# **VERIFIABILITY IN COMMUNICATION** A (PROSPECTIVE) EXPERIMENTAL ANALYSIS

Agata Farina Guillaume Frechette Alessandro Lizzeri Jacopo Perego NYU NYU Princeton

September 2022

Columbia

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> September 2022 very preliminary

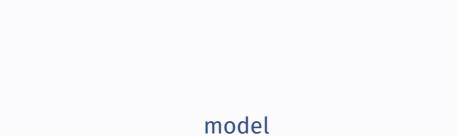
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An experimental study on the role of verifiability in communication

- Communication is fundamental problem in economics
- Verifiability (or lack thereof) is a core ingredient in our theories of communication

#### This Paper:

- ► Flexible framework to introduce rich variations in verifiability
- ▶ Develop novel comparative statics that inform experimental design
- Test main qualitative prediction of theory against observed subjects' behavior



- **1.** Sender privately observes the state  $\theta$ :
  - $-\theta \in \Theta$  with common prior  $p \in \Delta(\Theta)$

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  - $-\theta \in \Theta$  with common prior  $p \in \Delta(\Theta)$
- **2.** Given  $\theta$ , Sender draws  $N \in \mathbb{N}$  signals from:
  - An information structure  $f: \Theta \to \Delta(\Omega)$
  - N conditionally independent draws from  $f(\cdot|\theta)$

$$\bar{\omega} = (\omega_1, \ldots, \omega_N) \in \Omega^N$$

sender's "type"

- 3. Sender verifiably discloses at most K of her N signals
  - Given  $\bar{\omega}$ , sender chooses  $m \in M(\bar{\omega})$ :

$$\begin{split} M(\bar{\omega}) := \Big\{ m \in \Omega^k \mid k \leq K \text{ and } \exists \text{ injective} \\ \rho : \{1,...,k\} \to \{1,...,N\} \text{ s.t. } m = (\omega_{\rho(1)},...,\omega_{\rho(k)}) \Big\} \cup \{\varnothing\}. \end{split}$$

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- 4. Receiver observes m, takes an action, payoff realizes
  - Receiver's action  $a \in A$  and payoffs are:

$$u_S(\theta, a) = a$$
  $u_R(\theta, a) = -(a - \theta)^2$ 

# Summary: Three parameters of interests

- ightharpoonup N, the number of verifiable signals
- ► *K*, the number of reportable signals
- ightharpoonup f, the information structure

# **Assumptions:**

- $ightharpoonup \Theta$  and  $\Omega$  finite subsets of  $\mathbb{R}$ ;  $A = \mathbb{R}$
- f satisfies MLR property: For  $\theta'>\theta$ ,  $\dfrac{f(\omega|\theta')}{f(\omega|\theta)}$  strictly increasing in  $\omega$

Applications: News Media; VC financing; etc.

Interpretations K < N: institutional norm, attention cost

Closest papers that features partially verifiable information,  $\bar{\omega} \notin M(\bar{\omega})$ 

#### The Basic Setting:

- ▶ Milgrom (1981, Bell), example to showcase MLRP
- Fishman and Hagerty (1990, QJE), optimal amount of discretion

# Mechanism-Design Approach:

- lacktriangle Glazer and Rubinstein (2004, Ecma) Receiver's Verification, K=1
- ► Glazer and Rubinstein (2006, TE) Sender's verification

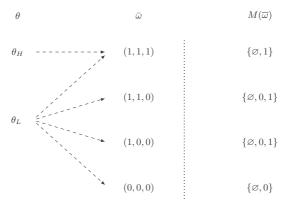
# Richer Settings: Uknown N or Endogenous K

- ► Shin (2003, Ecma)
- ► Dziuda (2011, JET)

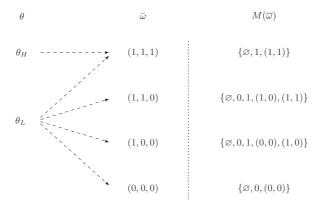


- ▶ Binary state  $\Theta = \{\theta_L, \theta_H\}$  and binary signals  $\Omega = \{0, 1\}$
- "Conclusive bad news":  $f(\omega = 1|\theta_H) = 1$  and  $f(\omega = 1|\theta_L) \in (0,1)$
- N = 3, K = 1

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#### A model of **partially verifiable** information:

- ▶ When K = N,  $\bar{\omega} \in M(\bar{\omega})$ , ubiquitous assumption  $\rightsquigarrow$  unravelling
- ▶ When  $K < N, \bar{\omega} \notin M(\bar{\omega})$ , Sender can only prove so much about herself: scope for imitation via **selective disclosure**

