Examine results

I tested the 4 model variants on real ALSFRS data. Here I summarise some of the fit statistics for each model in turn. In each case the same data was used in long or wide format as needed. The data had 834 individuals, with a total of 3,311 longitudinal timepoints of 12 questions each. All models were run across 4 chains on 4 separate cores with the default warm-up and sampling iterations.

To recap the models were: - Model 1 - Multiple latent dimensions - Model 2 - Modeling questions separately - multivariate - Model 3 - Using continuation ratio - Model 4 - Using a custom family

Each model had the following numbers of parameters:

[1] "Model 1: 11387" ## [1] "Model 2: 10543"

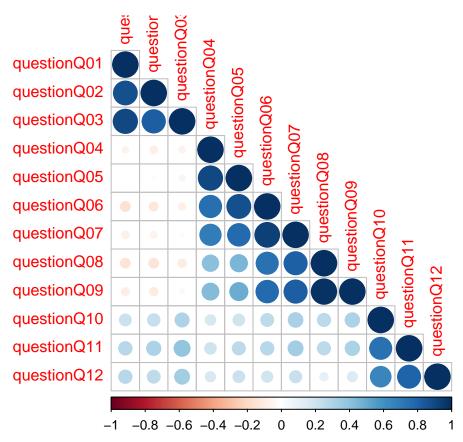
[1] "Model 4:"

```
## [1] "Model 3: 10521"
## [1] "Model 4: 10520"
and the following numbers of divergences:
## [1] "Model 1: 0"
## [1] "Model 2: 0"
## [1] "Model 3: 0"
## [1] "Model 4: 0"
The times for warmup and sampling for each chain of the models were:
## [1] "Model 1:"
##
             warmup sample
## chain:1 9811.56 9092.76
## chain:2 11060.30 7159.92
## chain:3 10605.00 8934.94
## chain:4 10828.40 4621.79
## [1] "Model 2:"
##
             warmup
                      sample
## chain:1 16890.50
                     3953.60
## chain:2 17234.10 41025.00
## chain:3 17194.00 4473.53
## chain:4 8102.01
                     5472.32
## [1] "Model 3:"
##
            warmup sample
## chain:1 21175.8 8673.85
## chain:2 30186.8 7764.63
## chain:3 53974.3 8212.70
## chain:4 22542.9 4482.03
```

```
## warmup sample
## chain:1 34091.0 14273.6
## chain:2 32847.6 14386.7
## chain:3 34468.0 14270.0
## chain:4 35844.6 14236.9
```

