

Machine-learning assisted workflows for inorganic molecular discovery

Jon Paul Janet¹ Chenru Duan² Aditya Nandy²
Heather Kulik ¹

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²Department of Chemistry, Massachusetts Institute of Technology



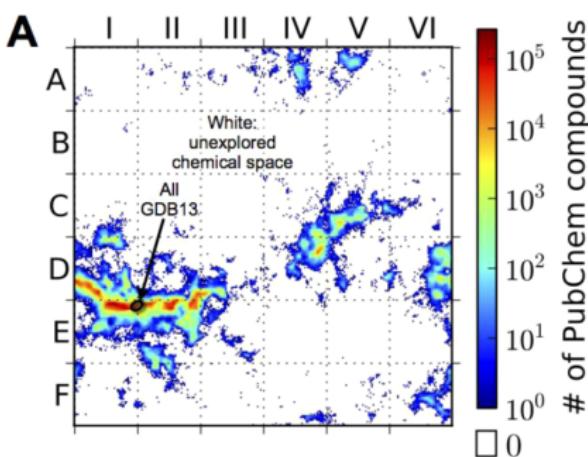
Machine Learning and Informatics for Chemistry and Materials

Motivation: chemical discovery

How can we design new materials using computers?

The space of possible chemistries is incredibly vast, with $\mathcal{O}(10^{60})$ small organic molecules.

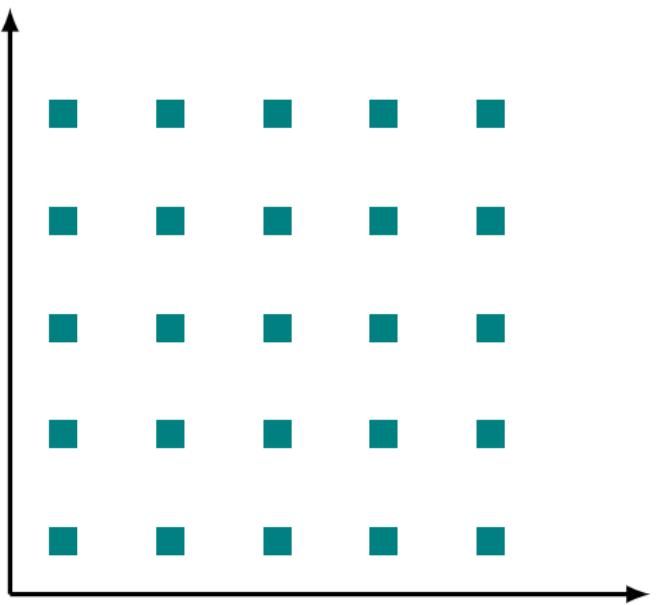
All potentially undiscovered medicines, catalysts and materials are somewhere, out in this huge space.



Virshup et al., J. Am. Chem. Soc., 135(19): 7296–7303, 2013.

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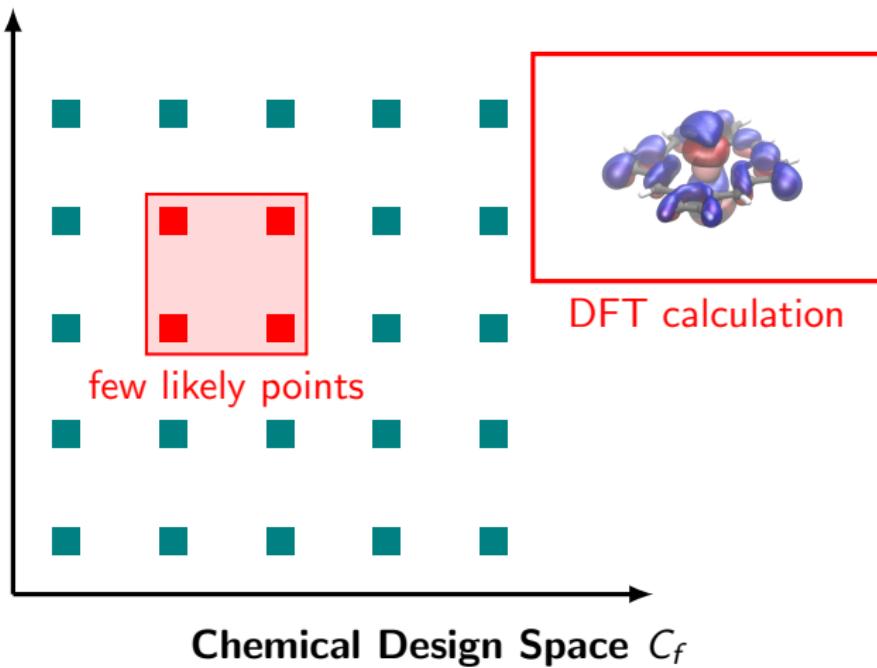
How can we design new materials using computers?



Chemical Design Space C_f

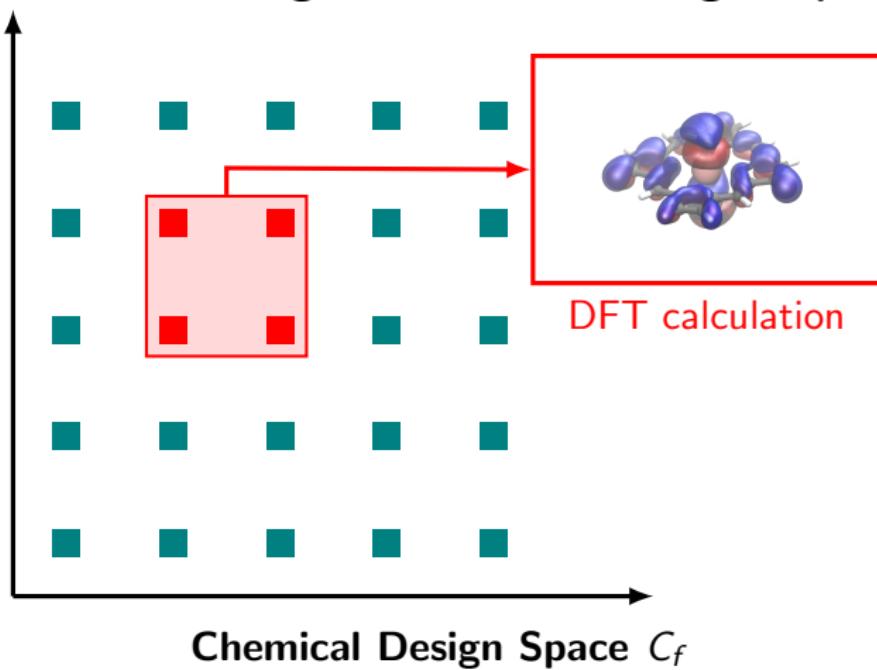
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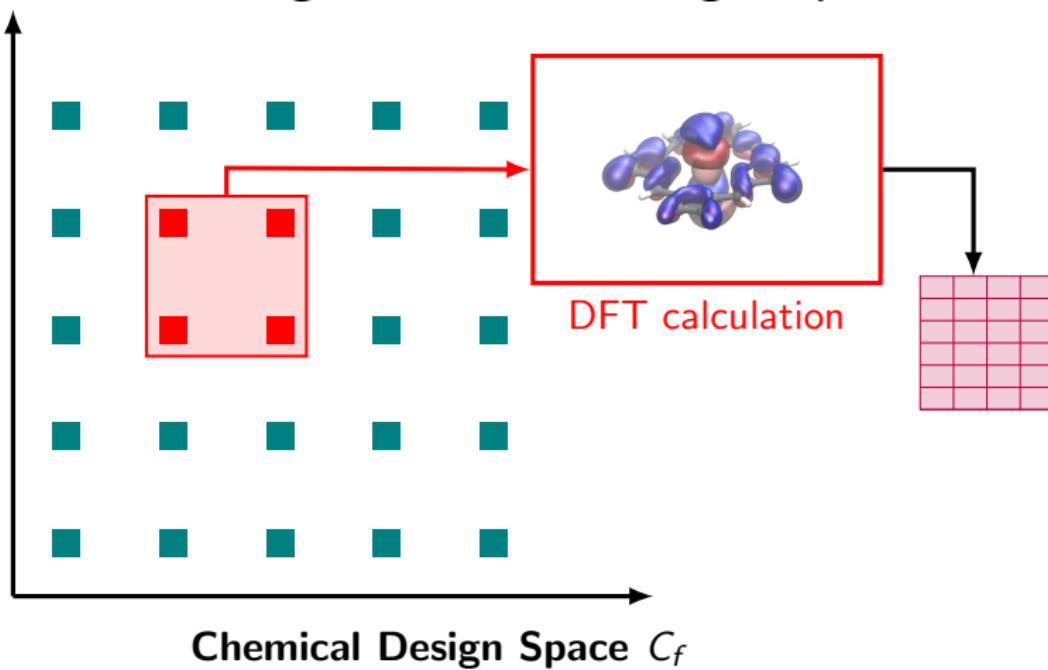
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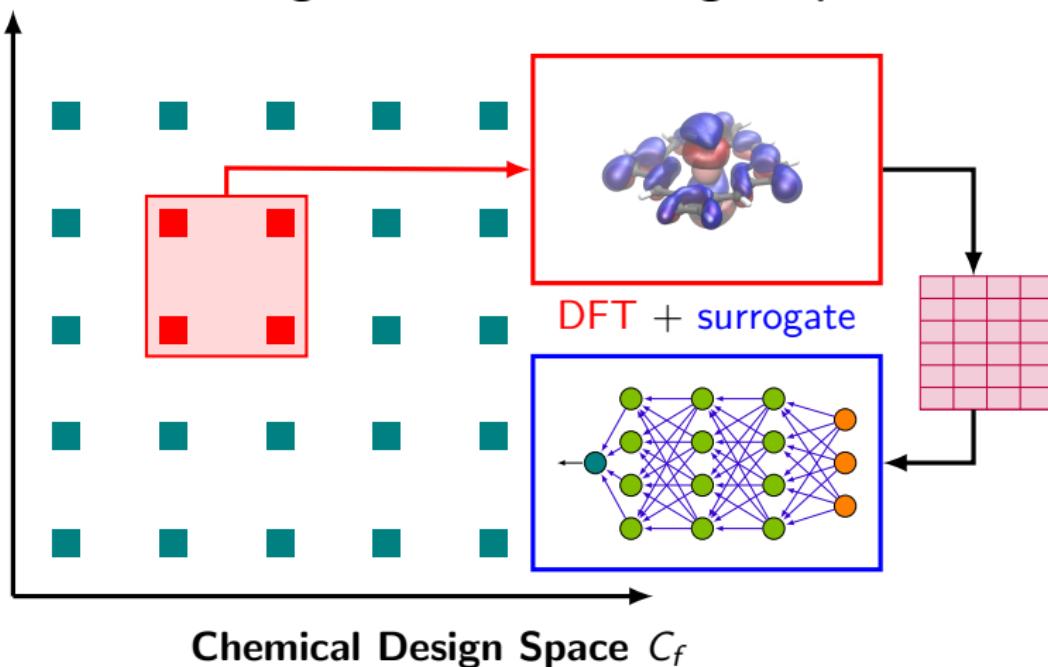
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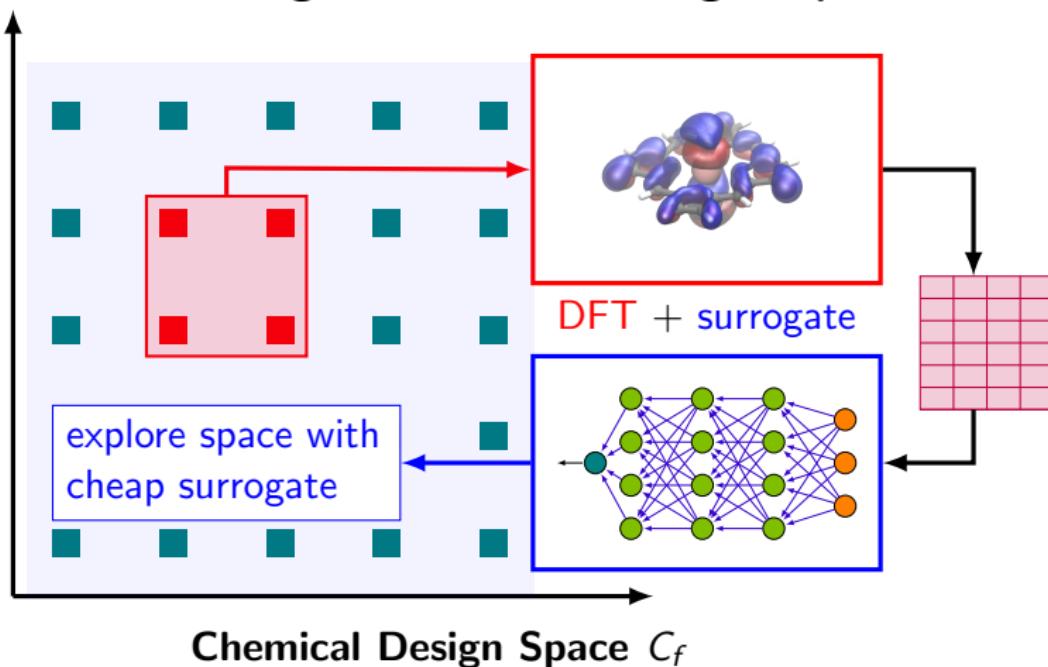
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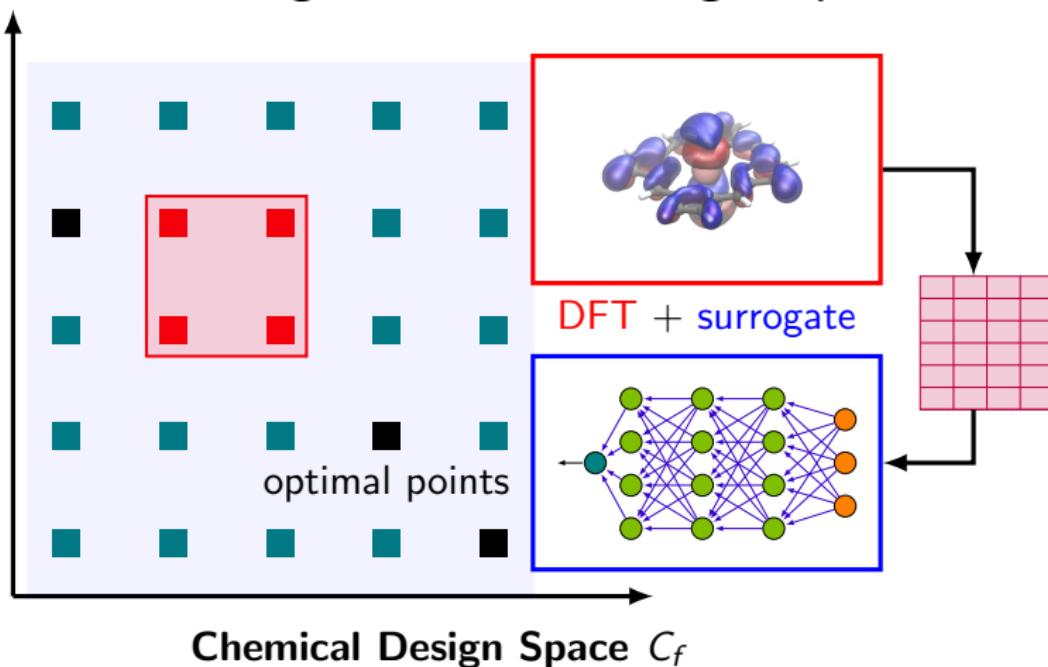
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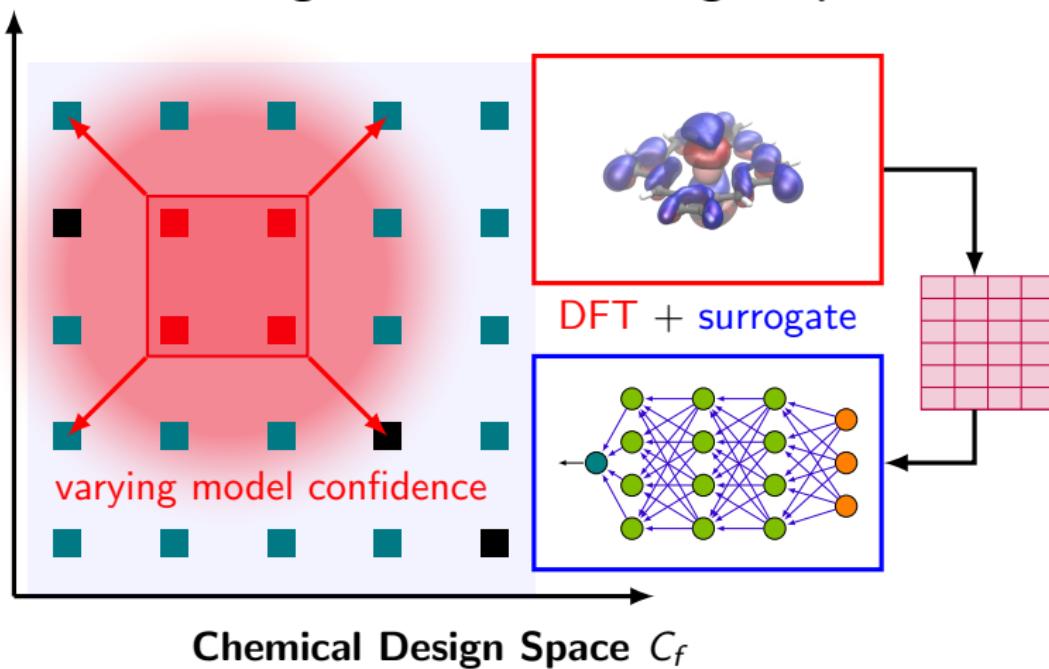
Motivation: chemical discovery

How can we design new materials using computers?



Motivation: chemical discovery

How can we design new materials using computers?



Introduction

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Features and models

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Uncertainty

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Discovery

○○

Case Study

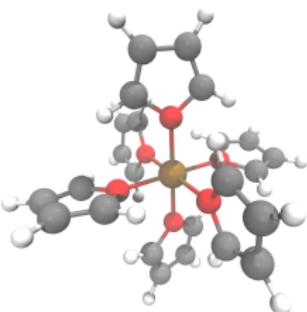
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Conclusions

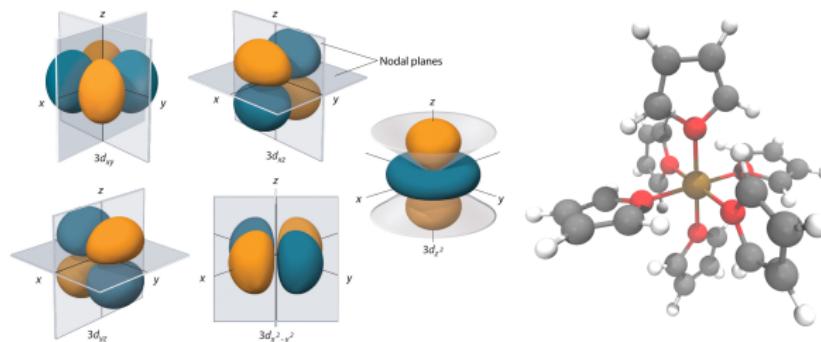
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Transition metal complexes

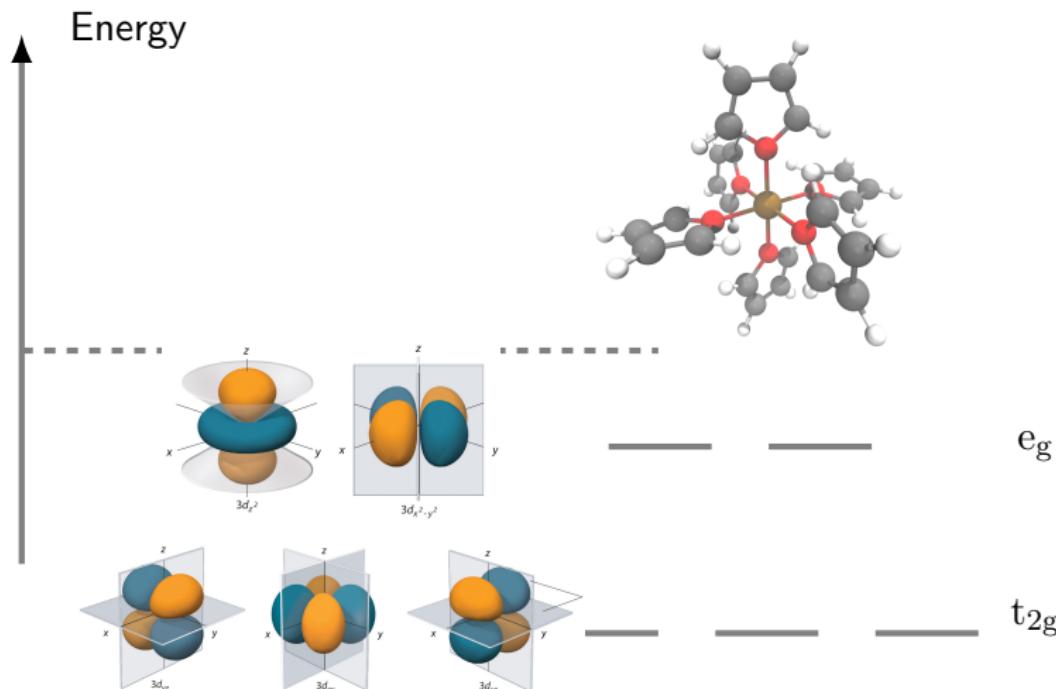
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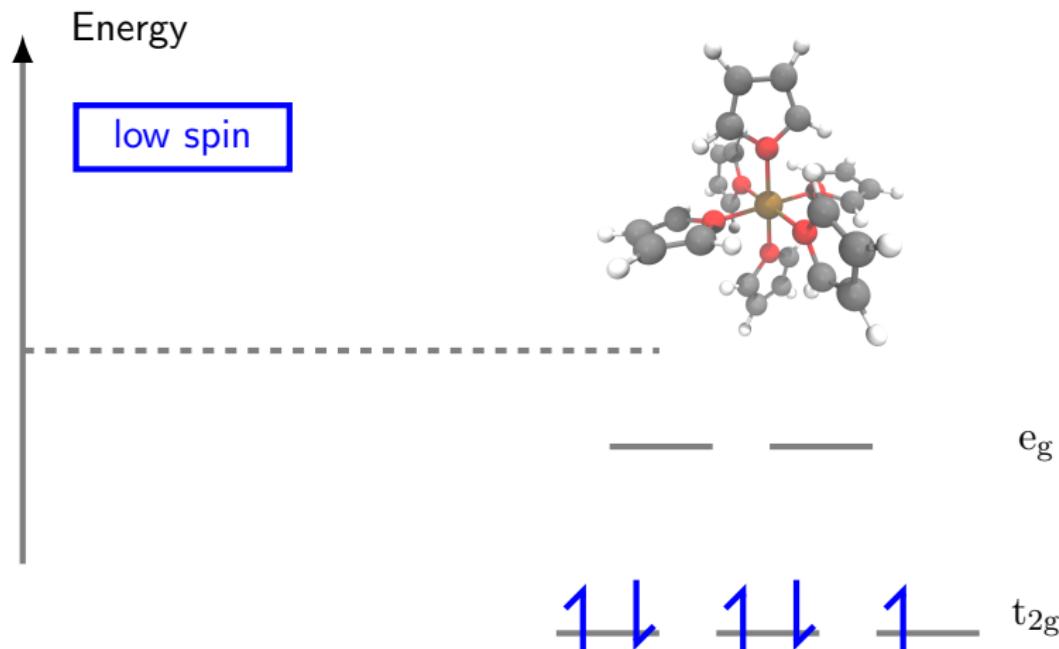
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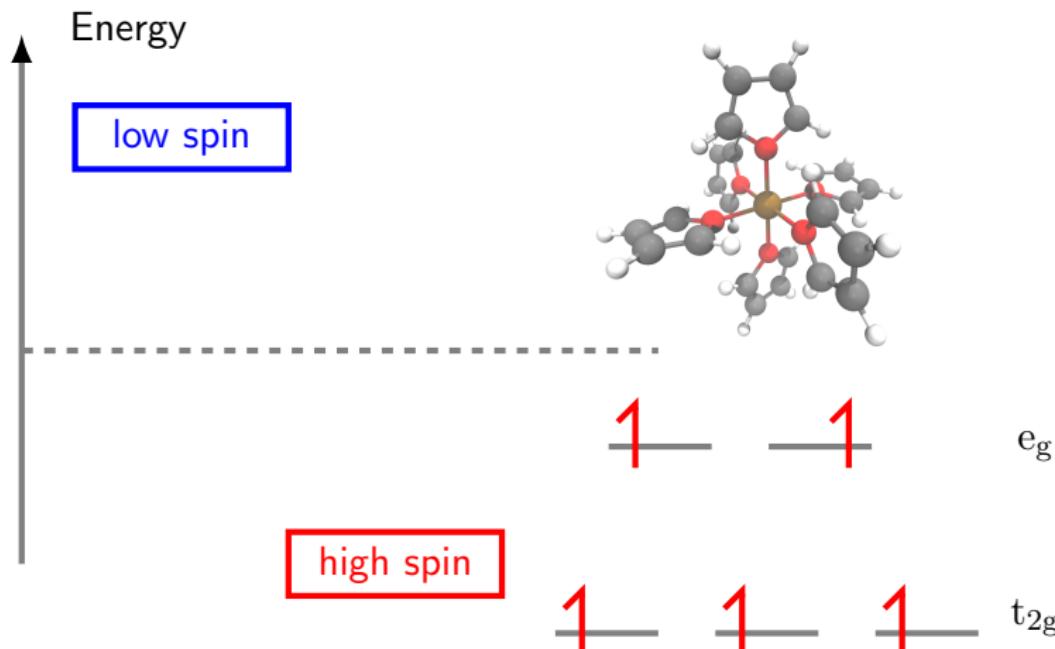
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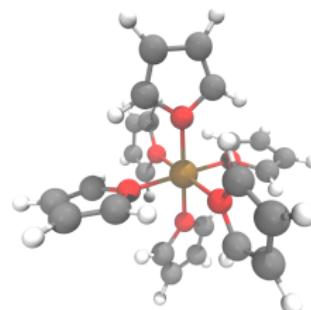
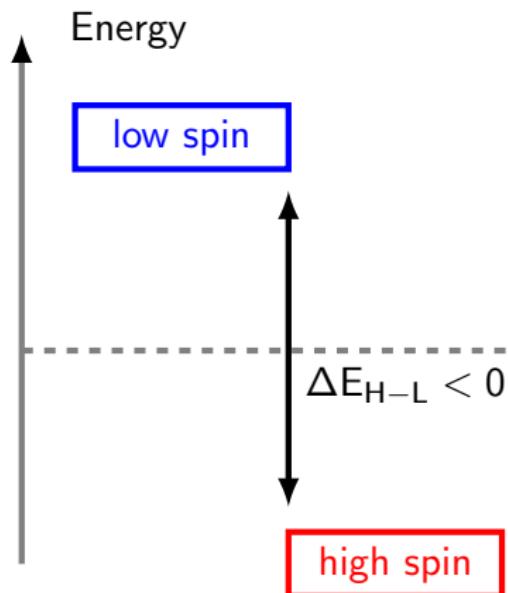
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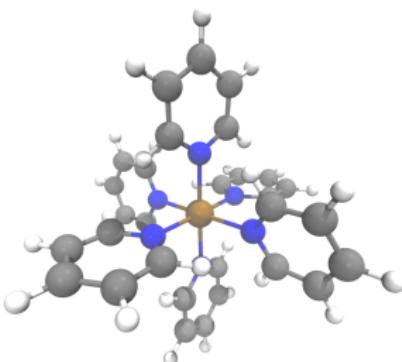
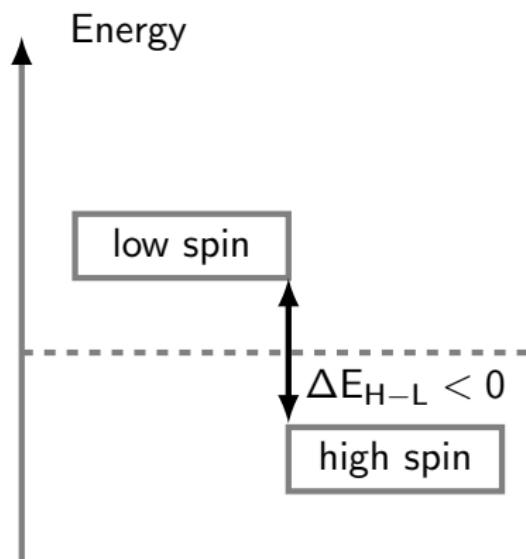
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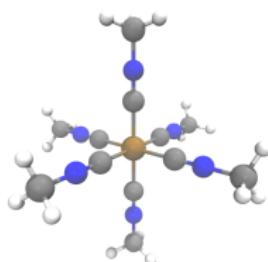
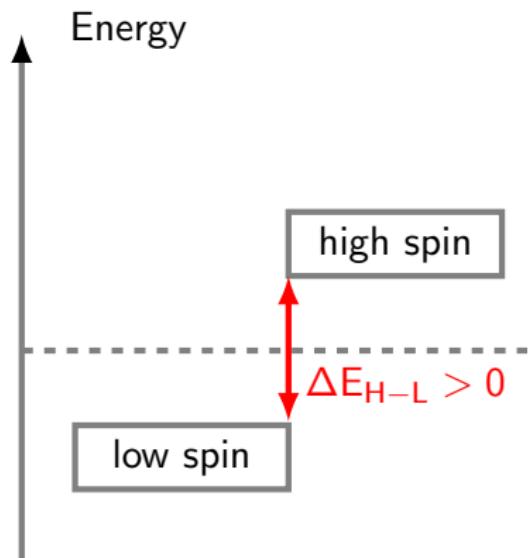
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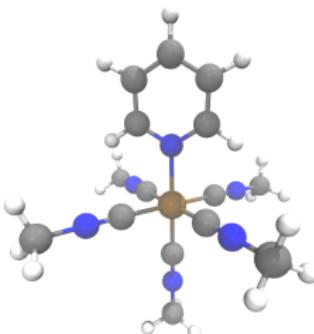
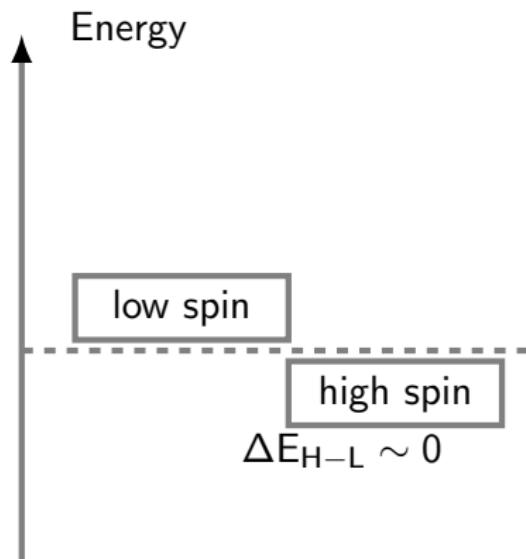
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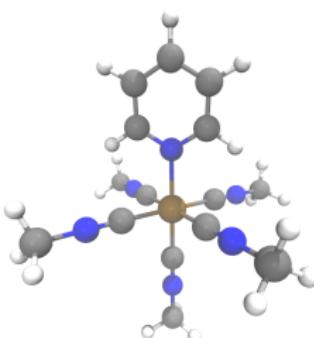
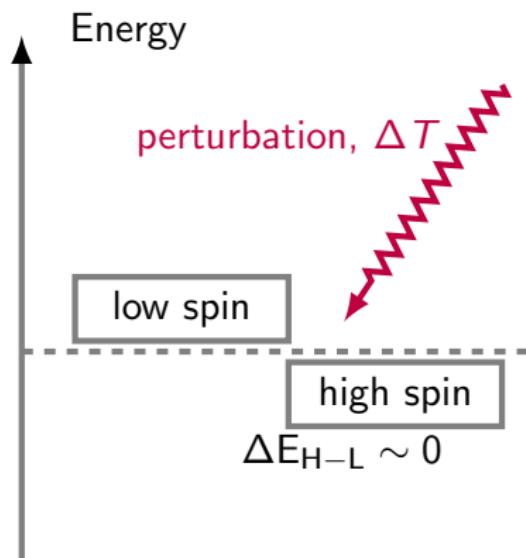
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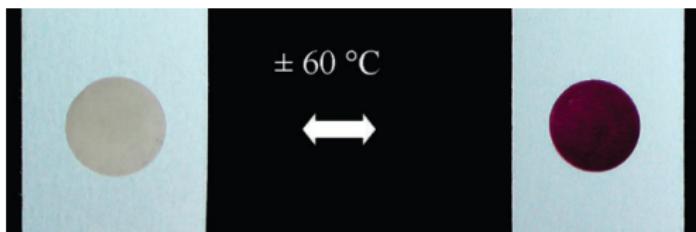
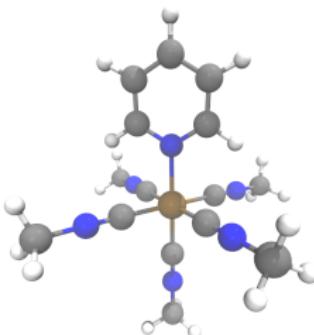
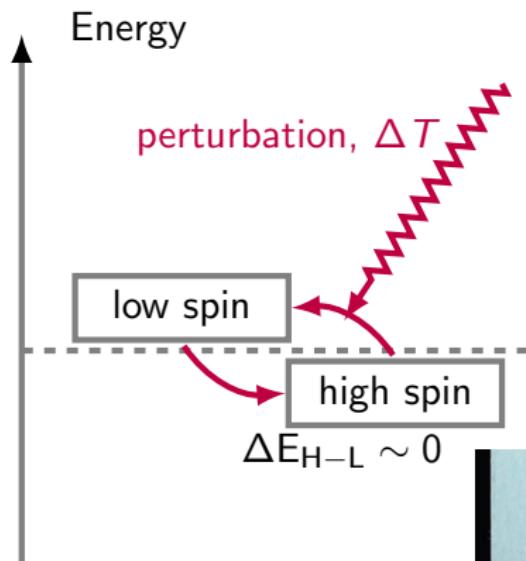
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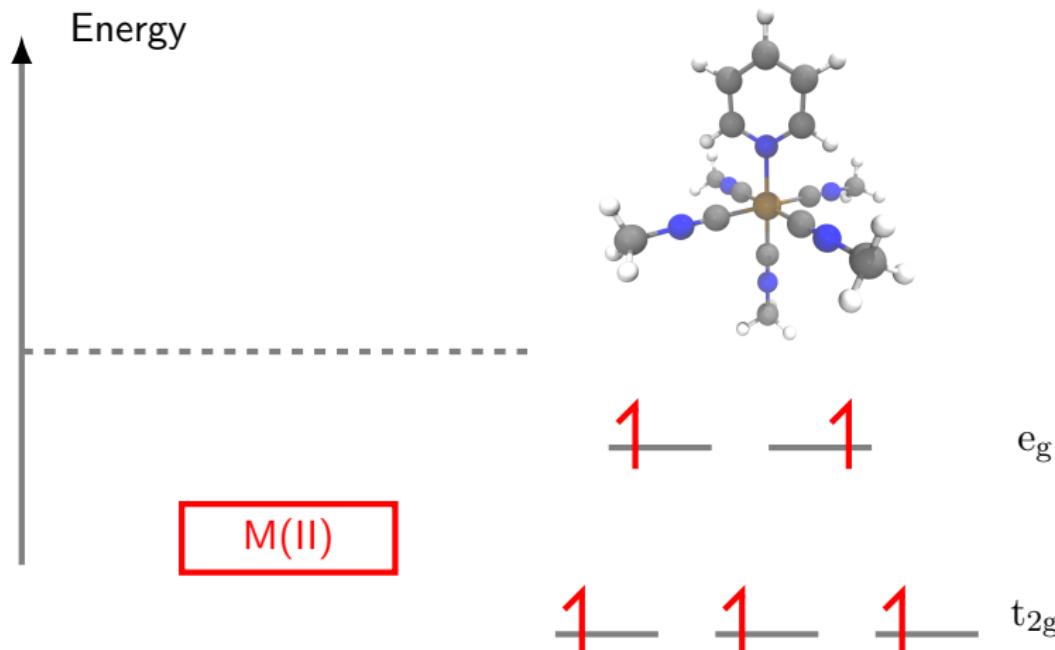


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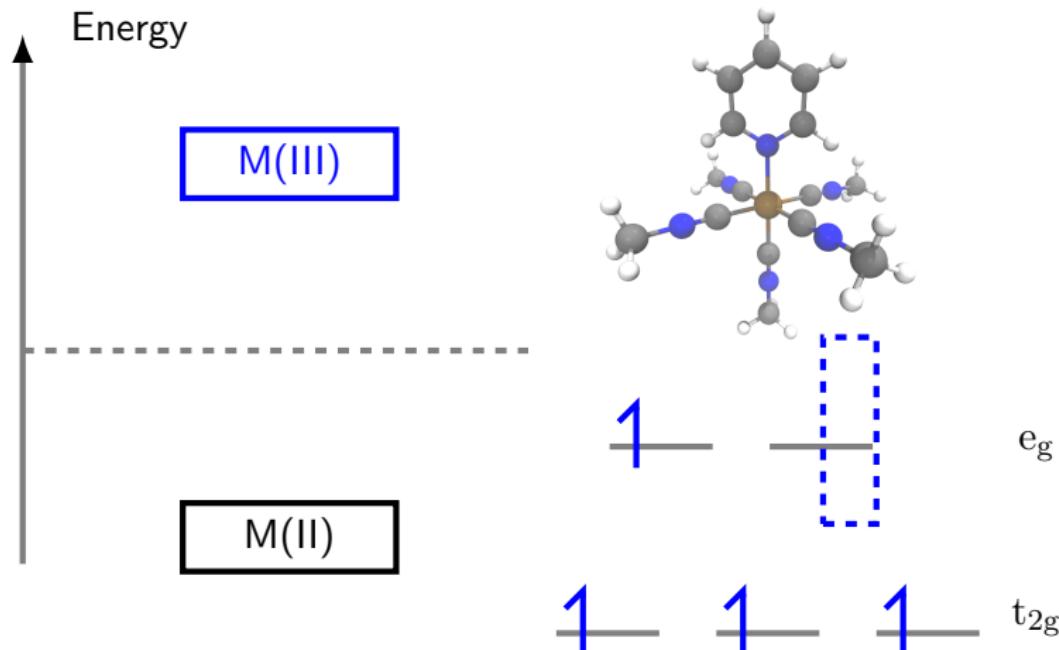


Seredyuk, M et al., *Chem. Mater.*, 18(10):2513–2519, 2006.

