

# CSCI 3104 PS10a

Jonathan Phouminh

TOTAL POINTS

**19.5 / 25**

QUESTION 1

11 pts

**1.1 2.5 / 2.5**

- ✓ + **2.5 pts** All values correct
- + **2 pts** One mistake
- + **1.5 pts** Two mistake
- + **0 pts** More than two mistake, or not attempted

**1.2 1.5 / 1.5**

- ✓ + **1.5 pts** Come up with the right example
- + **0 pts** Misunderstood the concept/ Incorrect
- + **1 pts** Understand the concept but did not come up with an example
- + **0 pts** No attempt

**1.3 0 / 2**

- + **2 pts** Correct number of recursive calls (25) mentioned and appropriate recursion tree shown
- + **1 pts** Correct recursion tree shown but number of recursive calls would be 25 and not 15. Please refer to the solution file.
- + **1 pts** Correct recursion tree shown but the number of calls not mentioned explicitly as 25 or incorrect number of calls mentioned due to partially correct recursion tree. Please refer to the solution file.
- + **1 pts** Correct number of recursion calls (25) mentioned without showing the appropriate recursion tree. Please refer to the solution file.
- + **0.5 pts** Number of recursive calls would be 25 and not 15. Also failed to show the recursion tree. Please refer to the solution file.
- ✓ + **0 pts** Incorrect or empty solution submitted. Please refer to the solution file.
- + **0.5 pts** Partially correct solution. Please refer to the solution file for complete correct solution.

- + **2 pts** Correct number of recursive calls is 25, not 24. Initial call is included

**1.4 2.5 / 3**

- + **3 pts** Correct.
- ✓ + **2 pts** All OPT values are correct.
- + **1 pts** Arrows are correct.
- + **1 pts** Partial OPT values are correct.
- ✓ + **0.5 pts** Partial arrows are correct.
- + **0 pts** Incorrect/Not attempted.

**1.5 2 / 2**

- ✓ + **2 pts** Correct.
- + **1 pts** The results are correct.
- + **1 pts** The explanations are reasonable.
- + **0 pts** Incorrect/Not attempted.

QUESTION 2

14 pts

**2.1 1 / 2**

- + **1 pts** Identified correctly the smaller sub-problems.
- ✓ + **1 pts** Written the correct representation of sub-problems.
- + **0 pts** No answer or incorrect answer.
- + **0.5 pts** Interchanged representation of insertion and deletion.
- 💬 You have to clearly write the subproblems in terms of  $\text{cost}[i][j]$ .

**2.2 3.5 / 4**

- ✓ + **2 pts** Drawn the arrows representing the optimal alignment.
- ✓ + **1 pts** Written the alignment corresponding to arrows correctly
- ✓ + **1 pts** Written the correct set of optimal operations

using the arrows drawn.

+ 0 pts (Non-scored rubric item) Identified the costs of insertion, deletion and substitution as 1.

+ 0 pts Incorrect answer or No answer

✓ - 0.5 pts Minor error in the set of optimal operations

① These two SUB should be no-op.

## 2.3 6.5 / 8

✓ + 3 pts Correct table values

✓ + 1.5 pts Correct first optimal path

+ 1.5 pts Correct second optimal path

✓ + 2 pts Correct optimal cost

+ 1 pts Correct Operations mentioned by not optimal cost or optimal cost mentioned as 2 instead of 4. Please refer to the solution file.

+ 0 pts Incorrect or empty solution submitted.

Please refer to the solution file.

- 1 pts Minor errors in table values. Please refer to the solution file.

- 0.5 pts Minor errors in first optimal path. Please refer to the solution file.

- 0.5 pts Minor errors in second optimal path. Please refer to the solution file.

Name: Jonathan Phouminh

ID: 106054641

**CSCI 3104, Algorithms**  
**Problem Set 10a (25 points)**

**Profs. Hoenigman & Agrawal**  
**Fall 2019, CU-Boulder**

*Advice 1:* For every problem in this class, you must justify your answer: show how you arrived at it and why it is correct. If there are assumptions you need to make along the way, state those clearly.

*Advice 2:* Verbal reasoning is typically insufficient for full credit. Instead, write a logical argument, in the style of a mathematical proof.

**Instructions for submitting your solution:**

- The solutions **should be typed** and we cannot accept hand-written solutions. Here's a short intro to Latex.
- You should submit your work through **Gradescope** only.
- If you don't have an account on it, sign up for one using your CU email. You should have gotten an email to sign up. If your name based CU email doesn't work, try the identikey@colorado.edu version.
- Gradescope will only accept **.pdf** files (except for code files that should be submitted separately on Gradescope if a problem set has them) and **try to fit your work in the box provided**.
- You cannot submit a pdf which has less pages than what we provided you as Gradescope won't allow it.

