^{-1}(m)) \quad \forall\, \bar{s}$$

   where $q(\bar{s}) = \sum_\theta p(\theta) f(\bar{s}|\theta)$

Equilibrium: Refinements

Unlike classic disclosure games, the sequential equilibrium outcome is **not unique** when $K < N$.

- Off-path beliefs can support other equilibrium outcome.
- Refinements for signalling games (e.g., Cho-Kreps '87, Banks-Sobel '87) have no force here.
- Refinements for cheap talk games: Farrel (1993)'s **Neologism Proofness**.

Equilibrium Multiplicity

$\Theta = \{0, 1\}$ and $p(1) = \frac{1}{2}$. $N = 2$ and $K = 1$.

$\Omega = \{A, B\}$, $f(A|\theta_H) = 1$ and $f(A|\theta_L) = \frac{1}{2}$.

θ	$\bar{s}$	$M(\bar{s})$	$\sigma^*(\bar{s})$
1	(A, A)	$\{\varnothing, A\}$	A
0	(A, B)	$\{\varnothing, A, B\}$	A
	(B, B)	$\{\varnothing, B\}$	B

$$\mathbb{E}[\theta|m = A] = \frac{4}{7} \text{ and } \mathbb{E}[\theta|m = B] = \mathbb{E}[\theta|m = \varnothing] = 0 \implies$$

No incentive to deviate

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	(B, B)	$\{\varnothing, B\}$	$\varnothing$

$$\mathbb{E}[\theta|m = \varnothing] = \frac{1}{2} \text{ and } \mathbb{E}[\theta|m = A] = \mathbb{E}[\theta|m = B] = 0 \implies$$

No incentive to deviate

Neologism Proof Equilibrium

A **neologism** is a a pair (m, C), $C \subseteq \{\bar{s} \in S^N : m \in M(\bar{s})\}$

Literal meaning of (m, C) $\rightsquigarrow$ "*My type* $\bar{s}$ *belongs to* C"

A neologism (m, C) is **credible** relative to equilibrium (σ^*, μ^*) if

1. $\sum_{\bar{s}'} q(\bar{s}'|C)\mathbb{E}(\theta|\bar{s}') > \sum_{\bar{s}'} \mu^*(\bar{\omega}'|\sigma^*(\bar{s}))\mathbb{E}(\theta|\bar{s}')$ for all $\bar{s} \in C$

2. $\sum_{\bar{s}'} q(\bar{s}'|C)\mathbb{E}(\theta|\bar{s}') \leq \sum_{\bar{s}'} \mu^*(\bar{s}'|\sigma^*(\bar{s}))\mathbb{E}(\theta|\bar{s}')$ for all $\bar{s} \notin C$

The equilibrium is **Neologism Proof** if no neologism is credible.

Equilibrium: Uniqueness

Proposition

The equilibrium with maximal selective disclosure is Neologism Proof.

Neologism Proofness delivers outcome uniqueness

An equilibrium (σ, μ) induces an outcome $x : S^N \to A$,

$$x(\bar{s}) = \sum_{\bar{s}'} \mu(\bar{s}' | \sigma(\bar{s})) \mathbb{E}(\theta | \bar{s}') \qquad \forall\, \bar{s}.$$

Belief Elicitation

Since Θ is binary and $u(a, \theta) = -(a - \theta)^2$, the receiver's task is equivalent to eliciting her beliefs via a quadratic scoring rule (QSR)

A large literature on belief elicitation has shown that QSR can be biased when subjects are not risk-neutral

To avoid this issue, we implement a binarized scoring rule *a la* Hossain and Okui (2013), which is robust to various risk preferences

Back

Back to the Example

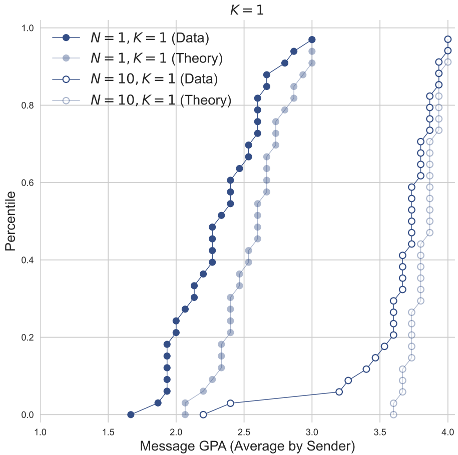
θ	$\bar{s}$	$M(\bar{s})$	$\sigma^*(\bar{s})$
1	(A, A)	$\{\varnothing, A\}$	$\varnothing$
0	(A, B)	$\{\varnothing, A, B\}$	$\varnothing$
	(B, B)	$\{\varnothing, B\}$	$\varnothing$