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Hybrid framework btw cheap-talk games and disclosure games

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Hybrid framework btw cheap-talk games and disclosure games

Changing K and N affects degree to which information is verifiable

- $ightharpoonup N \uparrow$ , Sender draws more verifiable signals about her type
- $\blacktriangleright$   $K \uparrow$ , Sender can report more signals to receiver

THIS PAPER discussion

Verifiability (or lack thereof) is a fundamental ingredient of communication

Changing K and N is tool to introduce variation in degree of verifiability

Generates rich and asymmetric comparative statics, which inform our experimental design

Test qualitative predictions against observed behavior

Question overlooked by experimental literature:

**Disclosure.** Failure of unraveling and explanations; e.g., Jin, Luca, Martin (2021) **Cheap Talk.** Lying aversion and overcommunication; e.g., Chen-Wang (2006) Methodologically closest to Frechette, Lizzeri, Perego (2021)



Solution Concept: Sequential Equilibrium

details

## Proposition (Existence)

Milgrom (1981)

For all N and  $0 \le K \le N$ , a sequential equilibrium exists where sender reports the K most favorable signals in  $\bar{\omega}$ .

Two predictions about sender's behavior:

- 1. Sender discloses K signals
- 2. When K < N, sender discloses most favorable signals

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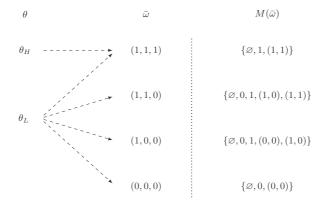
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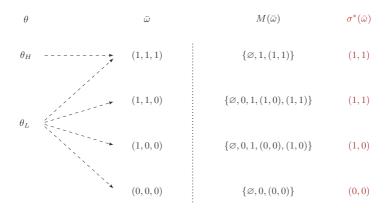
Two predictions about sender's behavior:

- 1. Sender discloses K signals "quantity"
- 2. When K < N, sender discloses most favorable signals "quality"

- Binary state  $\Theta = \{\theta_L, \theta_H\}$  and binary signals  $\Omega = \{0, 1\}$
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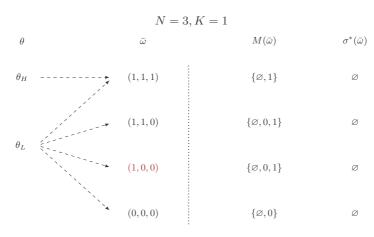


Unlike classic disclosure games, SE outcome not unique when  $K < {\cal N}$ 

Off-path beliefs can support other equilibrium outcome

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Off-path beliefs can support other equilibrium outcome



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Refinements for signalling games (e.g., Cho-Kreps '87, Banks-Sobel '87)
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The selective-disclosure outcome is the only one that survives certain refinements:

- ► Refinements for signalling games (e.g., Cho-Kreps '87, Banks-Sobel '87) have no force here
- ► Refinements for cheap talks: Farrel (1993)'s **Neologism Proofness**, Matthews, Okuno-Fujiwara, Postelwite (1991), and some weaker versions

Go to Credible Neologism

# Remark (Existence, again)

Our equilibrium is Neologism Proof.

Moreover, Neologism Proofness delivers outcome uniqueness

An equilibrium  $(\sigma, \mu)$  induces an outcome  $x: \Omega^N \to A$ ,

$$x(\bar{\omega}) = \sum_{\bar{\omega}'} \mu(\bar{\omega}' | \sigma(\bar{\omega})) \mathbb{E}(\theta | \bar{\omega}') \qquad \forall \bar{\omega}.$$

#### Proposition (Uniqueness)

Let  $(\sigma^*, \mu^*)$  be our equilibrium and  $(\sigma, \mu)$  be any other NP equilibrium. Let  $x^*$  and x their respective outcomes. Then,  $x^* = x$ .

# verifiability and communication

How does an increase in *K* affect information transmission?

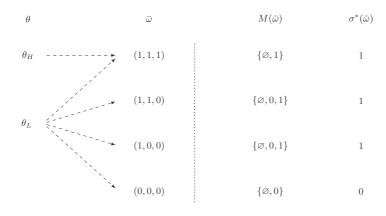
 $lackbox{M}(ar{\omega})$  becomes larger  $\Rightarrow$  Easier to send messages that others cannot imitate

#### **Proposition**

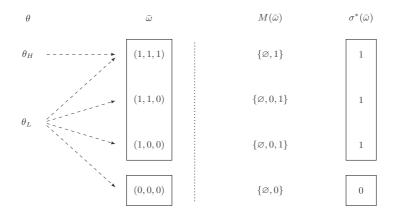
Fix N and f and  $K < K' \le N$ . The equilibrium under K' is Blackwell more informative than under K.

