

# Competitive Markets for Personal Data

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Consumers supply crucial input for modern economy: their **personal data**

Yet, they often have **limited control** over who uses it and are **imperfectly compensated** in return

- Expropriation and barter, common practice in the industry (FTC '15)

This status quo may be source of market failures (Seim et al. '22)

Could a competitive market for data avoid these problems?

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2. Propose three alternative **solutions**

- Data taxes; a data union; an making data markets more complete

**model**



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The **merchant** wants to sell products to consumers (zero MC)

Each **consumer** has unit demand for product and WTP  $\omega \in \Omega$  (finite)

Consumer's WTP distributed as  $\bar{q} \in \Delta(\Omega)$

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Two periods: 1. Data records are traded, 2. Data records are used

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## Demand Side:

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If type- $\omega$  consumer sells her record, she is paid price  $p(\omega)$

If consumer does not sell, she forgoes price and platform's "service" and obtains reservation utility  $r(\omega)$



Given acquired database  $q \in \mathbb{R}_+^\Omega$ , platform acts as **information designer**:

- It sends merchant signal about each consumer in database
- Given signal, merchant charges each consumer a personal fee  $a$
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The **payoffs** in period 2 are:

Consumer's:  $u(a, \omega) = \text{surplus}$

Merchant's:  $\pi(a, \omega) = \text{profits}$

Platform's:  $v(a, \omega) = \gamma_u u(a, \omega) + \gamma_\pi \pi(a, \omega)$

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I.e., Platform chooses recommendation mechanism  $x : \Omega \rightarrow \Delta(A)$  to solve

$$\begin{aligned} V(q) = & \max_{x: \Omega \rightarrow \Delta(A)} \sum_{\omega, a} v(a, \omega) x(a|\omega) q(\omega) \\ \text{s.t. } & \forall a, a': \sum_{\omega} \left( \pi(a, \omega) - \pi(a', \omega) \right) x(a|\omega) q(\omega) \geq 0 \end{aligned} \quad (\mathcal{P}_q)$$

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(d). Markets clear, i.e.  $q^*(\omega) = \zeta^*(\omega) \bar{q}(\omega) \quad \forall \omega$

**analysis**

Do equilibria “efficiently” allocate data records between consumers and platform?

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## Definition

An outcome  $(q^\circ, x^\circ)$  is **constrained efficient** if it solves

$$\begin{aligned} \max_{q, x} \quad & W(q, x) \\ \text{s.t.} \quad & q \leq \bar{q} \text{ and } x \text{ solves platform's ID problem given } q \end{aligned}$$

**Question:** Are equilibrium outcomes constrained efficient?

Eqm efficiency depends on how platform uses data, thus on its objective

$$\text{Recall: } v(a, \omega) = \gamma_u u(a, \omega) + \gamma_\pi \pi(a, \omega)$$

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## Proposition

- ▶ If  $\gamma_u < \gamma_\pi$ , equilibria are constrained efficient and thus consumers' welfare is maximal
- ▶ If  $\gamma_u \geq \gamma_\pi$ , equilibria can be inefficient (and consumers' welfare can be as low as  $R = \sum_{\omega} r(\omega) \bar{q}(\omega)$ )

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Equilibrium maximizes consumers welfare when platform cares more about merchant's payoff  $\rightsquigarrow$  **Why?**



- When  $\gamma_u \geq \gamma_\pi$ , platform withholds some information from merchant
- How? Platform pools consumers of different types
- Composition of a pool determines merchant's belief, thus his fee
- If a consumer does not sell her data, she affects pool composition and, thus, other consumers' payoff
- Consumers exert **externality** on each other (Relation to GLP '23)

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The paper contains many more results:

- Existence
- An iff characterization of eqm efficiency
- Extension to “social” welfare
- An illustrative example

**remedies**

How to fix this market failure?

We explore three alternative market designs:

1. Introducing **data taxes**
2. Introducing **data unions**
3. Making data markets more **complete**

**data taxes**

Introduce a simple **data tax** on consumers:

- ▶ When selling her record, consumer pays tax / receive subsidy  $t(\omega) \in \mathbb{R}$

We show that any constrained-efficient outcome can be supported by an equilibrium of the competitive economy with taxation

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## Proposition

Fix any constrained-efficient outcome  $(q^*, x^*)$ .

There exists an equilibrium of the competitive economy  $(p^*, \zeta^*, q^*, x^*)$  and taxes

$$t^*(\omega) := \sum_a u(a, \omega) x^*(a|\omega) + p^*(\omega) - \psi_{q^*}(\omega) \quad \forall \omega$$

supporting the constrained-efficient outcome. Thus, consumer welfare is maximized, regardless of platform's preferences.

Moreover, the budget is balanced.

**Idea:** with data tax, consumers internalize **social** benefit of selling their data

**data union**

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## Proposition

Equilibria of the data-union economy are constrained efficient and maximize consumers' welfare, regardless of platform's incentives

**more-complete markets**



We allow consumers to trade **the way** their records are used by platform

More-complete markets:

- There is a market where type- $\omega$  records can be sold for “intended use  $a$ ”
- The price of  $\omega$ -records,  $p(a, \omega)$ , can now depend on how it is used

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## Proposition

Equilibria of the Lindahl economy are (**unconstrained**) efficient and maximize consumers' welfare, regardless of platform's incentives

**monopsonist platform**

Drop competitive market assumption and suppose platform is **price maker**

- Platform sets data prices  $p$  by making take-it-or-leave-it offers to consumers

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## Definition

$(p^*, \zeta^*, q^*, x^*)$  is an equilibrium of the **monopsonist economy** if it solves

$$\begin{aligned} \max_{(p, \zeta, q, x)} \quad & V(q) - \sum_{\omega} p(\omega) q(\omega) \\ \text{s.t.} \quad & \text{conditions } (b), (c), (d) \text{ satisfied} \end{aligned}$$

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## Remark

In a monopsony equilibrium, outcomes are constrained-efficient (and vice versa). Moreover, platform's payoff is maximal, while consumers' welfare is minimal



**conclusion**

1. A stylized framework to study competitive markets for personal data

Rooted in GE tradition but leveraging recent progress in info-design literature

2. Emphasize a novel market failure

Platform's role as an information intermediary enables an externality that leads to inefficiencies

3. We propose three alternative market designs that fix inefficiency: data taxes, data unions, more-complete data markets