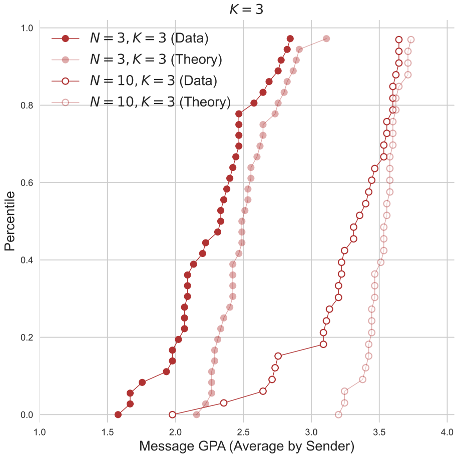
$$m = A \text{ and } C = \{(A, A), (A, B)\} \implies$$

$$\mathbb{E}[\theta | m = A] = \tfrac{4}{7} > \mathbb{E}[\theta | m = \varnothing] = \tfrac{1}{2}$$

Credible neologism $\implies$ no Neologism Proof equilibrium

Which Evidence is Disclosed?





Back

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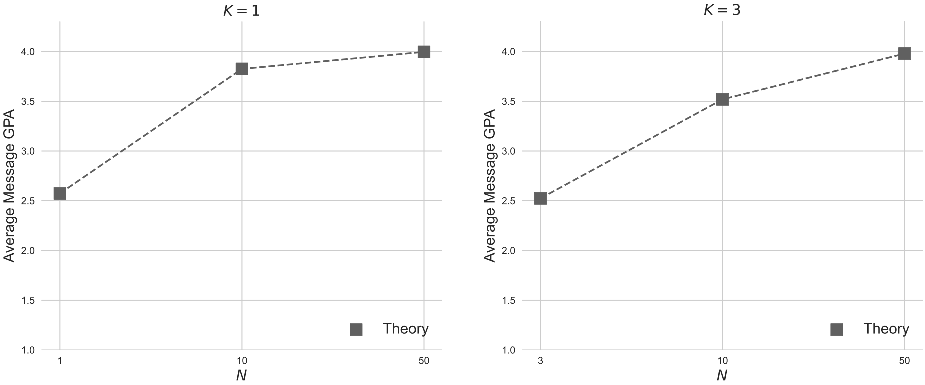

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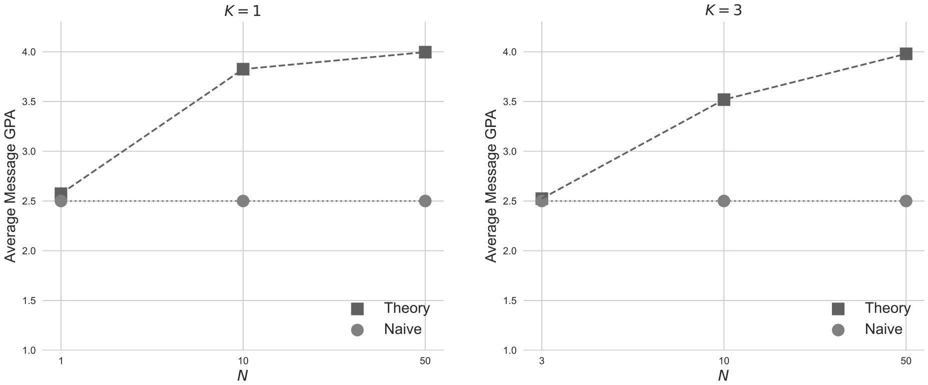

