# **Competitive Markets for Personal Data**

Simone Galperti Tianhao Liu Jacopo Perego

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**Motivation** introduction

Consumers supply a crucial input for modern economy: their personal data

Yet, they often have limited control over who uses their data and how:

 "Expropriation" and barter, common practice in the industry, may lead to inefficiencies and inequality
 FTC '15, Bergemann et al. '23

New legislation gives consumers more control over their data (GDPR, CCPA, ...)

Lays foundations upon which data markets could emerge

What properties would such markets have? Which institutions should be designed to ensure efficient outcomes?

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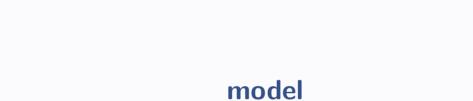
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     building on GLP '23
  - Not due to exogenous correlation in consumers' data as in Choi et al ('19),
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- 2. Propose three remedies to this market failure:
  - Data unions; Data taxes; Lindahl prices



One merchant, one platform, a unit mass of consumers

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Two periods: 1. Data markets are open 2. Product market is open

# **Period 1: Competitive Data Markets**

The consumers and the platform trade data records at market prices  $p=(p(\omega))_{\omega\in\Omega}$ , which they take as given

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## The supply side:

- If type- $\omega$  consumer sells her record to the platform, she is paid  $p(\omega)$  and is later intermediated with merchant
- If type- $\!\omega$  consumer doesn't sell her record, she obtains  $\bar{r}$

Given acquired database q, platform acts as **information intermediary**: (as in BBM'15)

- It sends signal to merchant about each consumer in database
- Given signal, merchant charges each consumer a fee a
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The payoffs in period 2 are:

Consumer's: 
$$u(a, \omega) = \max\{\omega - a, 0\}$$

Merchant's: 
$$\pi(a,\omega) = a \, \mathbb{1}(\omega \ge a)$$

Platform's: 
$$v(a,\omega) = \gamma_u \; u(a,\omega) + \gamma_\pi \; \pi(a,\omega)$$

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Info-design problem equiv to platform choosing mechanism  $x:\Omega \to \Delta(A)$  s.t.

$$\begin{split} V(q) &= \max_{x:\Omega \to \Delta(A)} \sum_{\omega,a} v(a,\omega) x(a|\omega) q(\omega) \\ \text{s.t. } \forall a,a' : \ \sum_{\omega} \Big( \pi(a,\omega) - \pi(a',\omega) \Big) x(a|\omega) q(\omega) \geq 0 \\ &\qquad \qquad \qquad \text{(canonical ID problem with endogenous } q) \end{split}$$

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# inefficiency of the data economy

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\max_{q,x} \quad \text{Consumers's Welfare}(q,x) + \text{Platform's Welfare}(q,x) s.t. q is feasible (i.e., q \leq \bar{q})
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Results extend to using social welfare and unconstrained efficiency

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**Result.** If Private and Social Benefits are aligned for all  $\omega$ , equilibrium is constrained efficient

### **Data Externality**

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What is the **social benefit** when a type- $\omega$  consumer sells her record?

**Note:** How can Private and Social benefits be misaligned given that we assumed data records are uncorrelated?

The misalignment depends on how platform uses consumers data, and thus on its objective  $\text{Recall: } v(a,\omega) = \textcolor{red}{\gamma_{\pmb{u}}} \; u(a,\omega) + \gamma_{\pi} \; \pi(a,\omega)$ 

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#### **Proposition**

- If  $\gamma_u < \gamma_\pi$ , equilibria are constrained efficient, and consumers' welfare is maximal
- If  $\gamma_u \ge \gamma_\pi$ , equilibria can be inefficient (and, in fact, consumers' welfare can be as low as  $\bar{r}$ )

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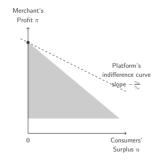
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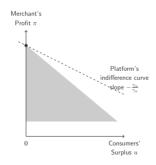






