

## **Problem 1:** Dynamic Arrays (Vectors)

Sample Input: *Two vectors, A and B*

Sample output:

Creating an empty array a...

Creating an array B with size 15, and initializing all values to 7...

Displaying array A: Array A is empty.

Displaying array B: 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7

Assigning the first 2 elements of A to 9...

Displaying array A: 9 9

Assigning the first 7 elements of B to 0...

Displaying array B: 0 0 0 0 0 0 0 7 7 7 7 7 7 7 7

Current size of array B: 15

Current number of elements in B: 15

Resizing B to 5...

Current size of array B: 5

Displaying array B: 0 0 0 0 0

Pushing back the number 88 to the array B

Inserting the value 44 at position 0...

Displaying array B: 44 0 0 0 0 0 88

Erasing the element at position 2...

The first element of B is 44

The last element of B is 88

Deleting the last element...

Displaying array B: 44 0 0 0 0

## **Problem 2: Queues**

### **Sample Input:**

Number of queues: 3

How many rounds would you like to run? 3

### **Sample Output:**

Round 1:

Numbers inputted into each queue: 3 4 10

Amount of data outputted from the system: 7

Size of queues after output:

q0.size(): 0

q1.size(): 0

q2.size(): 10

Round 2:

Numbers inputted into each queue: 7 3 1

Amount of data outputted from the system: 19

Size of queues after output:

q0.size(): 0

q1.size(): 0

q2.size(): 2

Round 3:

Numbers inputted into each queue: 9 1 6

Amount of data outputted from the system: 8

Size of queues after output:

q0.size(): 1

q1.size(): 1

q2.size(): 8

Average size of queues:

q0: 0.33333

q1: 0.33333

q2: 6.66667

The ratio between  $n_i$  and  $n$  should be that

$$n * 2 \geq \sum n_i$$

so that  $n_i$  doesn't start to increase uncontrollably. This makes sure  $n$  always dominates it.

### **Problem 3: Stacks**

#### **Sample Input:**

{8 6 4 1 1 7 1 4 1 3 7 1 4 4 4}

#### **Sample Output:**

Initial vector: 8 6 4 1 1 7 1 4 1 3 7 1 4 4 4

Sorted vector: 8 7 7 6 4 4 4 4 4 3 1 1 1 1 1

Stack 0: 8 1 1

Stack 1: 7 3

Stack 2: 7

Stack 3: 6 4

Stack 4: 4 4 1 1

Stack 5: 4 4 1

**Complexity of the function:**  $O(N \log N)$ , where  $N$  is the number of elements in the vector.

The complexities are from

- 1) The standard C++ sort function which has  $O(N \log N)$  complexity
- 2) A for loop that runs  $N$  times, in it a for loop that runs as many times as there exists stacks. In the worst-case scenario (if all elements of the vector were 10), this would amount to a  $O(N^2)$  complexity. But the actual run-time is way less than that and runs around  $O(N \log N)$ .

The total complexity becomes  $O(N \log N) + O(N \log N) = O(N \log N)$

## **Problem 4: Trees**

Sample Input: [TEXT FILE]

15

```
2 4 6 8 0 10 0 12 0 13 0 14 0 0 0
3 5 7 9 0 11 0 0 0 0 0 15 0 0 0
```

```
1 2 4 12 8 12 13 0
2 12 6 7 5 9 6 0
```

Sample Output:

```
1 and 2 are descendant-1
2 and 12 are descendant-3
4 and 6 are cousin2-2-1
12 and 7 are cousin4-2-1
8 and 5 are cousin2-1-2
12 and 9 are cousin2-1-4
13 and 6 are descendant-2
```

Complexity of the solution:

findPath() has a worst case of the node wanted being the last, i.e.  $O(n)$ , and an average case of  $O(\log N)$

findDirectRelation() uses an existing vector, and has an average/almost always complexity of  $O(\log N)$  (position of the node in the tree). The worst case is  $O(n)$  (When the two elements are the last two elements in the tree).

findCommonAncestor() also uses a vector, and has a worst case of  $O(\log N)$ , but can be way less than that. It really depends of where the ancestor is. The worst case is always less than  $O(n)$ .

**Total complexity:**

Average/Normal Case:  $O(\log N) + O(\log N) + O(\log N) = O(\log N)$

Worst Case:  $O(n)$

## **Problem 5: Sorting**

1) Sample Input: { 0,1,1,0,0,2,2,2,0,0,1,0,2,1 }

Sample output:

Initial array: 0 1 1 0 0 2 2 2 0 0 1 0 2 1

Sorted Array: 0 0 0 0 0 0 1 1 1 1 2 2 2 2

2) Sample Input: { 1,5,2,5,7,2,4,8,11,22,13,16,2,6,9,5,3,1 }

Sample Output: 1 1 2 2 2 3 4 5 5 5 6 7 8 9 11 13 16 22

Complexity: The complexity of the function is the complexity of passing once on each element of the input array  $\theta(n)$  and then, for each occurrence of the value  $0 \leq i < 27$  insert it in the output array. Since we have  $n$  elements, this only takes  $\theta(n)$  as well. The resulting complexity is  $\theta(2n)$ , or  $O(n)$ .

3a) Sample Input: { "cab", "bcd", "axz", "xwy", "mpo", "dcv" }

Sample Output: axz bcd cab dcv mpo xwy

Complexity: The complexity is identical to quicksort  $O(n \log n)$

3b) Sample Input: { "climate", "justify", "bracket", "fortune", "dignity", "routine", "unaware", "popular", "royalty", "paradox", "absence", "hostage", "factory", "abolish", "compose" }

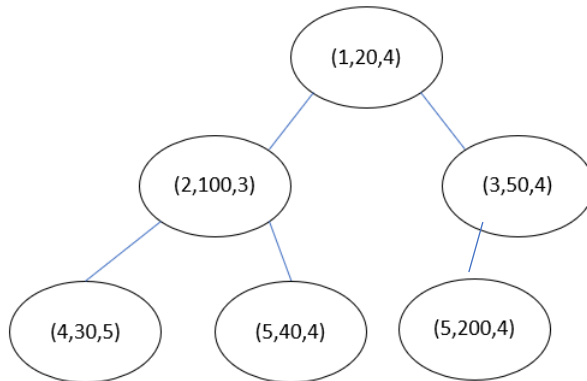
Sample Output: abolish absence bracket climate compose dignity factory fortune hostage justify paradox popular routine royalty unaware

Explanation/Reasoning: Radix sort is a sorting algorithm that repeatedly does a count sort based on the  $i$ -th digit in a number. We can modify that to count sort the  $i$ -th letter in a word. Moreover, it is even better because in normal radix sort you have to traverse the array once to get the maximum amount of digits, here we already know the fixed size  $m$ .

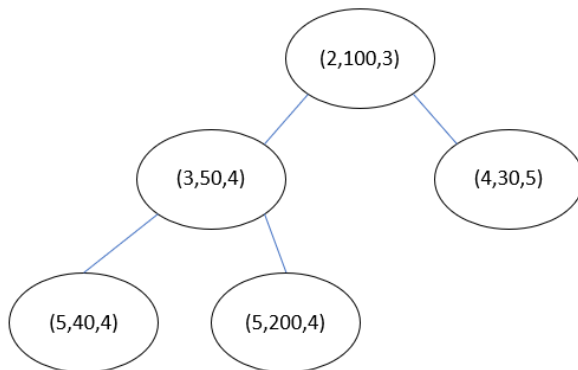
Complexity: The complexity of this radix sort is the complexity of doing count sort  $m$  times on  $n$  elements. One count sort on  $n$  elements is  $\theta(3n)$  or  $O(n)$ . So the total becomes  $m * \theta(3n) = \theta(3mn)$ , or  $m * O(n) = O(mn)$

## **Problem 6: Heaps**

Initial heap: (ordered by priority)



Heap after first task is done:



### **Sample Input/Output:**

Enter an id of a task: (20/30/40/50/100/200)

30

Your ID is: 30. The necessary time to print your task is: 14

### **Complexity of the function:**

The complexity of the function `calculateDuration()` is the complexity of the first loop (which runs until it finds the element desired in the array.). This has as a worst case a linear complexity of  $O(n)$  if it is the last element. Plus the complexity of the second loop, which visits all the elements of the array once ( $O(n)$ ). Hence the solution also has a complexity of  $O(n)$ .

## **Problem 7:** Hash Tables

### **Sample Input:**

[TEXT FILE] **dictionary.txt** :

glue qualify porter abandon driver oppose fountain quote loss morale  
bait stimulation

overall overeat wire produce way talkative dangerous land parameter

mail fur film name sanctuary end leader present stake retire fax

scheme attract cooperate be choice tense medal familiar news pocket

poison tap sum trip opinion reflect door take

[TEXT FILE] **paragraph.txt** :

glue constant module skate porter abandon tape slide detail fountain  
representative acute

prevent bait stimulation overall overeat wire produce deputy try agree

end accompany enter swallow fax scheme attract cooperate be choice

contrary news pocket conceive opinion reflect door take

### **Sample Output:**

constant

module

skate

tape

slide

detail

representative

acute

prevent

deputy

try

agree

accompany

enter

swallow

contrary

conceive

### **Complexity of the program:**

Insertion:  $O(n)$  (each insert is  $O(1)$ )

Output: to check if each word exists  $O(n)$ .

Total complexity:  $O(n)$