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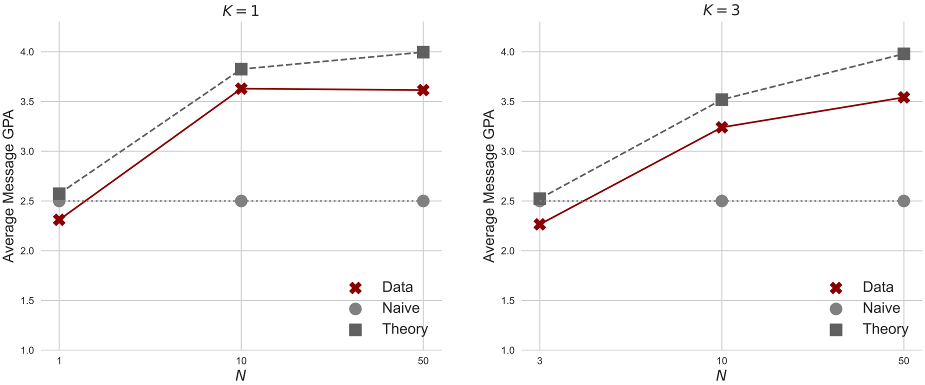

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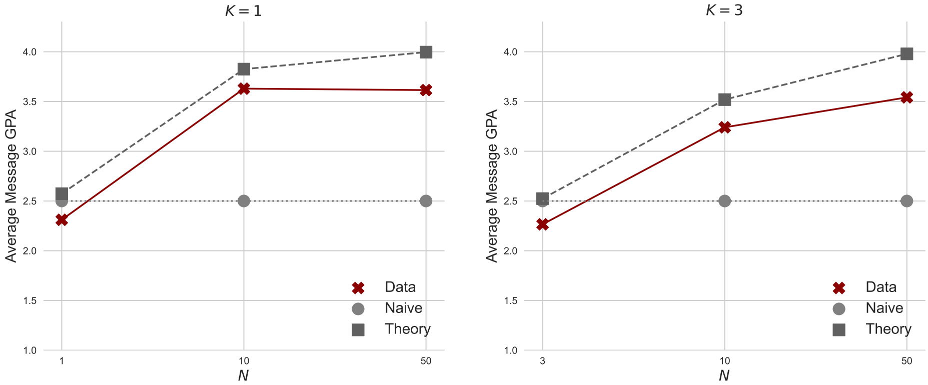

Qualitative predictions are corroborated by the data (pvals ~ 0.01)

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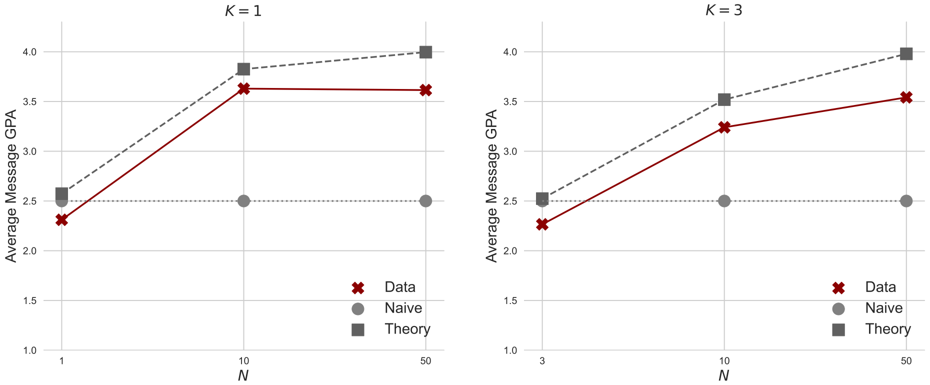
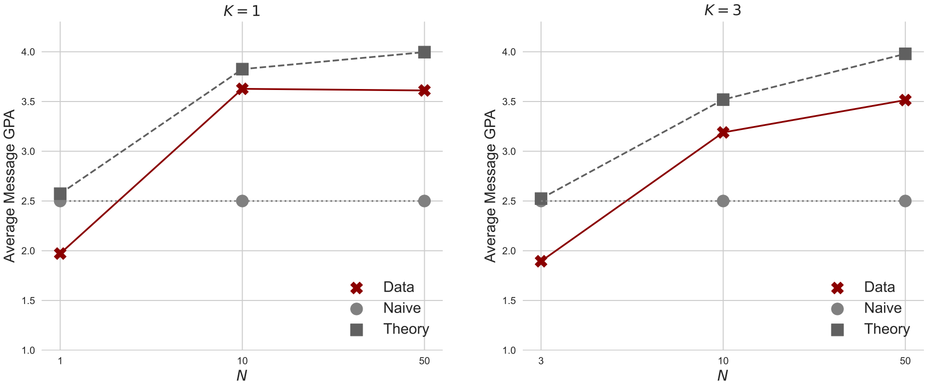