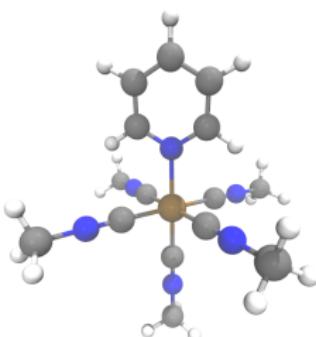
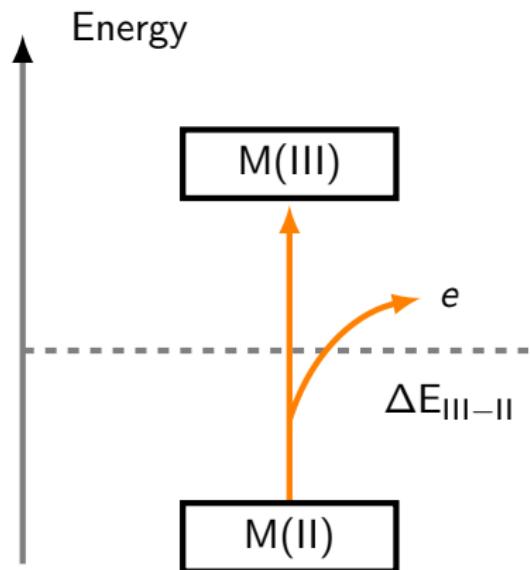
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Algorithmic chemical discovery

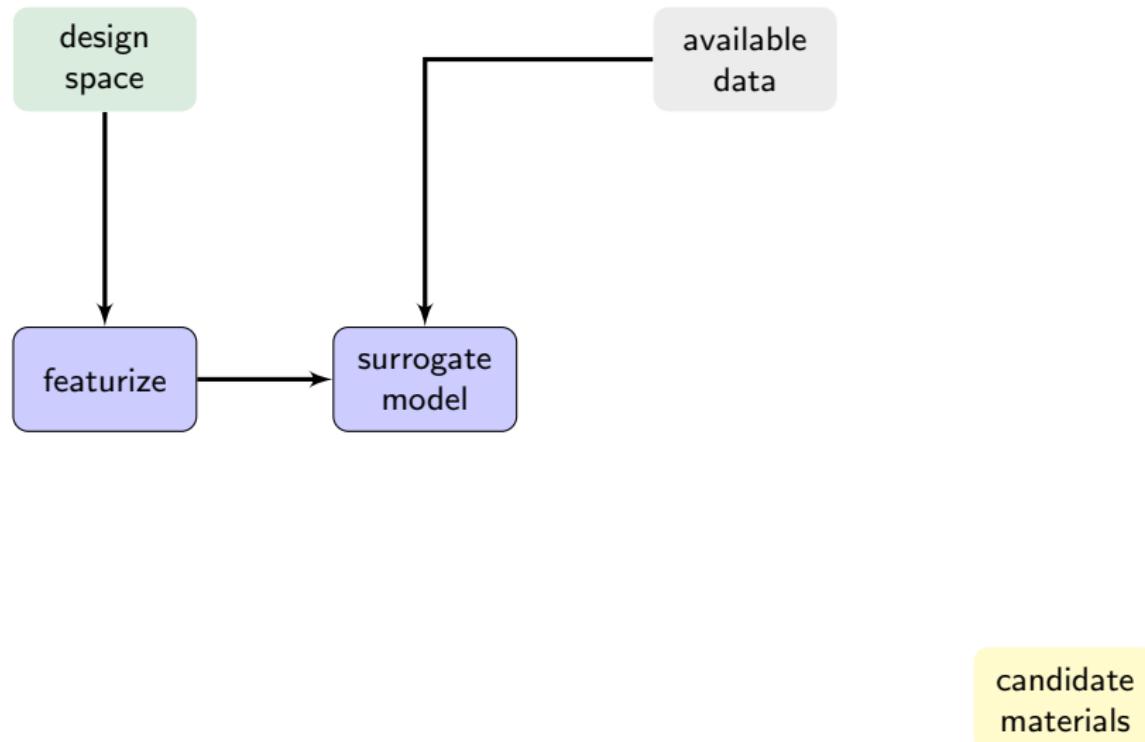
design
space

candidate
materials

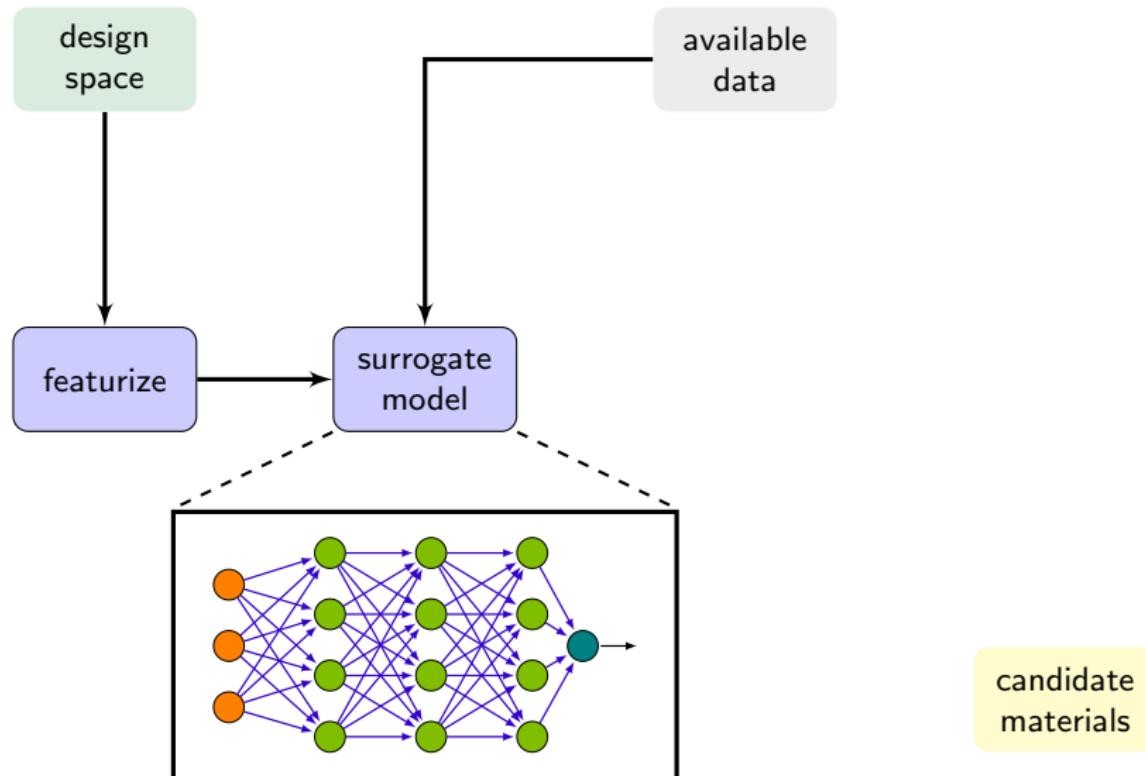
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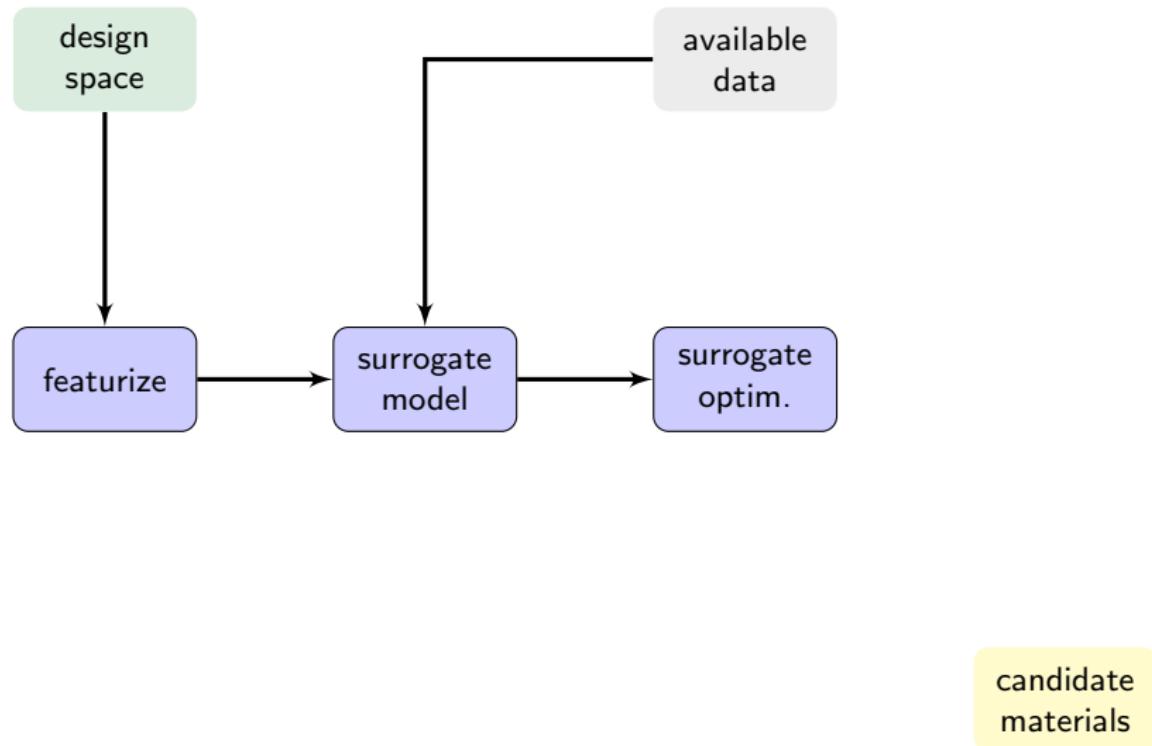
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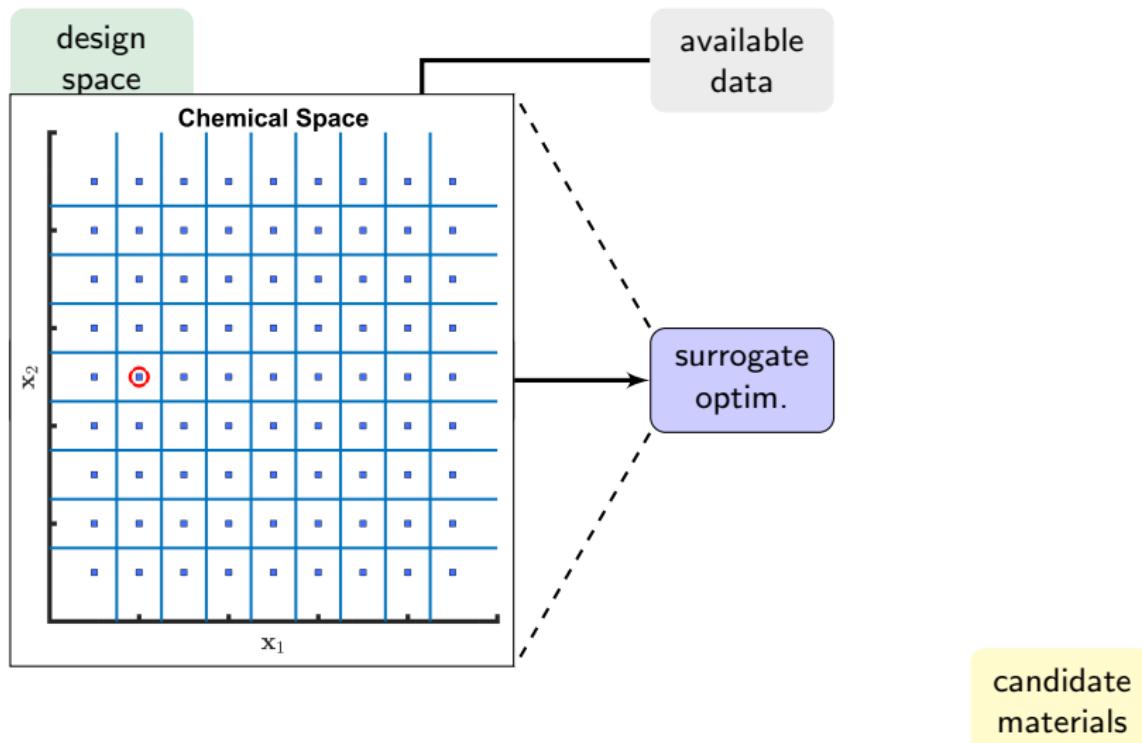
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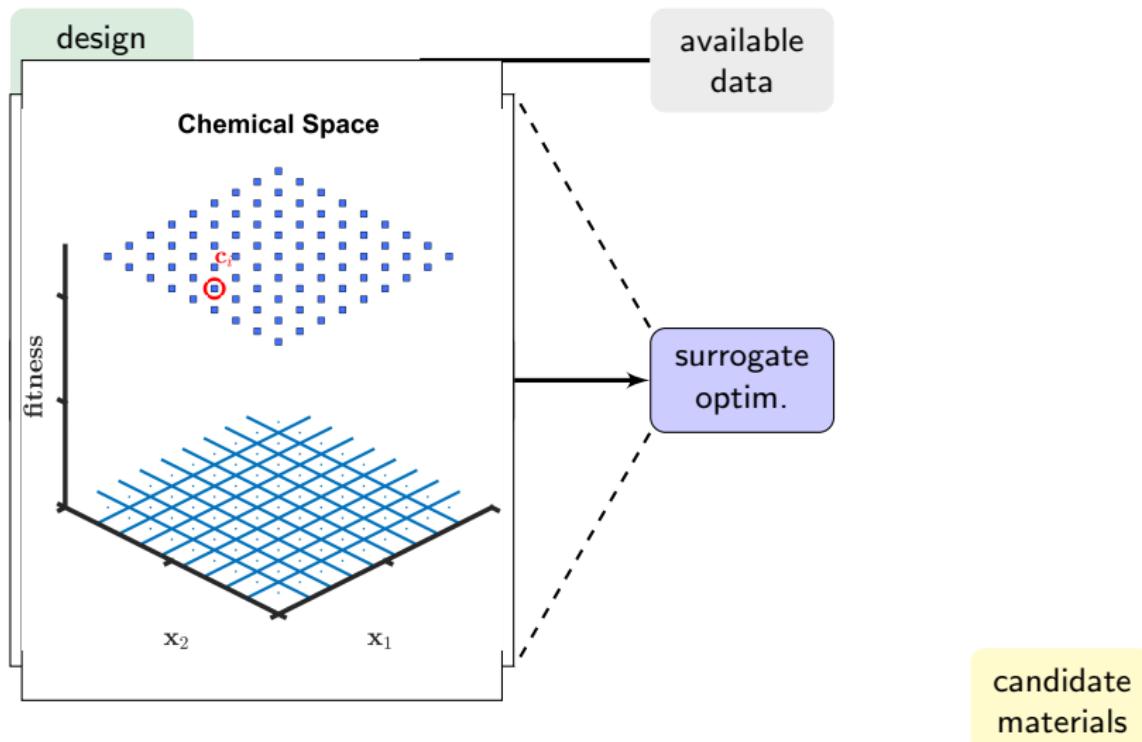
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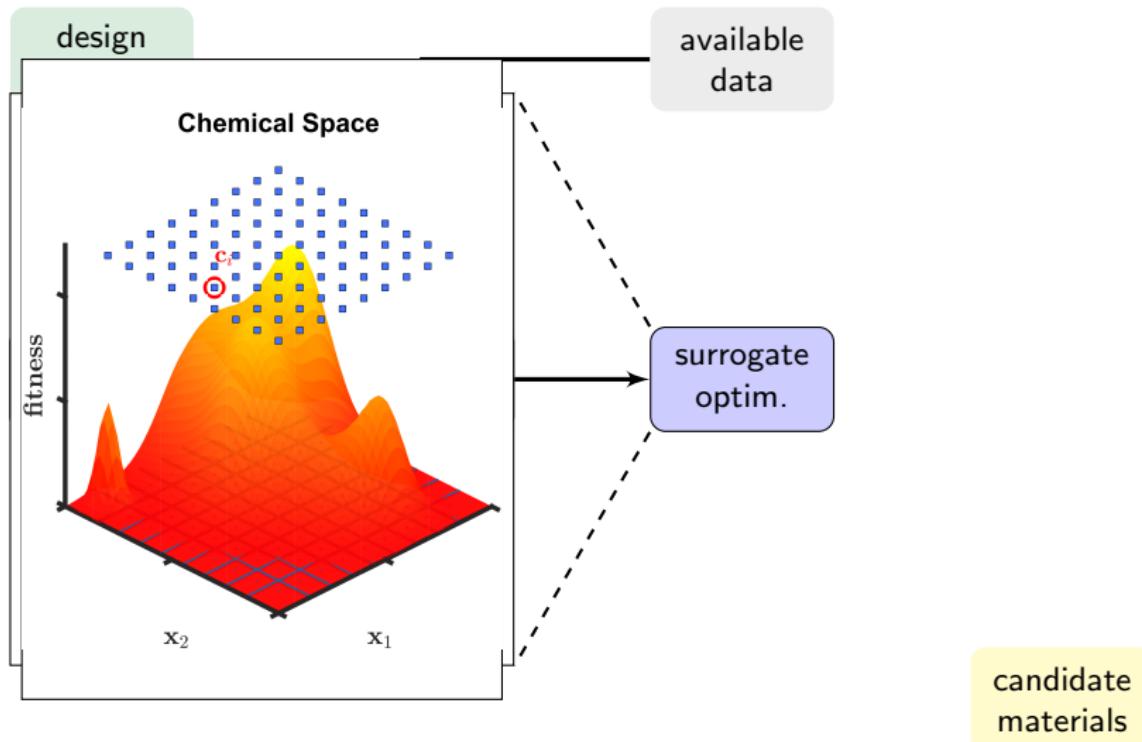
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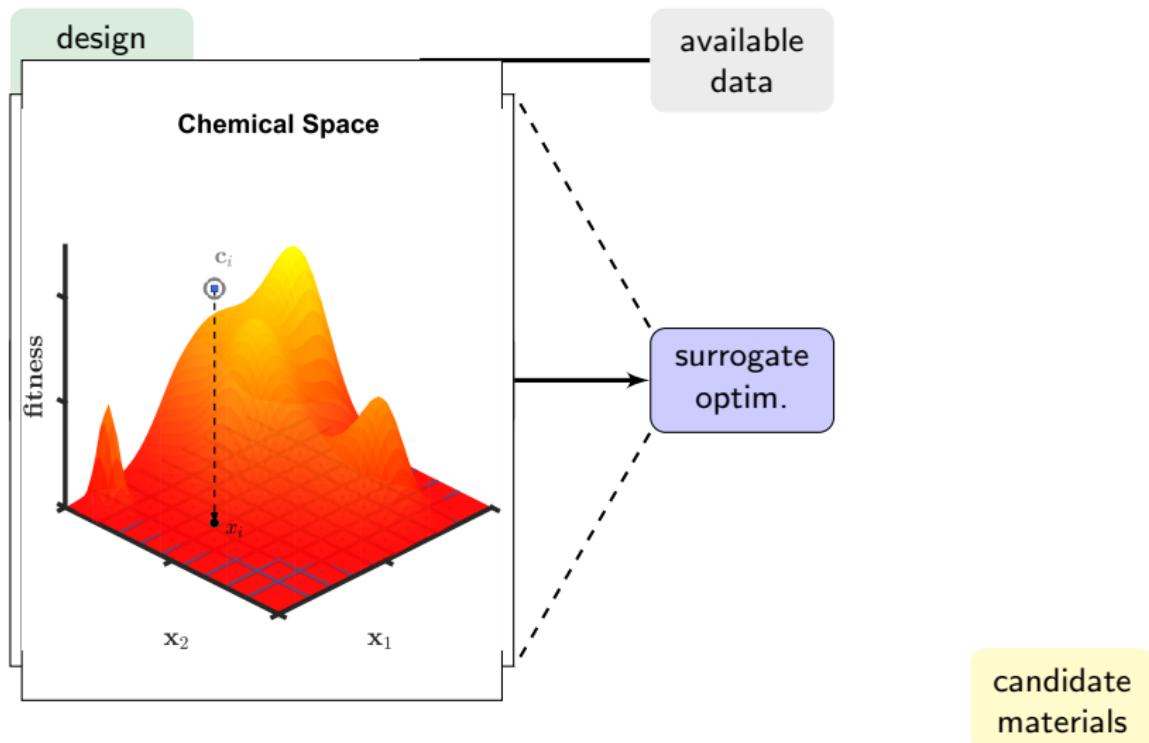
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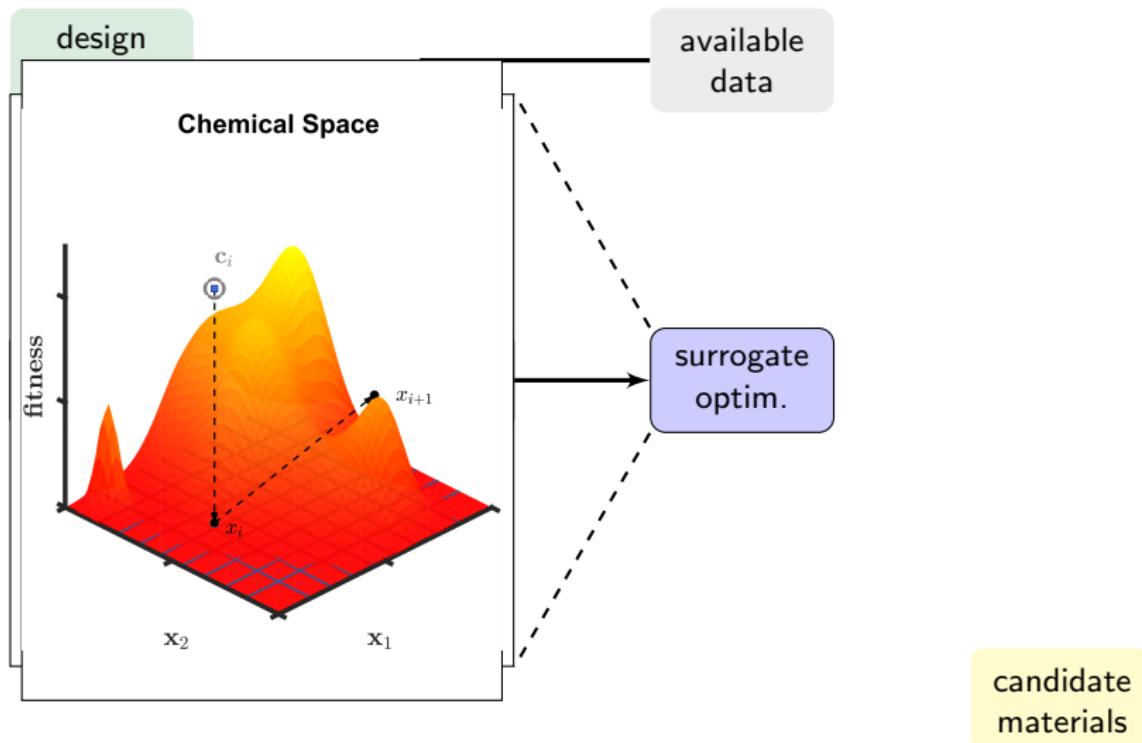
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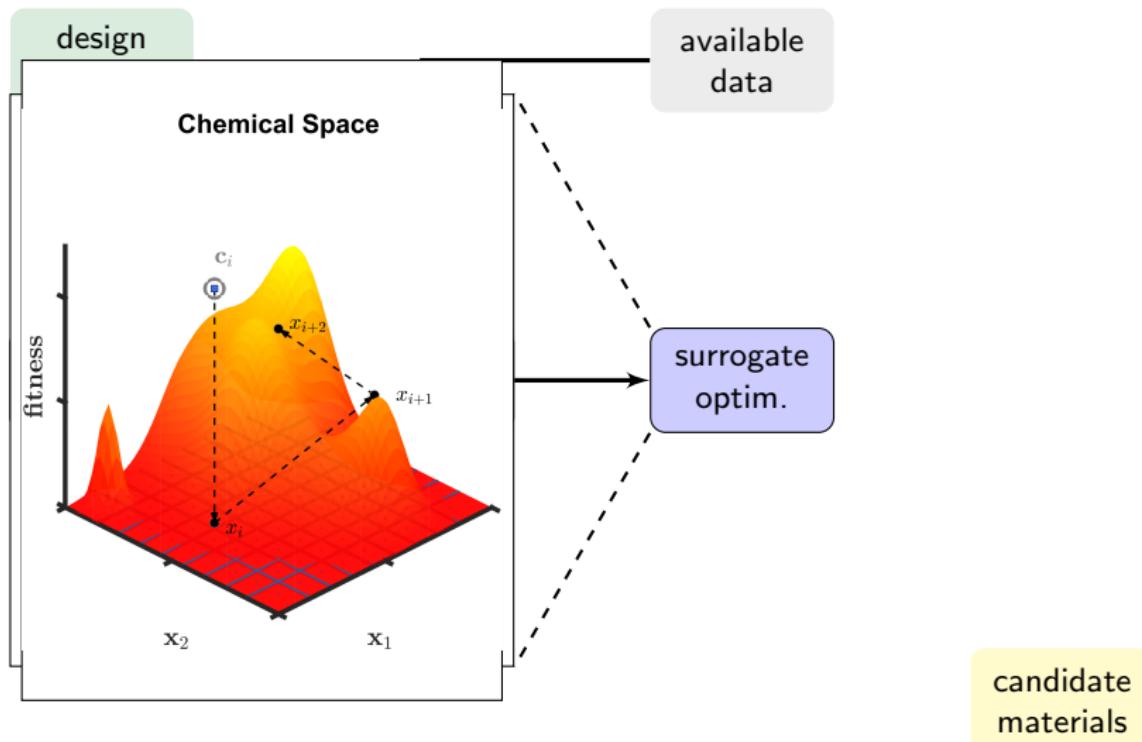
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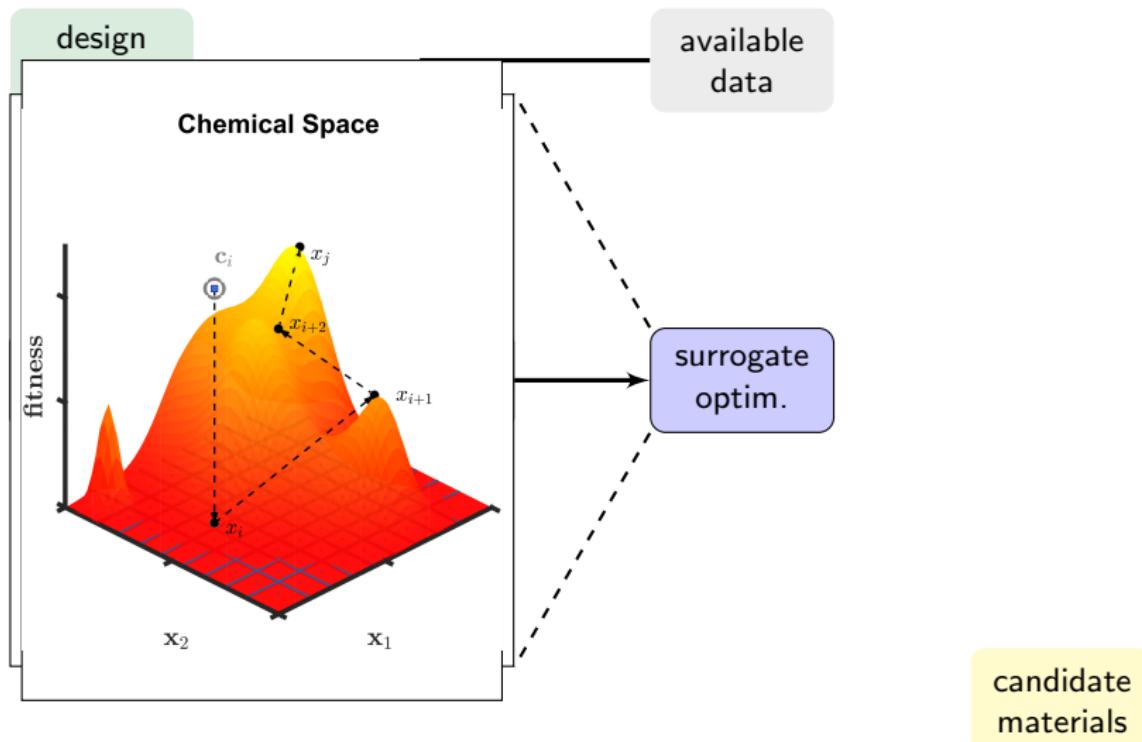
Algorithmic chemical discovery



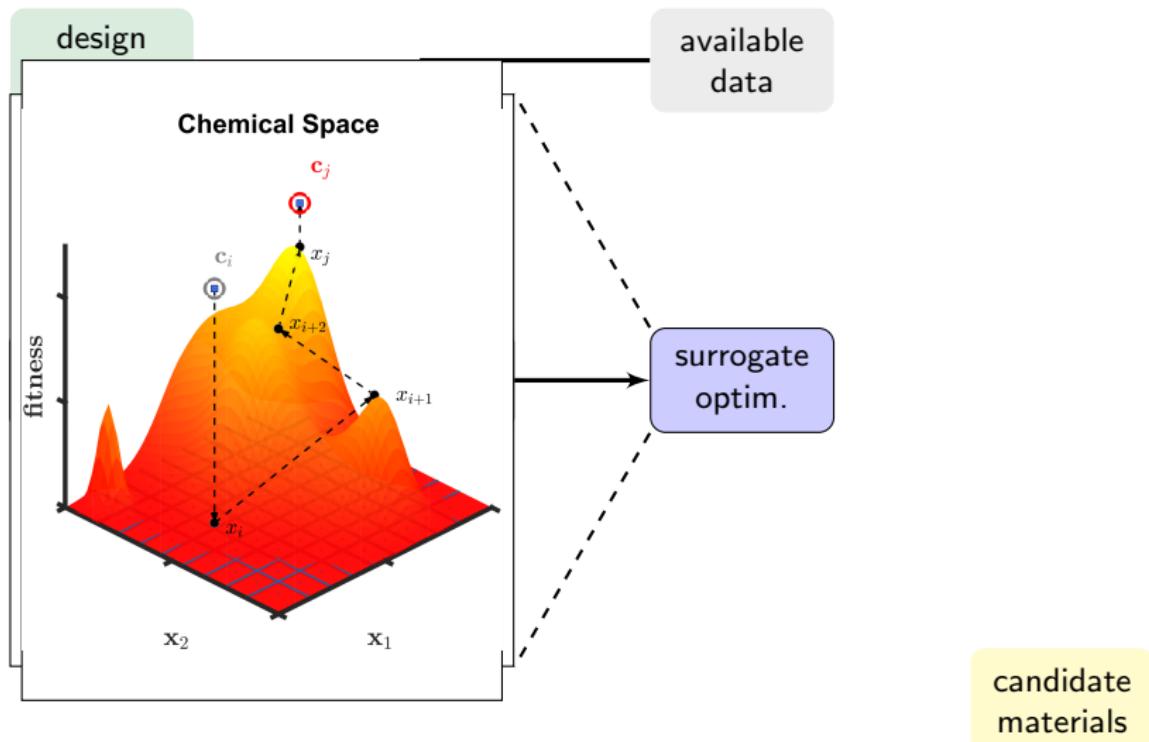
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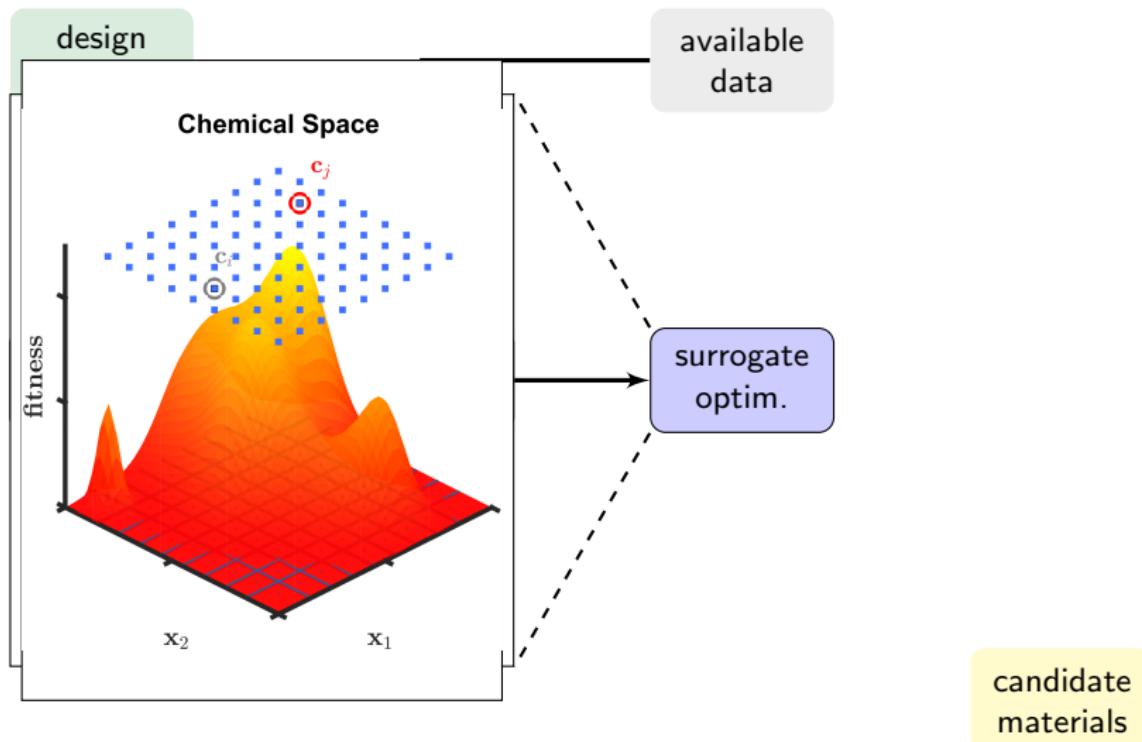
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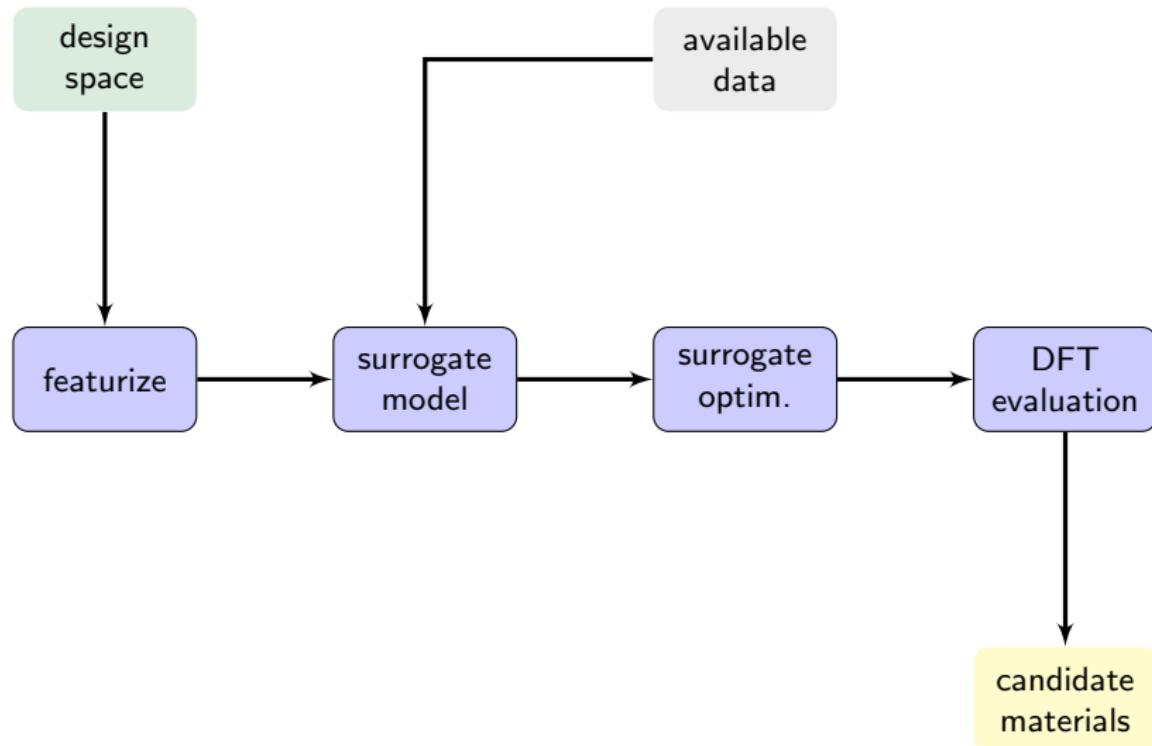
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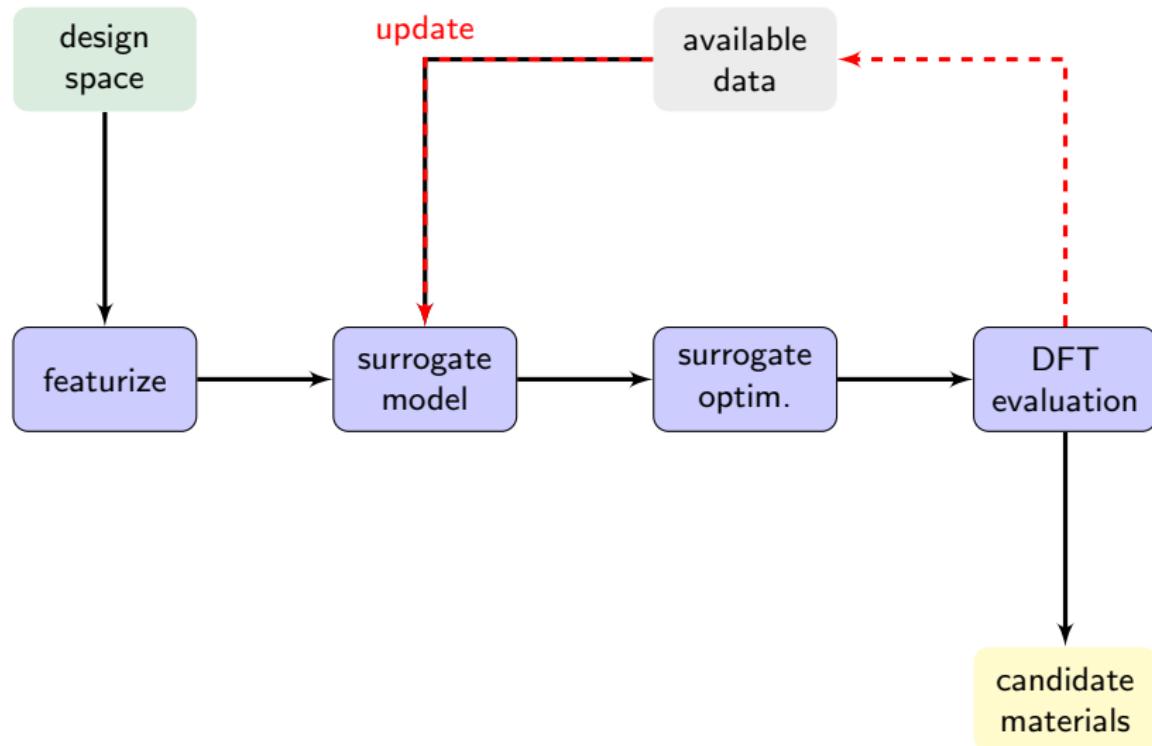
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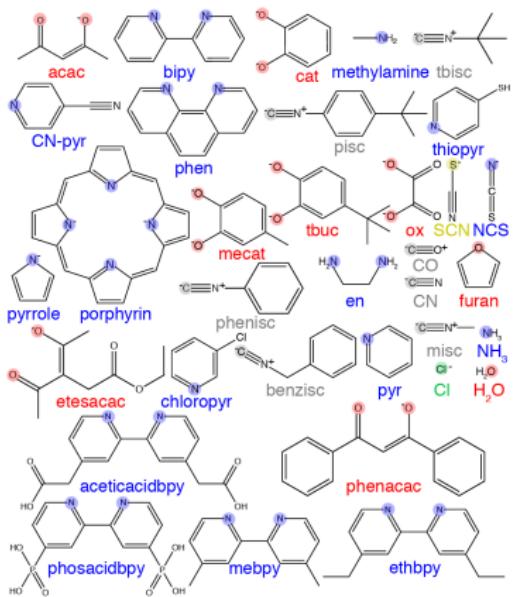


First-principles calculations

train on $\sim 100\text{--}2000$ DFT calculations:

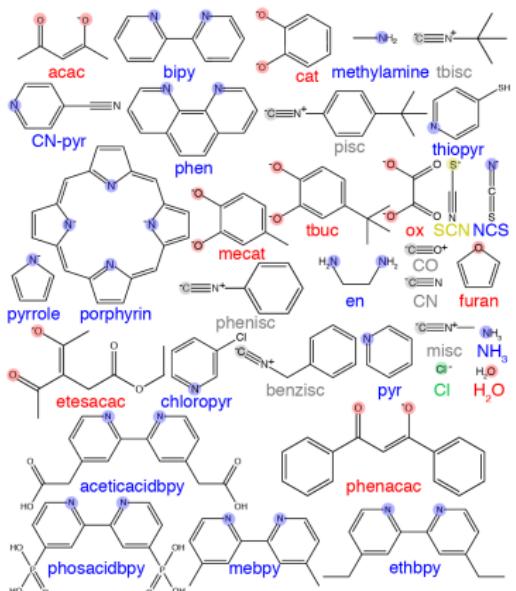
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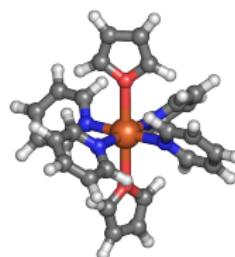
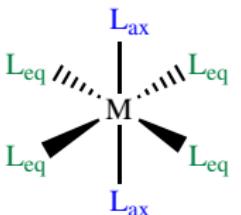
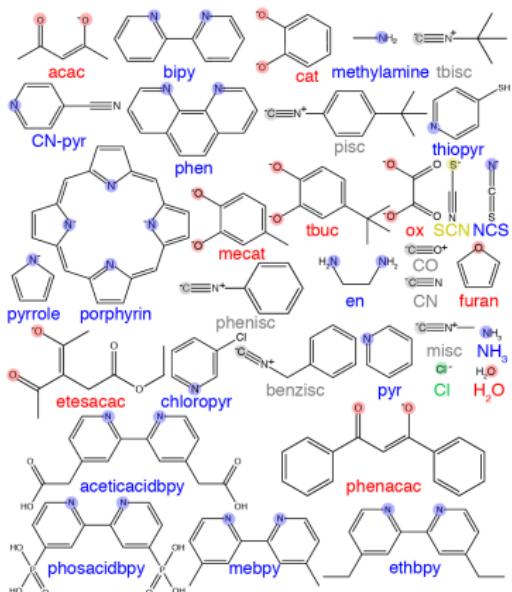
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Cr	Mn	Fe	Co
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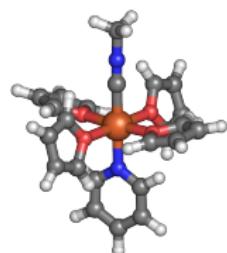
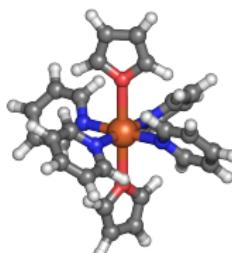
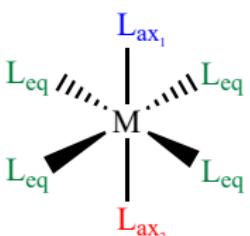
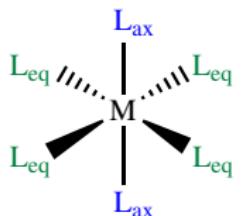
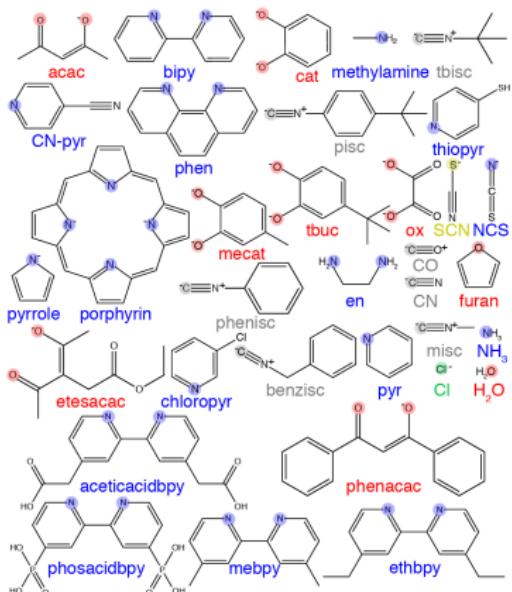
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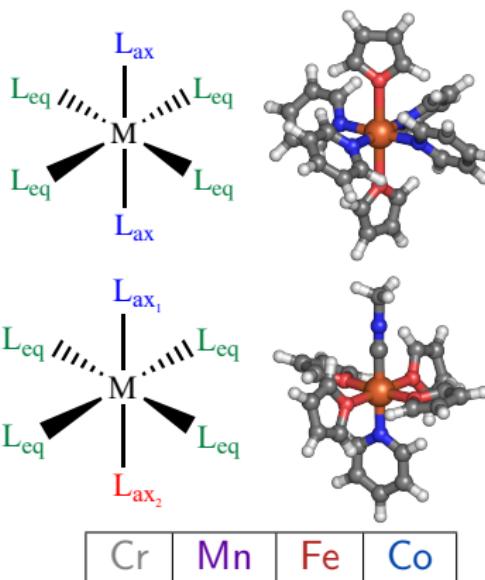
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First-principles calculations

train on $\sim 100\text{--}2000$ DFT calculations:

Details:

- B3LYP-like DFT
- gas phase optimization
- LANL2DZ/6-31G*
- COSMO solvents
- high- and low-spin M(II)/(III)



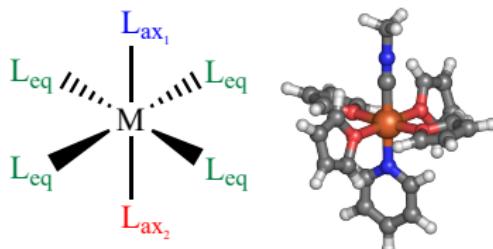
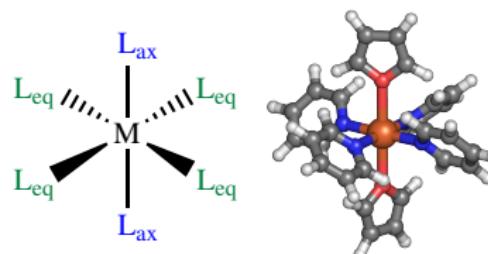
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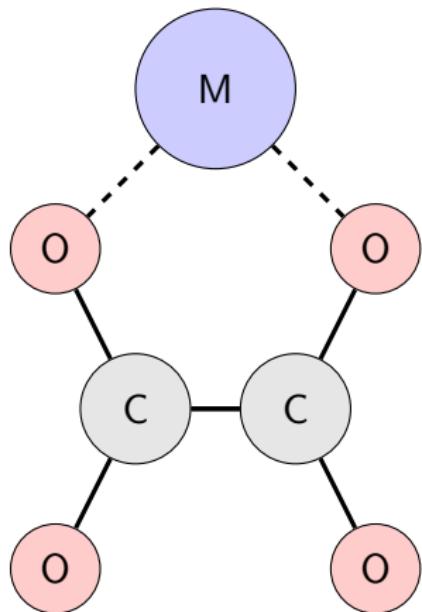
↗ HF exchange varied 0–30%



Cr	Mn	Fe	Co
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Featurization with RACs

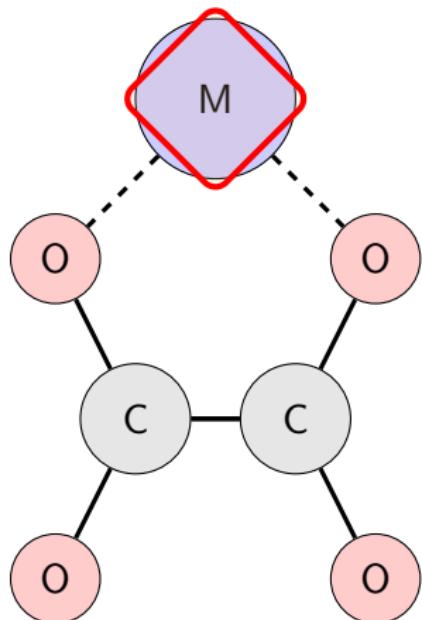
Graph-based features designed for TM complexes



Janet, J.P., and Kulik, H.J., *J. Phys. Chem. A*, 121(46):8939–8954, 2017.