Proof shows that equilibrium partition  $\{\sigma^{*-1}(m)\}_{m\in\sigma^*(\Omega^N)}\subseteq\Omega^N$  becomes finer as K increases

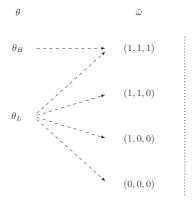
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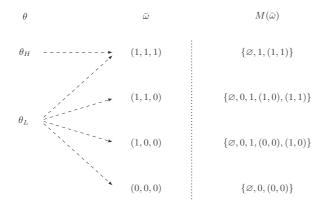


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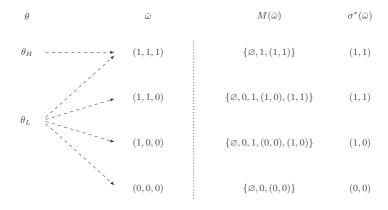


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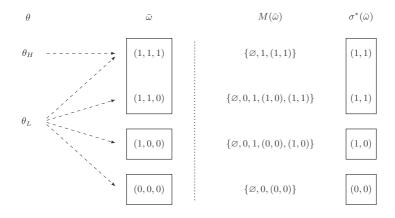
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INCREASING N results

How does an increase in N affect information transmission?

A nontrivial tradeoff:

- + Higher  $N \leadsto$  sender is endowed with more verifiable signals
- Higher  $N \rightsquigarrow$  sender can be more selective re signals to disclose

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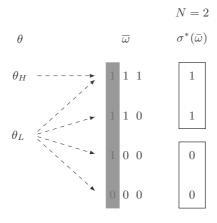
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# Today:

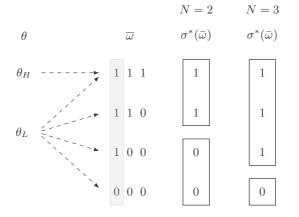
- ► Results for two special (but interesting) cases
- ► A conjecture for the general case

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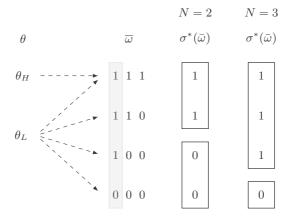
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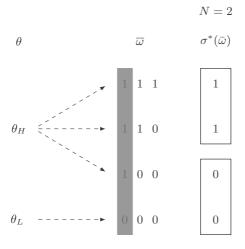
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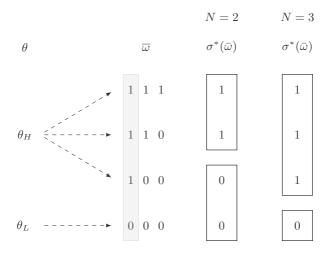
 $N \uparrow \leadsto$  more likely that  $\theta_L$  is able to imitate  $\theta_H \leadsto$  informativeness  $\downarrow$ 

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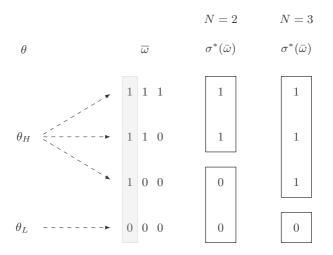
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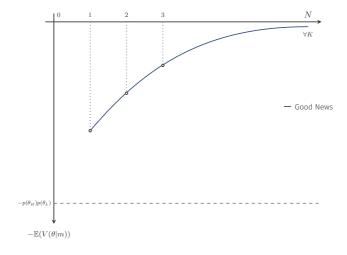
 $N\uparrow \leadsto$  less likely that  $\theta_L$  is able to imitate  $\theta_H \leadsto$  informativeness  $\uparrow$ 

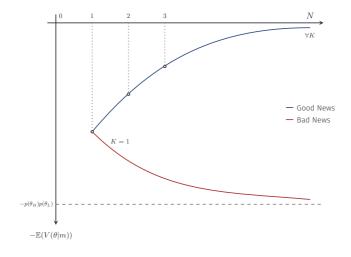
# **Proposition**

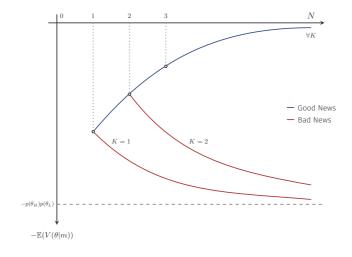
Let  $\Theta$  and  $\Omega$  be binary. Fix any K. As N increases, the receiver's payoff