Qualitative predictions are corroborated by the data (pvals ~ 0.01)

Quantitatively, senders select less than theory predicts (pvals < 0.05)

Back

Alternative GPA: Empty = 0



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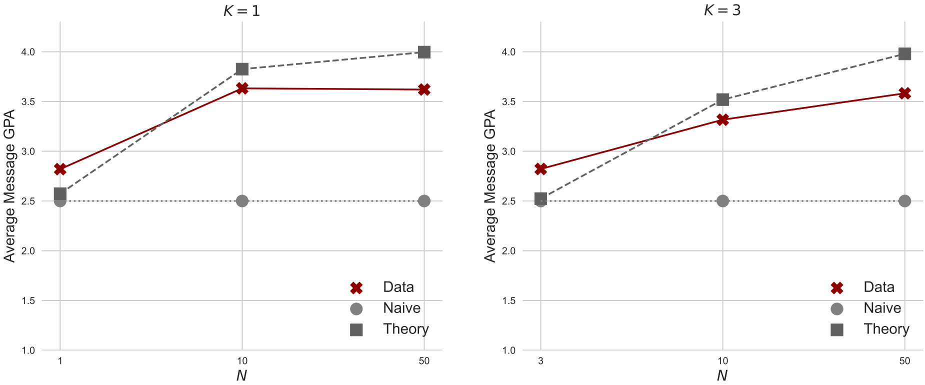
Alternative GPA: Empty = 2.5



Qualitative predictions are corroborated by the data (pvals ~ 0.01)

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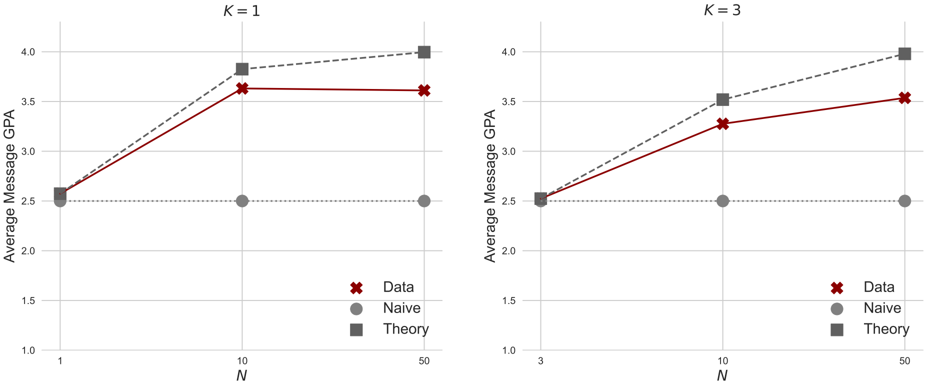
Alternative GPA: Empty = Avg Undisclosed



Qualitative predictions are corroborated by the data (pvals ~ 0.01)

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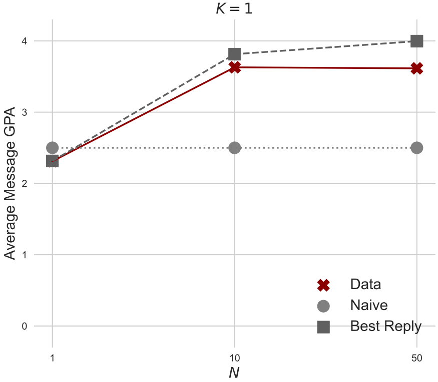
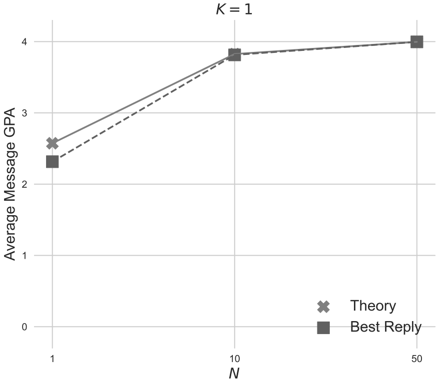
Which Evidence is Disclosed?

