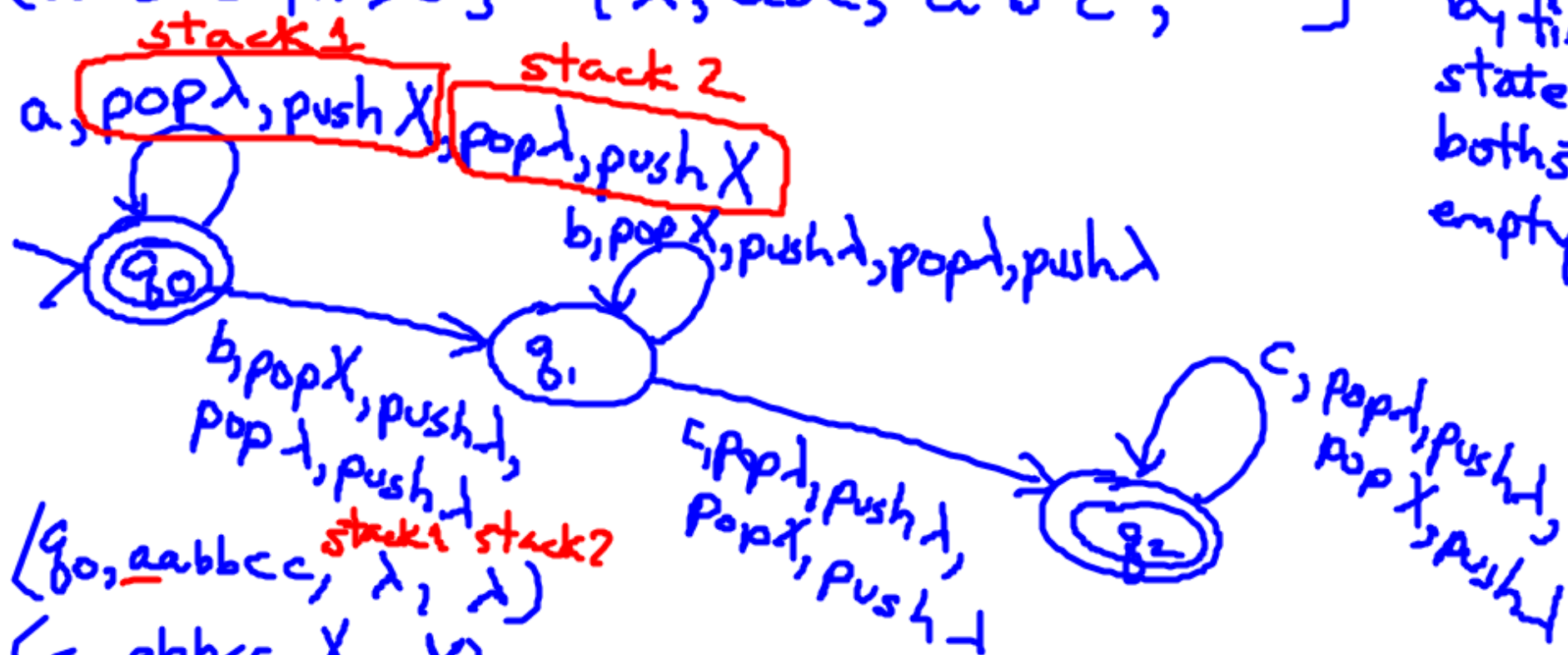


2-stack PDA  $\equiv$  FA + 2 stacks

$\{a^n b^n c^n \mid n \geq 0\} = \{\lambda, abc, a^2 b^2 c^2, \dots\}$

Acceptance  
by final  
state and  
both stacks  
empty



$(q_0, \underline{a}abbcc, \lambda, \lambda)$  stack 1 stack 2?