Model 1 correlation matrix

```
questionQ01 questionQ02 questionQ03 questionQ04 questionQ05
## questionQ01 " 1.0000"
                            " 0.8733"
                                         " 0.9001"
                                                      "-0.0639"
                                                                   "-0.0012"
## questionQ02 " 0.8733"
                            " 1.0000"
                                         " 0.8292"
                                                      "-0.0861"
                                                                   "-0.0148"
## questionQ03 " 0.9001"
                            " 0.8292"
                                         " 1.0000"
                                                      "-0.0689"
                                                                   " 0.0585"
                            "-0.0861"
## questionQ04 "-0.0639"
                                         "-0.0689"
                                                      " 1.0000"
                                                                   " 0.9025"
                            "-0.0148"
                                                                   " 1.0000"
## questionQ05 "-0.0012"
                                         " 0.0585"
                                                      " 0.9025"
## questionQ06 "-0.1517"
                            "-0.1219"
                                         "-0.0832"
                                                      " 0.7585"
                                                                   " 0.8752"
## questionQ07 "-0.0836"
                            "-0.0690"
                                         "-0.0246"
                                                      " 0.6917"
                                                                   " 0.7741"
## questionQ08 "-0.1469"
                            "-0.1447"
                                         "-0.1086"
                                                      " 0.4104"
                                                                   " 0.4526"
## questionQ09 "-0.0949"
                            "-0.1077"
                                         "-0.0373"
                                                      " 0.4368"
                                                                   " 0.4997"
                            " 0.2371"
                                                      " 0.1705"
## questionQ10 " 0.2175"
                                         " 0.3038"
                                                                   " 0.2095"
## questionQ11 " 0.2763"
                            " 0.3102"
                                         " 0.3910"
                                                      " 0.2061"
                                                                   " 0.2629"
## questionQ12 " 0.2724"
                            " 0.2568"
                                         " 0.3418"
                                                      " 0.1613"
                                                                   " 0.2104"
##
               questionQ06 questionQ07 questionQ08 questionQ09 questionQ10
## questionQ01 "-0.1517"
                            "-0.0836"
                                         "-0.1469"
                                                      "-0.0949"
                                                                   " 0.2175"
## questionQ02 "-0.1219"
                            "-0.0690"
                                         "-0.1447"
                                                      "-0.1077"
                                                                   " 0.2371"
## questionQ03 "-0.0832"
                            "-0.0246"
                                         "-0.1086"
                                                      "-0.0373"
                                                                   " 0.3038"
## questionQ04 " 0.7585"
                                         " 0.4104"
                            " 0.6917"
                                                      " 0.4368"
                                                                  " 0.1705"
## questionQ05 " 0.8752"
                            " 0.7741"
                                         " 0.4526"
                                                      " 0.4997"
                                                                   " 0.2095"
## questionQ06 " 1.0000"
                            " 0.9383"
                                         " 0.7499"
                                                      " 0.7750"
                                                                   " 0.2564"
## questionQ07 " 0.9383"
                            " 1.0000"
                                         " 0.8188"
                                                                   " 0.3277"
                                                      " 0.8217"
## questionQ08 " 0.7499"
                            " 0.8188"
                                                                   " 0.2687"
                                         " 1.0000"
                                                      " 0.9840"
## questionQ09 " 0.7750"
                            " 0.8217"
                                         " 0.9840"
                                                      " 1.0000"
                                                                   " 0.3174"
## questionQ10 " 0.2564"
                            " 0.3277"
                                         " 0.2687"
                                                      " 0.3174"
                                                                   " 1.0000"
## questionQ11 " 0.2716"
                            " 0.3418"
                                         " 0.2659"
                                                      " 0.3149"
                                                                    0.7459"
  questionQ12 " 0.1907"
                            " 0.2257"
                                         " 0.1088"
                                                      " 0.1520"
                                                                   " 0.6523"
##
               questionQ11 questionQ12
## questionQ01 " 0.2763"
                            " 0.2724"
## questionQ02 " 0.3102"
                            " 0.2568"
## questionQ03 " 0.3910"
                            " 0.3418"
## questionQ04 " 0.2061"
                            " 0.1613"
## questionQ05 " 0.2629"
                            " 0.2104"
## questionQ06 " 0.2716"
                            " 0.1907"
## questionQ07 " 0.3418"
                            " 0.2257"
## questionQ08 " 0.2659"
                            " 0.1088"
                            " 0.1520"
## questionQ09 " 0.3149"
## questionQ10 " 0.7459"
                            " 0.6523"
## questionQ11 " 1.0000"
                            " 0.8099"
## questionQ12 " 0.8099"
                            " 1.0000"
```



