

# Multi-Objective, Machine-Learning Assisted First-Principles Design of Transition Metal Complexes for Redox Couples

Jon Paul Janet <sup>1</sup>   Heather Kulik <sup>1</sup>

<sup>1</sup>Department of Chemical Engineering, Massachusetts Institute of Technology



Applications of Data Science in Molecular Sciences I

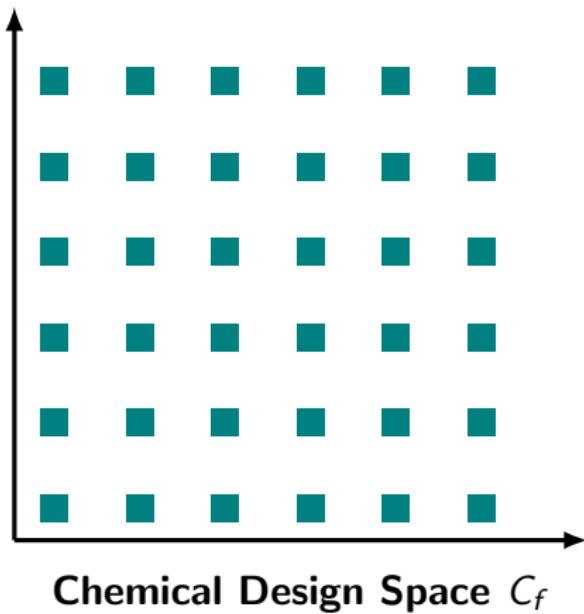
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# Motivation: chemical discovery

**How can we design new materials using computers?**

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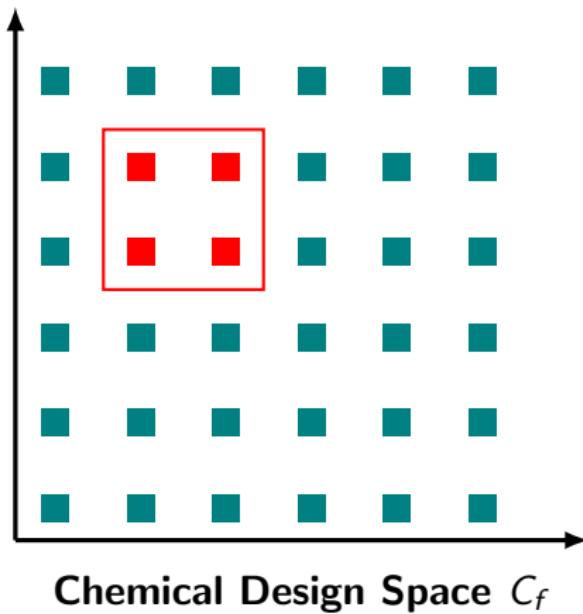
How can we design new materials using computers?



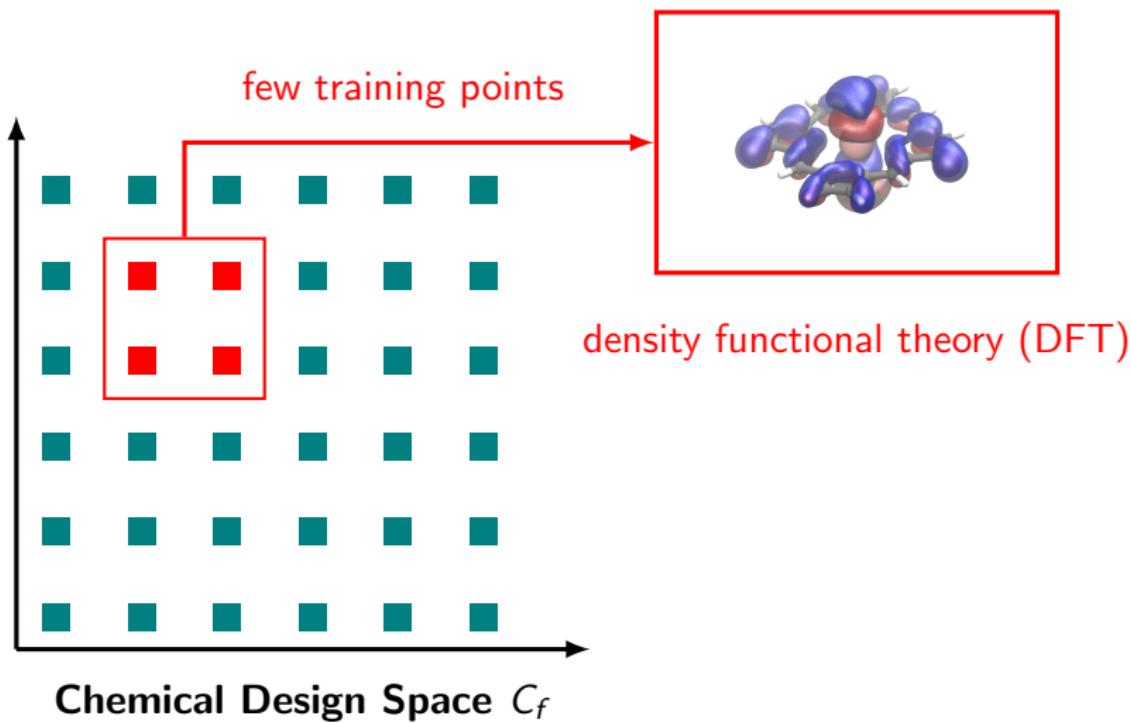
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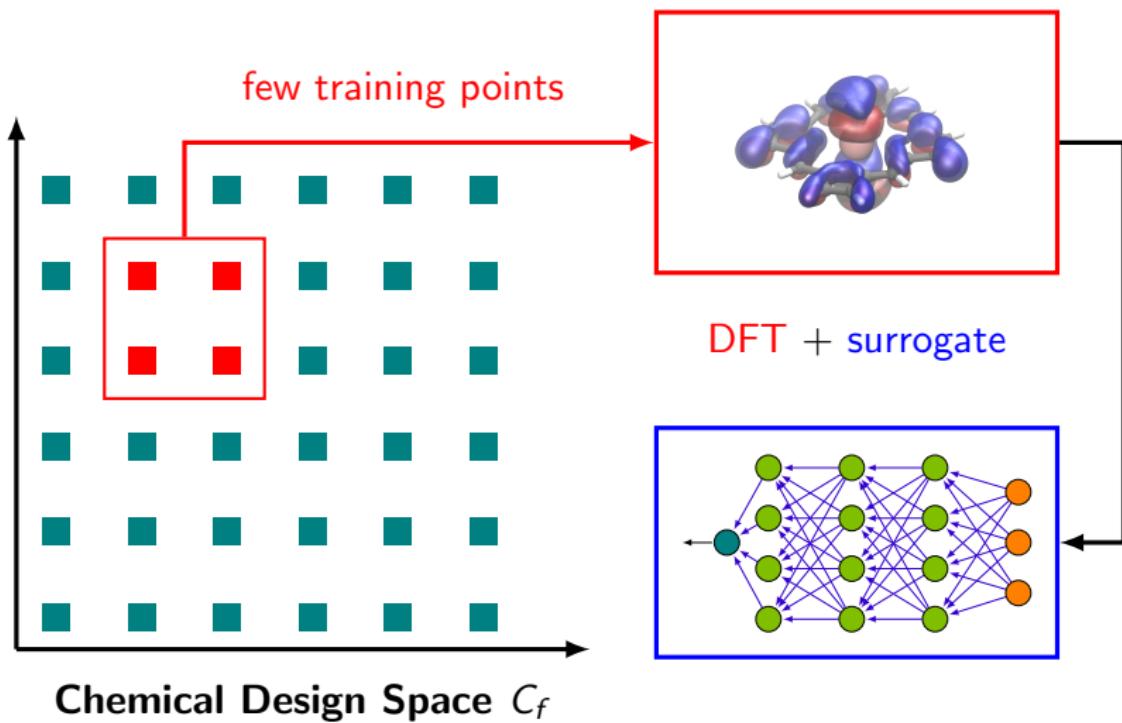
few training points



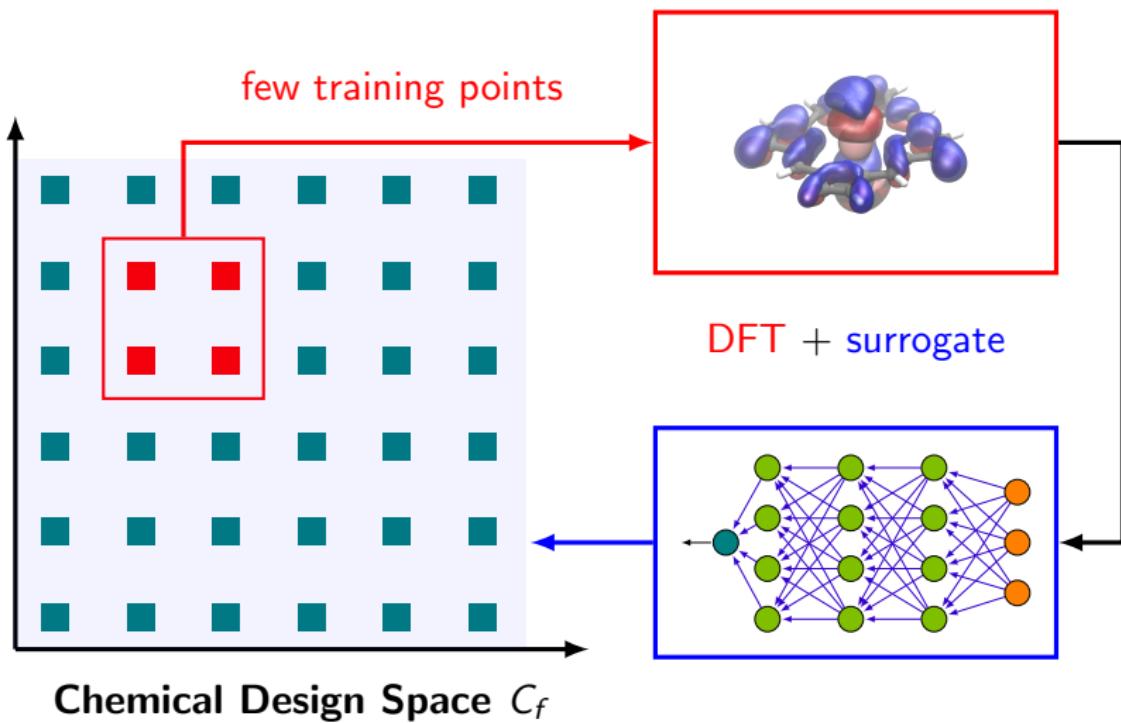
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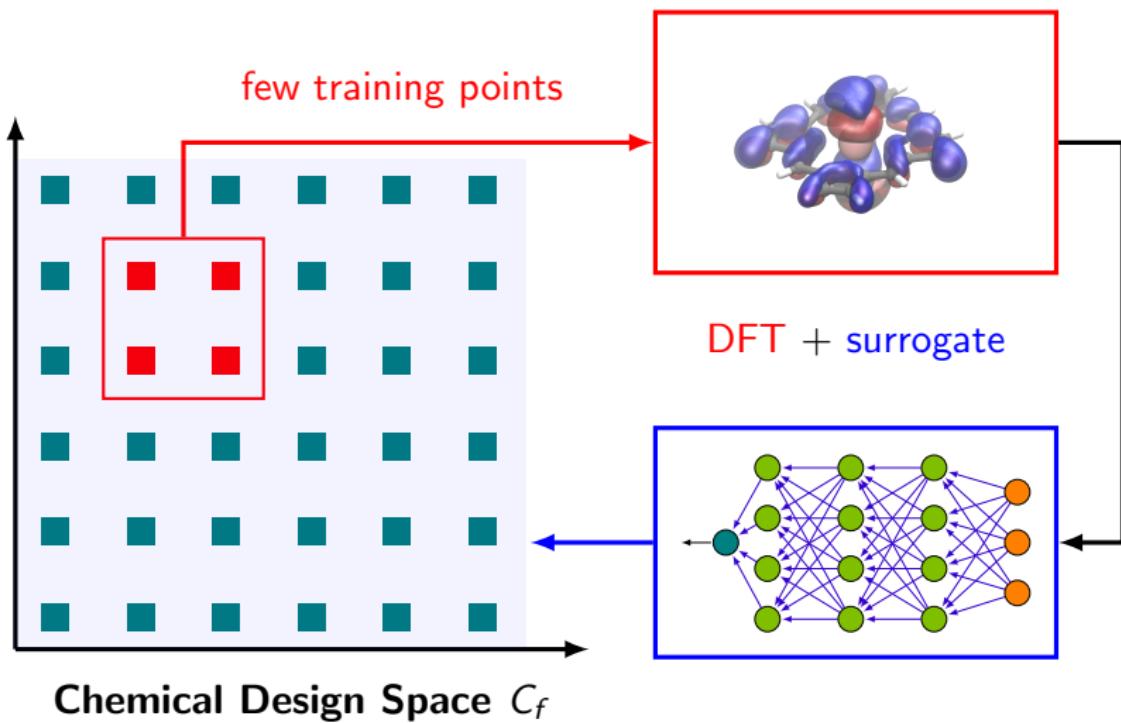
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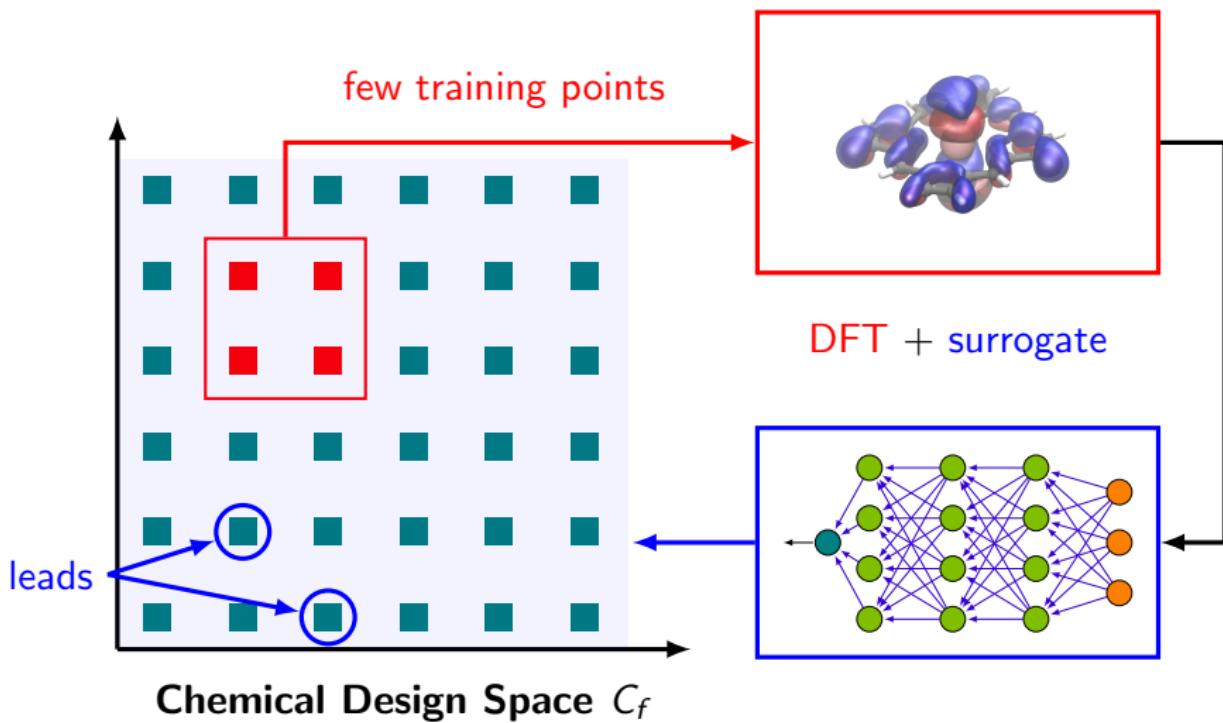
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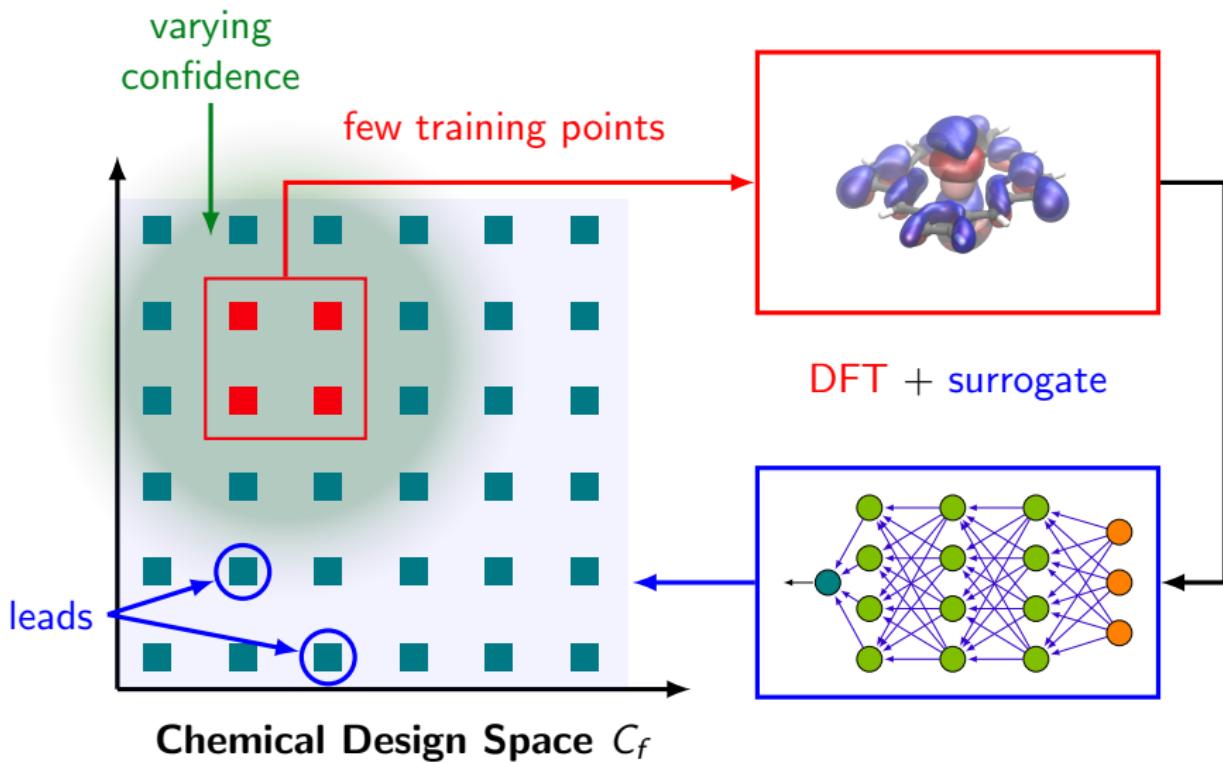
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Introduction

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Methods

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Designing RFBs

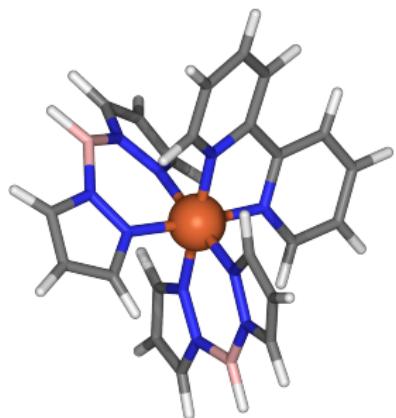
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Conclusions

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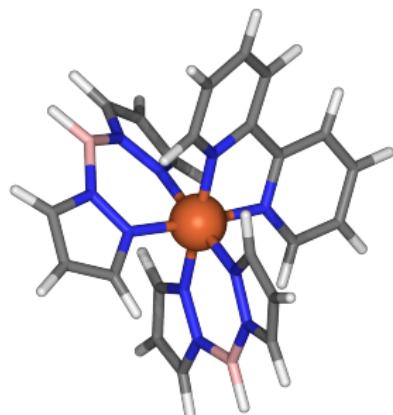
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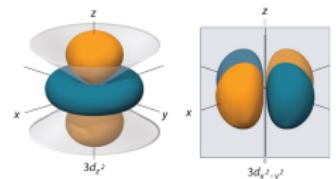
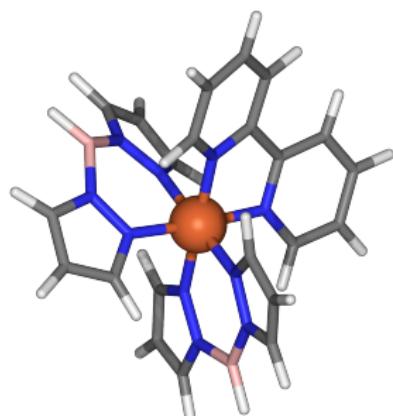
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Difficult chemistry with multiple spin & oxidation states!