Featurization with RACs

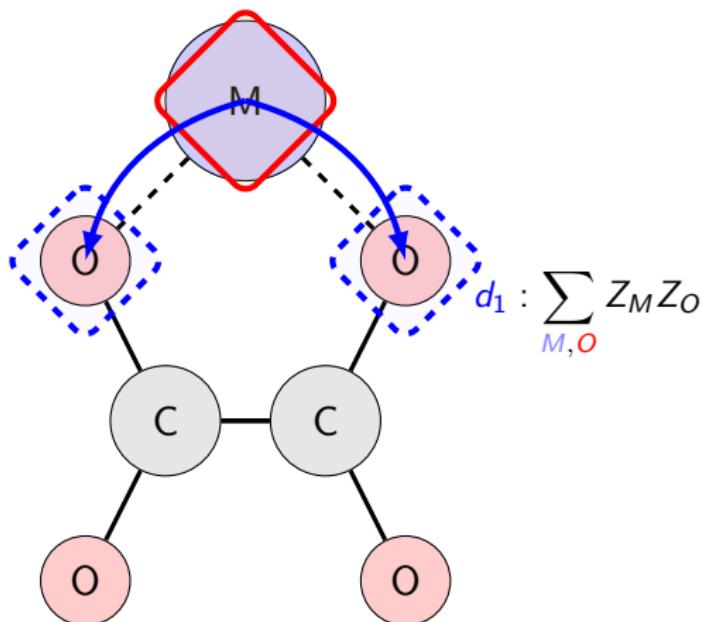
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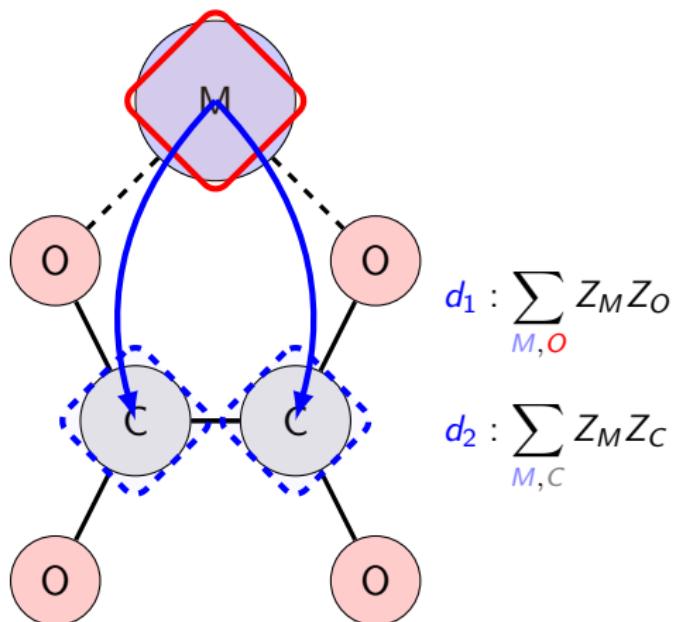
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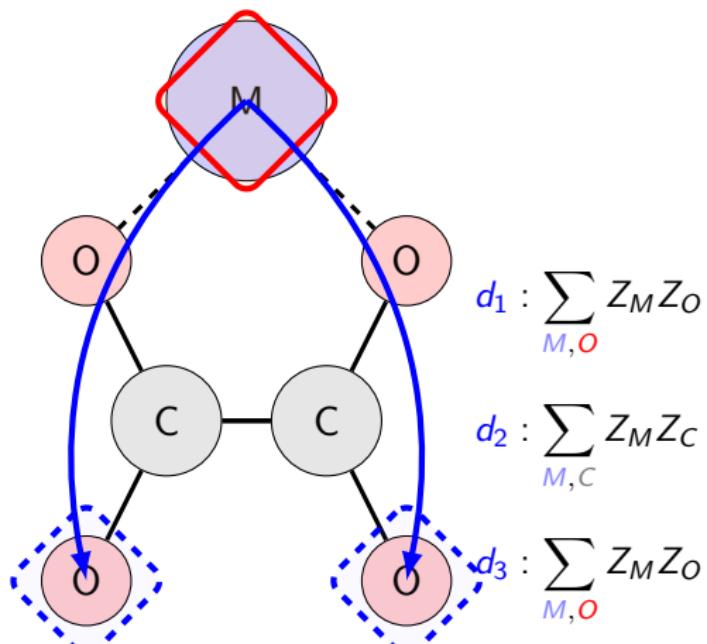
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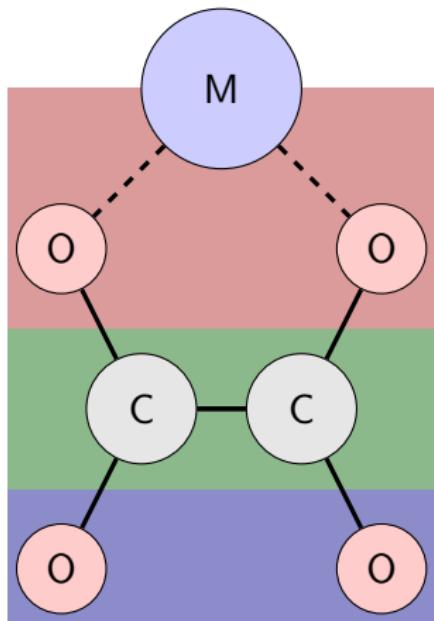
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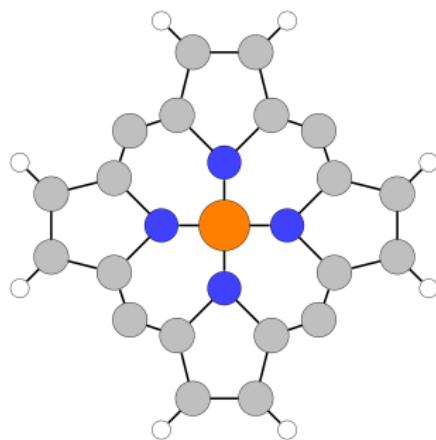
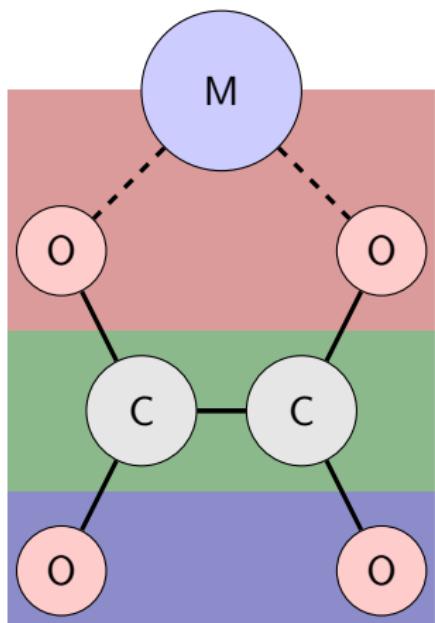
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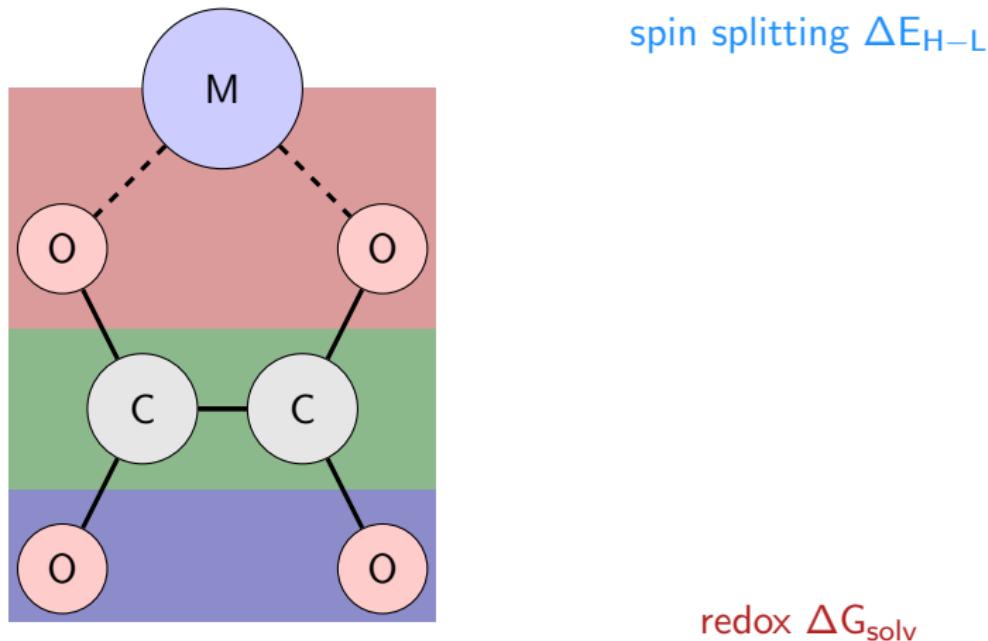
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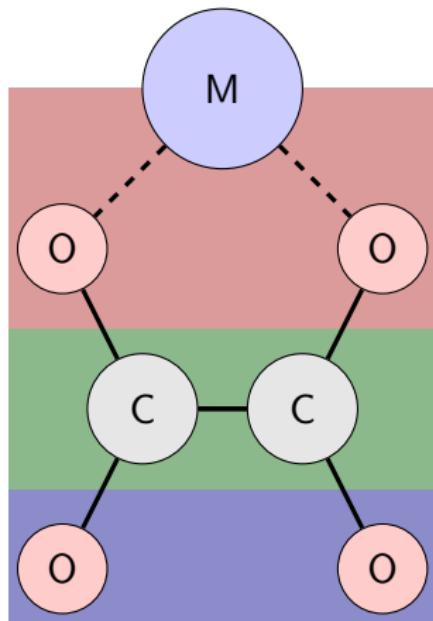
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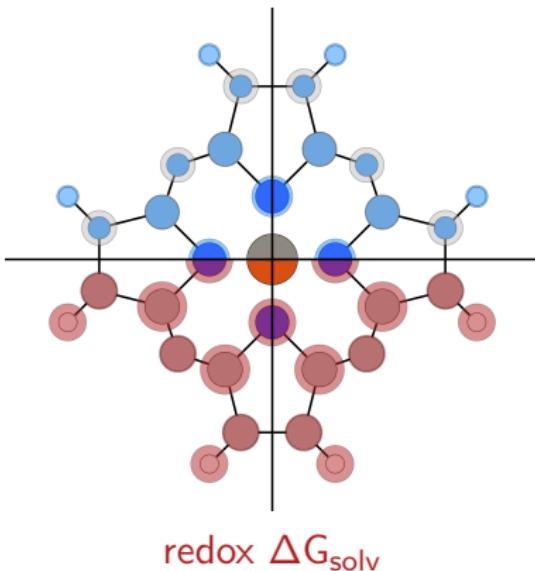
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spin splitting ΔE_{H-L}

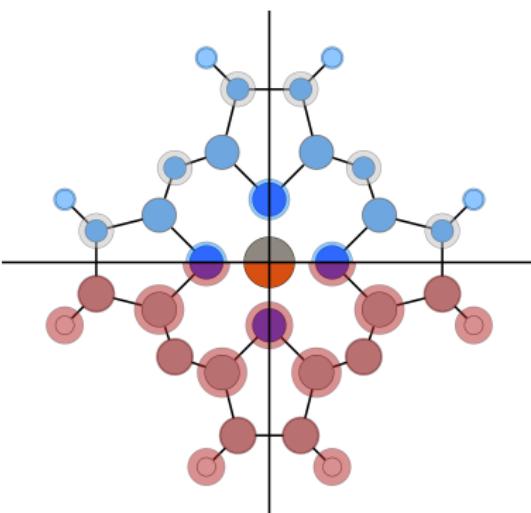
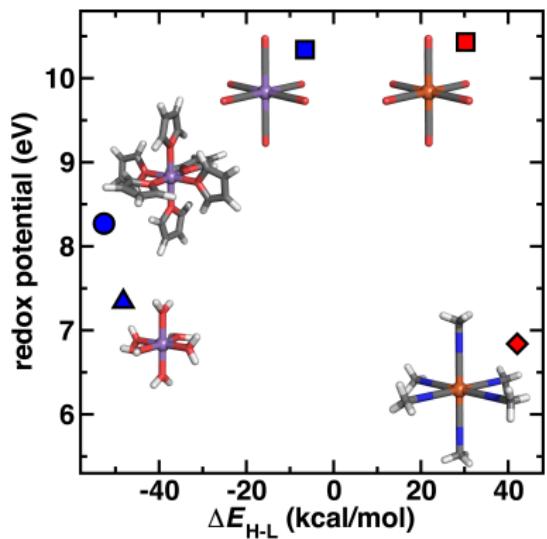


redox ΔG_{solv}

Janet, J.P., and Kulik, H.J., *J. Phys. Chem. A*, 121(46):8939–8954, 2017.

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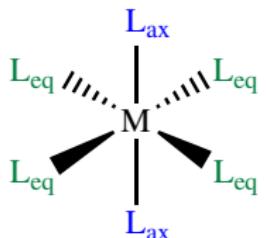
Janet, J.P. et al., *Inorg. Chem.*, 58(16):10592–10606, 2019.

Property inference with ANNs

Estimate properties using small artificial neural networks (ANNs)

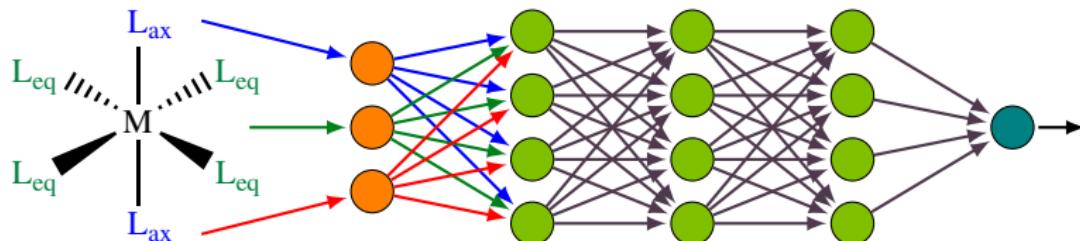
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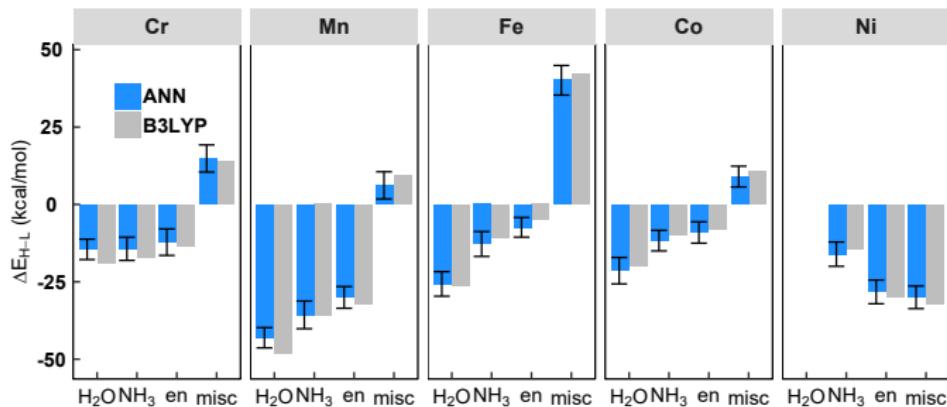
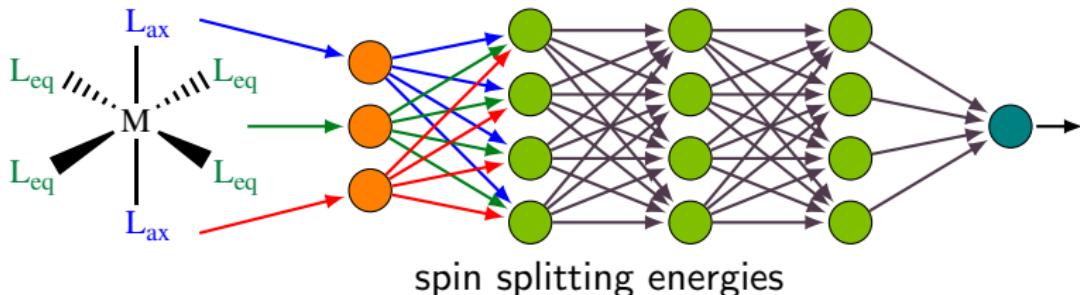
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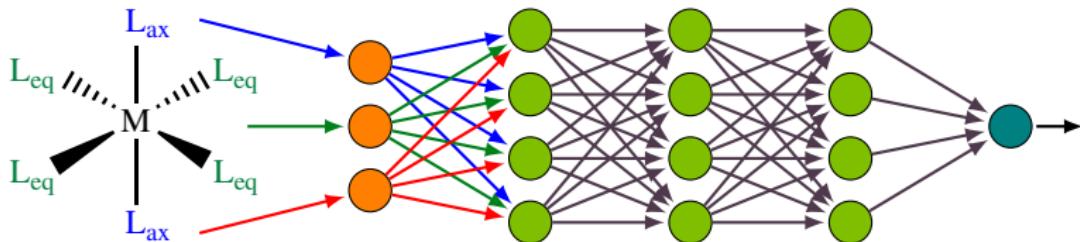
Property inference with ANNs

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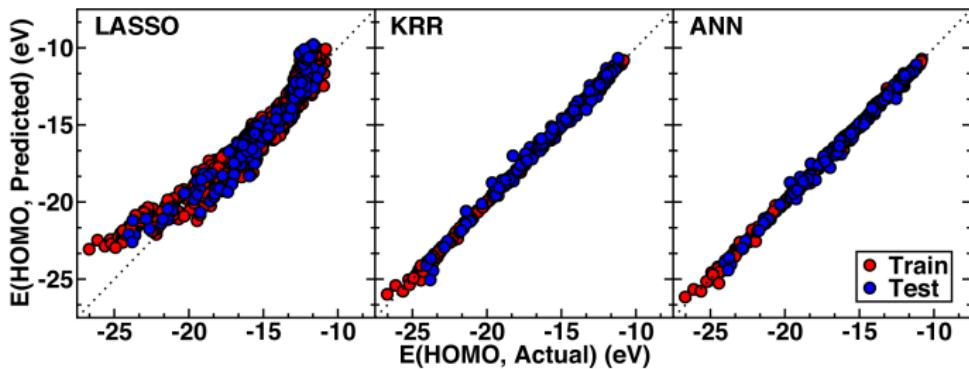


Property inference with ANNs

Estimate properties using small artificial neural networks (ANNs)



frontier orbital properties



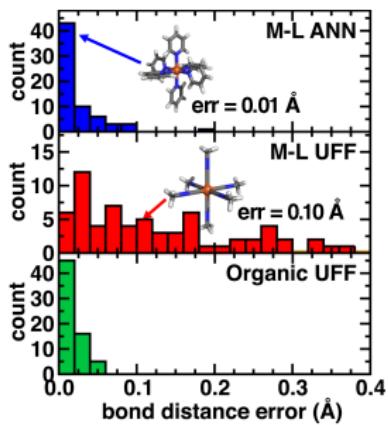
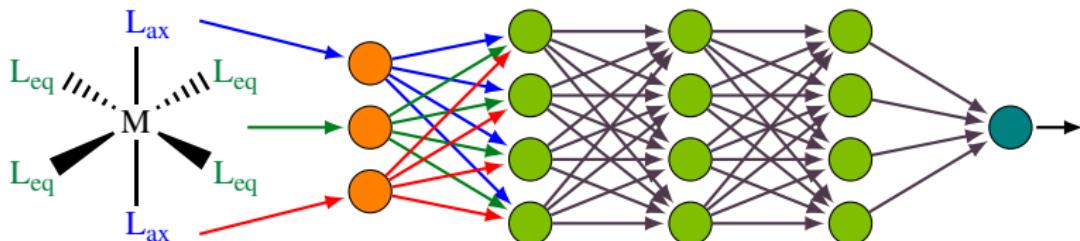
ANN: 500×500 ReLU nodes, fully connected

Nandy, A. et al., Ind. Eng. Chem. Res., 57(42):13973–13986, 2018.

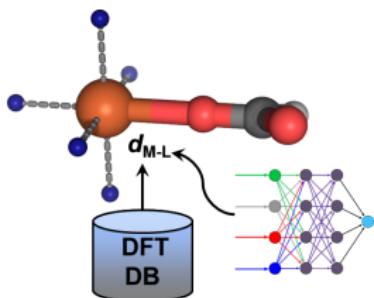
KRR: RFB + feature selection

Property inference with ANNs

Estimate properties using small artificial neural networks (ANNs)



DFT equilibrium bond lengths



Janet, J.P. et al., *Ind. Eng. Chem. Res.*, 56(17):4898–4910, 2017.

Janet, J.P. et al., *Inorg. Chem.*, 58(16):10592–10606, 2019. 300 × 200 × 200 tanh nodes, fully connected

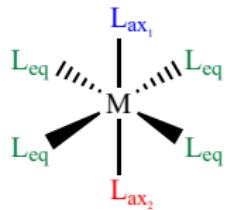
Beyond prediction: live job management

In high-throughput DFT screening, job failure is a frequent issue:

Beyond prediction: live job management

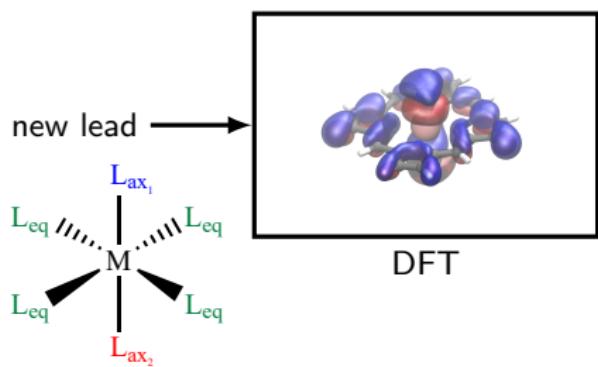
In high-throughput DFT screening, job failure is a frequent issue:

new lead



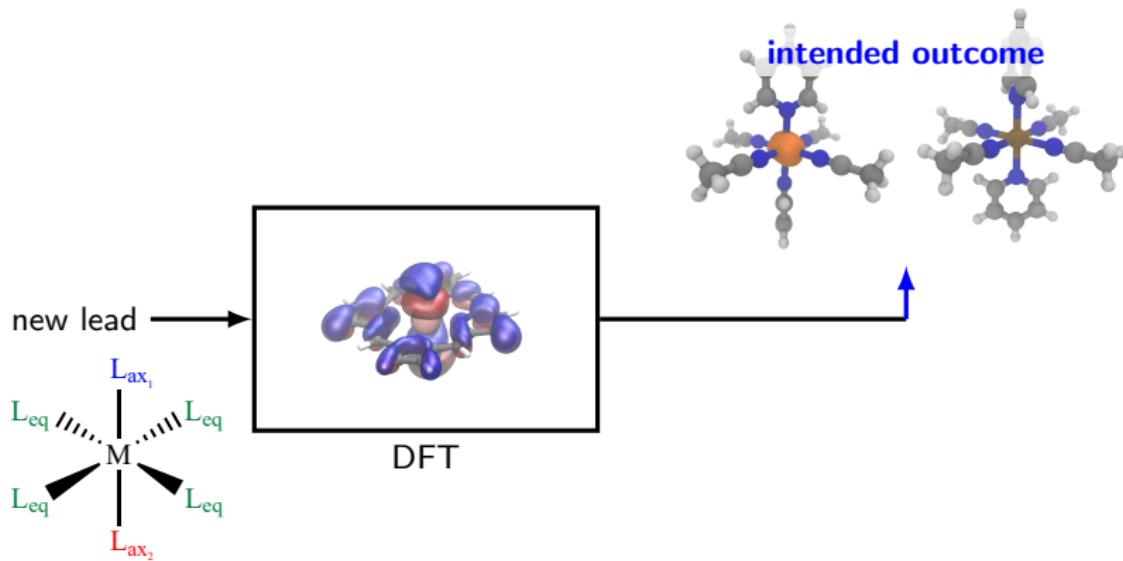
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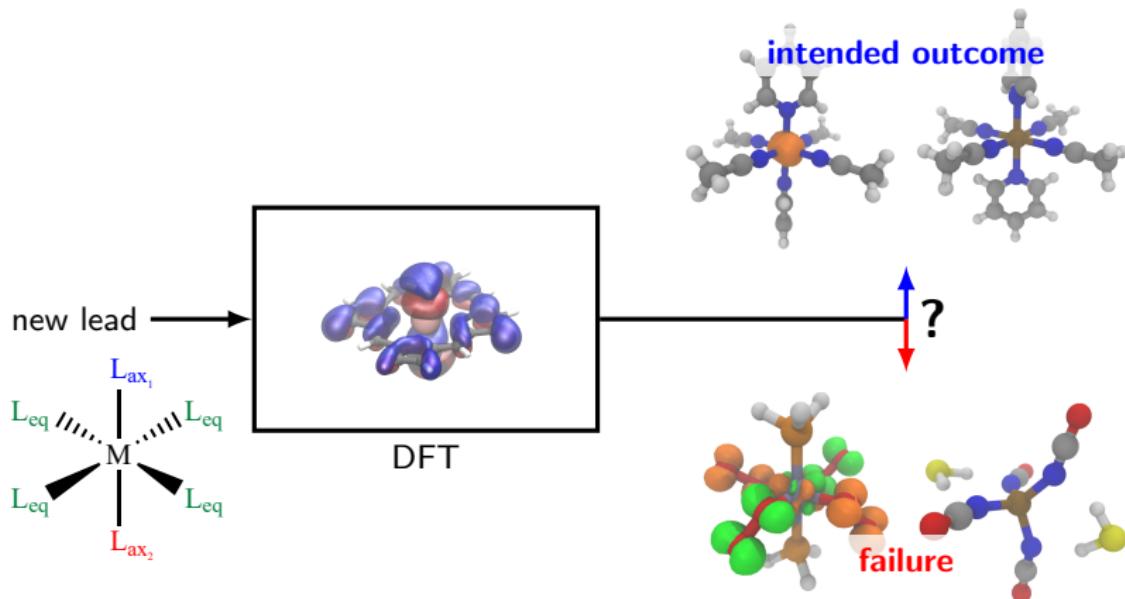
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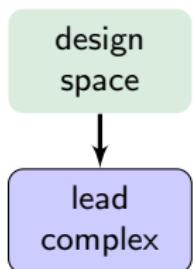


Beyond prediction: live job management

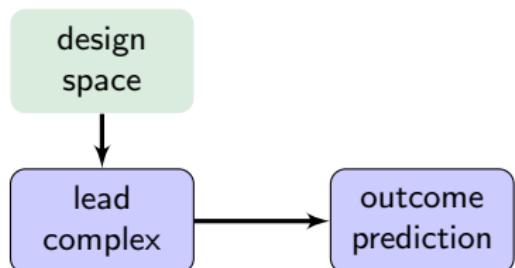
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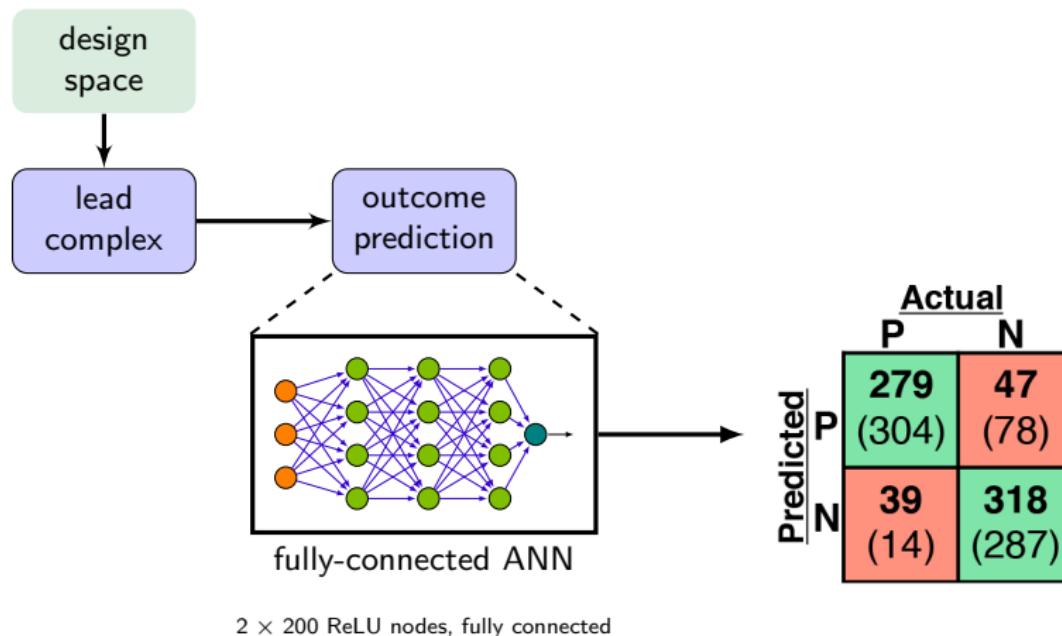
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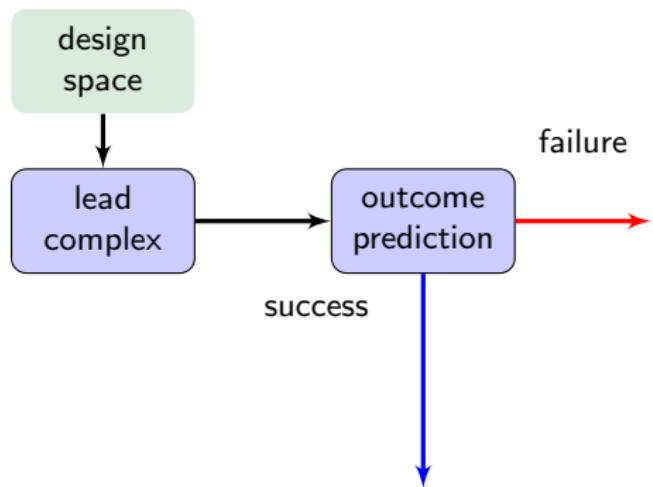
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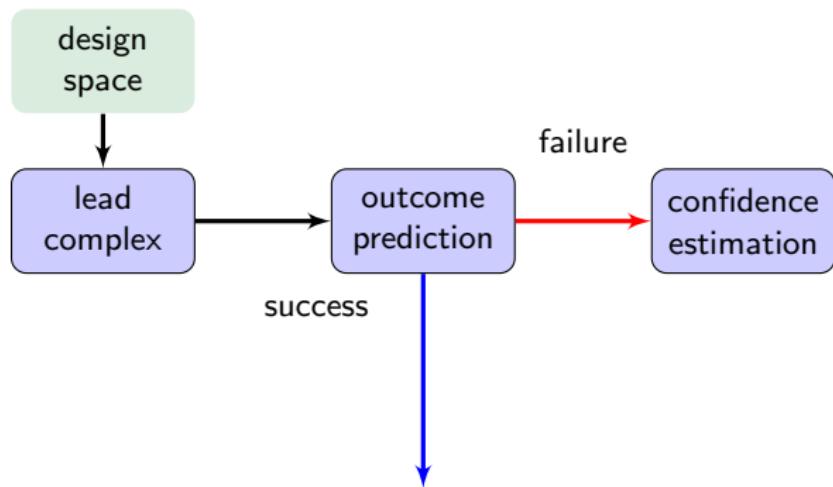
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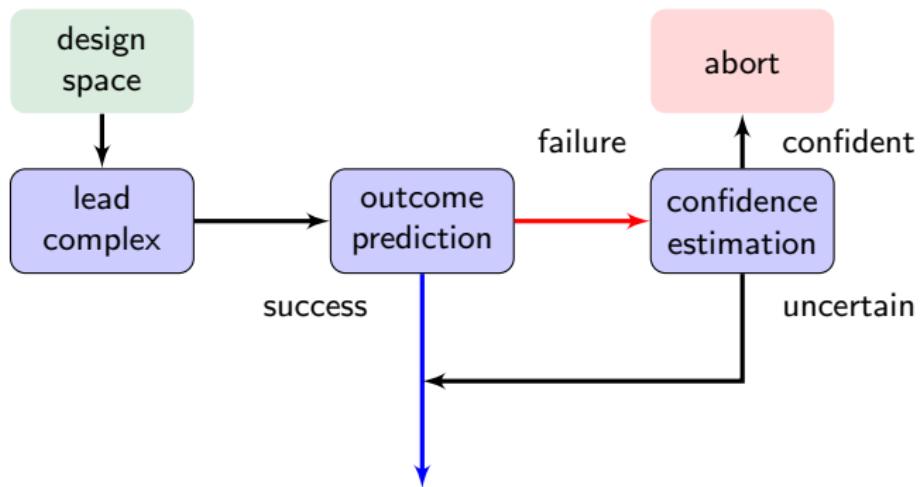
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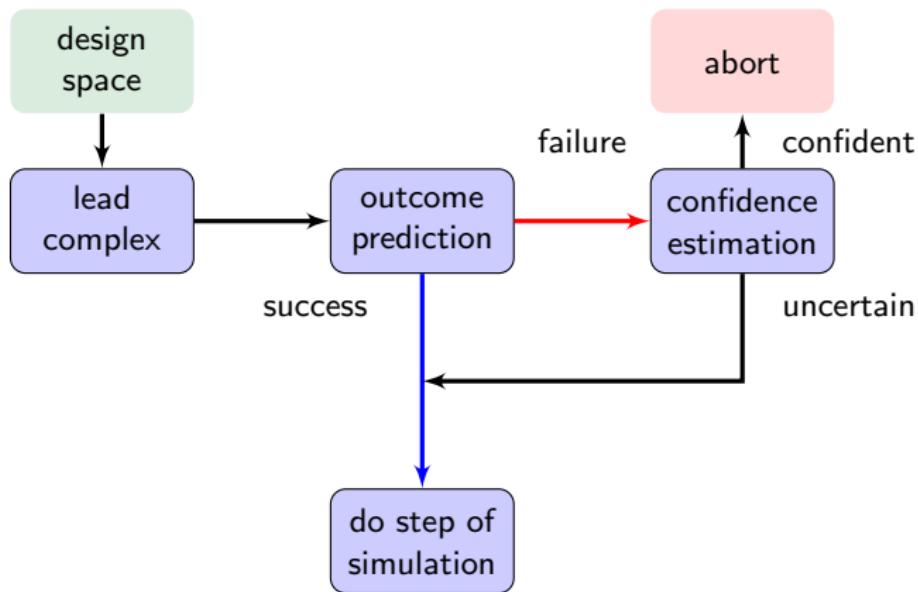
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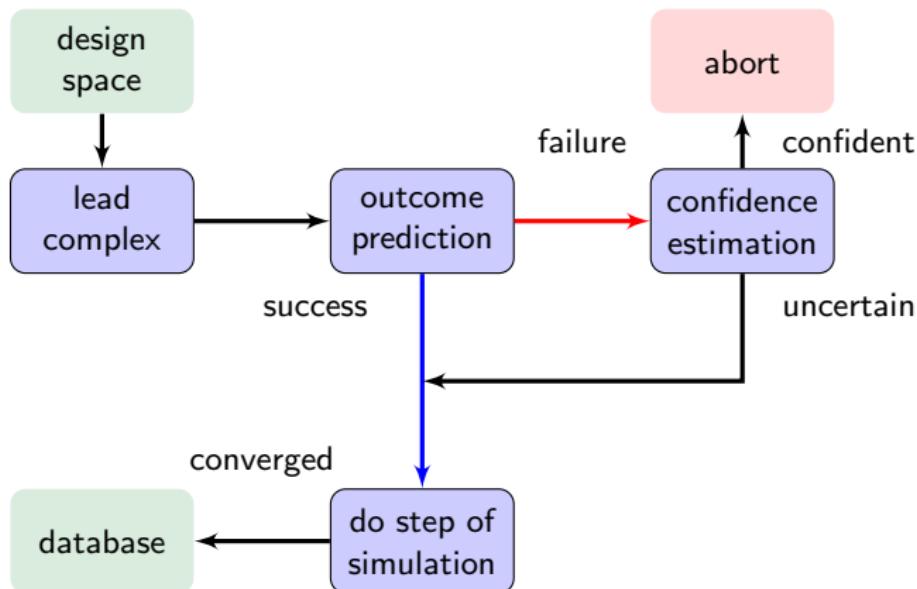
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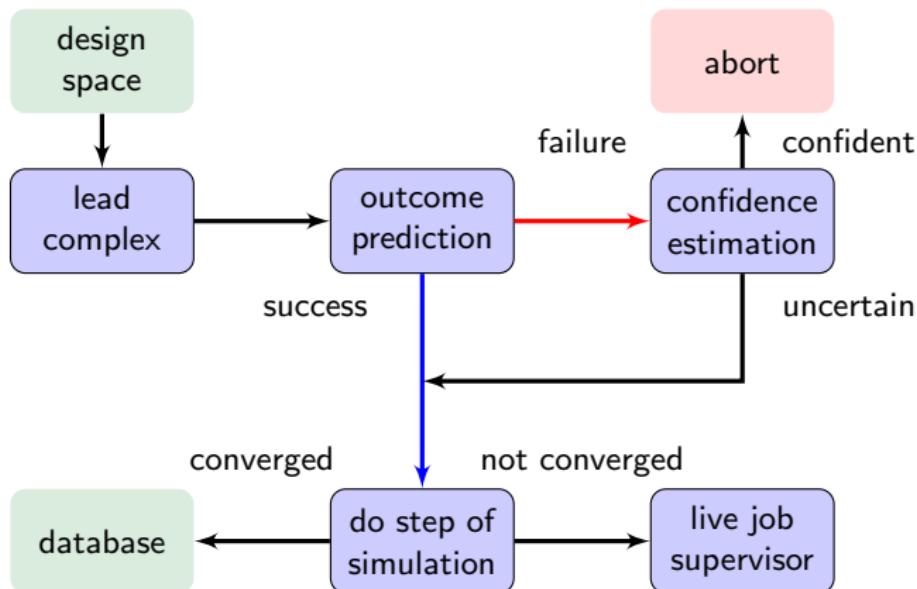
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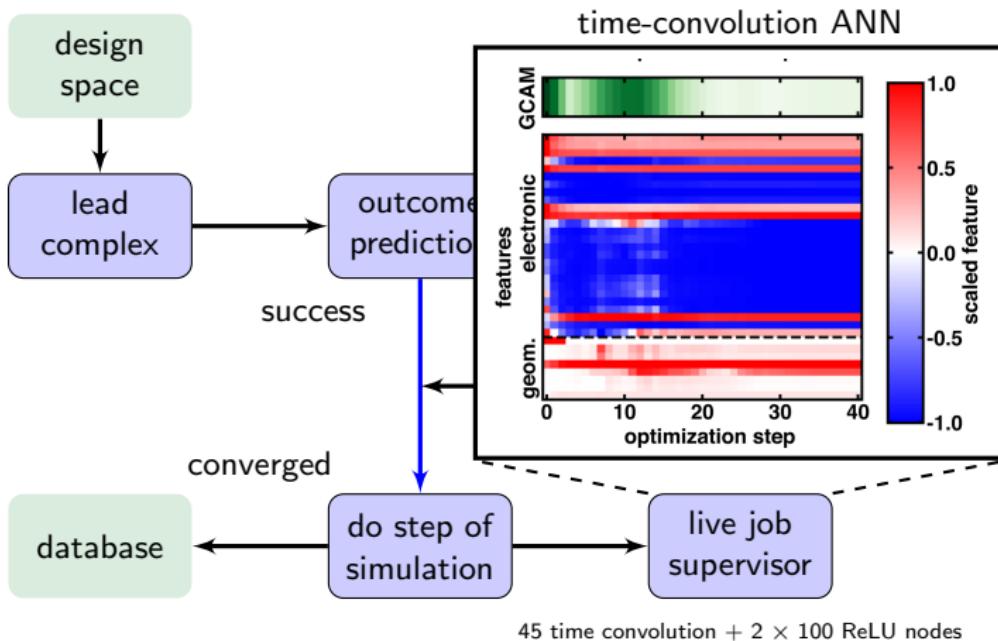
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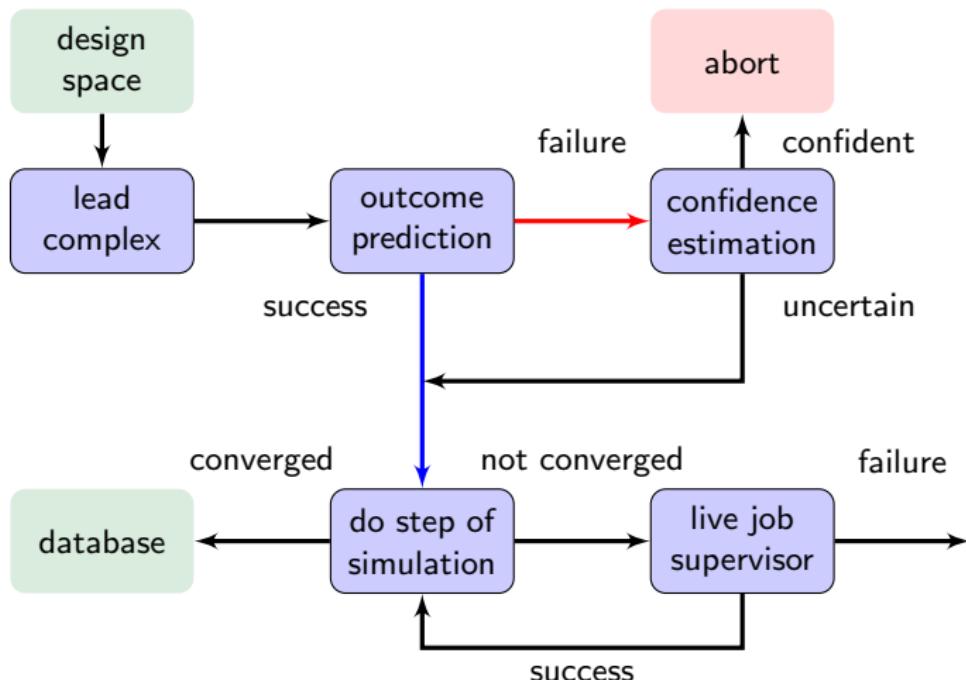
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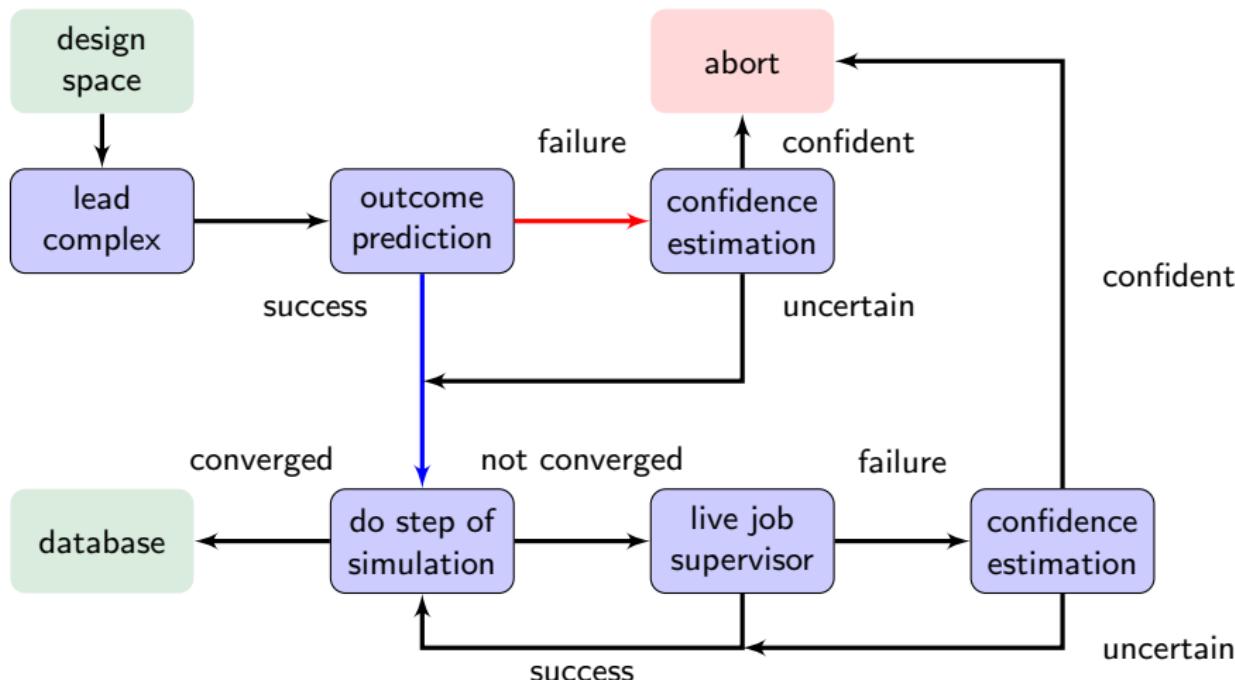
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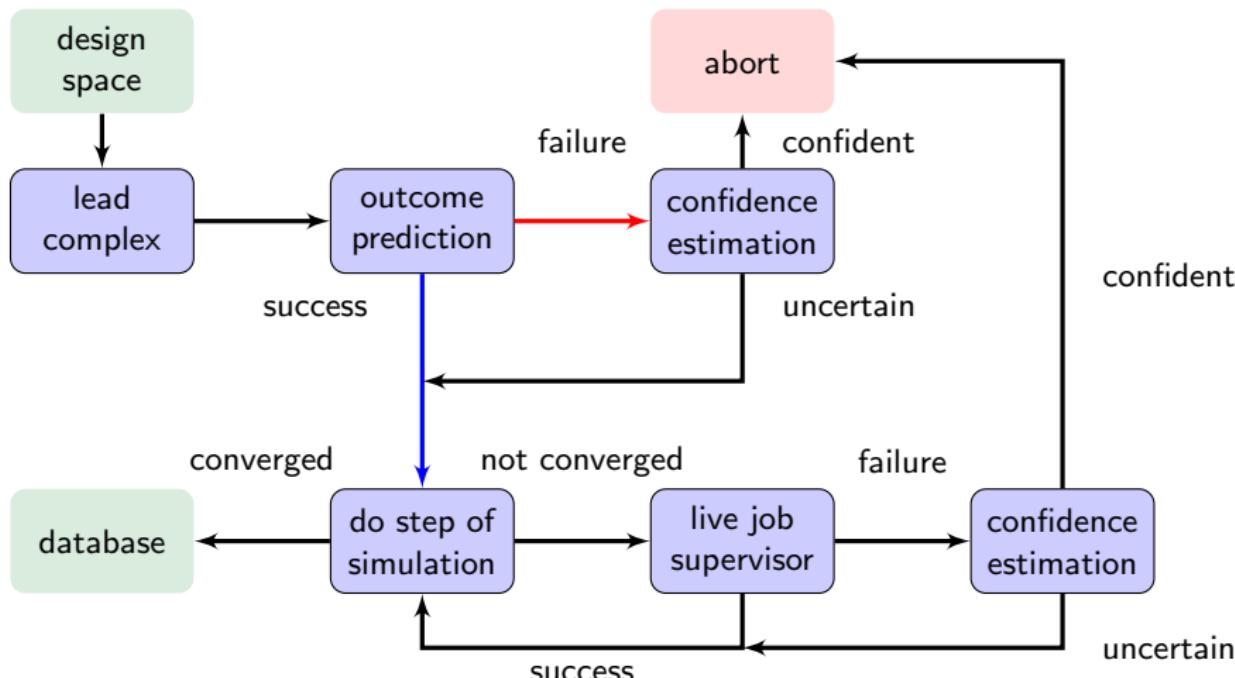
Beyond prediction: live job management



Beyond prediction: live job management



Beyond prediction: live job management



This leads to about **40% time savings** and can abort almost all failures.