Model 2 correlation matrix

##		Q01_Intercept	Q02_Intercept	Q03_Intercept	Q04_Intercept
##	Q01_Intercept	"1.000"	"0.881"	"0.911"	"0.267"
##	Q02_Intercept	"0.881"	"1.000"	"0.848"	"0.179"
##	Q03_Intercept	"0.911"	"0.848"	"1.000"	"0.295"
##	Q04_Intercept	"0.267"	"0.179"	"0.295"	"1.000"
##	Q05_Intercept	"0.329"	"0.248"	"0.399"	"0.927"
##	Q06_Intercept	"0.219"	"0.161"	"0.288"	"0.829"
##	Q07_Intercept	"0.267"	"0.199"	"0.324"	"0.794"
##	Q08_Intercept	"0.175"	"0.104"	"0.210"	"0.581"
##	Q09_Intercept	"0.245"	"0.159"	"0.300"	"0.634"
##	Q10_Intercept	"0.415"	"0.378"	"0.485"	"0.424"
##	Q11_Intercept	"0.519"	"0.483"	"0.612"	"0.494"
##	Q12_Intercept	"0.506"	"0.431"	"0.570"	"0.454"
##		Q05_Intercept	Q06_Intercept	Q07_Intercept	Q08_Intercept
	Q01_Intercept		Q06_Intercept "0.219"	Q07_Intercept "0.267"	Q08_Intercept "0.175"
##	Q01_Intercept Q02_Intercept	"0.329"			
##		"0.329" "0.248"	"0.219"	"0.267"	"0.175"
## ## ##	${\tt Q02_Intercept}$	"0.329" "0.248" "0.399"	"0.219" "0.161"	"0.267" "0.199"	"0.175" "0.104"
## ## ## ##	Q02_Intercept Q03_Intercept	"0.329" "0.248" "0.399" "0.927"	"0.219" "0.161" "0.288"	"0.267" "0.199" "0.324"	"0.175" "0.104" "0.210"
## ## ## ##	Q02_Intercept Q03_Intercept Q04_Intercept	"0.329" "0.248" "0.399" "0.927" "1.000"	"0.219" "0.161" "0.288" "0.829"	"0.267" "0.199" "0.324" "0.794"	"0.175" "0.104" "0.210" "0.581"
## ## ## ## ##	Q02_Intercept Q03_Intercept Q04_Intercept Q05_Intercept	"0.329" "0.248" "0.399" "0.927" "1.000" "0.908"	"0.219" "0.161" "0.288" "0.829" "0.908"	"0.267" "0.199" "0.324" "0.794" "0.852"	"0.175" "0.104" "0.210" "0.581" "0.616"
## ## ## ## ##	Q02_Intercept Q03_Intercept Q04_Intercept Q05_Intercept Q06_Intercept	"0.329" "0.248" "0.399" "0.927" "1.000" "0.908" "0.852"	"0.219" "0.161" "0.288" "0.829" "0.908" "1.000"	"0.267" "0.199" "0.324" "0.794" "0.852" "0.946"	"0.175" "0.104" "0.210" "0.581" "0.616" "0.797"
## ## ## ## ## ##	Q02_Intercept Q03_Intercept Q04_Intercept Q05_Intercept Q06_Intercept Q07_Intercept	"0.329" "0.248" "0.399" "0.927" "1.000" "0.908" "0.852" "0.616"	"0.219" "0.161" "0.288" "0.829" "0.908" "1.000" "0.946"	"0.267" "0.199" "0.324" "0.794" "0.852" "0.946" "1.000"	"0.175" "0.104" "0.210" "0.581" "0.616" "0.797" "0.847"
## ## ## ## ## ##	Q02_Intercept Q03_Intercept Q04_Intercept Q05_Intercept Q06_Intercept Q07_Intercept Q08_Intercept	"0.329" "0.248" "0.399" "0.927" "1.000" "0.908" "0.852" "0.616" "0.689"	"0.219" "0.161" "0.288" "0.829" "0.908" "1.000" "0.946" "0.797"	"0.267" "0.199" "0.324" "0.794" "0.852" "0.946" "1.000" "0.847"	"0.175" "0.104" "0.210" "0.581" "0.616" "0.797" "0.847" "1.000"
## ## ## ## ## ## ##	Q02_Intercept Q03_Intercept Q04_Intercept Q05_Intercept Q06_Intercept Q07_Intercept Q08_Intercept Q09_Intercept	"0.329" "0.248" "0.399" "0.927" "1.000" "0.908" "0.852" "0.616" "0.689" "0.459"	"0.219" "0.161" "0.288" "0.829" "0.908" "1.000" "0.946" "0.797"	"0.267" "0.199" "0.324" "0.794" "0.852" "0.946" "1.000" "0.847"	"0.175" "0.104" "0.210" "0.581" "0.616" "0.797" "0.847" "1.000" "0.964"

```
##
                  Q09_Intercept Q10_Intercept Q11_Intercept Q12_Intercept
## Q01_Intercept "0.245"
                                  "0.415"
                                                 "0.519"
                                                                "0.506"
                                                 "0.483"
## Q02 Intercept "0.159"
                                  "0.378"
                                                                "0.431"
## Q03_Intercept "0.300"
                                  "0.485"
                                                 "0.612"
                                                                "0.570"
## Q04_Intercept "0.634"
                                  "0.424"
                                                 "0.494"
                                                                "0.454"
## Q05 Intercept "0.689"
                                  "0.459"
                                                 "0.547"
                                                                "0.505"
## Q06 Intercept "0.848"
                                  "0.474"
                                                 "0.534"
                                                                "0.477"
## Q07_Intercept "0.880"
                                  "0.532"
                                                 "0.587"
                                                                "0.506"
## Q08 Intercept "0.964"
                                  "0.437"
                                                 "0.489"
                                                                "0.392"
## Q09_Intercept "1.000"
                                  "0.503"
                                                 "0.557"
                                                                "0.453"
## Q10_Intercept "0.503"
                                  "1.000"
                                                 "0.851"
                                                                "0.756"
## Q11_Intercept "0.557"
                                 "0.851"
                                                 "1.000"
                                                                "0.896"
## Q12_Intercept "0.453"
                                  "0.756"
                                                 "0.896"
                                                                "1.000"
                               Intercept
Q01 Intercept
Q02_Intercept
                                        Q06_Intercept
Q03_Intercept
                                            Intercept
Q04_Intercept
Q05_Intercept
                      Q06_Intercept
                                                         Q10 Intercept
Q07_Intercept
Q08_Intercept
Q09_Intercept
Q10_Intercept
Q11_Intercept
Q12_Intercept
                -1
                    -0.8 -0.6 -0.4 -0.2
                                           0
                                               0.2
                                                    0.4
                                                          0.6
                                                               0.8
```