Name: Jonathan Phouminh

ID: 106054641

**CSCI 3104, Algorithms**  
**Problem Set 10a (25 points)**

**Profs. Hoenigman & Agrawal**  
**Fall 2019, CU-Boulder**

1. (11 pts) Solve the following based on the given intervals.

Event Index	Interval	Value
1	[1, 10]	10
2	[11, 20]	5
3	[21, 30]	15
4	[9, 12]	7
5	[19, 22]	8

- (a) (2.5 pts) For the given set of requests with a start and finish time and a value, what is  $p(j)$  for each request  $j$ ?

*Solution.*

$$P(1) = 0$$

$$P(2) = 0$$

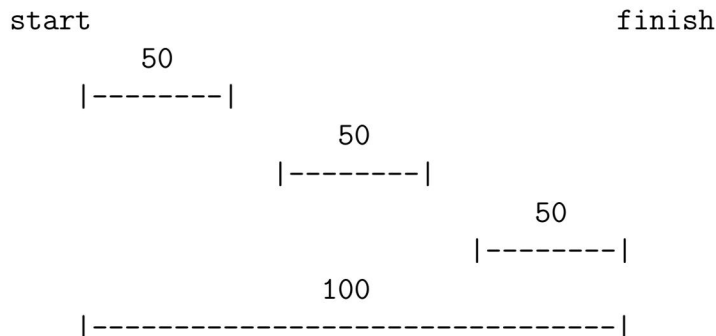
$$P(3) = 1$$

$$P(4) = 2$$

$$P(5) = 3$$

- (b) (1.5 pts) Assume you are given a greedy algorithm for the weighted interval scheduling problem that selects the requests in descending order of their value, i.e. highest valued requests are selected first. Provide an example set of intervals where this approach won't produce the optimal solution.

*Solution.*



Name: Jonathan Phouminh

ID: 106054641

CSCI 3104, Algorithms  
Problem Set 10a (25 points)

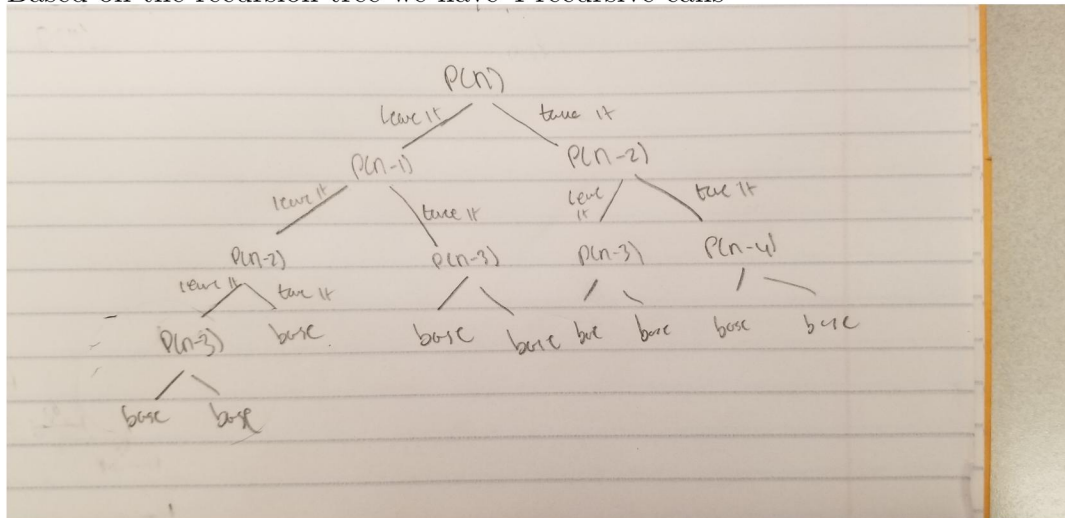
Prof. Hoenigman & Agrawal  
Fall 2019, CU-Boulder

- (c) (2 pts) In the following recursive formula for the weighted interval scheduling problem in Question 1, how many recursive calls are there to *WISNoMem*? Show the recursion tree to support your answer.

```
WISNoMem(j) {  
    if (j == 0)  
        return 0  
    else  
        return max(WISNoMem(j-1), v[j] + WISNoMem(p[j]))  
}
```