For $K = 1$ we can compare the observed message GPA with the one that would arise from an optimal empirical behavior of the sender: $\varnothing$ better than C and D



Quantitatively, GPA smaller than theory predicts for $N > K$ (pvals < 0.05)

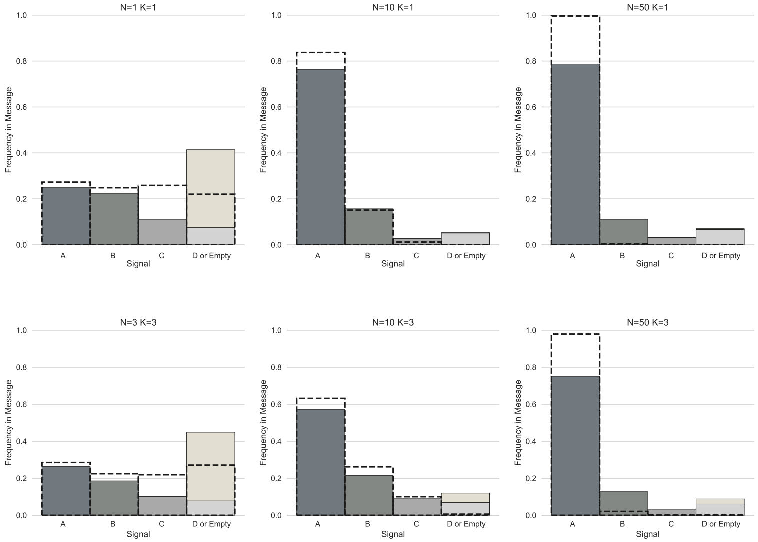
Best Reply vs Theoretical Predictions



Quantitatively, best reply and theory are different for $N < 50$ (pvals $<$ 0.01)

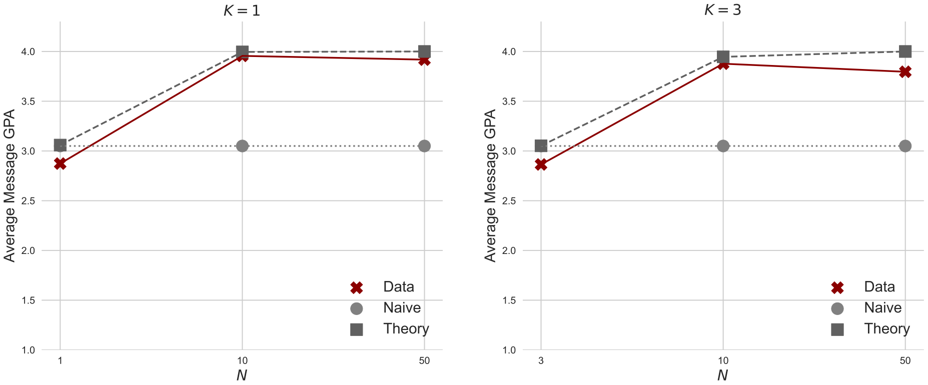
The behavior is the same 74% of the times for $N = 1$, 99% of the times for $N = 10$ and 100% of the times for $N = 50$

Frequency of Signals in Sender's Message



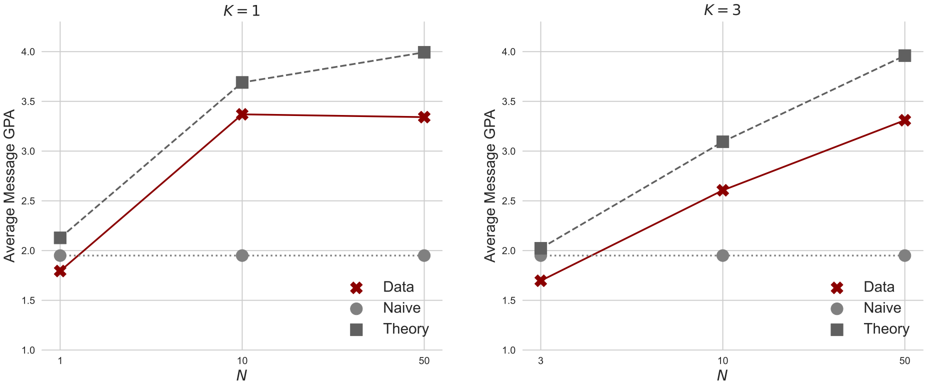
Back

Which Evidence is Disclosed? High Type



Quantitatively, senders select less than theory predicts (pvals < 0.1)