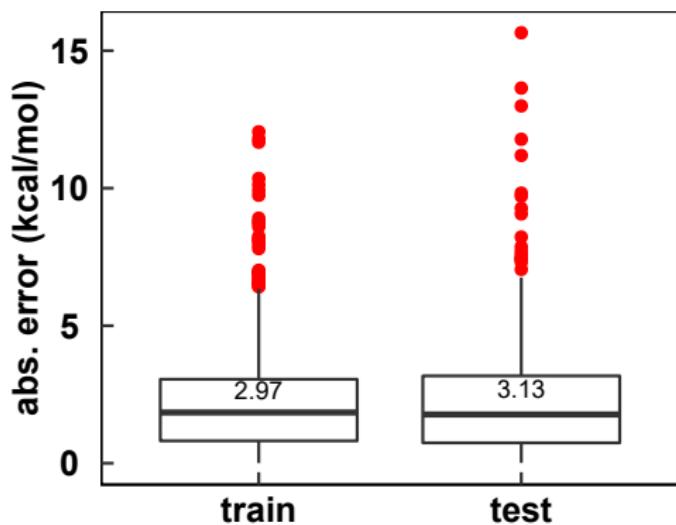
Duan, C., Janet, J.P. et al., *J. Chem. Theory Comp.*, 15(4):2331–2345, 2019.

Model transferability

Test-set performance is not necessarily a good metric for general transferability:

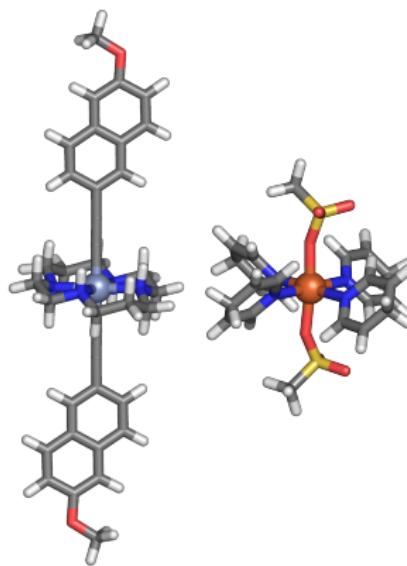
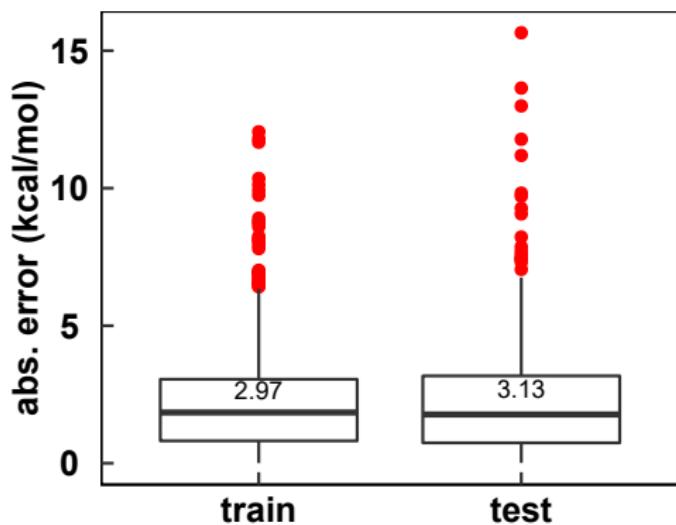
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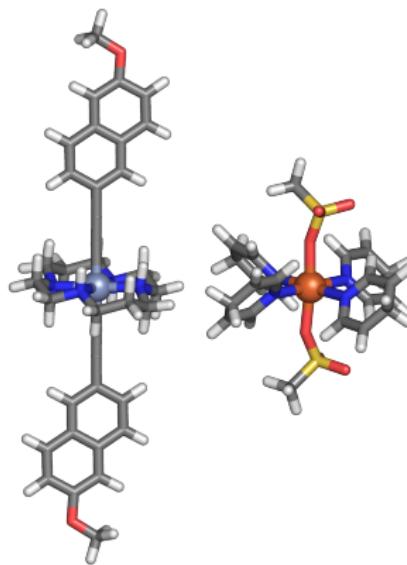
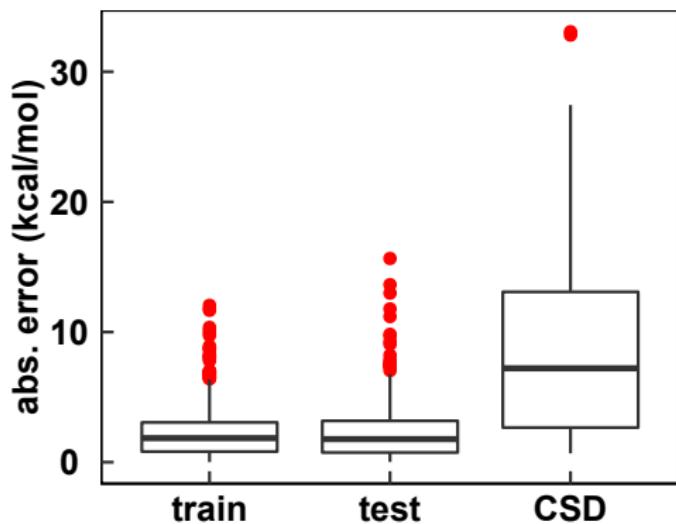
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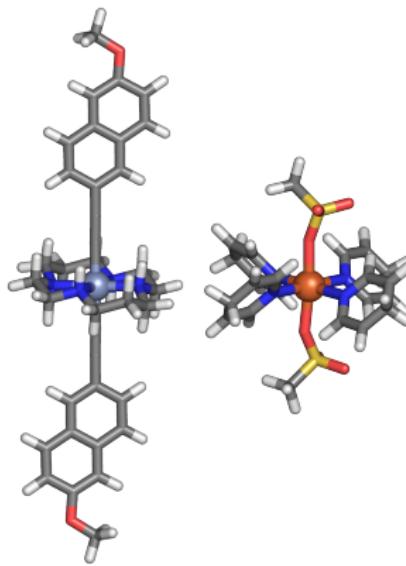
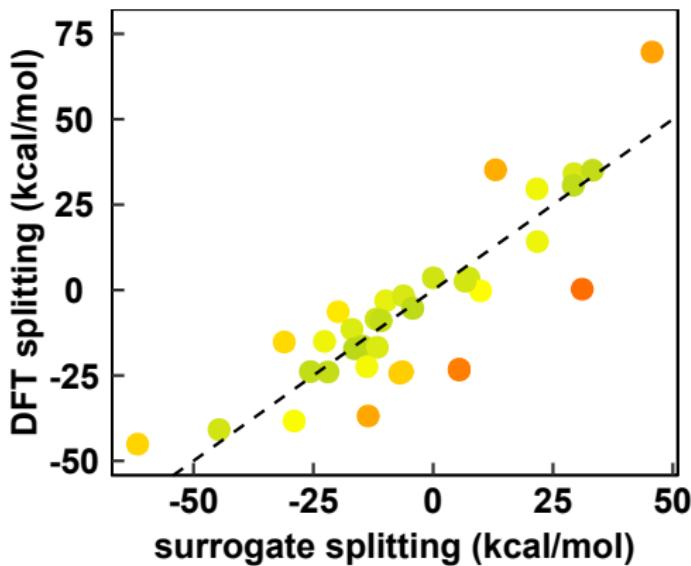
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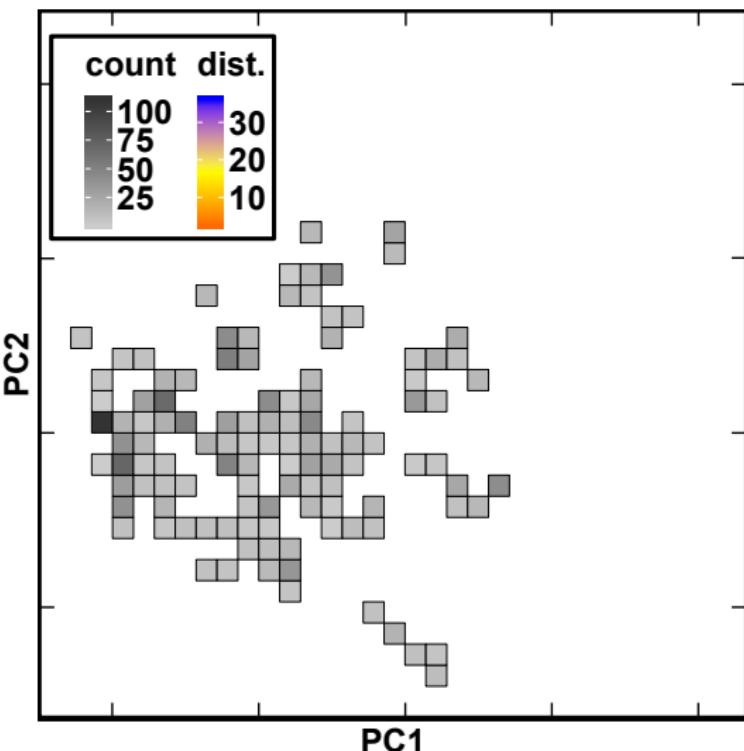


How far can we extrapolate?

'Out-of-distribution' test:
spin-splitting energies of
116 structures from the
CSD, from training-like to
very different.

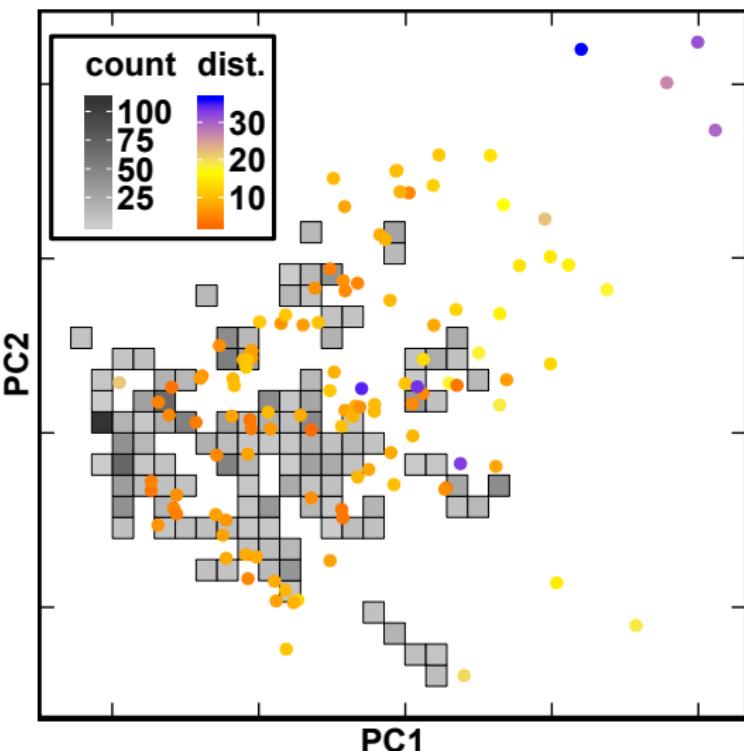
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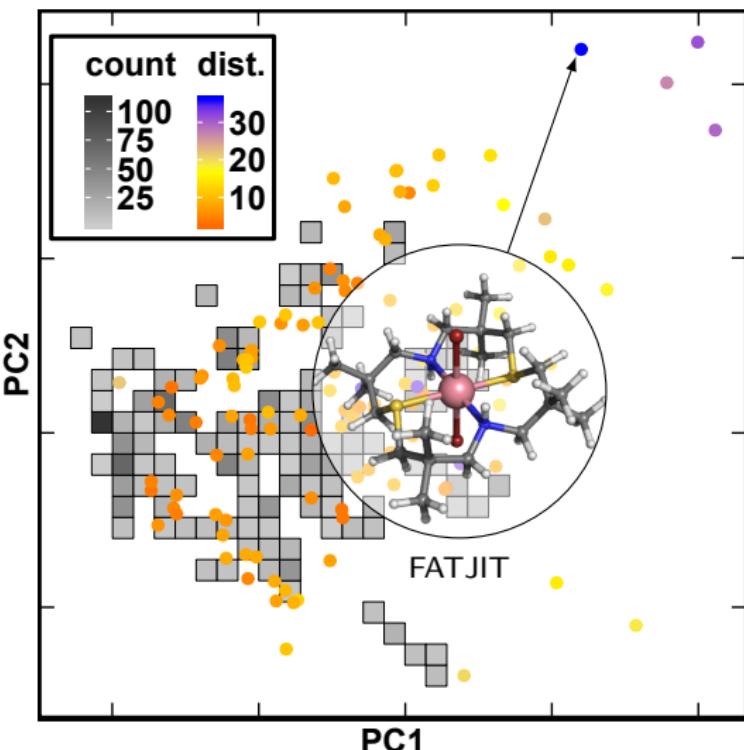
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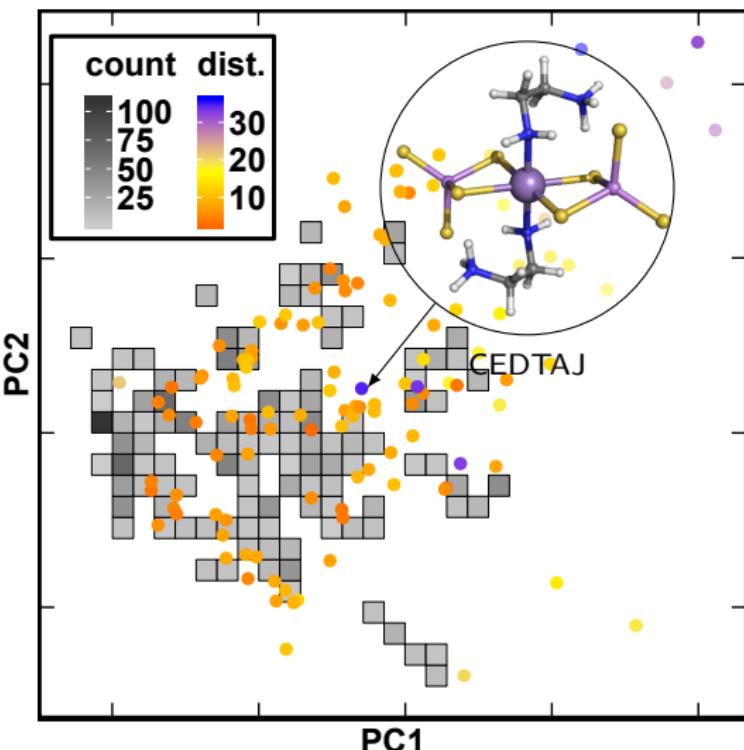
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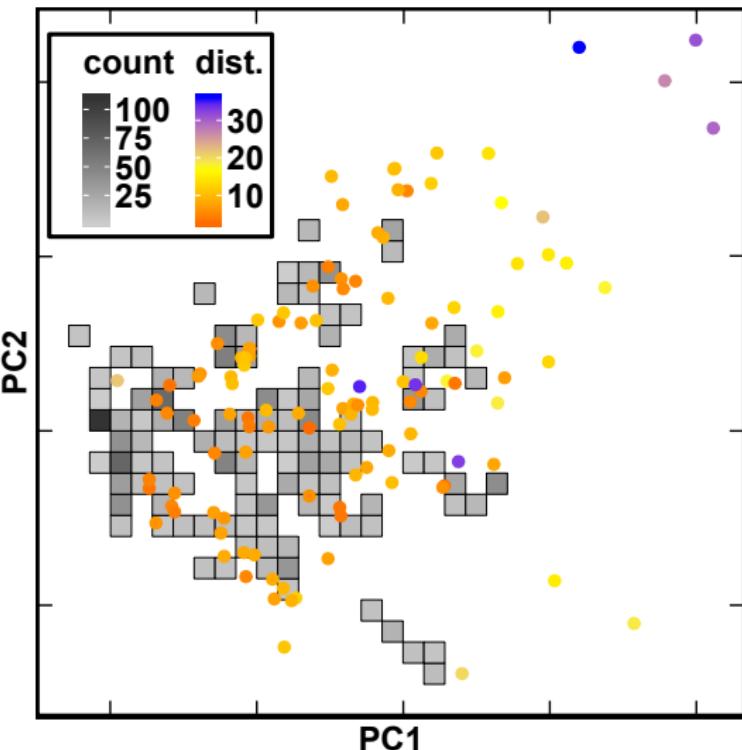
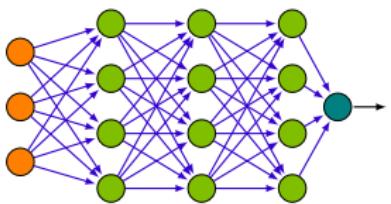
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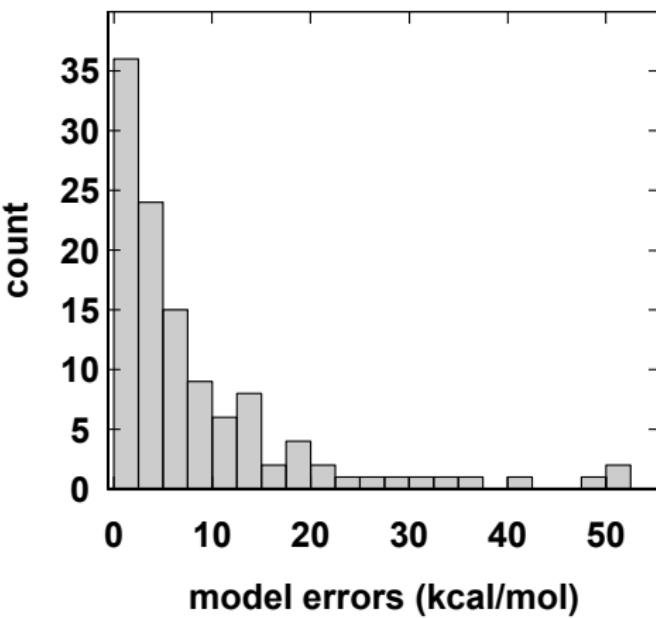
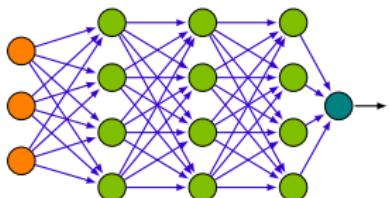
Train 3-layer fully connected ANN on 1900 DFT
results on simple ligands:



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Introduction
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Features and models
ooo

Uncertainty
oo●ooooo

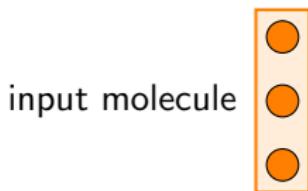
Discovery
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Case Study
oooooooo

Conclusions
ooo

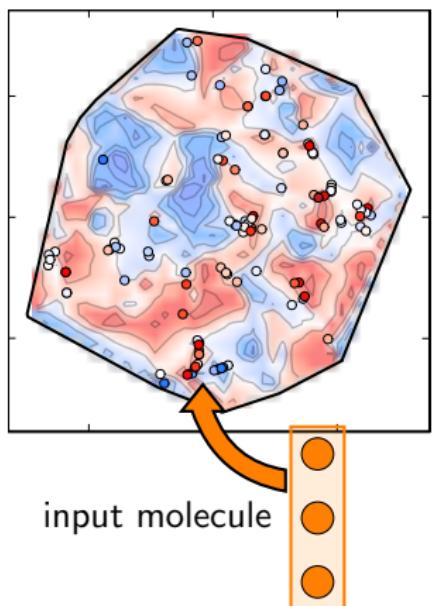
Latent distance similarity

Latent distance similarity



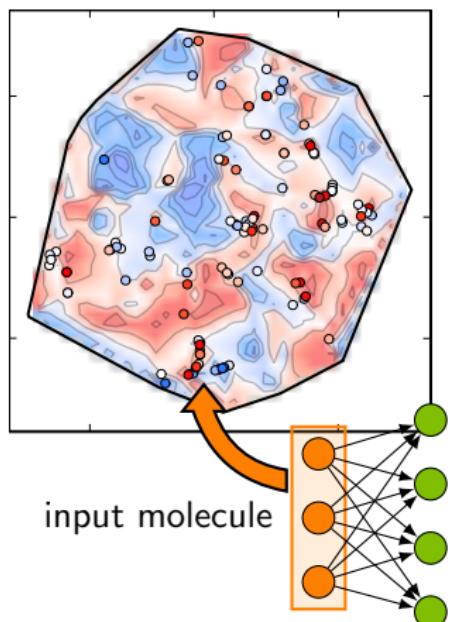
Latent distance similarity

feature space



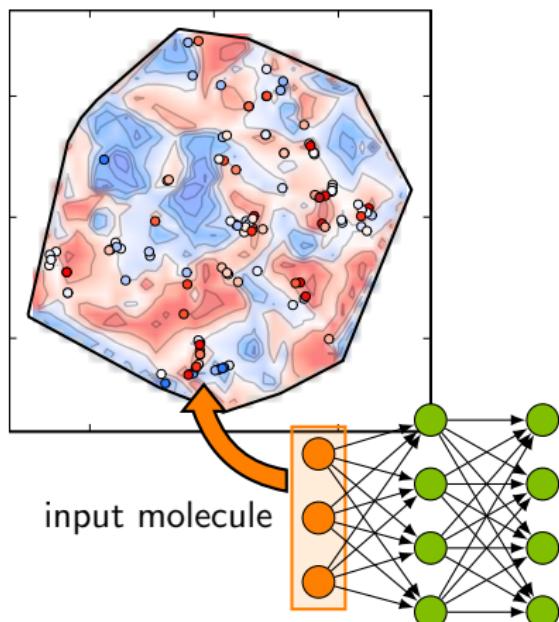
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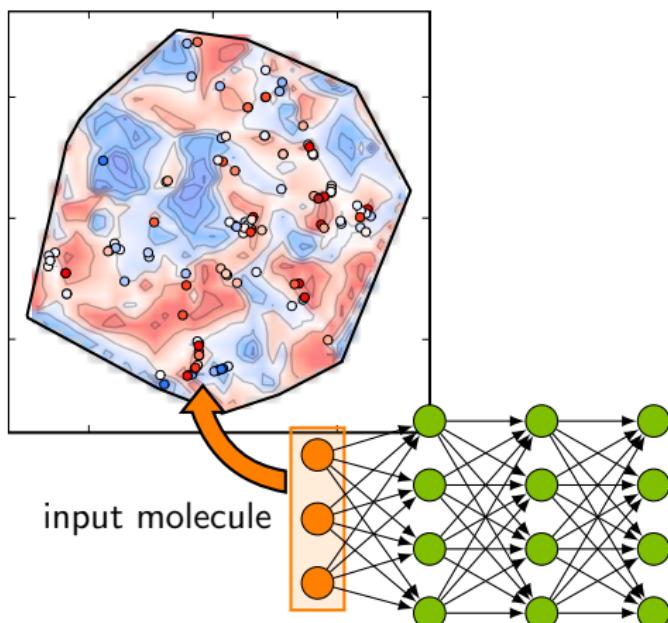
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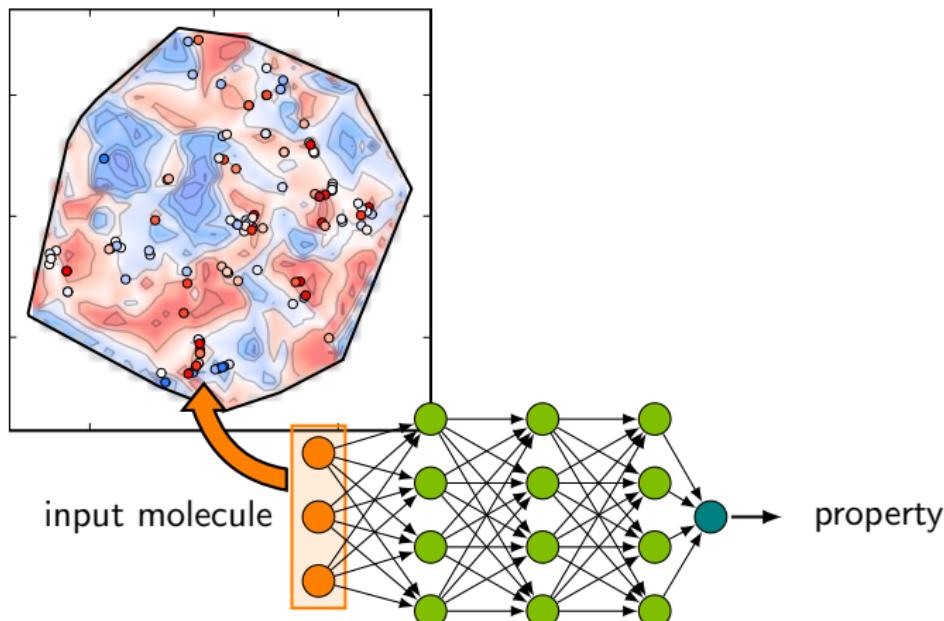
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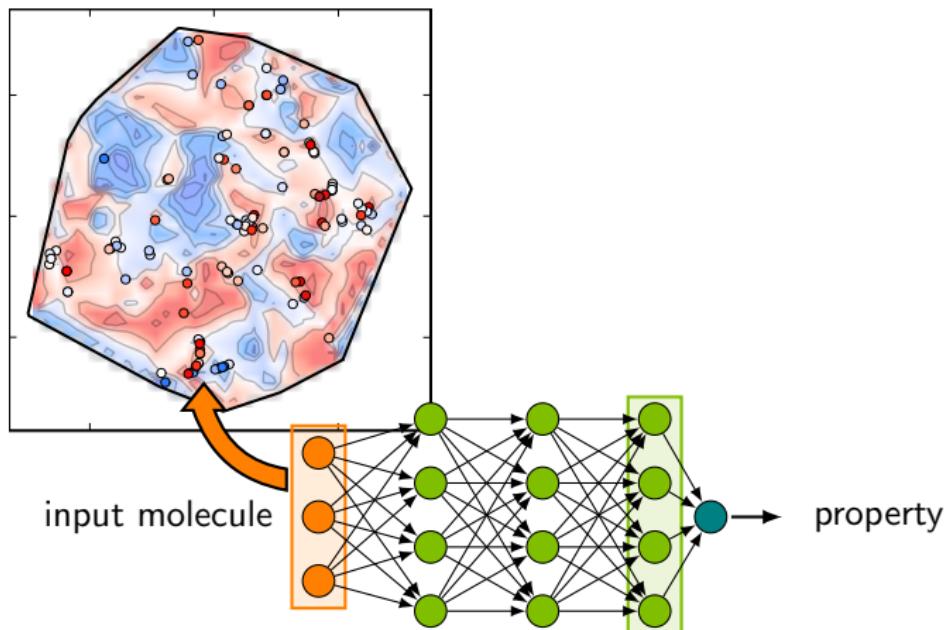
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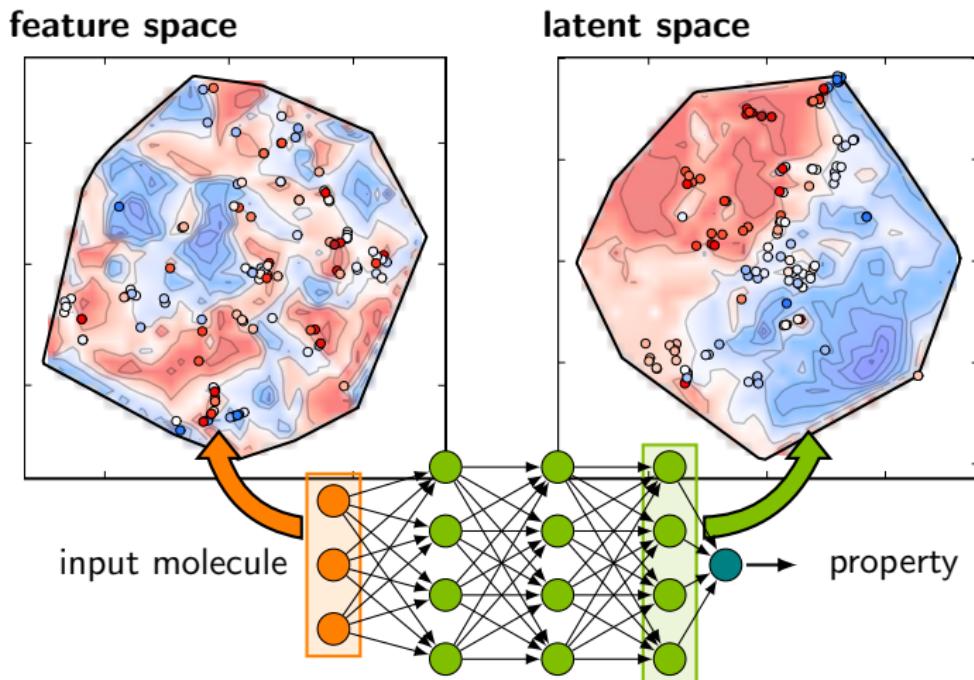


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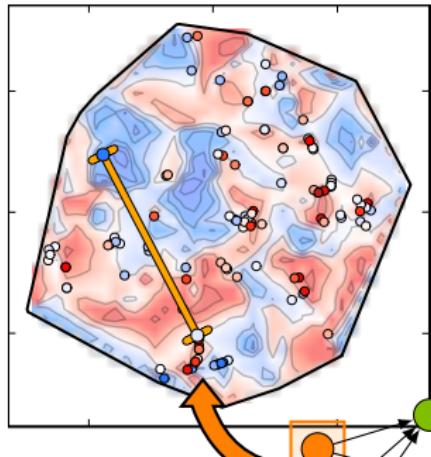


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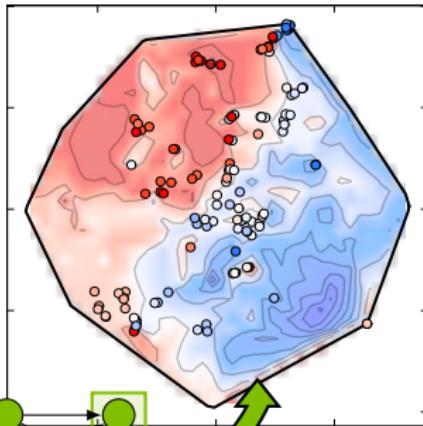


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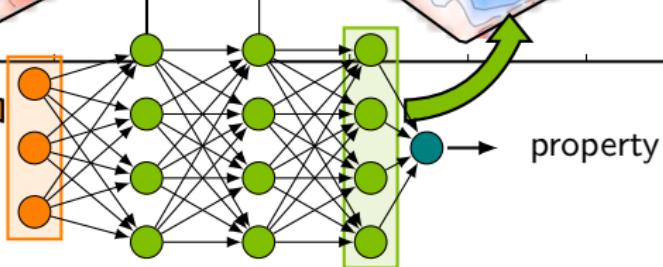
feature space geometry



latent space

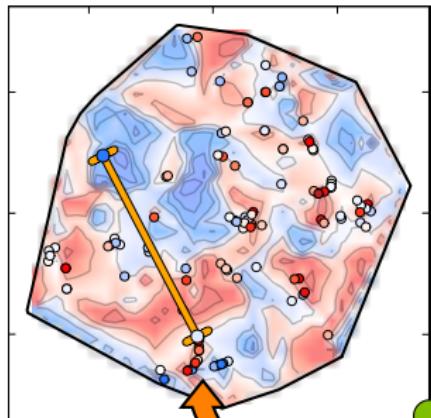


input molecule



Latent distance similarity

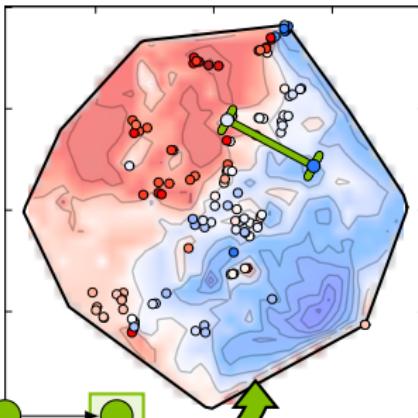
feature space geometry



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latent space geometry



property



From distance to energy

Propose a simple conditionally-Gaussian model for predicting error distribution with latent distance, d :

$$\varepsilon(d) \sim \mathcal{N}(0, \sigma_1^2 + d\sigma_2^2)$$

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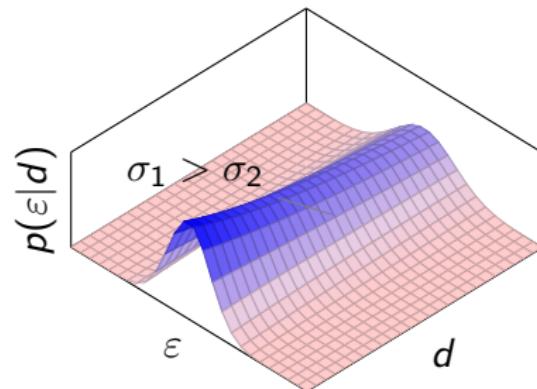
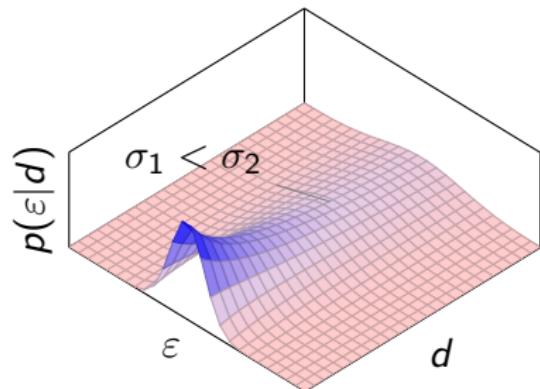
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Other UQ metrics

1) Data-sampling ensembles:

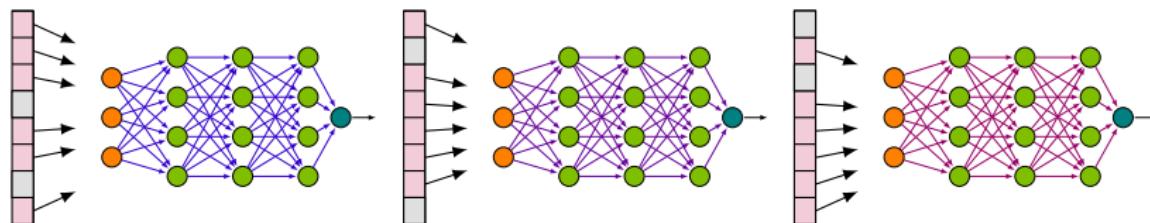
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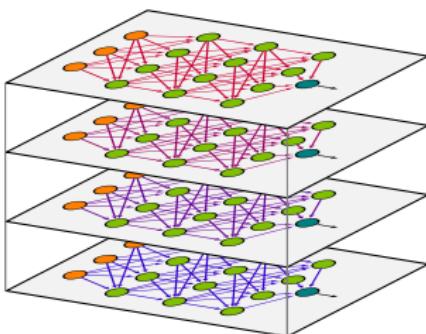
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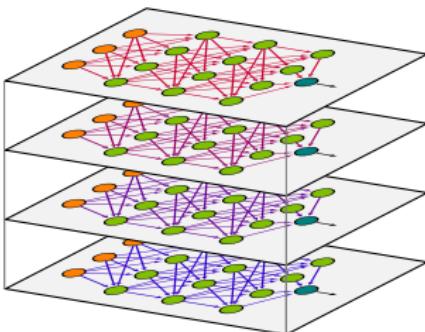
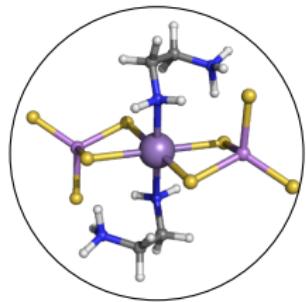
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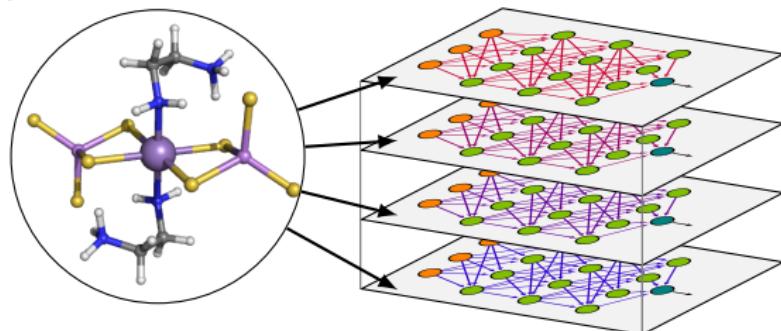
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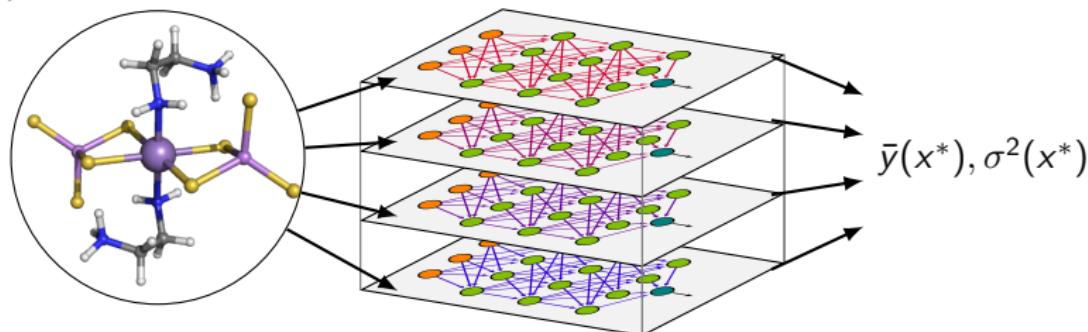
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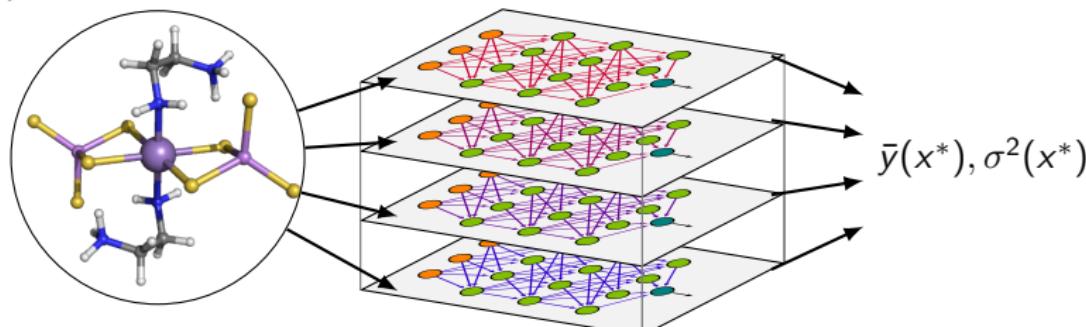
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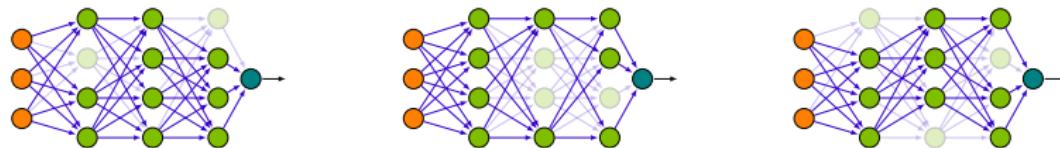


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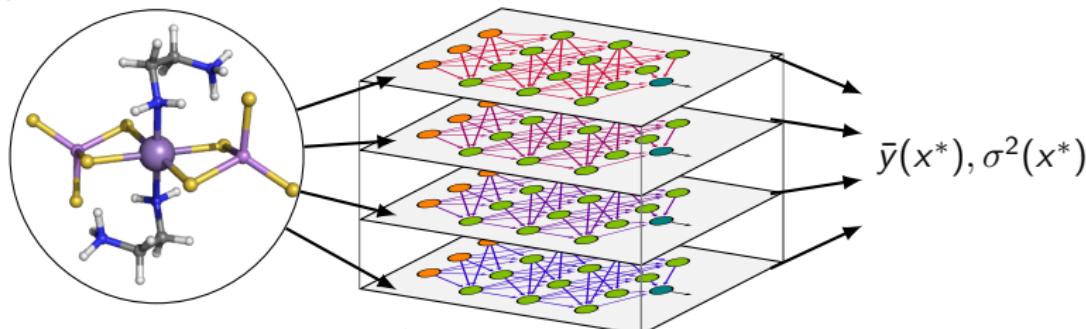
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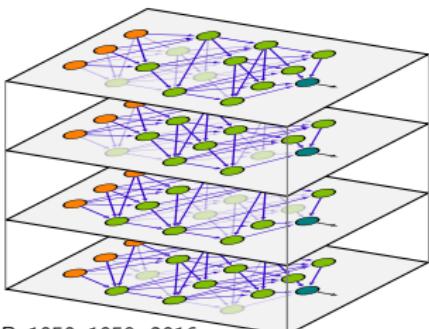
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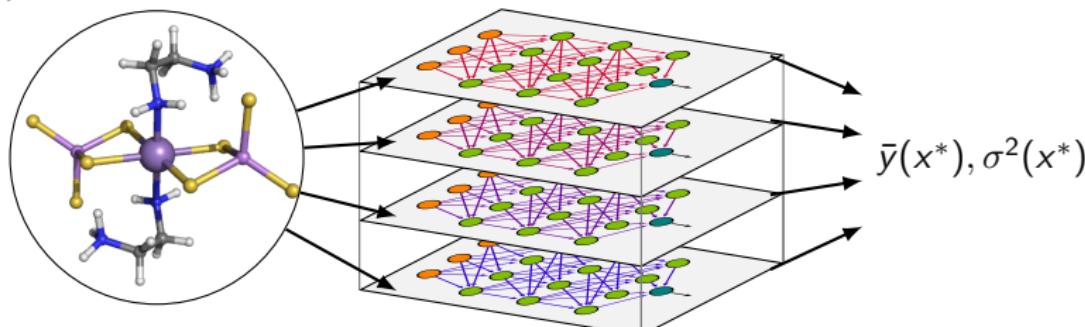
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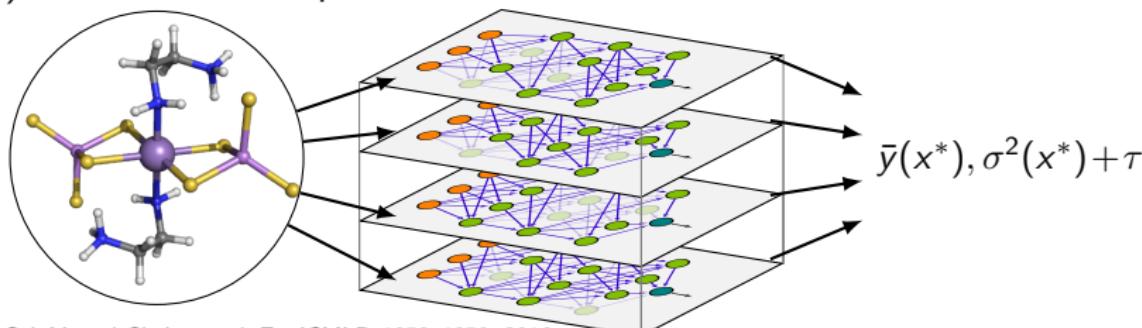
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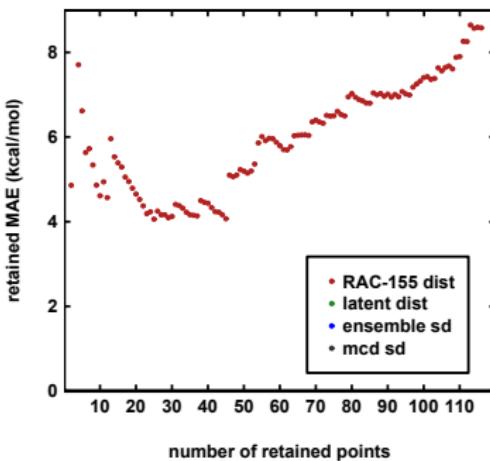
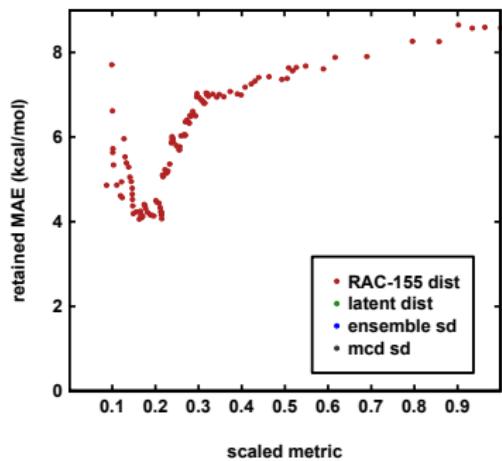


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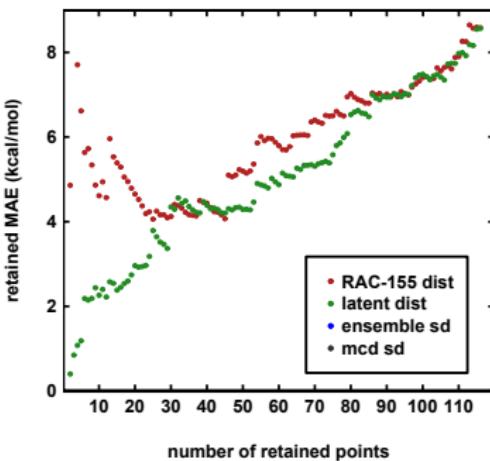
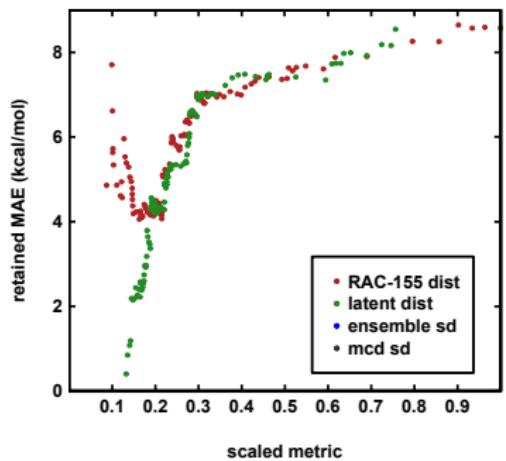
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How do these distributions compare?



