

$$\chi^2 = (\alpha_{12} - A_1 + A_2)^2 + (\alpha_{23} - A_2 + A_3)^2 + \dots \quad (1)$$

$$(\beta_{12} - B_1 + B_2)^2 + (\beta_{23} - B_2 + B_3)^2 + \dots \quad (2)$$

$$(T_1 - A_1 + B_1)^2 + (T_2 - A_2 + B_2)^2 + \dots \quad (3)$$

$$\frac{1}{2} \frac{\partial \chi^2}{\partial A_2} = (\alpha_{12} - A_1 + A_2) - (\alpha_{23} - A_2 + A_3) - (T_2 - A_2 + B_2) = 0 \quad (4)$$

$$\begin{pmatrix} 0 \\ \alpha_{23} - \alpha_{12} + T_2 \\ \alpha_{34} - \alpha_{23} + T_3 \\ \alpha_{45} - \alpha_{34} + T_4 \\ \alpha_{51} - \alpha_{45} + T_5 \\ \beta_{12} - \beta_{51} + T_1 \\ \beta_{23} - \beta_{12} + T_2 \\ \beta_{34} - \beta_{23} + T_3 \\ \beta_{45} - \beta_{34} + T_4 \\ \beta_{51} - \beta_{45} + T_5 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 3 & -1 & & & & -1 & & & \\ & -1 & 3 & -1 & & & & -1 & & \\ & & -1 & 3 & -1 & & & & -1 & \\ -1 & & & -1 & 3 & & & & & -1 \\ -1 & & & & & 3 & -1 & & & -1 \\ & -1 & & & & -1 & 3 & -1 & & \\ & & -1 & & & & -1 & 3 & -1 & \\ & & & -1 & & & -1 & 3 & -1 & \\ & & & & -1 & -1 & & -1 & 3 & \end{pmatrix} \begin{pmatrix} A_1 \\ A_2 \\ A_3 \\ A_4 \\ A_5 \\ B_1 \\ B_2 \\ B_3 \\ B_4 \\ B_5 \end{pmatrix}$$