Which Evidence is Disclosed? Low Type



Quantitatively, senders select less than theory predicts (pvals < 0.05)

Back

Heterogeneity: Senders

Challenge

- Large number of urn / balls / message combinations
- Specific behavior of interest varies across treatments
  - Number of balls sent ($K = 1$ vs $K = 3$)
  - Balls sent vs balls available ($N = K$ vs $N > K$)

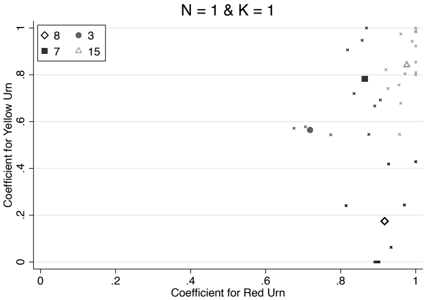
$\rightarrow$ Precludes a unified approach using those variables

Heterogeneity: Senders

Solution

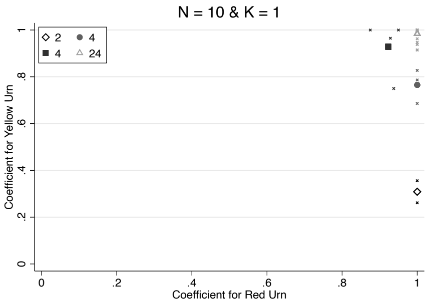
- Transform balls and messages to numbers ($B^{\#}$ and $M^{\#}$)
- Regress $M^{\#}$ on $B^{\#}|$yellow urn and $B^{\#}|$red urn
- Cluster the coefficient estimates
- Describe behavior along key dimensions of interest

Heterogeneity: Senders



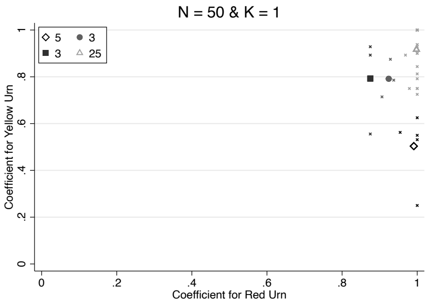
Cluster	Obs (33)	Urn	K	A	D
Triangle	15				
		Red	0.91	1	0.38
		Yellow	0.64	1	0.27
Square	7				
		Red	0.73	1	0.25
		Yellow	0.51	1	0.21
Circle	3				
		Red	0.5	0.92	n/a
		Yellow	0.54	0.67	0.49
Diamond	8				
		Red	0.71	1	0.20
		Yellow	0.30	0	0.46

Heterogeneity: Senders



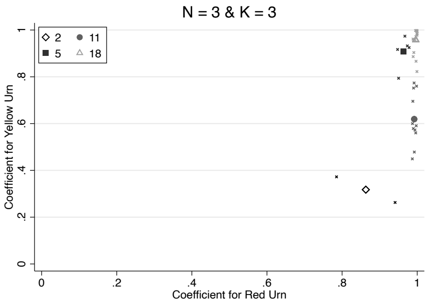
Cluster	Obs (34)	Urn	K	A	D
Triangle	24				
		Red	1	1	0
		Yellow	1	0.97	0.02
Square	4				
		Red	1	0.81	0.08
		Yellow	1	0.88	0.07
Circle	4				
		Red	1	1	0
		Yellow	1	0.46	0.14
Diamond	2				
		Red	1	1	0
		Yellow	1	0	0.89

Heterogeneity: Senders



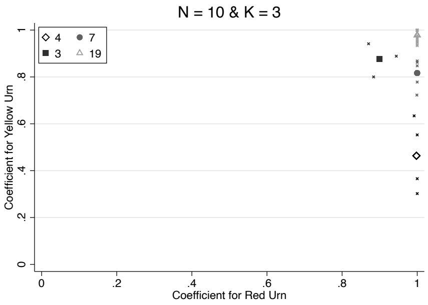
Cluster	Obs (36)	Urn	K	A	D
Triangle	25				
		Red	1	0.99	0
		Yellow	1	0.74	0.03
Square	3				
		Red	0.96	0.82	0.1
		Yellow	1	0.51	0.15
Circle	3				
		Red	1	0.78	0
		Yellow	1	0.63	0.18
Diamond	5				
		Red	1	0.96	0
		Yellow	0.95	0.26	0.46