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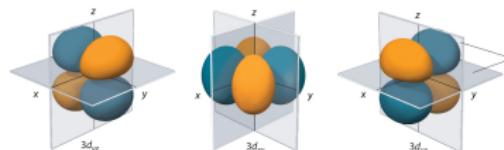
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e<sub>g</sub>

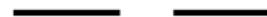
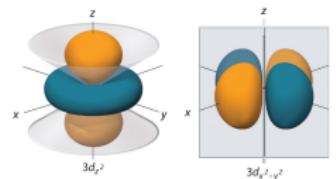
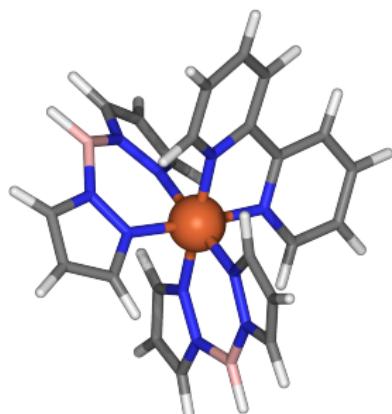


t<sub>2g</sub>



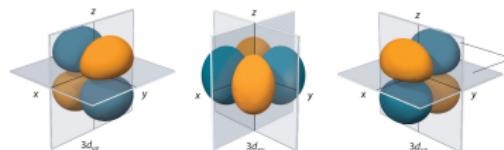
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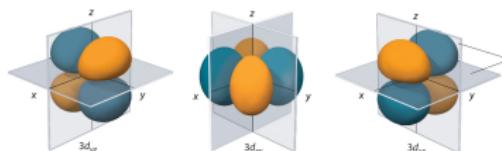
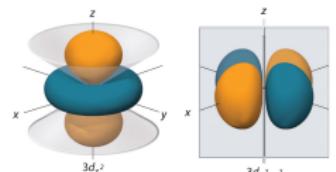
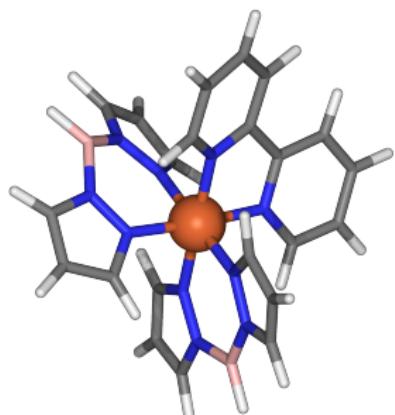
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1 ↑ 1 ↑ 1 t<sub>2g</sub>



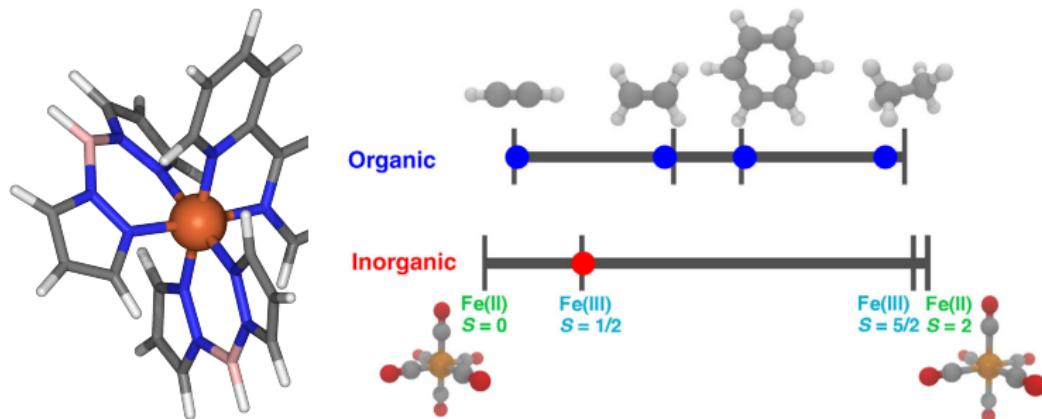
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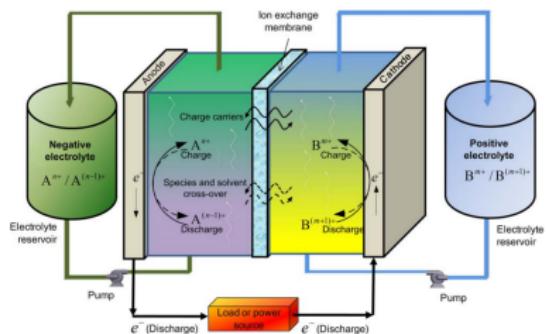


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Redox flow batteries (RFBs)  
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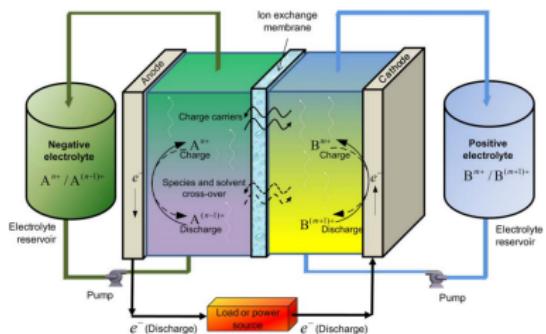
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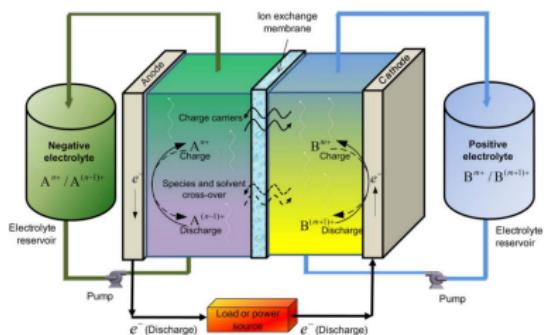


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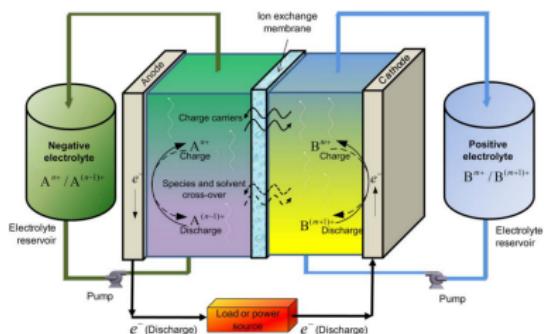
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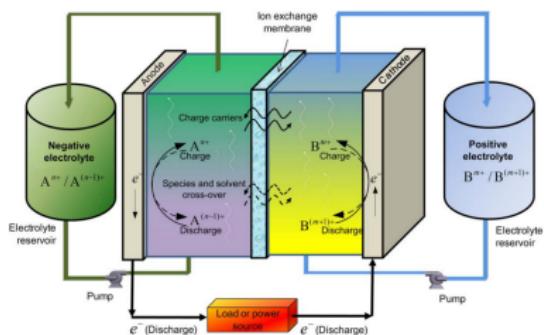
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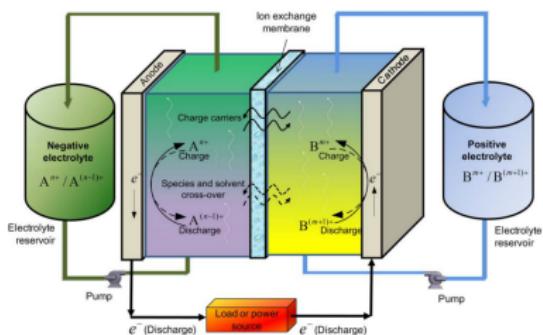
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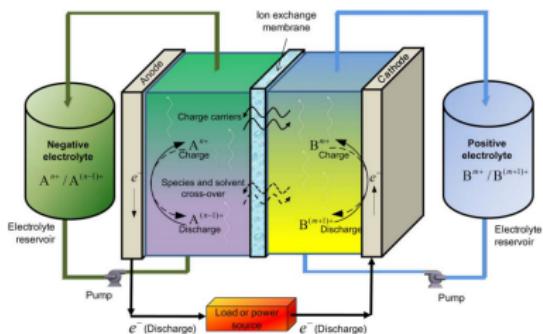
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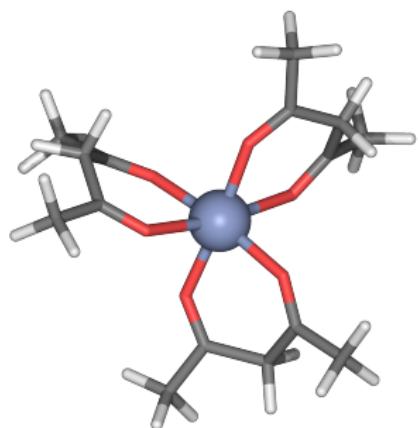
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We need complexes that have high redox potential **and** good solubility

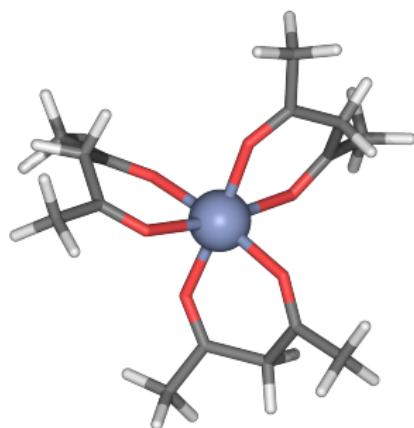
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# First principles methods

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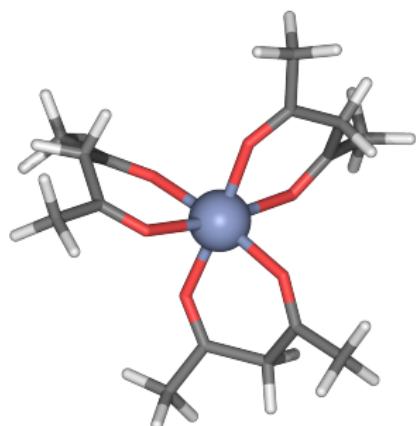
# First principles methods



Metals:

Cr	Mn	Fe	Co
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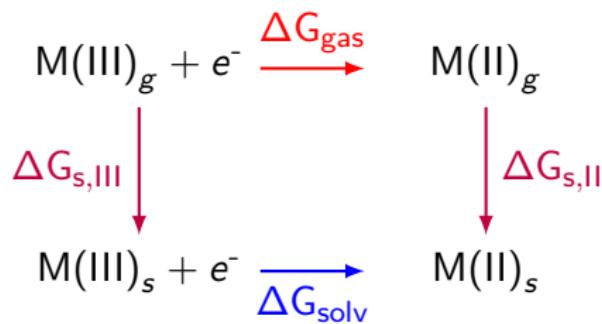
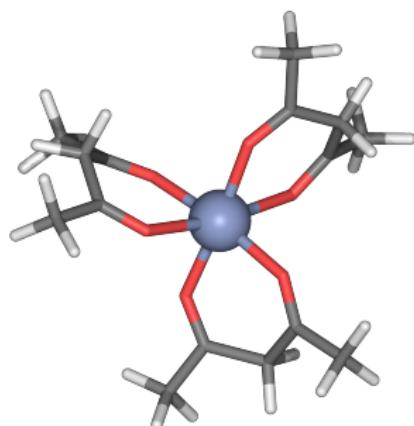
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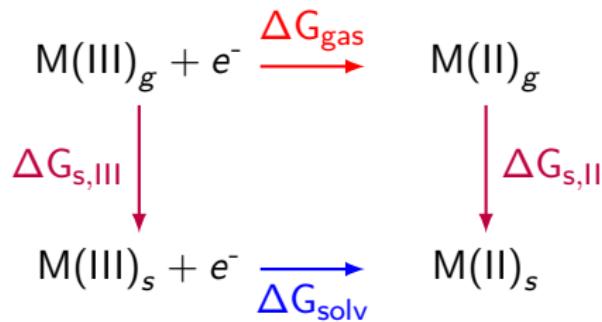
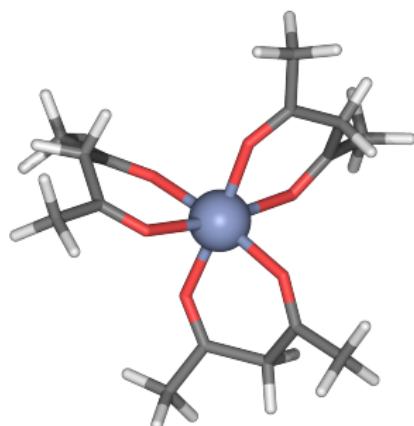
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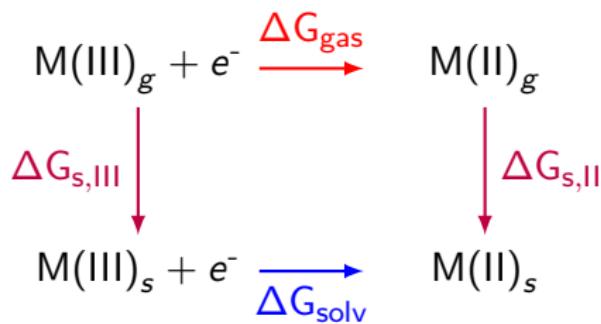
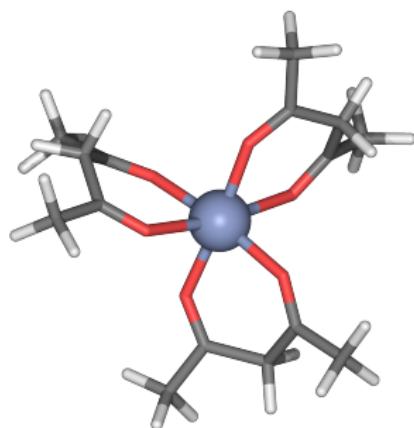


$$\log P \approx \log \frac{\Delta G_{s,\text{II},\text{octanol}}}{\Delta G_{s,\text{II},\text{water}}}$$

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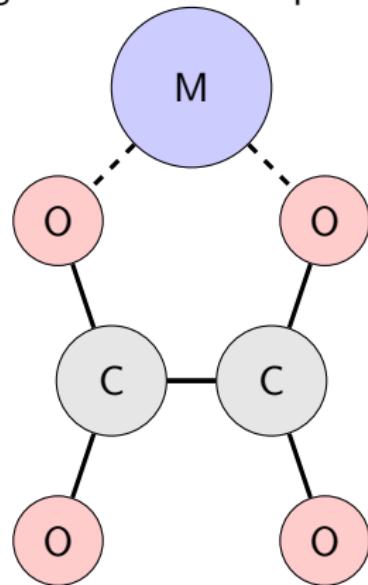
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- B3LYP-like DFT
- gas phase optimizations
- LANL2DZ/6-31G\*
- COSMO solvent,  $\varepsilon = 78.39$  or  $10.30$
- high- and low-spin

# Machine learning methods

## Featurization:

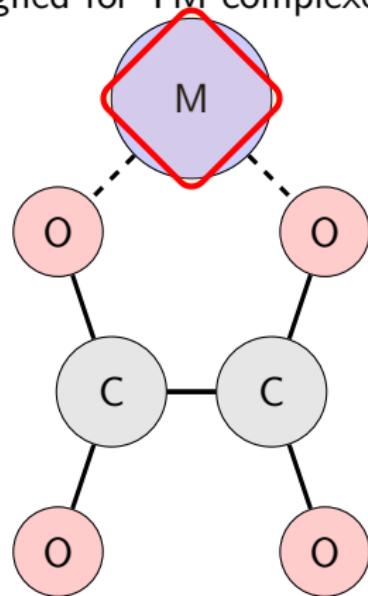
Graph-based features (RACs)  
designed for TM complexes:



# Machine learning methods

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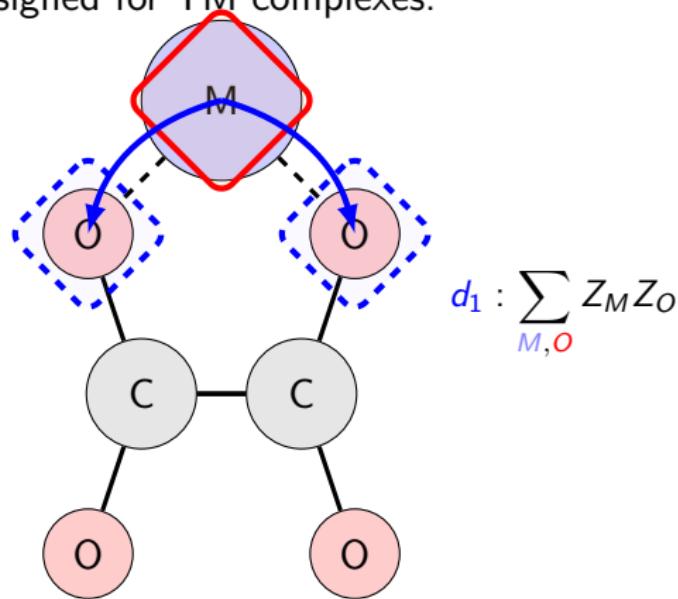
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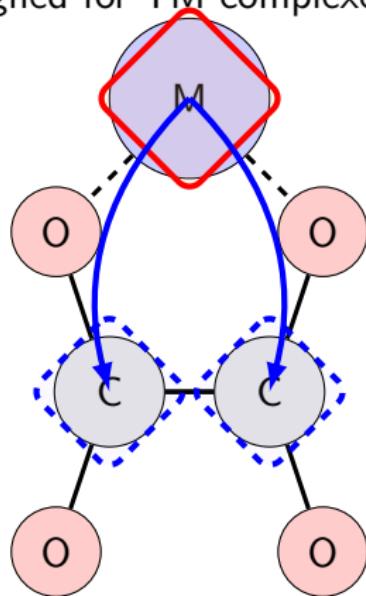
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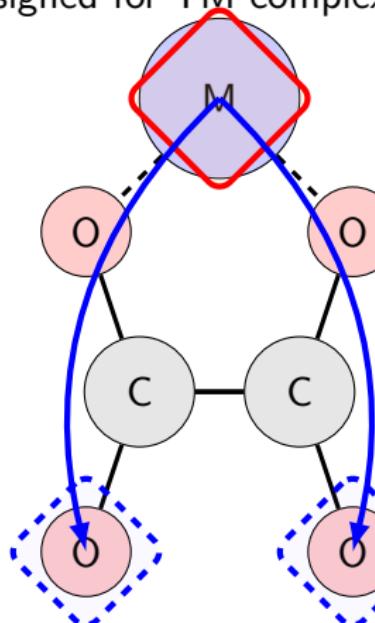
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$$d_2 : \sum_{M,C} Z_M Z_C$$

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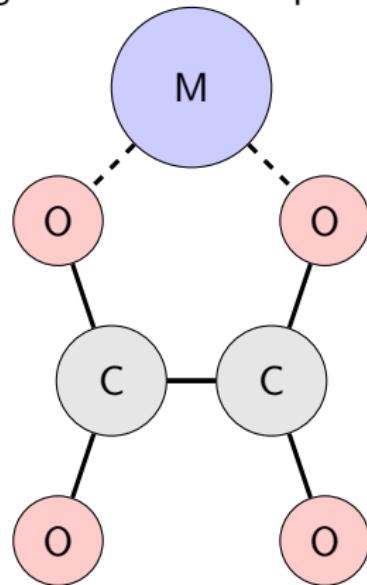
$$d_2 : \sum_{M,C} Z_M Z_C$$

$$d_3 : \sum_{M,O} Z_M Z_O$$

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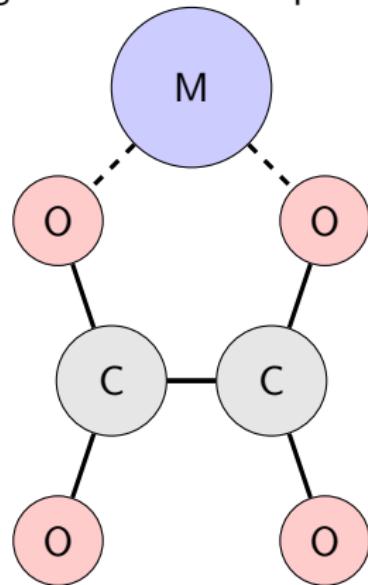


## Regression:

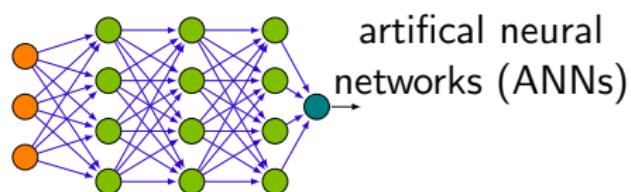
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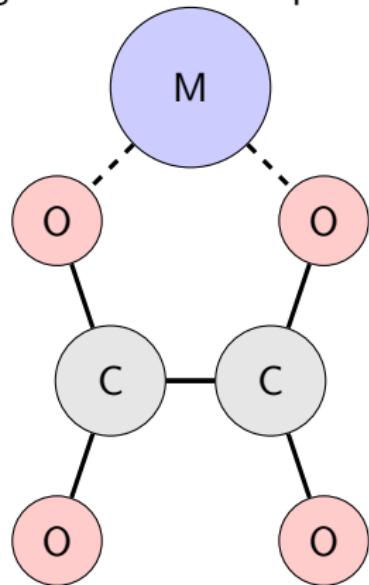


artifical neural  
networks (ANNs)

