

Modelos para diferentes cantones

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```
library(keras) # for deep learning
library(tidyverse) # general utility functions

## -- Attaching packages ----- tidyverse 1.3.1 --

## v ggplot2 3.3.6      v purrr 0.3.4
## v tibble 3.1.6       v dplyr 1.0.9
## v tidyr 1.2.0        v stringr 1.4.0
## v readr 2.1.2        v forcats 0.5.1

## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()

library(caret) # machine learning utility functions

## Loading required package: lattice

##
## Attaching package: 'caret'

## The following object is masked from 'package:purrr':
##
## lift

library(tibble)
library(readr)
library(ggplot2)
library(tensorflow)

##
## Attaching package: 'tensorflow'

## The following object is masked from 'package:caret':
##
## train
```

```
library(neuralnet)
```

```
##  
## Attaching package: 'neuralnet'  
  
## The following object is masked from 'package:dplyr':  
##  
##      compute
```

Datos

```
load("C:/Users/usuario1/Desktop/CIMPA/Github_CIMPA/PRACTICA_CIMPA/base_cantones.RData")
```

```
basecanton = basecanton %>%
```

```
  dplyr::select(Canton, Year, Month, Nino12SSTA, Nino3SSTA, Nino4SSTA, Nino34SSTA, Nino34SSTA1, Nino34SSTA2
```

```
  arrange(Canton, Year, Month) %>% ungroup() %>% mutate(Month=as.numeric(Month))
```

```
normalize <- function(x) {  
  return ((x - min(x)) / (max(x) - min(x)))  
}
```

```
basecanton2 = basecanton %>% group_by(basecanton$Canton) %>%  
  mutate_if(is.numeric, normalize)
```

```
## 'mutate_if()' ignored the following grouping variables:  
## * Column 'basecanton$Canton'
```

```
basecanton2 = basecanton2[, -35]
```

```
#Train y test
```

```
data_train = as.data.frame(basecanton2) %>% filter(Year < 1) #PARA ENTRENAR HASTA 2018  
data_test = as.data.frame(basecanton2) %>% filter(Year >= 1)
```

```
X_train = data_train[, -ncol(data_train)]  
y_train = as.data.frame(data_train[, c("Canton", "RR")])
```

```
X_test = as.data.frame(data_test[, -ncol(data_test)])  
y_test = as.data.frame(data_test[, c("Canton", "RR")])
```

```
#Almacen de eval de los modelos
```

```
NRMSE = NULL  
NIS_95 = NULL
```

Arquitectura y programación del modelo

Generar un Wrapper para el learning dropout

```
# R6 wrapper class, a subclass of KerasWrapper
ConcreteDropout <- R6::R6Class("ConcreteDropout",

  inherit = KerasWrapper,

  public = list(
    weight_regularizer = NULL,
    dropout_regularizer = NULL,
    init_min = NULL,
    init_max = NULL,
    is_mc_dropout = NULL,
    supports_masking = TRUE,
    p_logit = NULL,
    p = NULL,

    initialize = function(weight_regularizer,
                          dropout_regularizer,
                          init_min,
                          init_max,
                          is_mc_dropout) {
      self$weight_regularizer <- weight_regularizer
      self$dropout_regularizer <- dropout_regularizer
      self$is_mc_dropout <- is_mc_dropout
      self$init_min <- k_log(init_min) - k_log(1 - init_min)
      self$init_max <- k_log(init_max) - k_log(1 - init_max)
    },

    build = function(input_shape) {
      super$build(input_shape)

      self$p_logit <- super$add_weight(
        name = "p_logit",
        shape = shape(1),
        initializer = initializer_random_uniform(self$init_min, self$init_max),
        trainable = TRUE
      )

      self$p <- k_sigmoid(self$p_logit)

      input_dim <- input_shape[[2]]

      weight <- private$py_wrapper$layer$kernel

      kernel_regularizer <- self$weight_regularizer *
        k_sum(k_square(weight)) /
        (1 - self$p)

      dropout_regularizer <- self$p * k_log(self$p)
      dropout_regularizer <- dropout_regularizer +
```

```

        (1 - self$p) * k_log(1 - self$p)
dropout_regularizer <- dropout_regularizer *
    self$dropout_regularizer *
    k_cast(input_dim, k_floatx())

regularizer <- k_sum(kernel_regularizer + dropout_regularizer)
super$add_loss(regularizer)
},

concrete_dropout = function(x) {
  eps <- k_cast_to_floatx(k_epsilon())
  temp <- 0.1

  unif_noise <- k_random_uniform(shape = k_shape(x))

  drop_prob <- k_log(self$p + eps) -
    k_log(1 - self$p + eps) +
    k_log(unif_noise + eps) -
    k_log(1 - unif_noise + eps)
  drop_prob <- k_sigmoid(drop_prob / temp)

  random_tensor <- 1 - drop_prob

  retain_prob <- 1 - self$p
  x <- x * random_tensor
  x <- x / retain_prob
  x
},

call = function(x, mask = NULL, training = NULL) {
  if (self$is_mc_dropout) {
    super$call(self$concrete_dropout(x))
  } else {
    k_in_train_phase(
      function()
        super$call(self$concrete_dropout(x)),
      super$call(x),
      training = training
    )
  }
}
)
)

# function for instantiating custom wrapper
layer_concrete_dropout <- function(object,
    layer,
    weight_regularizer = 1e-6,
    dropout_regularizer = 1e-5,
    init_min = 0.1,
    init_max = 0.1,
    is_mc_dropout = TRUE,
    name = NULL,

```

```

                                trainable = TRUE) {
create_wrapper(ConcreteDropout, object, list(
  layer = layer,
  weight_regularizer = weight_regularizer,
  dropout_regularizer = dropout_regularizer,
  init_min = init_min,
  init_max = init_max,
  is_mc_dropout = is_mc_dropout,
  name = name,
  trainable = trainable
))
}

# sample size (training data)
n_train <- 232
# sample size (validation data)
n_val <- 3
# prior length-scale
l <- 1e-4
# initial value for weight regularizer
wd <- 1^2/232
# initial value for dropout regularizer
dd <- 2/3

```

Arquitectura del modelo:

```

input_dim <- 32
output_dim <- 1

input <- layer_input(shape = input_dim)

```

```
## Loaded Tensorflow version 2.8.0
```

```

output <- input %>% layer_concrete_dropout(
  layer = layer_dense(units = 100, activation = "relu"),
  weight_regularizer = wd,
  dropout_regularizer = dd
) %>% layer_concrete_dropout(
  layer = layer_dense(units = 50, activation = "relu"),
  weight_regularizer = wd,
  dropout_regularizer = dd
) %>% layer_concrete_dropout(
  layer = layer_dense(units = 50, activation = "relu"),
  weight_regularizer = wd,
  dropout_regularizer = dd
) %>% layer_concrete_dropout(
  layer = layer_dense(units = 50, activation = "relu"),
  weight_regularizer = wd,
  dropout_regularizer = dd
) %>% layer_concrete_dropout(

```

```

layer = layer_dense(units = 25, activation = "relu"),
weight_regularizer = wd,
dropout_regularizer = dd
) %>% layer_concrete_dropout(
layer = layer_dense(units = 25, activation = "relu"),
weight_regularizer = wd,
dropout_regularizer = dd
) %>% layer_concrete_dropout(
layer = layer_dense(units = 25, activation = "relu"),
weight_regularizer = wd,
dropout_regularizer = dd
) %>% layer_concrete_dropout(
layer = layer_dense(units = 12, activation = "relu"),
weight_regularizer = wd,
dropout_regularizer = dd
) %>% layer_concrete_dropout(
layer = layer_dense(units = 12, activation = "relu"),
weight_regularizer = wd,
dropout_regularizer = dd
) %>% layer_concrete_dropout(
layer = layer_dense(units = 6, activation = "relu"),
weight_regularizer = wd,
dropout_regularizer = dd
) %>% layer_concrete_dropout(
layer = layer_dense(units = 6, activation = "relu"),
weight_regularizer = wd,
dropout_regularizer = dd
)

```

Entrenamiento de modelos para cada cantón

Entrenar al modelo y predecir

```

Cantones = unique(basecanton$Canton)
Evaluacion3 = matrix(NA, ncol = 2, nrow = length(Cantones))
plot_list3 = list()

plot_list_c = list()
Evaluacion_c = matrix(NA, ncol = 2, nrow = length(Cantones))

for (i in 1:length(Cantones)) {

  X_trainc = X_train %>% filter(Canton == Cantones[i])
  X_trainc = as.matrix(X_trainc[, -1])
  y_trainc = y_train %>% filter(Canton == Cantones[i])
  y_trainc = as.matrix(y_trainc[, -1])

  X_testc = X_test %>% filter(Canton == Cantones[i])
  X_testc = as.matrix(X_testc[, -1])
  y_testc = y_test %>% filter(Canton == Cantones[i])
  y_testc = as.matrix(y_testc[, -1])
}

```

```

base = as.data.frame(basecanton %>% filter(Canton == Cantones[i]) %>% dplyr::select(RR))

## Output del Modelo

mean <- output %>% layer_concrete_dropout(
  layer = layer_dense(units = output_dim),
  weight_regularizer = wd,
  dropout_regularizer = dd
)

log_var <- output %>% layer_concrete_dropout(
  layer_dense(units = output_dim),
  weight_regularizer = wd,
  dropout_regularizer = dd
)

output <- layer_concatenate(list(mean, log_var))

model <- keras_model(input, output)

model %>% compile(
  optimizer = "adam",
  loss = "mse",
  metrics = "mae")

print(Cantones[i])

history <- model %>% fit(
  X_trainc,
  y_trainc,
  epochs = 50,
  batch_size = 18,
  validation_split = 0.1
)

## MonteCarlo sampling 3 meses

denorm <- function(x) {
  return (x*(max(base$RR) - min(base$RR))+min(base$RR))
}

num_MC_samples <- 100

MC_samples <- array(0, dim = c(num_MC_samples, nrow(X_testc), 2 * output_dim))
for (k in 1:num_MC_samples) {
  MC_samples[k, , ] <- denorm((model %>% predict(X_testc)))
}

```

```

}

## Generar intervalo de confianza 3 meses

# First, we determine the predictive mean as an average of the MC samples' mean output:

# the means are in the first output column
means = NULL
means <- MC_samples[, , 1:output_dim]

# average over the MC samples
predictive_mean <- apply(means, 2, mean)

# To calculate epistemic uncertainty, we again use the mean output, but this time we're interested in
epistemic_uncertainty <- apply(means, 2, var)

# Then aleatoric uncertainty is the average over the MC samples of the variance output. 1 .

logvar = NULL
logvar <- MC_samples[, , (output_dim + 1):(output_dim * 2)]
aleatoric_uncertainty <- exp(colMeans(logvar))

# Note how this procedure gives us uncertainty estimates individually for every prediction. How do they

#Obtener RR originales

y_testc = denorm(y_testc)

df <- data.frame(
  x = 1:nrow(X_testc),
  y_testc = y_testc,
  y_pred = predictive_mean,
  e_u_lower = predictive_mean - sqrt(epistemic_uncertainty),
  e_u_upper = predictive_mean + sqrt(epistemic_uncertainty),
  a_u_lower = predictive_mean - sqrt(aleatoric_uncertainty),
  a_u_upper = predictive_mean + sqrt(aleatoric_uncertainty),
  u_overall_lower = predictive_mean -
    sqrt(epistemic_uncertainty) -
    sqrt(aleatoric_uncertainty),
  u_overall_upper = predictive_mean +
    sqrt(epistemic_uncertainty) +
    sqrt(aleatoric_uncertainty)
)

```



```
)
```

#Here, first, is epistemic uncertainty, with shaded bands indicating one standard deviation above resp.

```
metricas <- function(df){  
  NRMSE <- mean((df$y_pred-y_testc)^2)/mean(y_testc)  
  NIS_95 <- mean((df$e_u_upper-df$e_u_lower)+  
    (2/0.05)*(df$e_u_lower-y_testc)*(y_testc<df$e_u_lower)+  
    (2/0.05)*(y_testc-df$e_u_upper)*(y_testc>df$e_u_upper))/mean(y_testc)  
  return(data.frame(NRMSE,NIS_95))  
}
```

```
Evaluacion3[i,1:2] = as.numeric(metricas(df))
```

```
title = paste("Tendencia", Cantones[i], sep = " ")
```

```
p = ggplot(df, aes(x, y_pred)) +  
  geom_line(colour = "blue") +  
  geom_line(aes(x, y = y_testc, colour = "red"))+  
  geom_ribbon(aes(ymin = e_u_lower, ymax = e_u_upper), alpha = 0.3)+  
  ggtitle(title)
```

```
plot_list3[[i]] = p
```

VALORES APROXIMADOS

```
X_test_all = basecanton2 %>% filter(Canton == Cantones[i])  
X_test_all = as.matrix(X_test_all[, -c(1,33)])  
y_test_all = basecanton %>% filter(Canton == Cantones[i])  
y_test_all = as.matrix(y_test_all$RR)
```

```
denorm <- function(x) {  
  return (x*(max(base$RR) - min(base$RR))+min(base$RR))  
}
```

```
num_MC_samples <- 100
```

```
MC_samples <- array(0, dim = c(num_MC_samples, 235, 2 * output_dim))  
for (k in 1:num_MC_samples) {  
  MC_samples[k, , ] <- denorm((model %>% predict(X_test_all)))  
}
```

```

## Generar intervalo de confianza 3 meses

# First, we determine the predictive mean as an average of the MC samples' mean output:

# the means are in the first output column
means = NULL
means <- MC_samples[, , 1:output_dim]

# average over the MC samples
predictive_mean <- apply(means, 2, mean)

# To calculate epistemic uncertainty, we again use the mean output, but this time we're interested in

epistemic_uncertainty <- apply(means, 2, var)

# Then aleatoric uncertainty is the average over the MC samples of the variance output. 1 .

logvar = NULL
logvar <- MC_samples[, , (output_dim + 1):(output_dim * 2)]
aleatoric_uncertainty <- exp(colMeans(logvar))

# Note how this procedure gives us uncertainty estimates individually for every prediction. How do they

#Obtener RR originales

df <- data.frame(
  x = 1:nrow(X_test_all),
  y_test_all = y_test_all,
  y_pred = predictive_mean,
  e_u_lower = predictive_mean - sqrt(epistemic_uncertainty),
  e_u_upper = predictive_mean + sqrt(epistemic_uncertainty),
  a_u_lower = predictive_mean - sqrt(aleatoric_uncertainty),
  a_u_upper = predictive_mean + sqrt(aleatoric_uncertainty),
  u_overall_lower = predictive_mean -
    sqrt(epistemic_uncertainty) -
    sqrt(aleatoric_uncertainty),
  u_overall_upper = predictive_mean +
    sqrt(epistemic_uncertainty) +
    sqrt(aleatoric_uncertainty)
)

```

#Here, first, is epistemic uncertainty, with shaded bands indicating one standard deviation above resp.

```
metricas <- function(df){
  NRMSE <- mean((df$y_pred-y_test_all)^2)/mean(y_test_all)
  NIS_95 <- mean((df$e_u_upper-df$e_u_lower)+
    (2/0.05)*(df$e_u_lower-y_test_all)*(y_test_all<df$e_u_lower)+
    (2/0.05)*(y_test_all-df$e_u_upper)*(y_test_all>df$e_u_upper))/mean(y_test_all)
  return(data.frame(NRMSE,NIS_95))
}

Evaluacion_c[i,1:2] = as.numeric(metricas(df))

title = paste("Tendencia", Cantones[i], sep = " ")

p1 = ggplot(df, aes(x, y_pred)) +
  geom_line(colour = "blue") +
  geom_line(aes(x, y = y_test_all, colour = "red"))+
  geom_ribbon(aes(ymin = e_u_lower, ymax = e_u_upper), alpha = 0.3)+
  ggtitle(title)

plot_list_c[[i]] = p1

}
```

```
## [1] "Alajuela"
## [1] "Alajuelita"
## [1] "Atenas"
## [1] "Cañas"
## [1] "Carrillo"
## [1] "Corredores"
## [1] "Desamparados"
## [1] "Esparza"
## [1] "Garabito"
## [1] "Golfito"
## [1] "Guacimo"
## [1] "La Cruz"
## [1] "Liberia"
## [1] "Limon"
## [1] "Matina"
## [1] "Montes de Oro"
## [1] "Nicoya"
## [1] "Orotina"
## [1] "Osa"
## [1] "Parrita"
## [1] "Perez Zeledón"
```

```
## [1] "Pococí"
## [1] "Puntarenas"
## [1] "Quepos"
## [1] "San Jose"
## [1] "Santa Ana"
## [1] "SantaCruz"
## [1] "Sarapiquí"
## [1] "Siquirres"
## [1] "Talamanca"
## [1] "Turrialba"
## [1] "Upala"
```

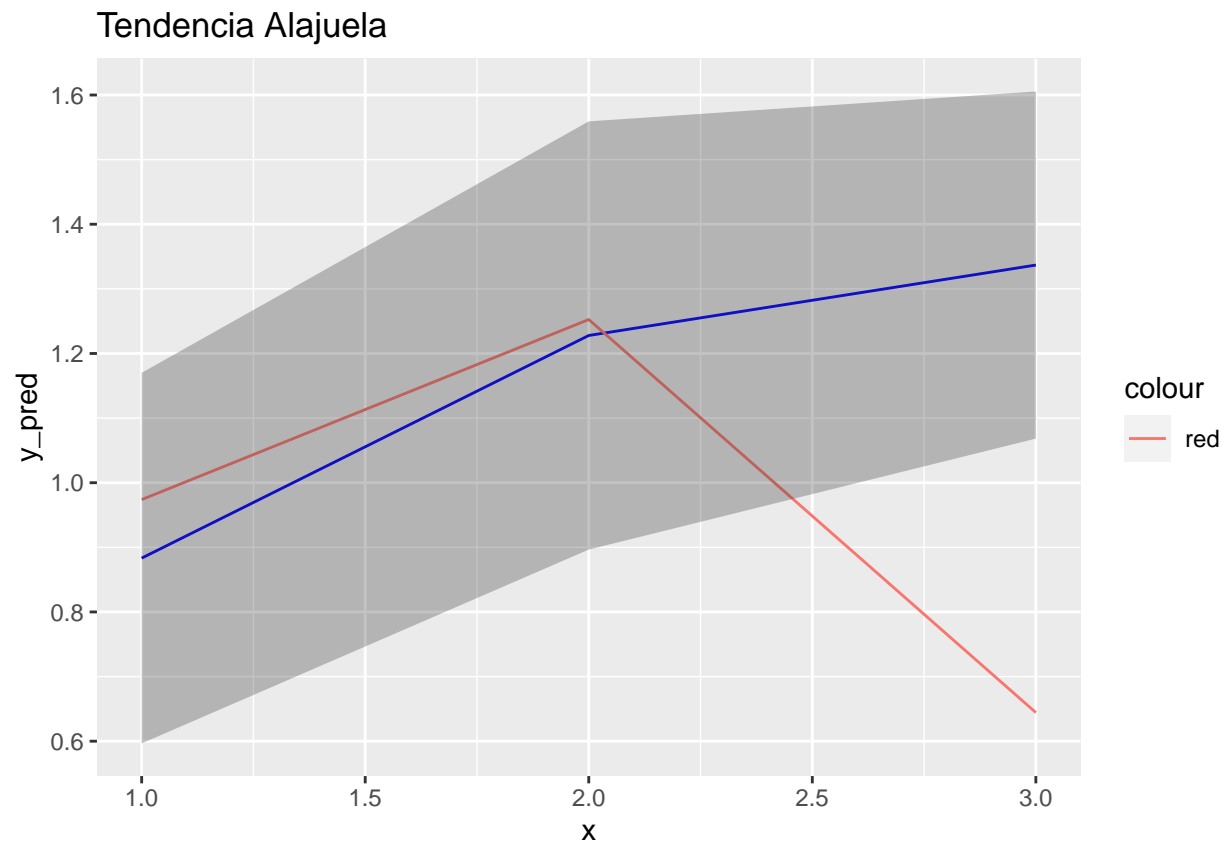
Resultados prediccion de últimos 3 meses

Evaluacion3

```
##           [,1]      [,2]
## [1,] 0.17011932  6.524133
## [2,] 0.33199908 18.106543
## [3,] 7.22101886 31.360214
## [4,] 3.41410027 35.612286
## [5,] 1.20446437 12.706318
## [6,] 0.81161020 11.955464
## [7,] 0.01211414  2.036241
## [8,] 2.93067384 34.283304
## [9,] 93.41126697 605.617233
## [10,] 2.38674048 65.836939
## [11,] 1.59495615  7.006489
## [12,] 7.97355052 176.684238
## [13,] 14.17128072 241.864840
## [14,] 1.05081536  7.988876
## [15,] 6.40902581 78.147739
## [16,] 28.16225601 300.766377
## [17,] 13.81792928 262.165734
## [18,] 0.99043378  9.697624
## [19,] 1.14230916 14.373638
## [20,] 45.79385218 260.683914
## [21,] 1.84331880 31.651908
## [22,] 1.05537546 19.384706
## [23,] 2.53953563 24.922700
## [24,] 48.88919669 325.151136
## [25,] 0.03141007  8.964273
## [26,] 0.59613111 54.446502
## [27,] 40.55697792 313.853031
## [28,] 0.47517315  9.351463
## [29,] 0.30451218  4.116998
## [30,] 14.87217978 34.892968
## [31,] 1.06090303 24.729816
## [32,]           Inf      Inf
```

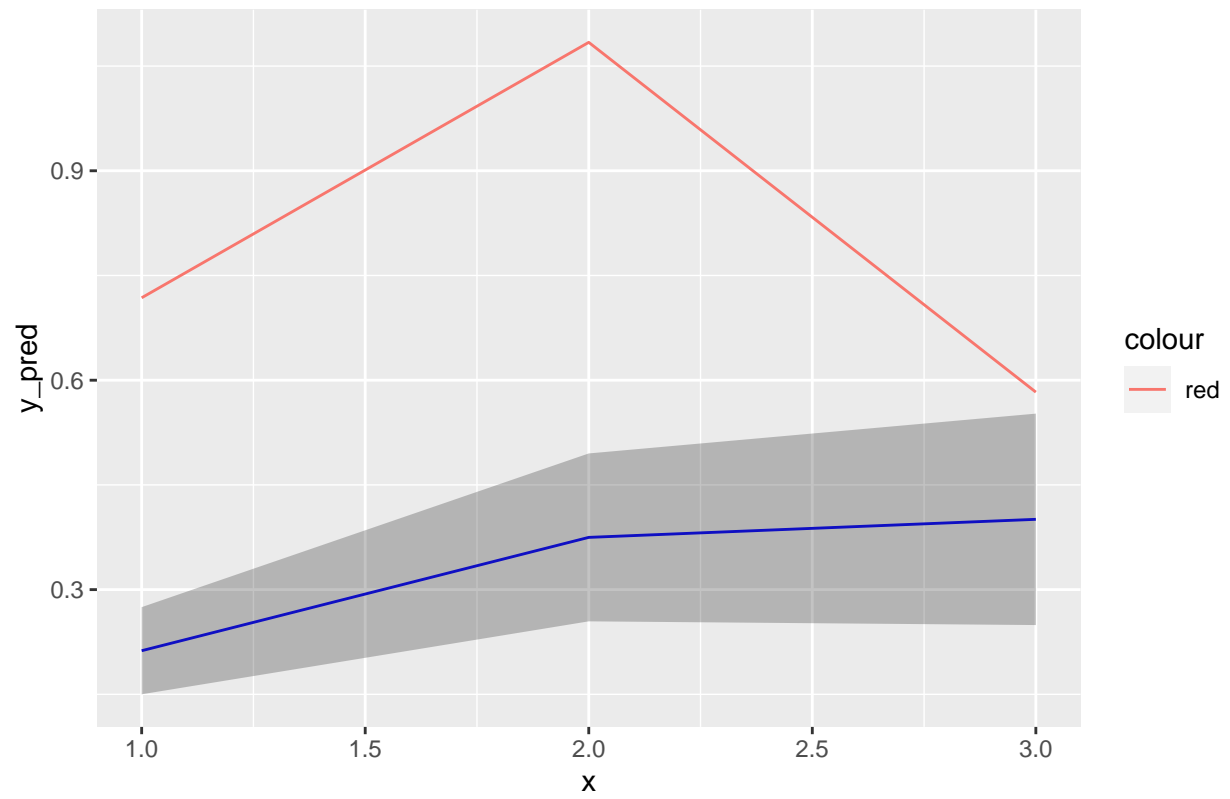
```
plot_list3
```