Heterogeneity: Senders



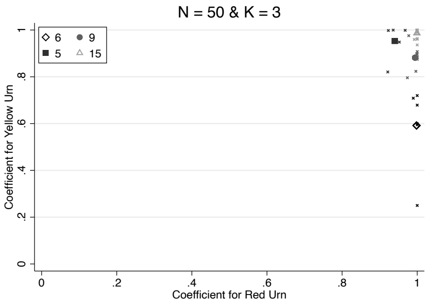
Cluster	Obs (36)	Urn	K	A	D
Triangle	18				
		Red	0.58	1	0.15
		Yellow	0.18	1	0.12
Square	5				
		Red	0.29	1	0
		Yellow	0.10	0.88	0.05
Circle	11				
		Red	0.26	1	0.06
		Yellow	0.15	0.23	0.60
Diamond	2				
		Red	0	1	0
		Yellow	0.06	0.25	0.50

Heterogeneity: Senders



Cluster	Obs (33)	Urn	K	A	D
Triangle	19				
		Red	0.99	0.99	0
		Yellow	0.88	0.96	0.01
Square	3				
		Red	1	0.46	0.17
		Yellow	1	0.43	0.04
Circle	7				
		Red	1	0.94	0
		Yellow	0.74	0.66	0.10
Diamond	4				
		Red	0.92	0.83	0
		Yellow	0.76	0.28	0.43

Heterogeneity: Senders



Cluster	Obs (35)	Urn	K	A	D
Triangle	15				
		Red	1	0.88	0
		Yellow	0.94	0.80	0
Square	5				
		Red	0.89	0.17	0
		Yellow	0.87	0.32	0
Circle	9				
		Red	0.97	0.70	0
		Yellow	0.94	0.31	0.04
Diamond	6				
		Red	1	0.86	0.03
		Yellow	0.95	0.31	0.41

Heterogeneity: Senders

Equilibrium type (56%)

- Most common
- $N > K$: Mostly report best balls independently of the state
- $N = K$: Disclose fewer than K balls

Deception Averse Type (17%)

- A's reported more often when the state is high
- D's reported more often when the state is low
- $N = K$: Disclose fewer than K balls

Others (27%)

- Similar to equilibrium types when the state is high
- Report A's less but do not report D's when the state is low
- Some low rates of A's when the state is high [confusion]

Heterogeneity: Receivers

Challenge

- Large number of messages
- Different messages across treatments
- Some messages have very few observations

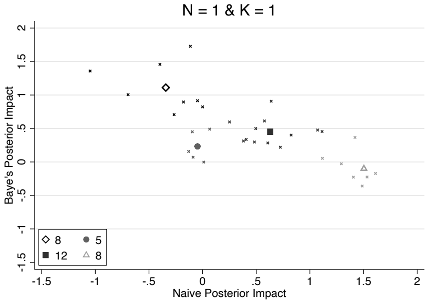
$\rightarrow$ Precludes a unified approach using that variable

Heterogeneity: Receivers

Solution

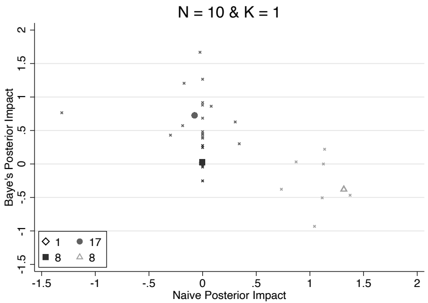
- Compute equilibrium update following each message
- Compute the update of someone who ignores selection: naive update
- Regress guesses on a constant (α) and the equilibrium and naive updates
- Cluster the coefficient estimates
- Describe behavior along key dimensions of interest

Heterogeneity: Receivers



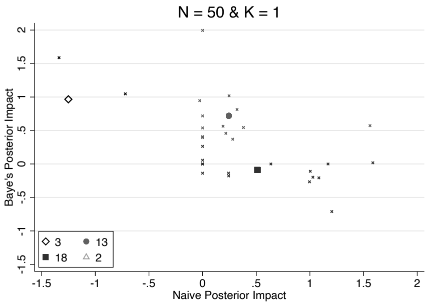
Cluster	Obs (33)	A	B	∅	C
Diamond $\alpha = 0.23$	8	0.87	0.67	0.23	0.47
Circle $\alpha = 0.39$	5	0.56	0.49	0.41	0.37
Square $\alpha = 0.02$	12	0.86	0.73	0.41	0.38
Triangle $\alpha = -0.23$	8	0.90	0.67	0.51	0.23