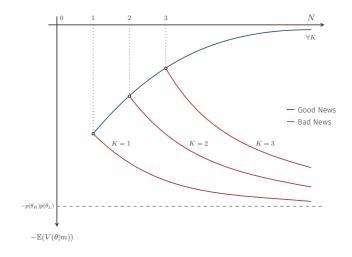
Increases if f has conclusive good news

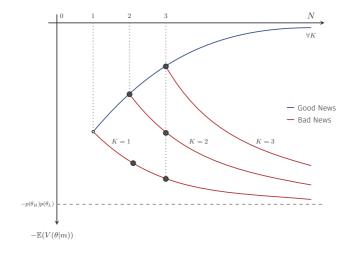
Decreases if f has conclusive bad news









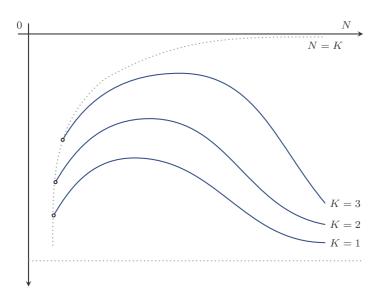


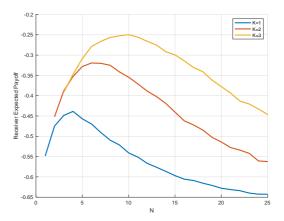
Experimental Design: Discussion of pros and cons

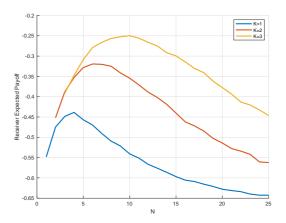
Binary state  $\theta$  + Binary signals  $\omega$  + Conclusive good/bad news f

## Conjecture

Fix K and f. There exists  $N^*\in\mathbb{N}\cup\{\infty\}$  such that informativeness increases up until  $N^*$  and decreases afterwards







Experimental Design: Discussion of pros and cons

The framework is conducive to analyze more questions:

- Partial verifiability enables study of preference alignement:
  Verifiability helps info transmission when preferences misaligned
  Verifiability may hurt info transmission when preferences aligned
- ightharpoonup Costly N
- ► Ex-ante disclosure



SUMMARY conclusions

Verifiability is a key ingredient in communication

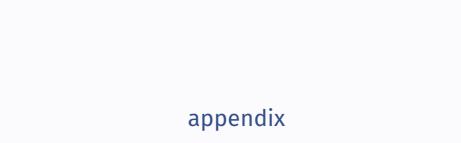
Flexible framework to introduce rich variations in verifiability

Stark comparative statics inform our experimental design

Test main qualitative predictions of the theory against observed subjects behavior (contrast with literature)

- If confirmed, this is empirical validation for a core component of our theories of communication
- ► If not, it indicates something off in our theories





Denote  $\mathcal{M} = \bigcup_{\bar{\omega} \in \Omega^N} M(\bar{\omega})$  the space of all messages

# Sender's Strategy

pure and heta-independent

$$-\sigma:\Omega^N\to\mathcal{M}$$
 s.t.  $\sigma(\bar{\omega})\in M(\bar{\omega})$ , for all  $\bar{\omega}$ 

# Receiver's Beliefs and Strategy

$$-\mu:\mathcal{M}\to\Delta(\Omega^N)$$

$$-a: \mathcal{M} \to \Delta(A)$$

Given  $\mu$ , receiver's optimal strategy given by

$$a(m) := \arg \max_{n} \mathbb{E}(-(a-\theta)^2|m) = \mathbb{E}(\theta|m)$$

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Given  $\mu$ , receiver's optimal strategy given by

$$a(m) := \arg\max_{a} \mathbb{E}(-(a-\theta)^2|m) = \mathbb{E}(\theta|m) = \sum_{\bar{-}} \mu(\bar{\omega}|m) \mathbb{E}(\theta|\bar{\omega}) \qquad \forall m \in \mathbb{E}(\theta|m) = \min_{a} \mu(\bar{\omega}|m) \mathbb{E}(\theta|\bar{\omega})$$

A Sequential Equilibrium is a pair  $(\sigma^*, \mu^*)$  s.t.