Model 3 correlation matrix

```
##
                Intercept questionQ02 questionQ03 questionQ04 questionQ05
                " 1.000"
                          "-0.402"
                                       "-0.432"
                                                                 "-0.676"
                                                    "-0.674"
## Intercept
## questionQ02 "-0.402"
                          " 1.000"
                                       " 0.387"
                                                    " 0.277"
                                                                 " 0.293"
                                       " 1.000"
## questionQ03 "-0.432"
                          " 0.387"
                                                    " 0.365"
                                                                 " 0.444"
## questionQ04 "-0.674"
                          " 0.277"
                                       " 0.365"
                                                    " 1.000"
                                                                 " 0.959"
## questionQ05 "-0.676"
                          " 0.293"
                                       " 0.444"
                                                    " 0.959"
                                                                 " 1.000"
  questionQ06 "-0.741"
                          " 0.342"
                                       " 0.448"
                                                    " 0.901"
                                                                 " 0.949"
                          " 0.344"
                                       " 0.444"
## questionQ07 "-0.761"
                                                    " 0.879"
                                                                 " 0.912"
## questionQ08 "-0.744"
                          " 0.301"
                                       " 0.384"
                                                    " 0.756"
                                                                 " 0.778"
## questionQ09 "-0.767"
                          " 0.311"
                                       " 0.431"
                                                    " 0.787"
                                                                 " 0.817"
## questionQ10 "-0.666"
                          " 0.357"
                                       " 0.498"
                                                    " 0.668"
                                                                 " 0.679"
                          " 0.385"
                                       " 0.558"
                                                    " 0.695"
                                                                 " 0.712"
## questionQ11 "-0.665"
```

```
## questionQ12 "-0.628" " 0.304"
                                        " 0.488"
                                                     " 0.634"
                                                                   " 0.654"
##
                questionQ06 questionQ07 questionQ08 questionQ09 questionQ10
                "-0.741"
## Intercept
                             "-0.761"
                                          "-0.744"
                                                       "-0.767"
                                                                     "-0.666"
  questionQ02 " 0.342"
                             " 0.344"
                                          " 0.301"
                                                       " 0.311"
                                                                     " 0.357"
## questionQ03 " 0.448"
                             " 0.444"
                                          " 0.384"
                                                       " 0.431"
                                                                     " 0.498"
  questionQ04 " 0.901"
                             " 0.879"
                                          " 0.756"
                                                       " 0.787"
                                                                     " 0.668"
## questionQ05 " 0.949"
                             " 0.912"
                                          " 0.778"
                                                       " 0.817"
                                                                     " 0.679"
   questionQ06 " 1.000"
                             " 0.975"
                                          " 0.897"
                                                         0.925"
                                                                     " 0.735"
   questionQ07 " 0.975"
                             " 1.000"
                                          " 0.925"
                                                         0.945"
                                                                       0.763"
   questionQ08 " 0.897"
                             " 0.925"
                                            1.000"
                                                         0.984"
                                                                       0.710"
  questionQ09 " 0.925"
                             " 0.945"
                                          " 0.984"
                                                         1.000"
                                                                     " 0.749"
   questionQ10 " 0.735"
                             " 0.763"
                                          " 0.710"
                                                         0.749"
                                                                     " 1.000"
                             " 0.781"
                                          " 0.729"
                                                        " 0.763"
                                                                      0.915"
   questionQ11 " 0.755"
                             " 0.702"
   questionQ12 " 0.691"
                                          " 0.640"
                                                       " 0.670"
                                                                     " 0.849"
##
                questionQ11 questionQ12
## Intercept
                "-0.665"
                             "-0.628"
   questionQ02 " 0.385"
                             " 0.304"
  questionQ03 " 0.558"
                             " 0.488"
  questionQ04 " 0.695"
                             " 0.634"
## questionQ05 " 0.712"
                             " 0.654"
## questionQ06 " 0.755"
                             " 0.691"
## questionQ07 " 0.781"
                             " 0.702"
## questionQ08 " 0.729"
                             " 0.640"
   questionQ09 " 0.763"
                             " 0.670"
## questionQ10 " 0.915"
                             " 0.849"
## questionQ11 " 1.000"
                             " 0.918"
                             " 1.000"
## questionQ12 " 0.918"
                         questionQ0
    Intercept
                                  questionQ05
questionQ02
                                      questionQ06
questionQ03
                                           questionQ07
questionQ04
                                               questionQ08
questionQ05
                                                    questionQ09
questionQ06
                                                        questionQ10
questionQ07
                                                             questionQ11
questionQ08
questionQ09
questionQ10
questionQ11
questionQ12
                  -0.8 -0.6 -0.4 -0.2
                                         0
                                              0.2
                                                   0.4
                                                        0.6
                                                              8.0
```

