# **Competitive Markets for Personal Data**

Simone Galperti Jacopo Perego UCSD Columbia

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**Preliminary** 

**Personal data** fuels multi-billion dollar industries and is essential input to the digital economy

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**Motivation** introduction

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Unrealistic yet natural benchmark we should know about

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So severe that consumers may be better off under expropriation

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- 3. Show that "more complete" markets restore efficiency

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Basic idea in the paper

Platform as an information designer:

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When consumers data are pooled, their payoff may depend on which other consumers have sold their data

We build a competitive economy around this idea and show when it leads to market failure

We know exogenous correlation in consumers' data can lead to externalities

Choi et al. 19, Bergemann et al. 22, Acemoglu et al. 22

We explore novel externality and its consequences on competitive mkts

It emerges endogenously from how platform uses data even when data are uncorrelated We know exogenous correlation in consumers' data can lead to externalities

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Our approach:

(GLP22, GP23, and this paper)

Use tools from information-design literature

Bergemann and Morris 19, Kamenica 19

- To answer questions about data markets

Acquisti et al 16, Bergemann and Bonatti 19, Bergemann and Ottaviani 21

- 1. Leading example to illustrate main ideas and results
- 2. General model
- 3. Results

# leading example

(many consumers, one platform, one merchant)

A  $\mathbf{merchant}$  want to sell product to consumers and charge fee  $a \in \{1,2\}$ 

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platform's expected payoff

$$\begin{array}{ll} & \underset{\text{expected payoff}}{\text{platform's}} \\ & & \underbrace{U(\bar{q})} \\ & & = \max_{x:A\times\Omega\to\mathbb{R}_+} & \sum_{\omega,a} u(a,\omega)x(a,\omega) \\ & & \text{such that:} & \sum_{\omega} \left(\pi(a,\omega) - \pi(\hat{a},\omega)\right)x(a,\omega) \geq 0 \qquad \forall \ a,\hat{a} \in A \\ & & \sum_{a} x(a,\omega) = \bar{q}(\omega) \\ & & \forall \ \omega \in \Omega \\ \end{array}$$

Main twist in this paper:

What data the platform has about consumers is **endogenous** It has to acquire consumers' data in a **competitive market** 

Each consumer owns a  ${\bf data}\ {\bf record}$  that reveals her type  $\omega.$ 

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- 2. Given q, platform intermediates consumers in its database with the merchant

## Payoffs:

### If a type- $\omega$ consumer:

	keeps her record	sells her record
Consumer	arepsilon	
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**Later:** many platforms, many merchants, many types, arbitrary objectives, partially informative records



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$$q^* \in \arg\max_q U(q) - \sum_{\omega} p^*(\omega)q(\omega)$$

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2. Given  $p^*$  and  $q^*$ ,  $\alpha^*(\omega)$  solves  $\omega$ -consumer's problem

$$\alpha^*(\omega) \in \arg\max_{\alpha \in [0,1]} (1-\alpha)\varepsilon + \alpha \Big(p^*(\omega) + \mathbb{E}_{q^*}(g(a,\omega))\Big)$$

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$$q^*(\omega) = \alpha^*(\omega)\bar{q}(\omega), \quad \forall \omega$$

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Social planner maximizes **Consumers Welfare** by picking a data allocation and transfers:

$$\begin{split} \max_{q,T} & T + \sum_{\omega} (\bar{q}(\omega) - q(\omega)) \varepsilon + q(\omega) \mathbb{E}_q \big( g(a,\omega) \big) \\ \text{such that:} & q(\omega) \leq \bar{q}(\omega) \qquad \forall \ \omega \in \Omega \\ & T \leq U(q) \end{split}$$

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Note: Merchant profit is excluded from welfare computation:

- ▶ In model, no way to transfer merchant profits to consumer
- ► This benchmark gives model a fair chance at efficiency (stronger negative result)



What is the competitive equilibrium of this economy?

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To illustrate, begin from the case  $\gamma=0,$  i.e.,

$$u(a,\omega) = \beta g(a,\omega) + \gamma \pi(a,\omega)$$

Platform objective is to maximize consumer's gains from trade

Imagine platform expropriated consumers of their records  $(\approx \text{status quo})$ 

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Record Type	Prices		Platform's Database
$\omega = 1$	0	0	1
$\omega = 2$	0	0	2

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 $(\approx$  status quo)

Record Type	Prices		Platform's Database	Use
$\omega = 1$	0	0	$1 \xrightarrow{\frac{1}{2}}$	$s^L \longrightarrow a = 1$
$\omega = 2$	0	0	$2 \xrightarrow{\frac{1}{2}}$	$s^H \longrightarrow a = 2$