# Machine learning methods

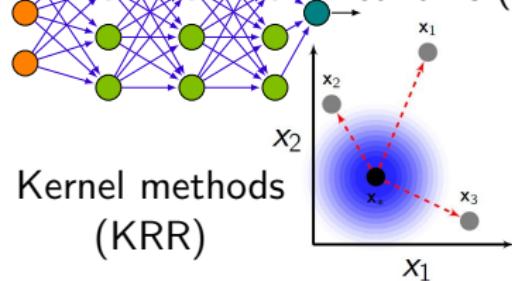
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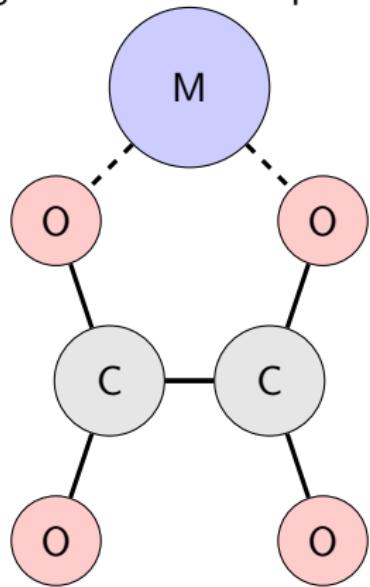


Kernel methods  
(KRR)

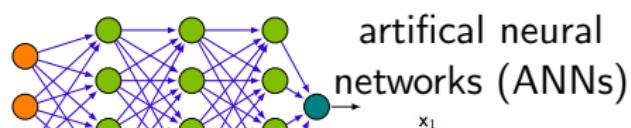
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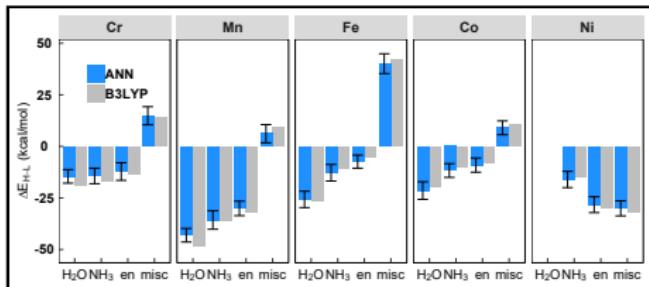


## Regression:



Kernel methods  
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spin splitting energies



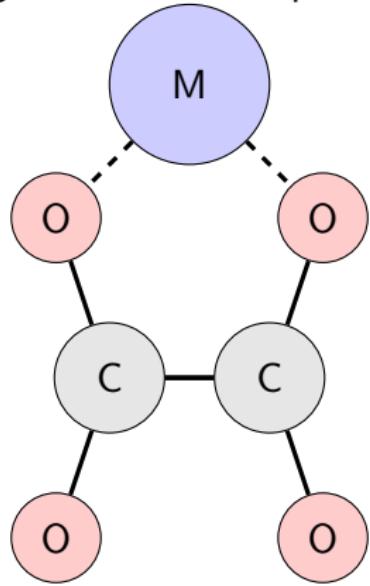
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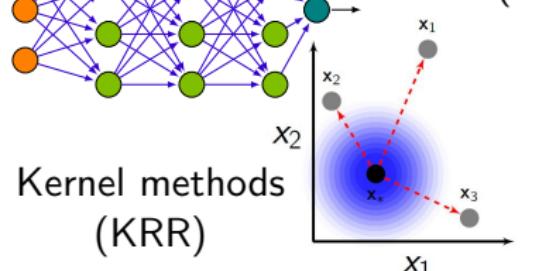
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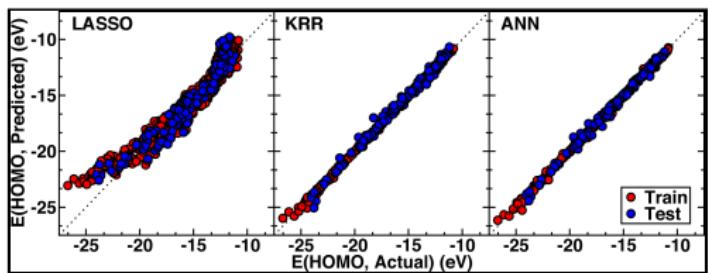
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Introduction  
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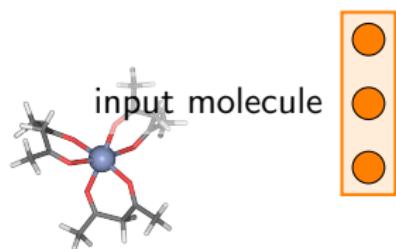
Methods  
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Designing RFBs  
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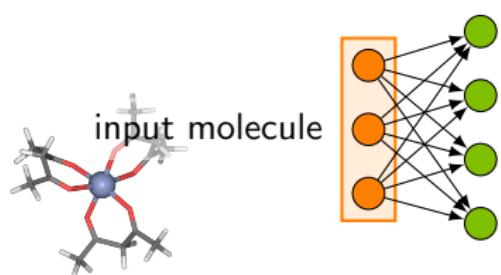
Conclusions  
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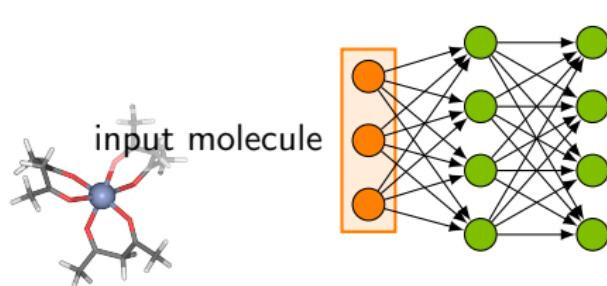
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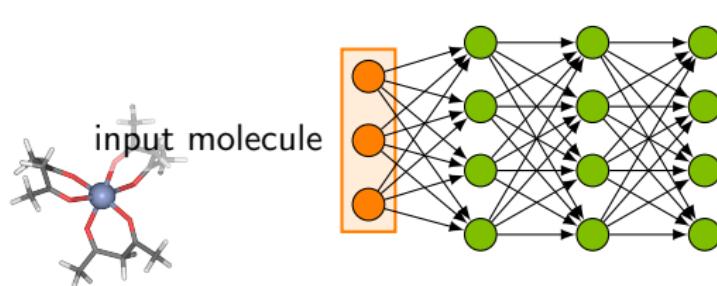
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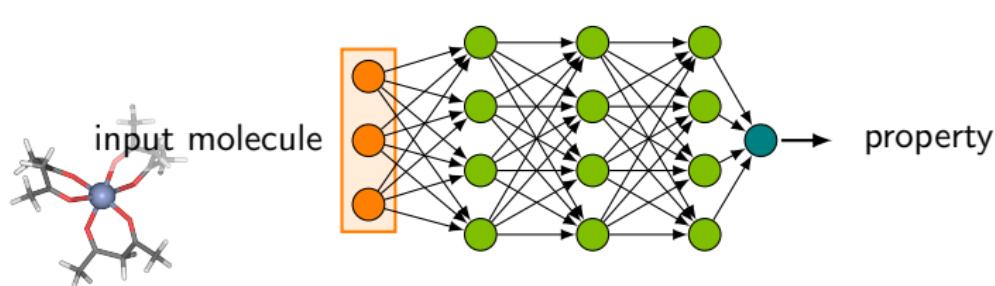
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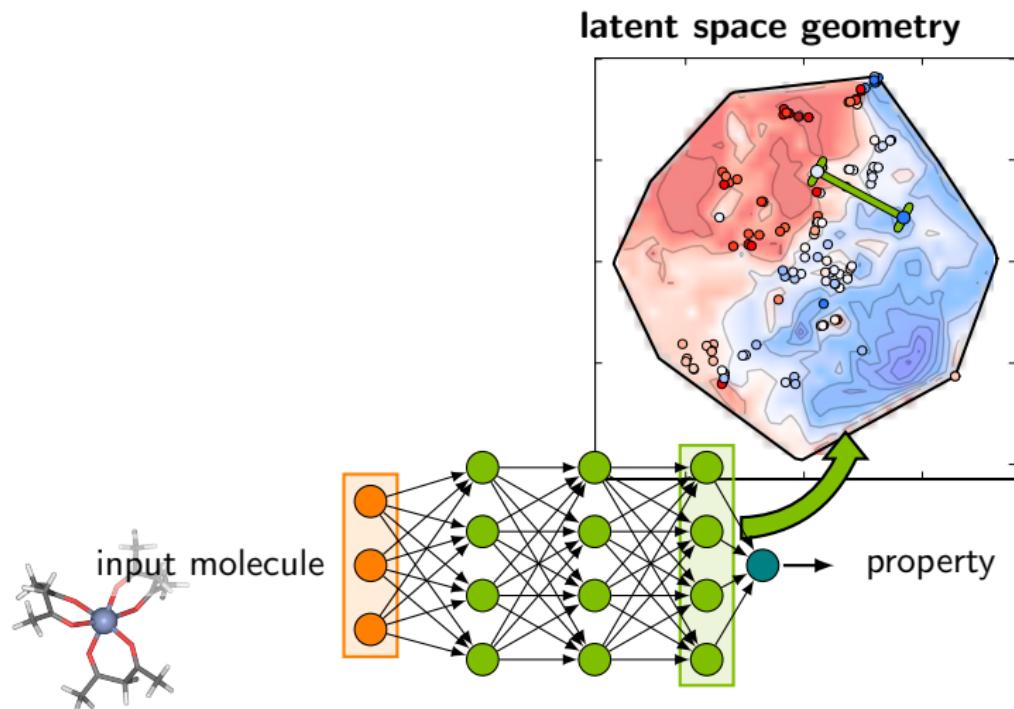
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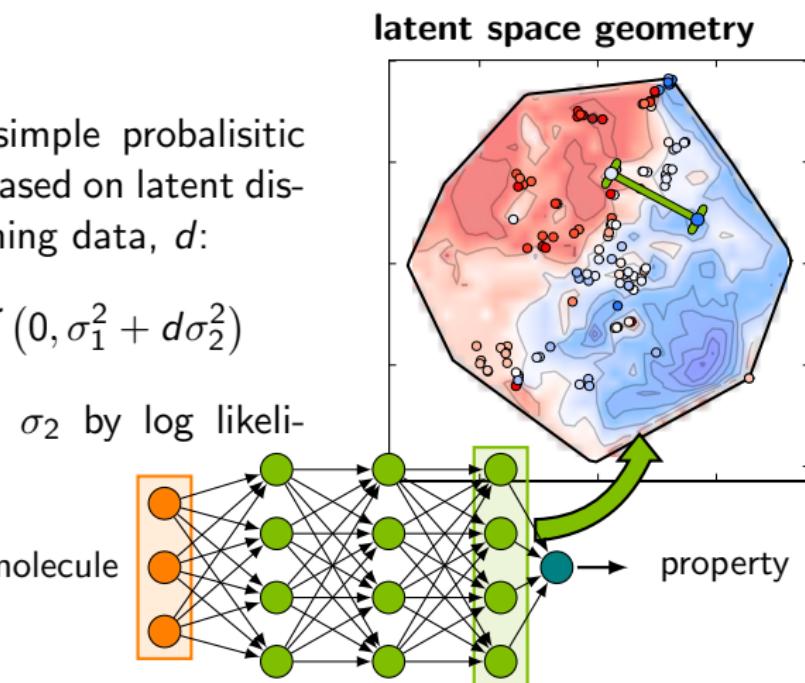
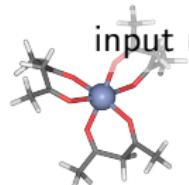


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Proposed a simple probabilistic error model based on latent distance to training data,  $d$ :

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Estimate  $\sigma_1$ ,  $\sigma_2$  by log likelihood

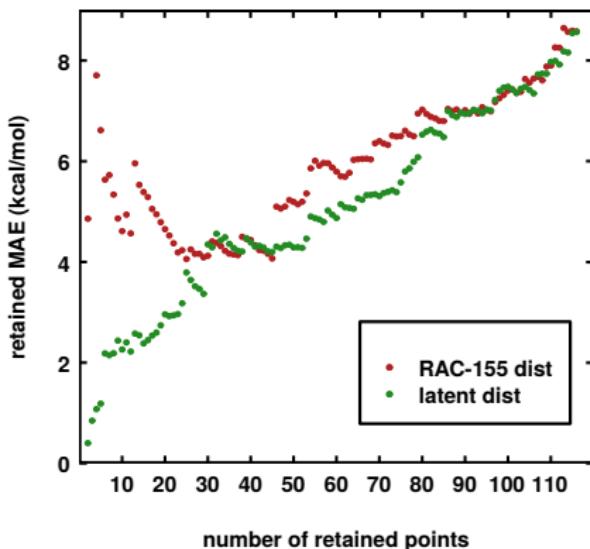


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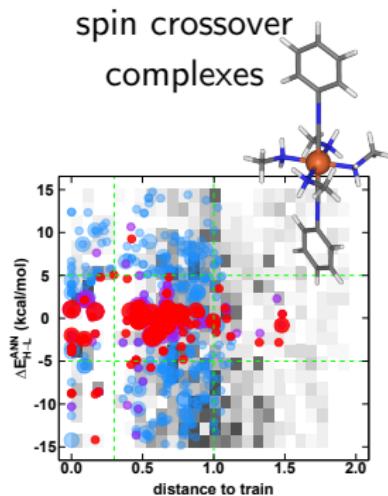


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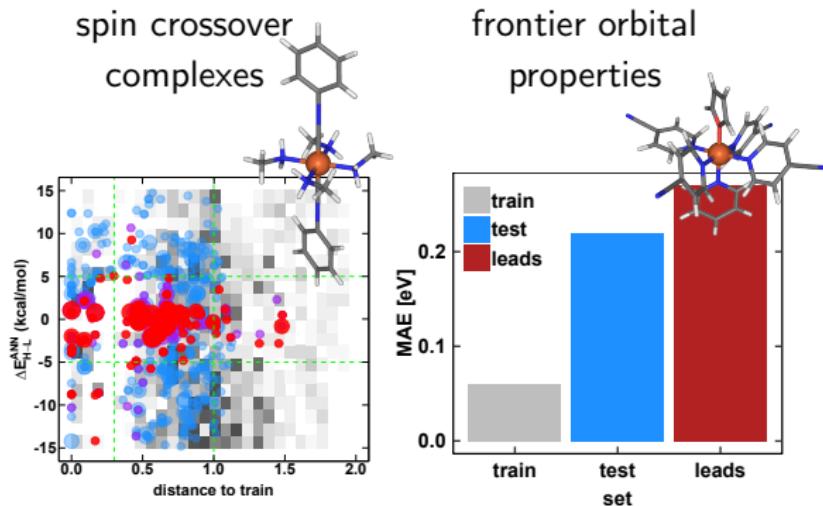
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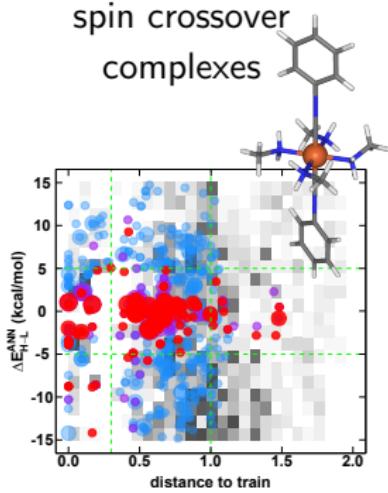


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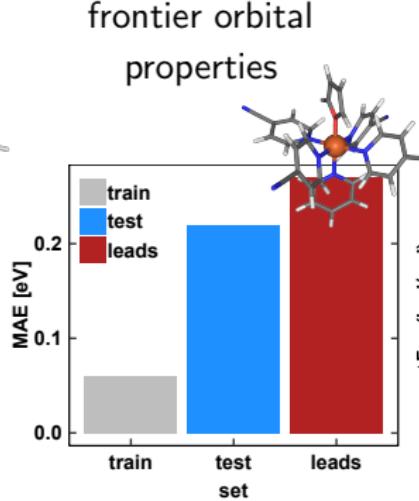
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We have used evolutionary algorithms for uncertainty-aware design for TM complexes:

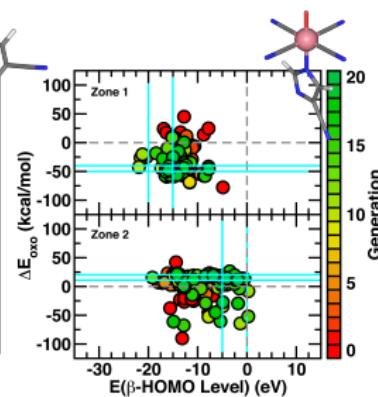
spin crossover  
complexes



frontier orbital  
properties



unusual catalytic  
reaction energies

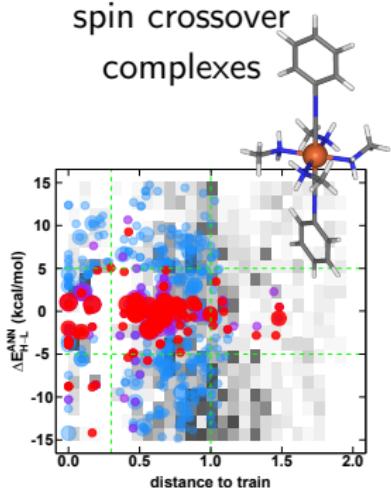


- Janet, J.P., Chan, L. and Kulik, H.J., *J. Phys. Chem. Lett.*, 9(5):1064–1071, 2018.  
Nandy, A. et al., *Ind. Eng. Chem. Res.*, 57(42):13973–13986, 2018.  
Nandy, A. et al., *ACS Catal.*, 9(9):8243–8255, 2019.

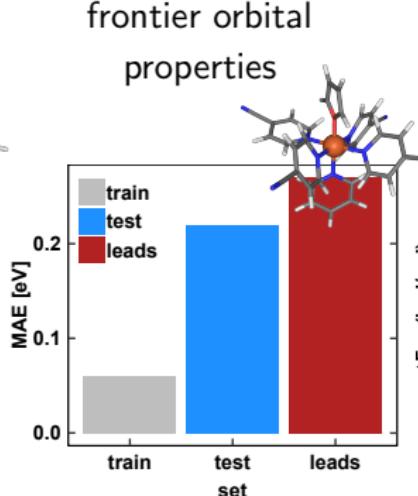
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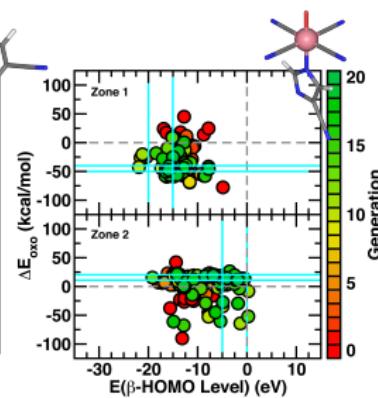
spin crossover  
complexes



frontier orbital  
properties



unusual catalytic  
reaction energies



443e: Aditya Nandy: Wednesday, 9:12 (Peacock Spring)

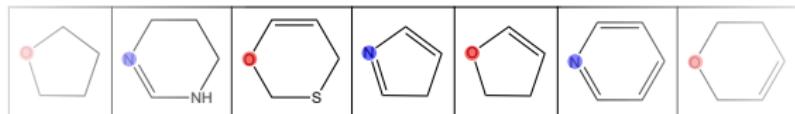
# A design space for RFBs

# A design space for RFBs



# A design space for RFBs

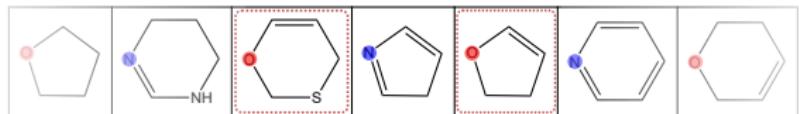
$\mathcal{O}(10^1)$



40 heterocycles

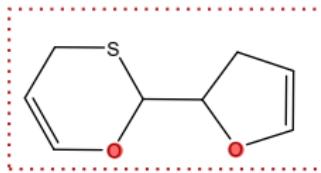
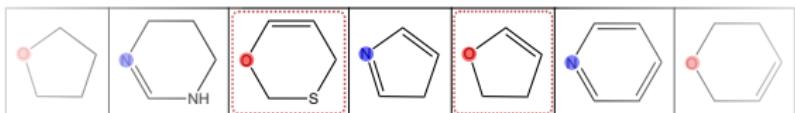
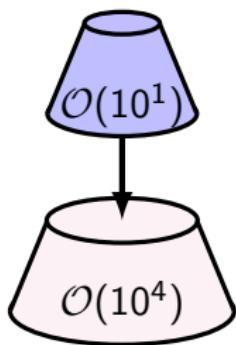
# A design space for RFBs