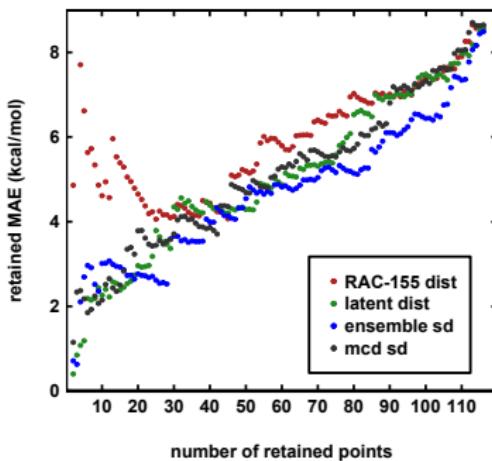
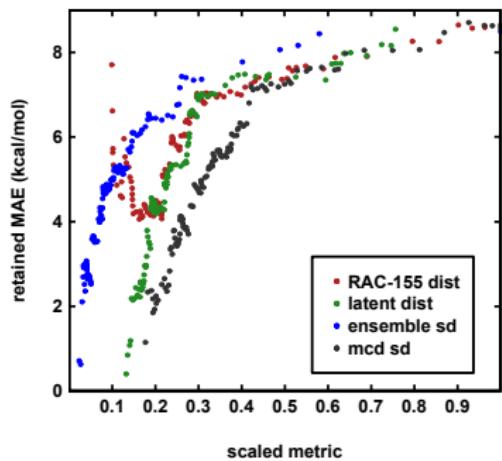
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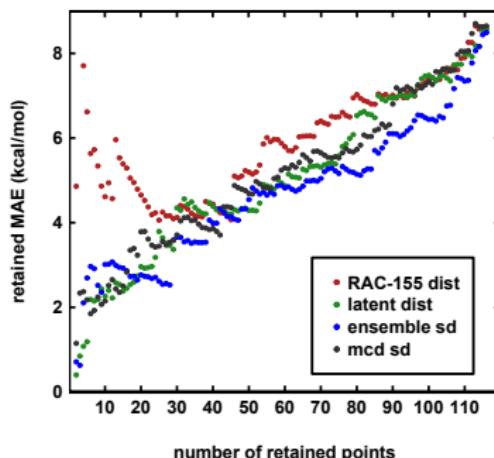
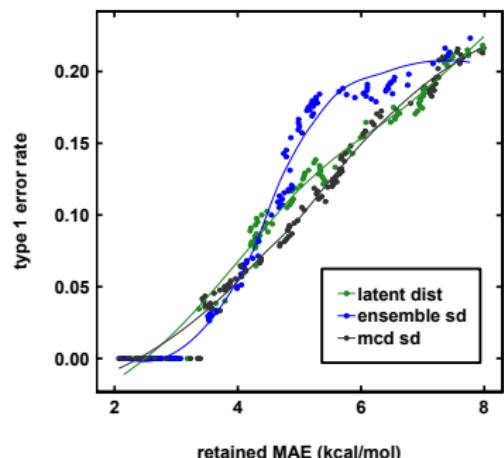
comparable with ensembles and mc dropout

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latent distances are superior to feature space distances



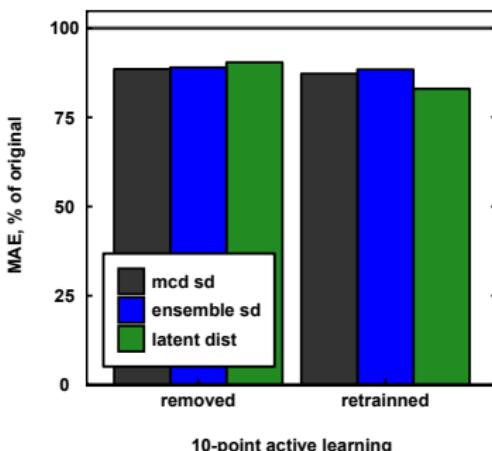
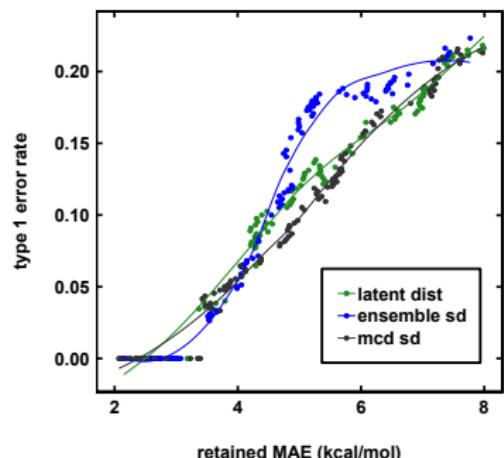
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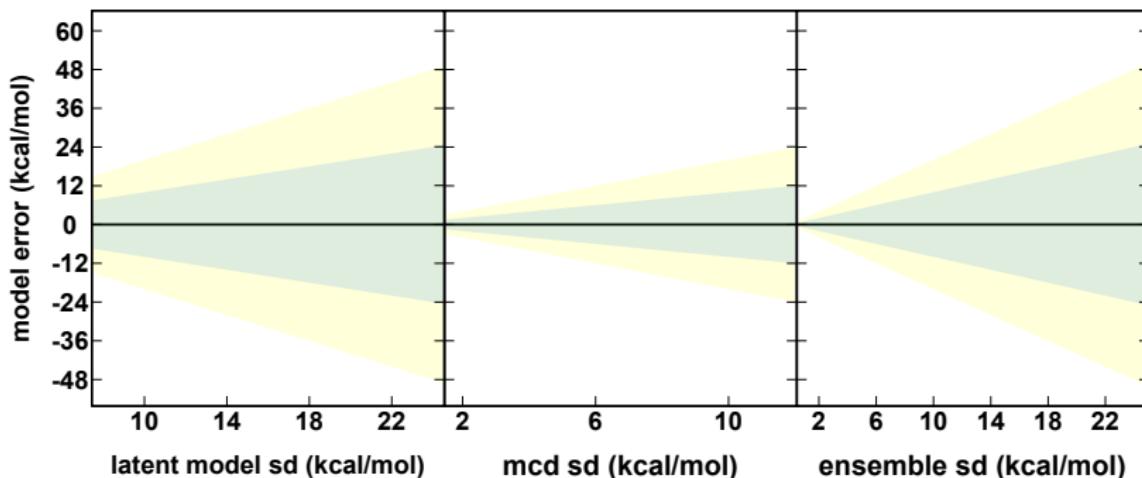


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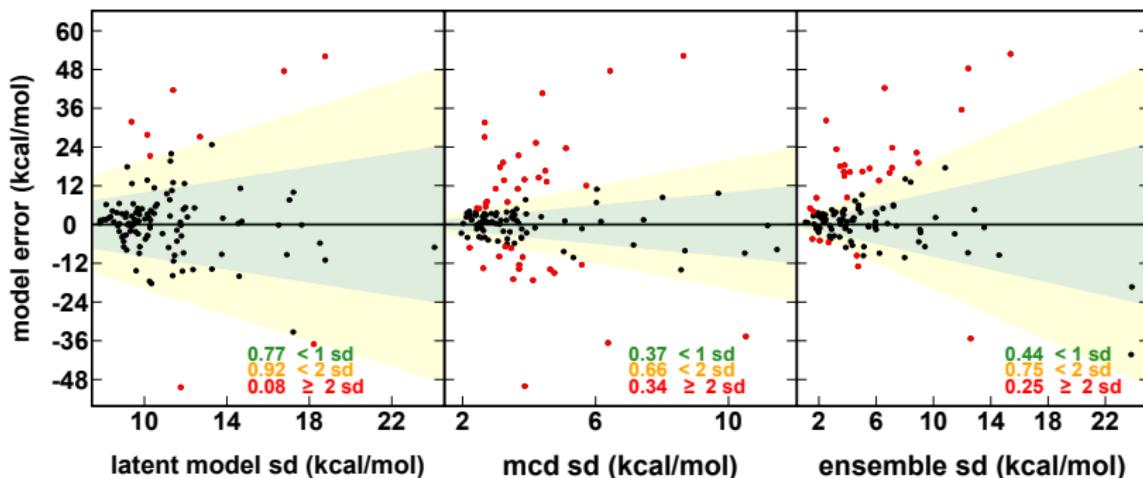
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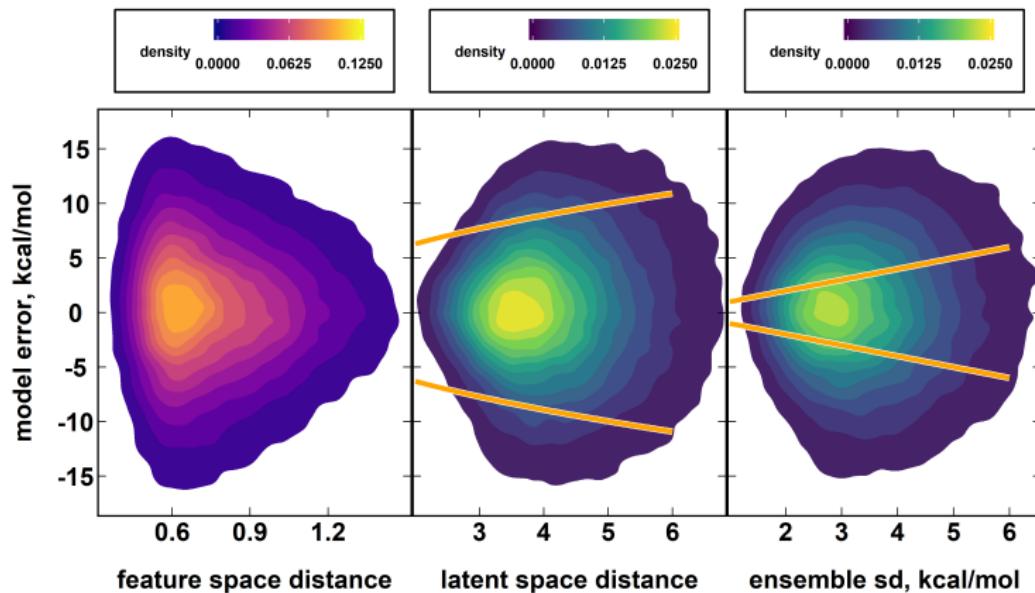
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How do these distributions compare?

Comparison in energy units: QM9 atomization energy data

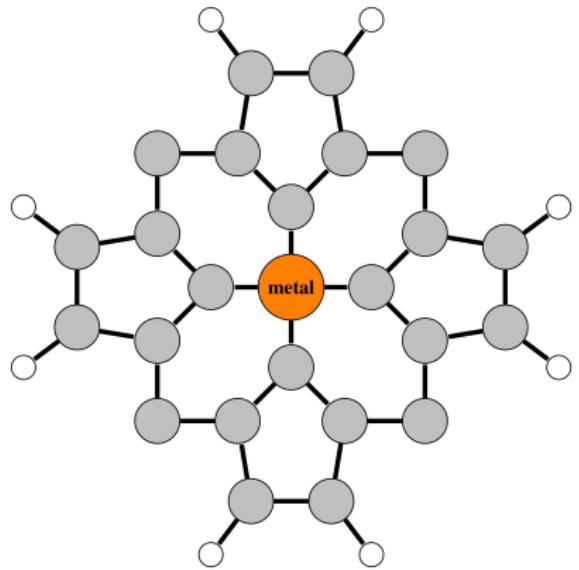


Targeted data acquisition

Lack of data is a persistent issue. We can exploit knowledge of feature importance to generate data:

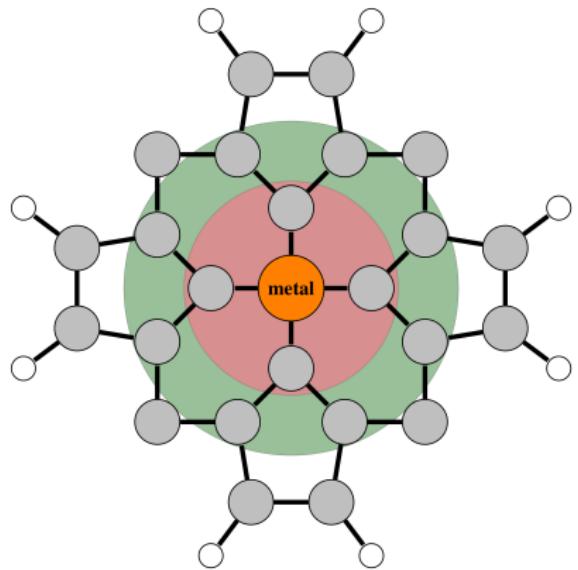
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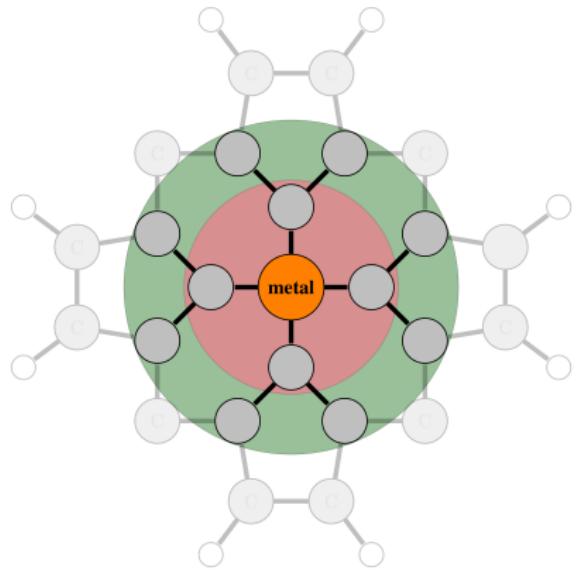
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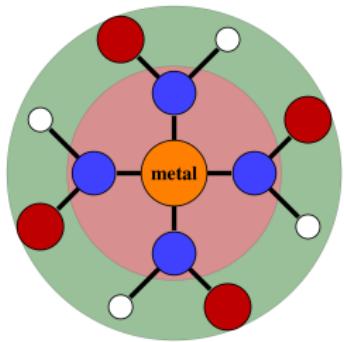
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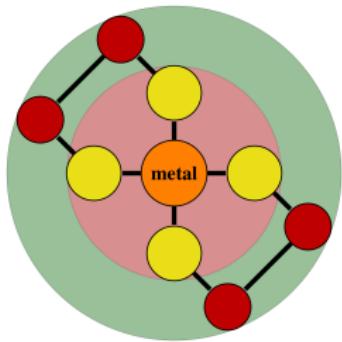
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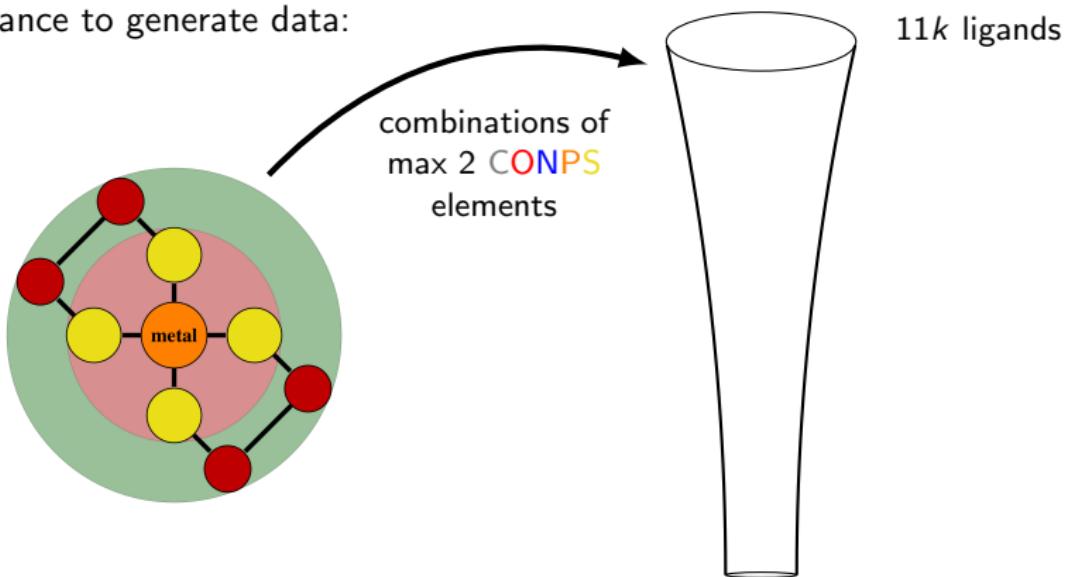
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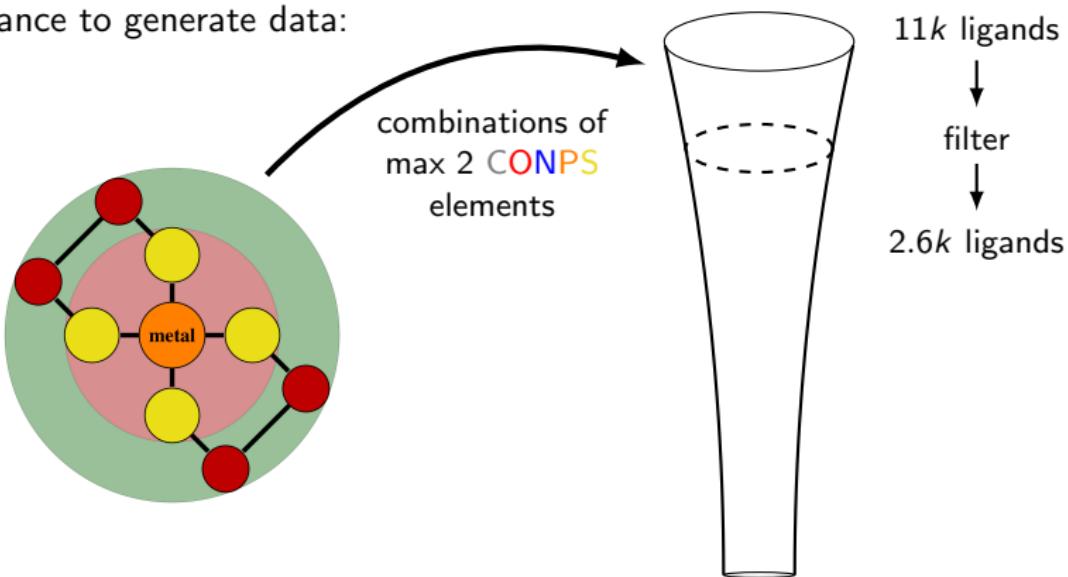
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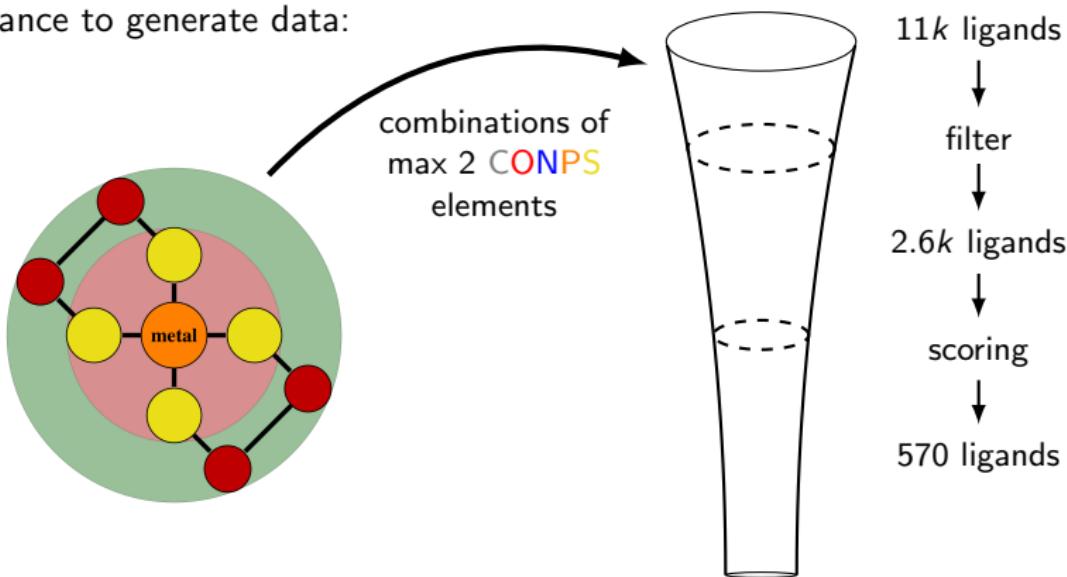
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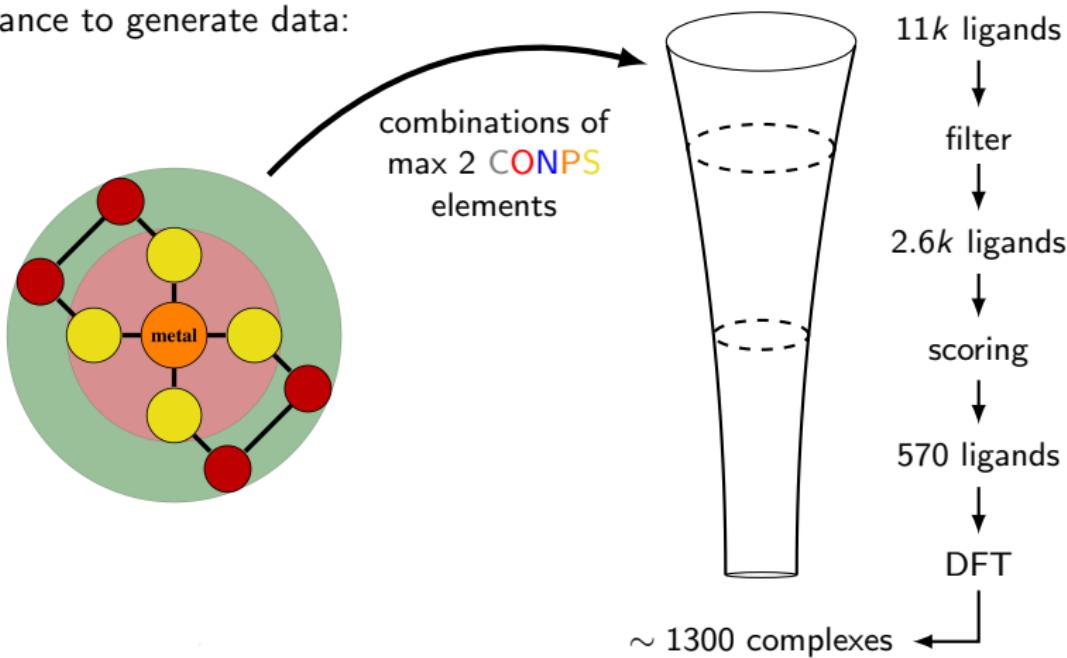
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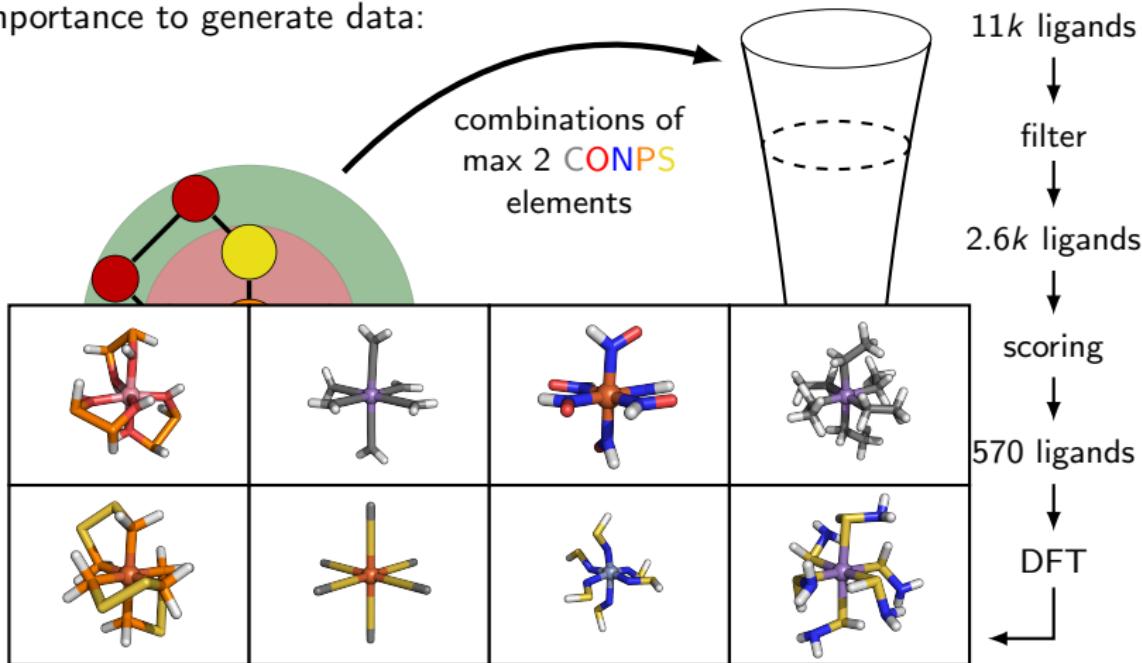
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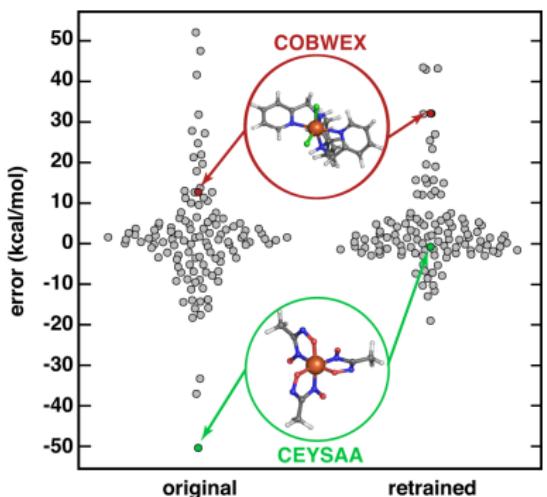
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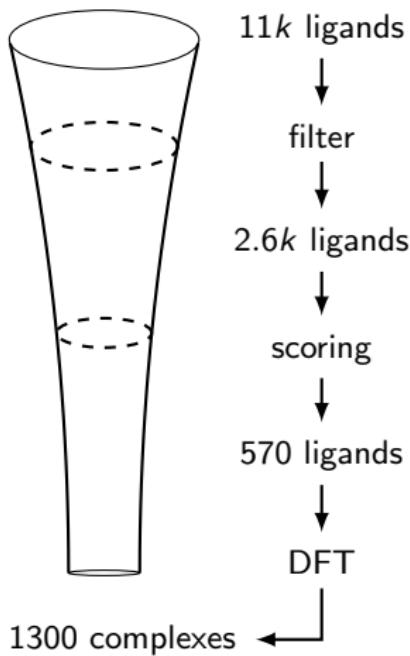
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add to surrogate model

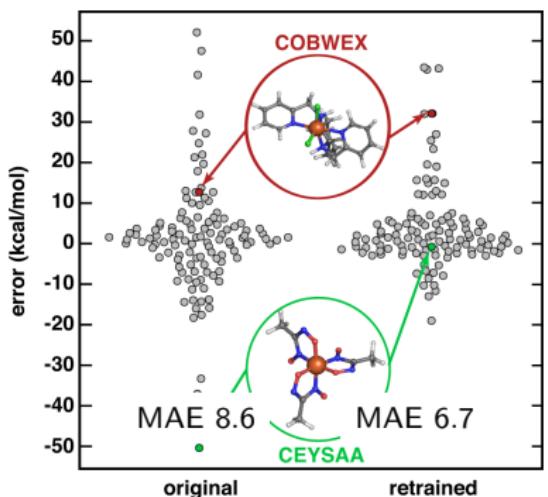
3 × 100 tanh nodes, fully connected ANN

Gugler, S., Janet, J.P., and Kulik, H.J., *Mol. Sys. Des. Eng.*, Advance Article, 2019.



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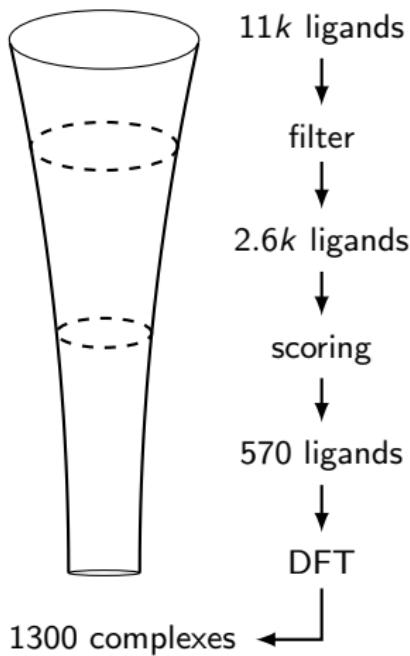
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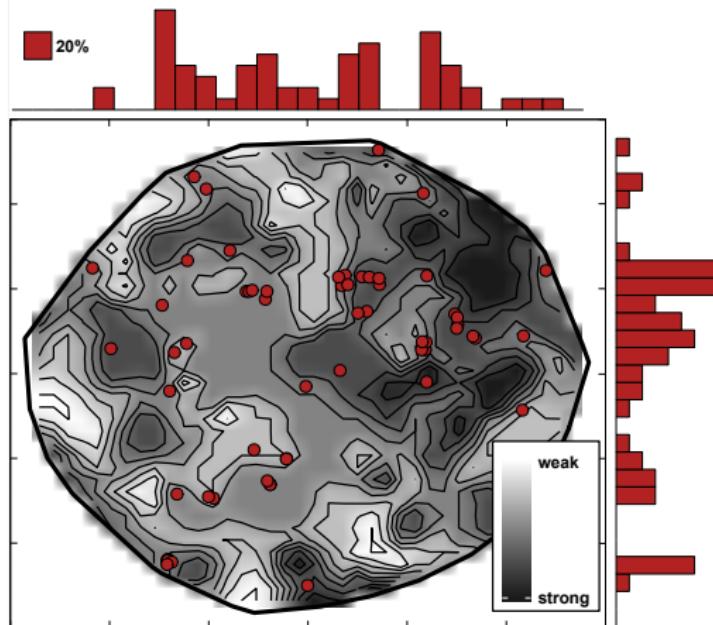


Hedging against DFT uncertainty

Because we have trained our models with varying exact exchange, we can tune functionals for design:

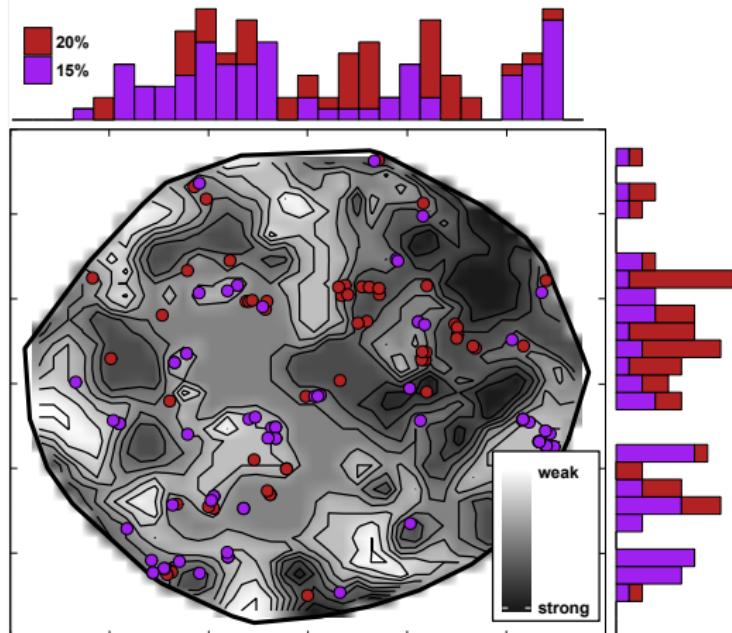
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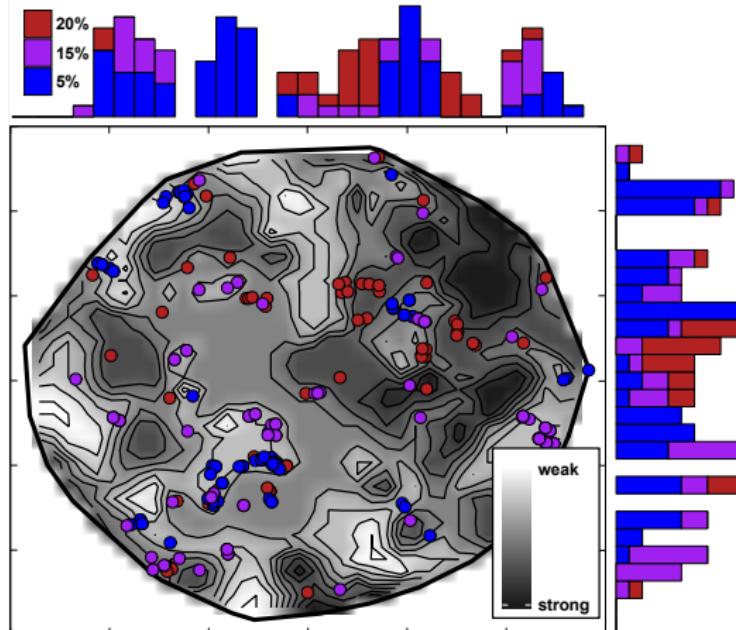
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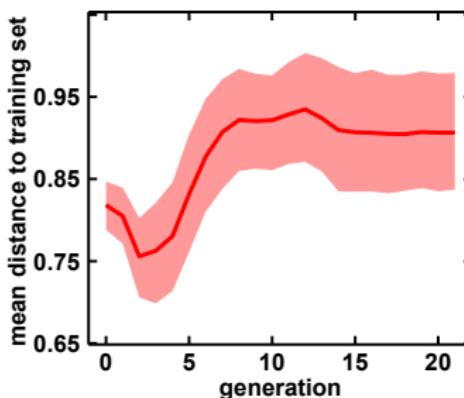
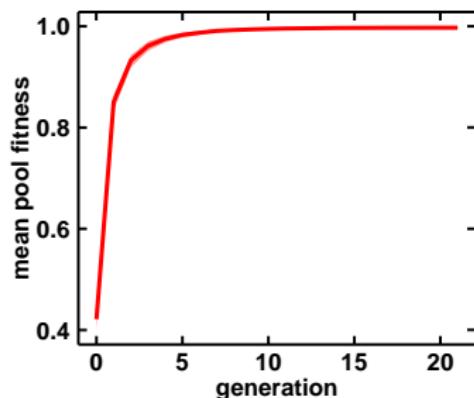
Using models for discovery

We utilize evolutionary algorithms to conduct design, guided by uncertainty metrics

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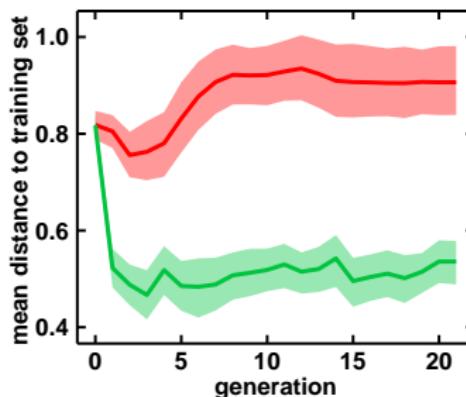
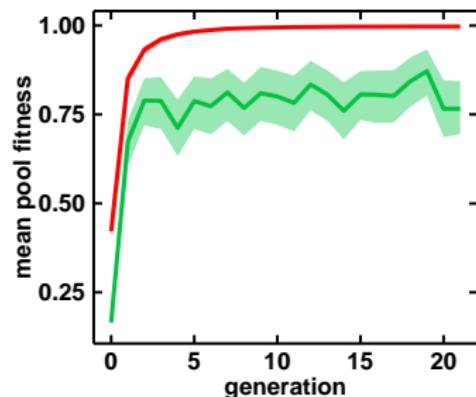
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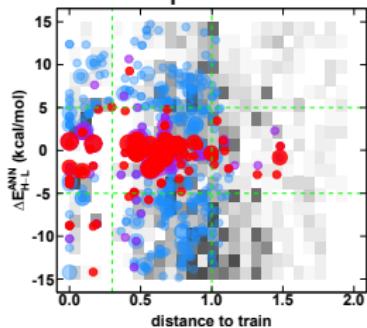
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spin crossover
complexes



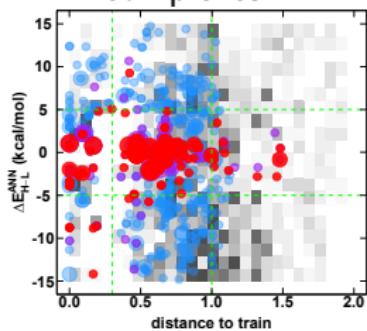
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Using models for discovery

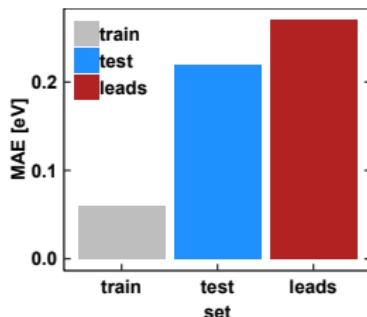
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frontier orbital
properties



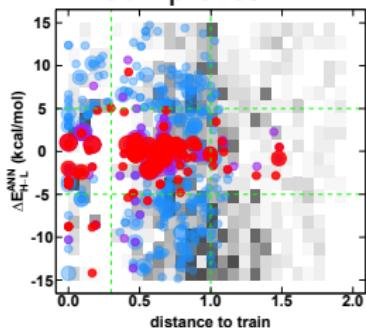
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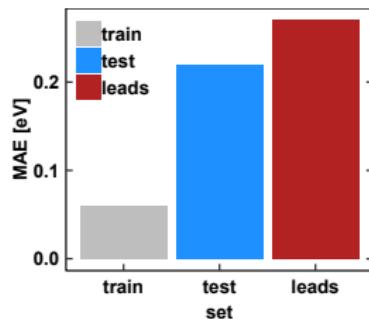
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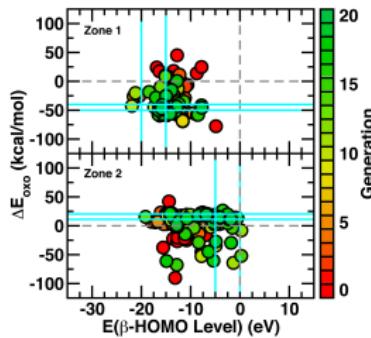
spin crossover
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unusual catalytic
reaction energies



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Introduction
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Features and models
ooo