```
## [[1]]
```

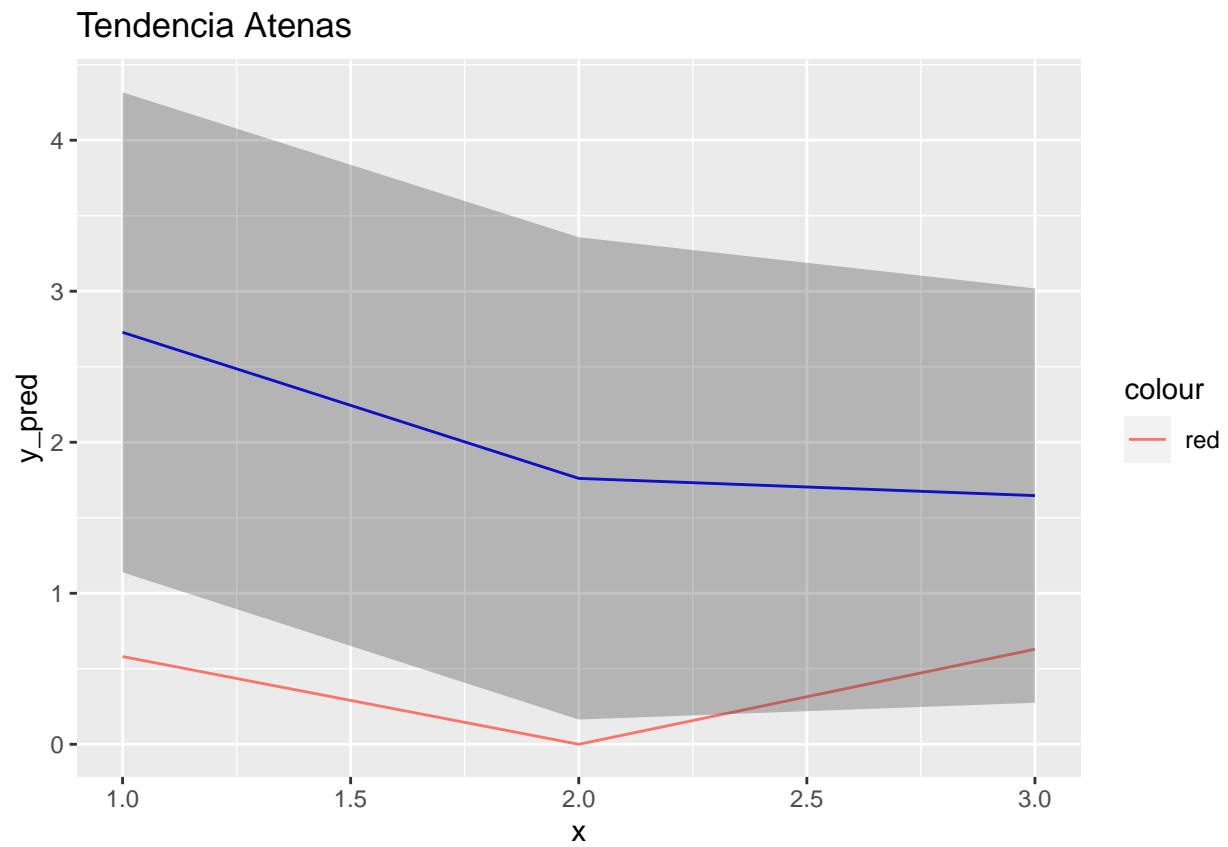


```
##  
## [[2]]
```

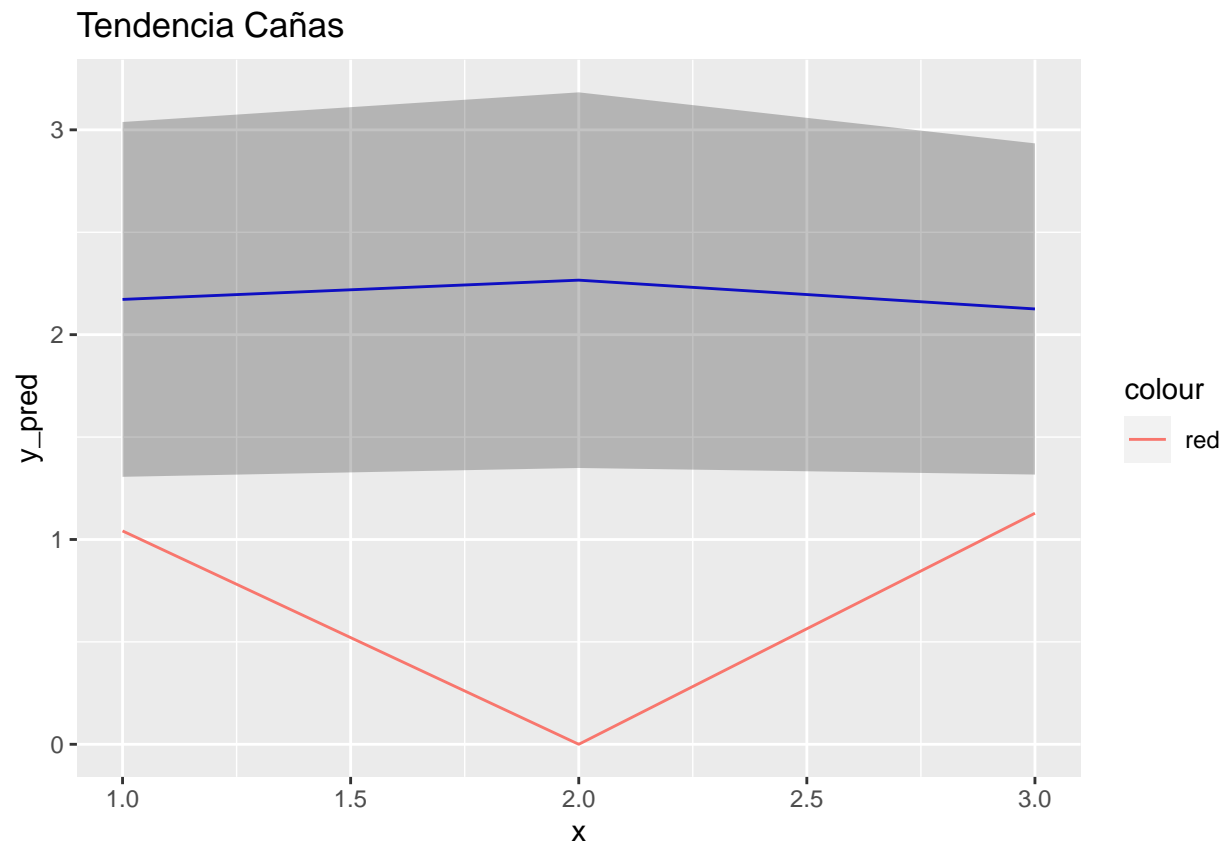
Tendencia Alajuelita



```
##  
## [[3]]
```

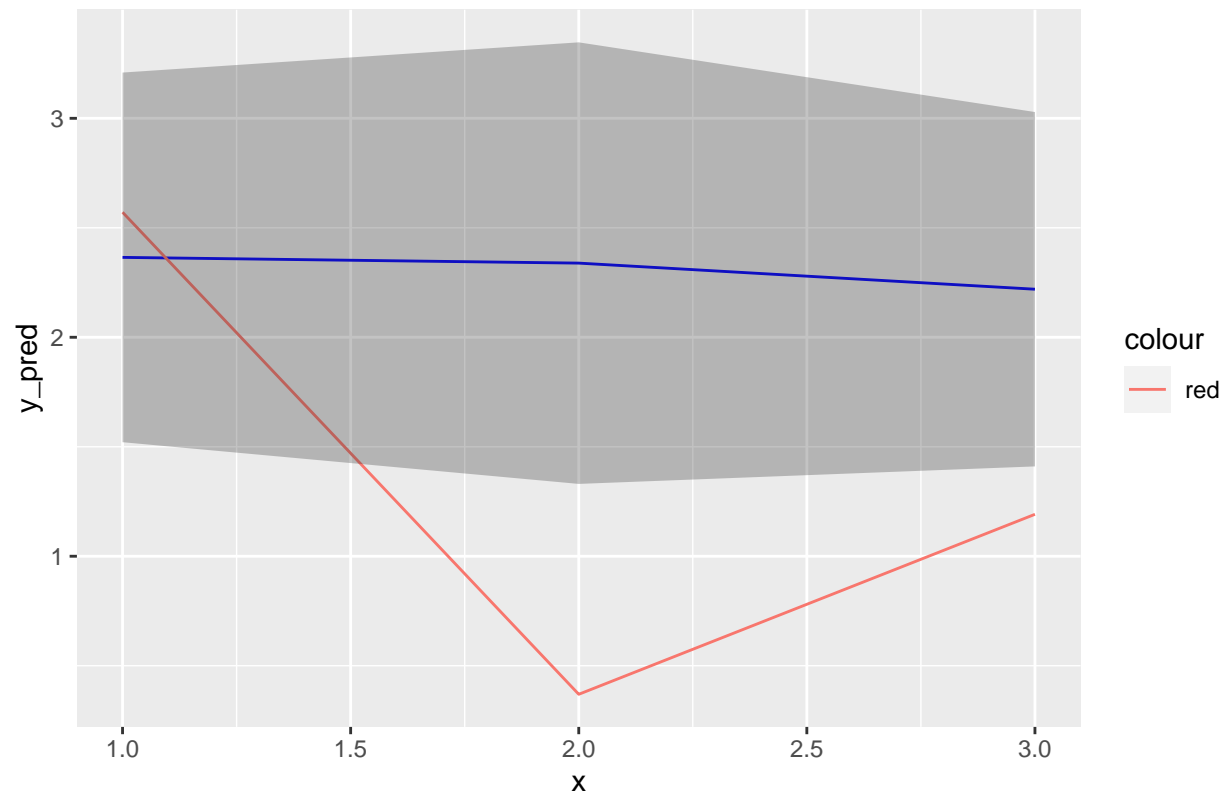


```
##  
## [[4]]
```



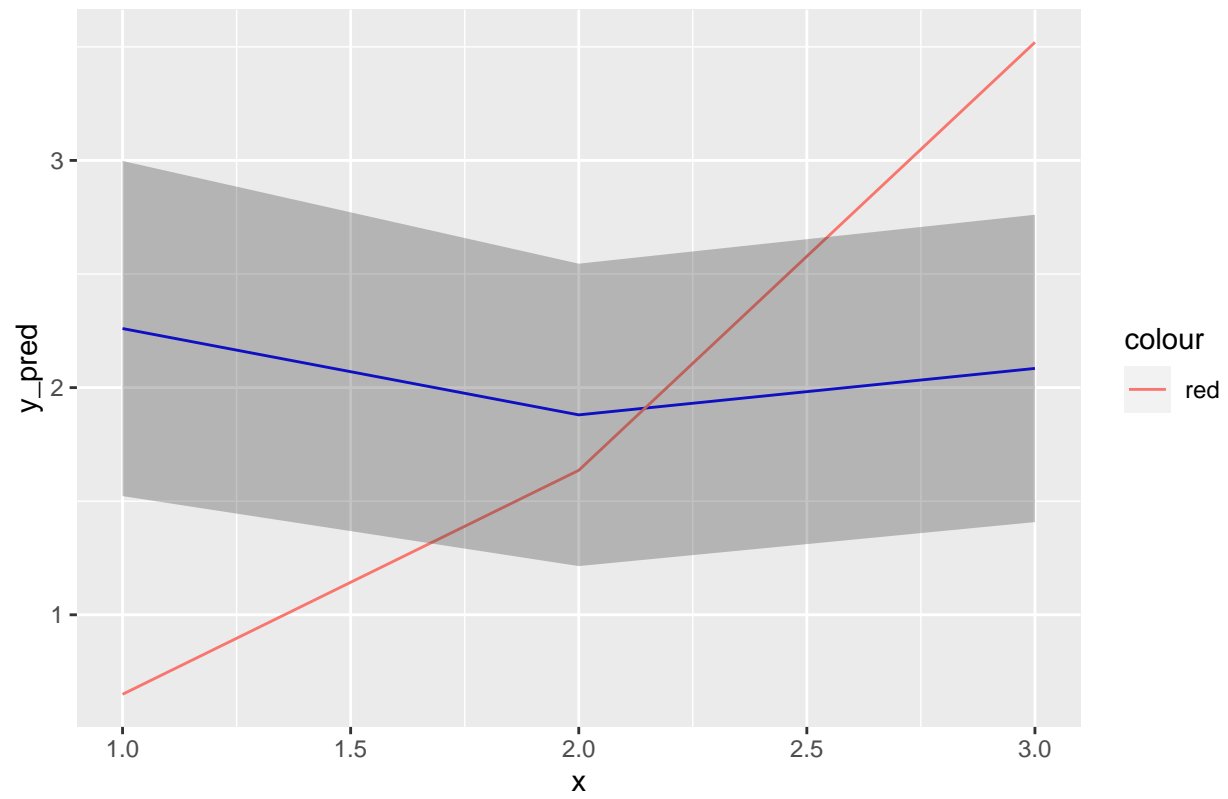
```
##  
## [[5]]
```


Tendencia Carrillo

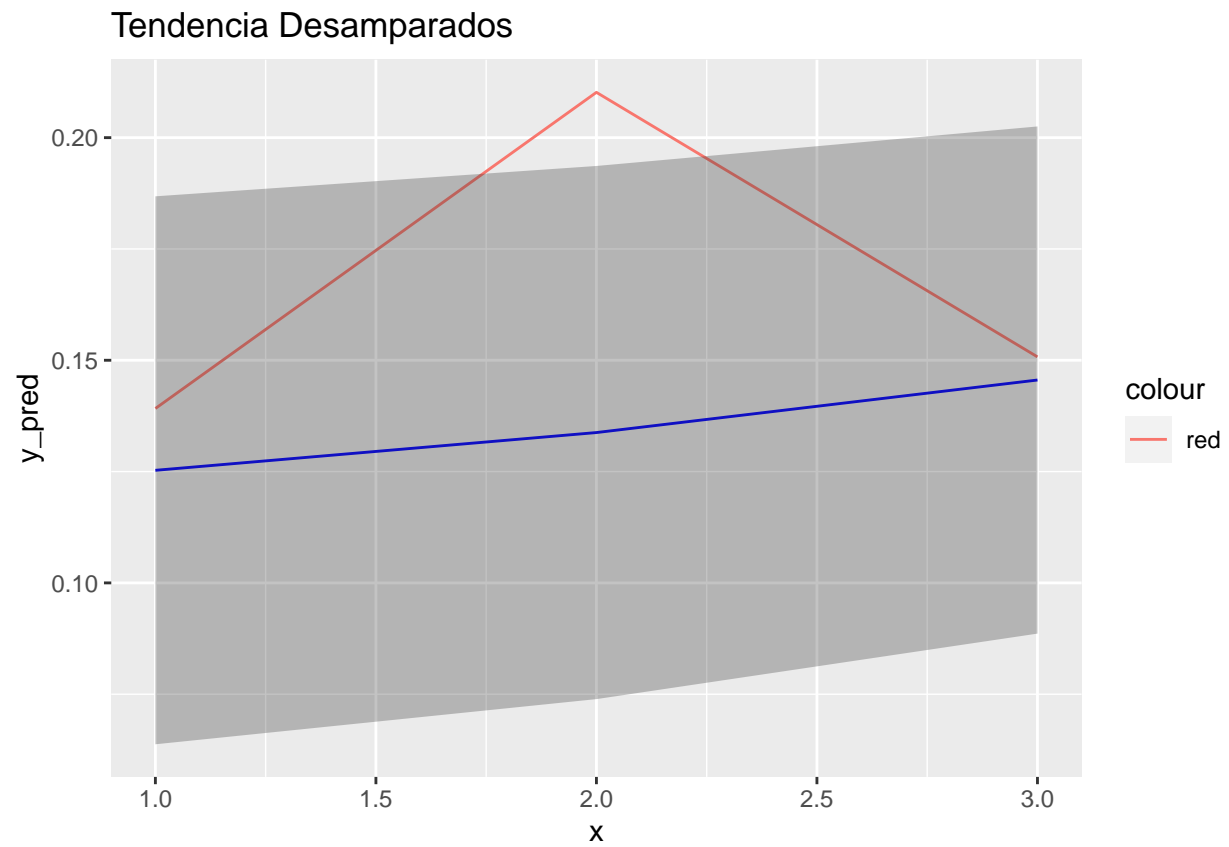


```
##  
## [[6]]
```

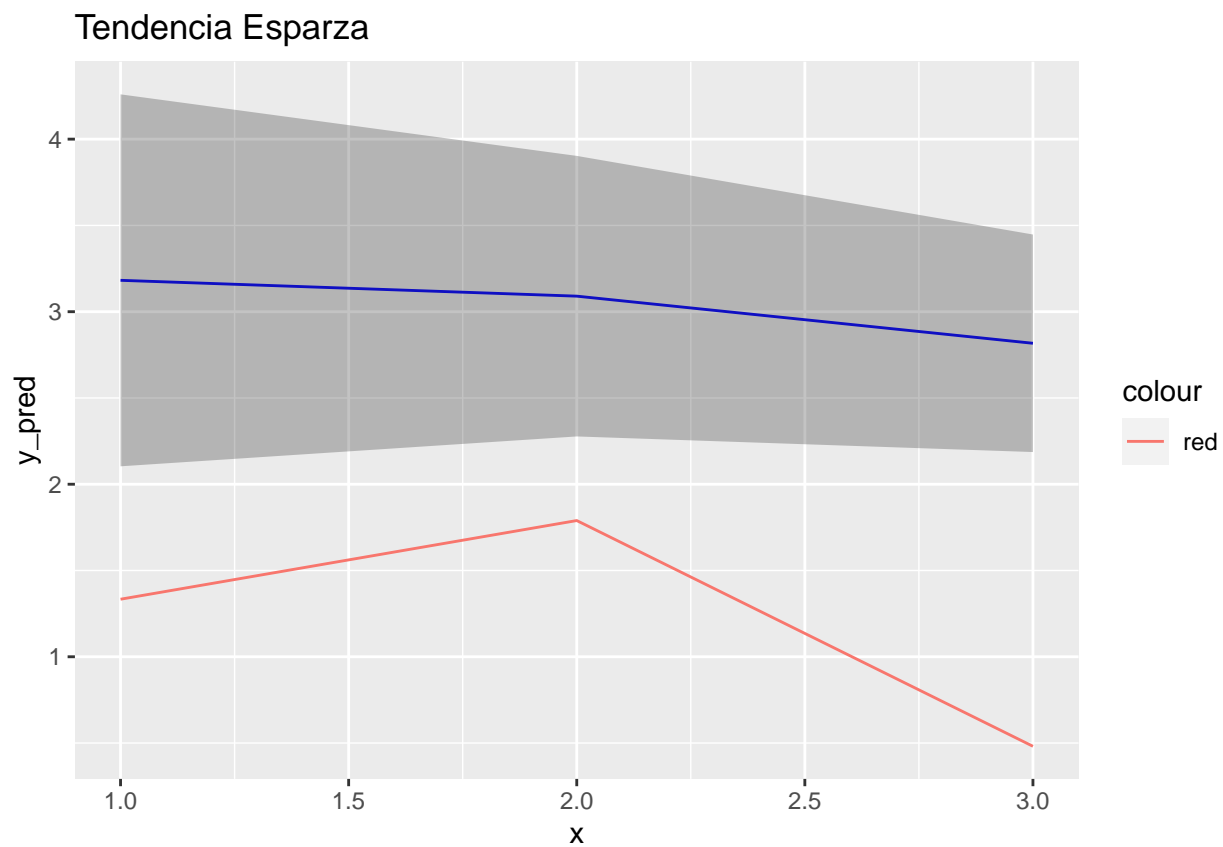
Tendencia Corredores



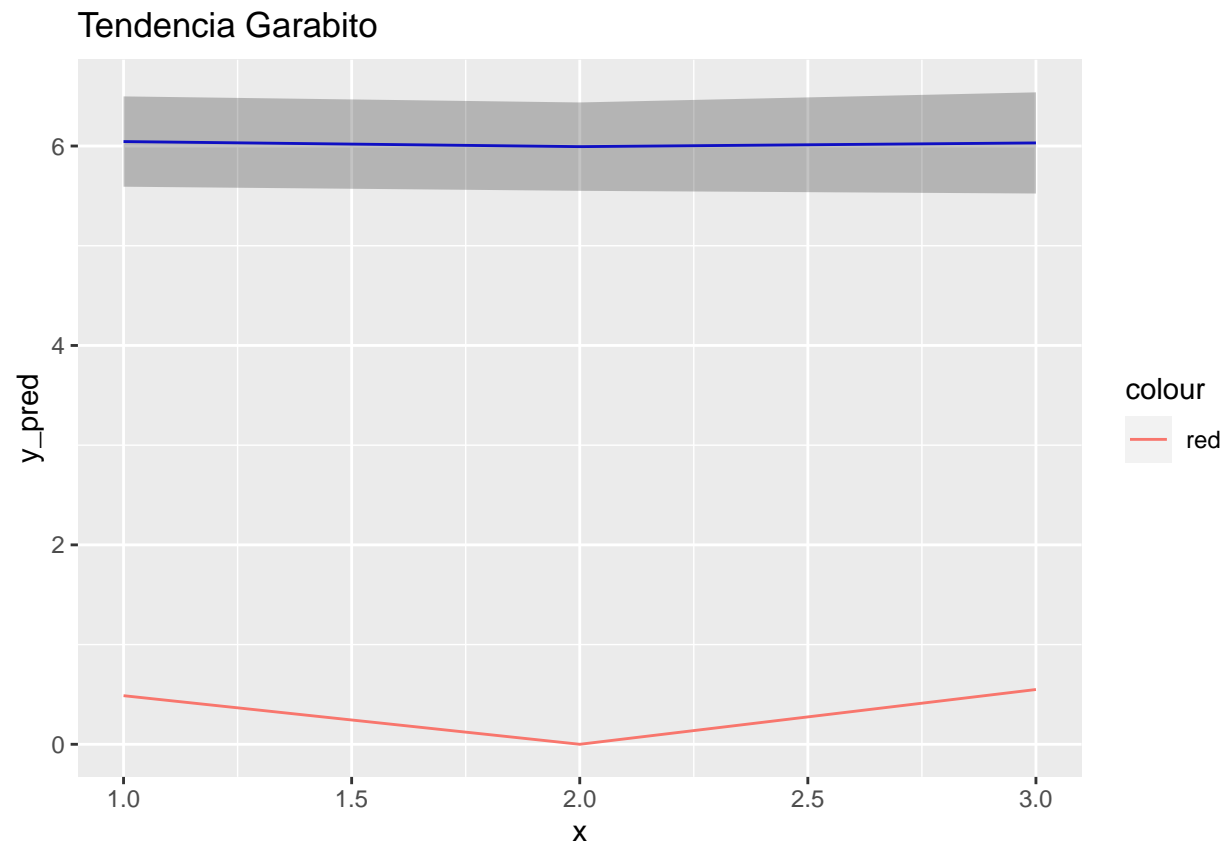
```
##  
## [[7]]
```



```
##  
## [[8]]
```

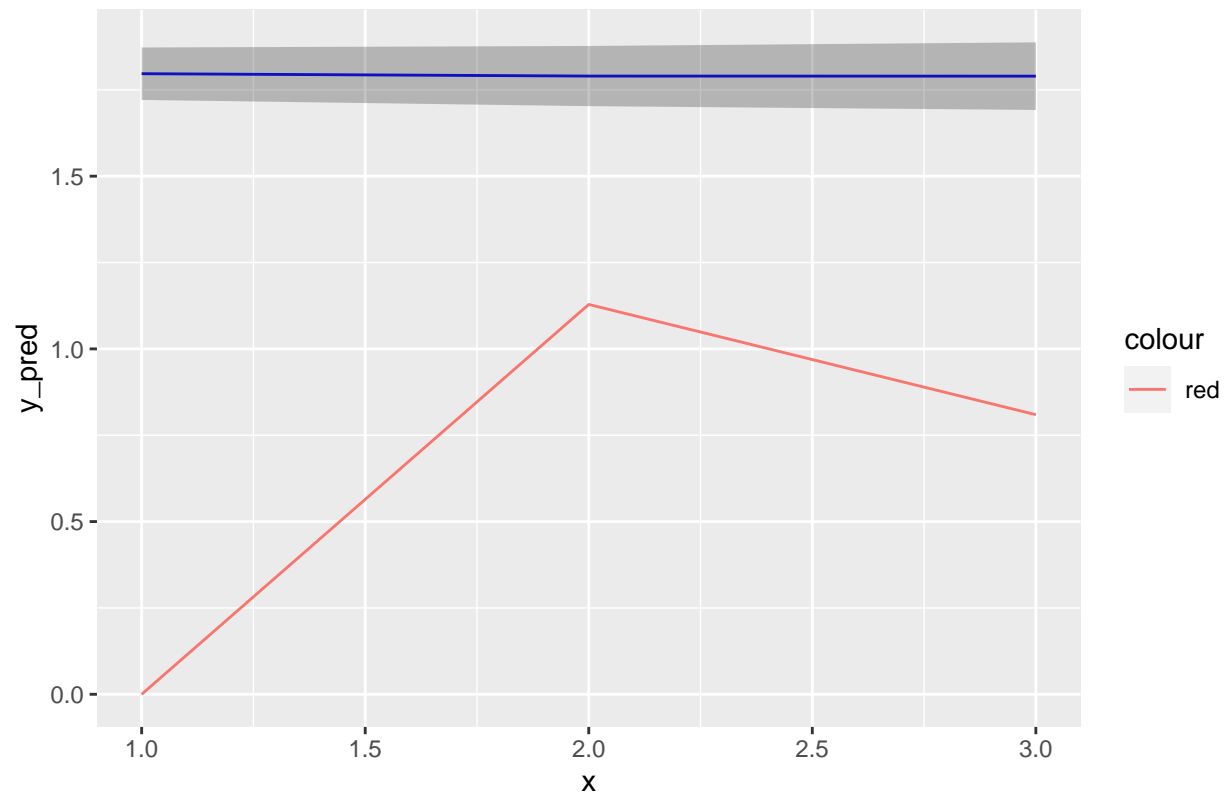


```
##  
## [[9]]
```

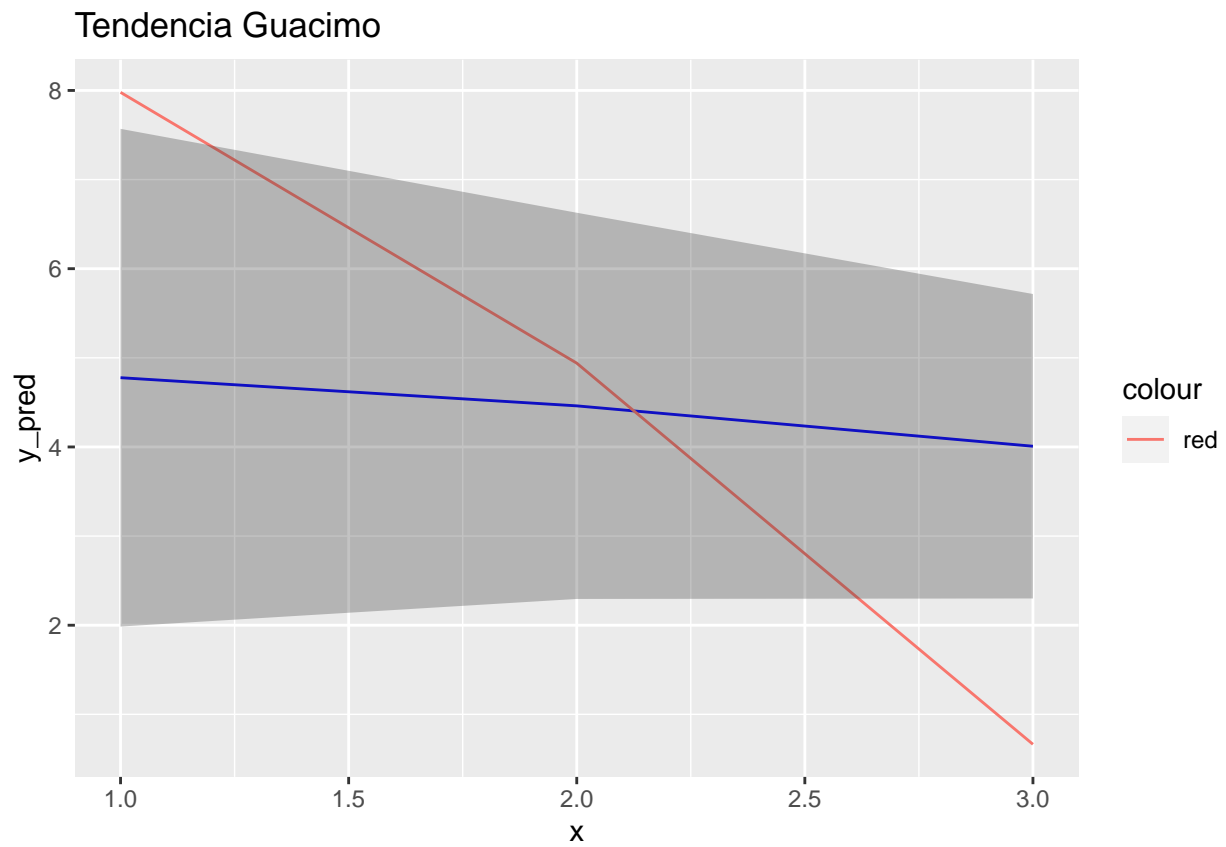


```
##  
## [[10]]
```

Tendencia Golfito

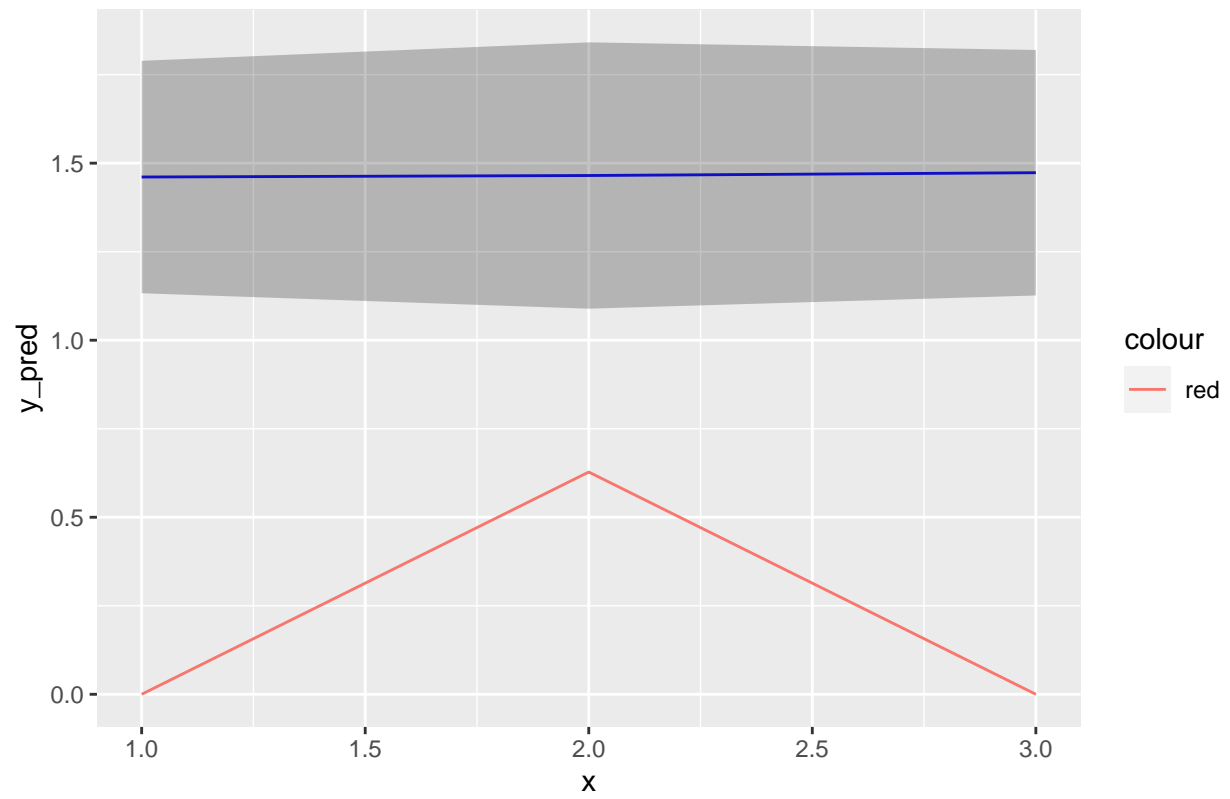