$\mathcal{O}(10^1)$



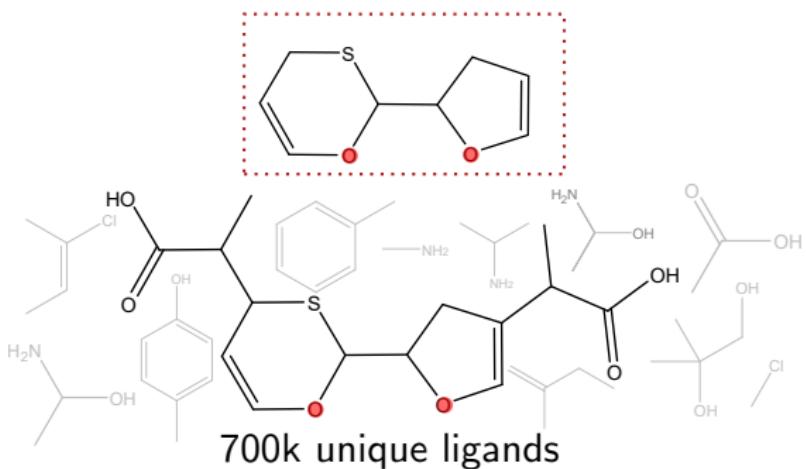
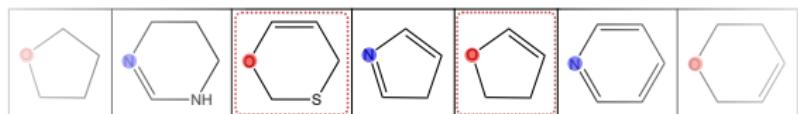
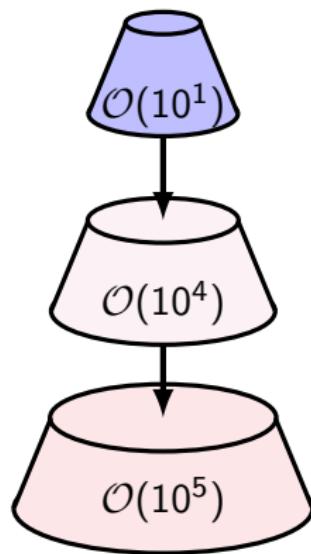
40 heterocycles

# A design space for RFBs

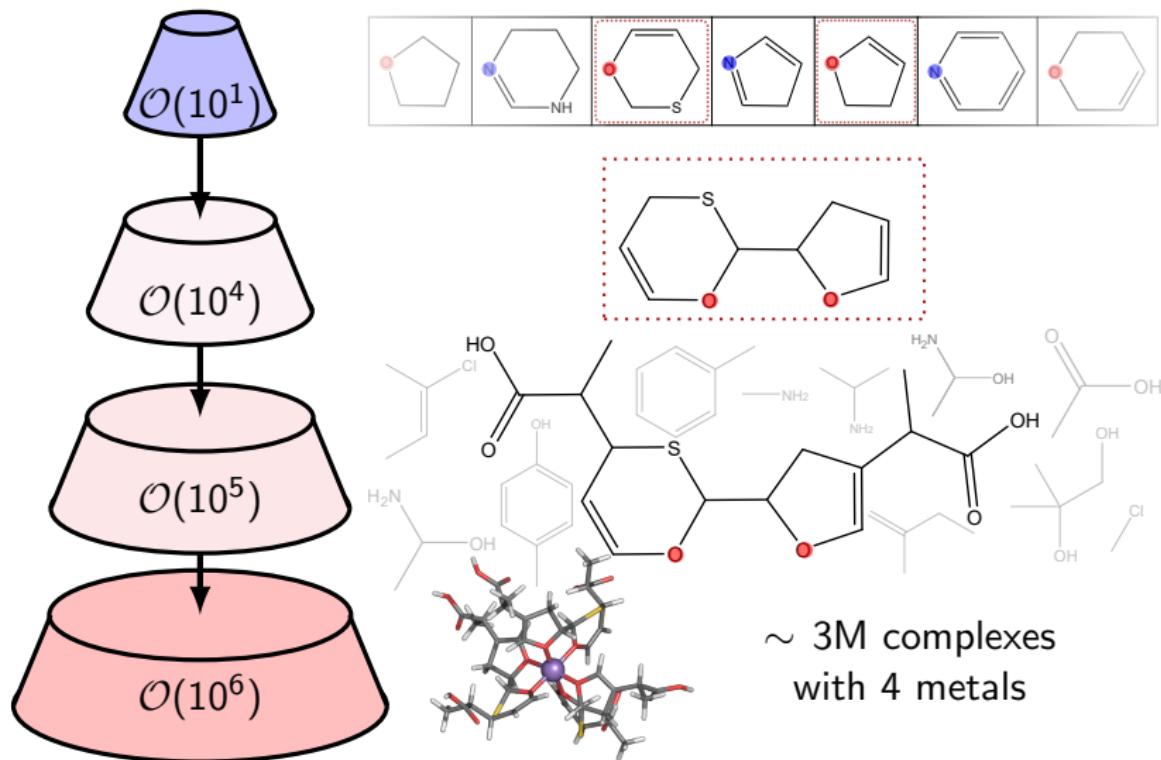


800 base ligands

# A design space for RFBs



# A design space for RFBs

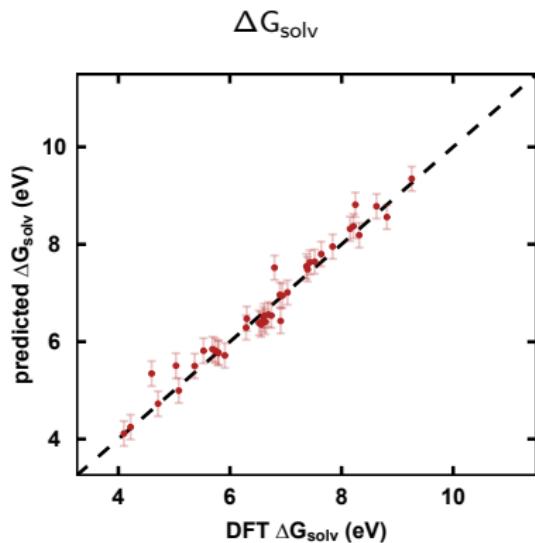


# Multiobjective optimization

We can predict quantites of interest for our RFBs:

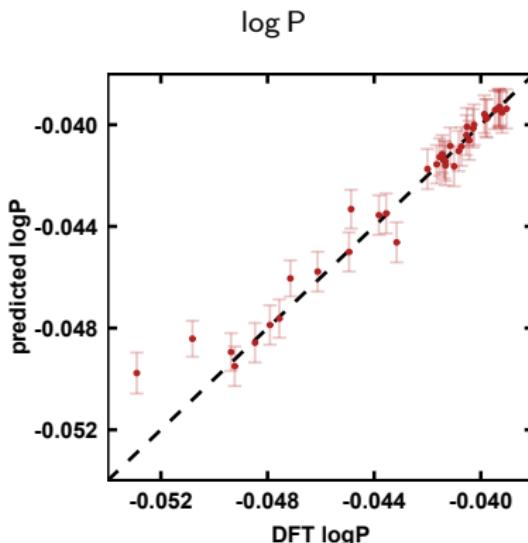
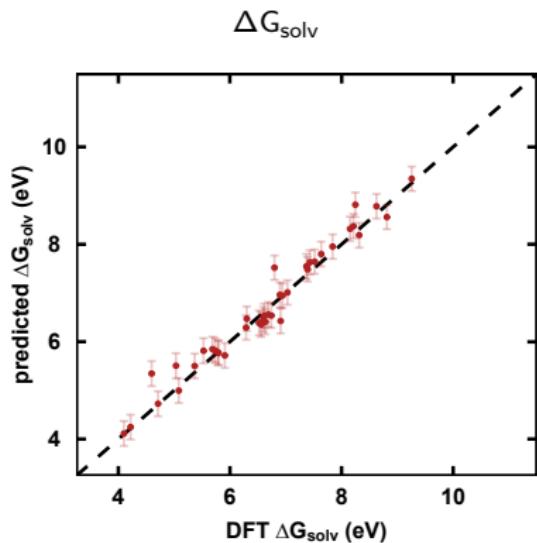
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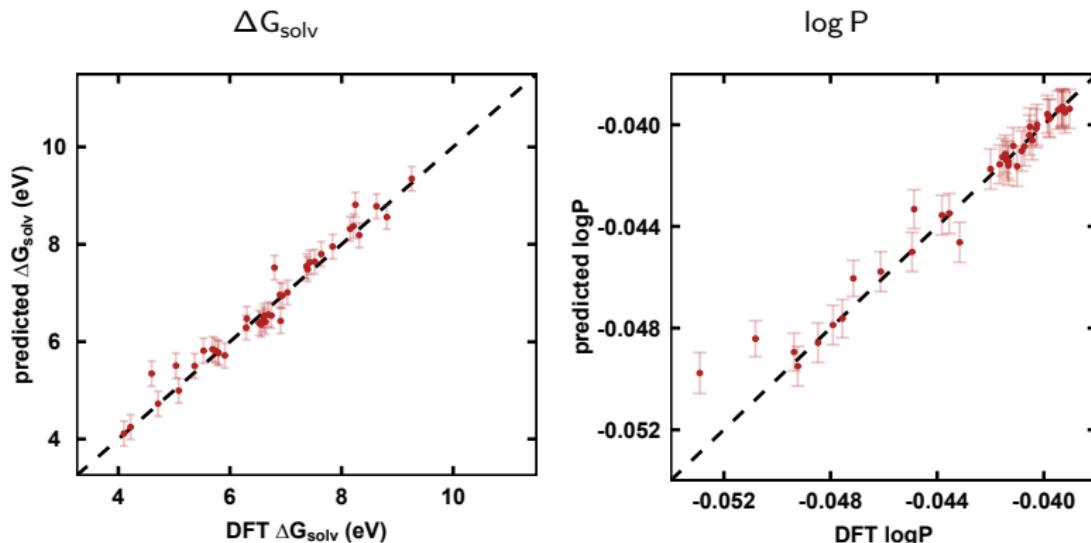
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# Multiobjective optimization

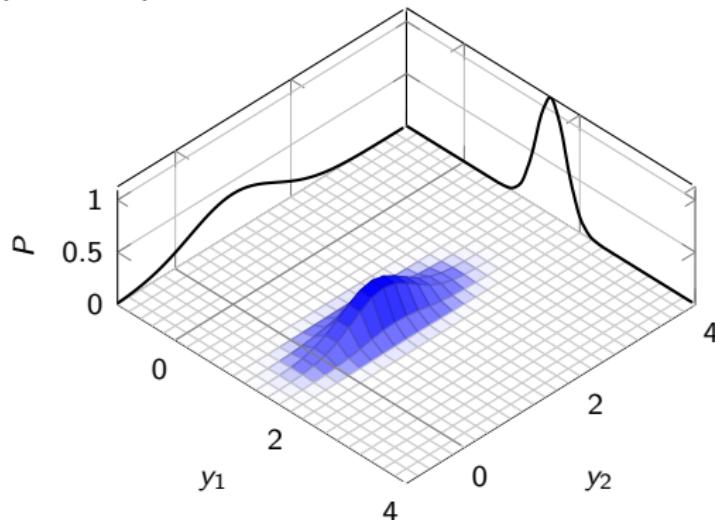
We can predict quantities of interest for our RFBs:



$$\begin{bmatrix} \Delta G_{\text{solv}} \\ \log P \end{bmatrix} = \begin{bmatrix} \hat{y}_1 \\ \hat{y}_2 \end{bmatrix} \sim \mathcal{N} \left( \begin{bmatrix} \hat{\mu}_1 \\ \hat{\mu}_2 \end{bmatrix}, \begin{bmatrix} \hat{\sigma}_1^2 & 0 \\ 0 & \hat{\sigma}_2^2 \end{bmatrix} \right)$$

# Multiobjective optimization

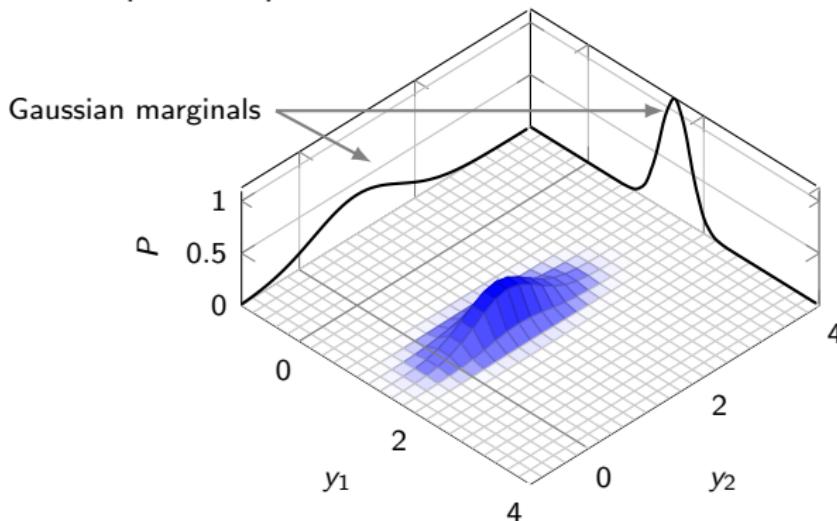
We can predict quantites of interest for our RFBs:



$$\Delta G_{\text{solv}} = \begin{bmatrix} \hat{y}_1 \\ \hat{y}_2 \end{bmatrix} \sim \mathcal{N} \left( \begin{bmatrix} \hat{\mu}_1 \\ \hat{\mu}_2 \end{bmatrix}, \begin{bmatrix} \hat{\sigma}_1^2 & 0 \\ 0 & \hat{\sigma}_2^2 \end{bmatrix} \right)$$

# Multiobjective optimization

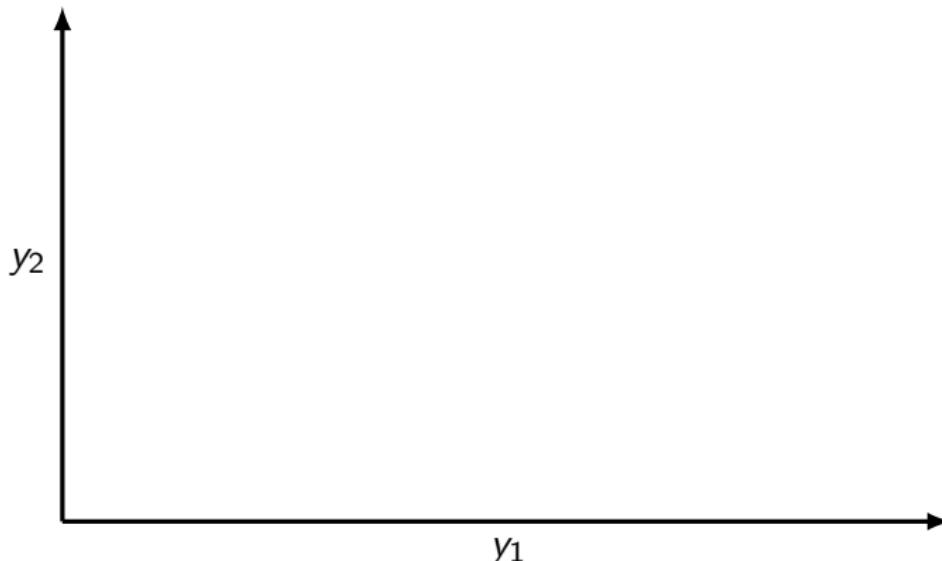
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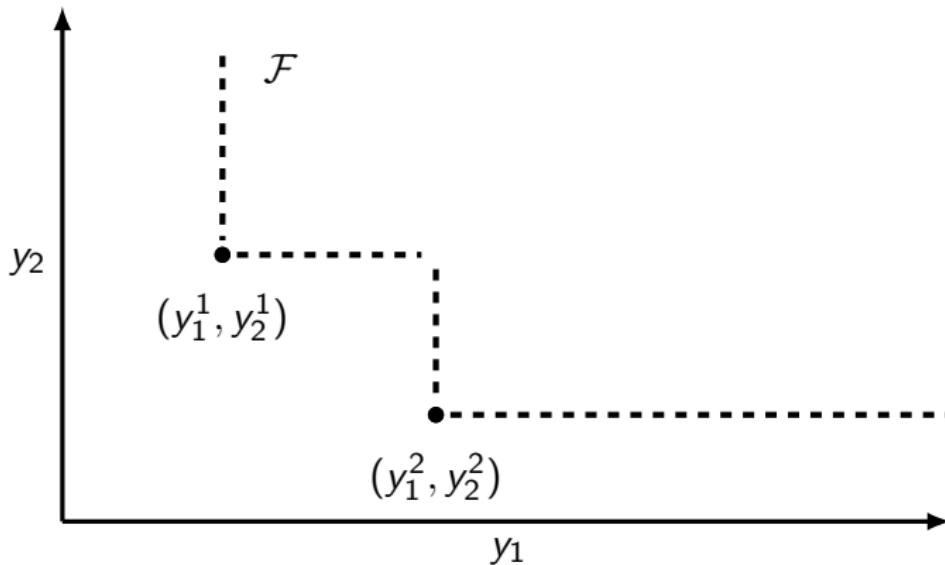
## 2D EGO Illustration

We will use a multiobjective expected improvement framework:



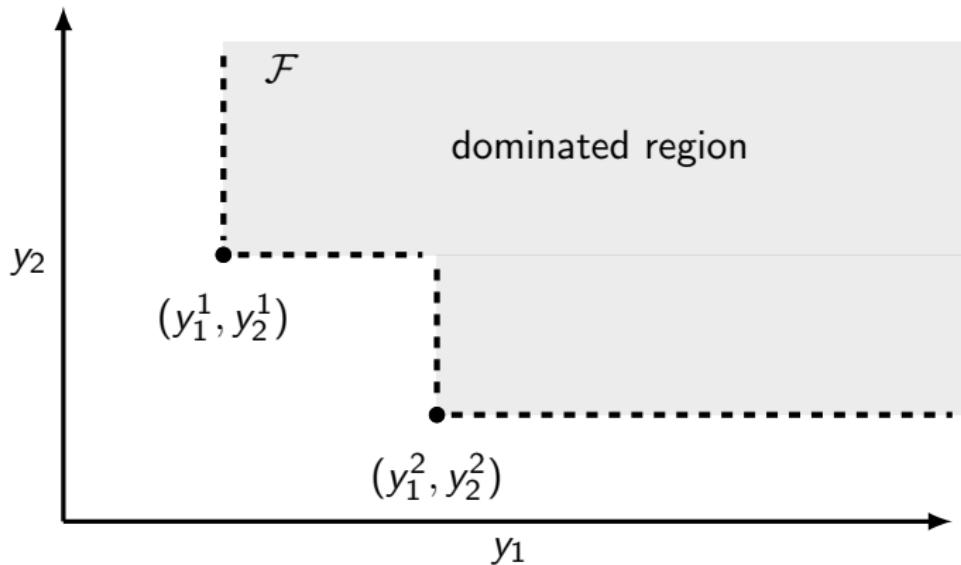
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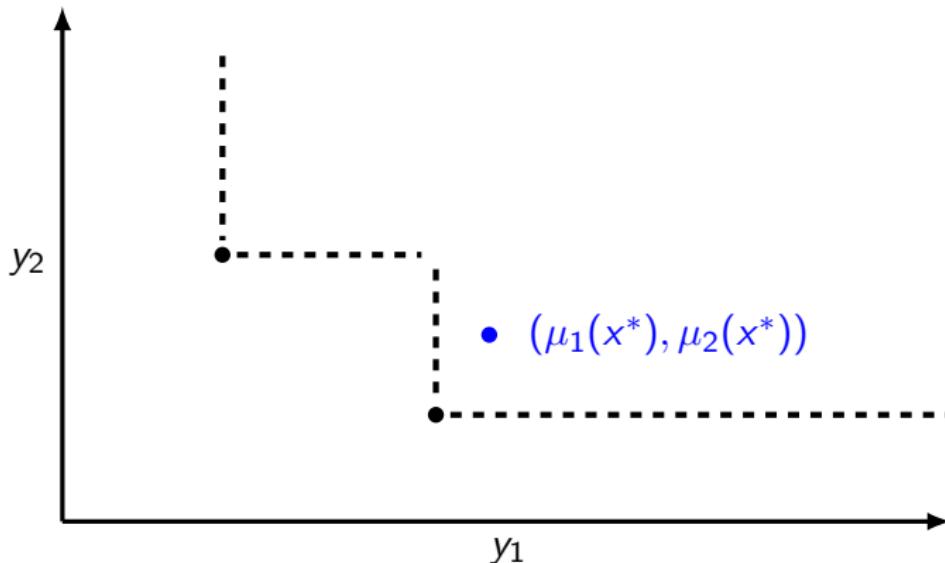
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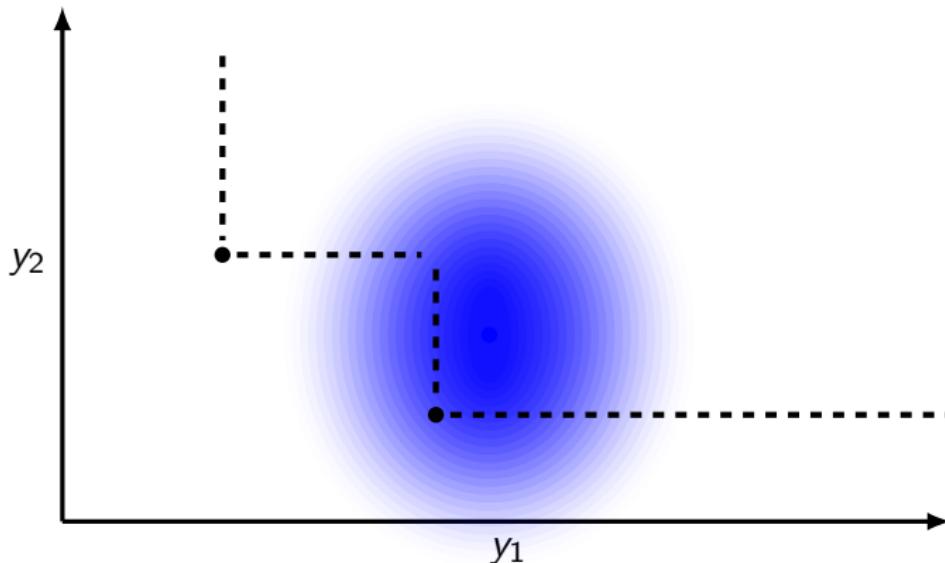
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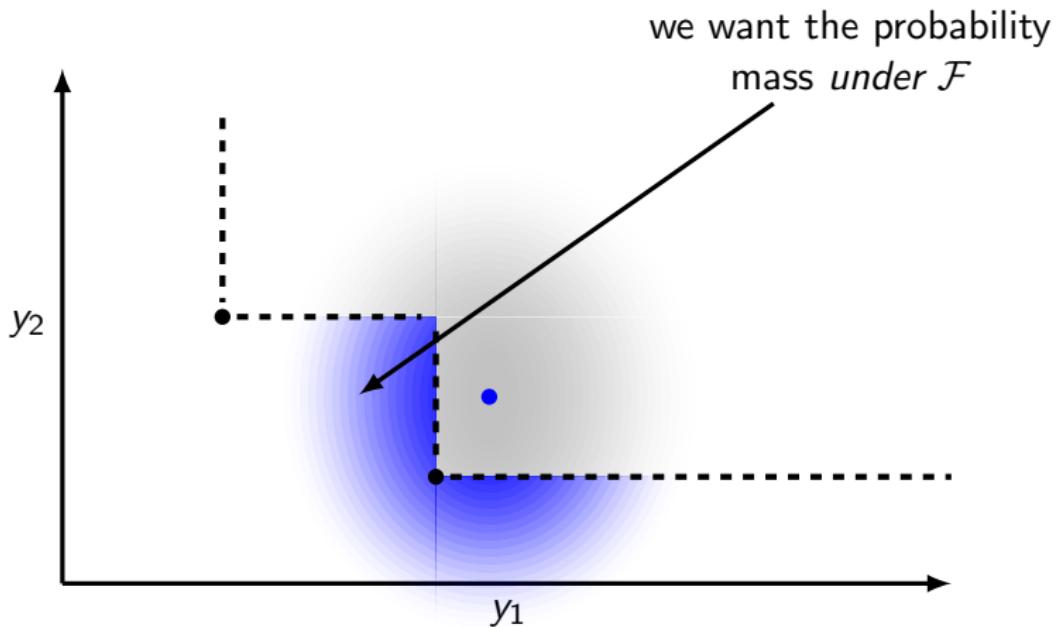
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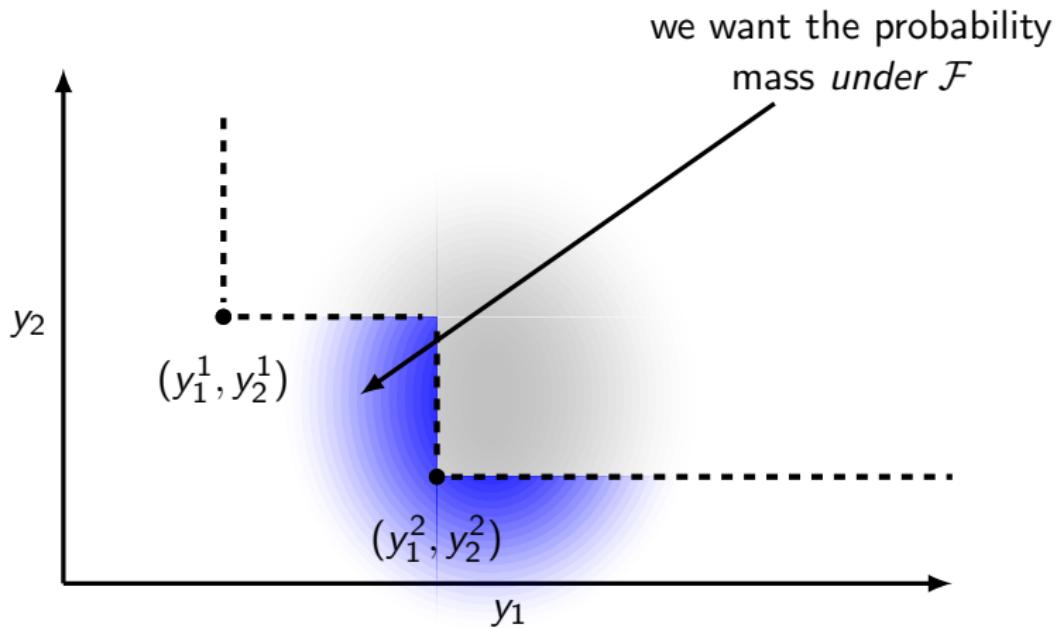
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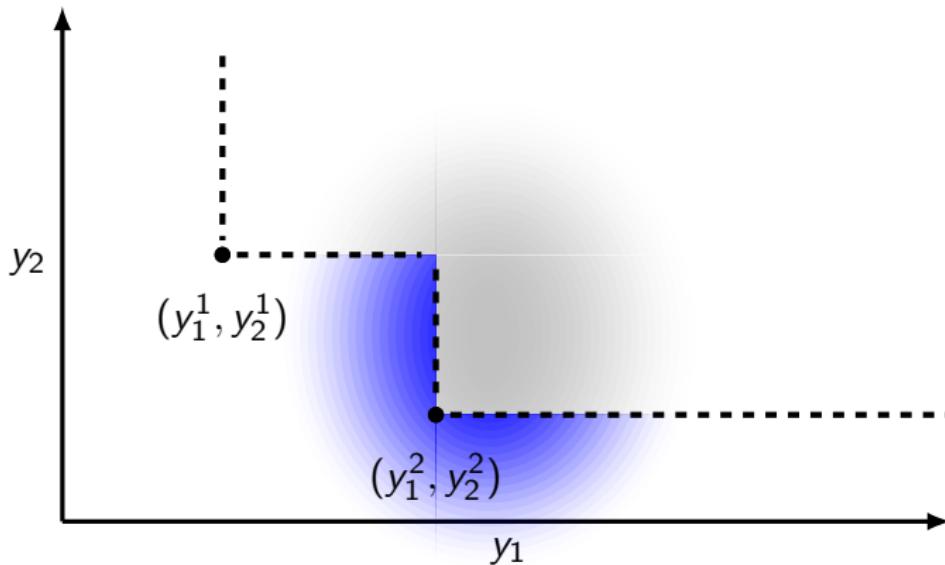
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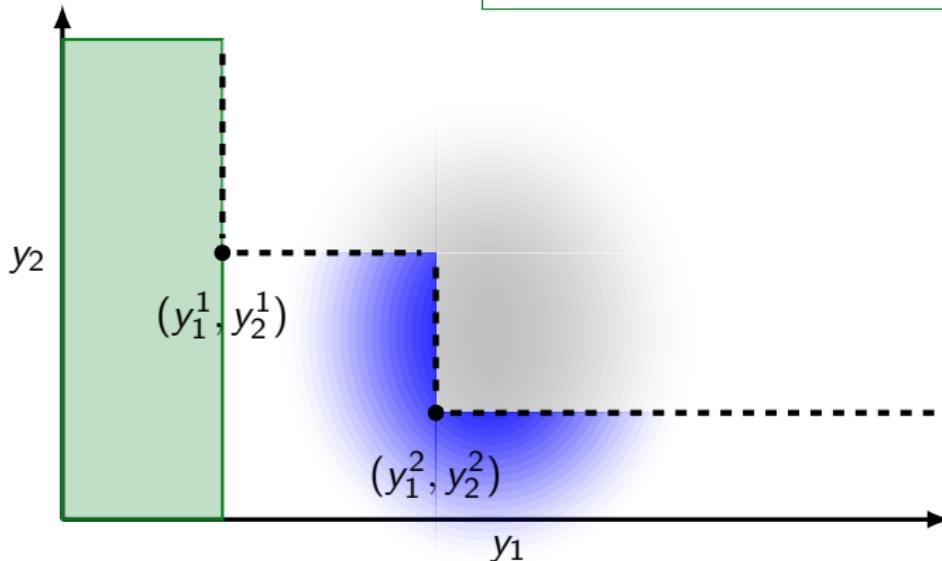
$$P(I) =$$



## 2D EGO Illustration

We will use a multiobjective expected improvement framework:

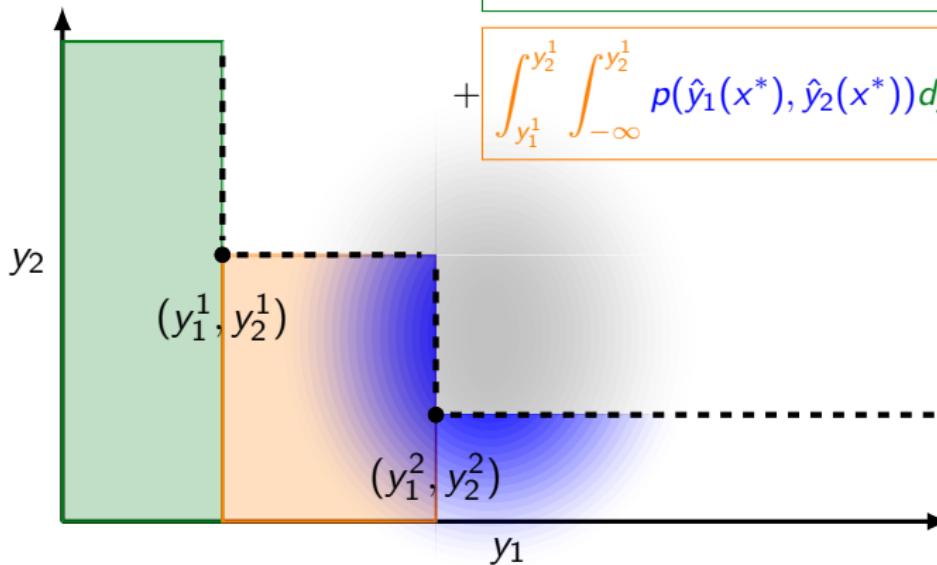
$$P(I) = \int_{-\infty}^{y_1^1} \int_{-\infty}^{\infty} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2$$



## 2D EGO Illustration

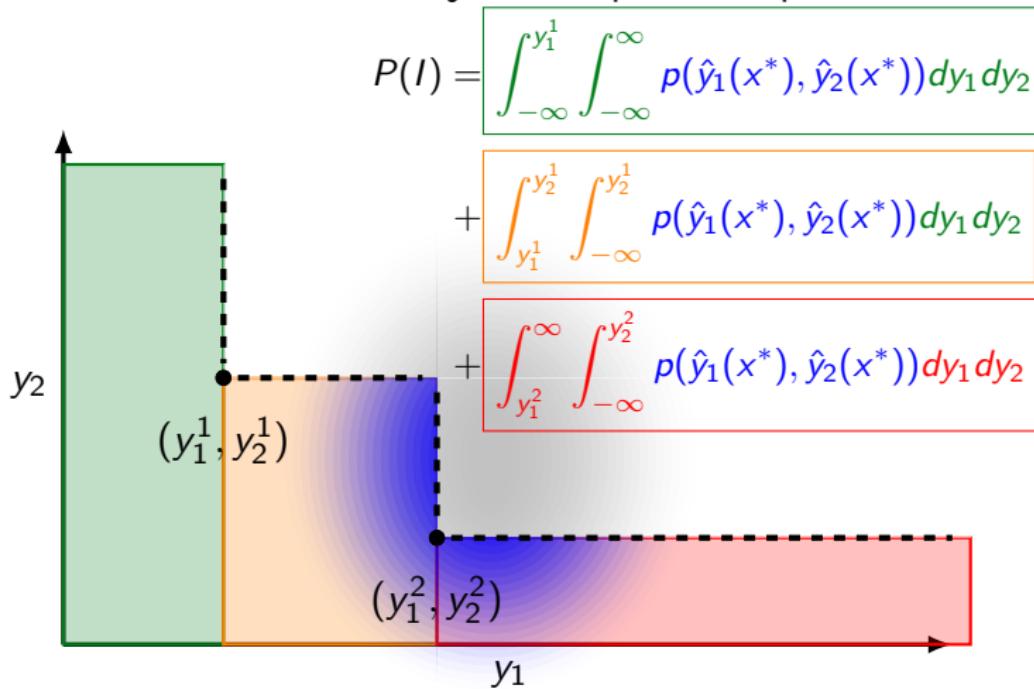
We will use a multiobjective expected improvement framework:

$$P(I) = \int_{-\infty}^{y_1^1} \int_{-\infty}^{\infty} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2$$
$$+ \int_{y_1^1}^{y_2^1} \int_{-\infty}^{y_2^1} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2$$



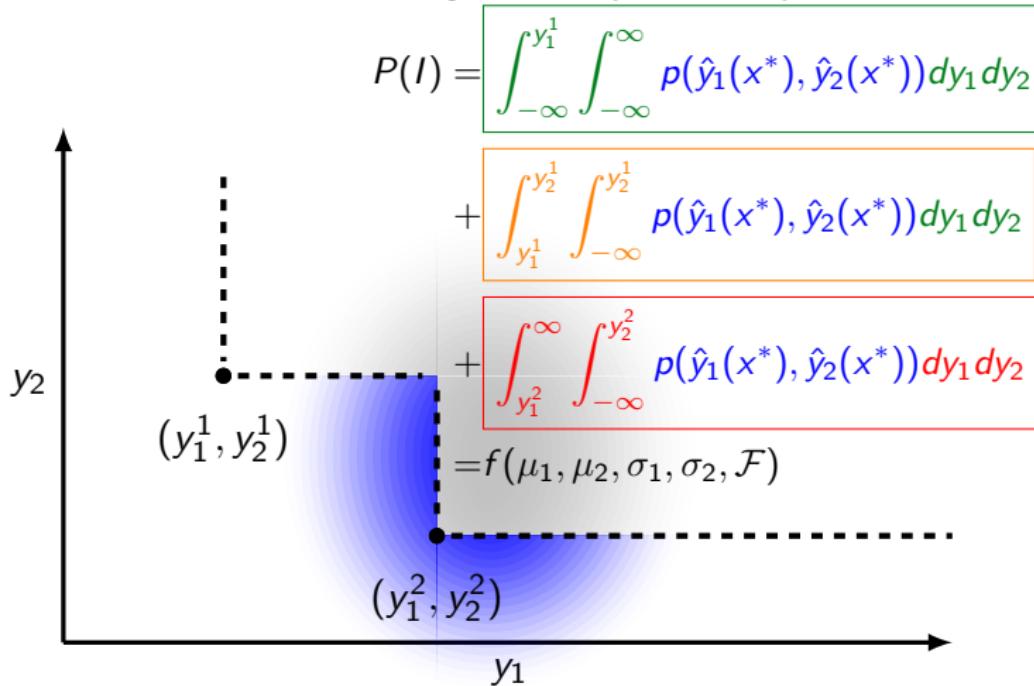
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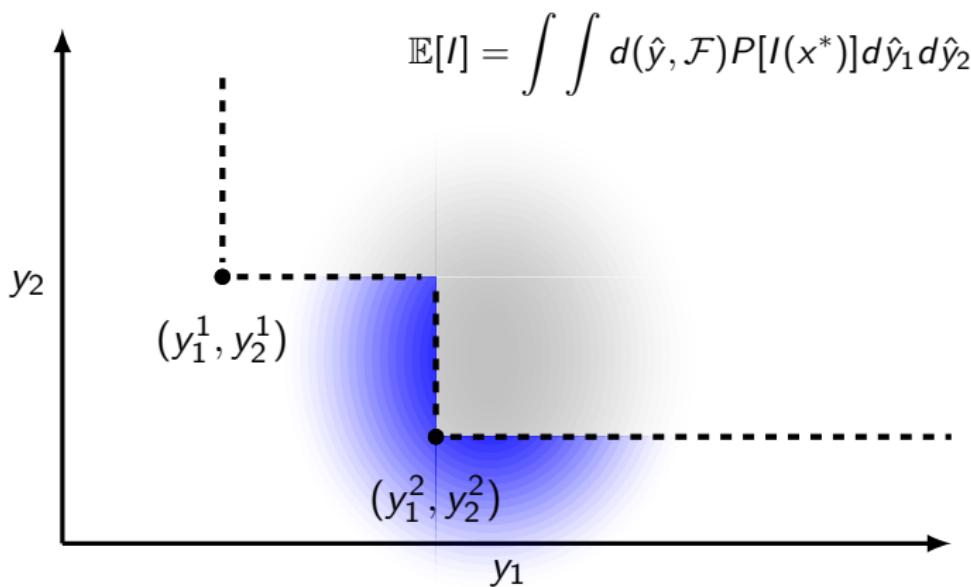
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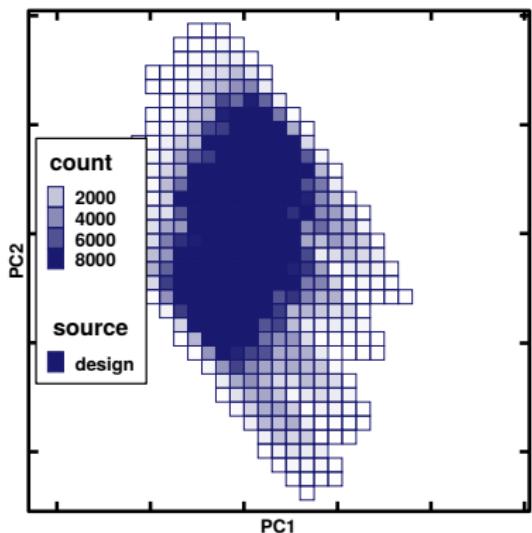
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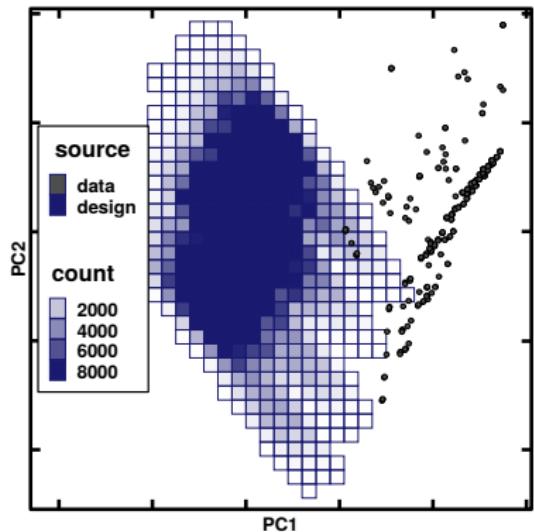
# Design space and clustering

We jump start with diversity-oriented cluster:



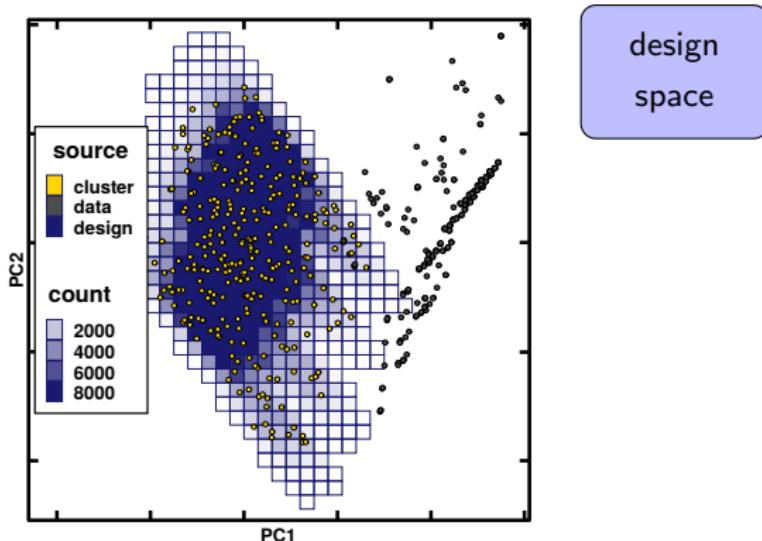
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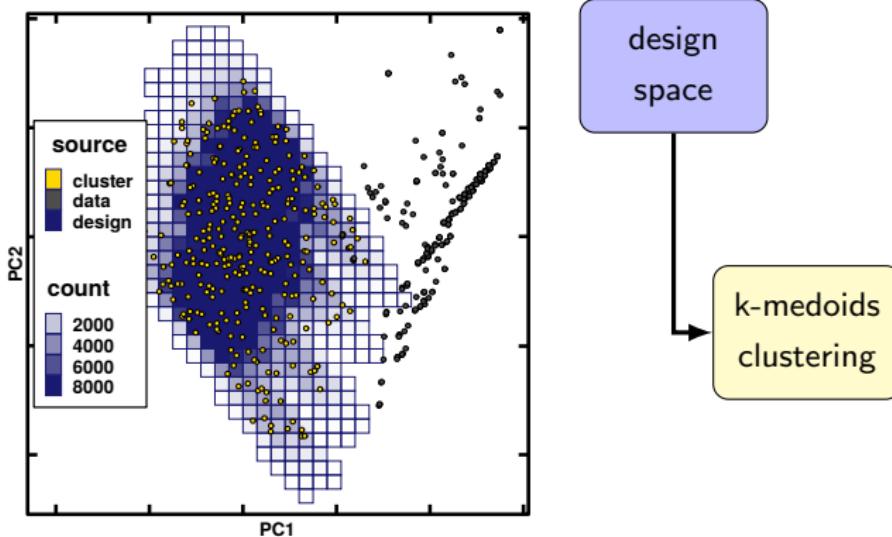
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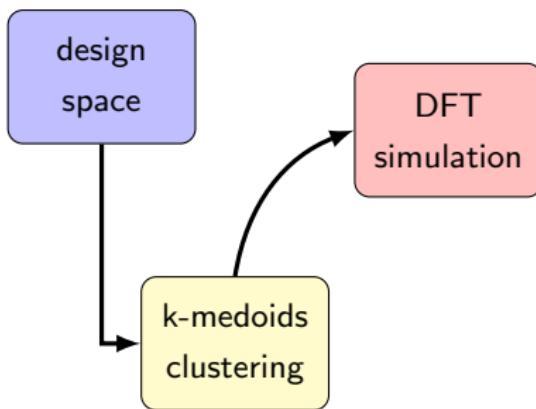
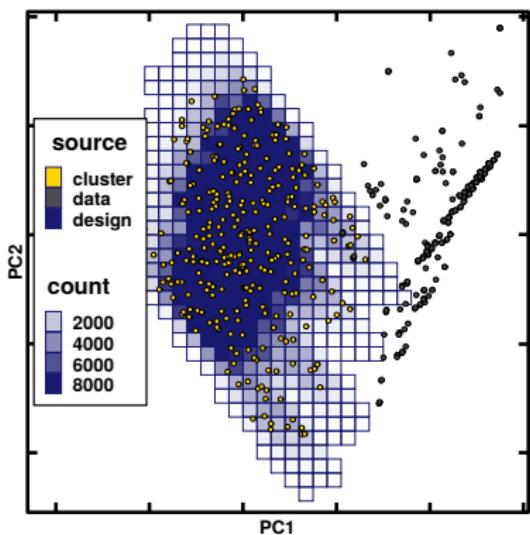
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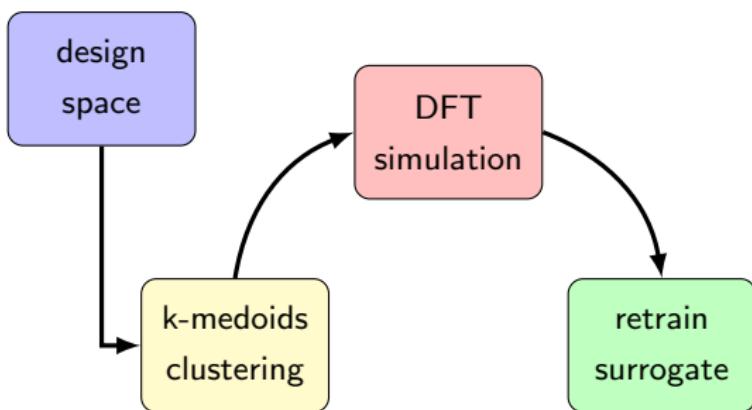
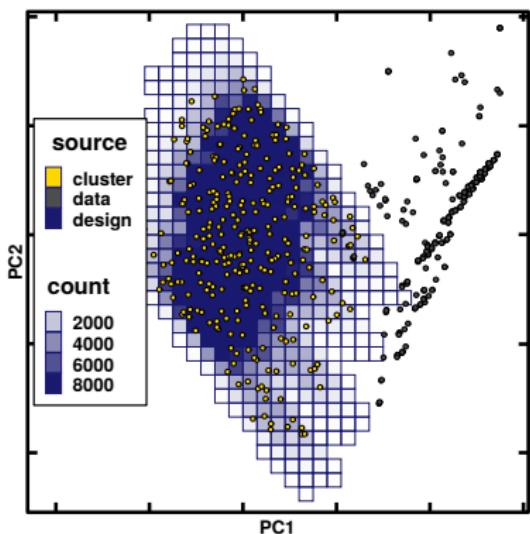
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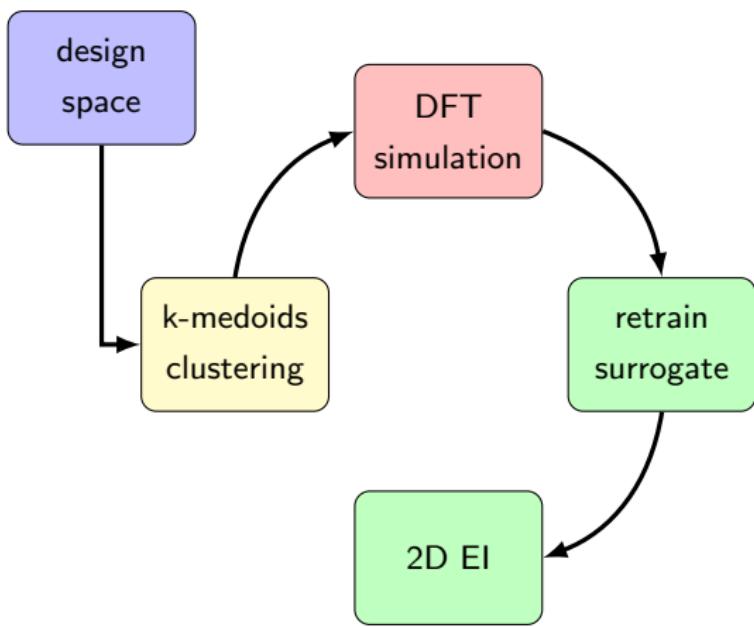
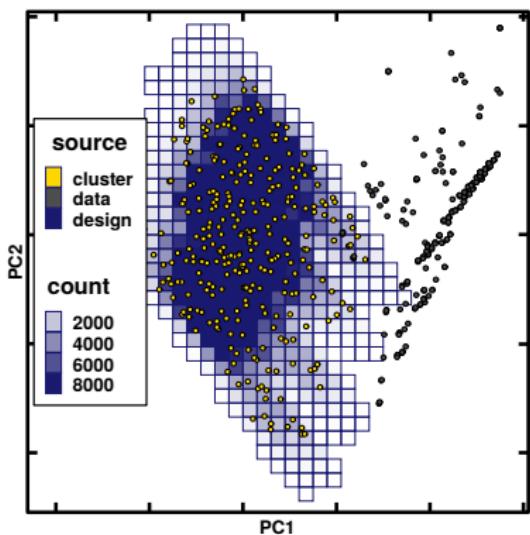
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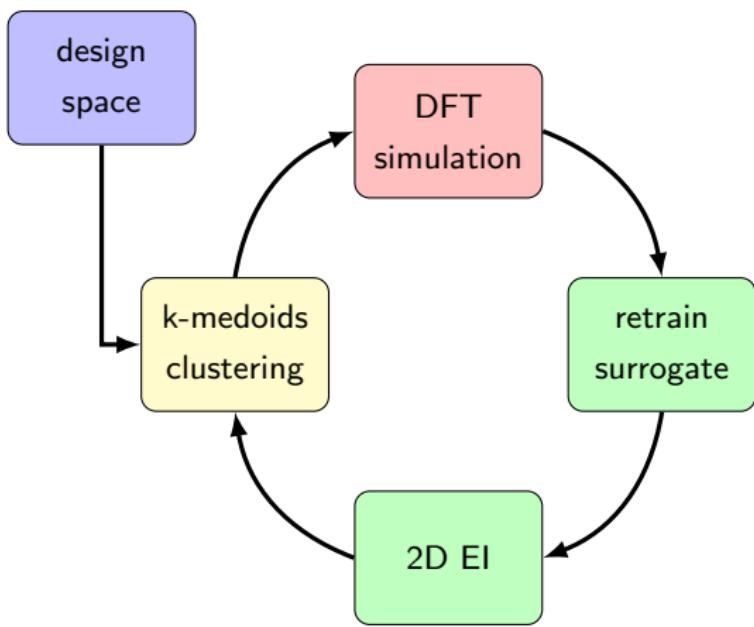
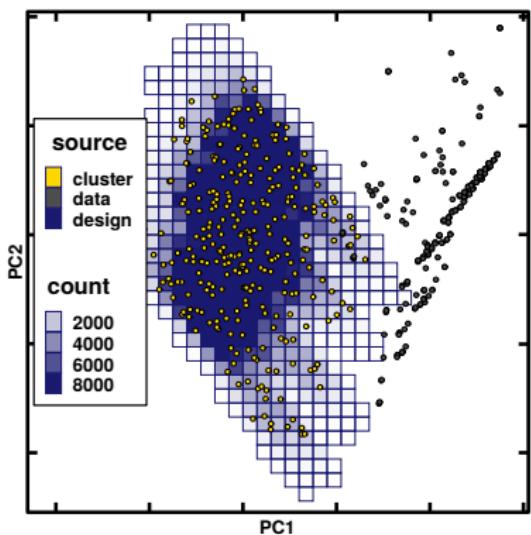
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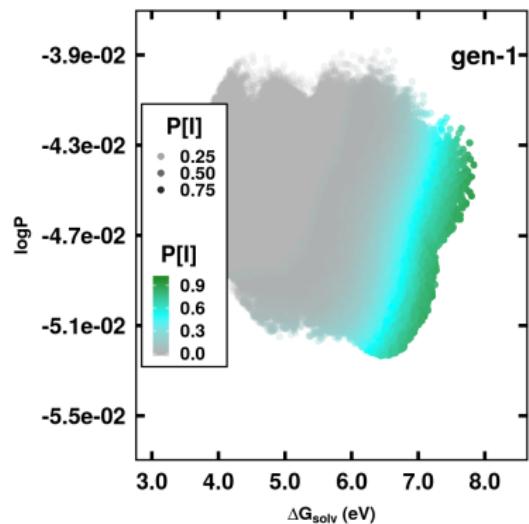
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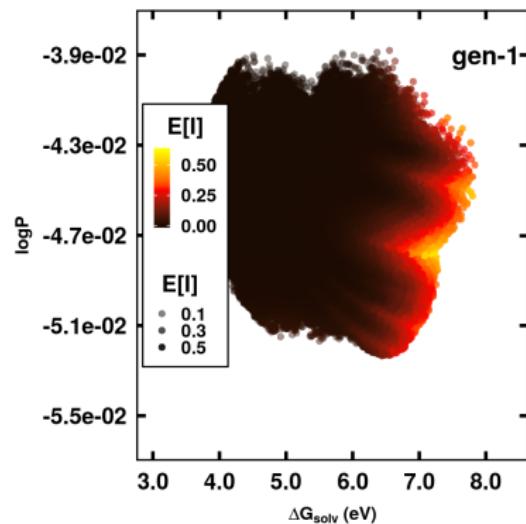


# EGO results

probability of improvement

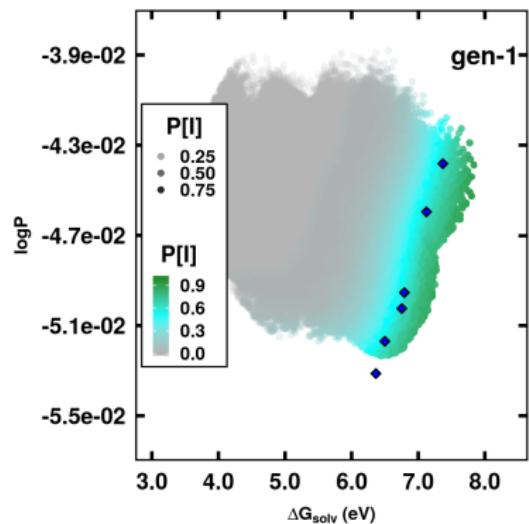


expected improvement

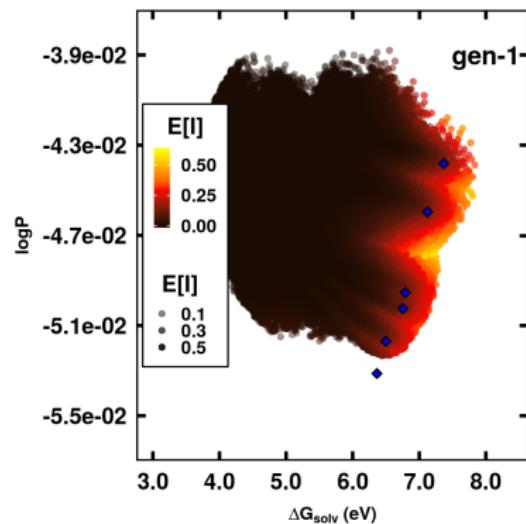


# EGO results

probability of improvement

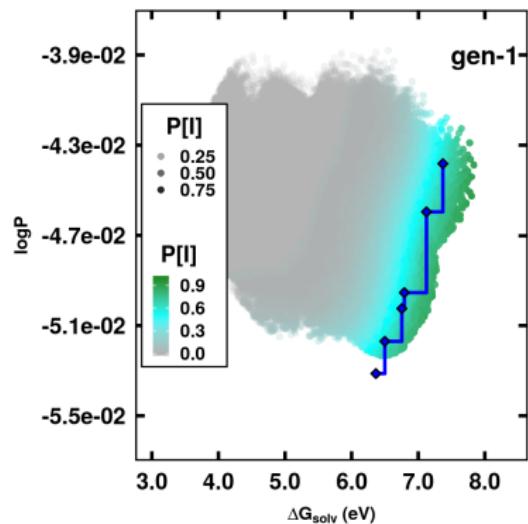


expected improvement

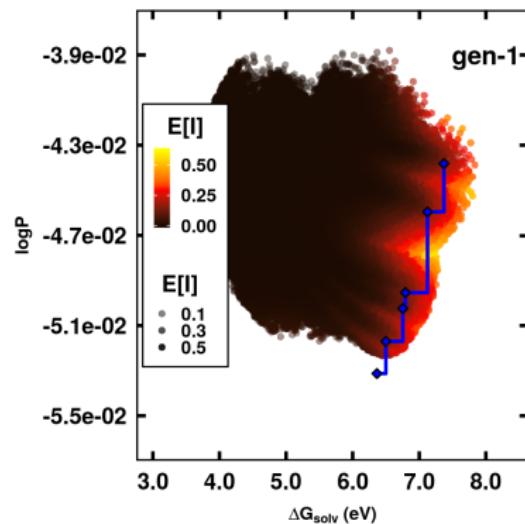


# EGO results

probability of improvement

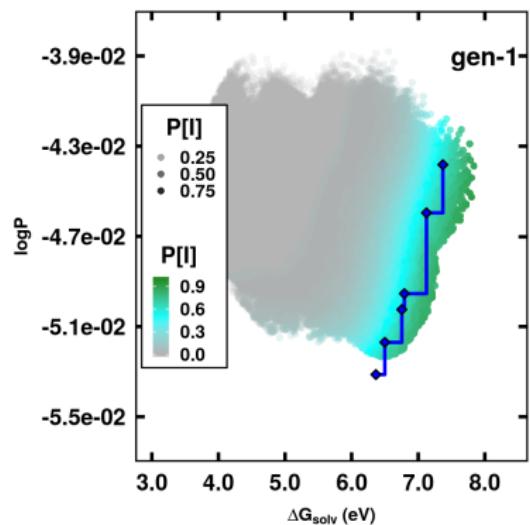


expected improvement

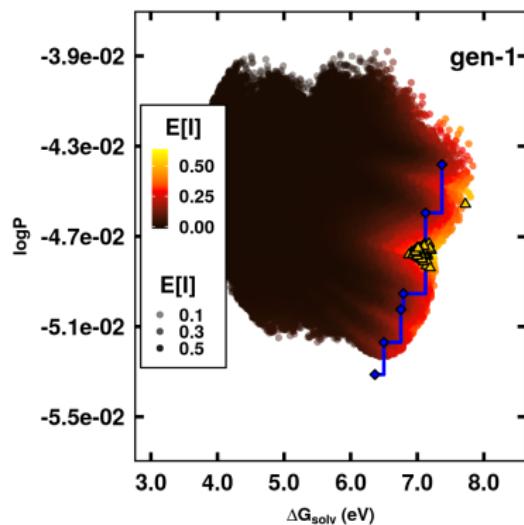


# EGO results

probability of improvement



expected improvement

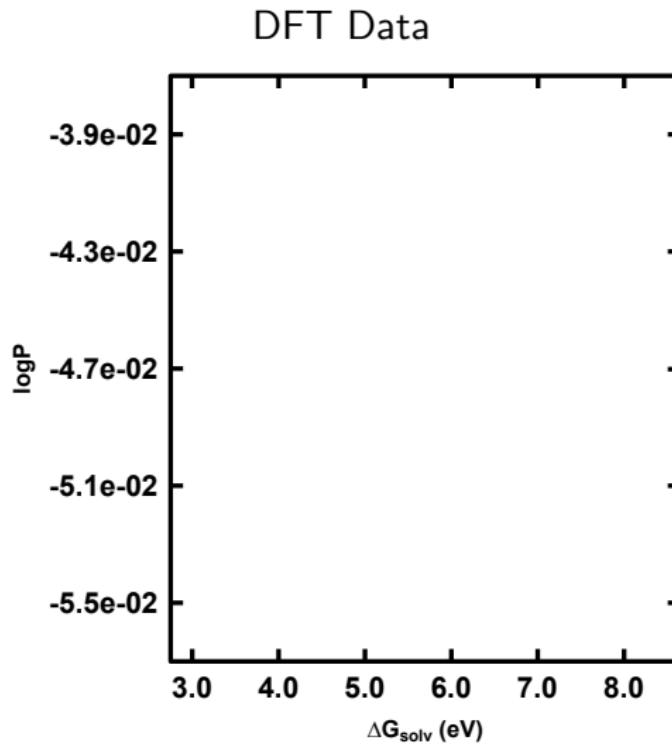


# EGO results

probability of improvement

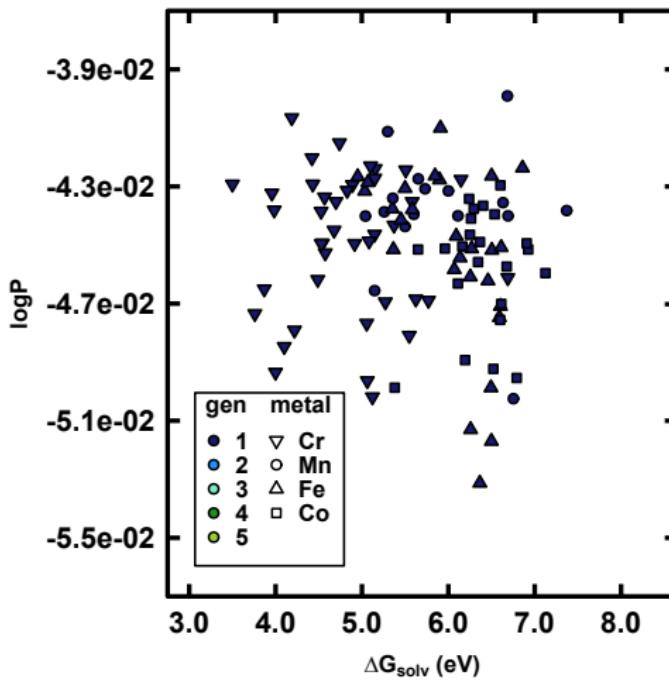
expected improvement

# DFT results



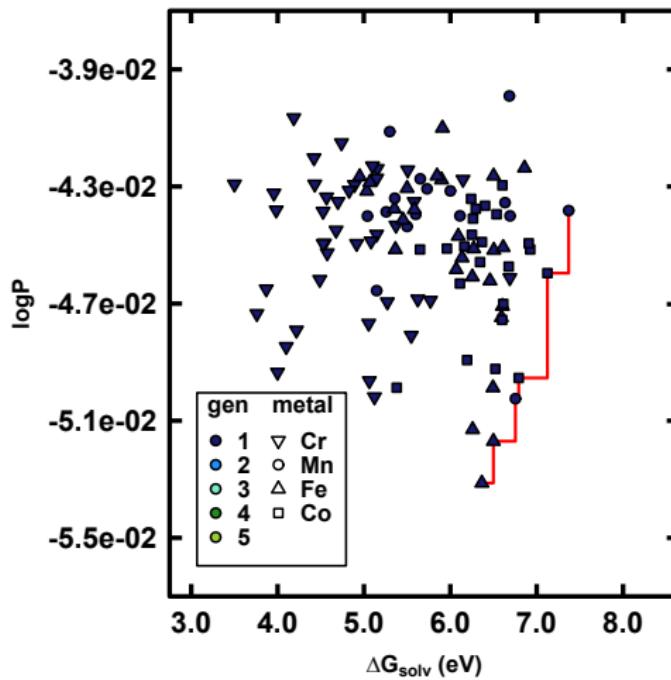
# DFT results

k-medoids points (generation 1)



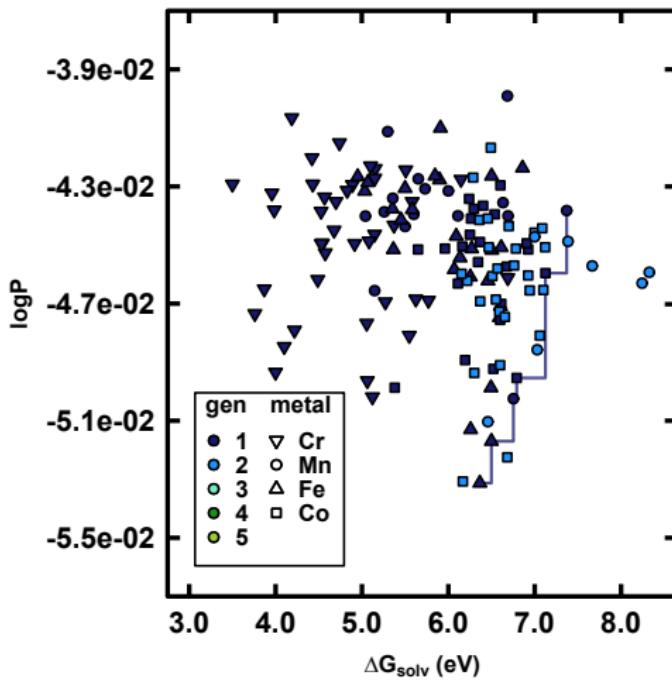
# DFT results

pareto front (generation 1)



