Geog 509 Chapter 2 Problem Set

Jesse Piburn 2020-01-27

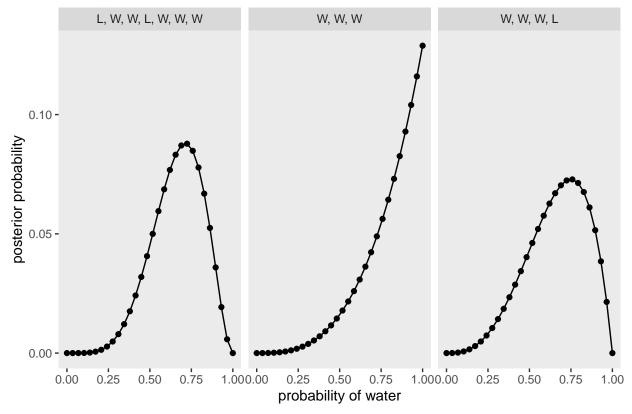
2E1

2 and 4 are both correct $\Pr(rain|monday)$ and $\frac{\Pr(rain|monday)}{\Pr(monday)}$

2M1

```
library(tidyverse)
tibble(
  label = c("W, W, W", "W, W, W, L", "L, W, W, L, W, W"),
     w = c(3, 3, 5),
     n = c(3, 4, 7),
     prior = 1
   ) %>%
  expand(
    nesting(w, n, prior, label),
    p_grid = seq(from = 0, to = 1, length.out = 30)
  ) %>%
  group_by(w, n) %>%
  mutate(
   likelihood = dbinom(w, size = n, prob = p_grid),
   unstd_posterior = likelihood * prior,
    posterior = unstd_posterior / sum(unstd_posterior)
  ggplot(aes(x = p_grid, y = posterior)) +
  geom_point() +
  geom_line() +
  labs(
    subtitle = "Grid Approximated Posterior Distrubtions",
    x = "probability of water",
    y = "posterior probability") +
  theme(panel.grid = element_blank()) +
facet_wrap(~label)
```

Grid Approximated Posterior Distrubtions



2H1

$$Pr(twins|A) = 0.1$$

$$Pr(twins|B) = 0.2$$

$$Pr(A) = 0.5$$

$$\Pr(B) = 0.5$$

$$\Pr(twins) = \Pr(twins|A) \Pr(A) + \Pr(twins|B) \Pr(B) = 0.1(0.5) + 0.2(0.5) = 0.15$$

$$\Pr(A|twins) = \frac{\Pr(twins|A)\Pr(A)}{\Pr(twins)} = \frac{0.1(0.5)}{0.15} = \frac{1}{3}$$

$$\Pr(B|twins) = \frac{\Pr(twins|B)\Pr(B)}{\Pr(twins)} = \frac{0.2(0.5)}{0.15} = \frac{2}{3}$$

$$\Pr(twins) = \Pr(twins|A)\Pr(A) + \Pr(twins|B)\Pr(B) = 0.1(\frac{1}{3}) + 0.2(\frac{2}{3}) = \frac{1}{6}$$

2H2

$$\Pr(A|twins) = \frac{\Pr(twins|A)\Pr(A)}{\Pr(twins)} = \frac{0.1(0.5)}{0.15} = \frac{1}{3}$$

2H3

$$\Pr(single|A) = 1$$
 $\Pr(twins|A) = 1$ $0.1 = 0.9$

$$Pr(single|B) = 1$$
 $Pr(twins|B) = 1$ $0.2 = 0.8$

$$\Pr(A) = \frac{1}{3}$$

$$\Pr(B) = \frac{2}{3}$$

$$\Pr(single) = \Pr(single|A)\Pr(A) + \Pr(single|B)\Pr(B) = 0.9(\frac{1}{3}) + 0.8(\frac{2}{3}) = \frac{5}{6}$$

$$\Pr(A|single) = \frac{\Pr(single|A)\Pr(A)}{\Pr(single)} = \frac{0.9(1/3)}{5/6} = 0.36$$