```
##  
## [[11]]
```

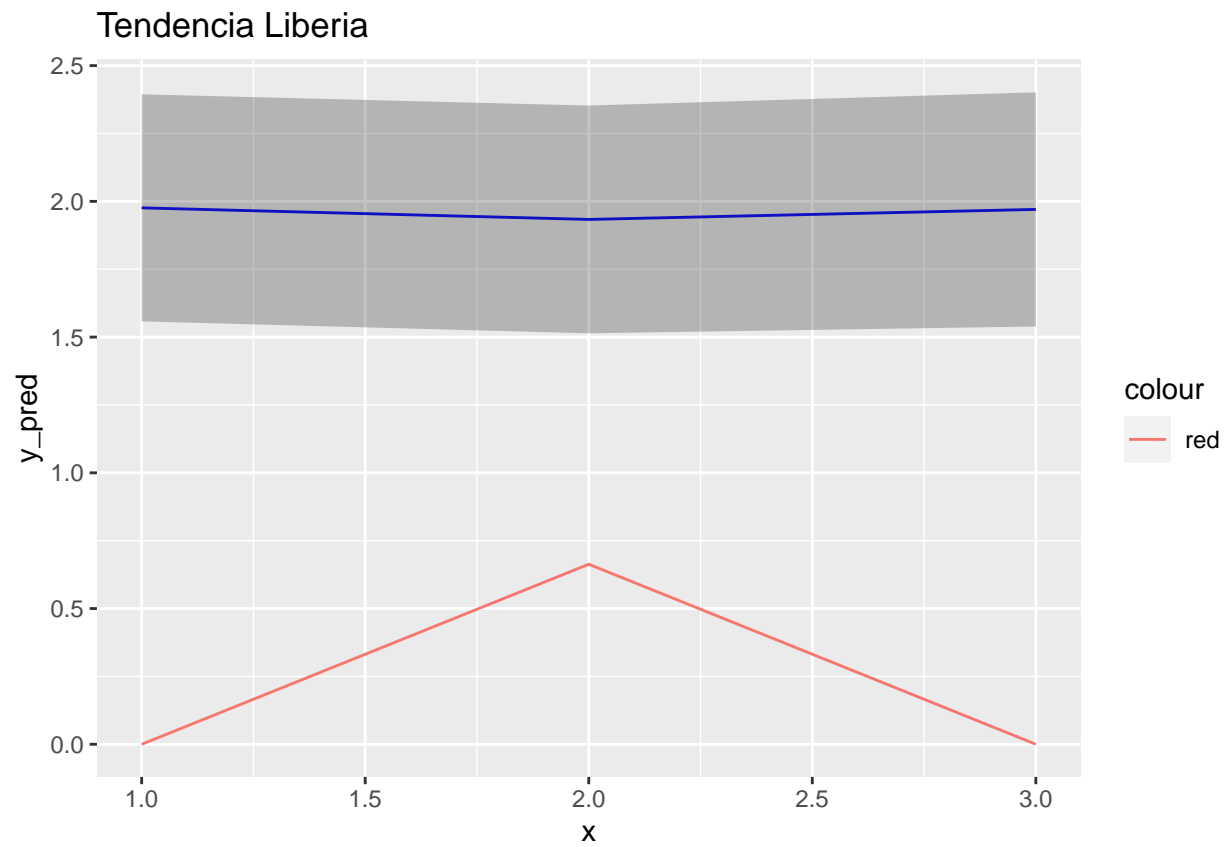


```
##  
## [[12]]
```

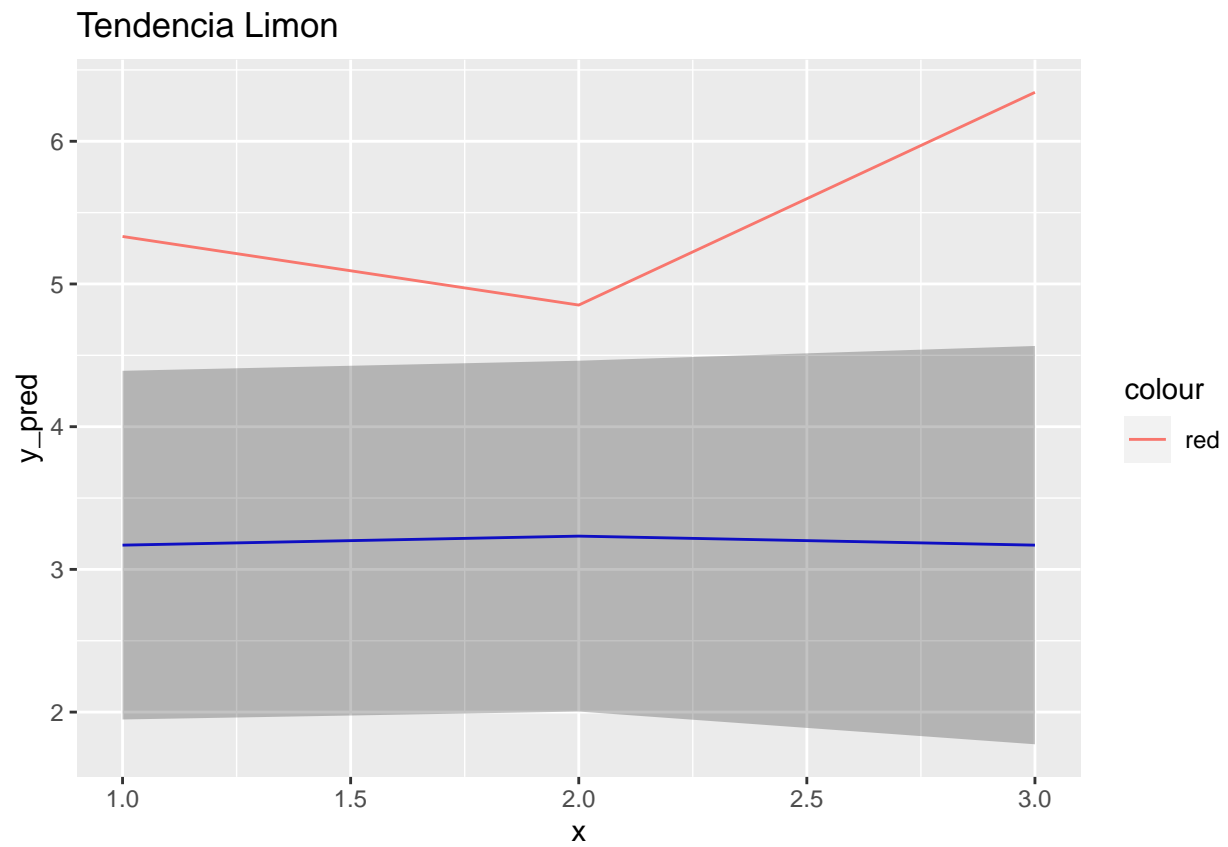
Tendencia La Cruz



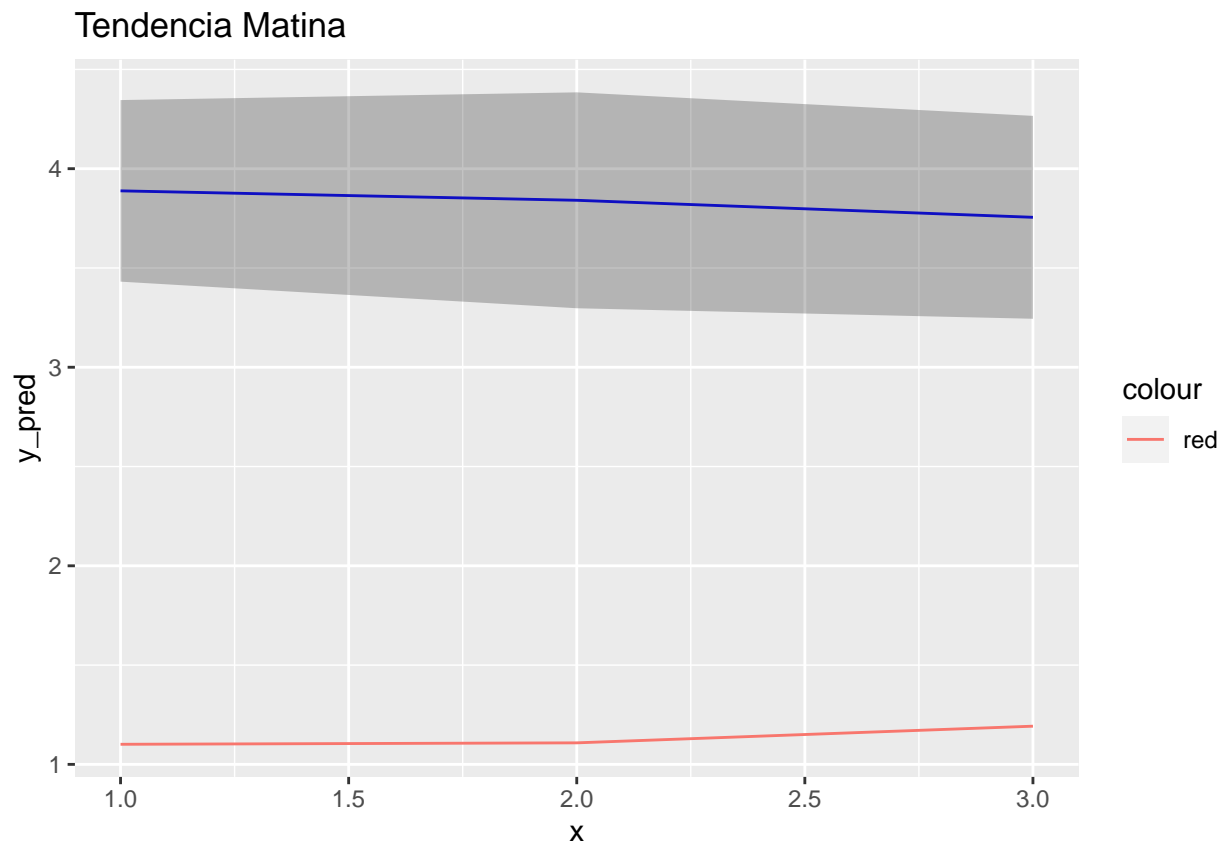
```
##  
## [[13]]
```

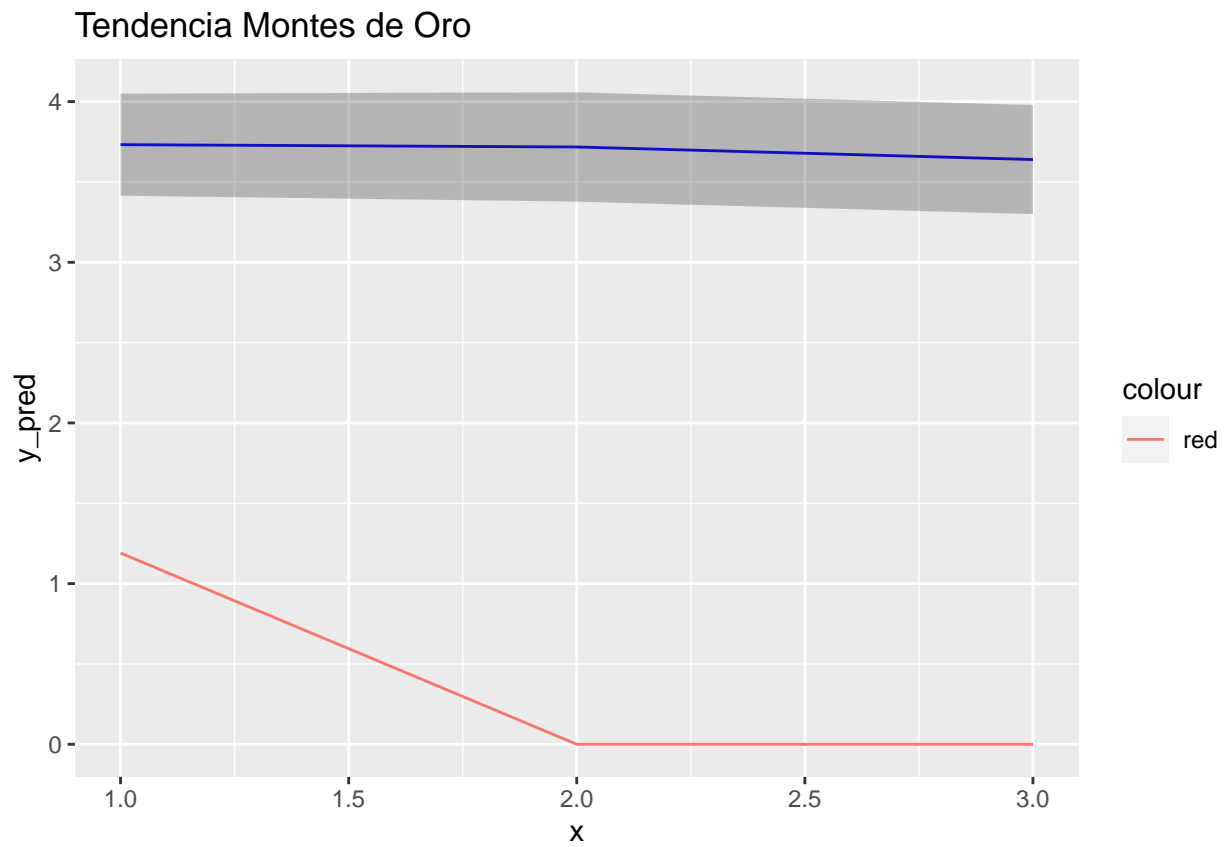
```
##  
## [[14]]
```



```
##  
## [[15]]
```

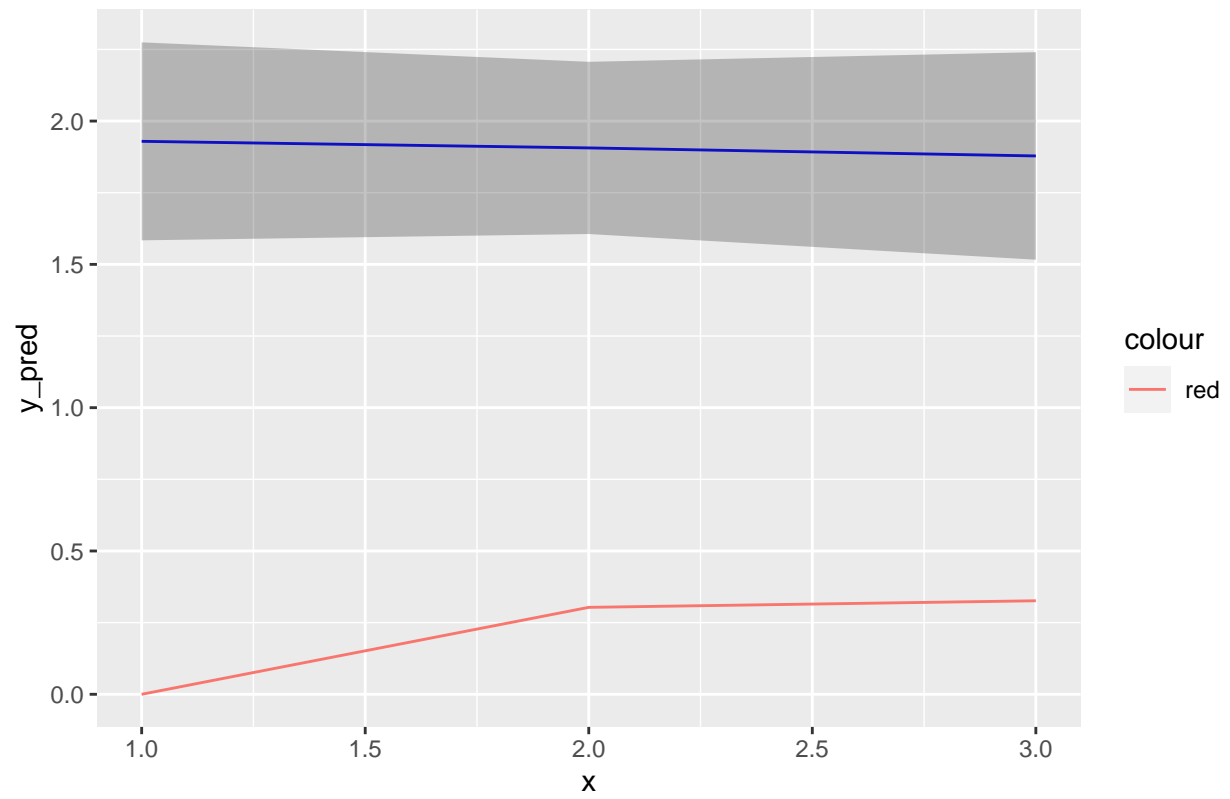


```
##  
## [[16]]
```



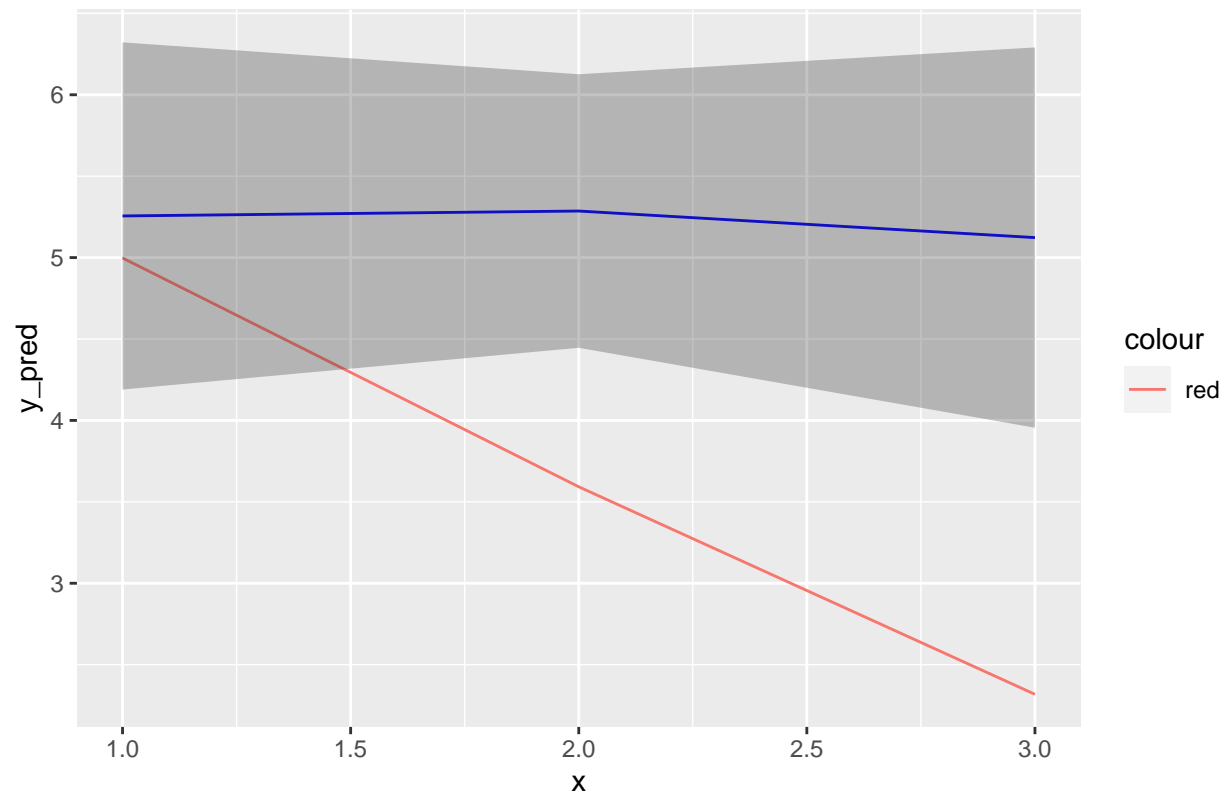
```
##  
## [[17]]
```

Tendencia Nicoya

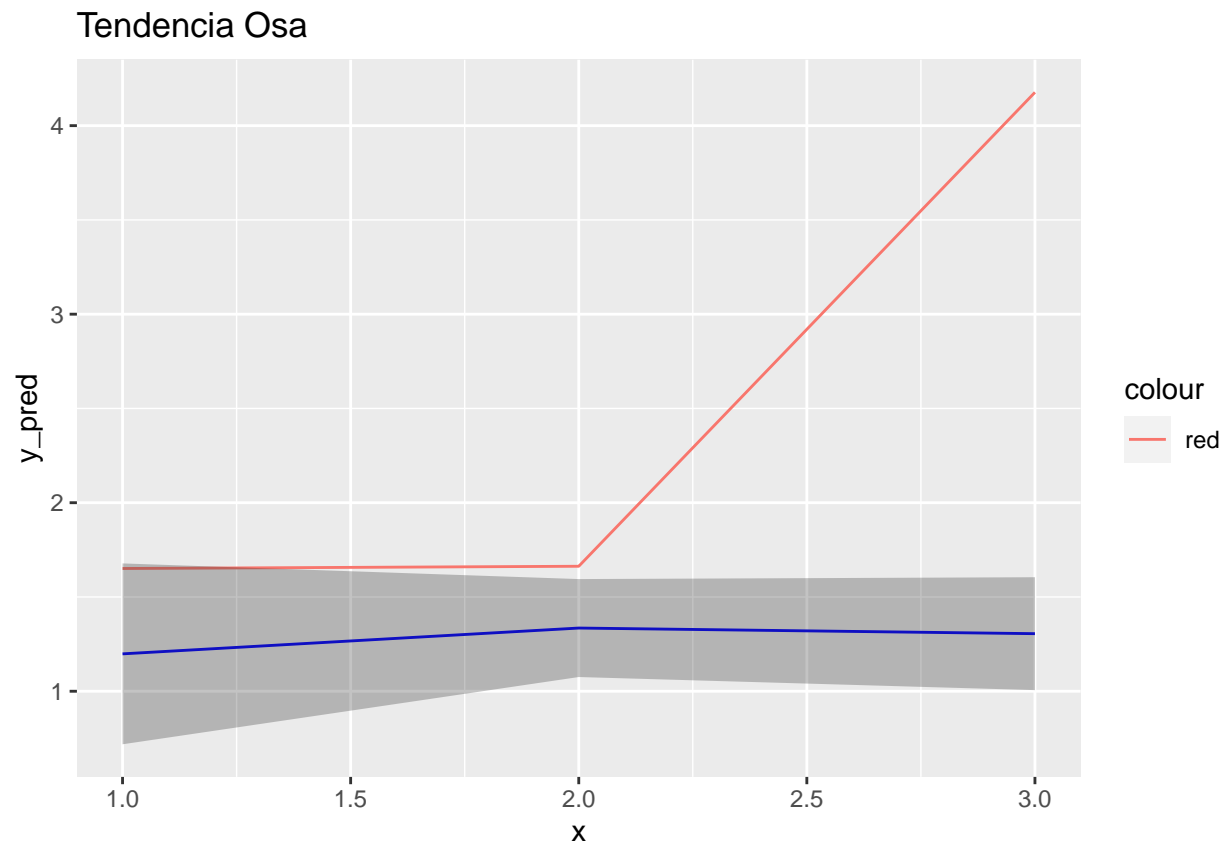