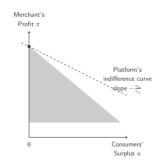


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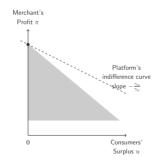
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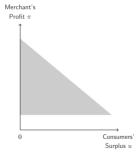
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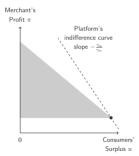


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- Private and social benefit are aligned
- All equilibria are constrained efficient

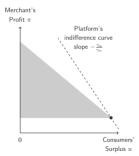




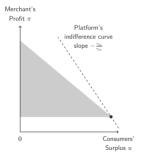






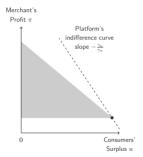


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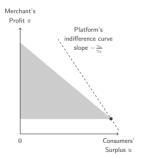
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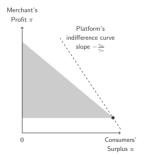
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- Leading to  $\sum_a x^*(a,\omega) u(a,\omega) \neq \xi^*(\omega)$
- Externalities → Eqm inefficiency
- Example: think of lowest-type consumer

example

#### Suppose:

- Only two types of consumers:  $\omega \in \{1,2\}$  with  $\bar{q}(1) < \bar{q}(2)$
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What's the **constrained-efficient** allocation  $(q^{\circ}, x^{\circ})$  in this case?:

All type-1 consumers sell records

$$q^{\circ}(1) = \bar{q}(1)$$

Some type-2 consumers sell records

$$q^{\circ}(2) = \bar{q}(1) < \bar{q}(2)$$

Platform provides no info to merchant

$$x^{\circ}(a=1|\omega)=1, \ \forall \omega$$

- Merchant charges lowest fee to all consumers in database

a = 1

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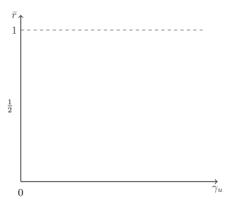
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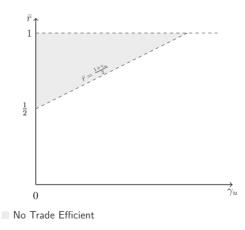
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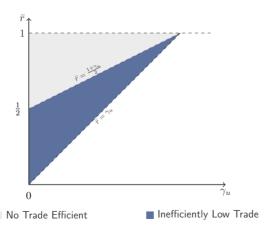
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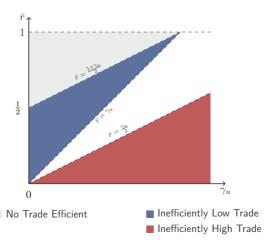
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- Hence, type-2 consumer do not want to sell either Why? Private benefit is  $p^*(2)+0 \leq \gamma_u < \bar{r}$
- Market unravels → No trade → Inefficiency

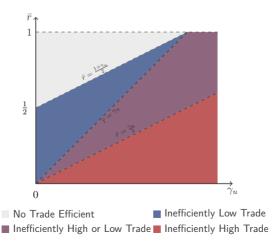
Low-type consumers do not internalize positive externality they exert

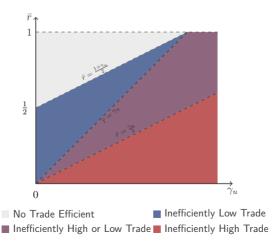












## **Stepping Back**

Information intermediaries play key role in digital markets

Acquisti et al. '16

They often intermediate agents with conflicting interests drivers-riders, etc.)

(sellers-buyers;

Due to conflicting interests, platforms may withhold some information from the agents  $\rightsquigarrow$  pooling  $\rightsquigarrow$  externality

This paper illustrates how this practice can lead to market failures

This force more general than our price-discrimination application, or the merchant being a monopolist

remedies

Remedies

How to fix this market failure?