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Record Type	Prices	Records Kept	Platform's Database	Use	Consumers Welfare
$\omega = 1$	0	0	$1 - \frac{1}{2}$	$s^L \longrightarrow a = 1$	1
$\omega = 2$	0	0	$2\frac{\sqrt{}}{\frac{1}{2}}$	$\rightarrow s^H \longrightarrow a = 2$	1

# Towards the Equilibrium (1): Expropriation

Platform withholds info from merchant (due to conflict of interest,  $\gamma=0)$ 

Platform withholds info by pooling data records

When data records are pooled, consumer' payoff depend on what other records platform has

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Model "enables" this externality, which will lead to inefficiencies

### Expropriation:

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$\omega = 2$	0	2	0 ——	$\rightarrow s^H \longrightarrow a=2$	96

# **Comments:**

1. Low-type consumers have no incentive to sell:

Price 
$$p^*(1) = \beta$$
 is too low

 $(\beta < \varepsilon)$ 

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# Comments:

2. High-type consumers have no incentive to sell:

Price 
$$p^*(2) = 0$$
 is too low  $(\varepsilon > 0)$ 

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$\omega = 2$	0	2	0 ——	$\rightarrow s^H \longrightarrow a=2$	32

#### Comments:

Platform has no strict incentive to buy.
 Equilibrium prices = marginal values

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## Comments:

4. Equilibrium welfare is inefficiently low

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# Comments:

**5.** If  $\varepsilon < \frac{1}{3}$ , equilibrium welfare is even lower than under expropriation!

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**6.** (Negative prices) – High-type consumers would want to subsidize low-type consumers to sell their data, but market is too incomplete

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$\omega = 1$	β	0	$1 - \frac{1}{2}$	$s^L \longrightarrow a = 1$	$1 + \beta$
$\omega = 2$	0	0	$2{\frac{1}{2}}$	$\rightarrow s^H \longrightarrow a = 2$	1   β

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$\omega = 1$	β	0	$1 - \frac{1}{2}$	$s^L \longrightarrow a = 1$	$1 + \beta$
$\omega = 2$	0	0	$2\frac{1}{2}$	$\rightarrow s^H \longrightarrow a = 2$	1   1

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#### Comments:

1. Too many high-type consumers sell. Attracted by expected gain  $(\frac{1}{2})$ , they decrease each other payoffs

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## Comments:

2. Welfare is inefficiently low

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### Comments:

3. Negative price on high-type consumers? Again, not an equilibrium...

The example illustrates that inefficiency can be generic

(for all  $\varepsilon$ )

Also, inefficiency can be severe: Welfare higher under expropriation

- Perverse consequence of empowering consumers

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# Example shows two kinds of failures:

- "Too little data:" When low-type consumer keeps her data, she decreases payoff of high types
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## Example shows two kinds of failures:

- "Too little data:" When low-type consumer keeps her data, she decreases payoff of high types
- "Too much data:" When high-type consumer sells, she decreases payoff of other high types

## Both failures originates from same source:

Platform has incentives to withhold information

$$u(a,\omega) = \beta g(a,\omega) + \gamma \pi(a,\omega)$$

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$$u(a,\omega) = \beta g(a,\omega) + \gamma \pi(a,\omega)$$

Record Type	Prices	Records Kept	Platform's Database	Use (Full Info)
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$5\gamma$	$1 \longrightarrow s^L \longrightarrow a = 1$	0	$\gamma$	$\omega = 1$
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#### Comments:

 Platform does not withhold information from the merchant → price discrimination

Suppose that  $\beta = 0$  and  $\gamma > \varepsilon$ :

$$u(a,\omega) = \beta g(a,\omega) + \gamma \pi(a,\omega)$$

Consumer Welfar	Platform's Use (Full Info)	Records Kept	Prices	Record Type
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#### Comments:

Crucially, payoff of a consumer is independent of decisions of other consumers. No externalities

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#### Comments:

3. Consumers get fully compensated: They get payoff that platform makes with their data. → Equilibrium is efficient



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consumer:  $g_i(a_i, \omega)$ 

merchant:  $\pi_i(a_i, \omega)$ 

platform:  $u_i(a_i, \omega)$ 

1. Info about this consumer's WTP  $\omega$ 

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Exclusivity is key: Data record is rival good

A collection of data records is called a **database**: denoted  $q_i \in \mathbb{R}_+^\Omega$ 