```
##  
## [[18]]
```

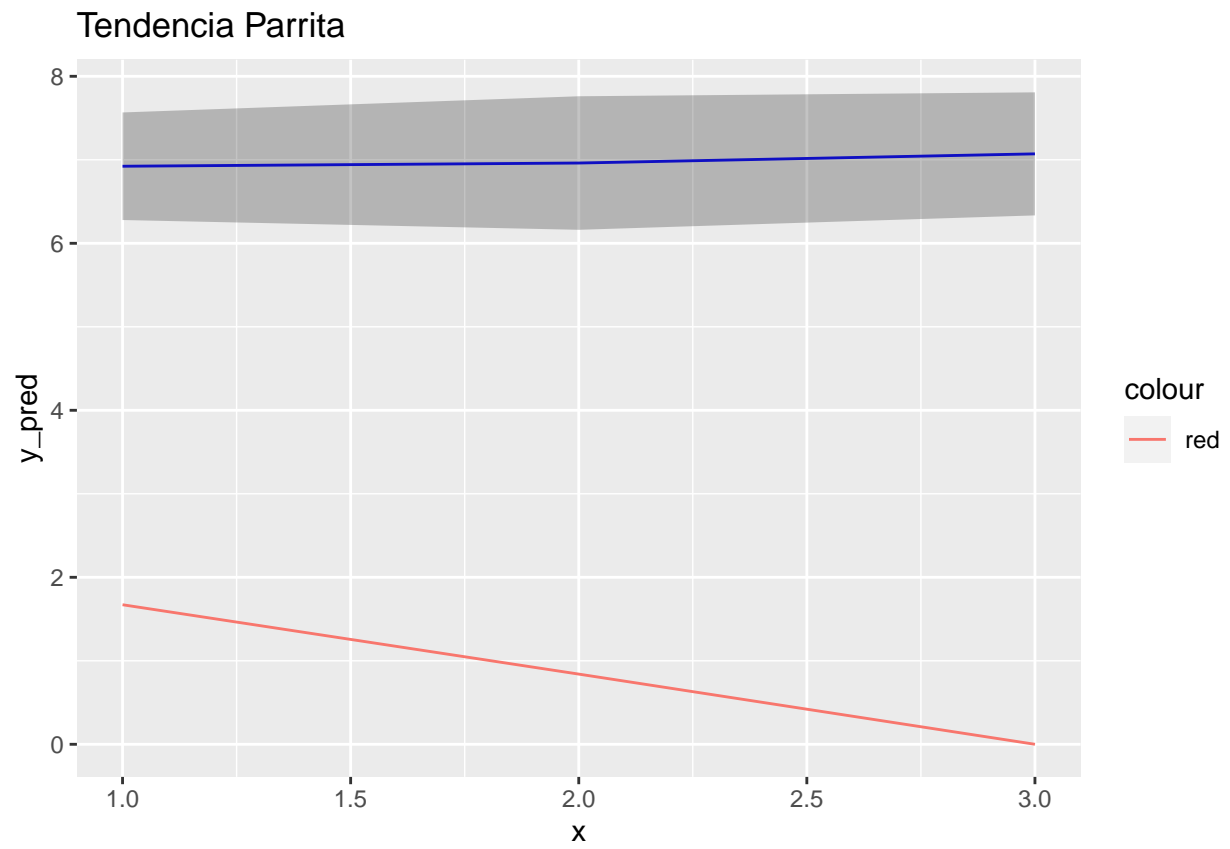
Tendencia Orotina



```
##  
## [[19]]
```

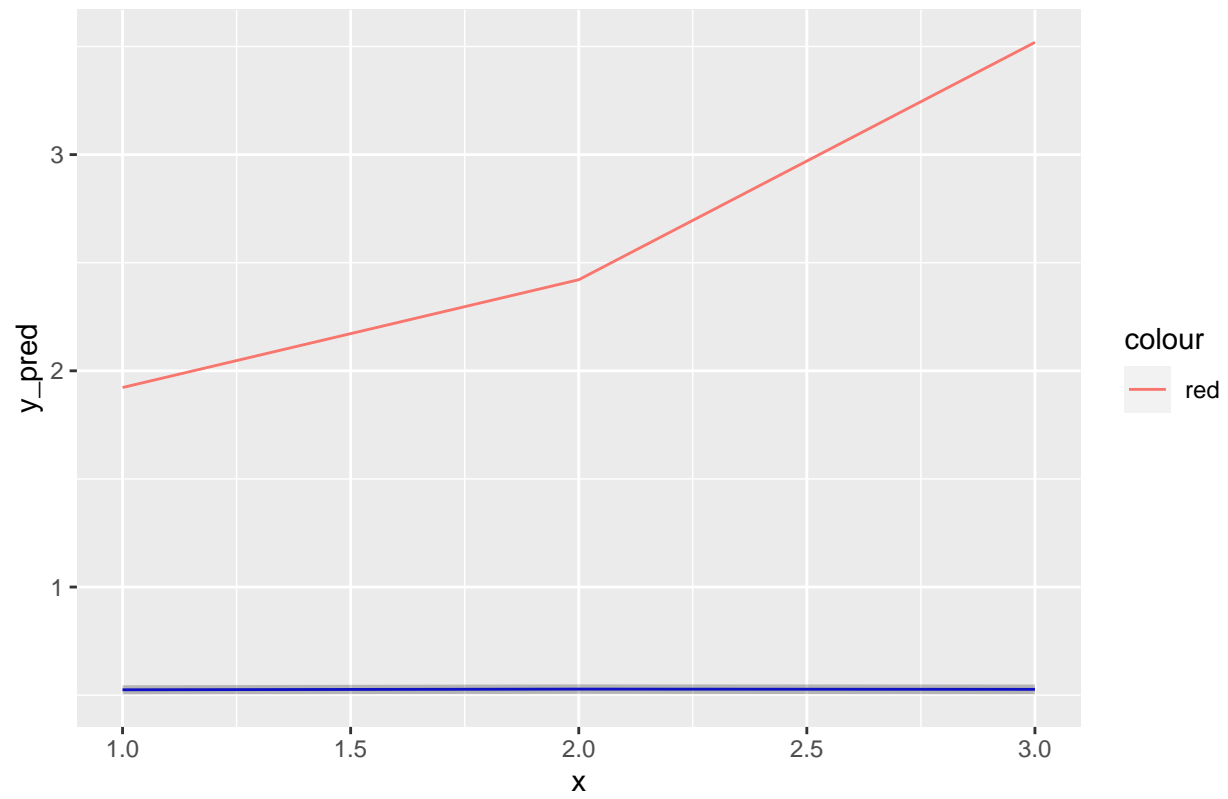


```
##  
## [[20]]
```

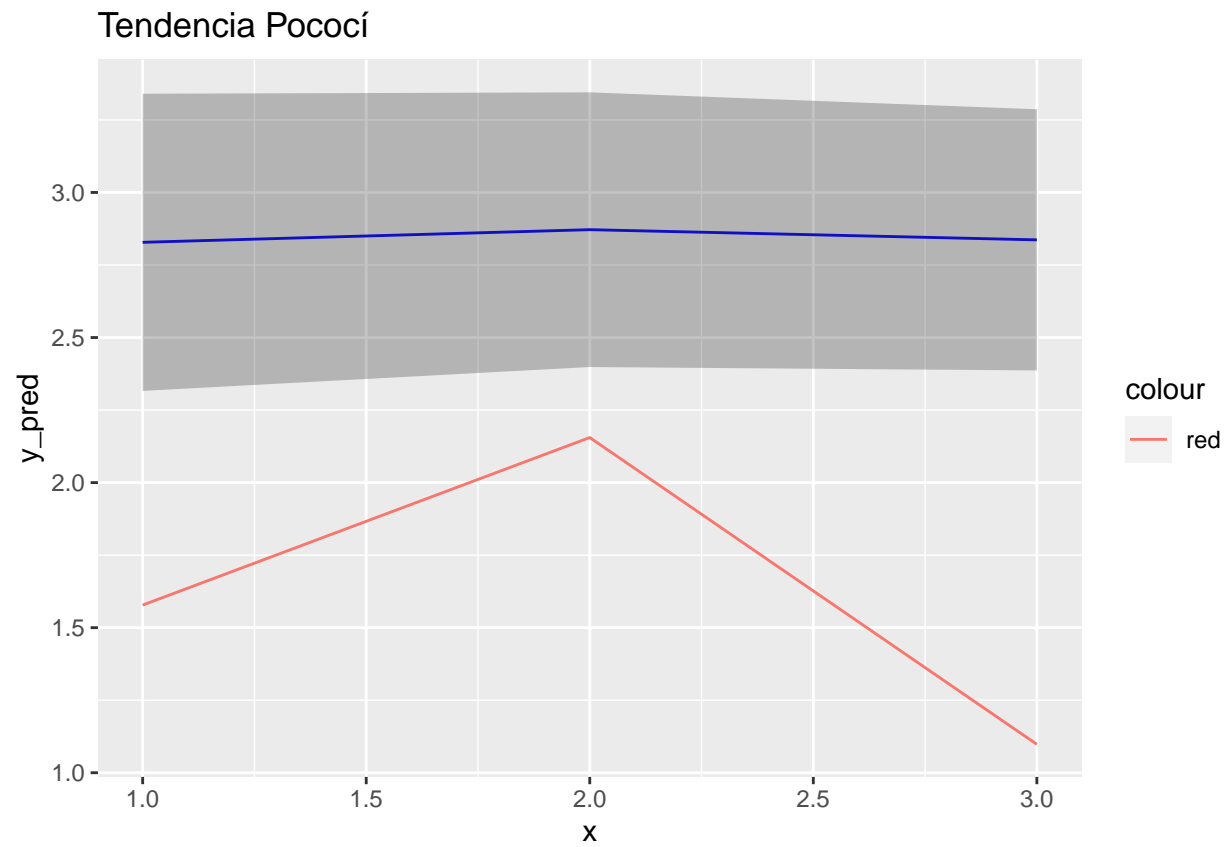


```
##  
## [[21]]
```


Tendencia Perez Zeledón

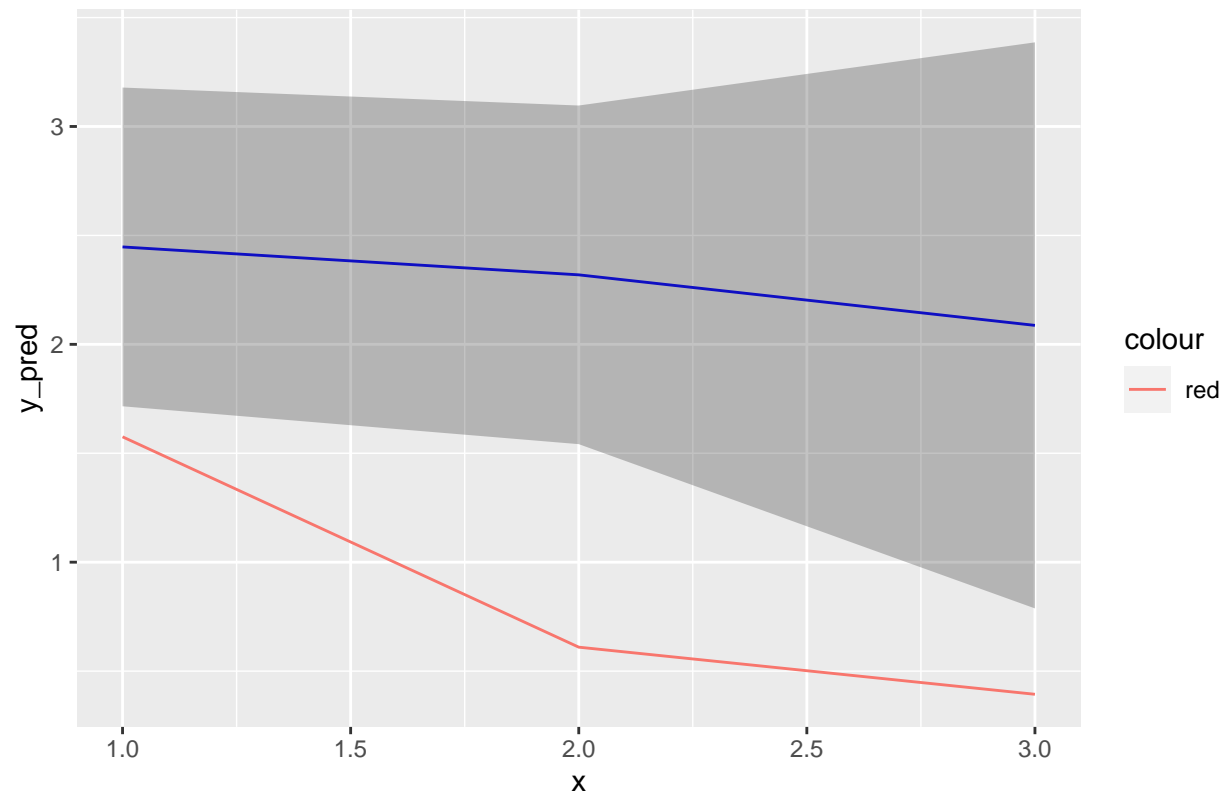


```
##  
## [[22]]
```

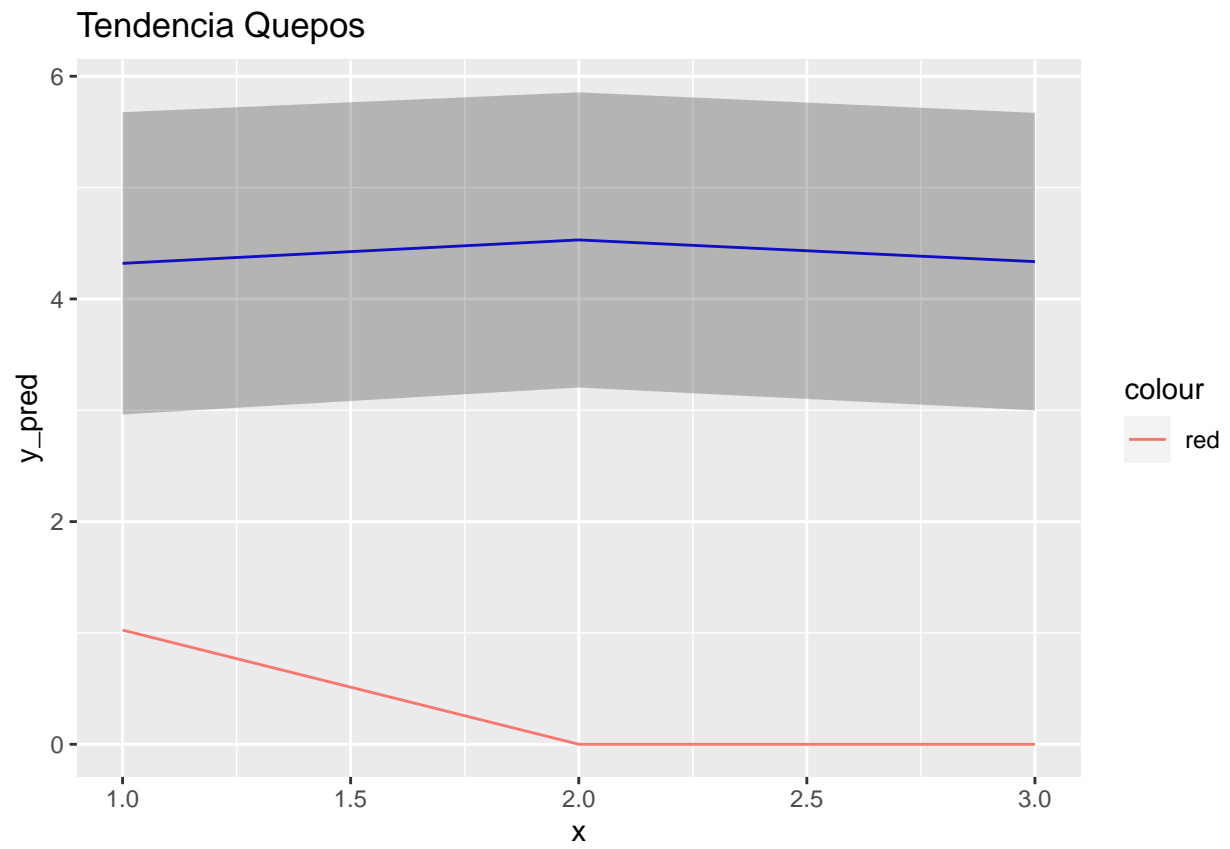


```
##  
## [[23]]
```

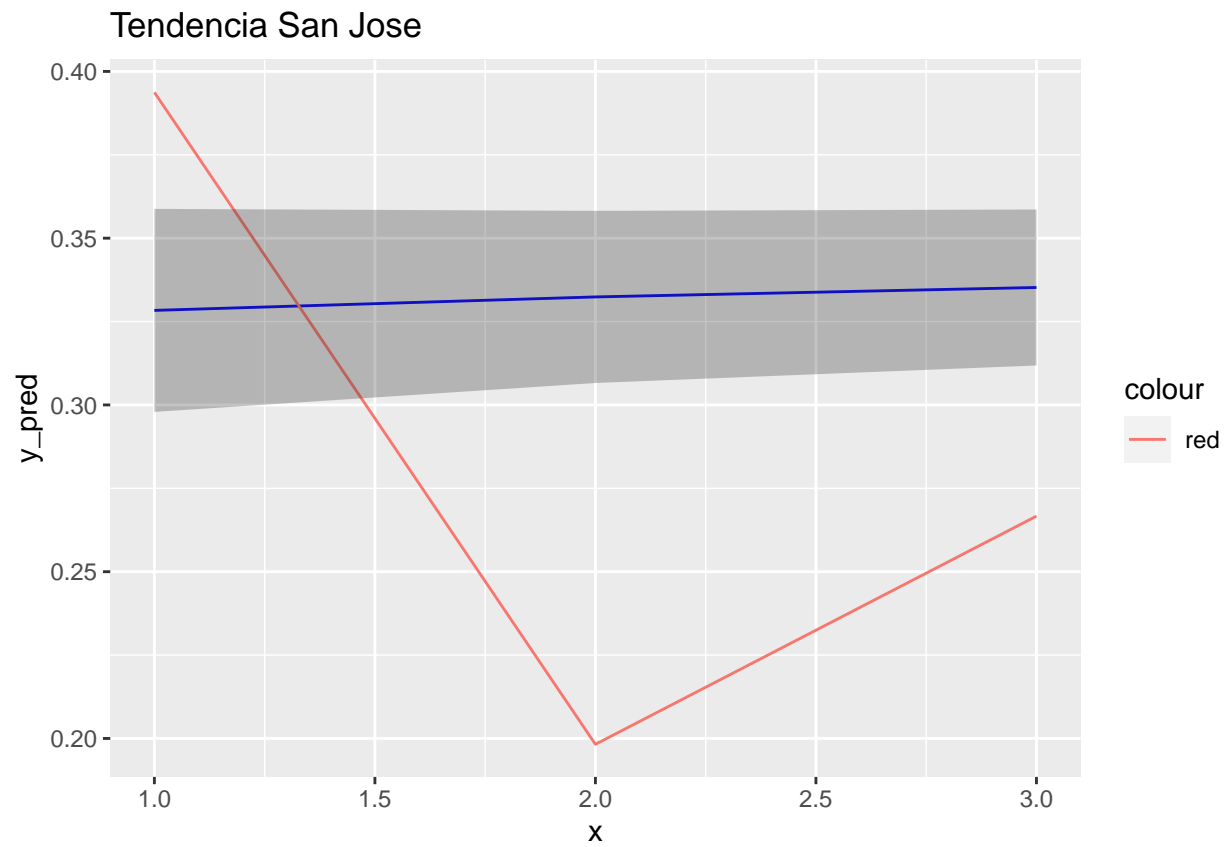
Tendencia Puntarenas



```
##  
## [[24]]
```

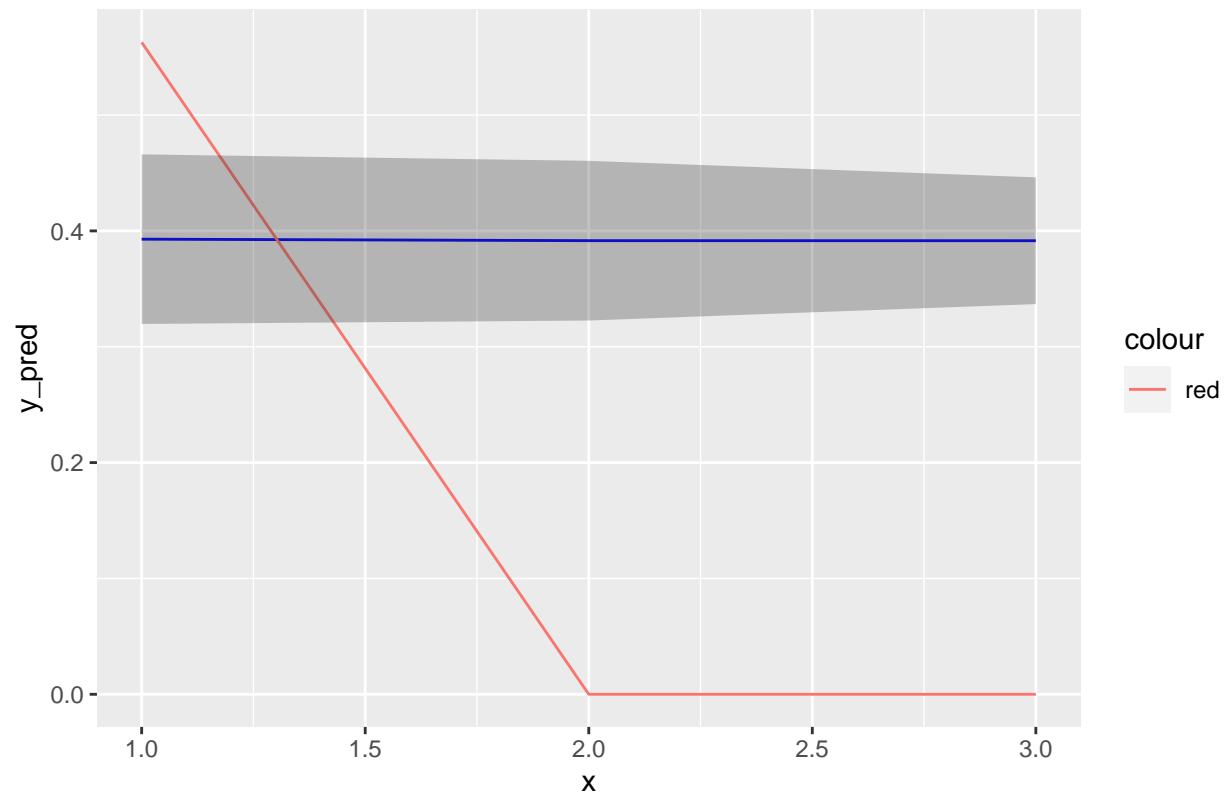


```
##  
## [[25]]
```



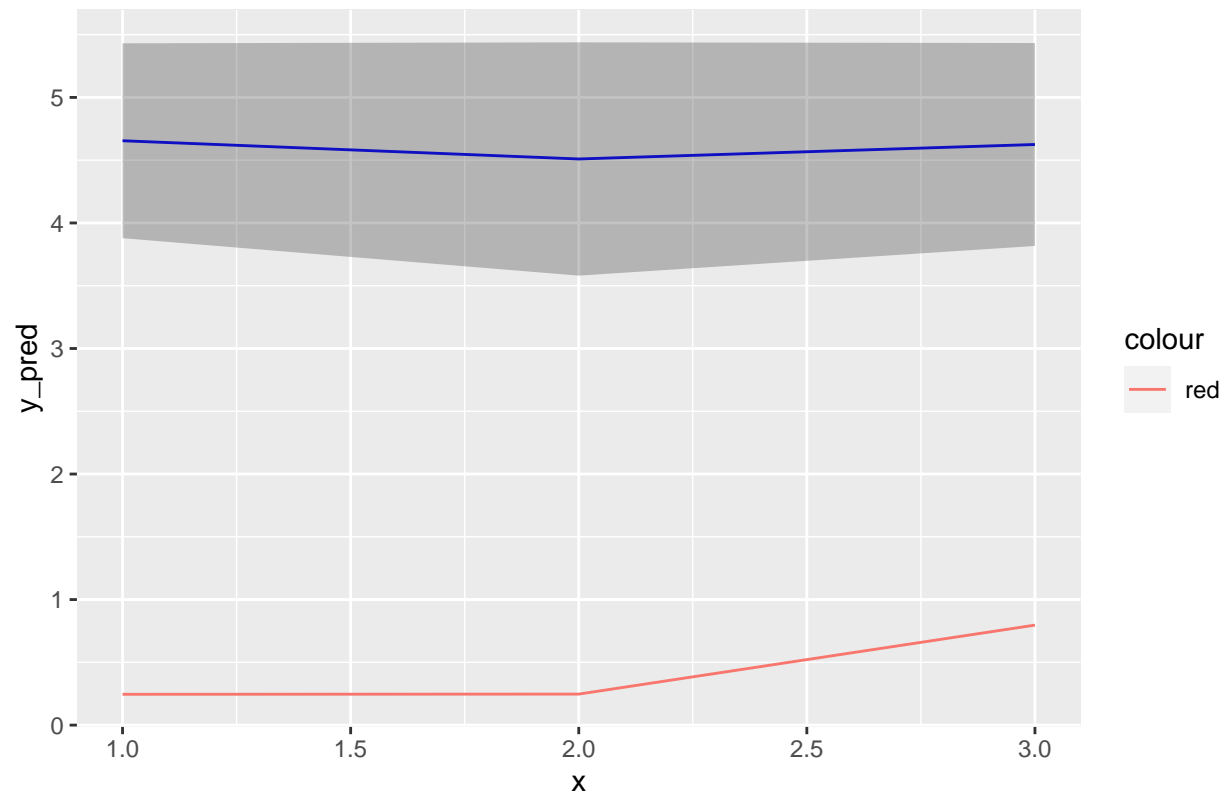
```
##  
## [[26]]
```

Tendencia Santa Ana



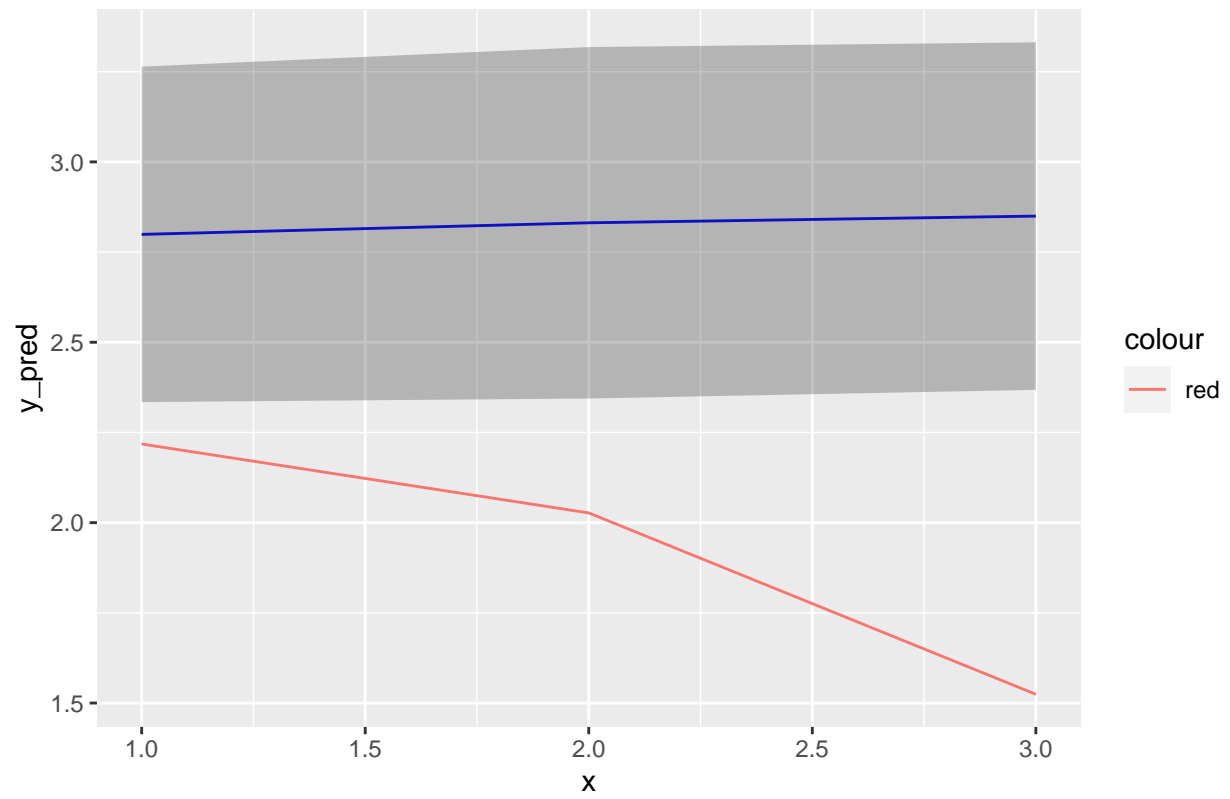
```
##  
## [[27]]
```

Tendencia SantaCruz

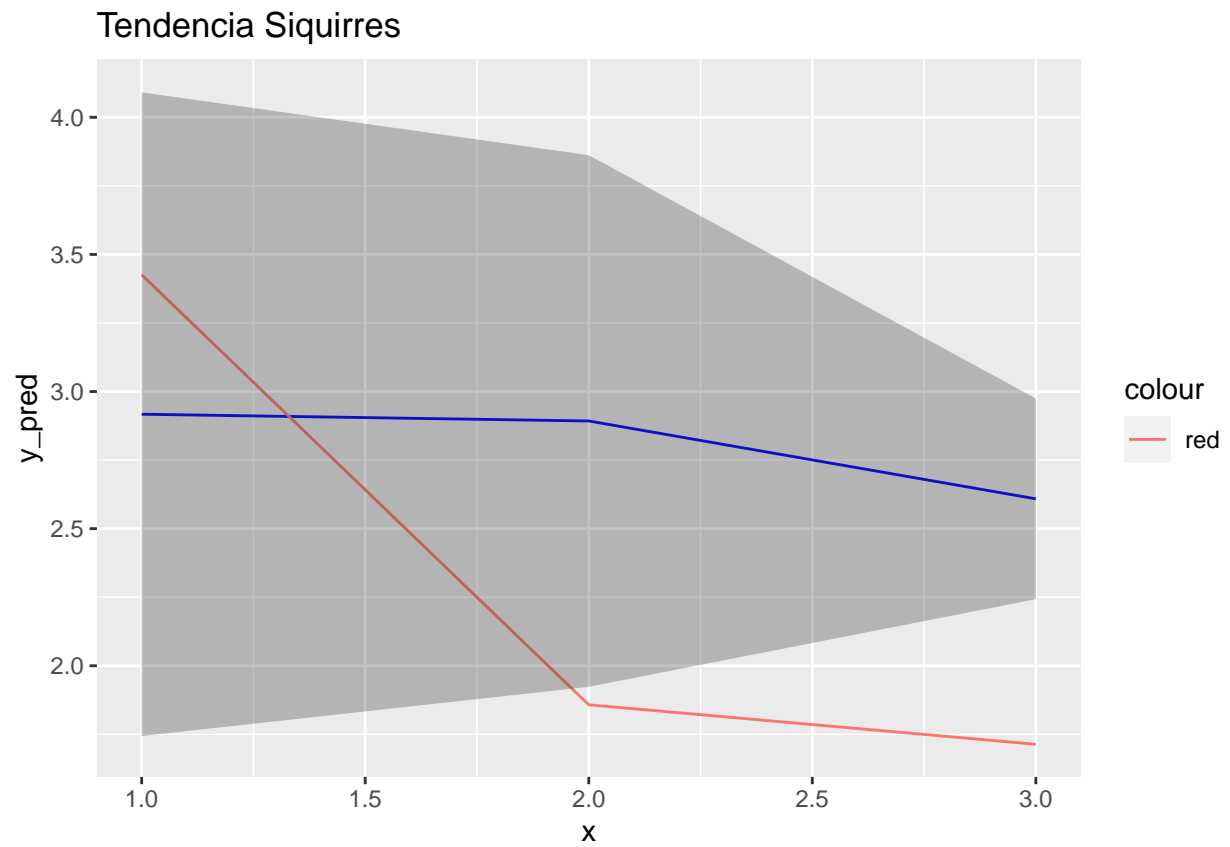