*Solution.*

Based on the recursion tree we have 4 recursive calls



Name: Jonathan Phouminh

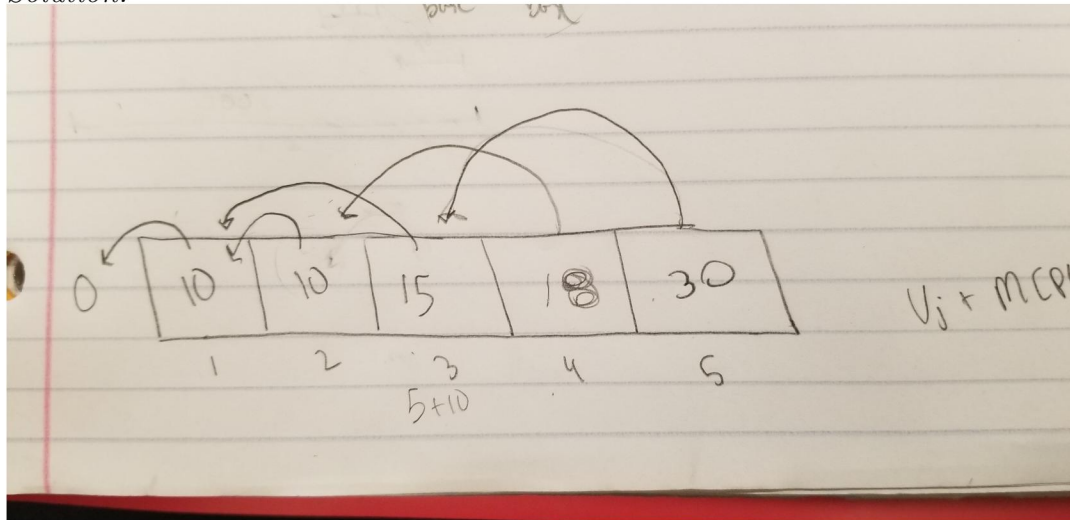
ID: 106054641

CSCI 3104, Algorithms  
Problem Set 10a (25 points)

Prof. Hoenigman & Agrawal  
Fall 2019, CU-Boulder

- (d) (3 pts) Using the bottom-up iterative algorithm presented in lecture, show the  $OPT(j)$  values for all requests. Also draw the arrows to show the previous sub-problem you used to fill an entry.

*Solution.*



- (e) (2 pts) Show which requests are selected in the optimal solution and the value of the solution. Provide a 2-3 sentence explanation of how you retrieved the solution using the arrows you drew.

*Solution.*

We find which requests were selected in the optimal solution by keeping track of indexes that arrows point to until the back traced arrow points to 0. In our example the first back traced arrow starts at index 5 then the next arrow points at index 3 then index 1, then finally to index 0. So the events selected in the optimal solution are events 5,3,1 which leaves the optimal subsets weight equal to 30 ( this can also be found by looking at the value in the last index of the array.

Name: Jonathan Phouminh

ID: 106054641

**CSCI 3104, Algorithms**  
**Problem Set 10a (25 points)**

**Profs. Hoenigman & Agrawal**  
**Fall 2019, CU-Boulder**

2. (14 pts) Solve the following sequence alignment questions.

- (a) (2 pts) Consider the sub-problem represented by  $i$  and  $j$  i.e.  $\text{cost}[i][j]$  which represents the minimum cost of aligning sub-sequences in the source and target respectively.

What are the smaller sub-problems needed to solve this sub-problem?

What operation do each of the smaller sub-problems represent **with respect to the source sequence**?

*Solution.*

The smaller sub-problems needed to solve subproblems are values that are already calculated for the three operations ( delete, sub, insert ). These operations represent the different manipulations we can perform between the source and the string and the cost of the operation will vary depending on the previous sub-problems cost.

Name: Jonathan Phouminh

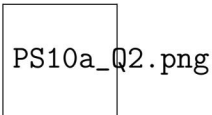
ID: 106054641

**CSCI 3104, Algorithms**  
**Problem Set 10a (25 points)**

**Profs. Hoenigman & Agrawal**  
**Fall 2019, CU-Boulder**

- (b) (4 pts) Consider the source sequence  $s = \text{BEAR}$ , the target sequence  $t = \text{BARE}$ , and the given cost table. **Draw the arrows that represent the optimal alignment** of  $s$  and  $t$ . You don't need to draw arrows which are not part of this optimal alignment.

(Note that you have to do the back tracing starting from the cell representing the solution to the full problem and traverse to the base case. You can infer the parent from observing the relevant sub-problems.)