$(q_0, \underline{a}bbcc, X, X)$

$(q_0, \underline{b}bcc, XX, XX)$

$(q_1, \underline{b}cc, X, XX)$

$(q_1, \underline{c}, \lambda, XX)$

$(q_2, \underline{c}, \lambda, X)$

$(q_2, \lambda, \lambda, \lambda)$  ✓✓✓ accept

$$\{a^n b^m \mid m, n \geq 0, n \leq m \leq 2n\}$$

$$G = (N, \Sigma, P, S)$$

$$\begin{aligned} S &\rightarrow \lambda \\ S &\rightarrow a S b \\ S &\rightarrow a S b b \end{aligned}$$

Any CFG can be converted into an equivalent 1-stack PDA.

make transition

$$\delta(q_0, A) = \lambda$$

$$\delta(q_1, \text{pop } Z) = \lambda$$

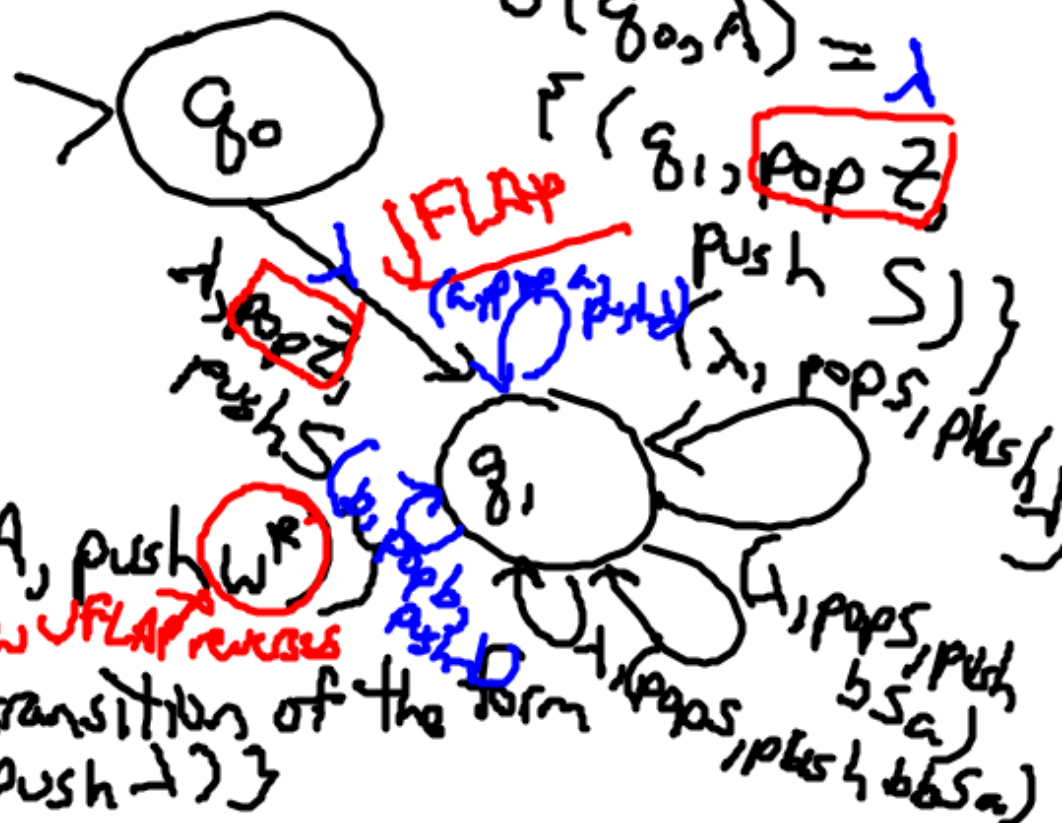
$$\delta(q_1, \text{push } S) = \lambda$$