Heterogeneity: Receivers



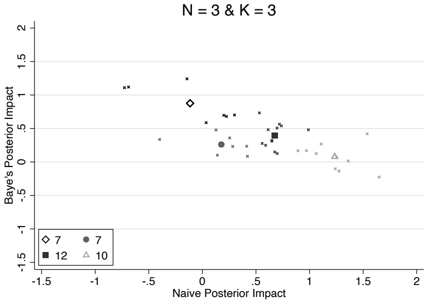
Cluster	Obs (34)	A	B	∅	D
Diamond	1				
$\alpha = 4.20$		0.60^*	0.23^*	0.60^*	n/a
Circle	17				
$\alpha = 0.28$		0.66	0.26	n/a	0.11
Square	8				
$\alpha = 0.56$		0.58	0.60	n/a	0.60
Triangle	8				
$\alpha = -0.23$		0.62	0.52	n/a	0.11

Heterogeneity: Receivers



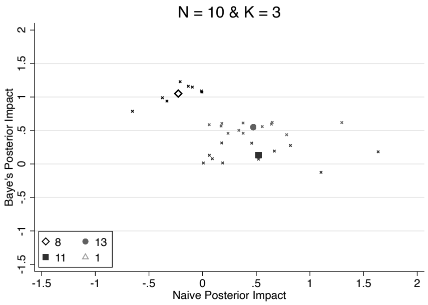
Cluster	Obs (36)	A	B	∅	D
Diamond $\alpha = 0.89$	3	0.35	0.17	0.21*	0.75
Circle $\alpha = 0.15$	13	0.71	0.29	0.46*	0.11
Square $\alpha = 0.26$	18	0.63	0.53	n/a	0.19
Triangle $\alpha = -1.15$	2	0.69	0.41	n/a	n/a

Heterogeneity: Receivers



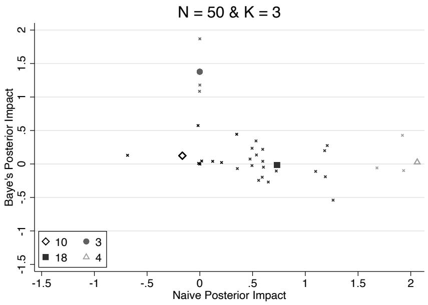
Cluster	Obs (36)	AAA	AAB	AA	AB
Diamond $\alpha = 0.20$	7	0.92*	0.86	0.86	0.62
Circle $\alpha = 0.30$	7	0.72	0.66	0.63	0.68
Square $\alpha = -0.04$	12	0.88	0.92	0.91	0.86
Triangle $\alpha = -0.24$	10	1	0.97	0.96	0.90

Heterogeneity: Receivers



Cluster	Obs (33)	AAA	AAB	AA	ABB
Diamond	8				
$\alpha = 0.19$		0.95	0.11	0.02	0.03
Circle	13				
$\alpha = -0.07$		0.89	0.70	0.24	0.26
Square	11				
$\alpha = 0.10$		0.74	0.70	n/a	0.61
Triangle	1				
$\alpha = -3.98$		1^*	0.54^*	n/a	0.02^*

Heterogeneity: Receivers



Cluster	Obs (35)	AAA	AAB	AA	DDD
Diamond	10				
$\alpha = 0.64$		0.54	0.49	0.33	0.32
Circle	3				
$\alpha = 0.11$		0.84	0.01*	n/a	0.07
Square	18				
$\alpha = -0.04$		0.67	0.69	0.57	0.12
Triangle	4				
$\alpha = -1.16$		0.89	0.80	0.91*	n/a

Heterogeneity: Receivers

- Variation in updating strategies
  - Extent they account for selection
- Being closer to equilibrium $\not\to$ higher payoffs
- However, in many treatments, groups better at accounting for selection are among the highest
- With $N = 50$, few differences in payoffs

Summary

Senders

- The majority:
  - Select the better balls to send.
  - Behave similarly for both urns.
- Some convey more information by conditioning on the type.

$\rightarrow$ More information transmitted than predicted.

Receivers

- Many do not fully account for selection.
- Some are not very responsive.

$\rightarrow$ Less information received than predicted.