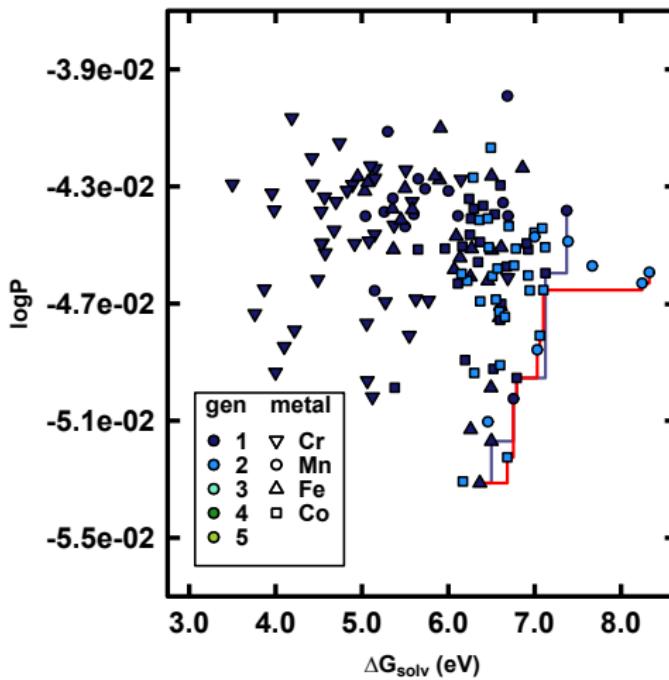
# DFT results

El points (geneneration 2)



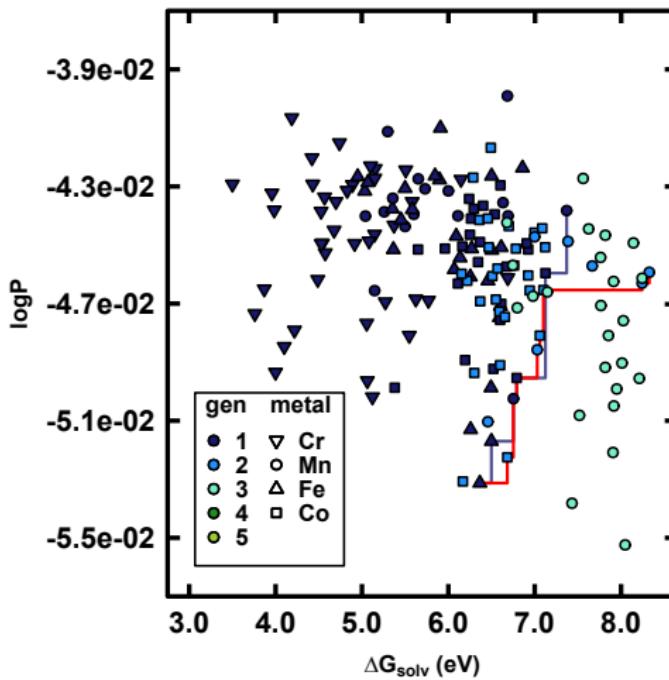
# DFT results

pareto front (generation 2)



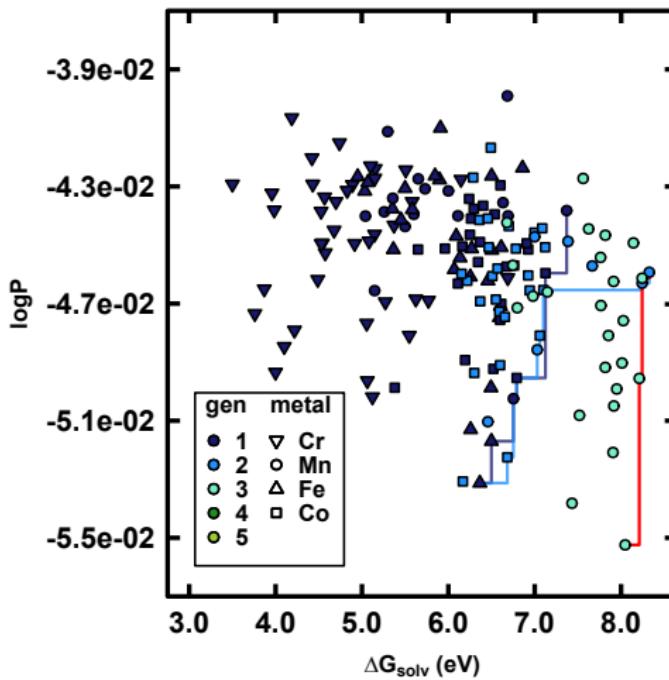
# DFT results

El points (generation 3)



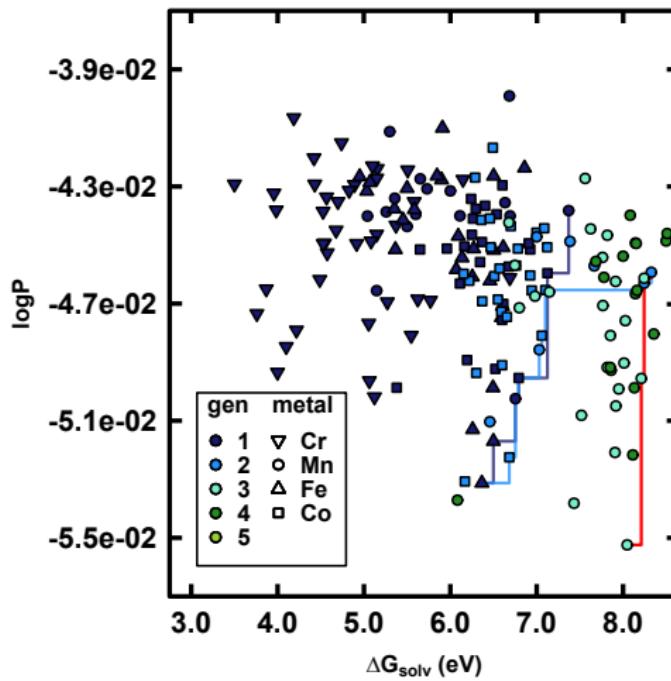
# DFT results

pareto front (generation 3)



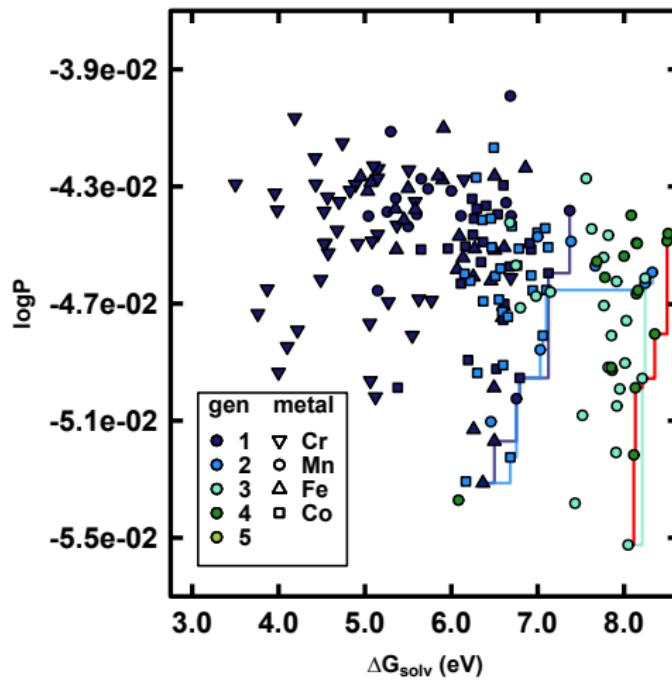
# DFT results

El points (generation 4)



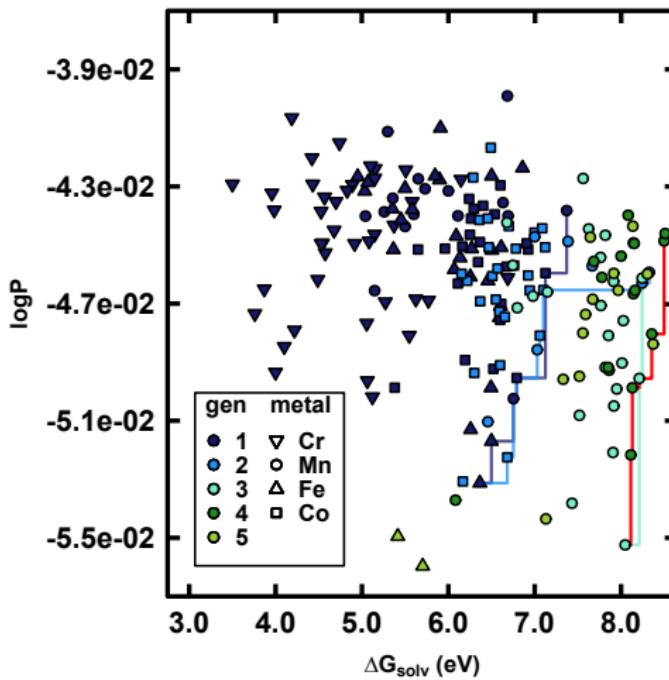
# DFT results

pareto front (generation 4)



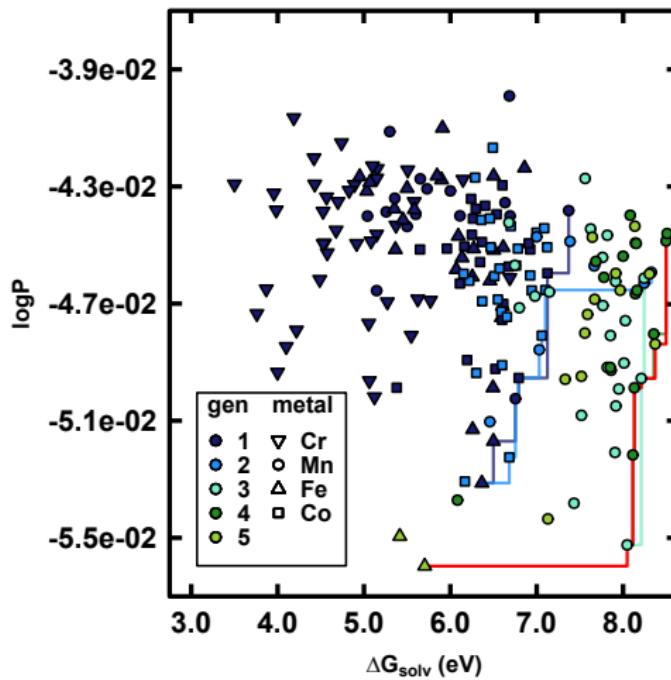
# DFT results

El points (generation 5)

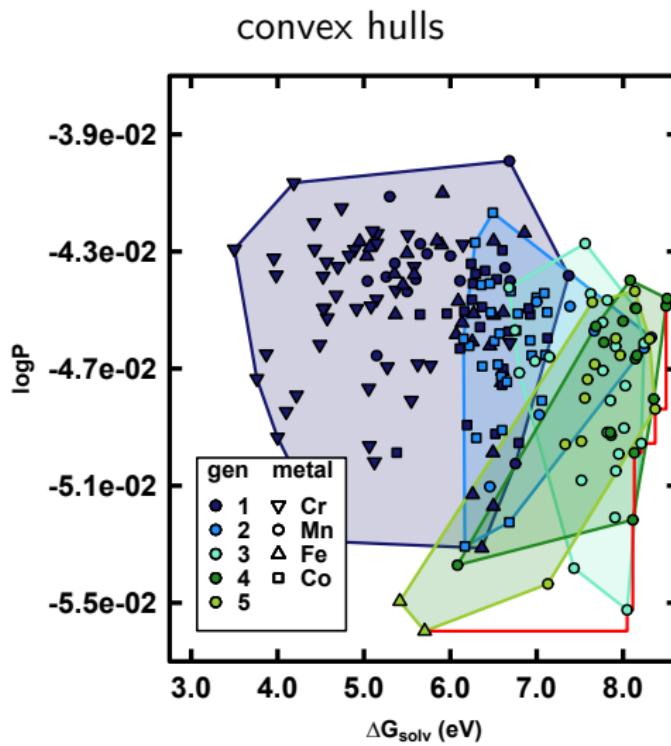


# DFT results

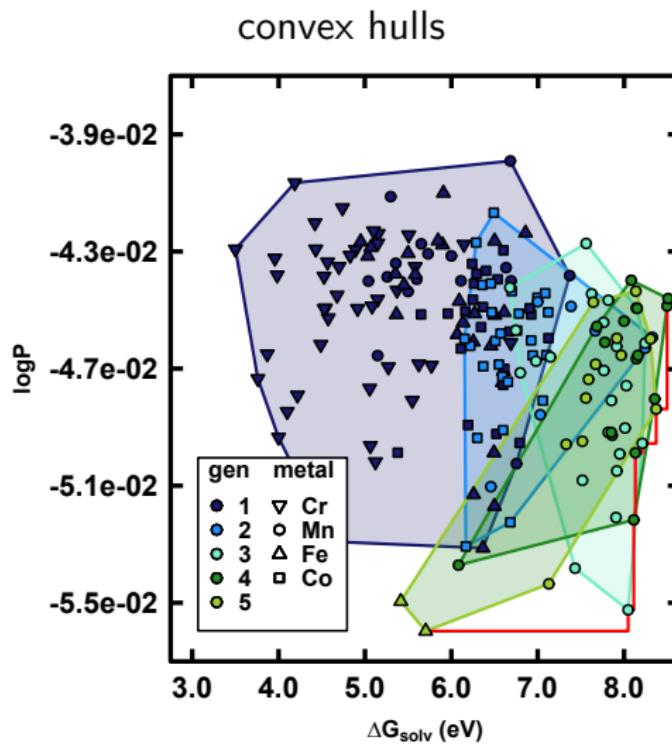
pareto front (generation 5)



# DFT results

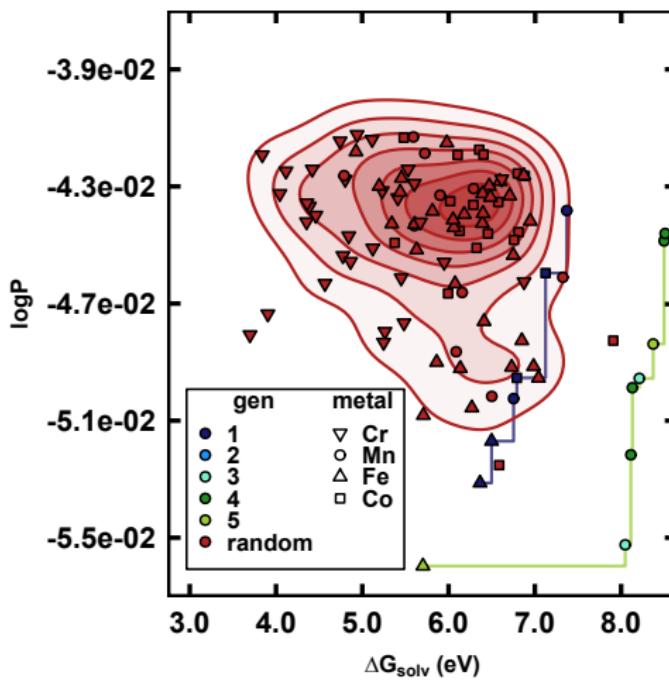


# DFT results



# DFT results

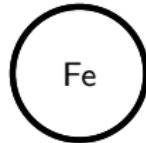
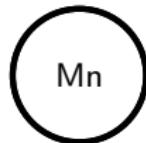
comparison to random sampling



# Final lead analysis

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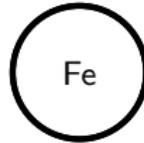
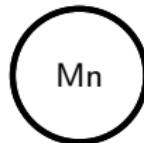
metal  
center



# Final lead analysis

metal  
center

6-member  
heterocycle

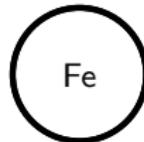


# Final lead analysis

metal  
center

6-member  
heterocycle

5-member  
heterocycle

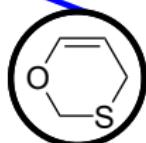
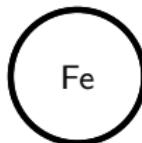
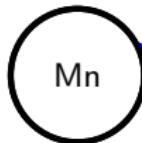