Suppose platform i has acquired database  $\ensuremath{q}_i$ 

i.e., i has exclusive access to consumers whose records belong to  $q_i$ 

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$$\begin{split} \max_{x_i:A\times\Omega\to\mathbb{R}_+} & & \sum_{\omega,a} u_i(a,\omega)x_i(a,\omega) \\ \text{such that:} & & \sum_{\omega} \left(\pi_i(a,\omega) - \pi_i(\hat{a},\omega)\right)x_i(a,\omega) \geq 0 \qquad \forall \ a,\hat{a}\in A \\ & & \sum_{a} x_i(a,\omega) = q_i(\omega) \qquad \qquad \forall \ \omega\in\Omega \end{split}$$

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$$\begin{aligned} & \overbrace{U_i(q_i)}^{\text{platform's}} &= \max_{x_i: A \times \Omega \to \mathbb{R}_+} & \sum_{\omega, a} u_i(a, \omega) x_i(a, \omega) \\ & \text{such that:} & \sum_{\omega} \left( \pi_i(a, \omega) - \pi_i(\hat{a}, \omega) \right) x_i(a, \omega) \geq 0 \qquad \forall \ a, \hat{a} \in A \\ & \sum_{\alpha} x_i(a, \omega) = q_i(\omega) \qquad \qquad \forall \ \omega \in \Omega \end{aligned}$$

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Platform i is an information designer: It sends a signal about each consumers's  $\omega$  to its vendor to influence his price a

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Denote by  $x_{q_i}^*$  a solution (note: it depends on the entire database)

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## platforms

(1)

(2)

3

# platforms vendors

1)....

2

3).....

#### consumers

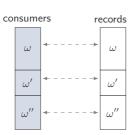


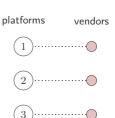
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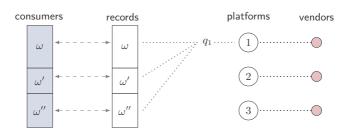






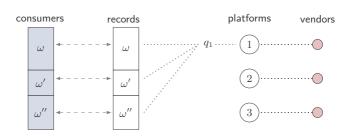






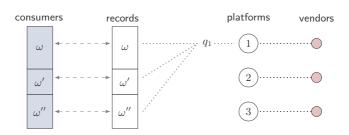
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- 3. Payoffs realize



We study the welfare properties of three different economies:

 $\mathcal{E}_1$  An economy with expropriation

Platforms own consumers data and can trade

 $\mathcal{E}_2$  An economy with data ownership

Consumers own their data and can trade

 $\mathcal{E}_3$  An economy with data ownership and Lindhal prices

Data are priced conditional on how it is used

### In this economy:

- ► Consumers "expropriated" of their records: no control, imperfect compns
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## Definition. Equilibrium in $\mathcal{E}_1$

Prices  $p^* \in \mathbb{R}^\Omega$  and a feasible data allocation  $q^* \in \mathbb{R}_+^{\Omega \times I}$  are an equilibrium of  $\mathcal{E}_1$  if:

- 1. Platforms maximize given prices  $q_i^* \in \arg\max_{q_i} U_i(q_i) \sum_{\omega} p^*(\omega) q_i(\omega)$
- 2. All markets clear  $\text{for all } \omega, \ p^*(\omega) \Big( \bar{q}(\omega) \sum_i q_i^*(\omega) \Big) = 0$

Platform i's payoff depends only on  $q_i$ , not on  $q_j$ 

(exclusivity)

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economy  $\mathcal{E}_1$ 

## Proposition. Equilibrium Characterization in $\mathcal{E}_1$

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Every platform-optimal allocation can be supported as an equilibrium of  $\mathcal{E}_1$ 

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### Equilibrium in $\mathcal{E}_2$ :

Prices  $p^* \in \mathbb{R}^{\Omega}$ , data allocation  $q^* \in \mathbb{R}_+^{\Omega \times (I+1)}$ , consumers' decisions  $\alpha^* \in (\Delta(I))^{\Omega}$  are an equilibrium if:

1. Given  $p^*$ , database  $q_i^*$  solves platform i's problem

$$q_i^* \in \arg\max_{q_i} U_i(q_i) - \sum_{\omega} p^*(\omega) q_i(\omega)$$

2. Given  $p^*$  and  $q^*$ ,  $\alpha^*(\omega)$  solves  $\omega$ -consumer's problem

$$\alpha^*(\omega) \in \arg\max_{\alpha(\omega) \in \Delta(I)} (1 - \alpha(0|\omega)) r(\omega) + \sum_i \alpha(i|\omega) \Big( p^*(\omega) + \mathbb{E}_{q_i^*}(g_i(a_i, \omega)) \Big)$$

3. Markets clear

$$q_i^*(\omega) = \alpha^*(i|\omega)\bar{q}(\omega), \quad \forall \omega, i$$

economy  $\mathcal{E}_2$ 

#### What We Know:

- ► Equilibrium *can* be inefficient ~ our leading example
- Sufficient conditions for efficiency:

### **Proposition. No-Intermediation Case**

When  $u_i = \pi_i$  for all i, equilibria in  $\mathcal{E}_2$  exist and are efficient

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### What We Don't Know (yet):

- ► Sufficient conditions for inefficiency beyond examples?
- ▶ Sufficient conditions for existence in the intermediation case?

economy  $\mathcal{E}_3$ 

How can we fix inefficiencies discussed so far?