```
##  
## [[28]]
```

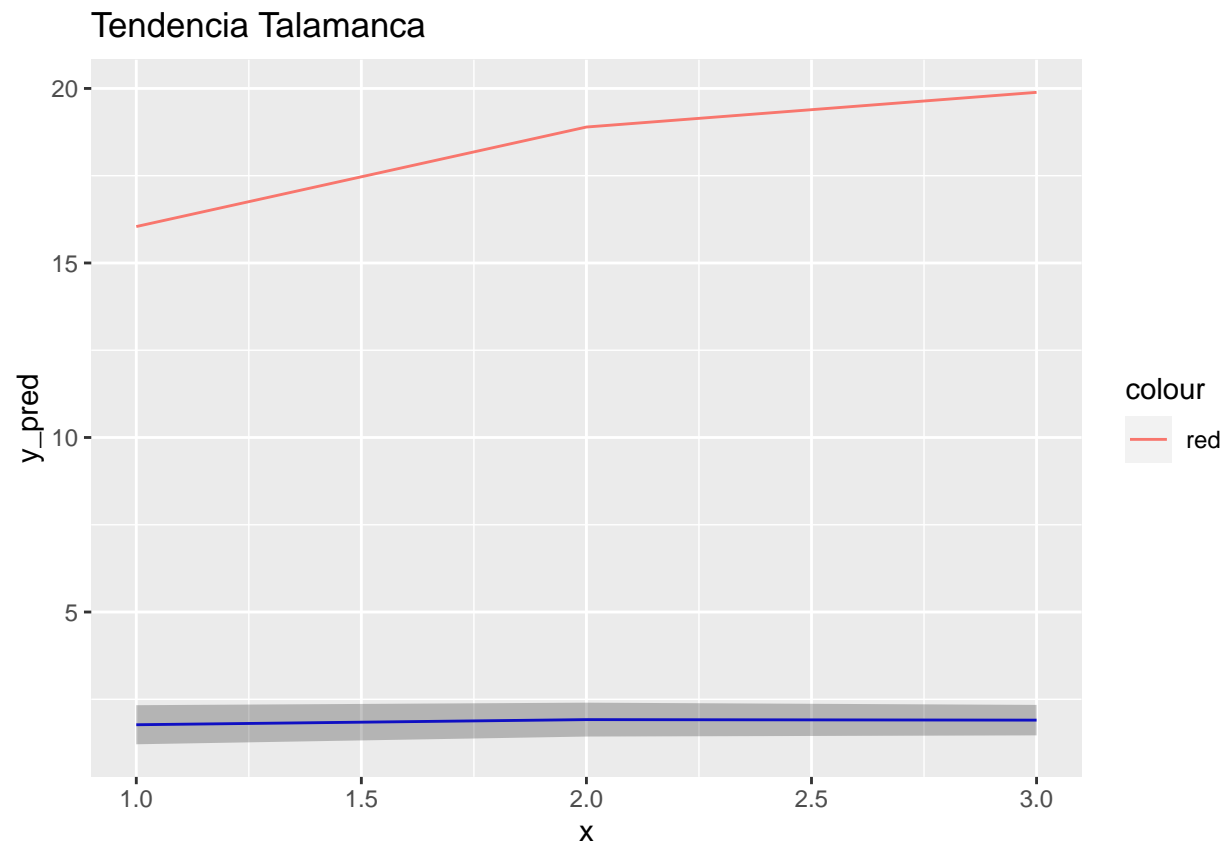
Tendencia Sarapiquí



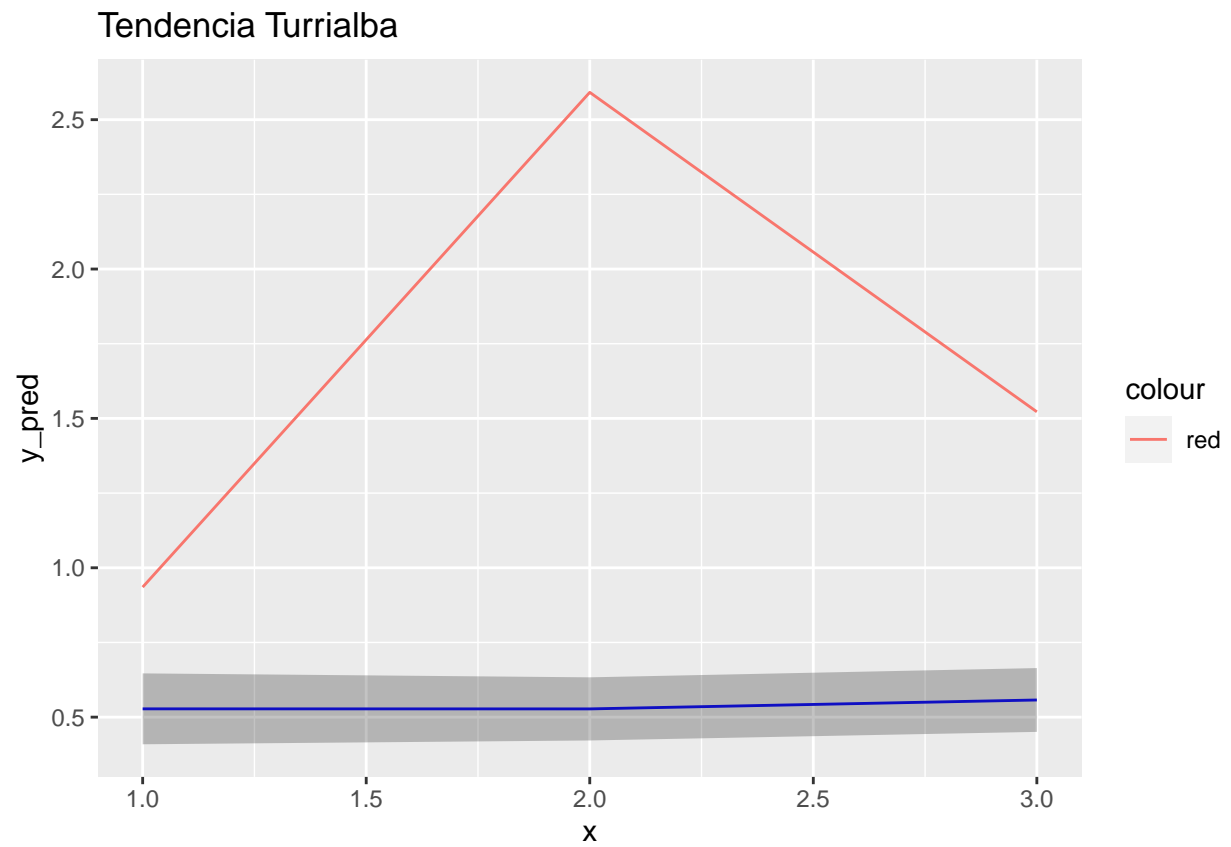
```
##  
## [[29]]
```

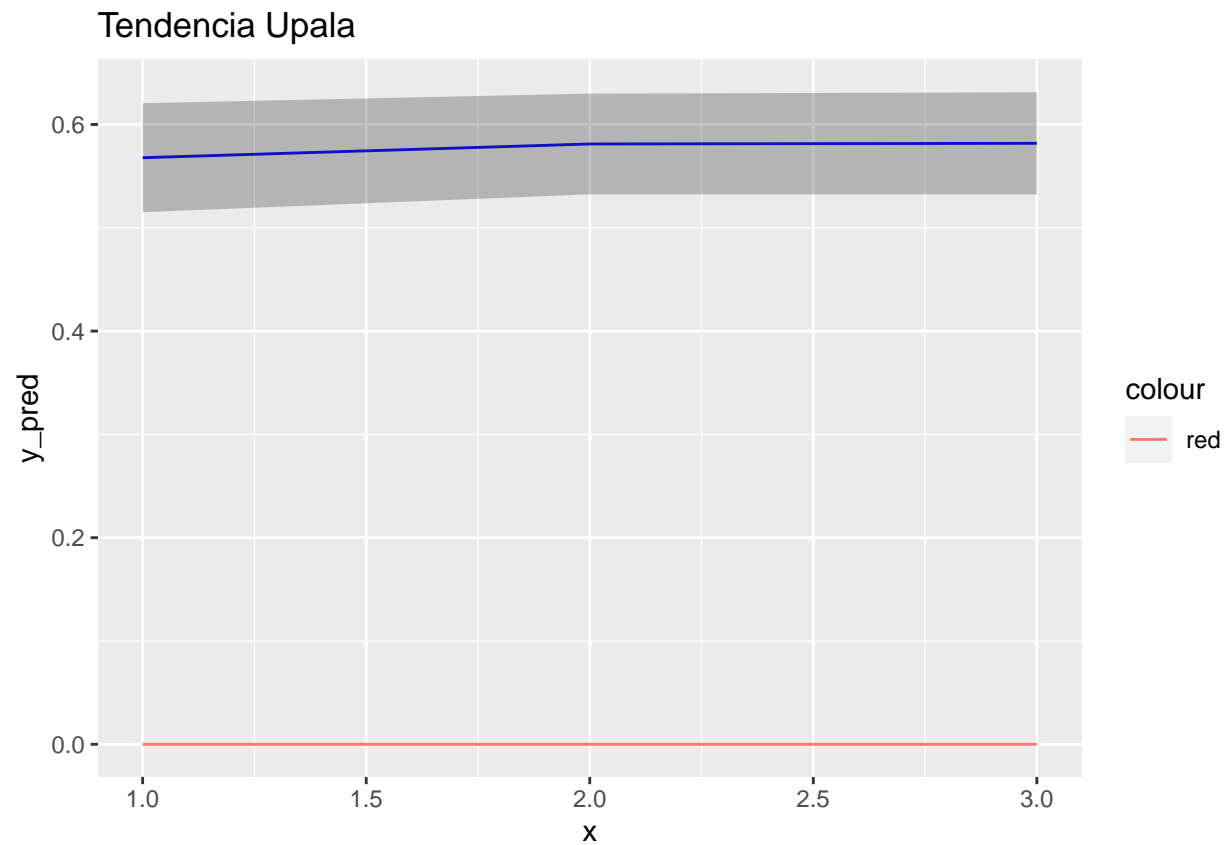
```
##  
## [[30]]
```



```
##  
## [[31]]
```



```
##  
## [[32]]
```



Valores aproximados dentro del modelo

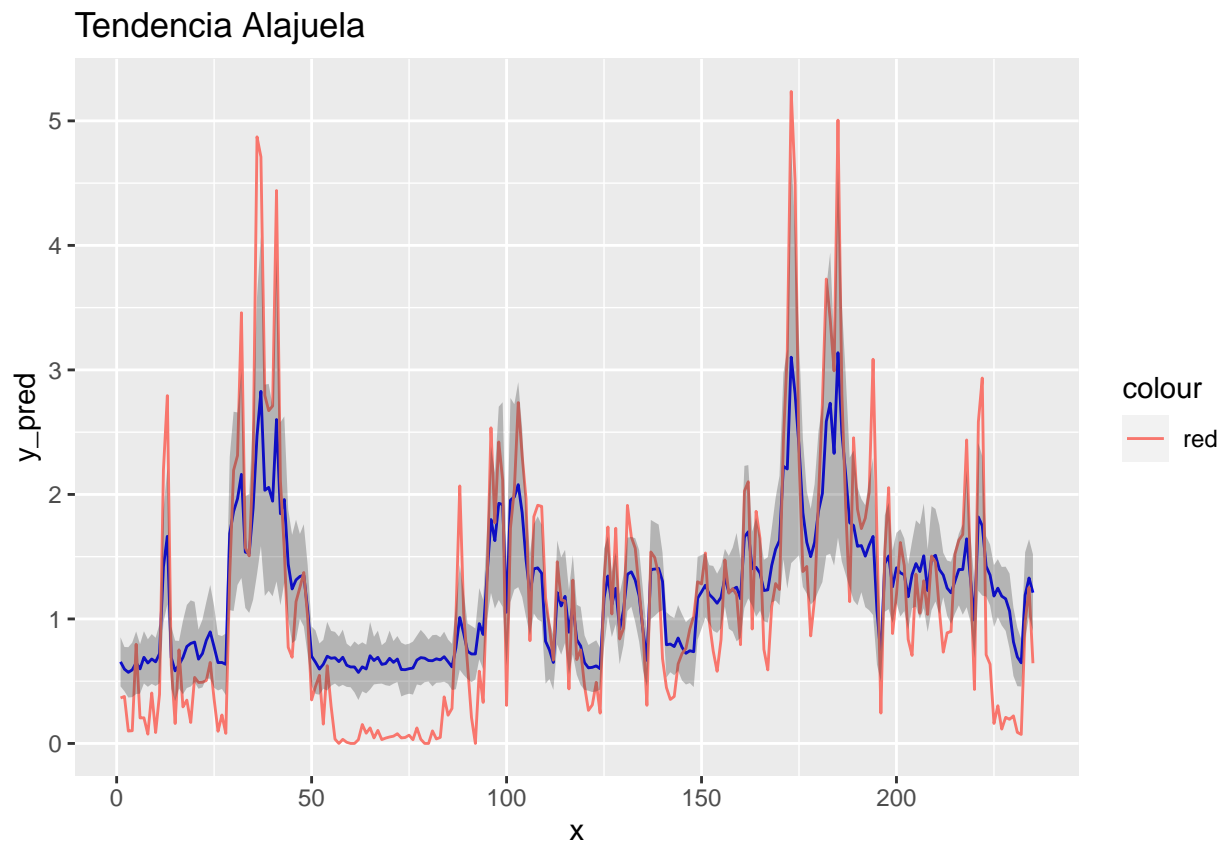
Evaluacion_c

```
##           [,1]      [,2]
## [1,] 0.2899243  6.336410
## [2,] 0.1813619 19.050655
## [3,] 1.7255596  6.675219
## [4,] 1.8958163  7.522802
## [5,] 2.6655264 11.338539
## [6,] 2.0497242  9.302687
## [7,] 0.1076688  7.695768
## [8,] 2.6457528 13.860206
## [9,] 10.8421340 34.949097
## [10,] 4.3718985 38.283779
## [11,] 1.1330518  5.475617
## [12,] 6.5355781 31.057102
## [13,] 3.9604497 32.579141
## [14,] 2.8038554 19.099305
## [15,] 4.0965862 23.858428
## [16,] 5.6003805 31.238513
## [17,] 2.7808634 25.681097
## [18,] 7.1941154 17.314984
## [19,] 4.1884385 25.271802
```

```
## [20,] 52.9163807 47.646329
## [21,]  2.2312385 38.103876
## [22,]  1.7547487 11.751129
## [23,]  1.4211853 11.730373
## [24,] 12.7761314 21.242980
## [25,]  0.2431911 23.236959
## [26,]  0.8458298 28.842565
## [27,] 13.0292622 37.035652
## [28,]  9.9773632 34.243826
## [29,]  2.2199829 16.523835
## [30,]  7.1376112 33.175337
## [31,]  2.6884849 30.789798
## [32,]  1.4040543 33.155706
```

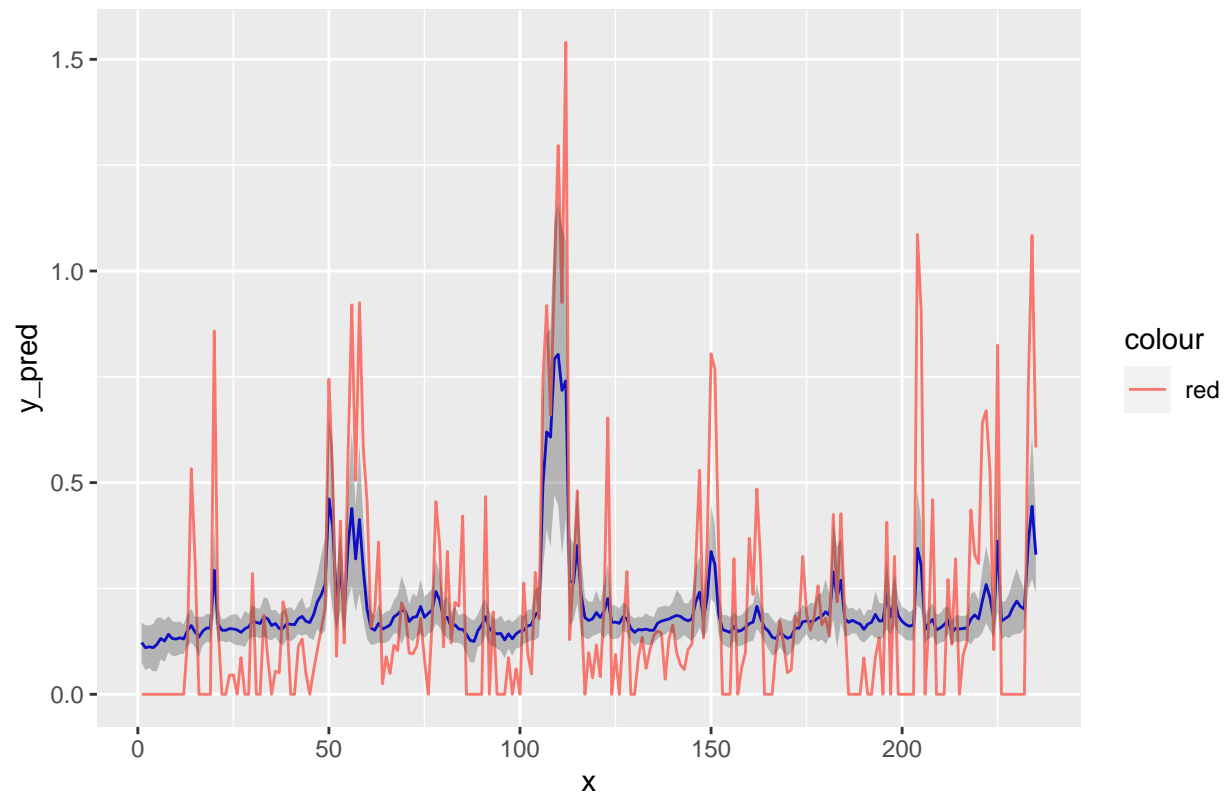
```
plot_list_c
```

```
## [[1]]
```

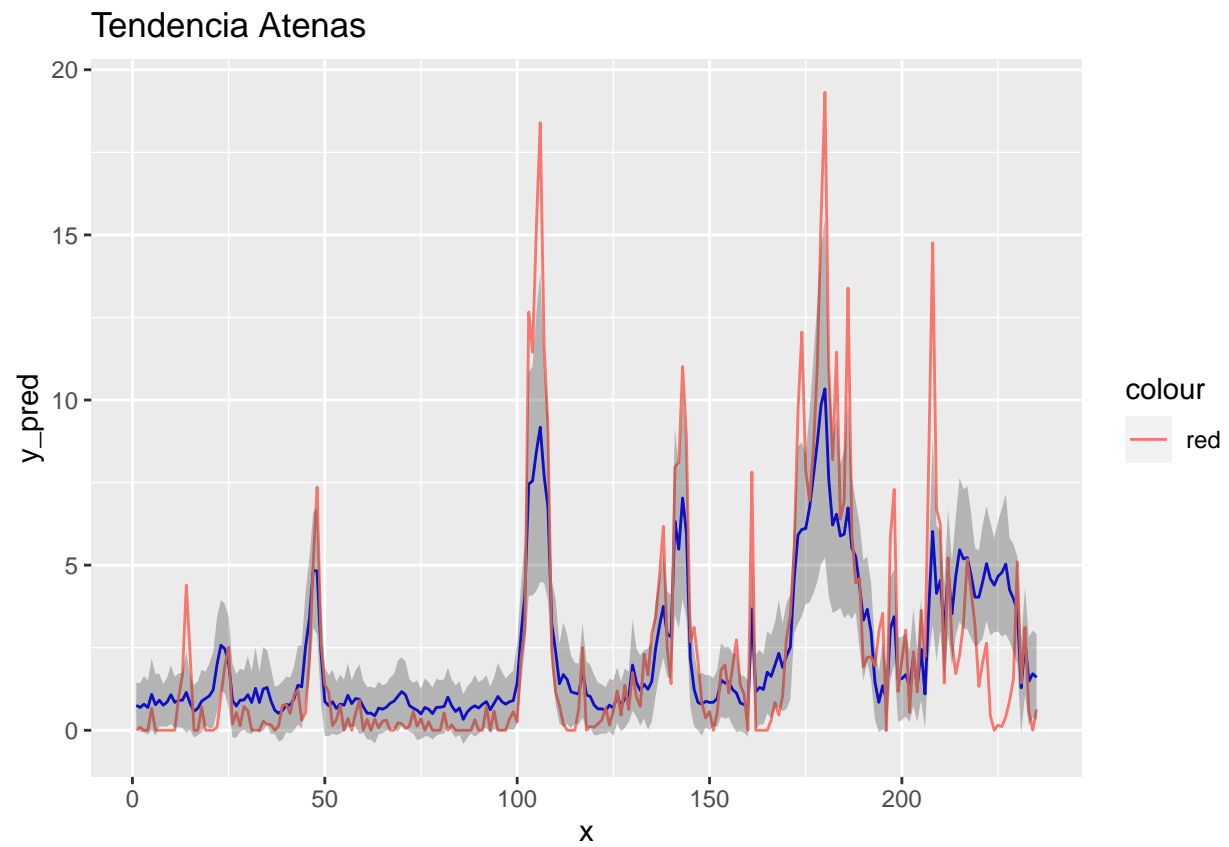


```
##
## [[2]]
```

Tendencia Alajuelita

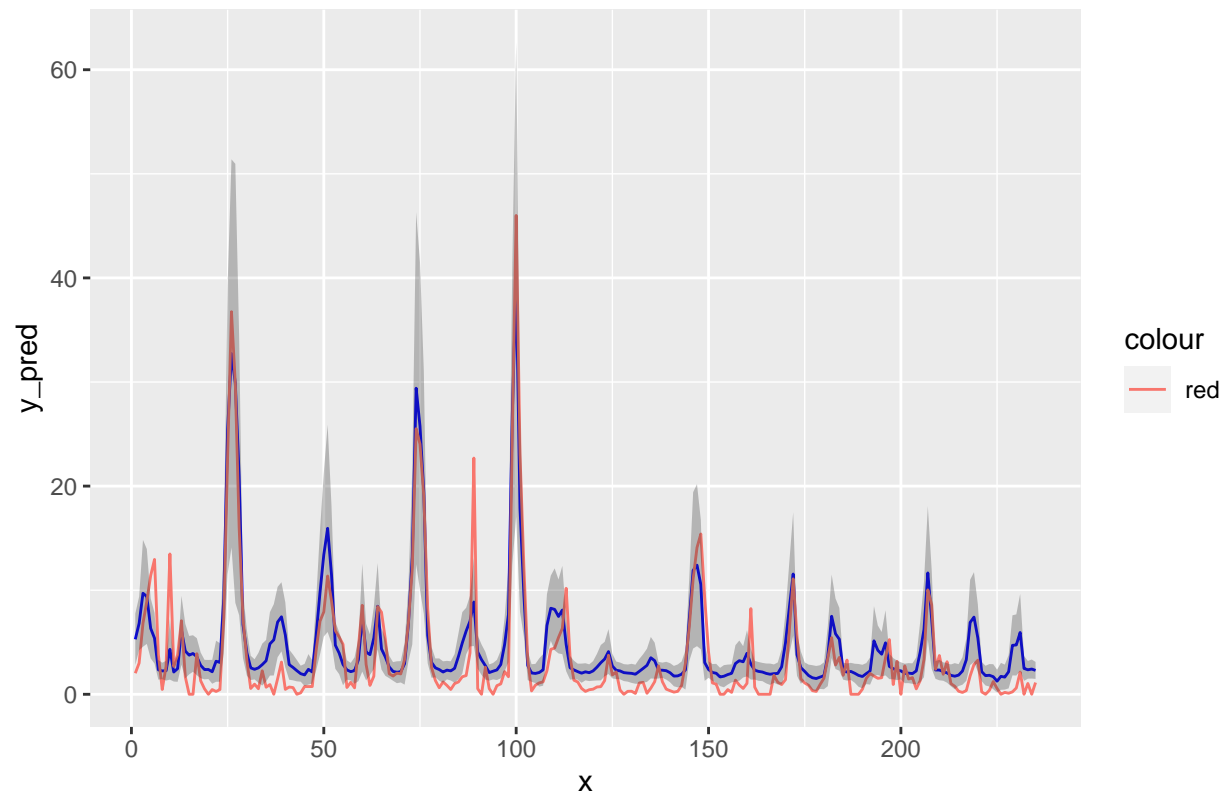