# Final lead analysis

metal  
center

6-member  
heterocycle

5-member  
heterocycle

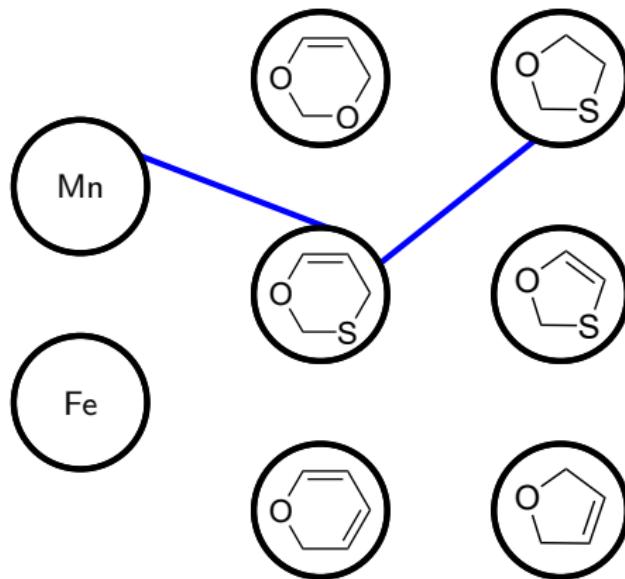


# Final lead analysis

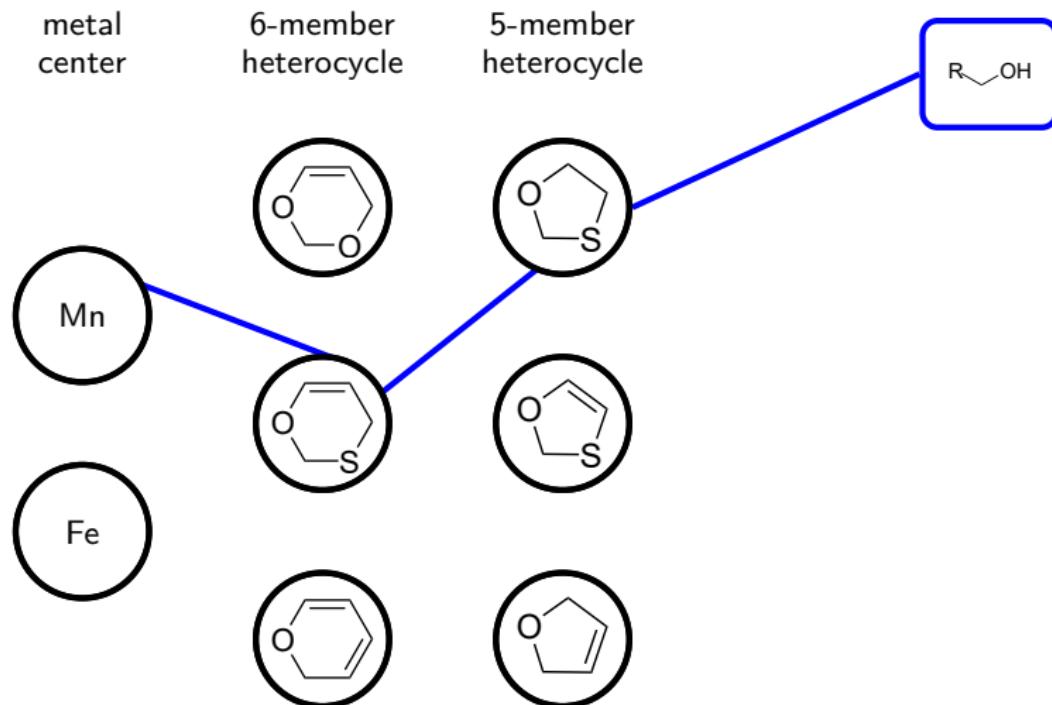
metal  
center

6-member  
heterocycle

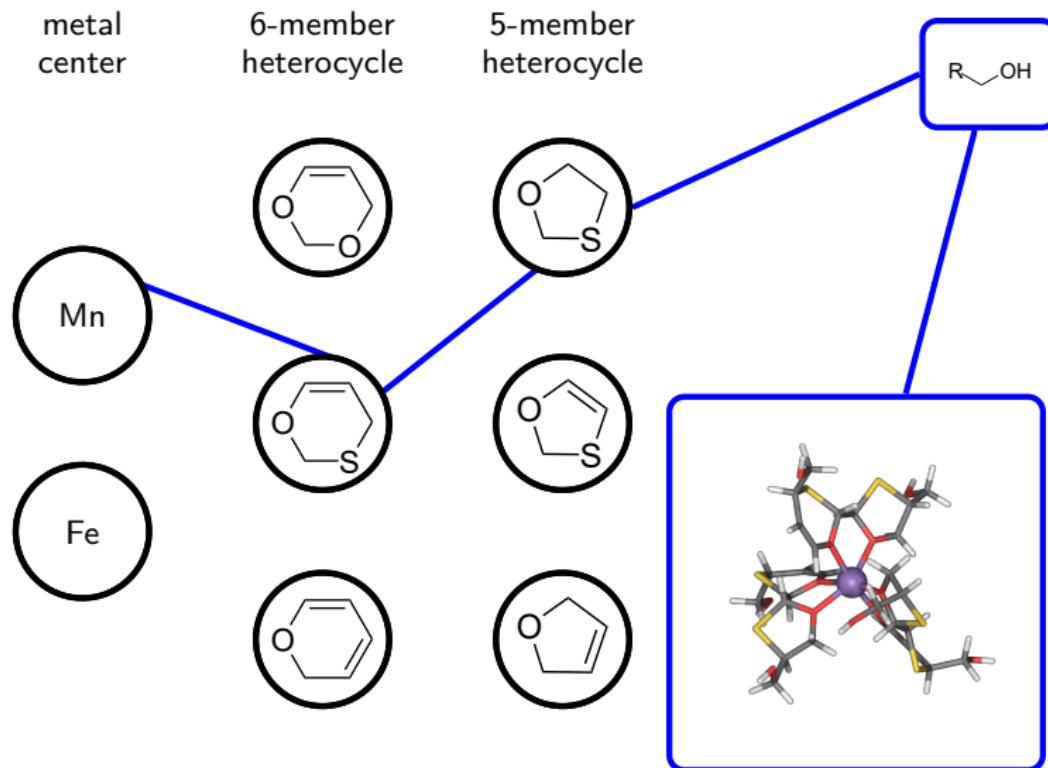
5-member  
heterocycle



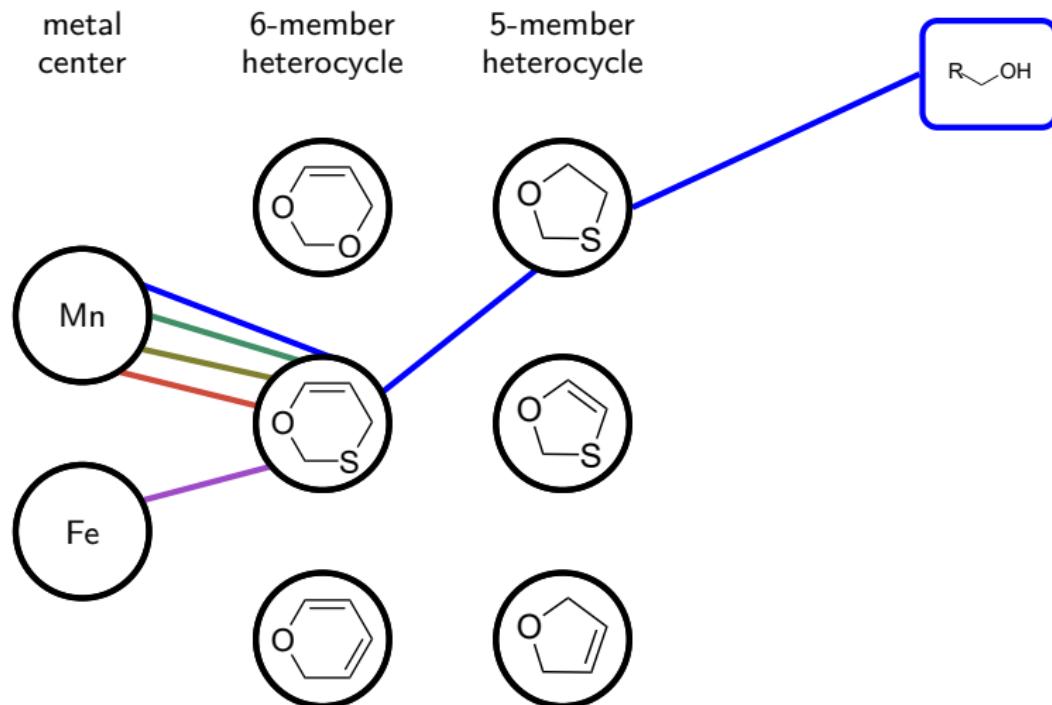
# Final lead analysis



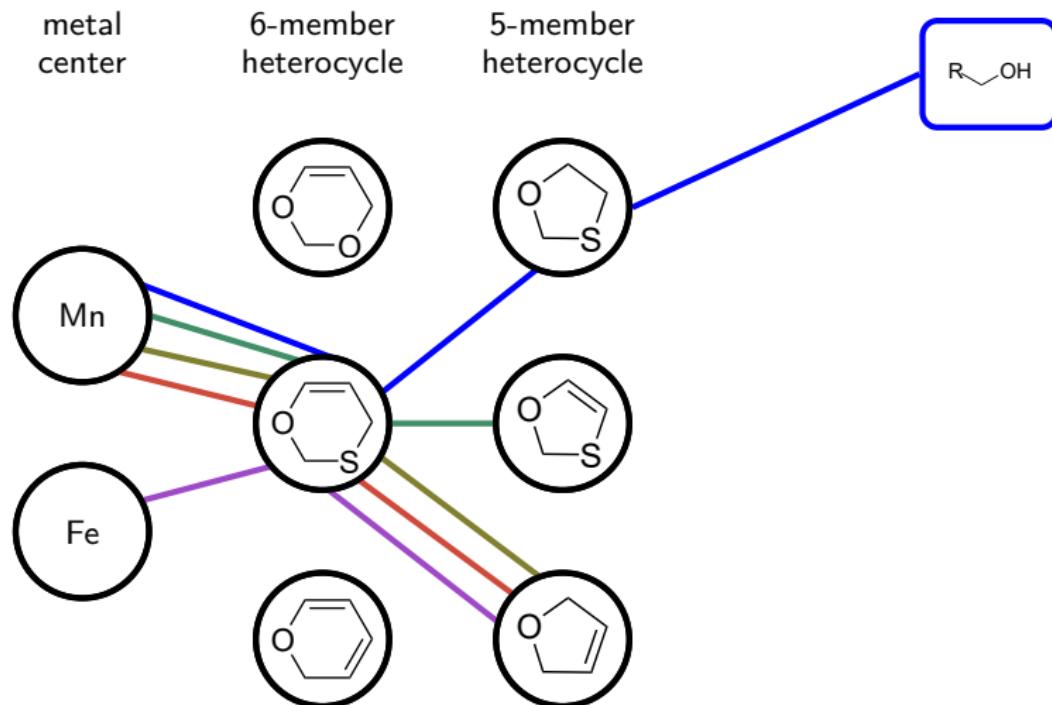
# Final lead analysis



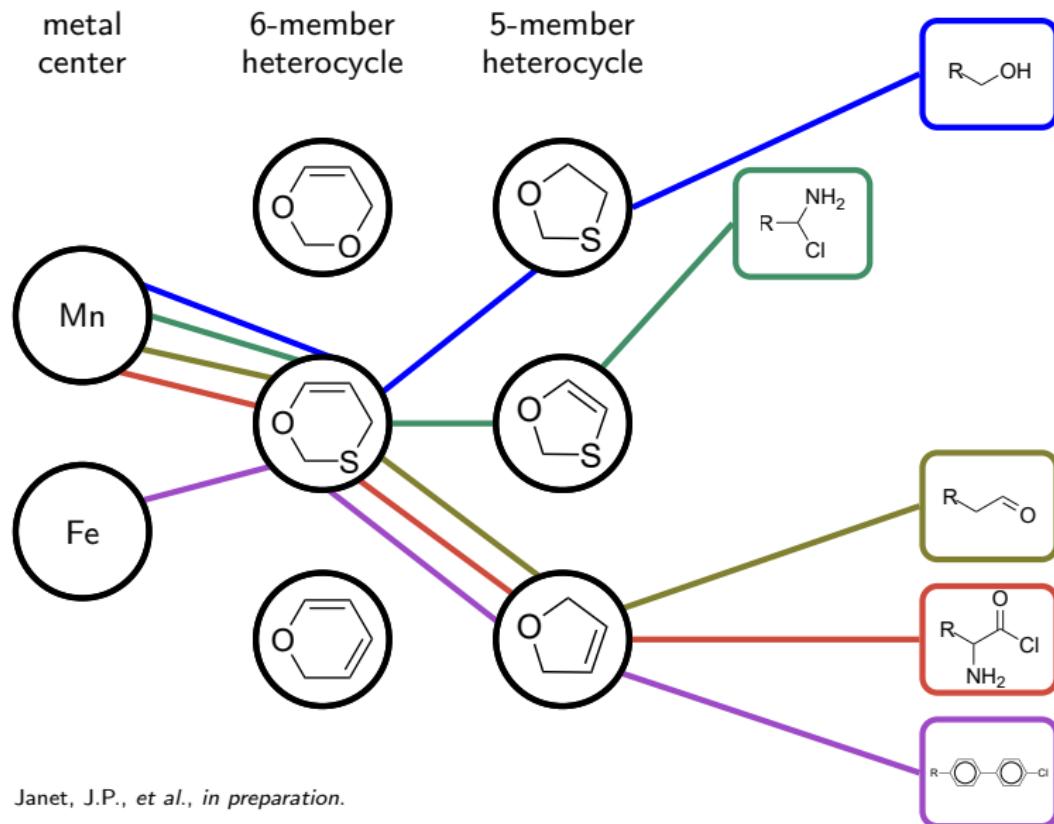
# Final lead analysis



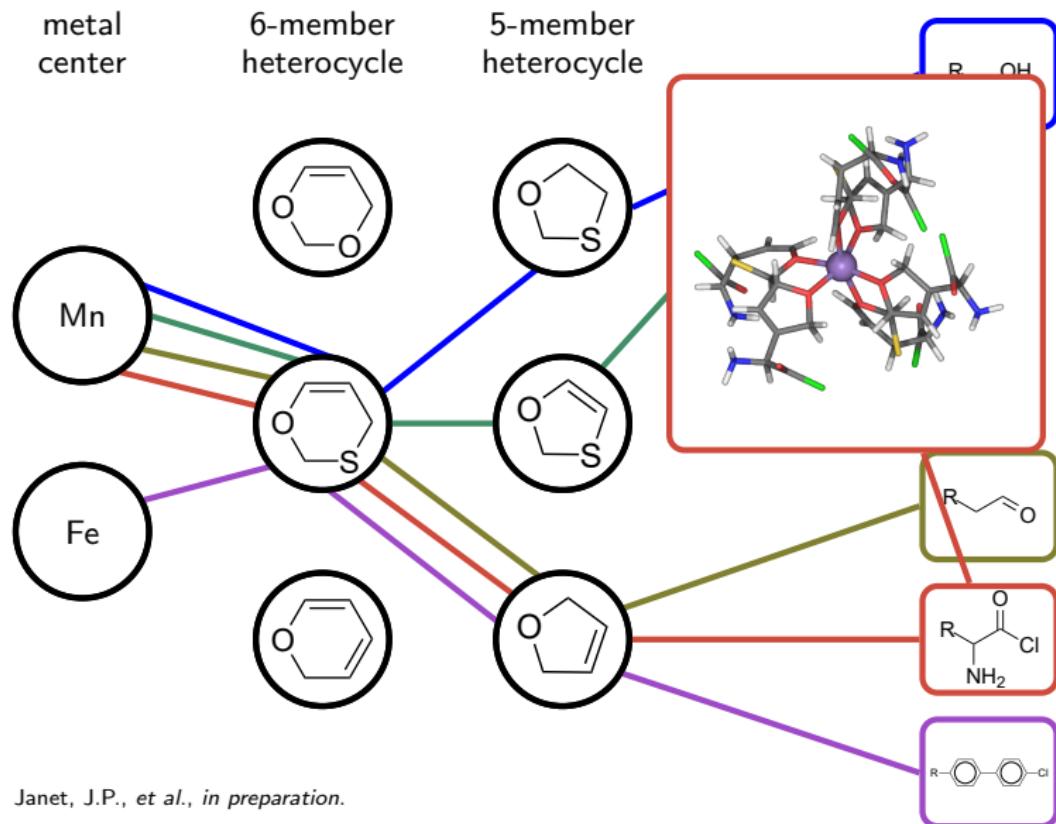
# Final lead analysis



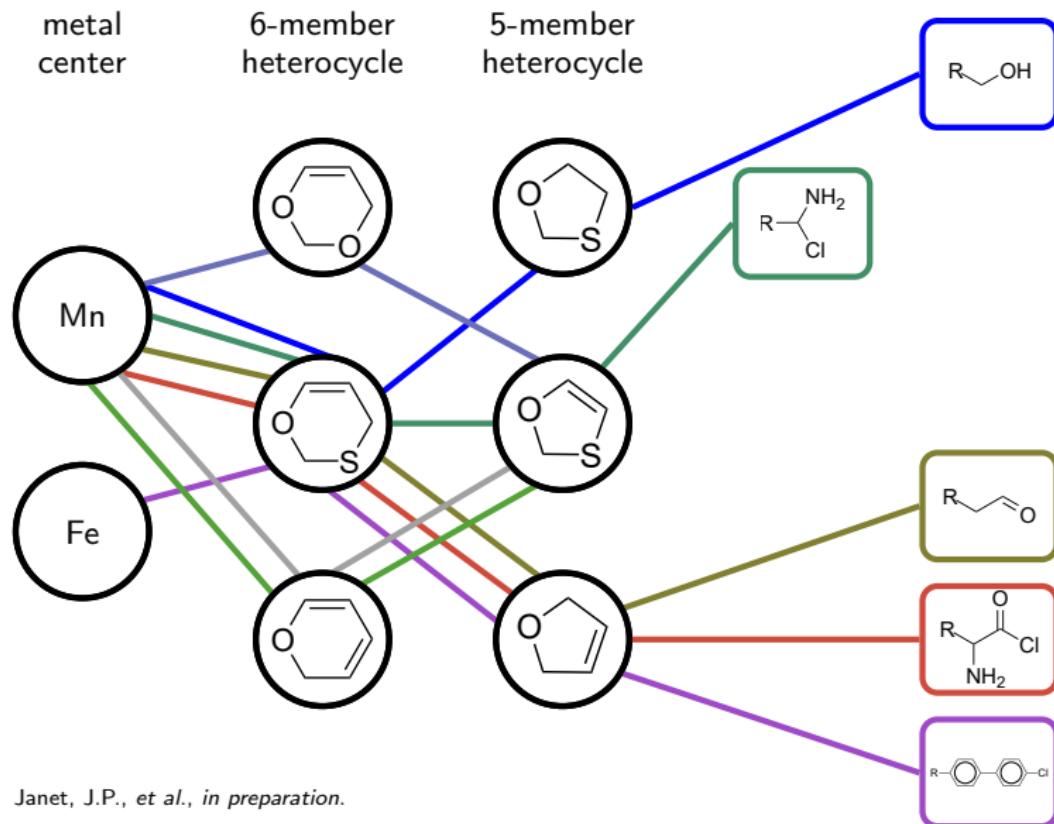
# Final lead analysis



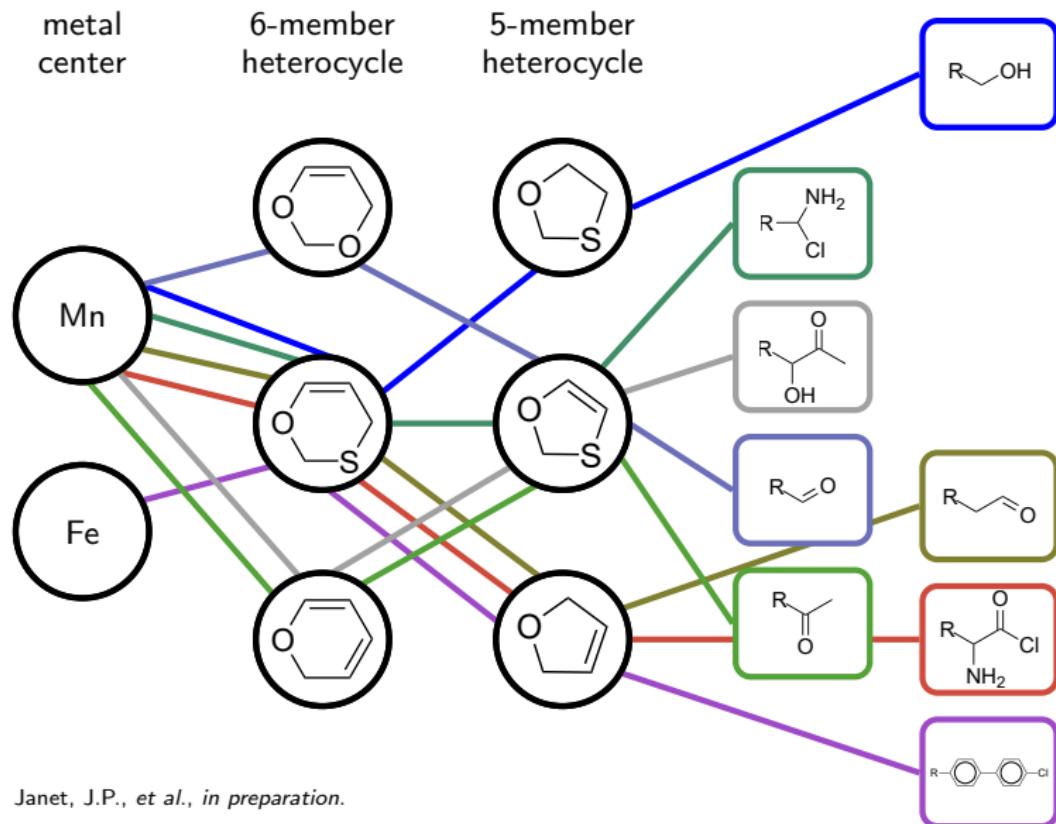
# Final lead analysis



# Final lead analysis



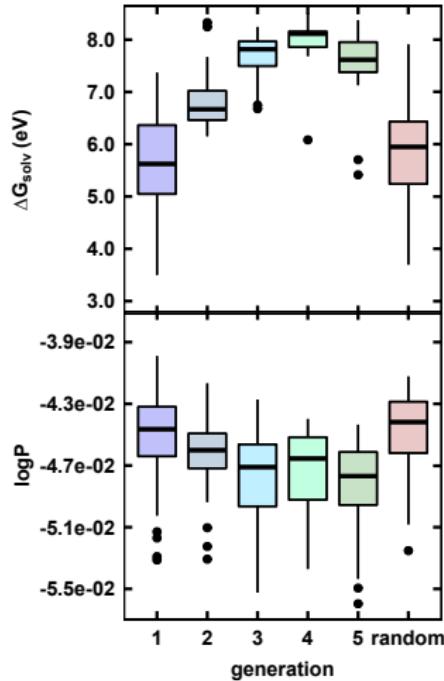
# Final lead analysis



# Case study conclusions

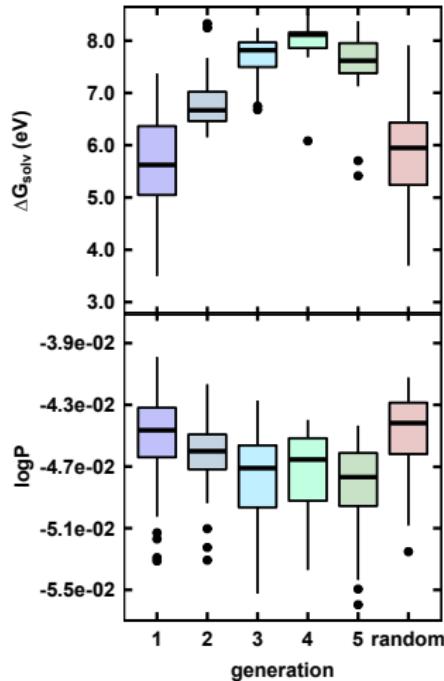
## Case study conclusions

- EI framework provides high resolution in the region of interest (c.f. maximum uncertainty), converges quickly



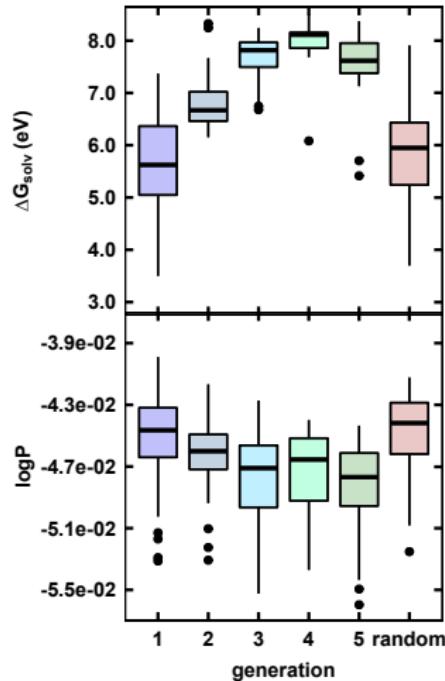
## Case study conclusions

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## Case study conclusions

- EI framework provides high resolution in the region of interest (c.f. maximum uncertainty), converges quickly
- We are able to identify fruitful regions from large chemical spaces based on few DFT evaluations
- Multiobjective DFT optimization guided by data-driven method efficiency generates lead complexes



# Acknowledgments

Thanks to the Kulik group and funding partners:

