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Profs.	Hoe	nigman	& Agi	rawal
	Fall	2019, C	U-Bo	ulder

CSCI 3104, Algorithms Problem Set 1b (44 points)

Advice 1: For every problem in this class, you must justify your answer: show how you arrived at it and why it is correct. If there are assumptions you need to make along the way, state those clearly.

Advice 2: Verbal reasoning is typically insufficient for full credit. Instead, write a logical argument, in the style of a mathematical proof.

Instructions for submitting your solution:

- The solutions **should be typed** and we cannot accept hand-written solutions. Here's a short intro to Latex.
- You should submit your work through **Gradescope** only.
- If you don't have an account on it, sign up for one using your CU email. You should have gotten an email to sign up. If your name based CU email doesn't work, try the identikey@colorado.edu version.
- Gradescope will only accept .pdf files (except for code files that should be submitted separately on Gradescope if a problem set has them) and try to fit your work in the box provided.
- You cannot submit a pdf which has less pages than what we provided you as Gradescope won't allow it.
- 1. (34 pts total) Let $A = \langle a_1, a_2, \ldots, a_n \rangle$ be an array of numbers. Let's define a 'flip' as a pair of distinct indices $i, j \in \{1, 2, \ldots, n\}$ such that i < j but $a_i > a_j$. That is, a_i and a_j are out of order.
 - For example In the array A = [1, 3, 5, 2, 4, 6], (3, 2), (5, 2) and (5, 4) are the only flips i.e. the total number of flips is 3. (Note that in this example the indices are the same as the actual values)
 - (a) (8 pts) Write a Python code for an algorithm, which takes as input a positive integer n, **randomly shuffles an array of size n** with elements $[1, \ldots, n]$ and counts the total number of flips in the shuffled array.
 - Also, run your code on a bunch of n values from $[2, 2^2, 2^3, 2^{20}]$ and present your result in a table with one column as the value of n and another as the number of flips. Alternatively, you can present your table in form of a labeled plot with the

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columns forming the 2 axes.

Note: The .py file should run for you to get points and name the file as Lastname-Firstname-MMDD-PSXi.pdf. You need to submit the code via Canvas but the table or plot should be on the main .pdf.

Erase this before you answer - This space is NOT for the code but only for the table or plot.

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(b)	(4 pts) At most, how many flips can A co	ntain in terms of the array size n? Hint
	The code you wrote in (a) can help you	find this. Explain your answer with
	short statement.	

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that, on each pass through A, exconsecutive pair forms a flip, the order pair). So, if your array A 4 and 2, then compare (but not and 6, etc. Formulate pseudo-coe Hint: After the first pass of the would be. The second pass can	d if A has no flips. Design a sorting algorithm xamines each pair of consecutive elements. If a algorithm swaps the elements (to fix the out of was [4,2,7,3,6,9,10], your first pass should swap swap) 4 and 7, then swap 7 and 3, then swap 7 de for this algorithm, using nested for loops. Outer loop think about where the largest element then safely ignore the largest element because on. You should keep repeating the process for all t.

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(d)	(d) (4 pts) Your algorithm has an inner loop and an outer loop. Provide the 'loop invariant (LI) for the inner loop. You don't need to show the complete				
	proof.	ioi the iiiiei ic	op. rou don t r	reed to show t	ne complete Li

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2. (6 pt) If r is a real number not equal to 1, then for every $n \geq 0$,

$$\sum_{i=0}^{n} r^{i} = \frac{(1 - r^{n+1})}{(1 - r)}.$$

Rewrite the inductive hypothesis from Q3 on PS1a and provide the inductive step to complete the proof by induction. You can refer to Q3 on PS1a to recollect the first 2 steps.

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3.	(4 pt) Refer to	Q2b on PS1a and fine	ish the LI based proof	f with all the steps.	