```
##  
## [[3]]
```

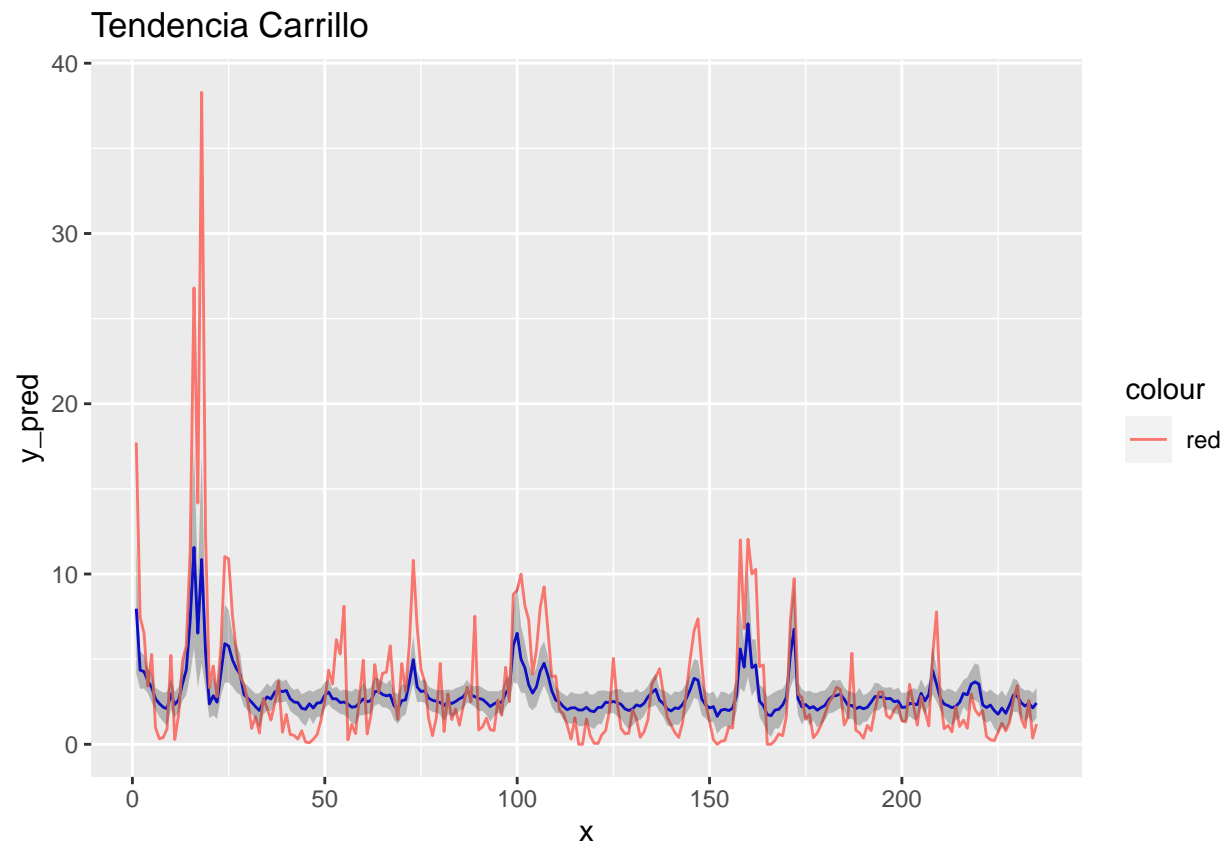


```
##  
## [[4]]
```

Tendencia Cañas

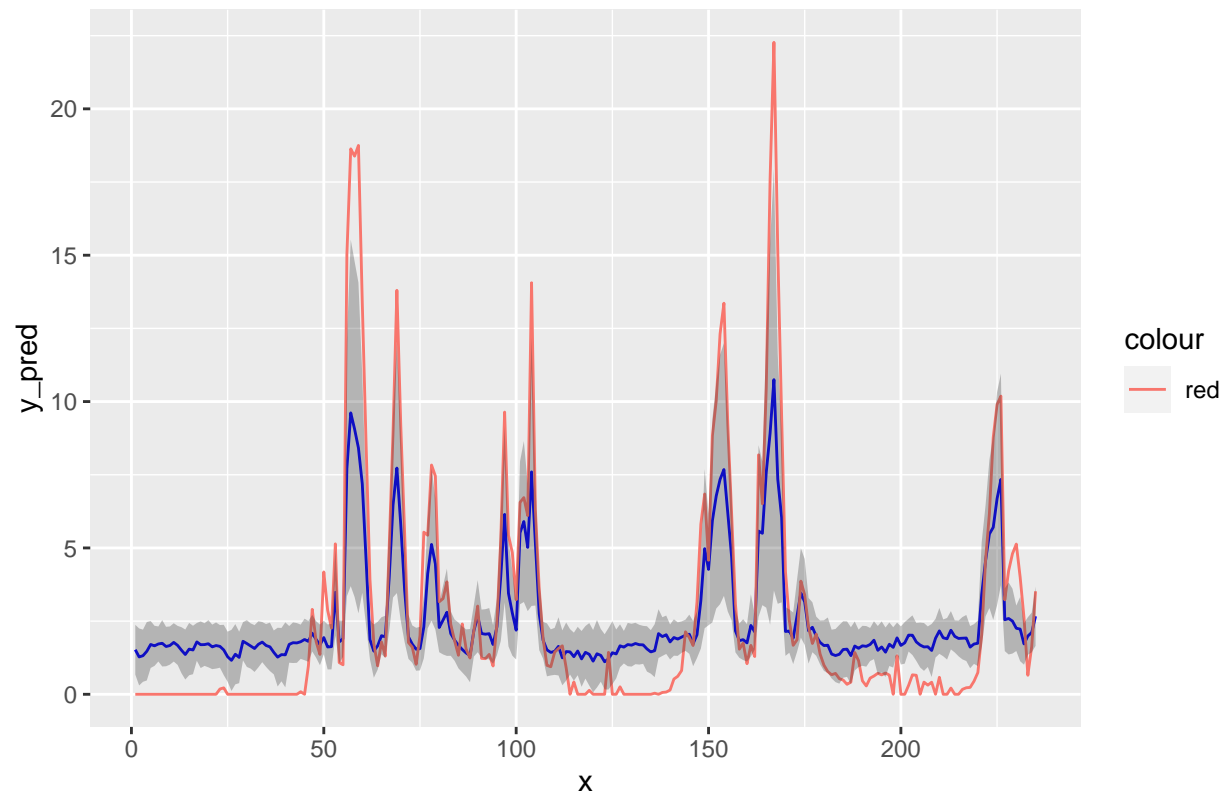


```
##  
## [[5]]
```

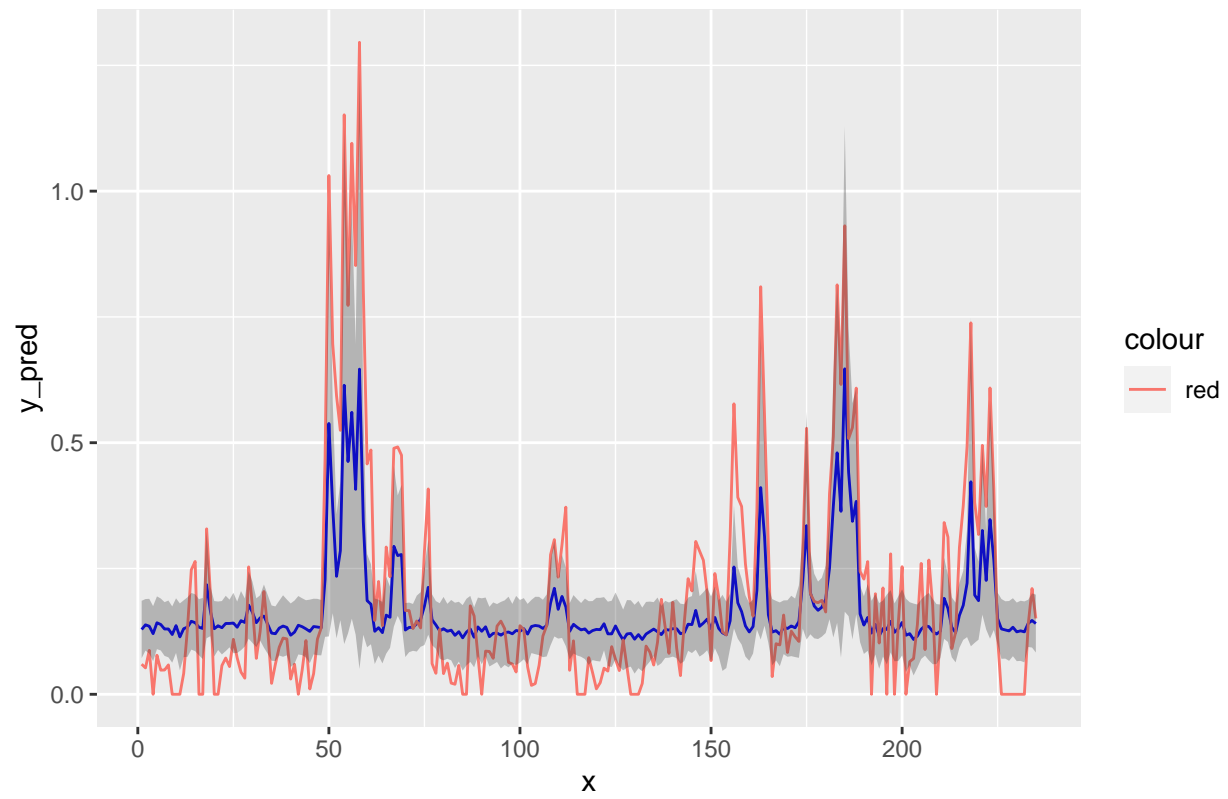
```
##  
## [[6]]
```

Tendencia Corredores



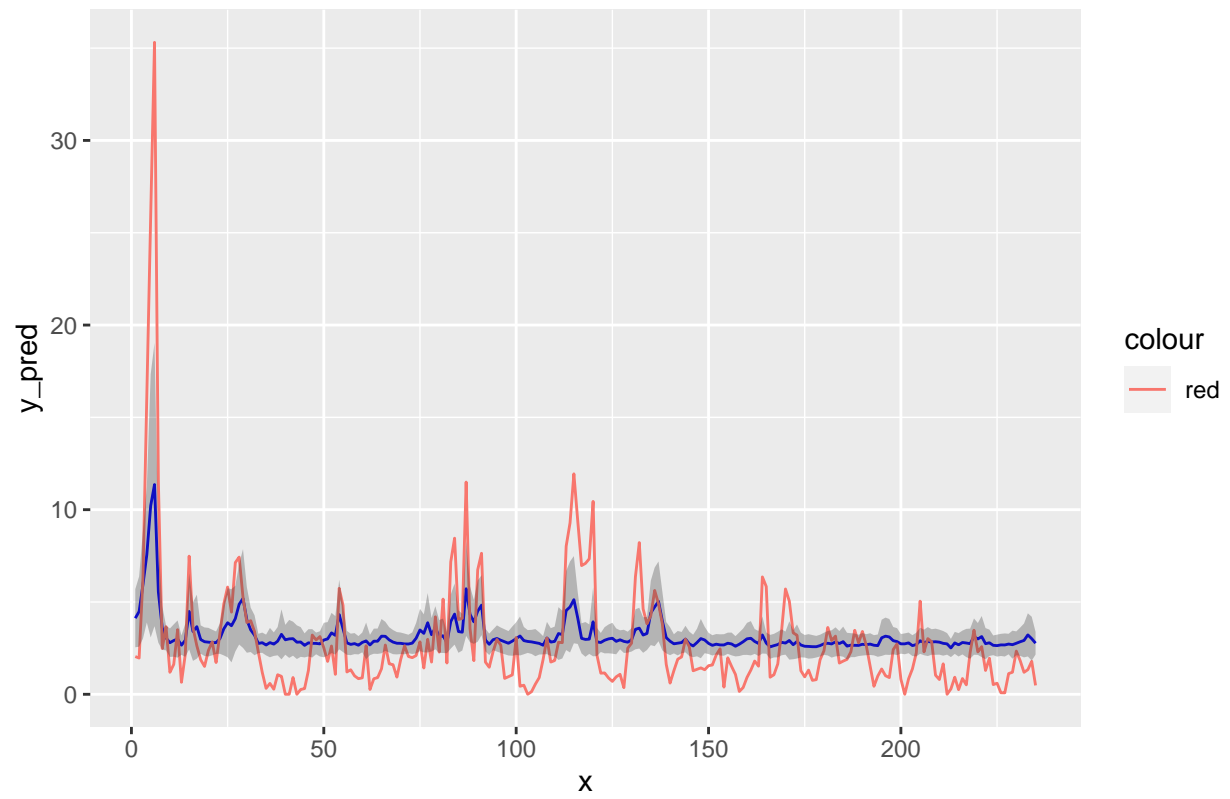
```
##  
## [[7]]
```

Tendencia Desamparados



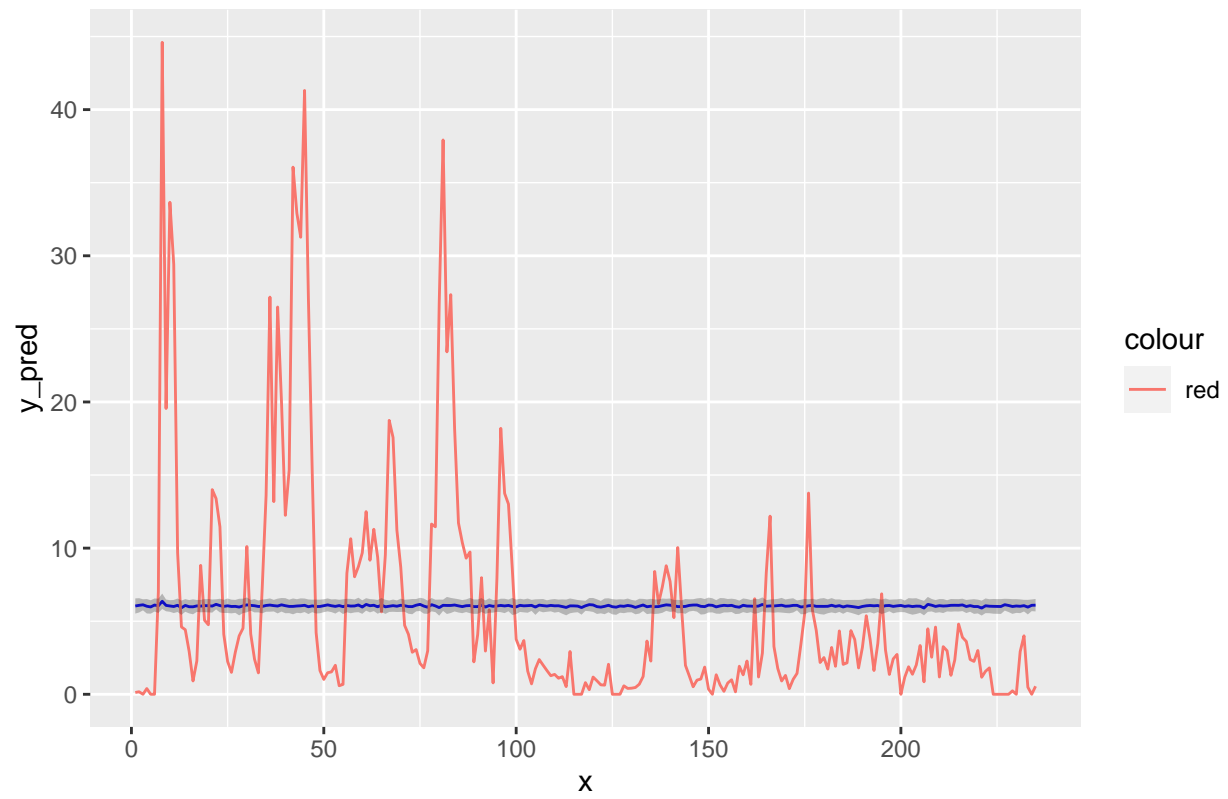
```
##  
## [[8]]
```

Tendencia Esparza

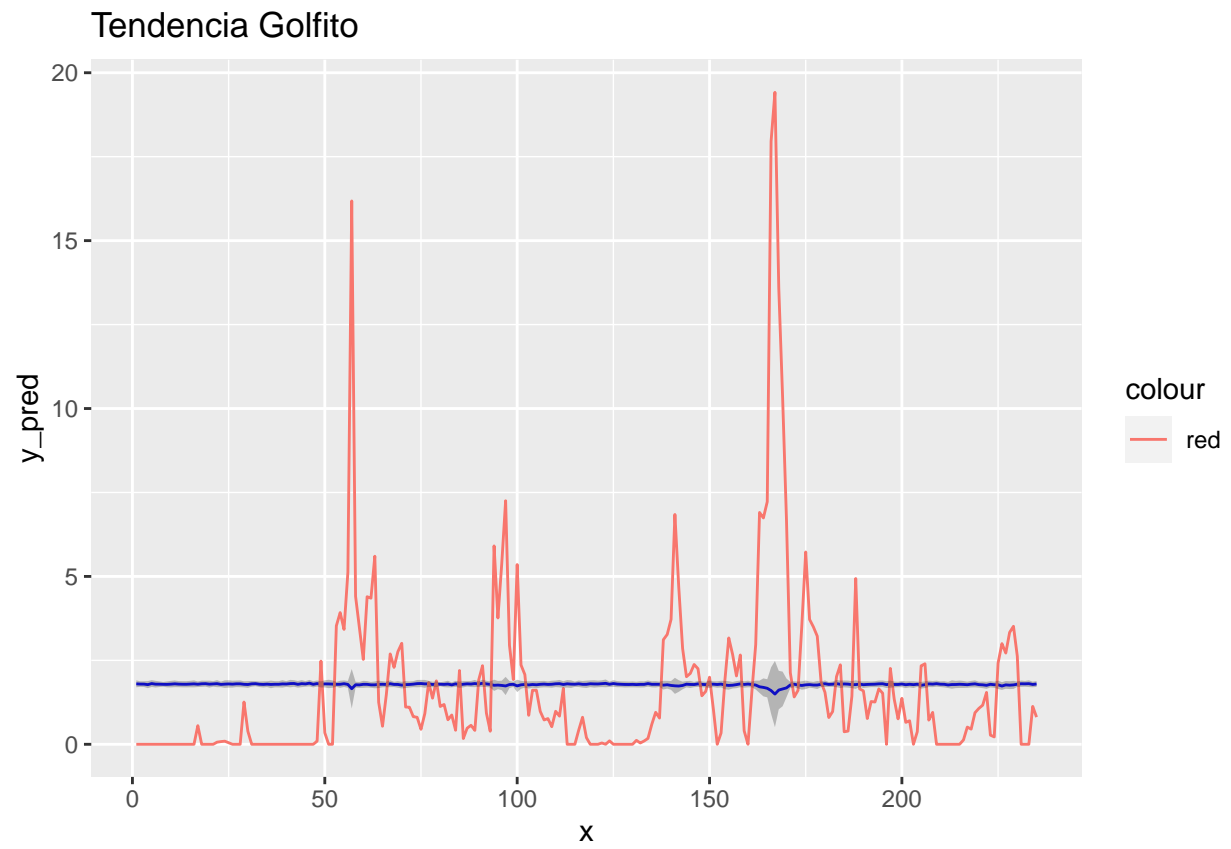


```
##  
## [[9]]
```

Tendencia Garabito

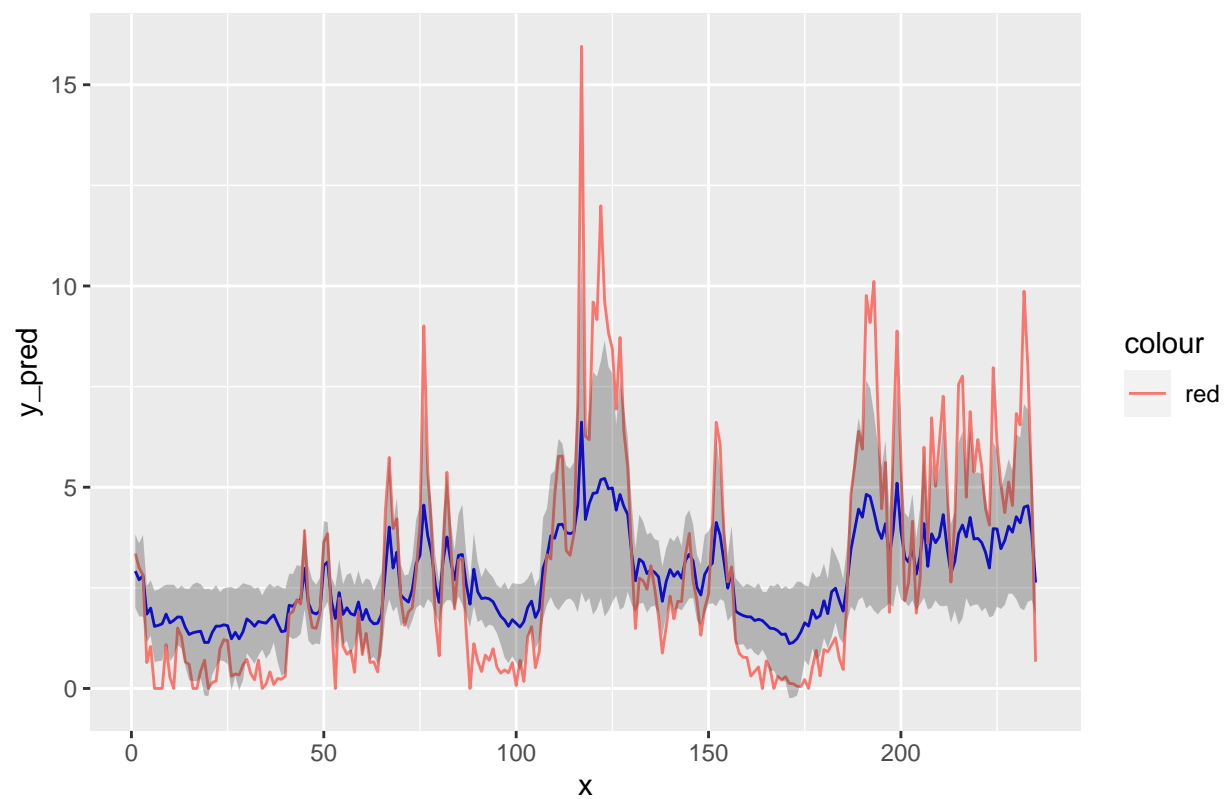