Uncertainty
oooooooo

Discovery
○●

Case Study
ooooooooo

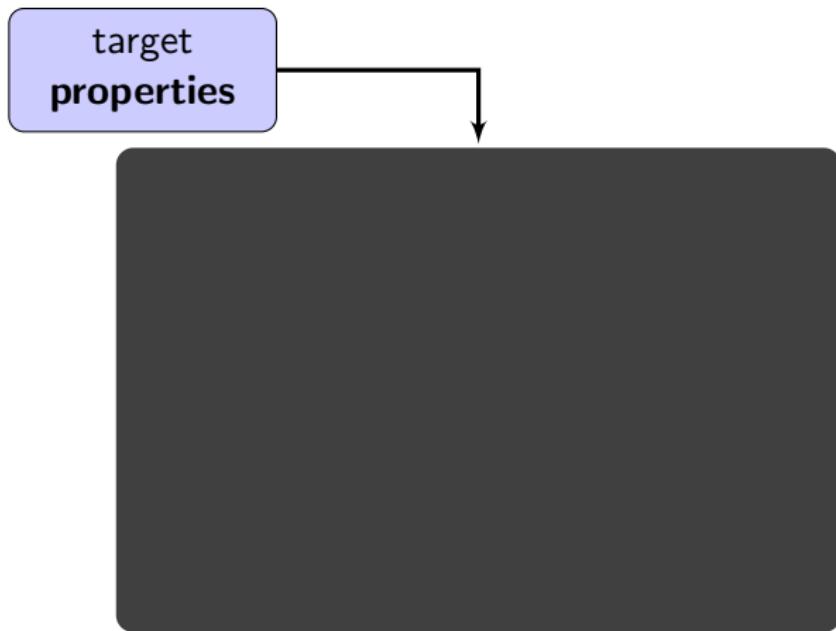
Conclusions
ooo

More than just ML

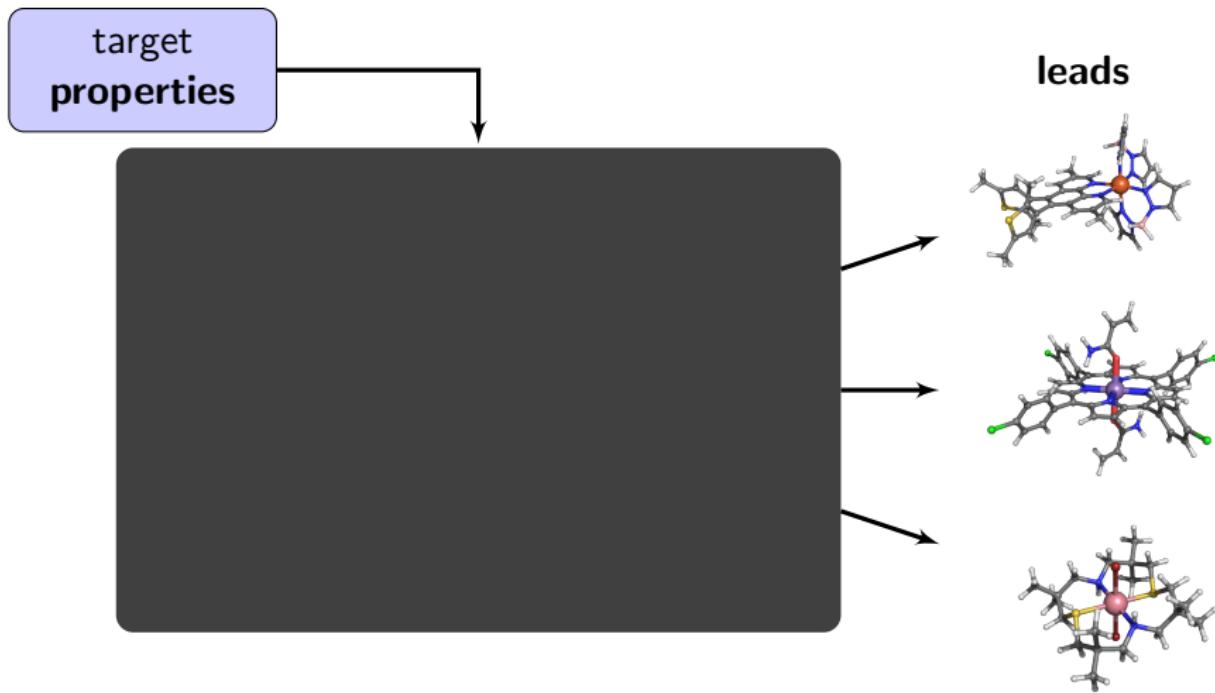
More than just ML

target
properties

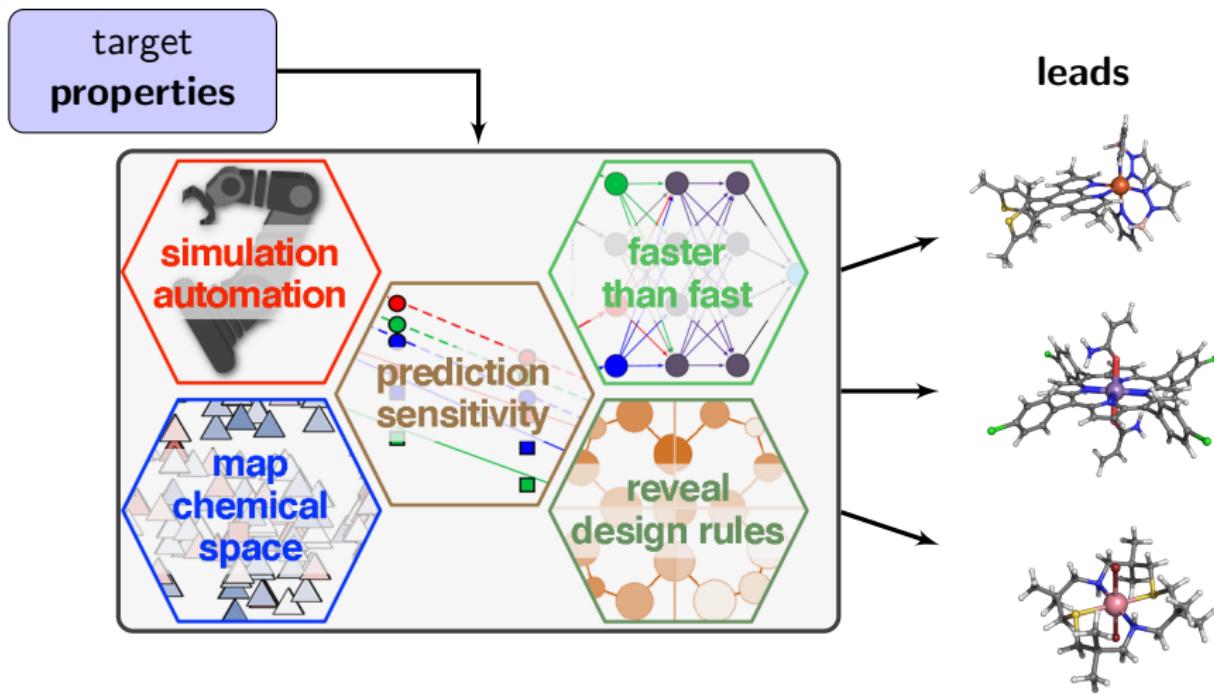
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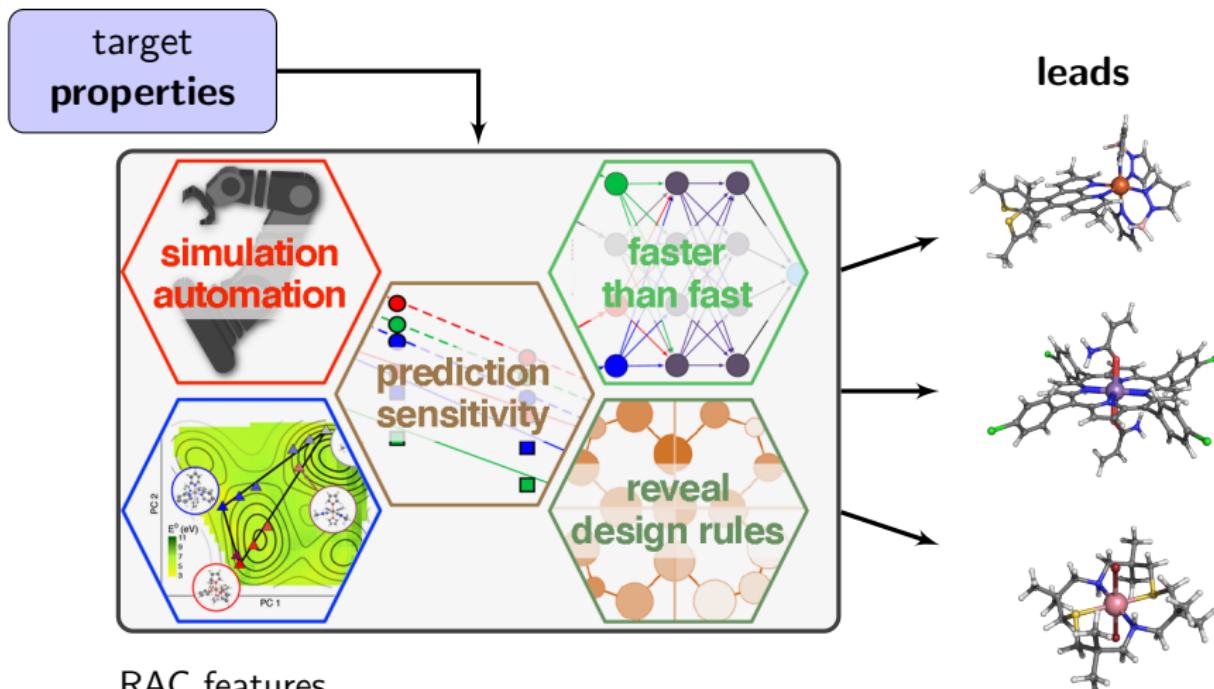
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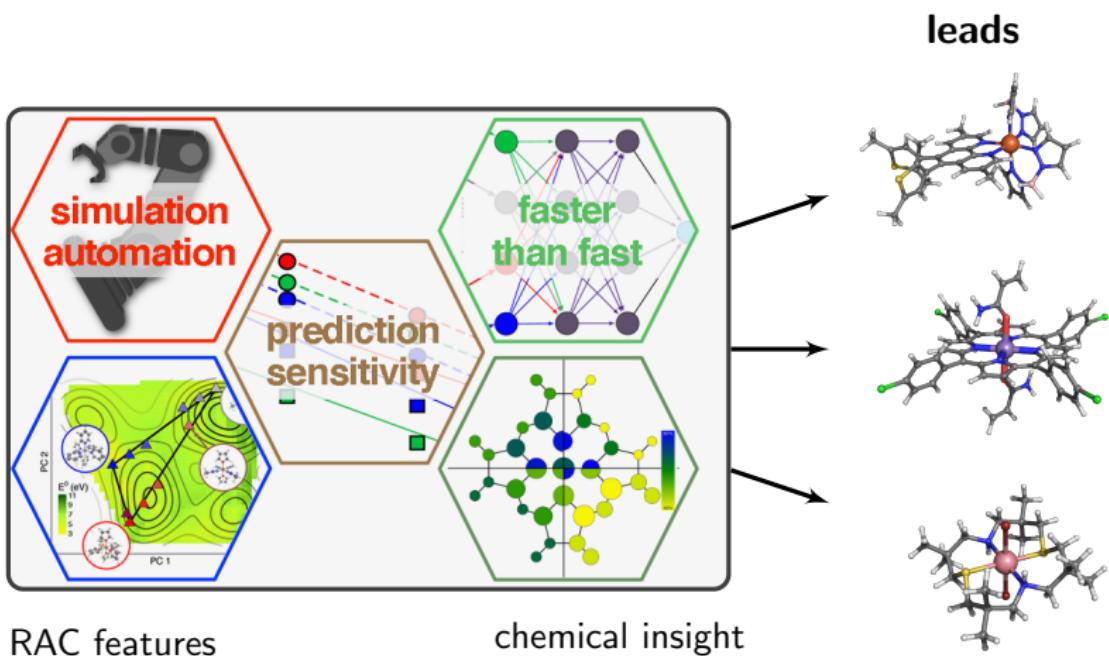
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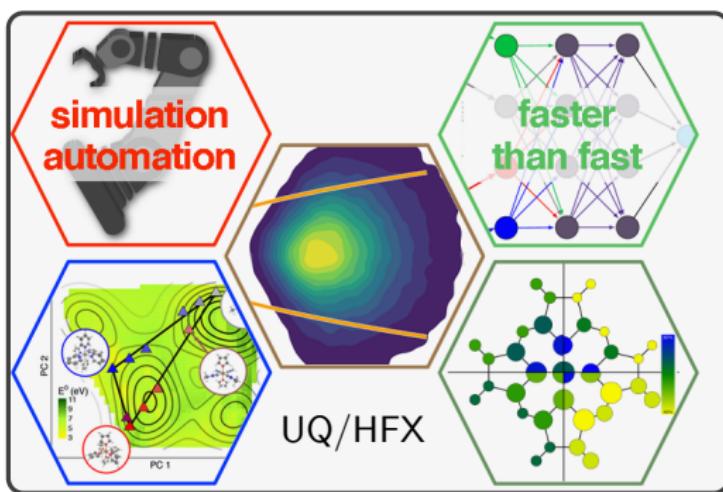
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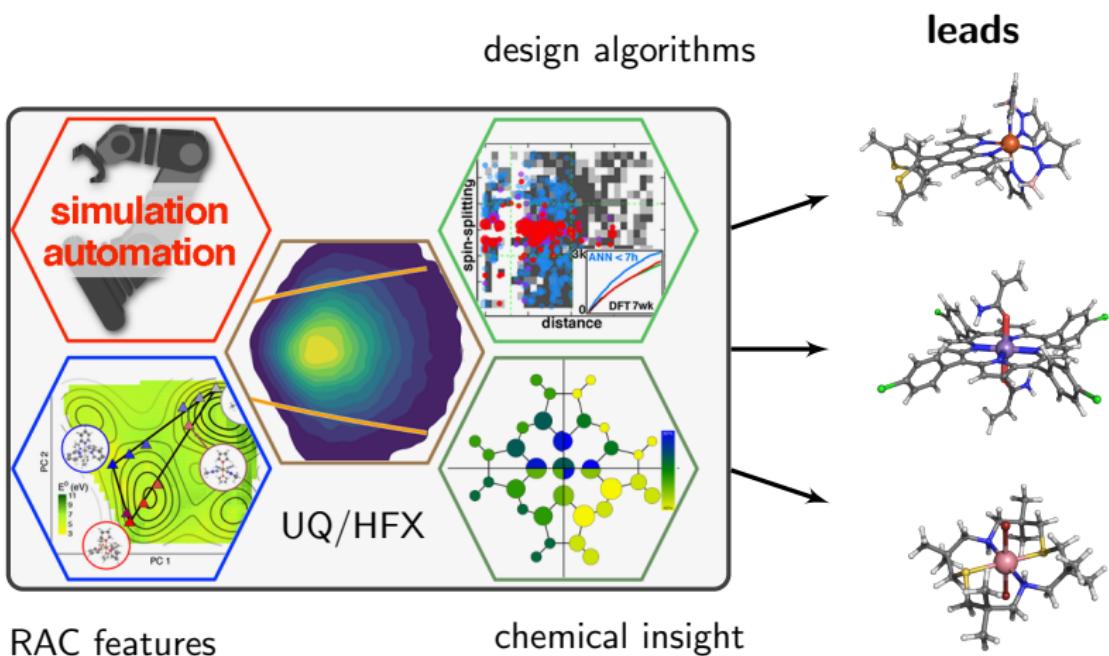
More than just ML



RAC features

chemical insight

More than just ML

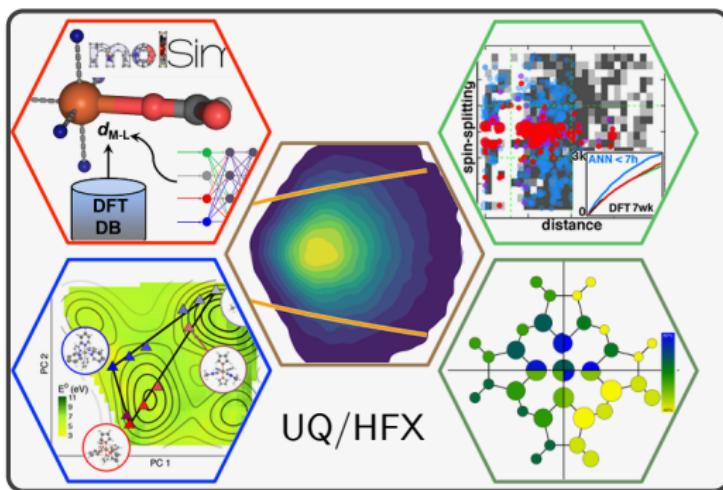


More than just ML



github.com/hjkgrp

mAD/molSimplify



design algorithms

leads

RAC features

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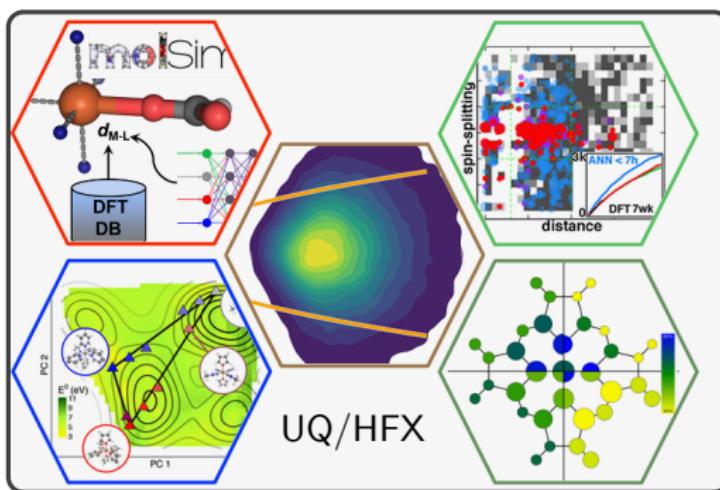


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An end-to-end approach for rational TM complex design

Case study: redox couples

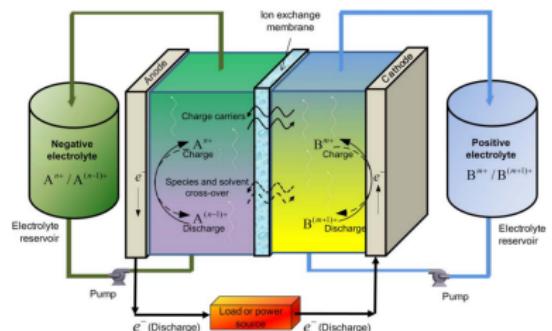
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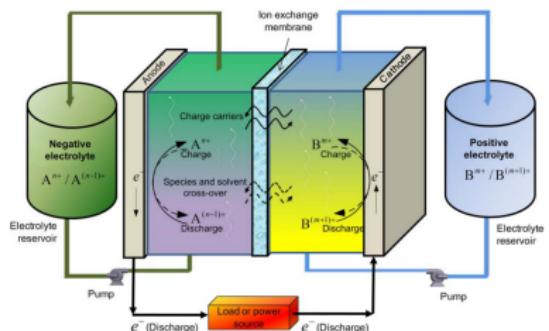
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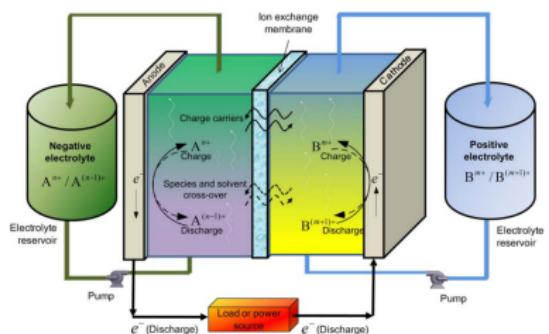


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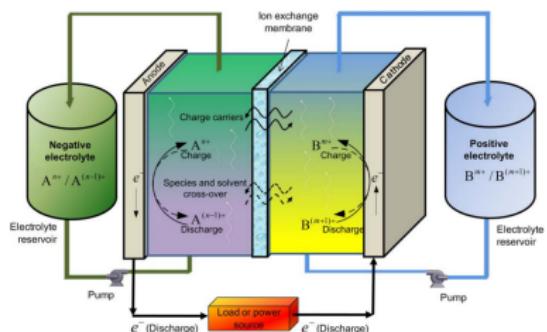
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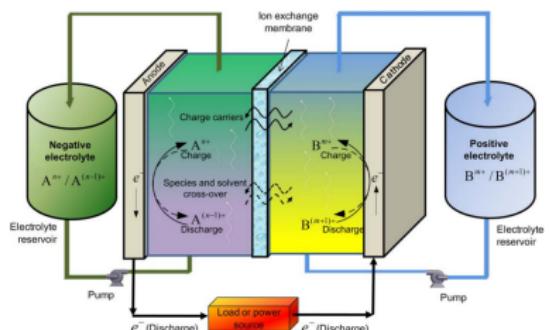
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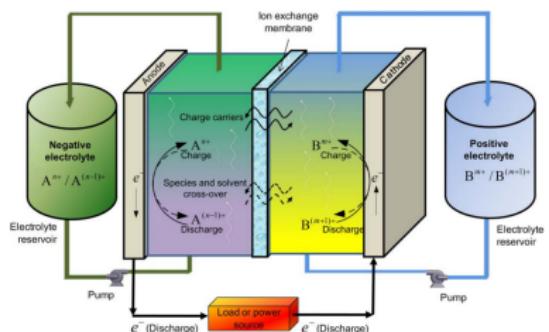
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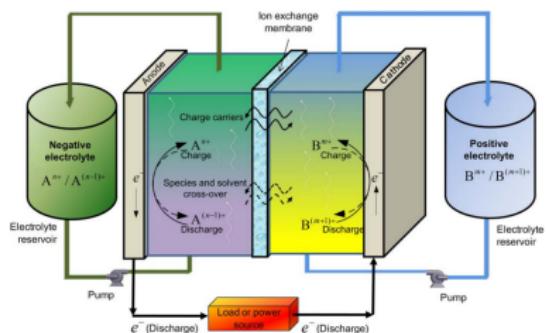
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We need complexes that have high redox potential **and** good solubility

Introduction
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Features and models
ooo

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oooooooo

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oo

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○●oooooooo

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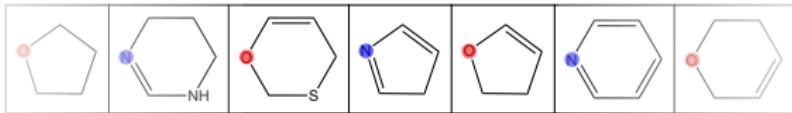
Design space construction

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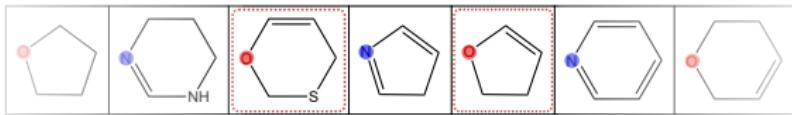
$\mathcal{O}(10^1)$



40 heterocycles

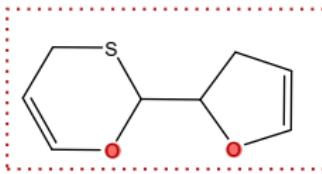
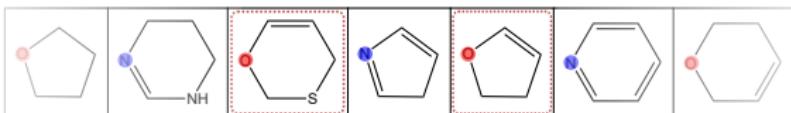
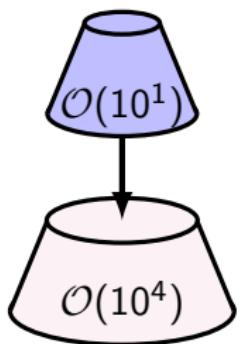
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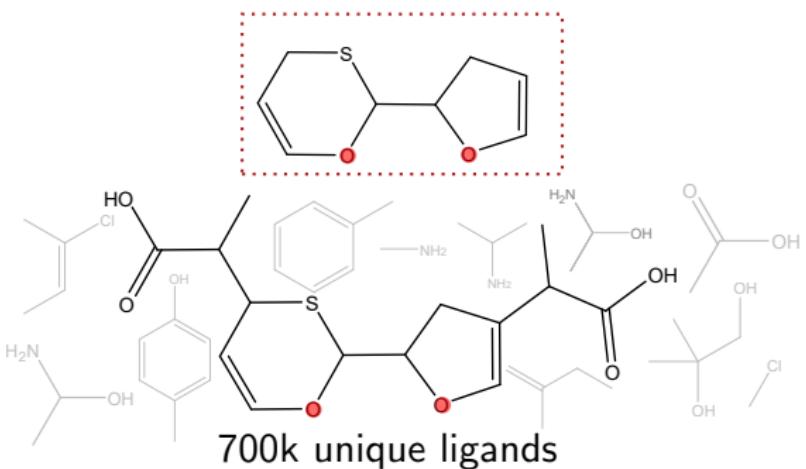
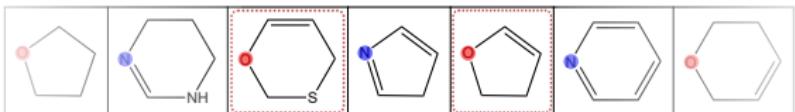
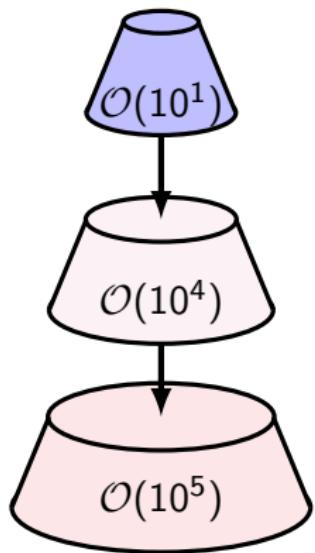
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Design space construction

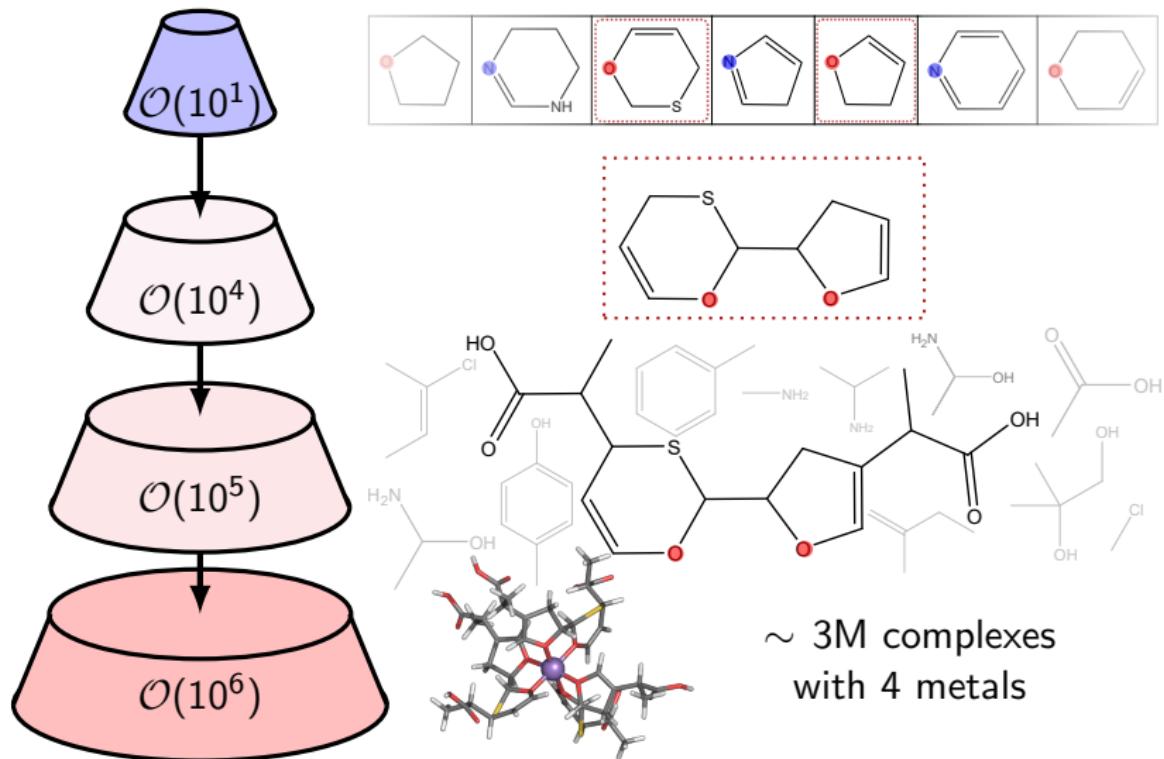


800 base ligands

Design space construction



Design space construction



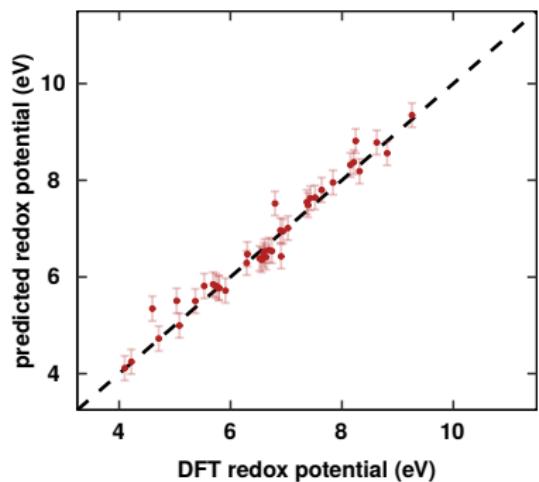
Multiobjective framework

We can predict quantities of interest for our RFBs:

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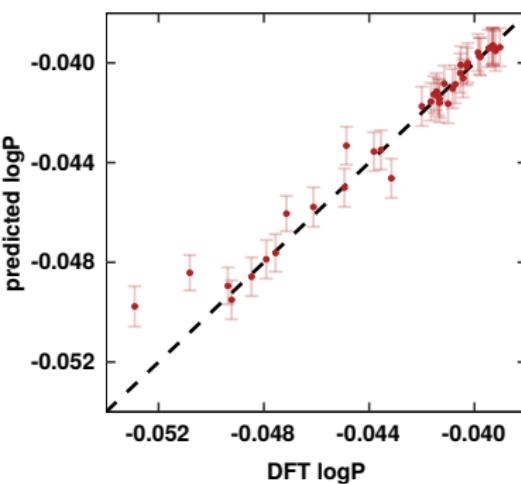
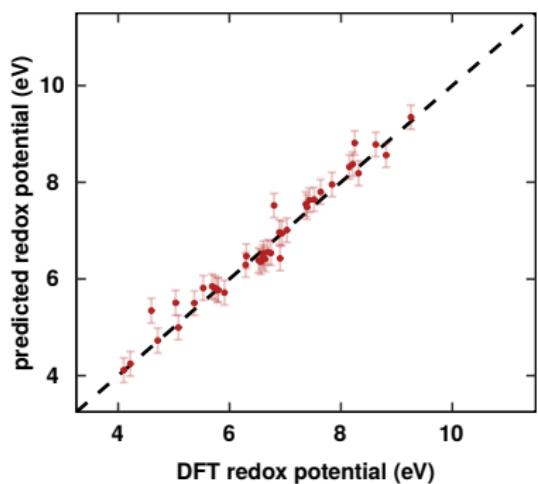


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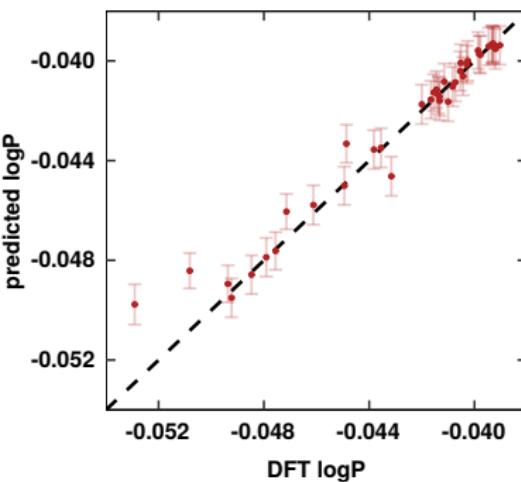
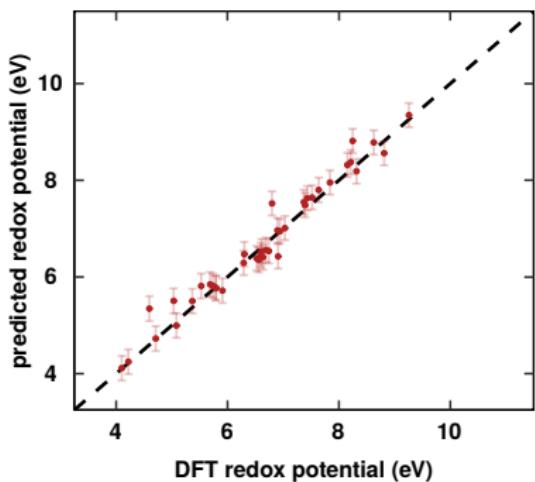


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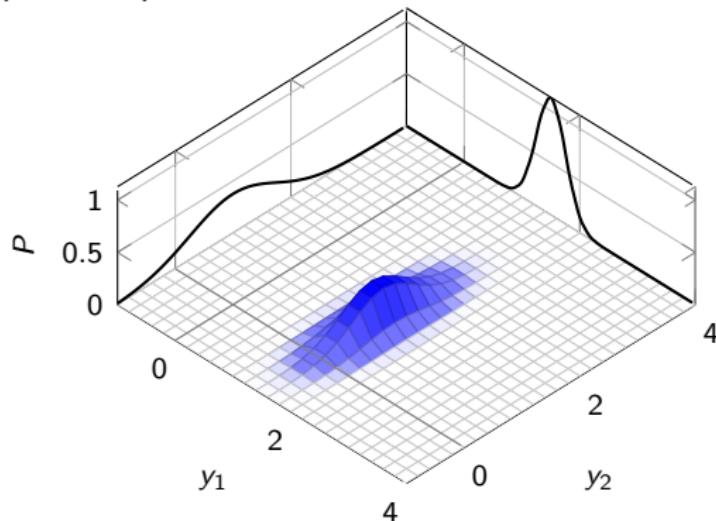
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$$\begin{aligned} \Delta G_{\text{solv}} &= \begin{bmatrix} \hat{y}_1 \\ \hat{y}_2 \end{bmatrix} \sim \mathcal{N} \left(\begin{bmatrix} \hat{\mu}_1 \\ \hat{\mu}_2 \end{bmatrix}, \begin{bmatrix} \hat{\sigma}_1^2 & 0 \\ 0 & \hat{\sigma}_2^2 \end{bmatrix} \right) \\ \log P & \end{aligned}$$

Multiobjective framework

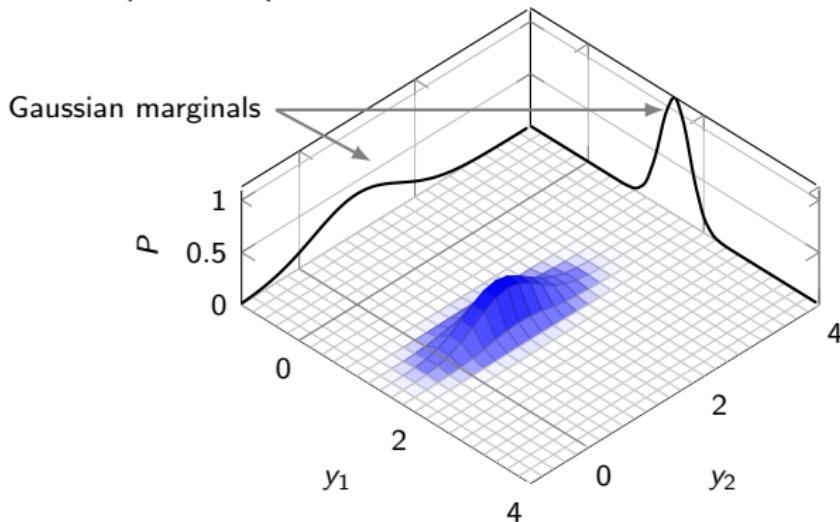
We can predict quantites of interest for our RFBs:



$$\Delta G_{\text{solv}} = \begin{bmatrix} \hat{y}_1 \\ \hat{y}_2 \end{bmatrix} \sim \mathcal{N} \left(\begin{bmatrix} \hat{\mu}_1 \\ \hat{\mu}_2 \end{bmatrix}, \begin{bmatrix} \hat{\sigma}_1^2 & 0 \\ 0 & \hat{\sigma}_2^2 \end{bmatrix} \right)$$

Multiobjective framework

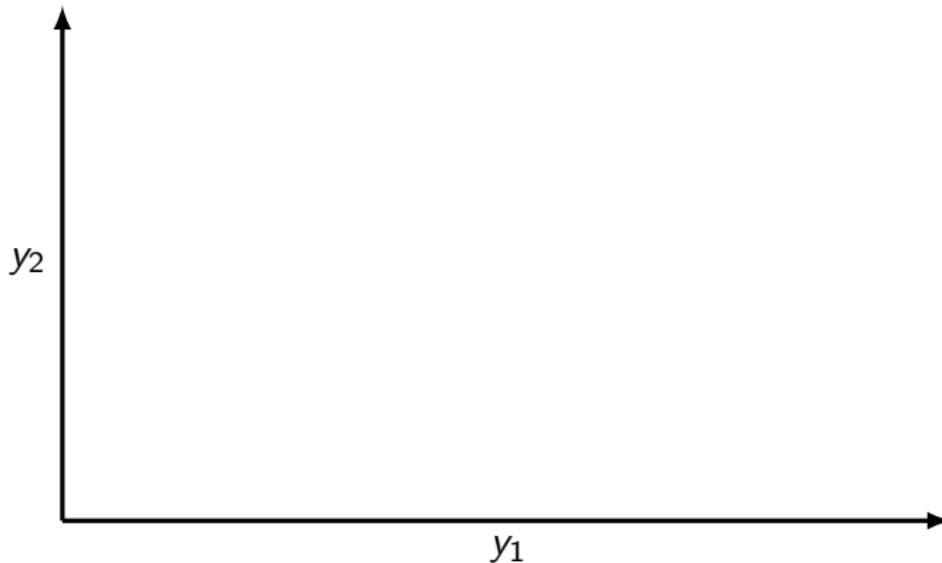
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$$\Delta G_{\text{solv}} = \begin{bmatrix} \hat{y}_1 \\ \hat{y}_2 \end{bmatrix} \sim \mathcal{N} \left(\begin{bmatrix} \hat{\mu}_1 \\ \hat{\mu}_2 \end{bmatrix}, \begin{bmatrix} \hat{\sigma}_1^2 & 0 \\ 0 & \hat{\sigma}_2^2 \end{bmatrix} \right)$$

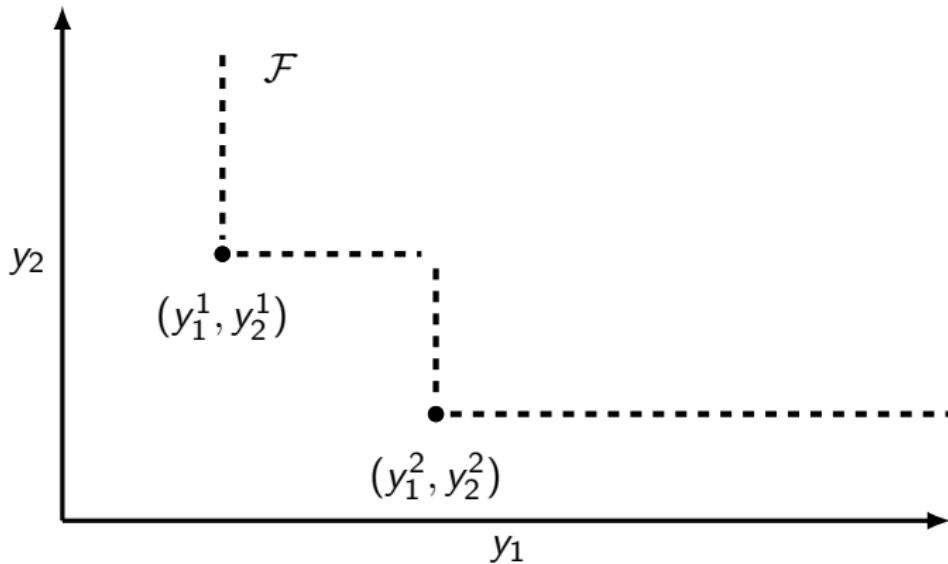
2D EGO Illustration

We will use a multiobjective expected improvement framework:



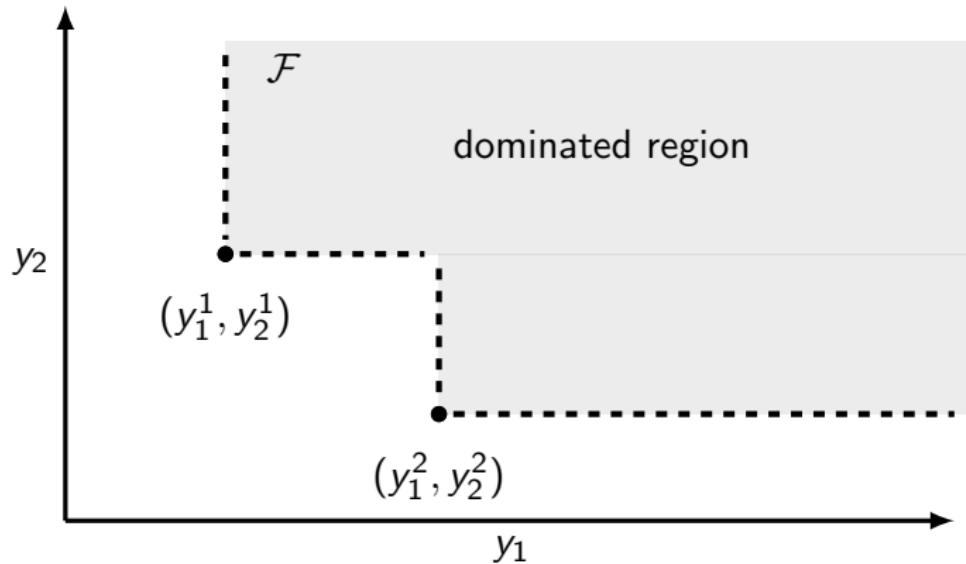
2D EGO Illustration

We will use a multiobjective expected improvement framework:



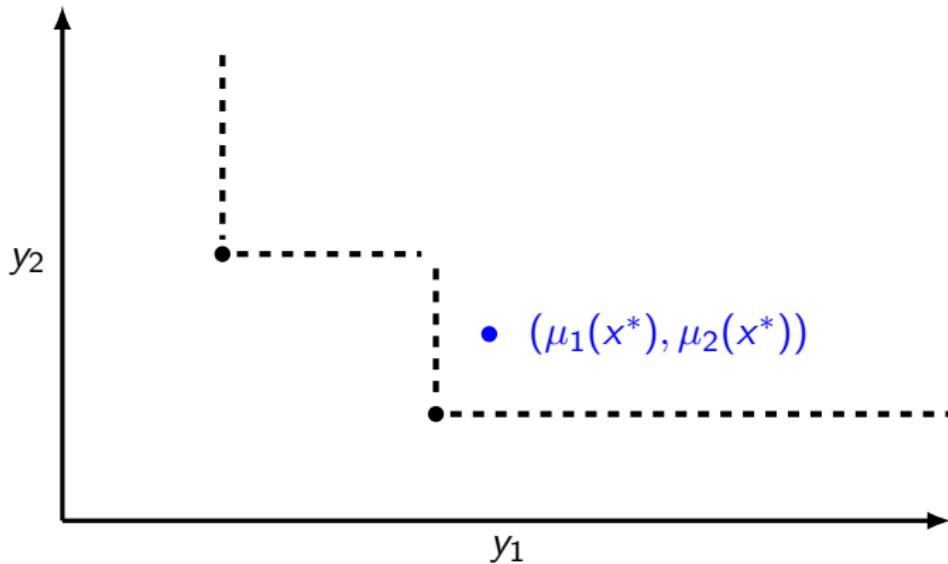
2D EGO Illustration

We will use a multiobjective expected improvement framework:



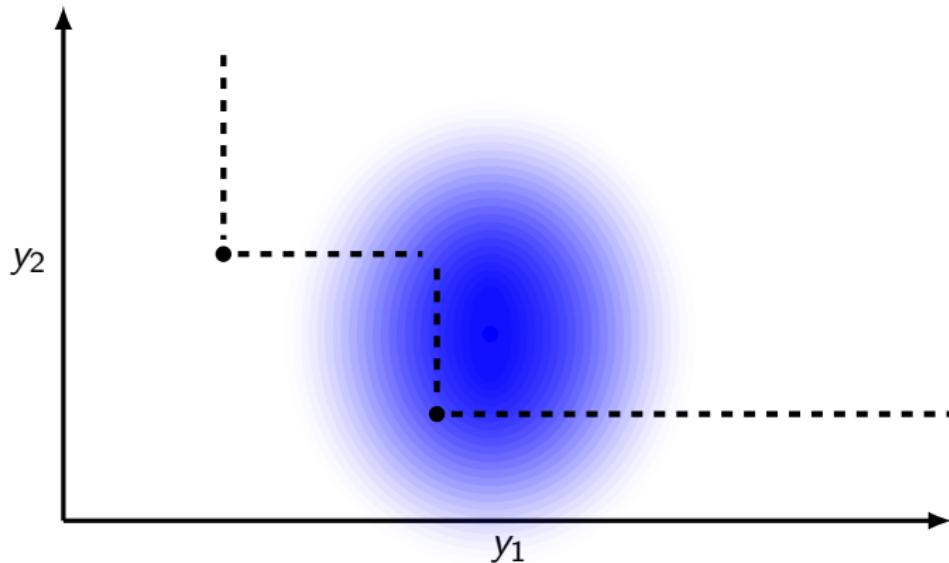
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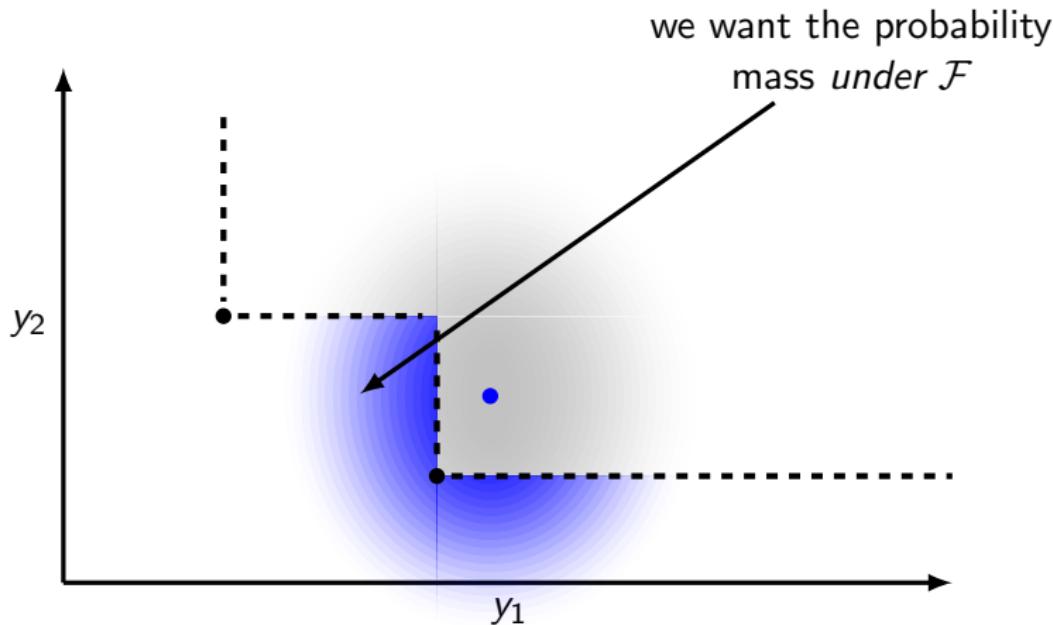
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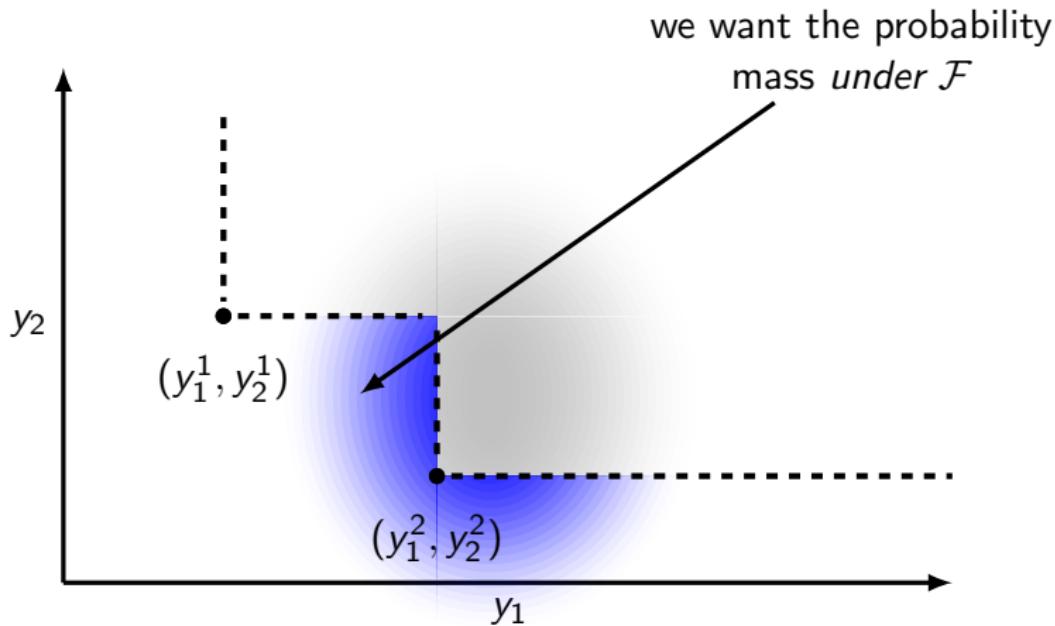
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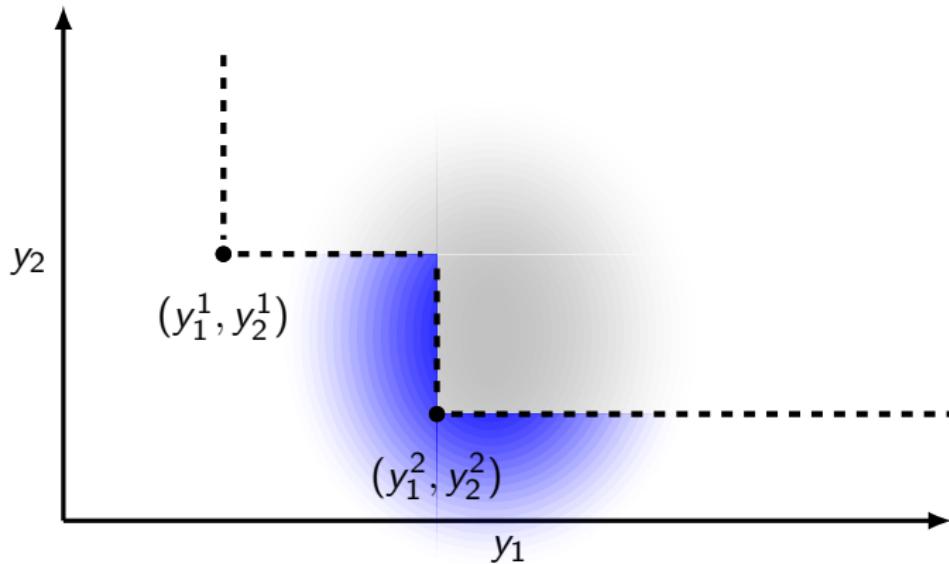
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2D EGO Illustration