We explore three alternative market designs:

- 1. Introducing a data union
- 2. Implementing data taxes
- 3. Making data markets more complete

# data union

Data Union remedies

A data union manages the data of participating consumers on their behalf

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It works as follows:

- Consumers choose whether to become members of the union
- If they do, they relinquish their data to the union
- Union chooses which data to sells to the platform
  - Consumers retain reservation utility unless record is sold to platform
- With the proceeds of sale, union compensates all participating consumers (to incentivize their participation)
- Union maximizes welfare of participating consumers

Formally, the data union problem is:

$$\begin{split} \max_{(p,q,x)} & & \sum_{\omega} p(\omega) \bar{q}(\omega) + \sum_{a,\omega} u(a,\omega) x(a|\omega) q(\omega) + \sum_{\omega} (\bar{q}(\omega) - q(\omega)) r(\omega) \\ \text{such that} & & q \leq \bar{q}, \\ \text{and} & & \sum_{\omega} p(\omega) \bar{q}(\omega) = V(q), \\ \text{and} & & x \text{ solves } \mathcal{P}_q, \\ \text{and} & & p(\omega) + \frac{q(\omega)}{\bar{q}(\omega)} \sum_a u(a,\omega) x(a|\omega) + \left(1 - \frac{q(\omega)}{\bar{q}(\omega)}\right) r(\omega) \geq r(\omega). \end{split}$$

Data Union remedies

#### **Proposition**

Equilibria of the data-union economy are constrained efficient and maximize consumers' welfare

Union coordinates consumers by deciding which records should be sold and how consumers should be compensated

This offers theoretical support to recent policy proposals that discuss role data unions could play in the data economy

Posner Weyl 18; Bergemann et al 23



Data Taxes remedies

Enrich competitive economy by introducing a simple data tax:

lacktriangle When selling her record, consumer pays tax  $au(\omega)\in\mathbb{R}$  to the govt

#### **Proposition**

Let  $(q^\circ, x^\circ)$  be a constrained-efficient allocation. There exists a profile of taxes  $\tau^*$  and an equilibrium of the economy with taxation  $\tau^*$  that implements  $(q^\circ, x^\circ)$ .

When properly designed, data taxes force consumers to internalize effects that selling their records create on economy

Let allocation  $(q^{\circ}, x^{\circ})$  be constrained efficient

Let  $p^*$  be a supergradient of  $V(q^\circ)$ 

Define 
$$\tau^*(\omega) \triangleq p^*(\omega) + \sum_a x^{\circ}(a|\omega)u(a,\omega) - r(\omega)$$

Notice that  $U^*(\omega) - \tau^*(\omega) \equiv r(\omega)$ 

Therefore, all consumers indifferent  $\leadsto$  choose  $\zeta^*$  to implement  $q^\circ$ 

more-complete markets

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We let price of data depend not only on its type (i.e.,  $\omega$ ) but also on its "intended use" (i.e., a)

Price of data is now  $p(\omega, a)$ 

Platform and the consumer trade on how record will be used

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#### **Proposition**

Equilibria of this Lindahl economy are (unconstrained) efficient and maximize consumers' welfare



conclusion

### **Summary**

1. A stylized framework to study competitive markets for personal data

Rooted in GE tradition but leveraging recent progress in info-design

Identify novel inefficiency leading this otherwise perfectly competitive market to fail

Show how inefficiency critically depends on platform's role as an information intermediary

**3.** Propose three alternative market designs that fix inefficiency: data unions, data taxes, richer data prices

# **Competitive Markets for Personal Data**

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Thank You!

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- 2. We exclude merchant's payoff from W(q,x) If not, detect inefficiency driven by platform not fully internalizing merchant's payoff (main results extend to "aggregate" welfare)

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**Bonus:** In eqm, platform makes not profits. Thus,  $W(q^*, x^*)$  equals consumer welfare. Thus, any constrained-efficient eqm maximizes consumer welfare

A profile  $(p^*,\zeta^*,q^*,x^*)$ 

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### **Equilibrium**

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- (c). Given  $p^*$  and  $x^*$ ,  $\zeta^*$  solves consumers' problem, i.e.,

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### **Discussion of Main Assumptions**

Single platform takes data prices as given:

Substantive: price-taking behavior, i.e. competitiveness of the market

Expositional: single platform richer economy studied in GP '22

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Tractability a dynamic microfoundation in XY '23

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Three aspects of the consumer problem have been simplified:

Record fully reveals underlying type alt see GLP '23

Record bundles access and information alt see ALV '22

Reservation utility  $r(\omega)$  is exogenous alt see BB '23