Model 4 correlation matrix

```
##
               Intercept questionQ02 questionQ03 questionQ04 questionQ05
## Intercept
               " 1.000"
                          "-0.407"
                                       "-0.408"
                                                    "-0.660"
                                                                "-0.653"
## questionQ02 "-0.407"
                          " 1.000"
                                       " 0.385"
                                                    " 0.281"
                                                                " 0.291"
## questionQ03 "-0.408"
                          " 0.385"
                                       " 1.000"
                                                    " 0.360"
                                                                " 0.438"
                          " 0.281"
                                       " 0.360"
                                                                " 0.954"
## questionQ04 "-0.660"
                                                    " 1.000"
## questionQ05 "-0.653"
                          " 0.291"
                                       " 0.438"
                                                    " 0.954"
                                                                " 1.000"
## questionQ06 "-0.726"
                          " 0.341"
                                       " 0.433"
                                                    " 0.897"
                                                                " 0.944"
## questionQ07 "-0.744"
                          " 0.341"
                                       " 0.429"
                                                    " 0.876"
                                                                " 0.906"
## questionQ08 "-0.732"
                                       " 0.369"
                                                                " 0.769"
                          " 0.307"
                                                    " 0.754"
## questionQ09 "-0.750"
                          " 0.309"
                                       " 0.416"
                                                    " 0.783"
                                                                " 0.808"
                                       " 0.483"
## questionQ10 "-0.651"
                          " 0.360"
                                                    " 0.666"
                                                                " 0.672"
## questionQ11 "-0.640"
                          " 0.388"
                                       " 0.540"
                                                    " 0.682"
                                                                " 0.696"
  questionQ12 "-0.605"
                          " 0.305"
                                       " 0.473"
                                                    " 0.625"
                                                                " 0.640"
##
               questionQ06 questionQ07 questionQ08 questionQ09 questionQ10
               "-0.726"
                            "-0.744"
                                         "-0.732"
                                                      "-0.750"
                                                                   "-0.651"
## Intercept
## questionQ02 " 0.341"
                            " 0.341"
                                         " 0.307"
                                                                   " 0.360"
                                                      " 0.309"
## questionQ03 " 0.433"
                            " 0.429"
                                         " 0.369"
                                                      " 0.416"
                                                                   " 0.483"
## questionQ04 " 0.897"
                            " 0.876"
                                         " 0.754"
                                                      " 0.783"
                                                                   " 0.666"
## questionQ05 " 0.944"
                            " 0.906"
                                         " 0.769"
                                                      " 0.808"
                                                                   " 0.672"
                            " 0.973"
## questionQ06 " 1.000"
                                         " 0.894"
                                                      " 0.922"
                                                                  " 0.732"
## questionQ07 " 0.973"
                            " 1.000"
                                         " 0.923"
                                                      " 0.940"
                                                                   " 0.760"
## questionQ08 " 0.894"
                            " 0.923"
                                         " 1.000"
                                                      " 0.984"
                                                                   " 0.710"
## questionQ09 " 0.922"
                            " 0.940"
                                         " 0.984"
                                                      " 1.000"
                                                                   " 0.744"
## questionQ10 " 0.732"
                                                                   " 1.000"
                            " 0.760"
                                         " 0.710"
                                                      " 0.744"
## questionQ11 " 0.743"
                                                      " 0.751"
                            " 0.767"
                                         " 0.719"
                                                                   " 0.910"
## questionQ12 " 0.678"
                            " 0.690"
                                         " 0.629"
                                                      " 0.658"
                                                                   " 0.840"
##
               questionQ11 questionQ12
               "-0.640"
                            "-0.605"
## Intercept
                            " 0.305"
## questionQ02 " 0.388"
## questionQ03 " 0.540"
                            " 0.473"
## questionQ04 " 0.682"
                            " 0.625"
## questionQ05 " 0.696"
                            " 0.640"
## questionQ06 " 0.743"
                            " 0.678"
## questionQ07 " 0.767"
                            " 0.690"
## questionQ08 " 0.719"
                            " 0.629"
## questionQ09 " 0.751"
                            " 0.658"
## questionQ10 " 0.910"
                            " 0.840"
## questionQ11 " 1.000"
                            " 0.920"
## questionQ12 " 0.920"
                            " 1.000"
```