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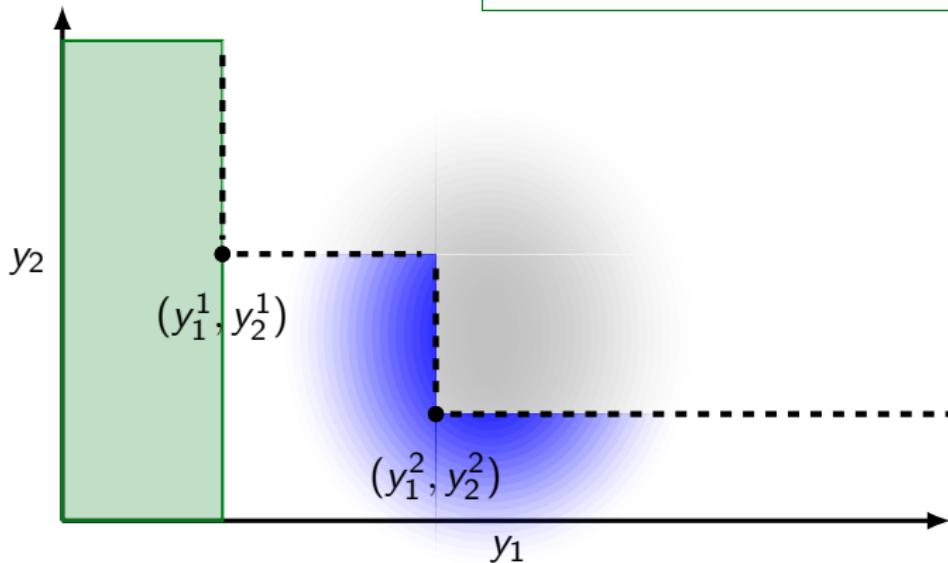
$$P(I) =$$



2D EGO Illustration

We will use a multiobjective expected improvement framework:

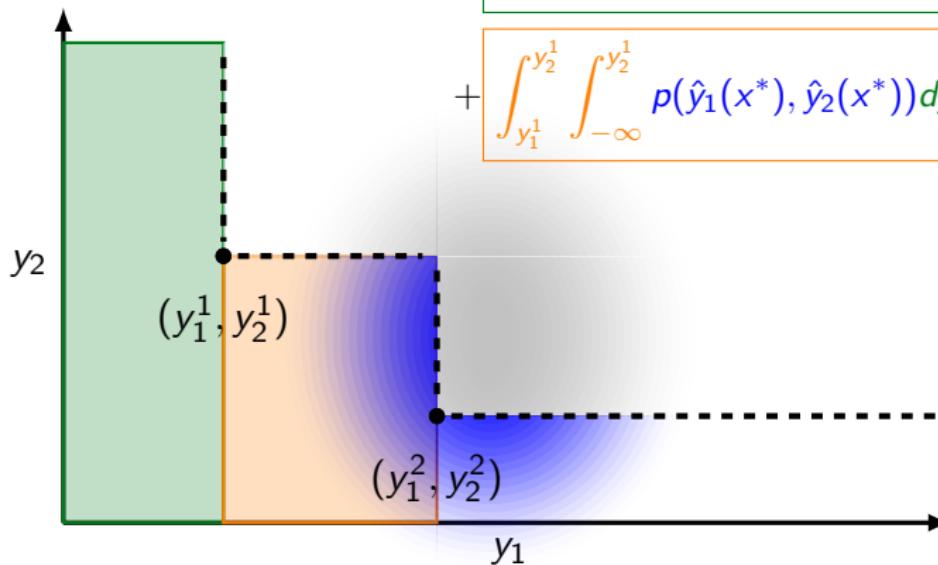
$$P(I) = \int_{-\infty}^{y_1^1} \int_{-\infty}^{\infty} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2$$



2D EGO Illustration

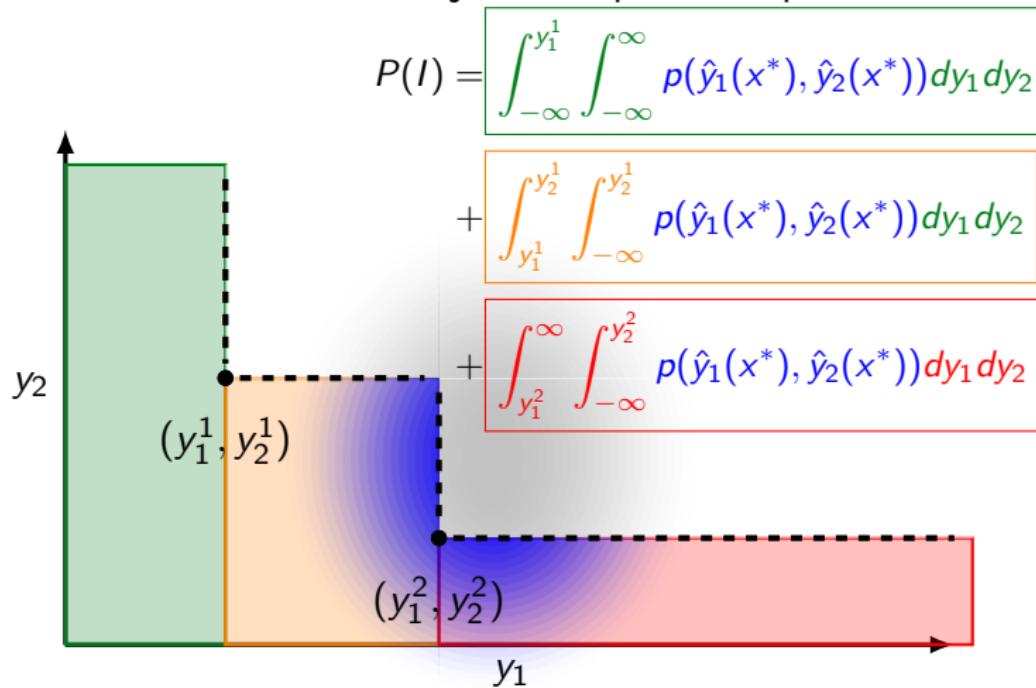
We will use a multiobjective expected improvement framework:

$$P(I) = \int_{-\infty}^{y_1^1} \int_{-\infty}^{\infty} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2 + \int_{y_1^1}^{y_2^1} \int_{-\infty}^{y_2^1} p(\hat{y}_1(x^*), \hat{y}_2(x^*)) dy_1 dy_2$$



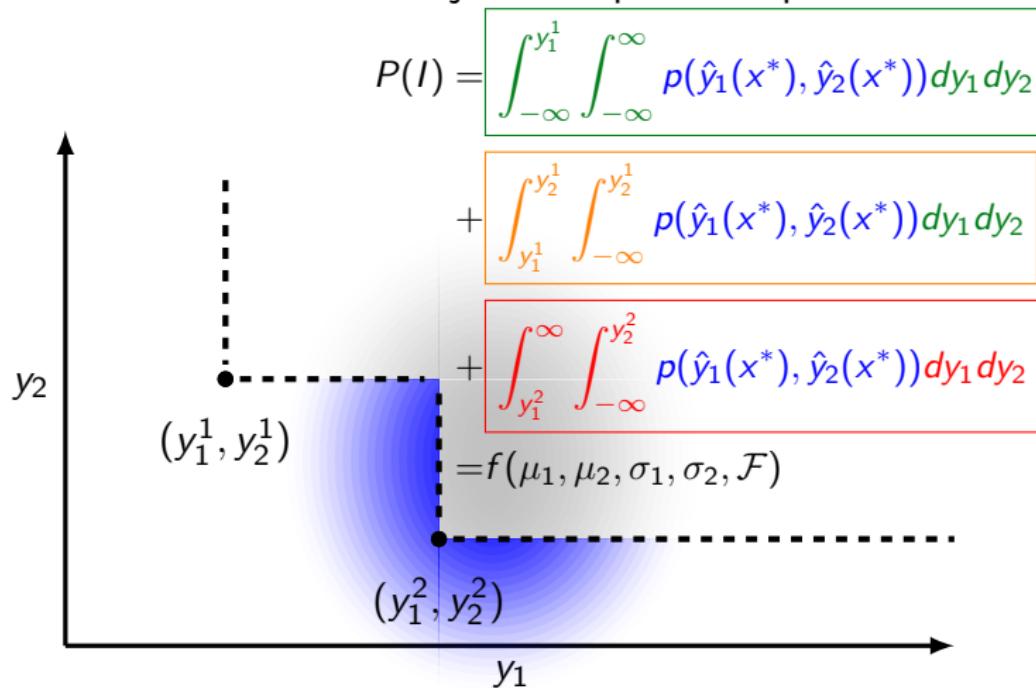
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We will use a multiobjective expected improvement framework:



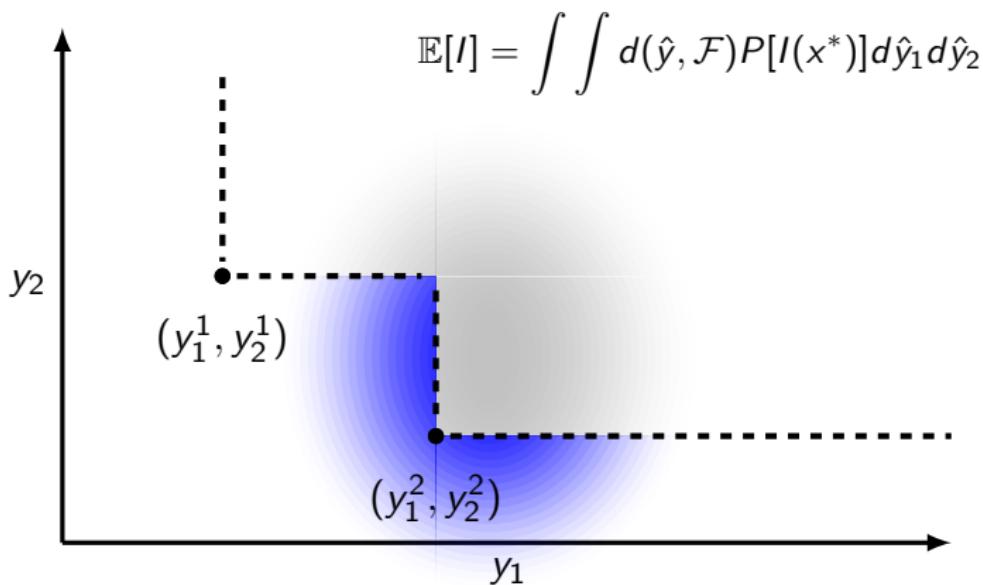
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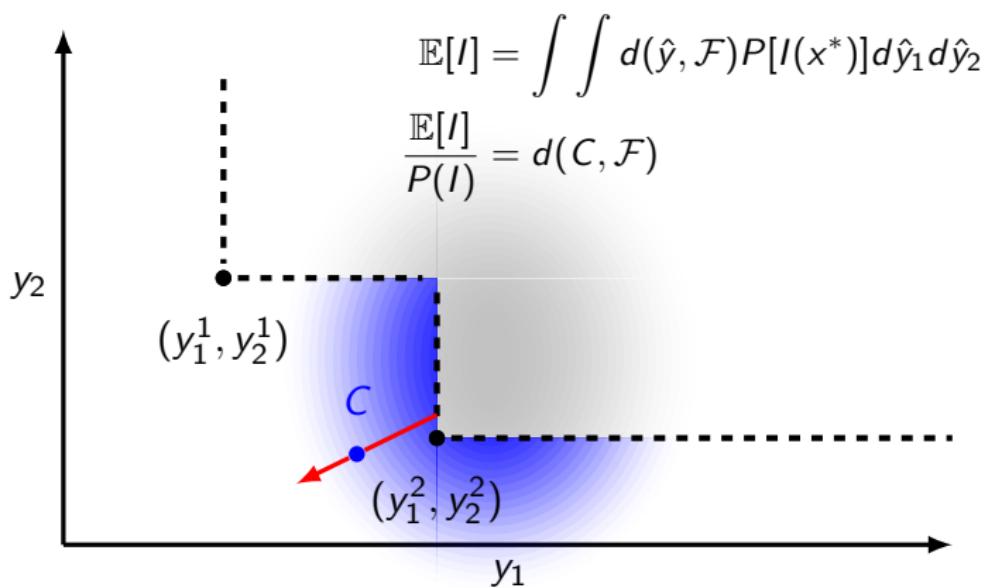
2D EGO Illustration

We will use a multiobjective expected improvement framework:



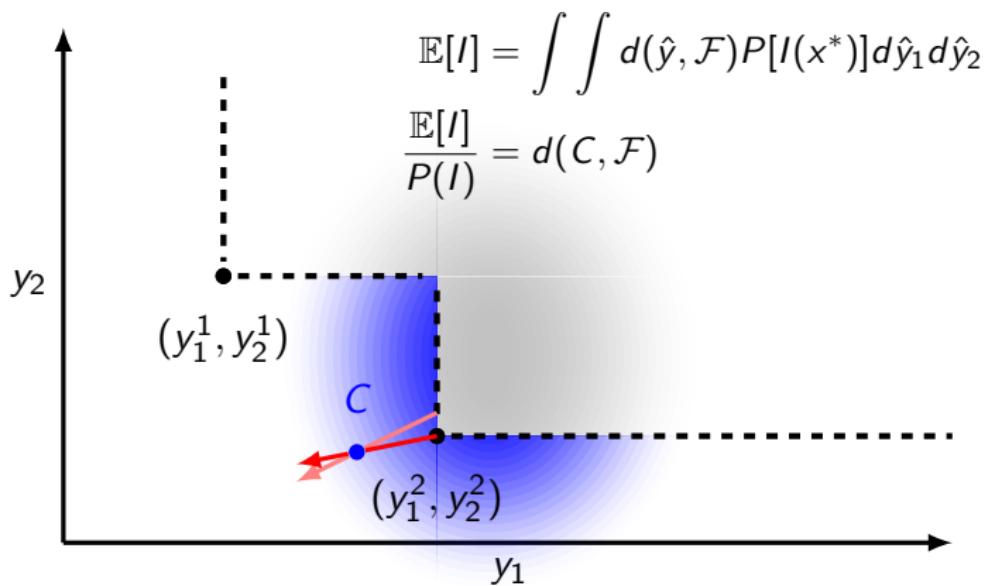
2D EGO Illustration

We will use a multiobjective expected improvement framework:



2D EGO Illustration

We will use a multiobjective expected improvement framework:

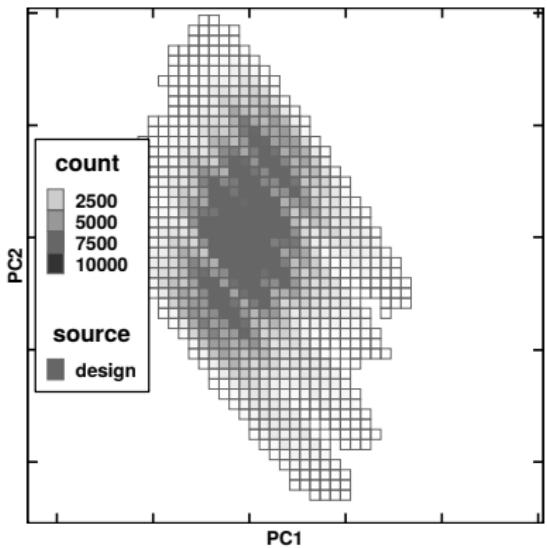


Design space and existing data

We observe poor overlap between existing data and design space:

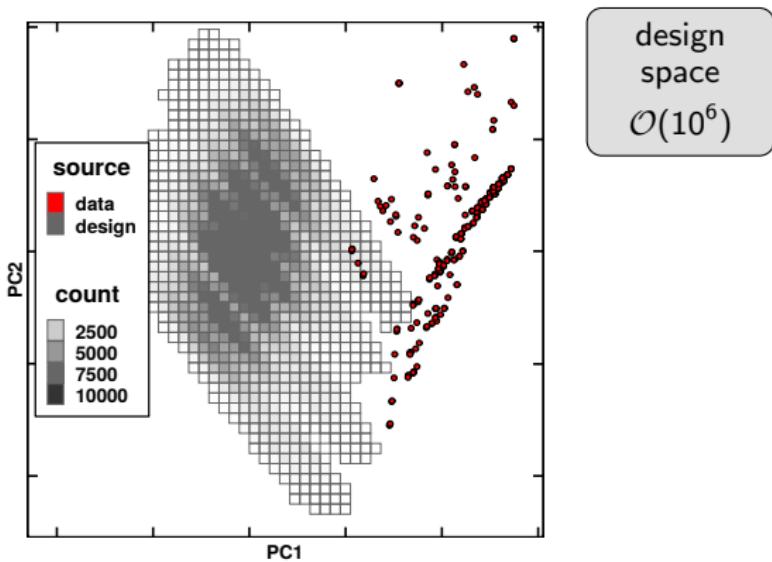
Design space and existing data

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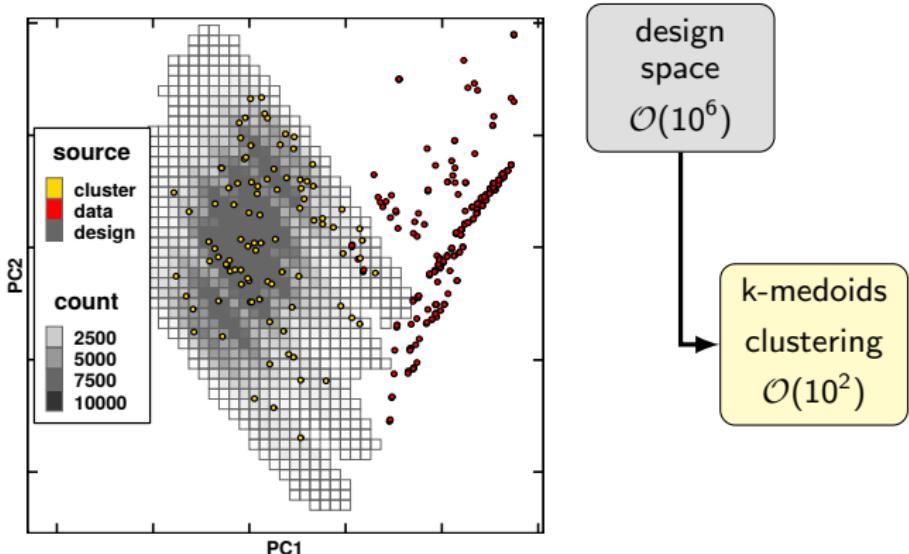
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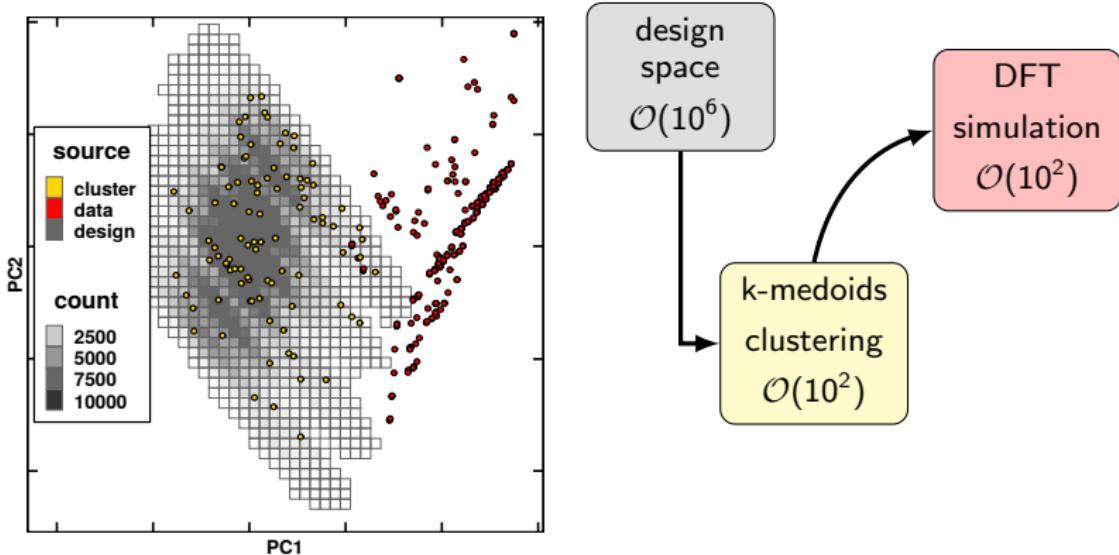
Design space and existing data

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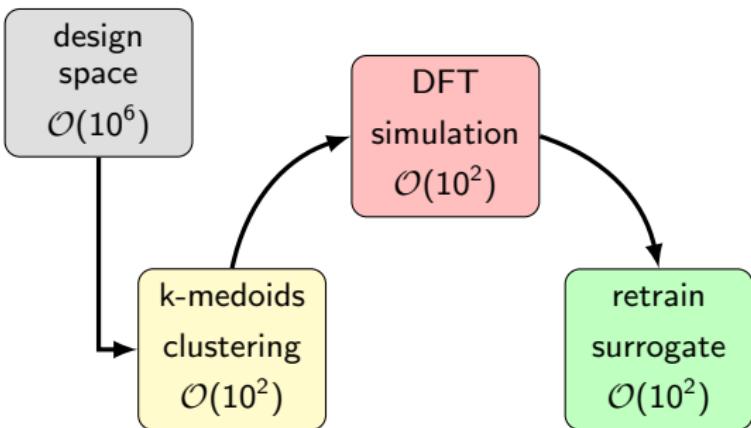
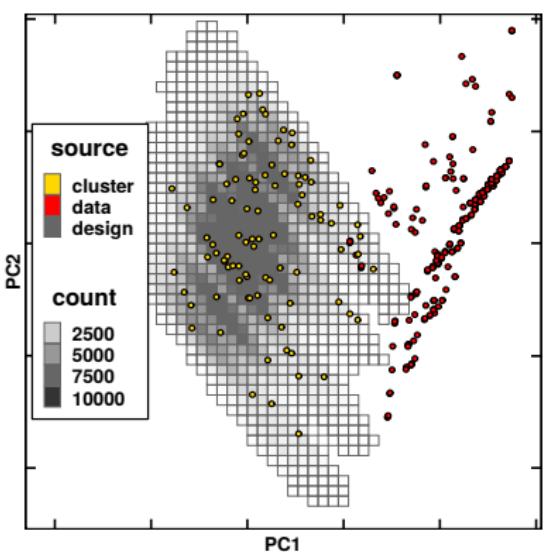
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We observe poor overlap between existing data and design space:



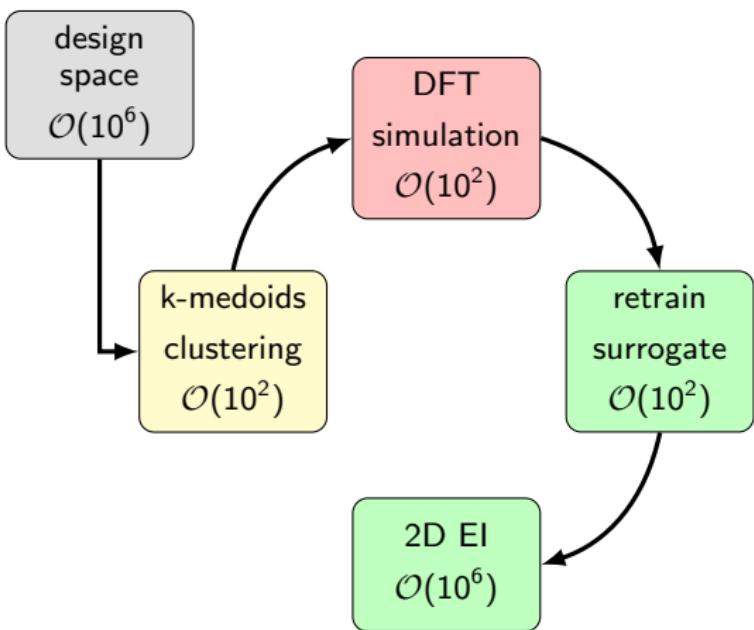
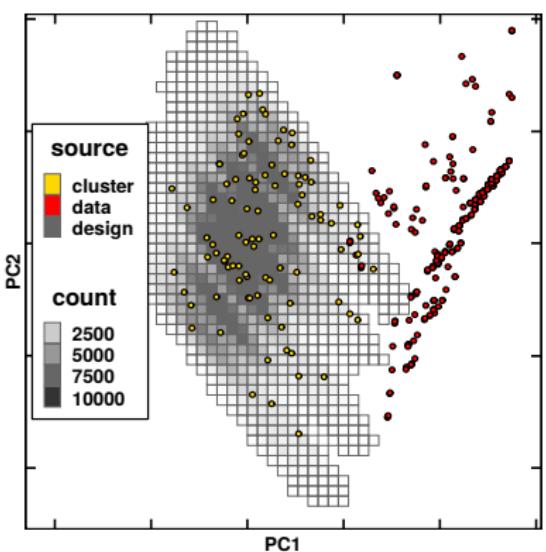
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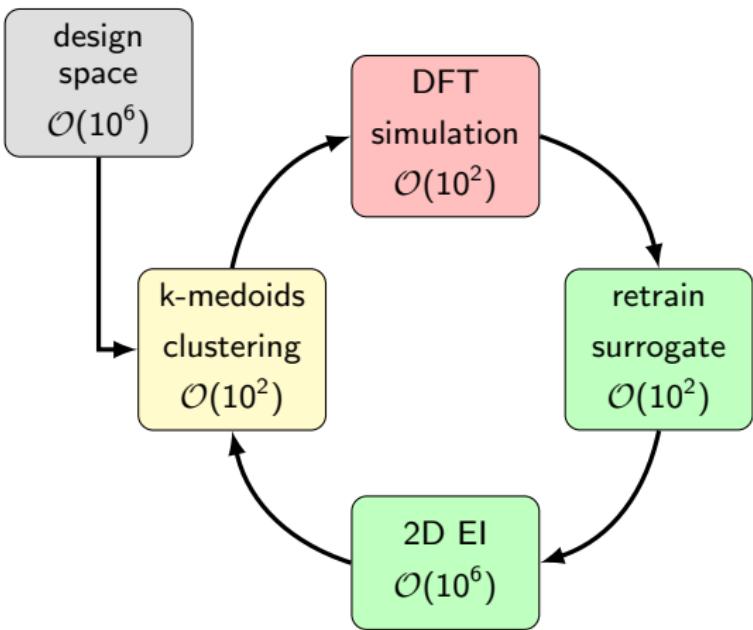
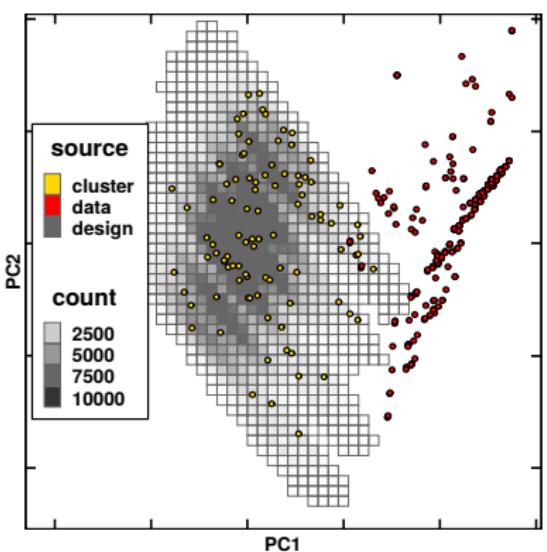
Design space and existing data

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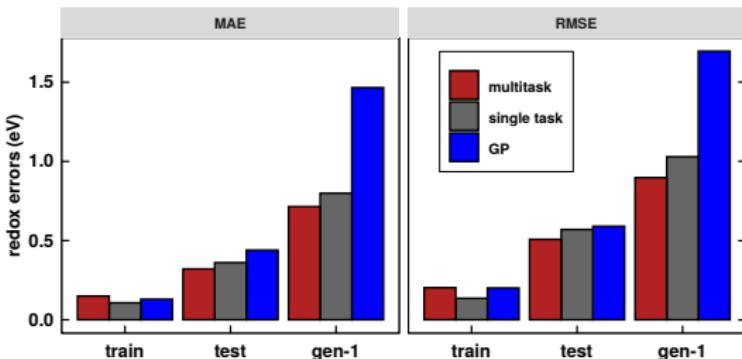
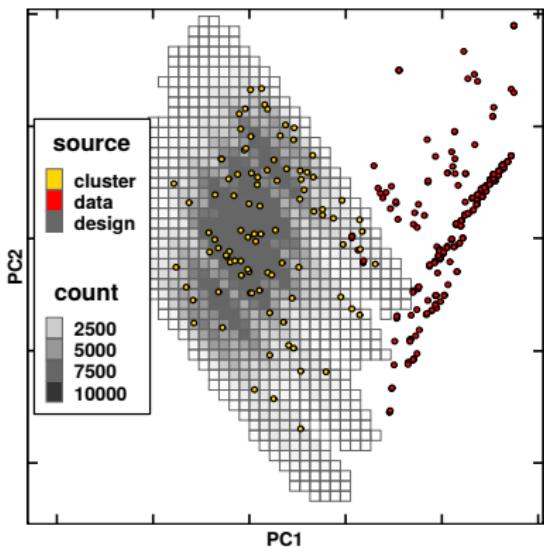
Design space and existing data

We observe poor overlap between existing data and design space:



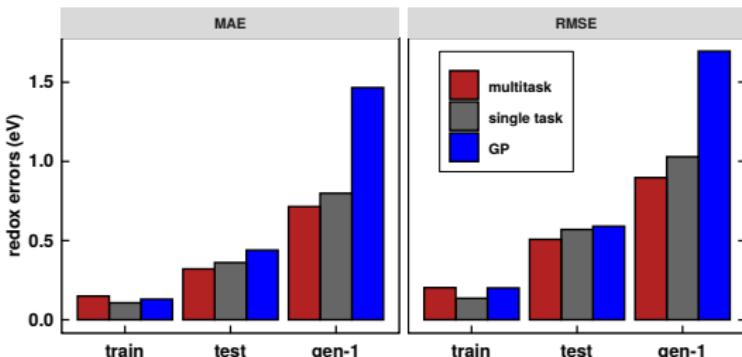
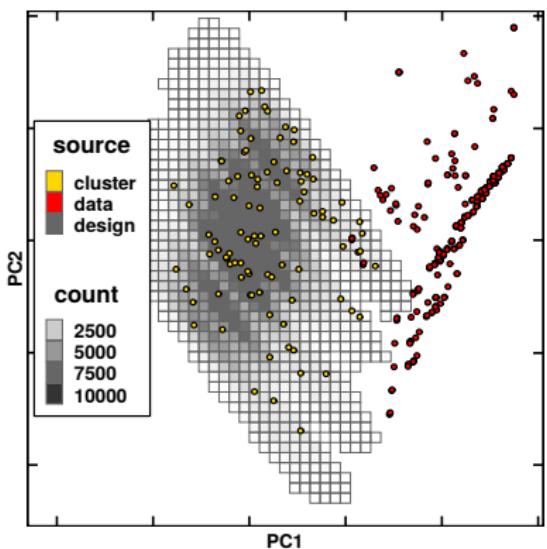
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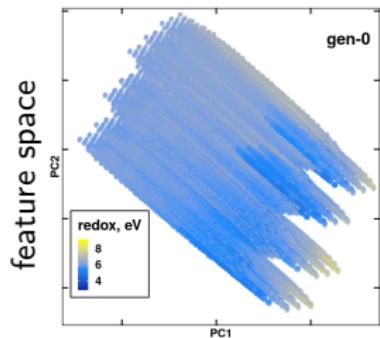


Therefore, we will use multitask ANN to drive the design process

single task redox: 3×100 tanh nodes, fully connected
single task log P: 2×50 ReLU nodes, skip + residual connections
multitask: 2×100 tanh nodes, fully connected

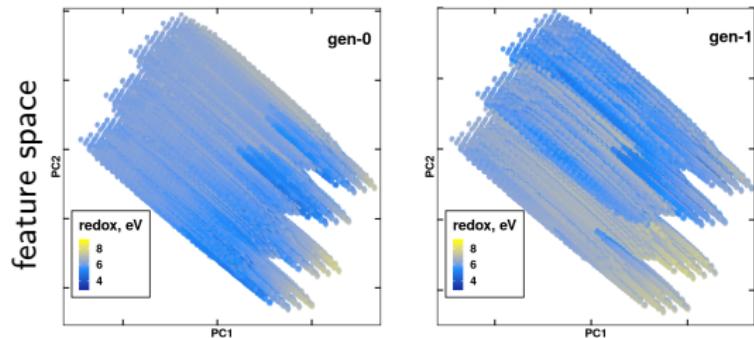
Active learning

We can monitor the evolution of the model as data is acquired



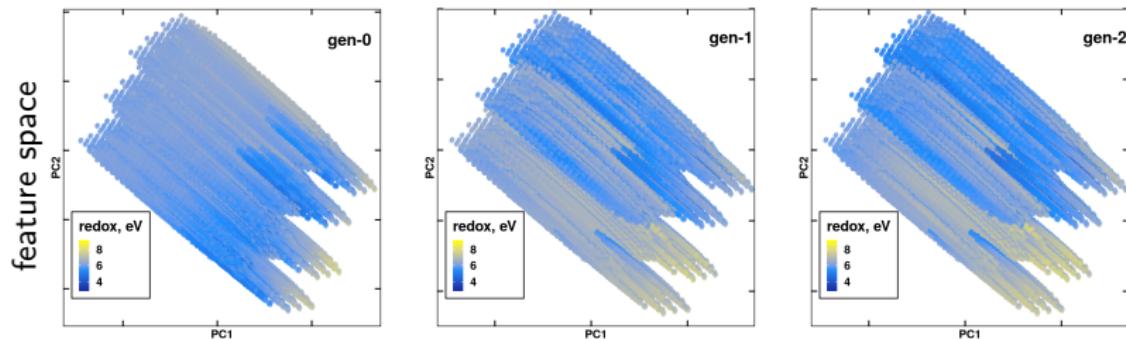
Active learning

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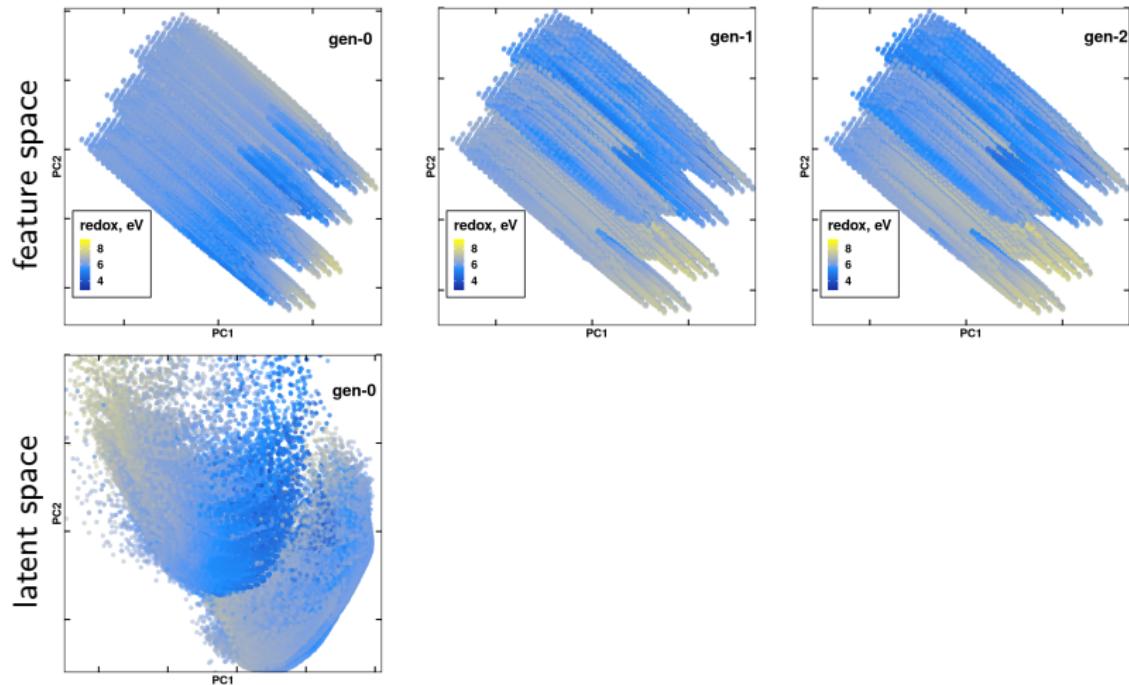
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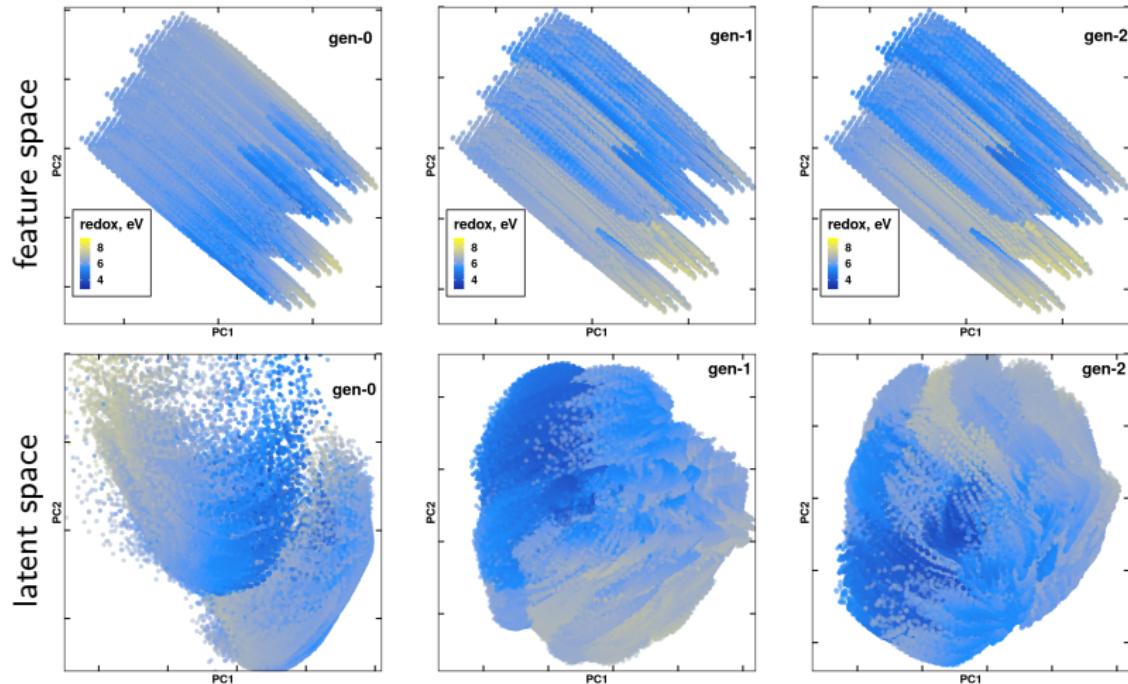
Active learning

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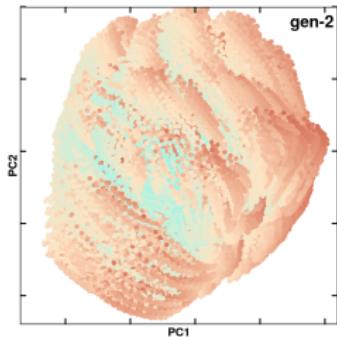
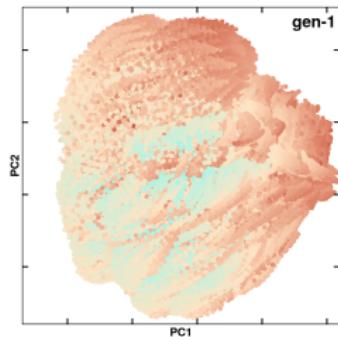
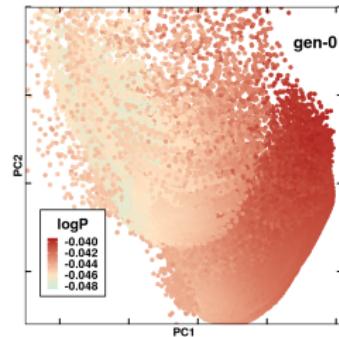
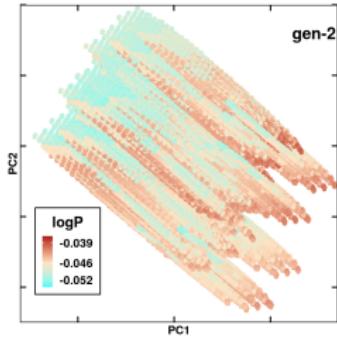
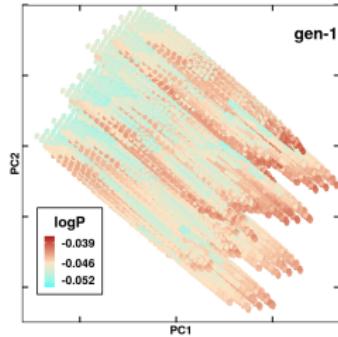
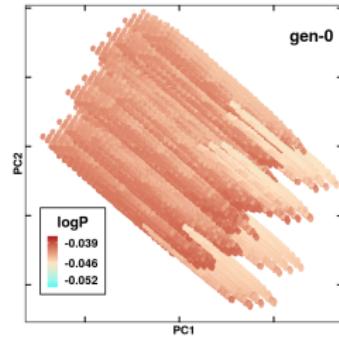
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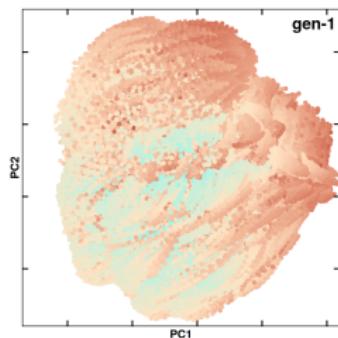
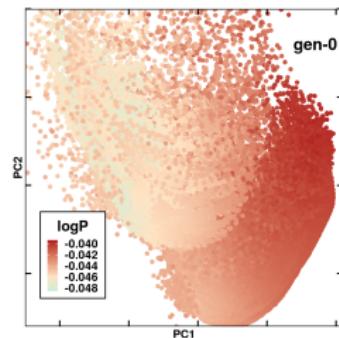
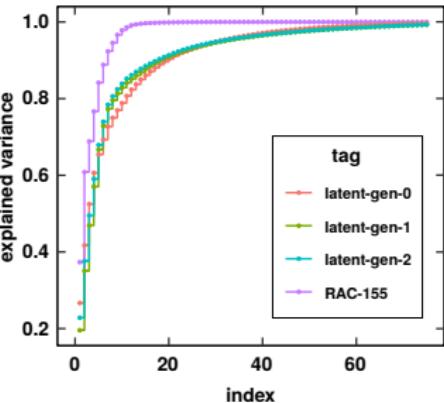
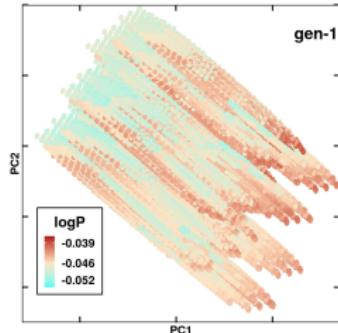
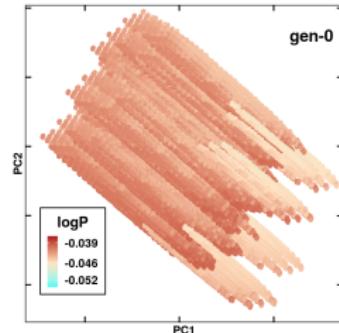
Active learning