1. For all  $\bar{\omega} \in \Omega^N$ ,  $\sigma^*(\bar{\omega}) \in M(\bar{\omega})$  and

$$\sum_{\bar{\omega}'} \mu^*(\bar{\omega}'|\sigma^*(\bar{\omega})) \mathbb{E}(\theta|\bar{\omega}') \ge \sum_{\bar{\omega}'} \mu^*(\bar{\omega}'|m') \mathbb{E}(\theta|\bar{\omega}') \qquad m' \in M(\bar{\omega})$$

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 $\tilde{C}(m):=\{\bar{\omega}\in\Omega^N:m\in M(\bar{\omega})\}$ ; types that could have sent m

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2. For all m, supp  $\mu^*(\cdot|m)\subseteq \tilde{C}(m)$ . In particular, if  $m\in\sigma^*(\Omega^N)$ ,

$$\mu^*(\bar{\omega}|m) = \mathbf{q}(\bar{\omega}|\sigma^{\star^{-1}}(m)) \quad \forall \bar{\omega}$$

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1. For all  $\bar{\omega} \in \Omega^N$ ,  $\sigma^*(\bar{\omega}) \in M(\bar{\omega})$  and

$$\sum_{\bar{\omega}'} \mu^*(\bar{\omega}'|\sigma^*(\bar{\omega})) \mathbb{E}(\theta|\bar{\omega}') \ge \sum_{\bar{\omega}'} \mu^*(\bar{\omega}'|m') \mathbb{E}(\theta|\bar{\omega}') \qquad m' \in M(\bar{\omega})$$

2. For all m, supp  $\mu^*(\cdot|m)\subseteq \tilde{C}(m)$ . In particular, if  $m\in\sigma^*(\Omega^N)$ ,

$$\mu^*(\bar{\omega}|m) = \mathbf{q}(\bar{\omega}|\sigma^{\star^{-1}}(m)) \quad \forall \bar{\omega}$$

#### **Notation:**

 $\tilde{C}(m) := \{\bar{\omega} \in \Omega^N : m \in M(\bar{\omega})\}$ ; types that could have sent m

Total Prob:  $q(\bar{\omega}) = \sum_{\theta} p(\theta) f(\bar{\omega}|\theta)$ ; Conditional Prob:  $q(\bar{\omega}|K)$ 

We refine off-path beliefs via Neologism Proofness (Farrel, 1993)

A neologism is a a pair (m, C) such that  $C \subseteq \tilde{C}(m)$ .

Literal meaning of  $(m, C) \rightsquigarrow \text{"My type } \bar{\omega} \text{ belongs to } C$ "

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## Definition

A neologism (m,C) is **credible** relative to equilibrium  $(\sigma^*,\mu^*)$  if

$$(i) \ \sum_{\bar{\omega}'} q(\bar{\omega}'|C) \mathbb{E}(\theta|\bar{\omega}') > \sum_{\bar{\omega}'} \mu^*(\bar{\omega}'|\sigma^*(\bar{\omega})) \mathbb{E}(\theta|\bar{\omega}') \text{ for all } \bar{\omega} \in C,$$

$$(ii) \ \sum_{\bar{\omega}'} q(\bar{\omega}'|C) \mathbb{E}(\theta|\bar{\omega}') \leq \sum_{\bar{\omega}'} \mu^*(\bar{\omega}'|\sigma^*(\bar{\omega})) \mathbb{E}(\theta|\bar{\omega}') \text{ for all } \bar{\omega} \notin C,$$

The equilibrium is neologism proof if no neologism is credible

# Remark (Existence, again)

Our equilibrium is Neologism Proof.

Moreover, Neologism Proofness delivers outcome uniqueness

An equilibrium  $(\sigma, \mu)$  induces an outcome  $x: \Omega^N \to A$ ,

$$x(\bar{\omega}) = \sum_{\bar{\omega}'} \mu(\bar{\omega}' | \sigma(\bar{\omega})) \mathbb{E}(\theta | \bar{\omega}') \qquad \forall \bar{\omega}.$$

### Proposition (Uniqueness)

Let  $(\sigma^*, \mu^*)$  be our equilibrium and  $(\sigma, \mu)$  be any other NP equilibrium. Let  $x^*$  and x their respective outcomes. Then,  $x^* = x$ .

In lab implementation, we may not need all these neologisms in:

$$\{(m,C): m \in \mathcal{M}, C \subseteq \tilde{C}(m)\}$$

When  $\Omega$  is binary, it is sufficient to consider these neologisms:

If m is off-path its literal meaning is "my highest k signals are m"

# Proposition

If  $\Omega$  is binary, weaker refinement guarantees outcome uniqueness.