```
##  
## [[10]]
```



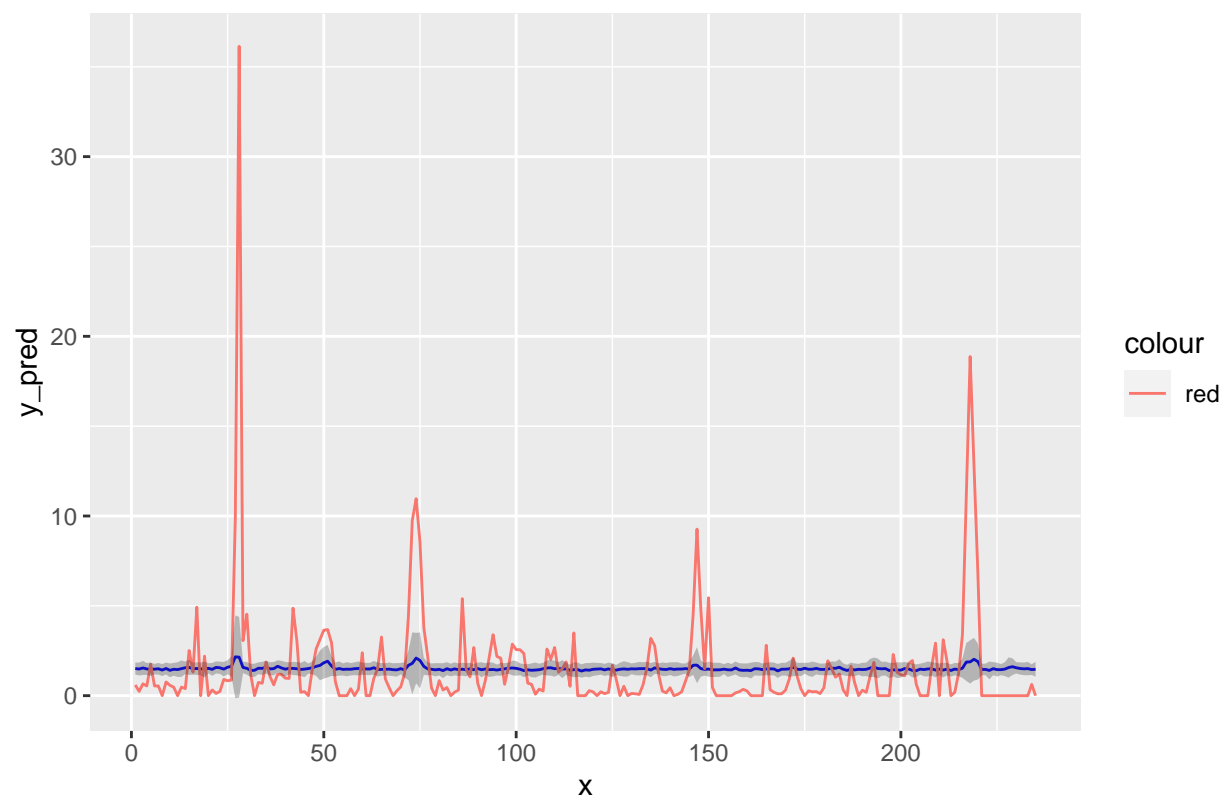
```
##  
## [[11]]
```

Tendencia Guacimo



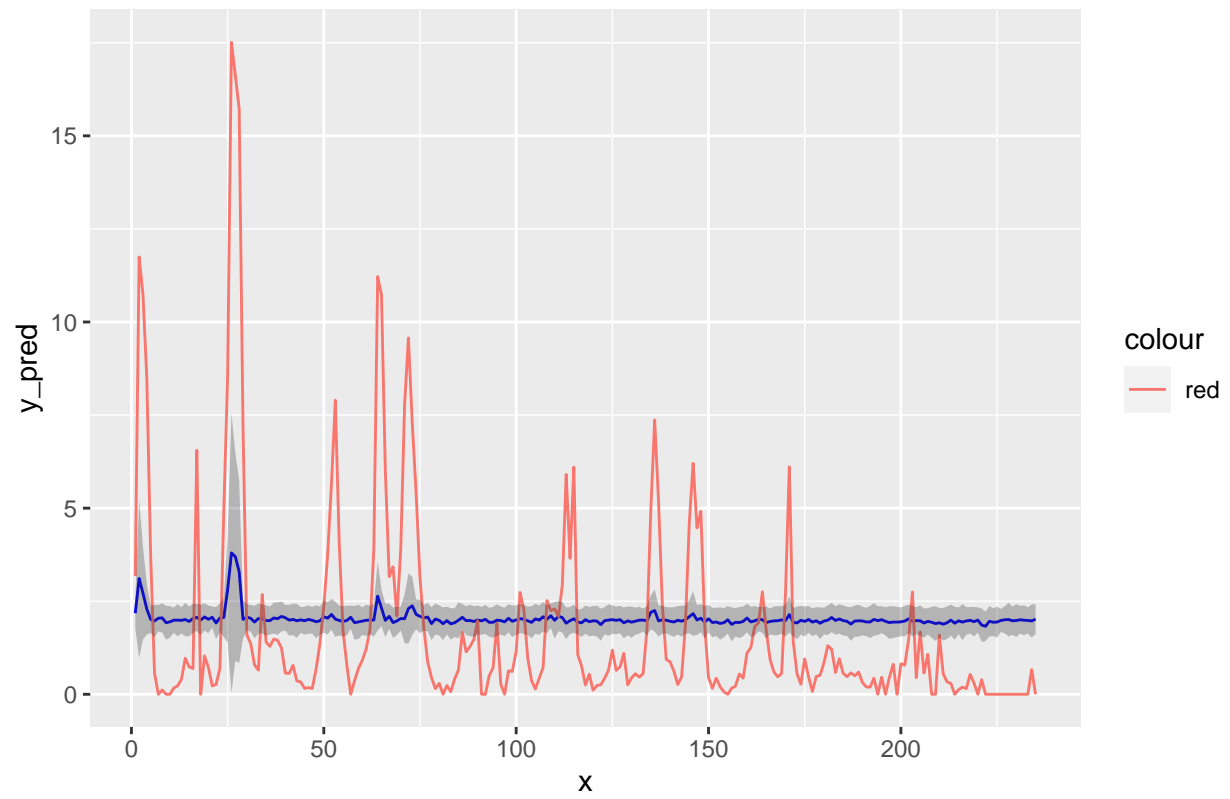
```
##  
## [[12]]
```

Tendencia La Cruz



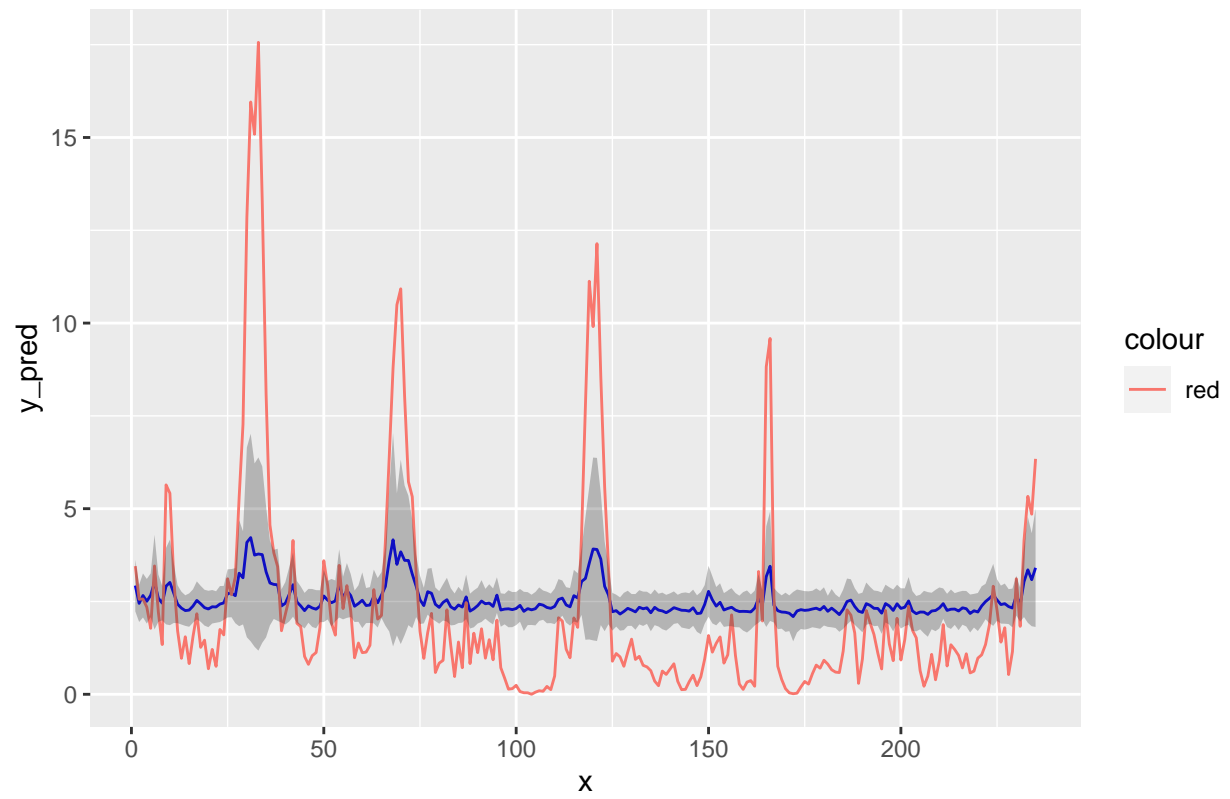
```
##  
## [[13]]
```


Tendencia Liberia



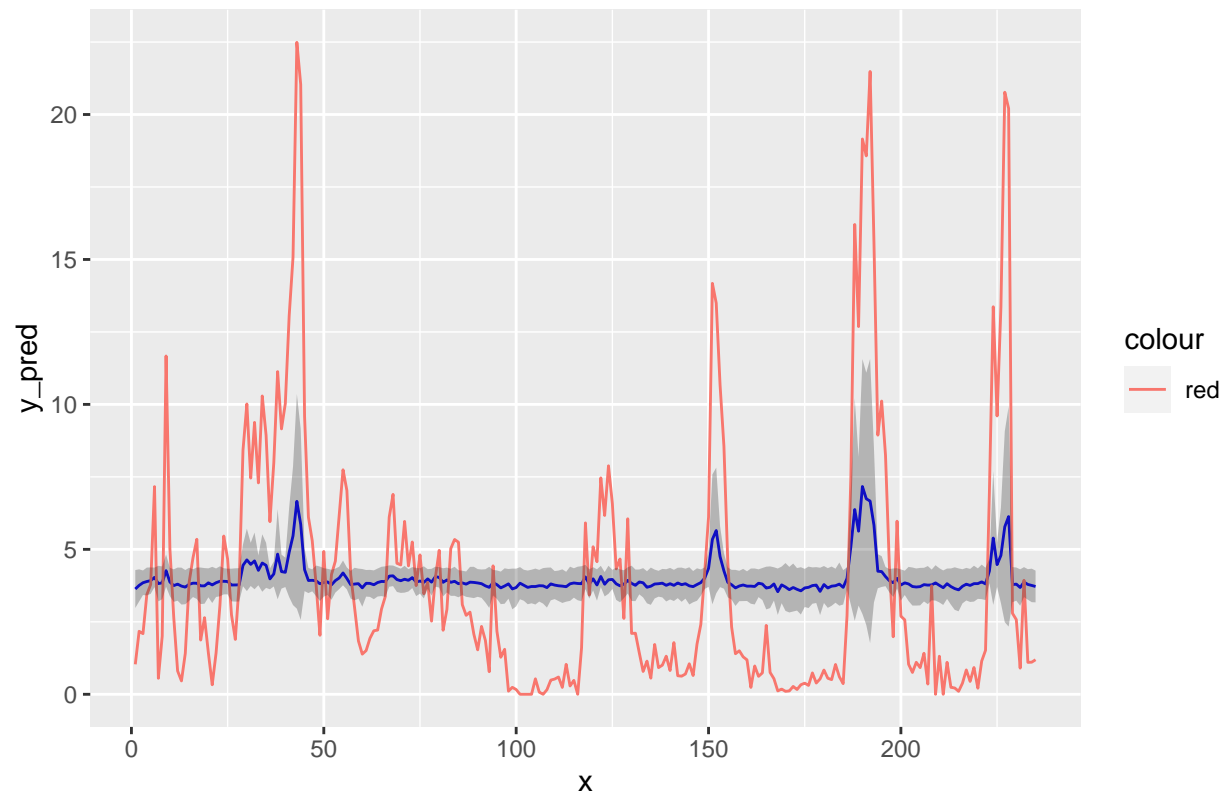
```
##  
## [[14]]
```

Tendencia Limon



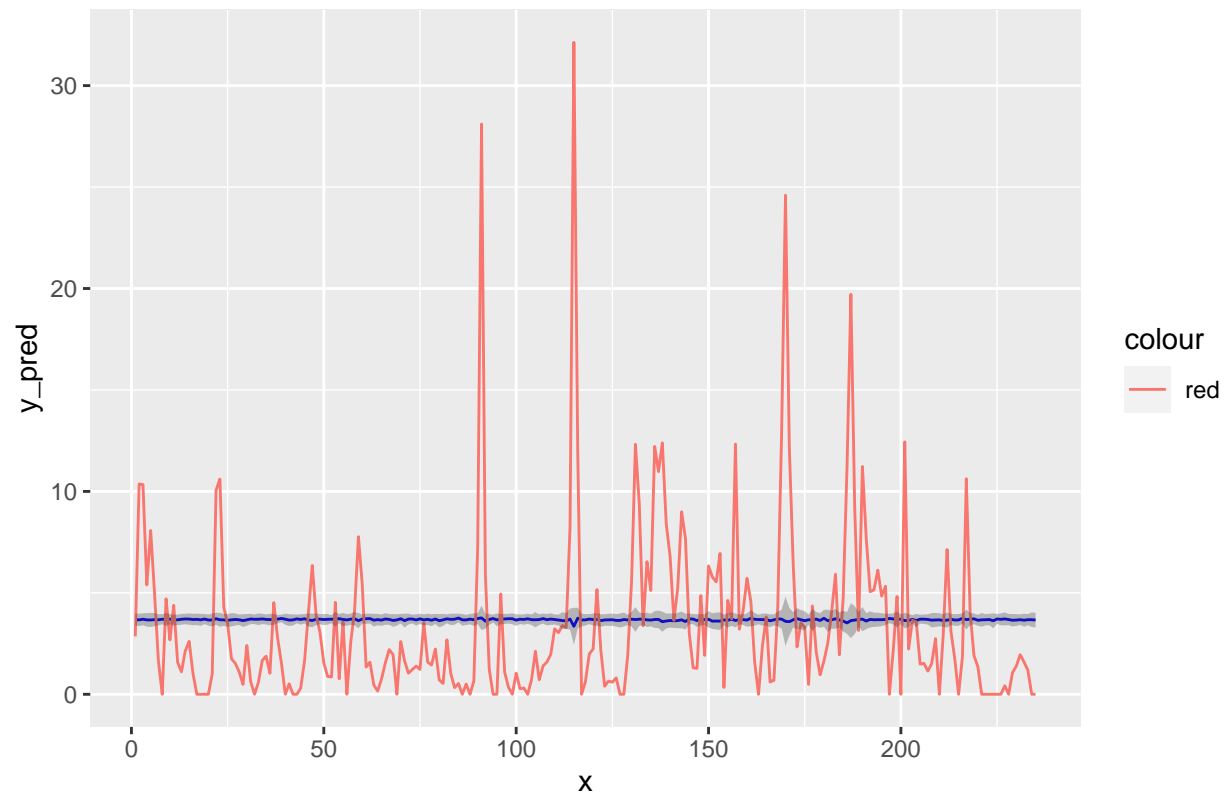
```
##  
## [[15]]
```

Tendencia Matina



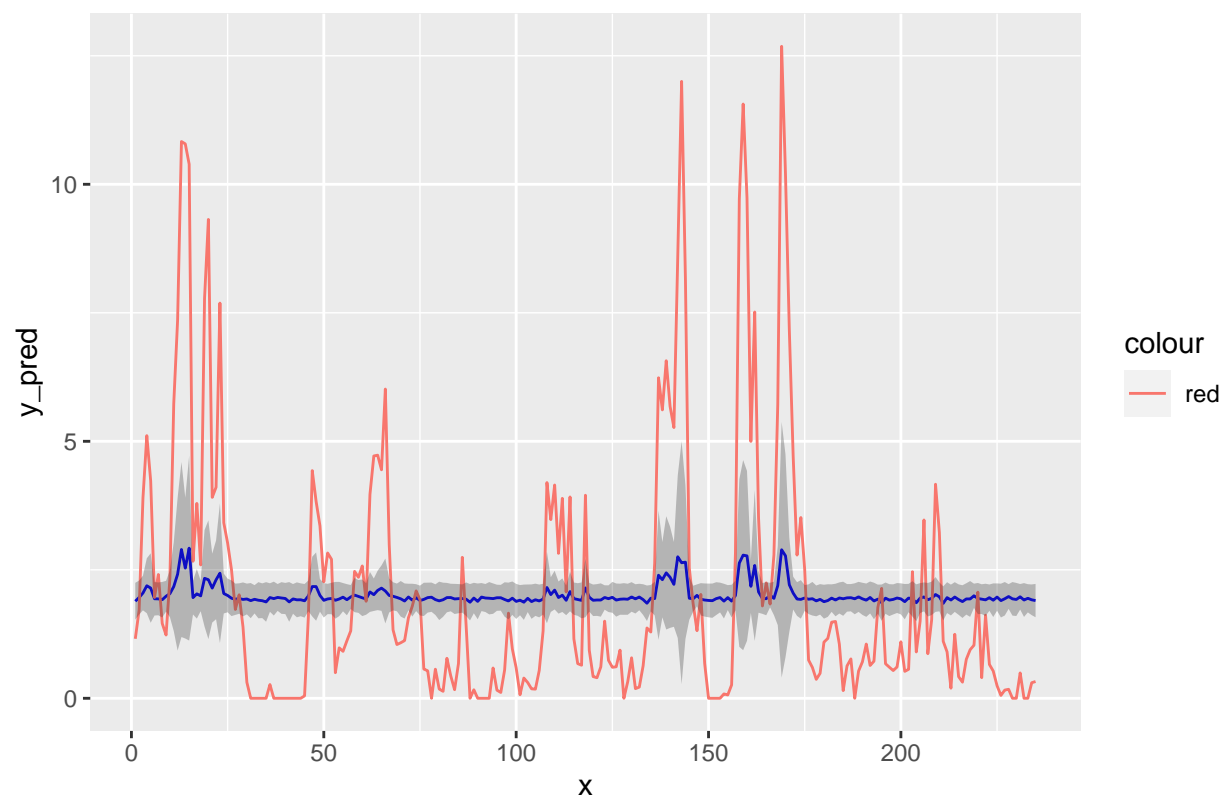
```
##  
## [[16]]
```

Tendencia Montes de Oro



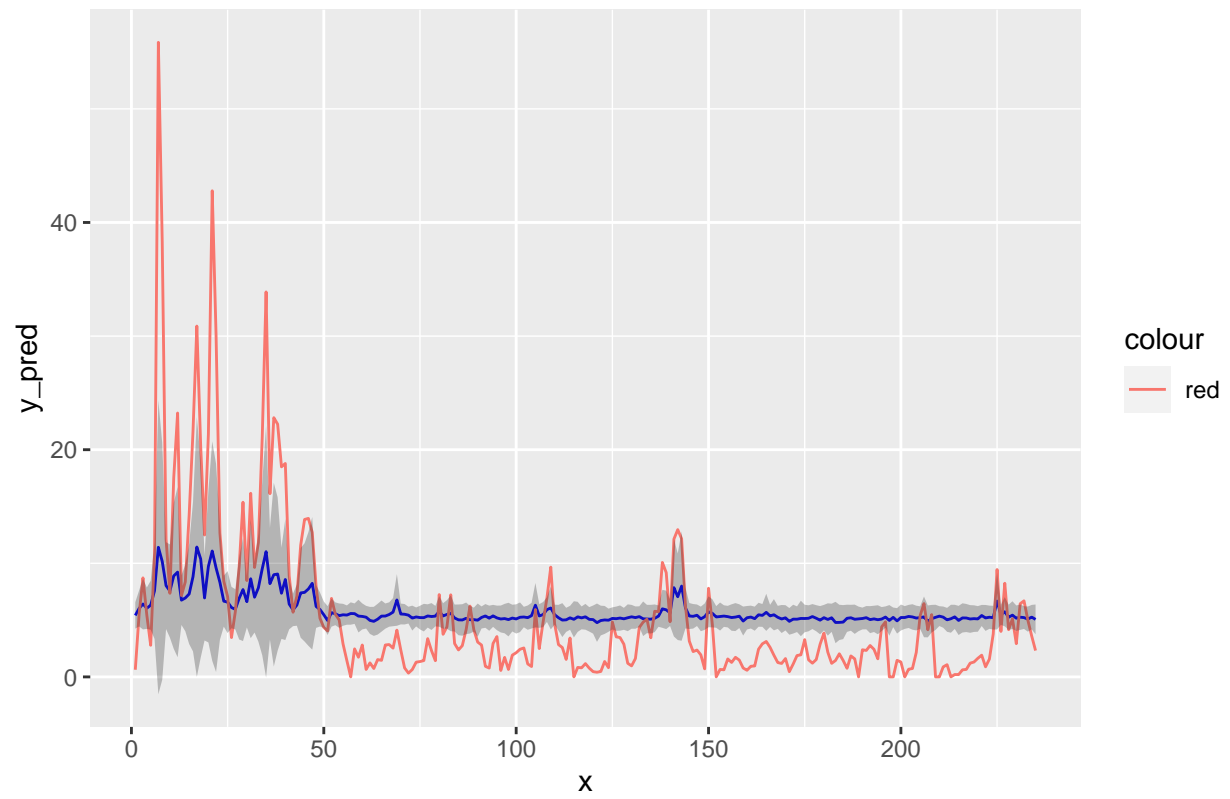
```
##  
## [[17]]
```

Tendencia Nicoya



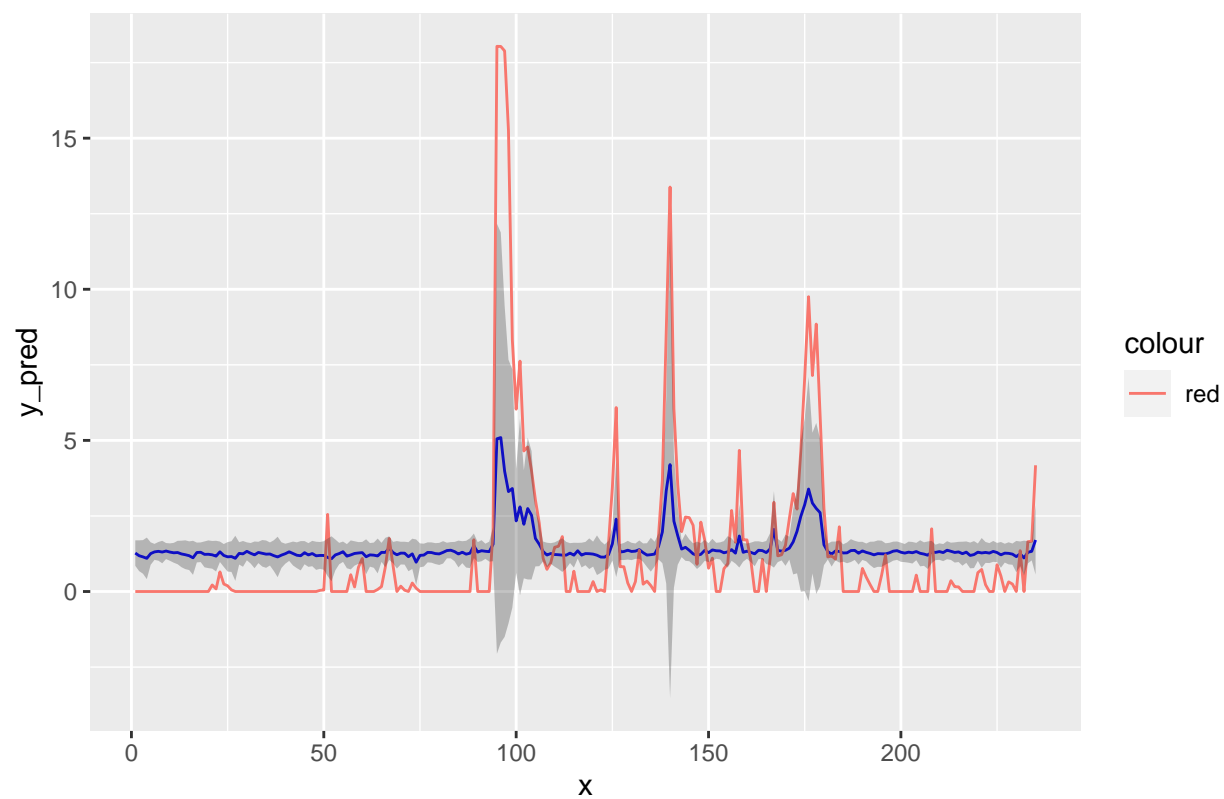
```
##  
## [[18]]
```

Tendencia Orotina



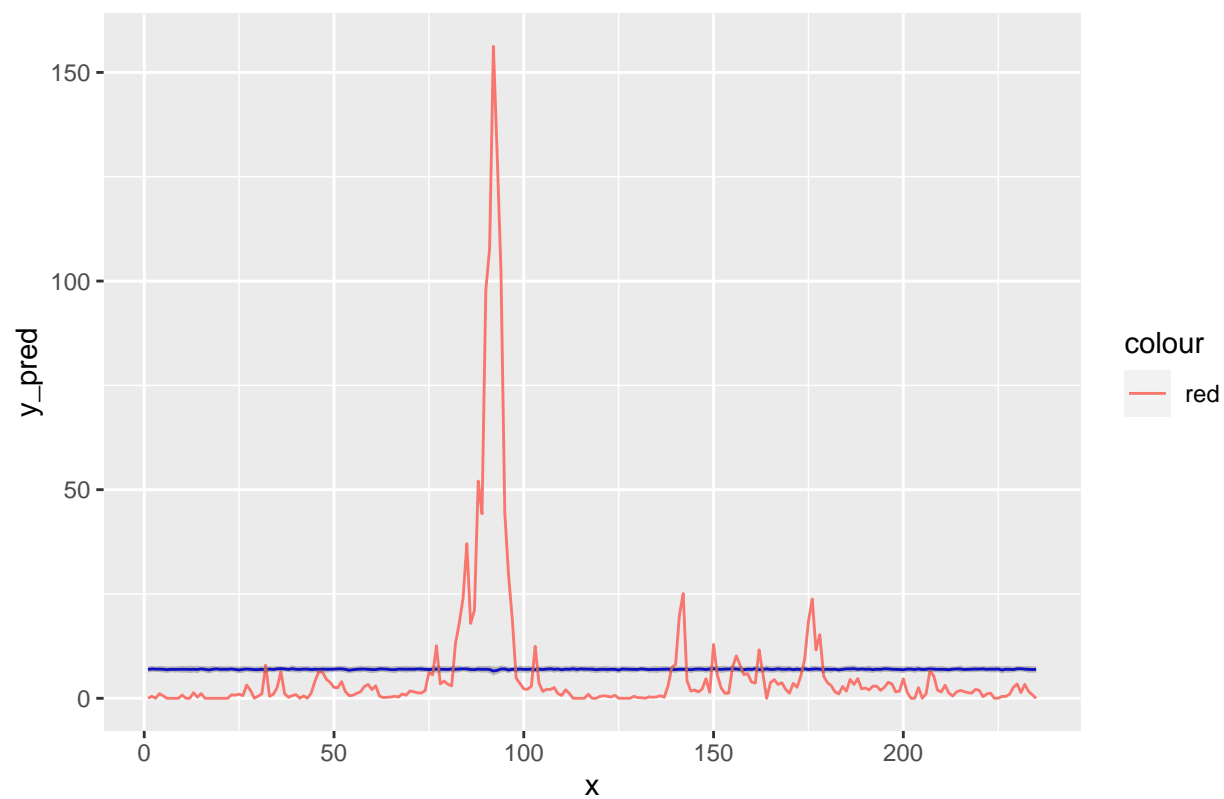
```
##  
## [[19]]
```

Tendencia Osa



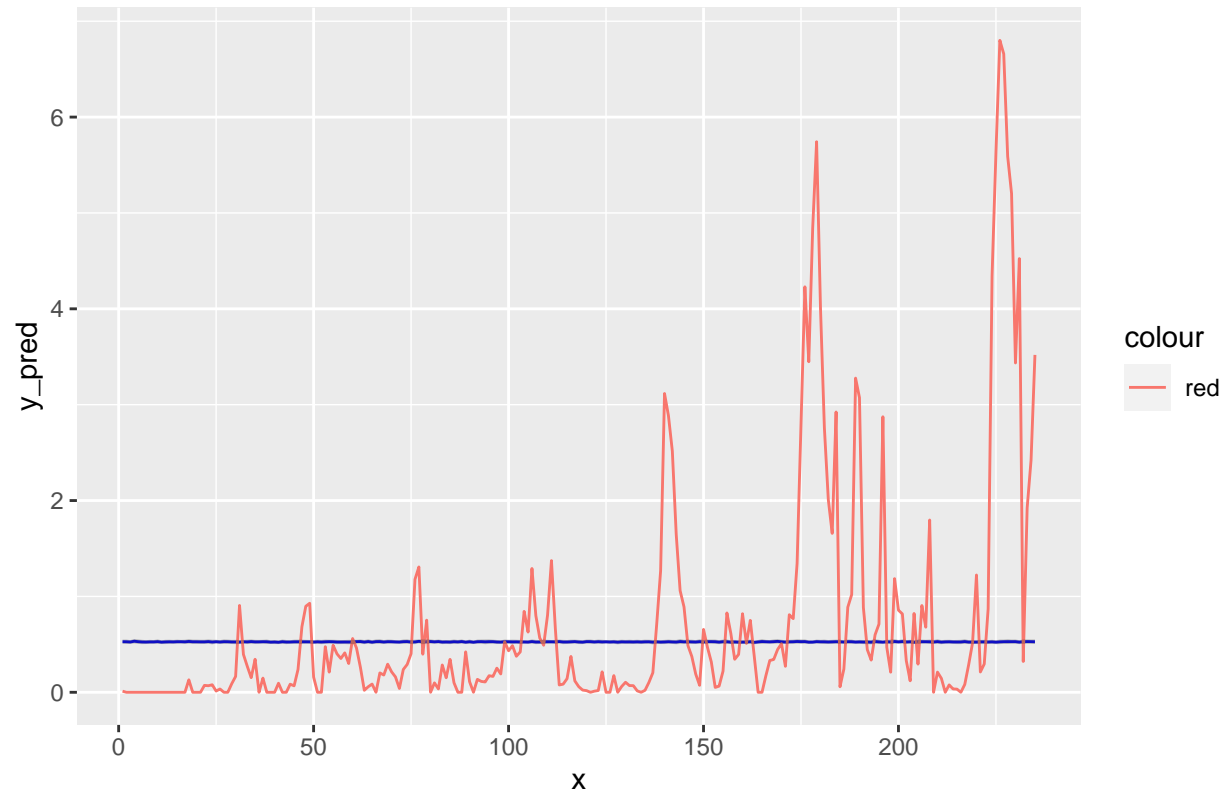
```
##  
## [[20]]
```

Tendencia Parrita