We can monitor the evolution of the model as data is acquired

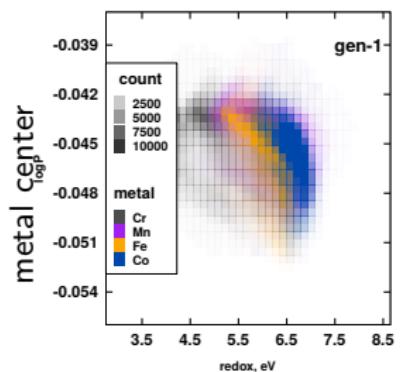


Active learning

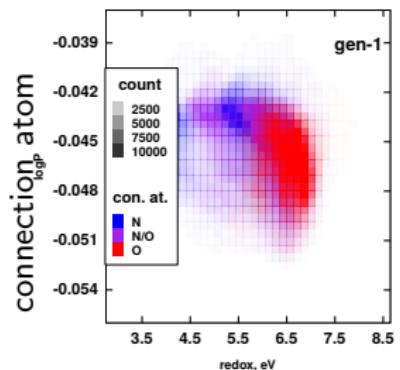
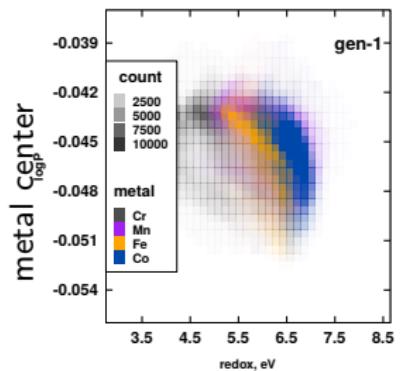
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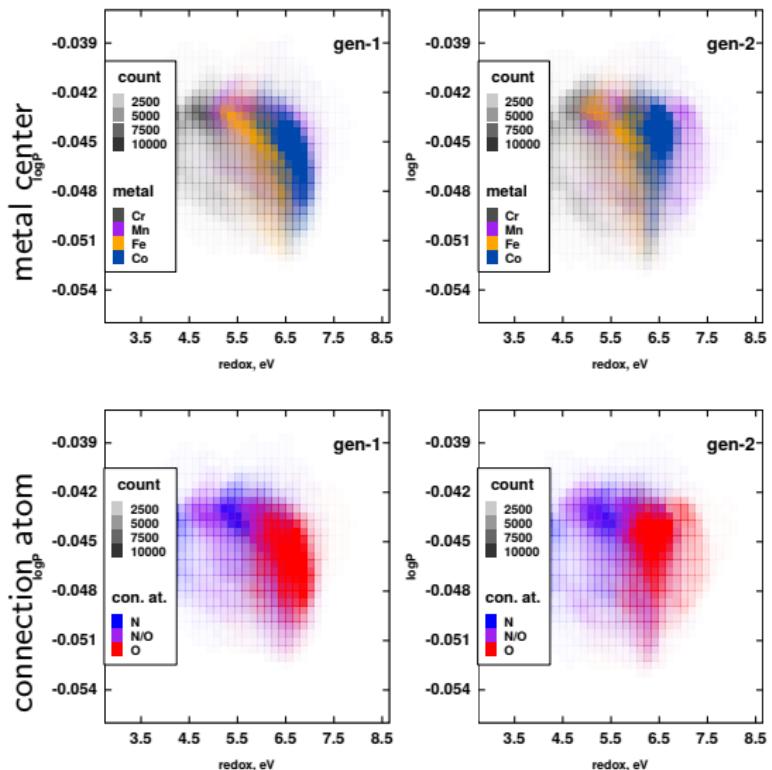
Mapping output space



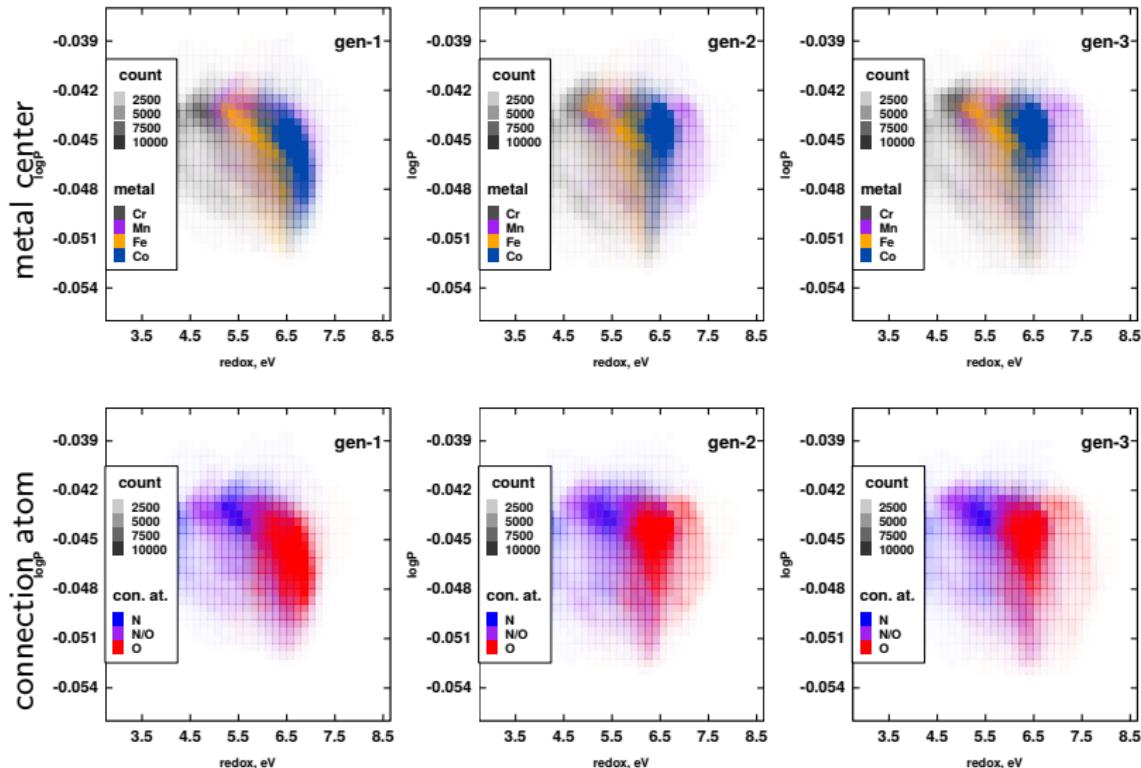
Mapping output space



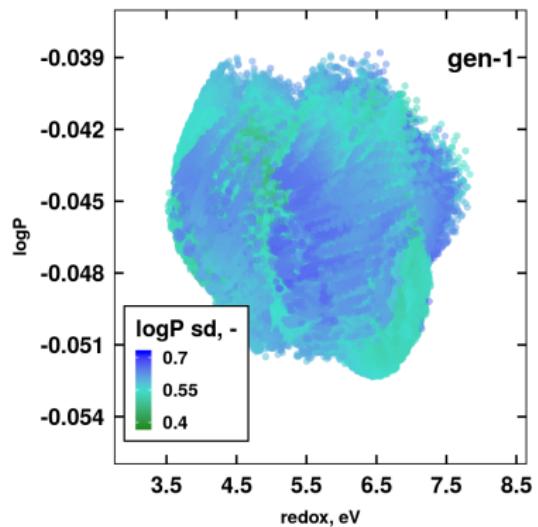
Mapping output space



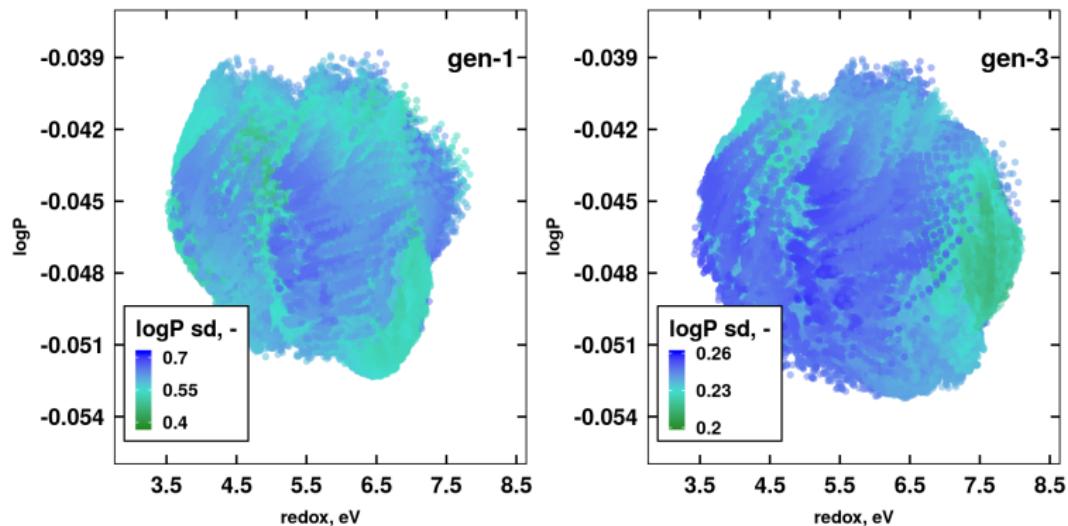
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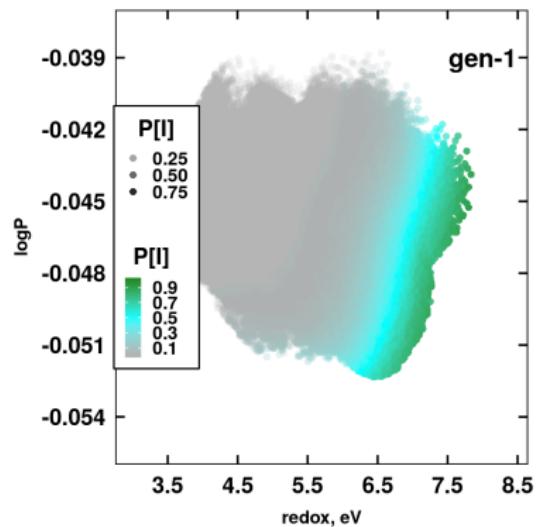
Mapping output space



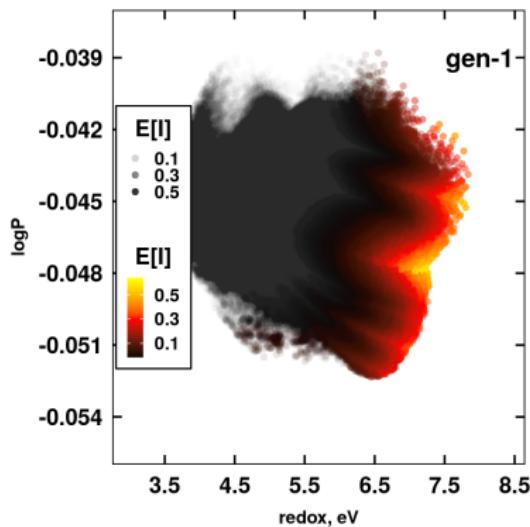
model confidence is localized in target region!

EGO results

probability of improvement

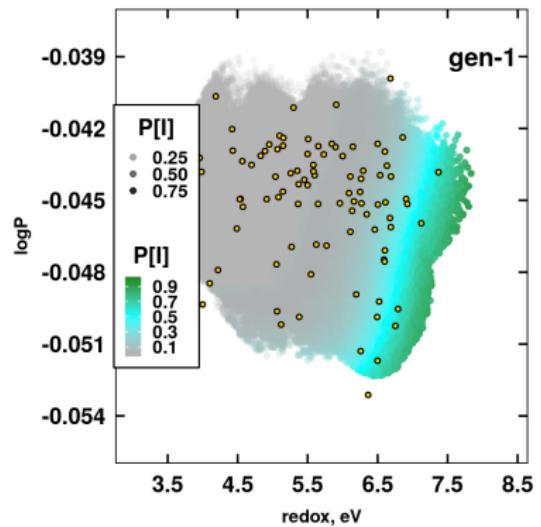


expected improvement

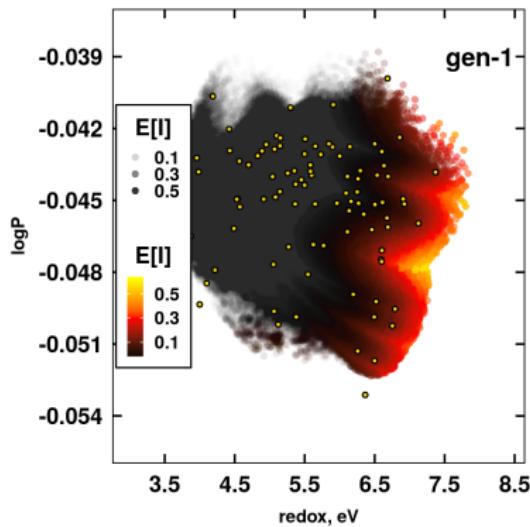


EGO results

probability of improvement

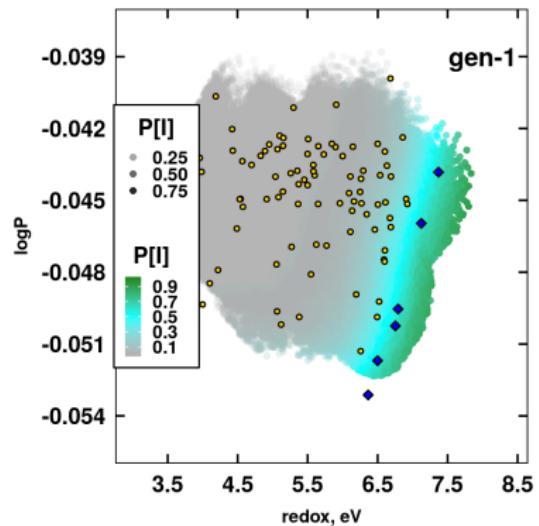


expected improvement

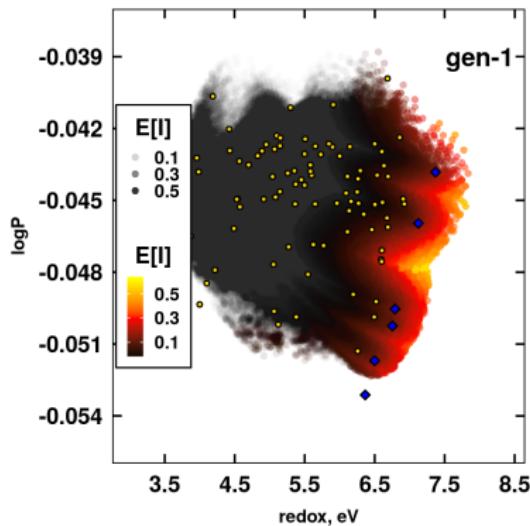


EGO results

probability of improvement

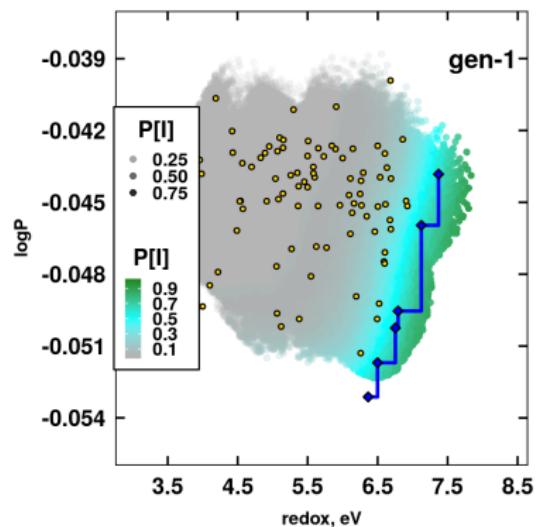


expected improvement

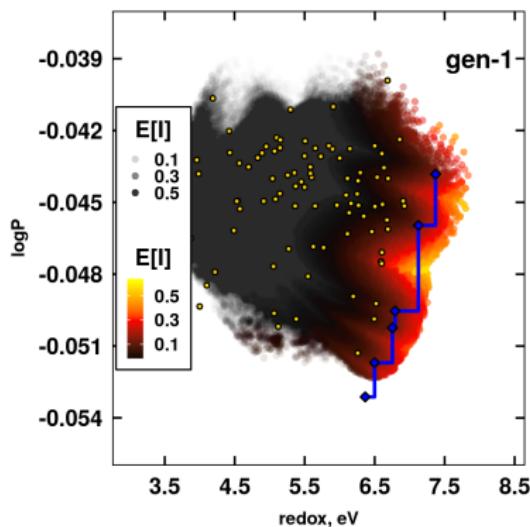


EGO results

probability of improvement



expected improvement

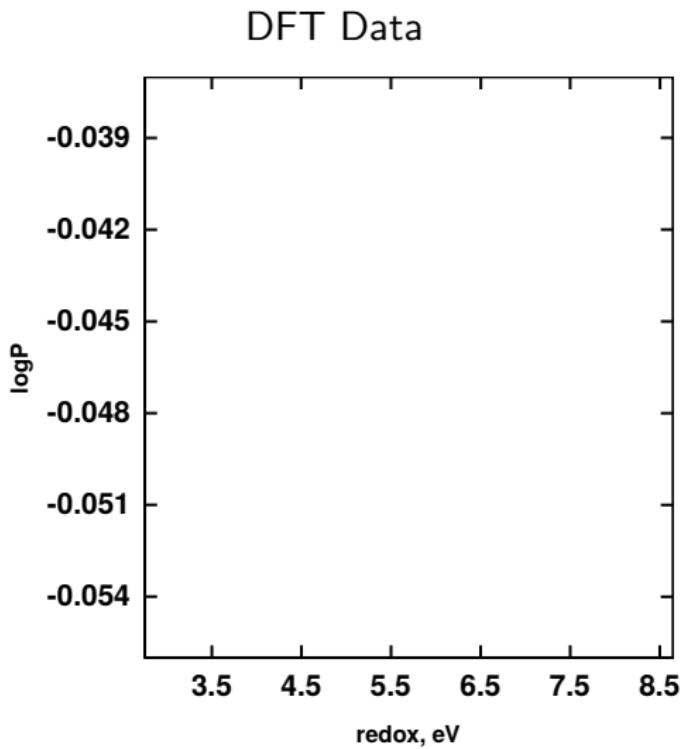


EGO results

probability of improvement

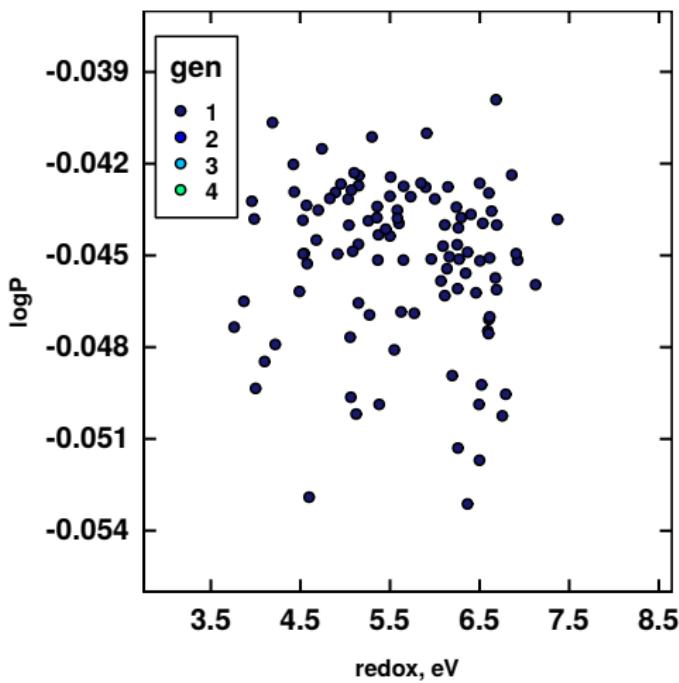
expected improvement

DFT results

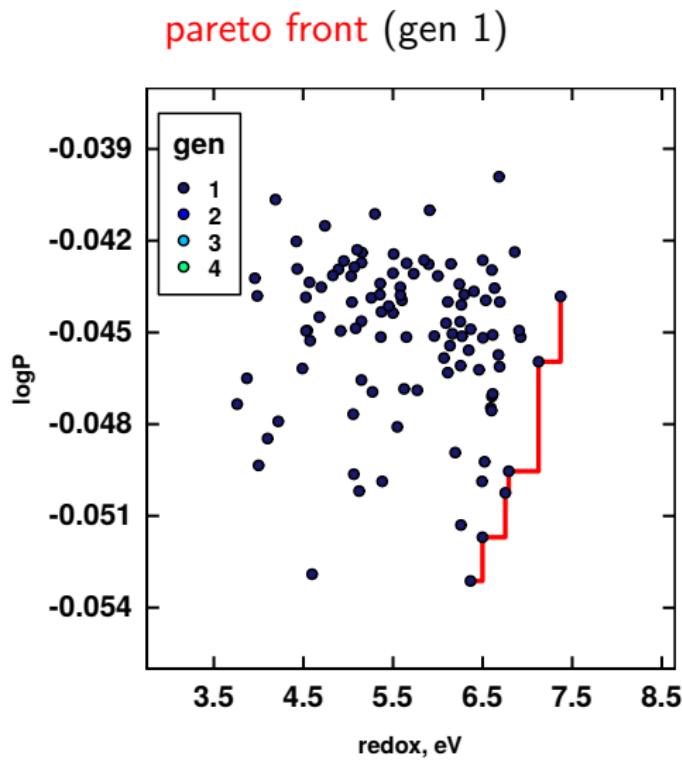


DFT results

k-medoids points (gen 1: 107 complexes)

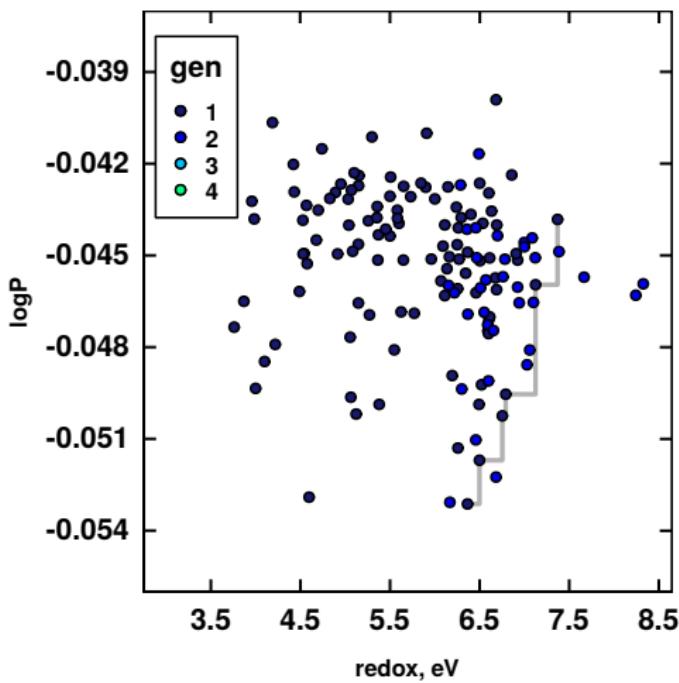


DFT results

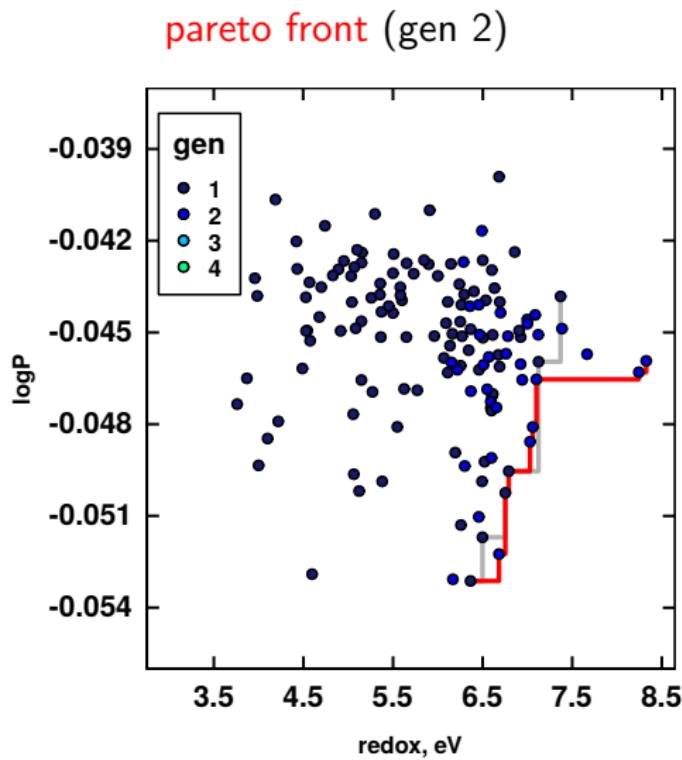


DFT results

El points (gen 2: 34 complexes)

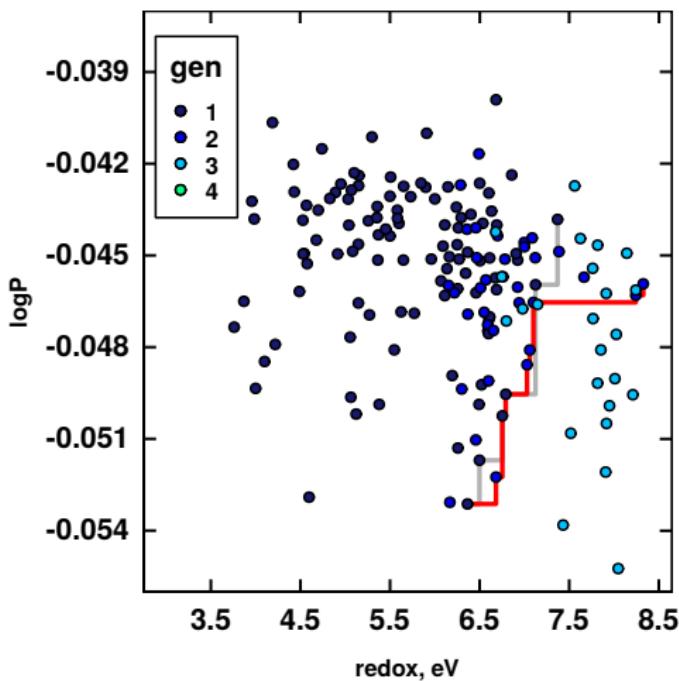


DFT results

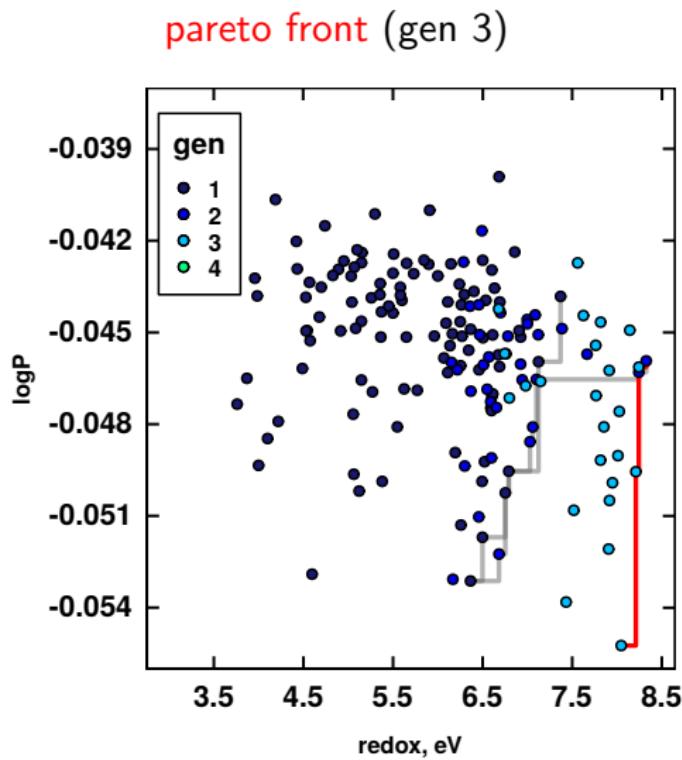


DFT results

El points (gen 3: 24 complexes)

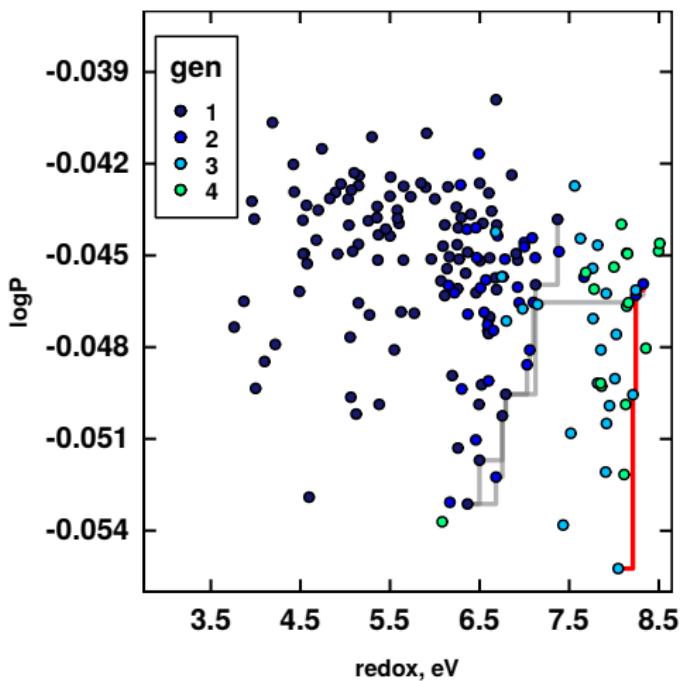


DFT results

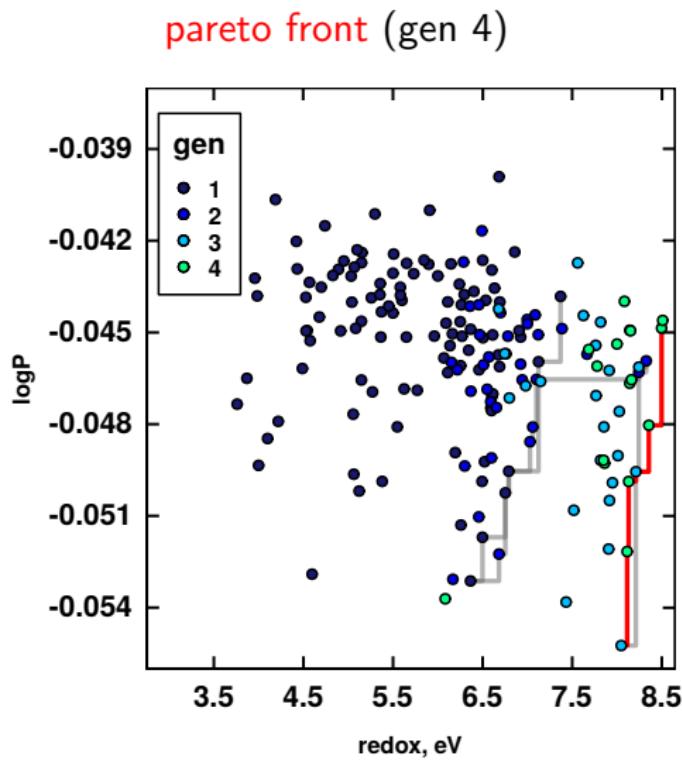


DFT results

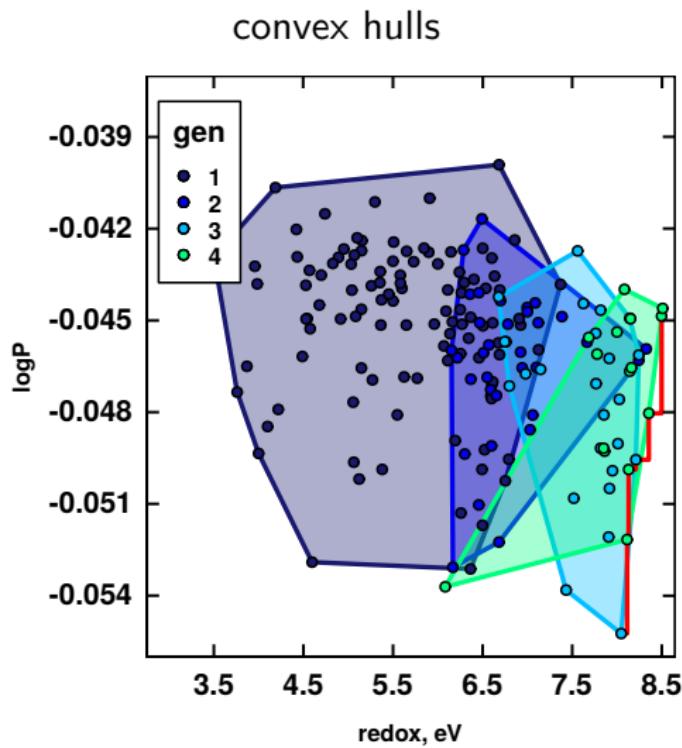
El points (gen 4: 15 complexes)



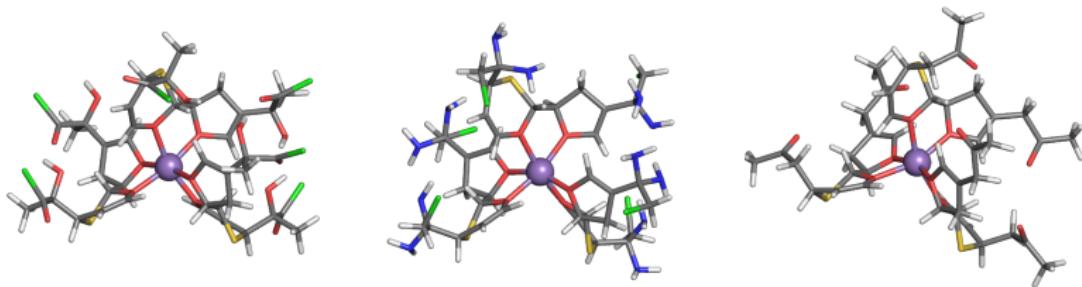
DFT results



DFT results



DFT results



Introduction
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Features and models
ooo

Uncertainty
oooooooo

Discovery
oo

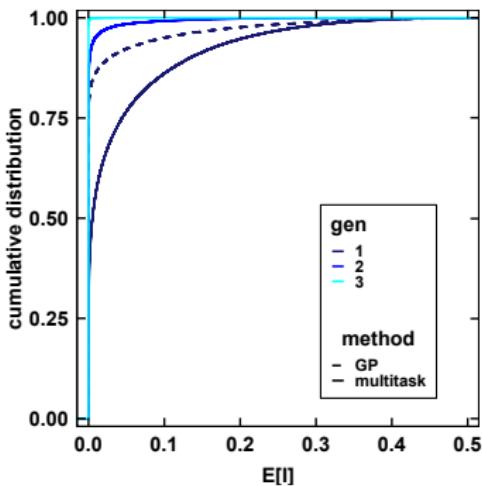
Case Study
oooooooooooo

Conclusions
●○○

Case study conclusions

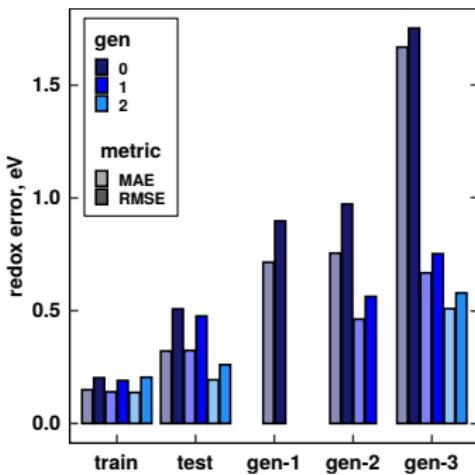
Case study conclusions

- EI framework provides high resolution in the region of interest (c.f. maximum uncertainty), converges quickly



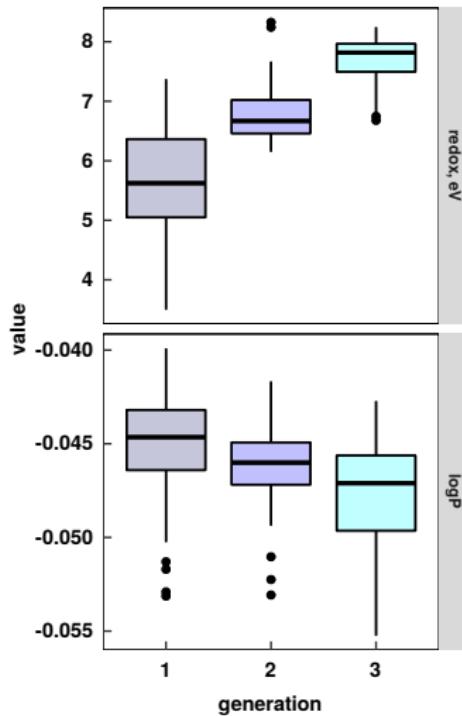
Case study conclusions

- EI framework provides high resolution in the region of interest (c.f. maximum uncertainty), converges quickly
- We are able to identify fruitful regions from large chemical spaces based on few DFT evaluations



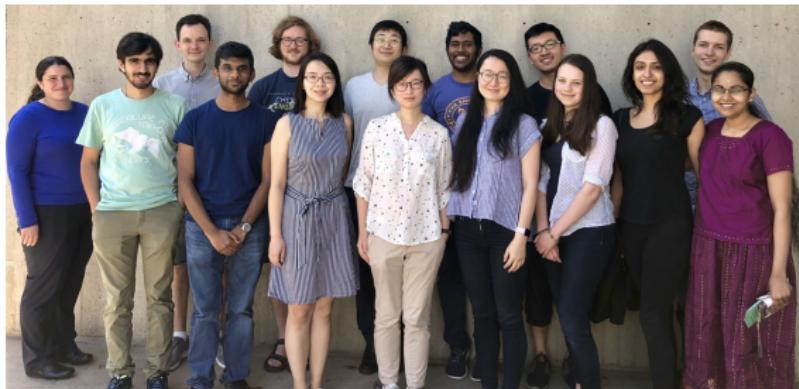
Case study conclusions

- EI framework provides high resolution in the region of interest (c.f. maximum uncertainty), converges quickly
- We are able to identify fruitful regions from large chemical spaces based on few DFT evaluations
- Multiobjective DFT optimization guided by data-driven method efficiency generates lead complexes



Acknowledgments

Thanks to the Kulik group and funding partners:



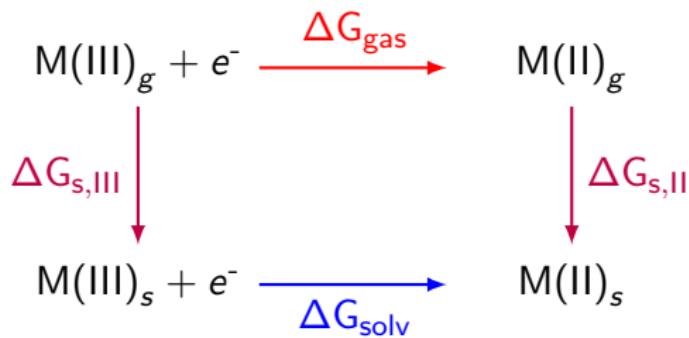
Thermodynamic cycle



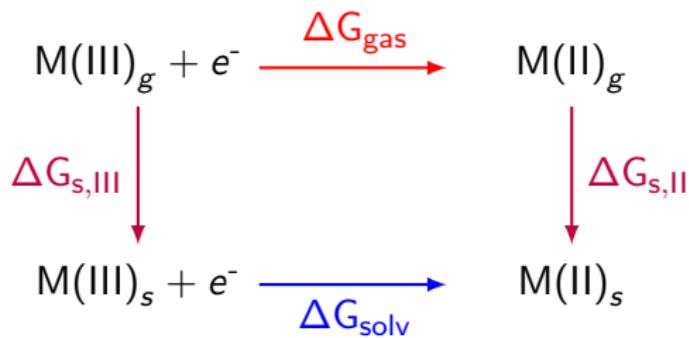
Thermodynamic cycle



Thermodynamic cycle

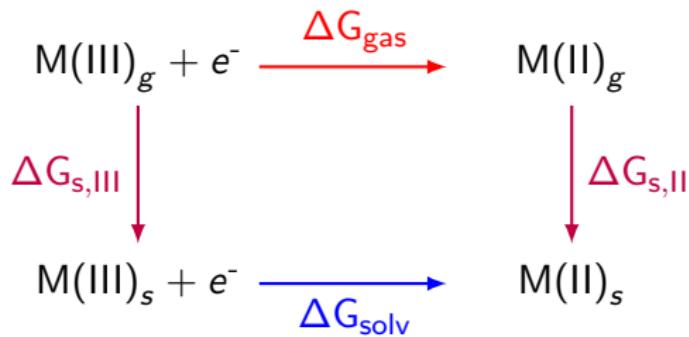


Thermodynamic cycle



$$\Delta G_{\text{solv}} = \Delta G_{\text{gas}} + \Delta \Delta G_s$$

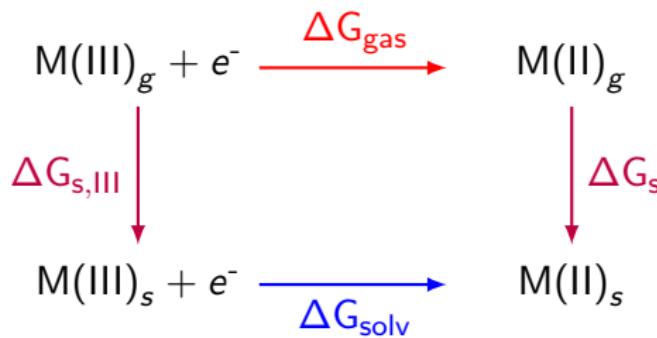
Thermodynamic cycle



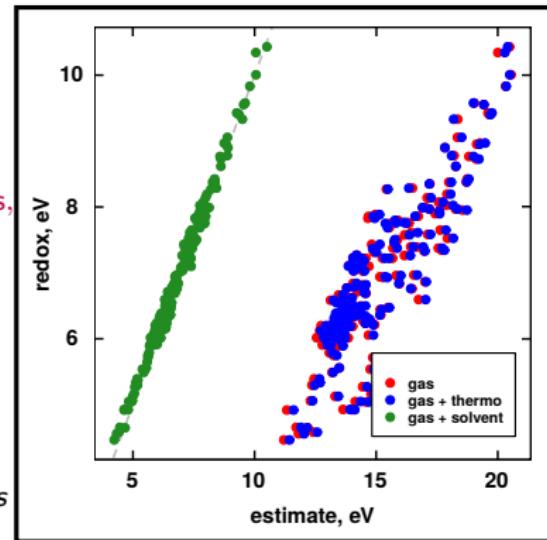
$$\Delta G_{\text{solv}} = \Delta G_{\text{gas}} + \Delta \Delta G_s$$

$$\approx \Delta E_{\text{gas},\text{III}-\text{II}} + \Delta \Delta G_s$$

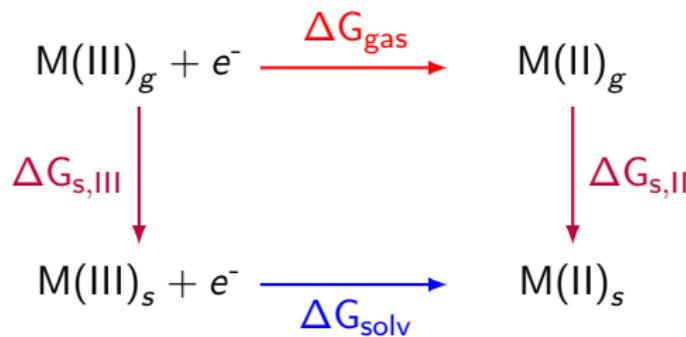
Thermodynamic cycle



$$\begin{aligned}\Delta G_{\text{solv}} &= \Delta G_{\text{gas}} + \Delta \Delta G_s \\ &\approx \Delta E_{\text{gas},\text{III}-\text{II}} + \Delta \Delta G_s\end{aligned}$$



Thermodynamic cycle



$$\Delta G_{\text{solv}} = \Delta G_{\text{gas}} + \Delta \Delta G_s$$

$$\approx \Delta E_{\text{gas},\text{III}-\text{II}} + \Delta \Delta G_s$$

$$\log P \approx \log \frac{\Delta G_{s,\text{II},\text{octanol}}}{\Delta G_{s,\text{II},\text{water}}}$$

- Spin state taken as the $M(II)$ ground state
- Need 3 geometry optimizations at minimum