**Also, draw the alignment corresponding to the arrows** for the given sequences  $s = \text{BEAR}$  and  $t = \text{BARE}$  and **give the set of optimal operations** on the  $s = \text{BEAR}$  which will transform it to  $t = \text{BARE}$  (using the cost table with relevant arrows you drew earlier).

An example drawn alignment and set of operations for  $s = \text{STEP}$  and  $t = \text{APE}$  look like following. (Show the 'no-op' using a colon (:) to differentiate with a regular sub.)

**Drawn alignment =**      **Ops =** ['sub', 'sub', 'no-op', 'delete']  
S T E P  
| | : |  
A P E \_

*Solution.*

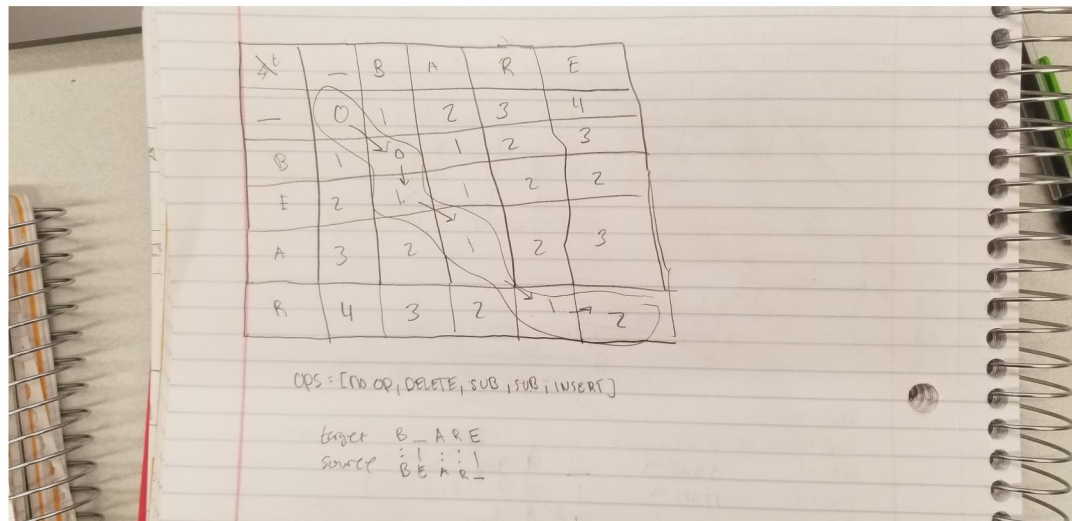


Name: Jonathan Phouminh

ID: 106054641

CSCI 3104, Algorithms  
Problem Set 10a (25 points)

Profs. Hoenigman & Agrawal  
Fall 2019, CU-Boulder



Ops = [no-op, DELETE, SUB, **1**UB, INSERT]

Target: B \_ A R E

: | : : |

Source: B E A R \_

Name: Jonathan Phouminh

ID: 106054641

CSCI 3104, Algorithms  
Problem Set 10a (25 points)

Profs. Hoenigman & Agrawal  
Fall 2019, CU-Boulder

(c) (8 pts) Consider the source sequence  $s = \text{PLAIN}$ , the target sequence  $t = \text{PLANE}$ ,  $\text{cost}(\text{insert}) = 2$ ,  $\text{cost}(\text{delete}) = 2$ , and  $\text{cost}(\text{sub}) = 2$ . Your goal is to align (or transform) the source to the target with minimum cost. Align the source sequence to the target sequence using a bottom-up tabular approach like the one shown on Q2 part b.

- Draw the DP table showing the cost of alignment.
  - Show the arrows representing the optimal alignment. Note that there are more than one optimal alignment. Show **two** of the optimal alignments in separate tables using arrows.
- One such example for different sequences and costs -

Example.jpeg

- Draw the alignments corresponding to the **two** optimal alignments like you drew in the last part of Q2 part b.
- Provide the cost of the optimal alignment.

target \ source		P	L	A	N	E	
	—	0	2	4	6	8	10
P	2	0	2	4	6	8	
L	4	2	0	2	4	6	
A	6	4	2	0	2	4	
I	8	6	4	2	2	4	
N	10	8	6	4	2	4	

Solution.

Source: P L A I N \_  
          : : : | : |  
Target: P L A \_ N E  
Cost = 4

Name: Jonathan Phouminh

ID: 106054641

**CSCI 3104, Algorithms**  
**Problem Set 10a (25 points)**

**Profs. Hoenigman & Agrawal**  
**Fall 2019, CU-Boulder**

---

COLLABORATED WITH: BAO NGUYEN , ZACH CHOMMALA