## $\mathcal{E}_3$ – An Economy with Lindhal prices

How can we fix inefficiencies discussed so far?

We enrich our economy by opening "more complete" markets following e.g. Arrow 69, Laffont 78

- ightharpoonup Consumers can sell record for a **specific purpose** (i.e. an action  $a_i$ )
- A richer price system: prices  $p_i(\omega,a_i)$  depend on record type, on platform identity, and on intended use  $a_i$

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This presumes data use is contractible

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We enrich our economy by opening "more complete" markets following e.g. Arrow 69, Laffont 78

- ightharpoonup Consumers can sell record for a **specific purpose** (i.e. an action  $a_i$ )
- A richer price system: prices  $p_i(\omega,a_i)$  depend on record type, on platform identity, and on intended use  $a_i$

This presumes data use is contractible

## Proposition. Equilibrium Characterization in $\mathcal{E}_3$

Equilibria in  $\mathcal{E}_3$  exist and are (first-best) efficient.

Every (first-best) efficient data allocation can be supported in an eqm

Return to case of market unravelling ( $\beta < \epsilon$ ,  $\gamma = 0$ ):

$$u(a,\omega) = \beta g(a,\omega) + \gamma \pi(a,\omega)$$

#### Record Type

 $\omega = 1$ 

 $\omega = 2$ 

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Record Type	Prices
$\omega = 1$	$p^{*}(1)$
$\omega = 2$	$p^{*}(2)$

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$$u(a,\omega) = \beta \ g(a,\omega) + \gamma \ \pi(a,\omega)$$

Record Type	Prices
$\omega = 1$	$p^*(1, a = 1)$ $p^*(1, a = 2)$
$\omega = 2$	$p^*(2, a = 1)$ $p^*(2, a = 2)$

Return to case of market unravelling ( $\beta < \epsilon$ ,  $\gamma = 0$ ):

$$u(a,\omega) = \beta \ g(a,\omega) + \gamma \ \pi(a,\omega)$$

Record Type	Prices
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$\omega = 2$	$p^*(2, a = 1)$ $p^*(2, a = 2)$

$$u(a,\omega) = \beta \ g(a,\omega) + \gamma \ \pi(a,\omega)$$

Type	Prices
$\omega = 1$	$p^*(1,1) = \beta + 1 - \varepsilon$ $p^*(1,2) = 0$
$\omega = 2$	$p^*(2,1) = -(1-\varepsilon)$ $p^*(2,2) = 0$

$$u(a,\omega) = \beta \ g(a,\omega) + \gamma \ \pi(a,\omega)$$

Record Type	Prices	Records Kept	Records Used
$\omega = 1$	$p^*(1,1) = \beta + 1 - \epsilon p^*(1,2) = 0$	0	$1 \leadsto a = 1$
$\omega = 2$	$p^*(2,1) = -(1 - \varepsilon)$ $p^*(2,2) = 0$	1	$1 \leadsto a = 1$

$$u(a,\omega) = \beta \ g(a,\omega) + \gamma \ \pi(a,\omega)$$

Record Type	Prices	Records Kept	Records Used	Consumers Welfare
$\omega = 1$	$p^*(1,1) = \beta + 1 - \epsilon $ $p^*(1,2) = 0$	0	$1 \leadsto a = 1$	$1 + \beta + \varepsilon$
$\omega = 2$	$p^*(2,1) = -(1 - \varepsilon)$ $p^*(2,2) = 0$	1	$1 \leadsto a = 1$	$1 + \beta + \varepsilon$

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## Comments

- High-type consumers subsidize the platform to acquire low-type consumers data
- Previously this was not an equilibrium. Why?

It captures a qualitative feature of recent privacy-protection policies

► EU's GDPR: "The **specific purposes** for which personal data are processed should be explicit and determined at the time of the collection of the personal data"

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## **Open Questions:**

- 1. Intermediate solutions, partial decentralization?
- 2. "Non-market" solutions: Data Unions?



## **Summary**

- 1. We introduce framework to study competitive markets for personal data and their equilibria
  - ▶ Rather general setting: many platforms, many merchants, arbitrary objectives, partially informative records, multiple types
- 2. We identify a novel externality that can make these markets inefficient
  - The way platforms withhold information creates externalities that can lead to market failures
- 3. We discuss possible solutions and their limits