For each rule  $A \rightarrow w \in P$   
make a transition of the form

$$\delta(q_1, A) = \{ (q_1, \text{pop } A, \text{push } w) \}$$

For each  $a \in \Sigma$ , make a transition of the form

$$\delta(q_1, a) = \{ (q_1, \text{pop } a, \text{push } \lambda) \}$$



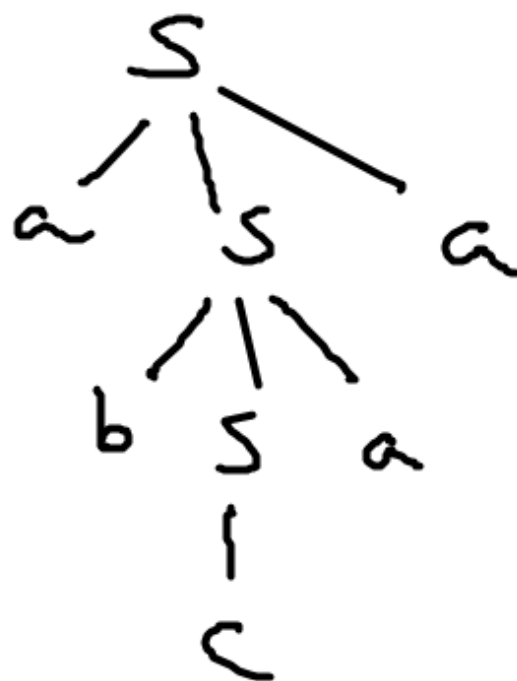
String  $x$  is a palindrome iff  $x = x^R$ .  
 6/14/16 ...

$$L(G) = \{ w c w^R \mid w \in \{a, b\}^* \}$$

$$S \rightarrow a S a$$

$$S \rightarrow b S b$$

$$S \rightarrow c$$



$$(xy)^R = y^R x^R$$

$$\boxed{(w c w^R)^R} =$$

$$| \quad (w^R)^R \quad c^R \quad w^R =$$

$$\boxed{w c w^R}$$



$$\text{Let } L = \{x \in \Sigma^* \mid \exists w \in \Sigma^* \mid x = ww^R\} \quad \text{even length palindromes}$$

$$\Sigma = \{a, b\}$$

$$x^R = (ww^R)^R =$$

$$(w^R)^R w^R = ww^R = x$$

$$L_{\text{allPalindromes}} = \{x \in \Sigma^* \mid x = x^R\}$$

$$S \rightarrow aSa$$

$$S \rightarrow bSb$$

$$S \rightarrow \lambda$$

$$S \rightarrow a \quad S \rightarrow b \quad \text{for odd length palindromes}$$

$$L_{\text{oddPalindromes}} = \{x \in \Sigma^* \mid \exists w \in \Sigma^* \mid x = wcw^R \text{ for some } c \text{ in } \Sigma\}$$

Derivation in PDA's

$$(q_i, \underbrace{aw}_{\substack{\text{what's left} \\ \text{to consume}}}, \underbrace{Ay}_{\substack{\text{full stack}}}) \xrightarrow{m} (\tilde{q}_i, \underbrace{w}_{\substack{\text{what's left}}}, \underbrace{By}_{\substack{\text{full stack}}})$$

$\uparrow$  where we are     $\uparrow$  current char.     $\uparrow$  top of stack     $\uparrow$  where to go     $\uparrow$  what's left     $\uparrow$  new top.

$$a \in \Sigma \cup \{\lambda\}$$

$$aw \in \Sigma^*$$

$$A \in \Gamma \cup \{\lambda\}$$

$$Ay \in \Gamma^*$$

$$B \in \Gamma \cup \{\lambda\}$$

$$q_i, \tilde{q}_i \in Q$$

When  $\delta(q_i, a, A)$  contains  $(q_j, B)$

$\uparrow$  where we are     $\uparrow$  char/ $\lambda$      $\uparrow$  what to pop A     $\uparrow$  where to go     $\uparrow$  what to push/ $\lambda$



appears in picture

p.222  $(q_j, B) \in \delta(q_i, a, A)$ .