```
##  
## [[21]]
```


Tendencia Perez Zeledón



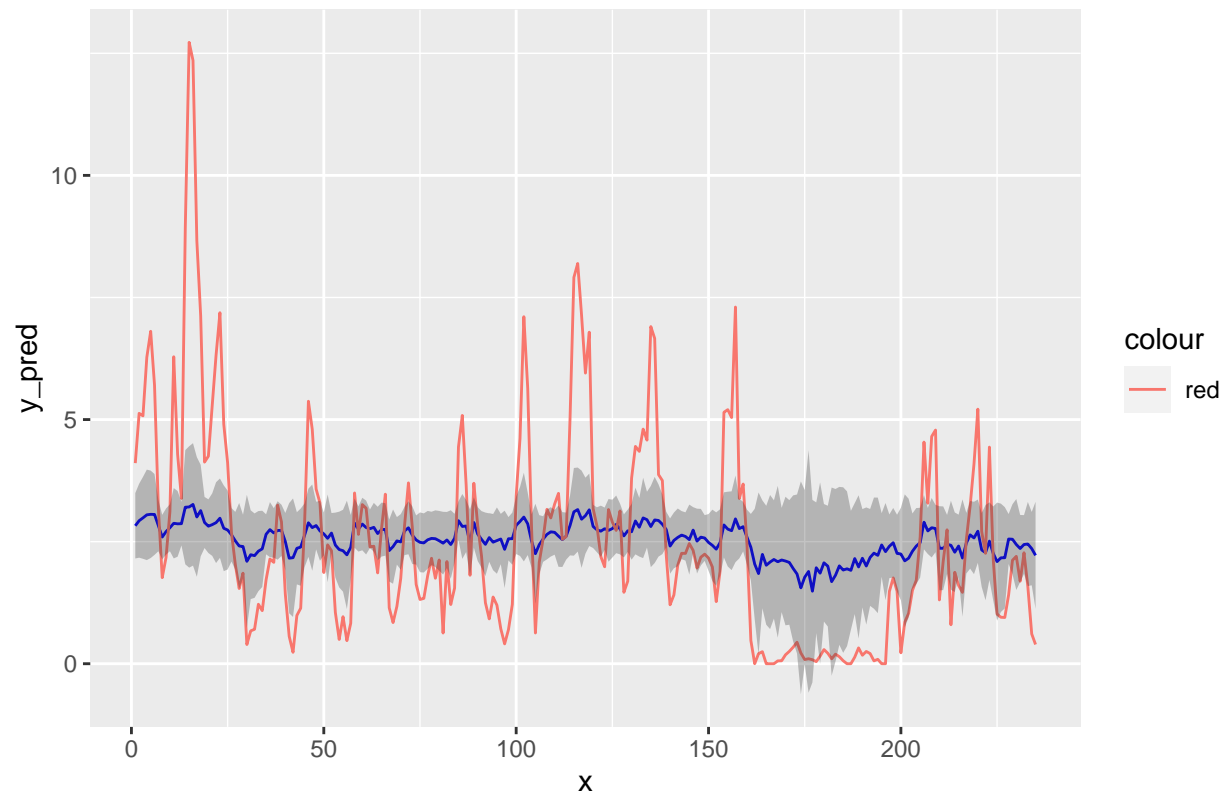
```
##  
## [[22]]
```

Tendencia Pococí



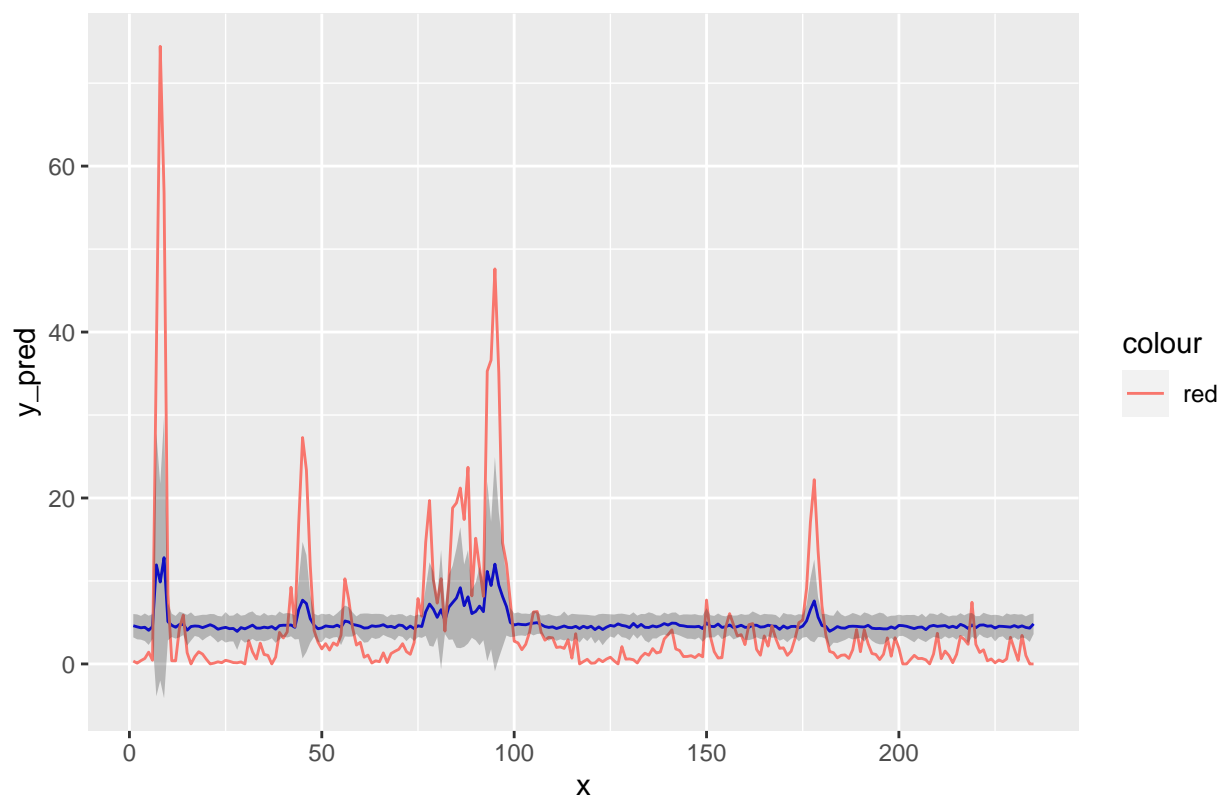
```
##  
## [[23]]
```

Tendencia Puntarenas



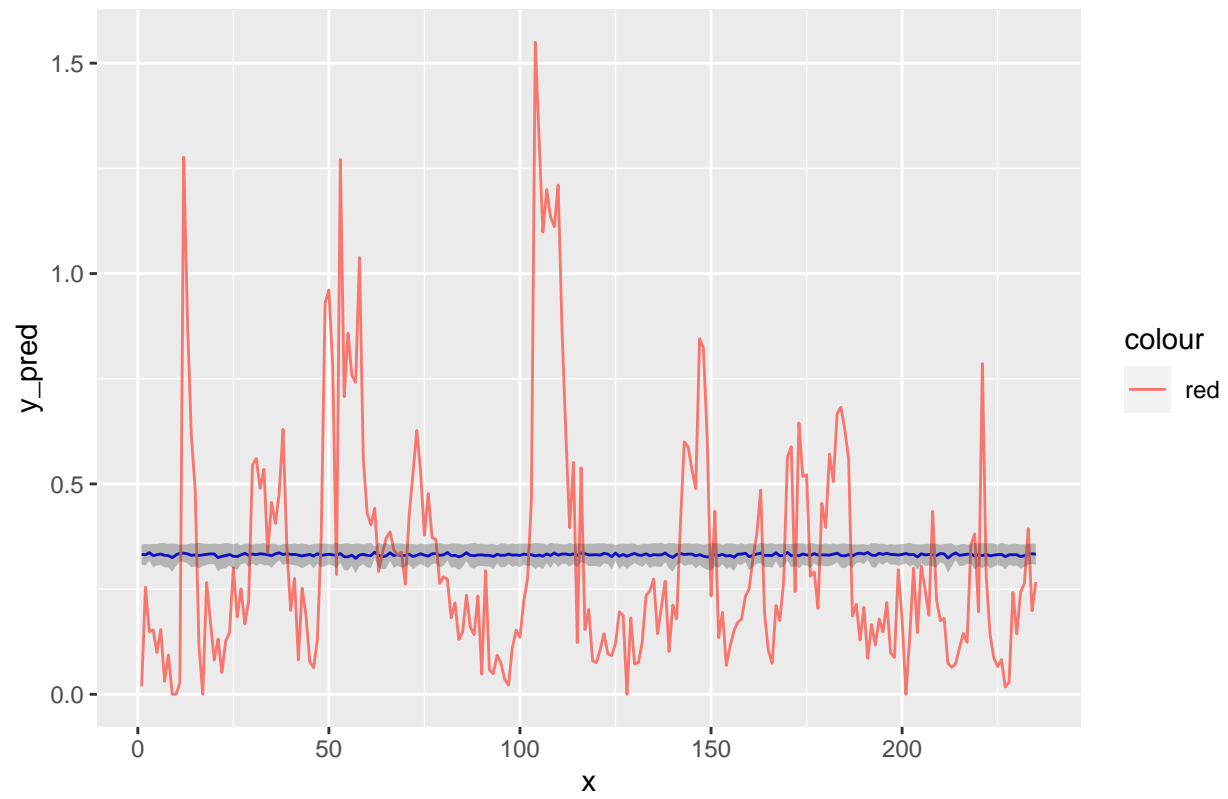
```
##  
## [[24]]
```

Tendencia Quepos



```
##  
## [[25]]
```

Tendencia San Jose



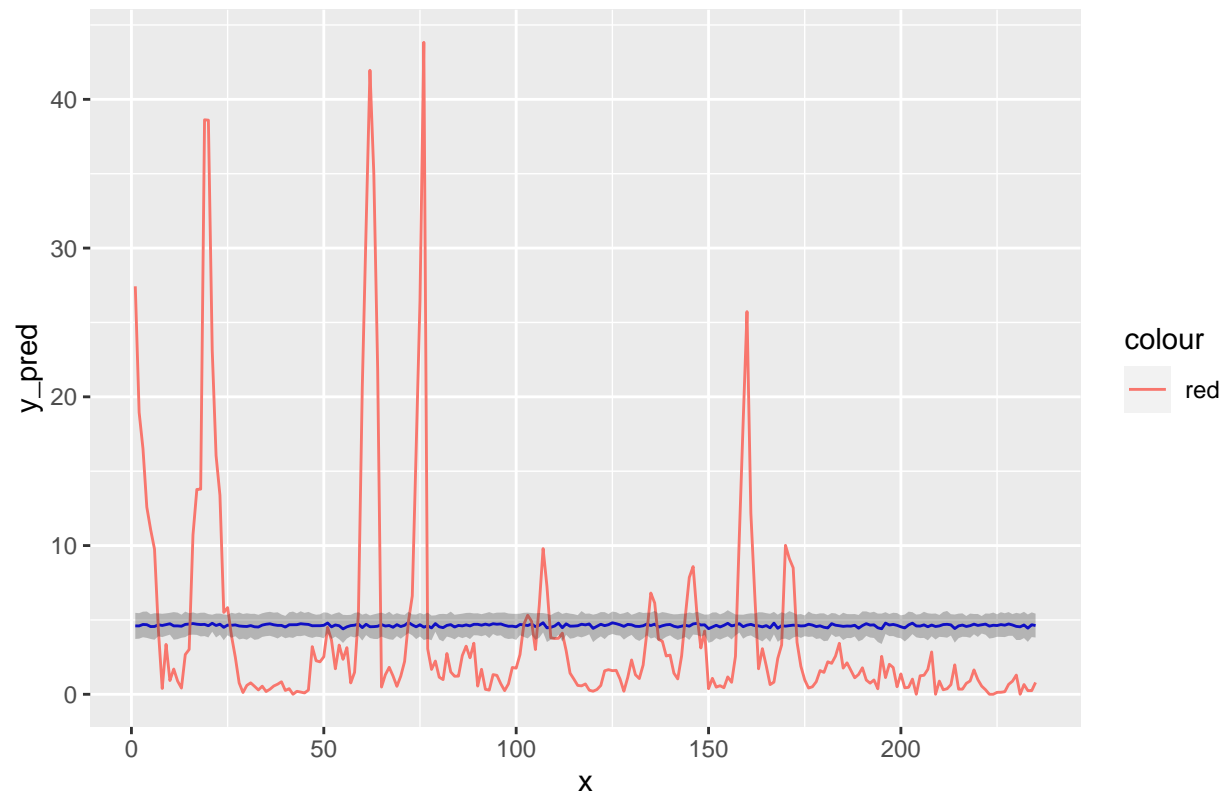
```
##  
## [[26]]
```

Tendencia Santa Ana



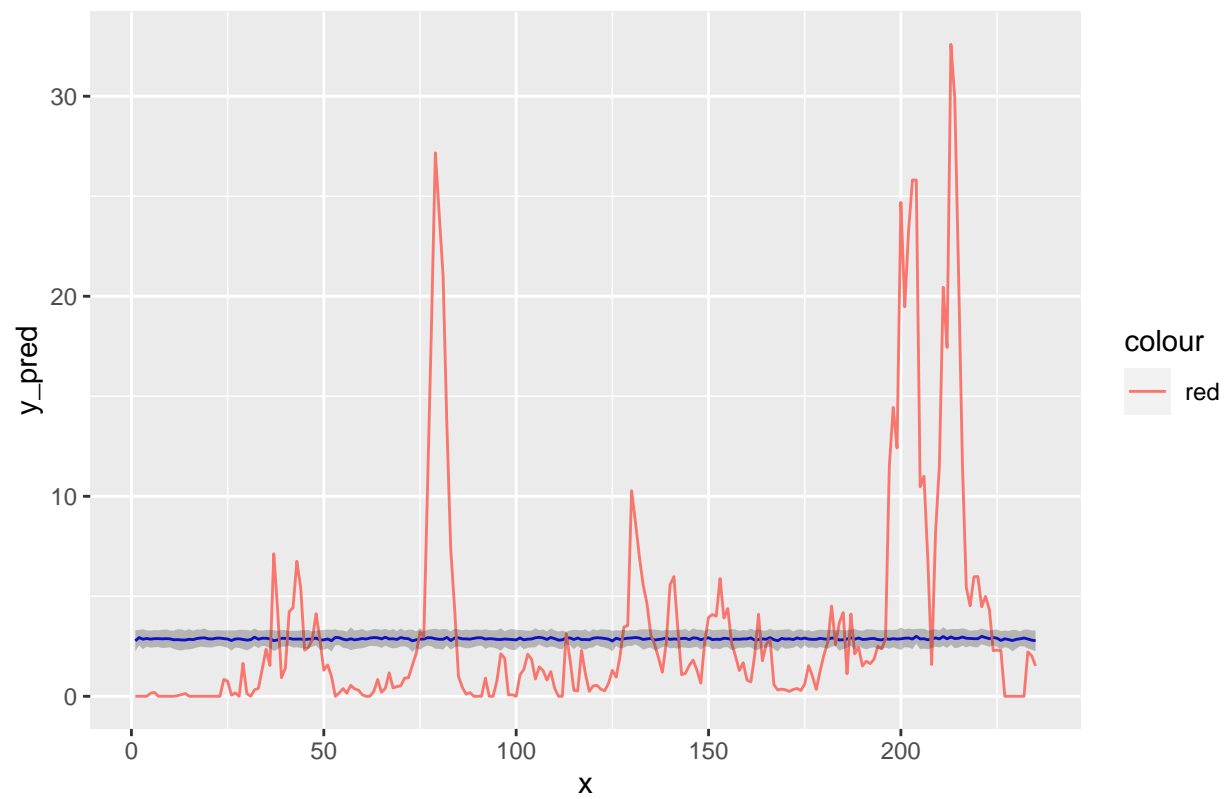
```
##  
## [[27]]
```

Tendencia SantaCruz

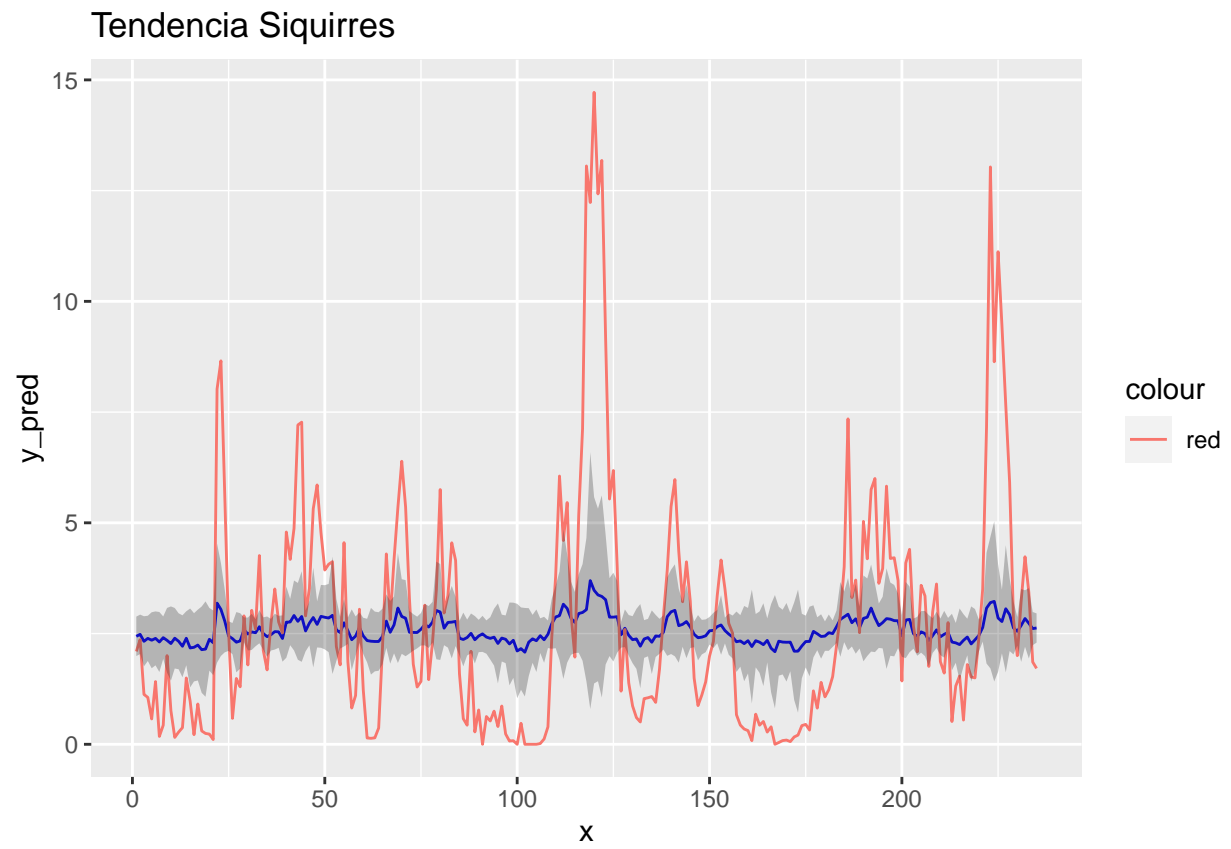


```
##  
## [[28]]
```

Tendencia Sarapiquí

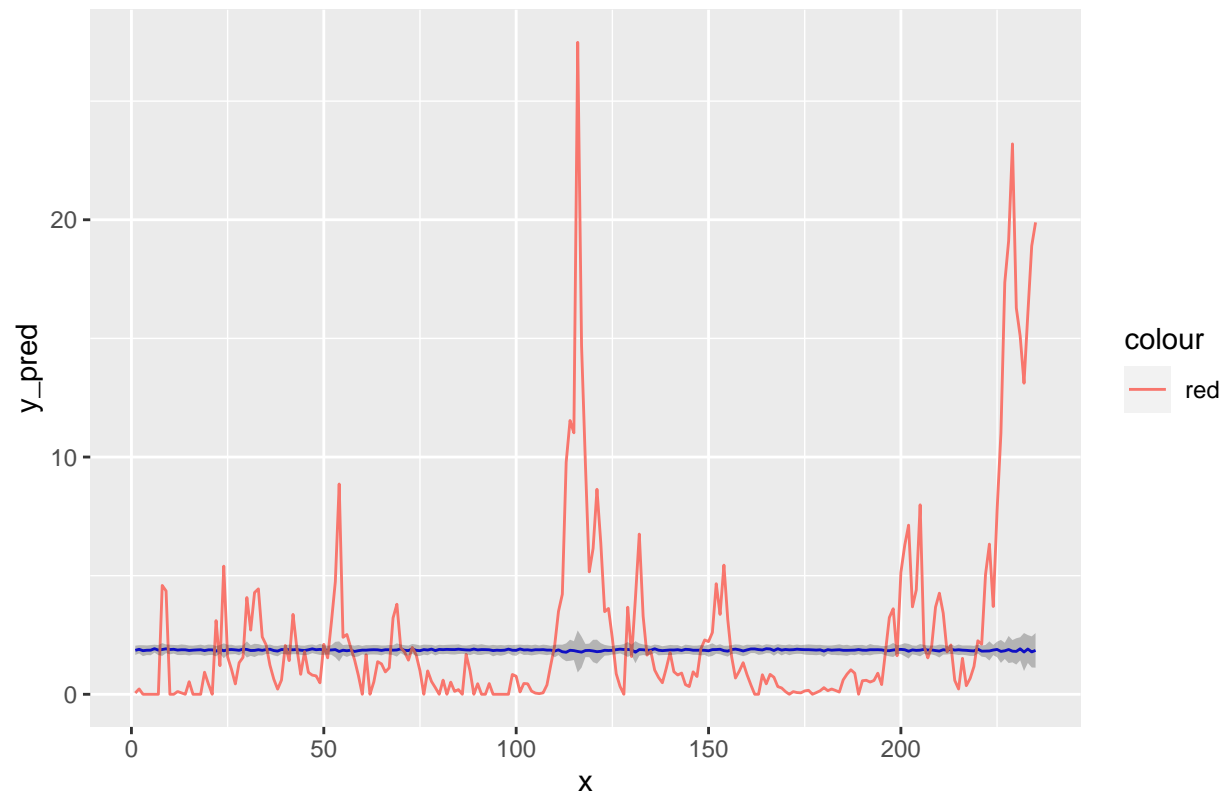


```
##  
## [[29]]
```

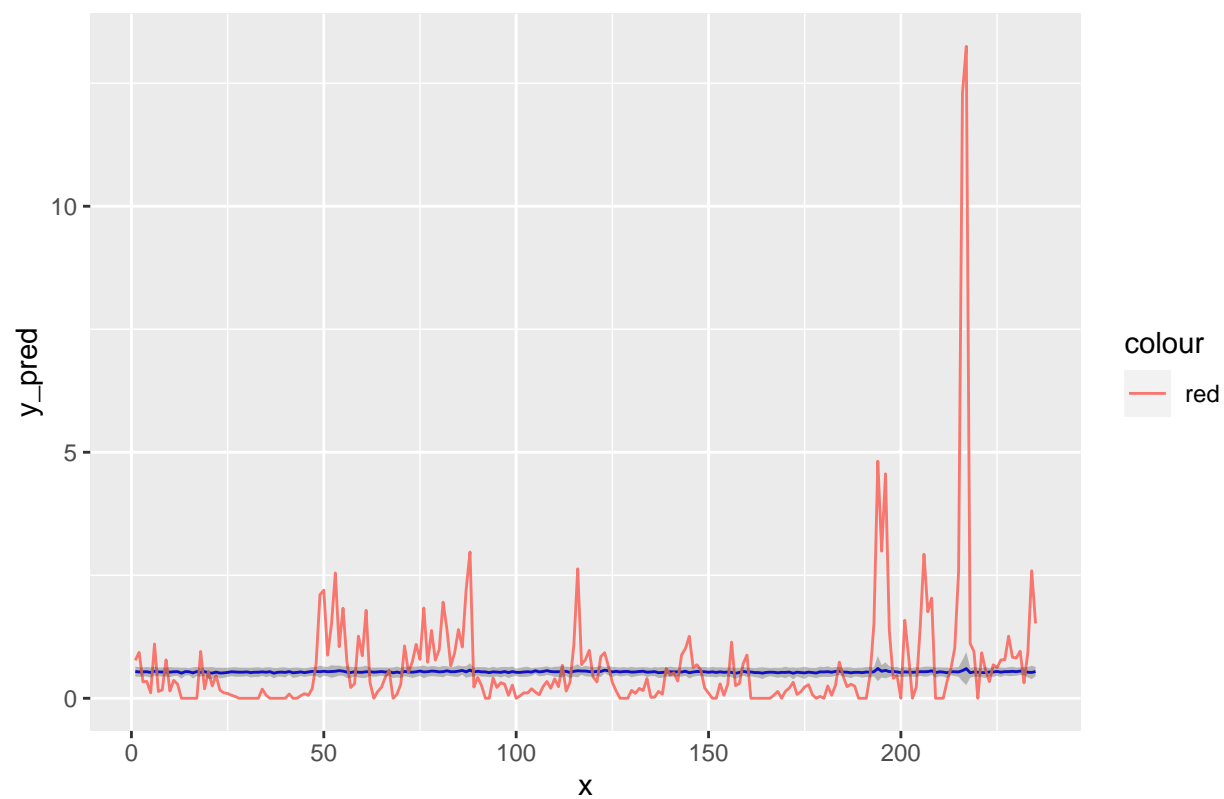
```
##  
## [[30]]
```

Tendencia Talamanca



```
##  
## [[31]]
```

Tendencia Turrialba



```
##  
## [[32]]
```

Tendencia Upala

