

Optimizers Demo

SGD, Momentum, Adam, AdamW

From-scratch NumPy implementations

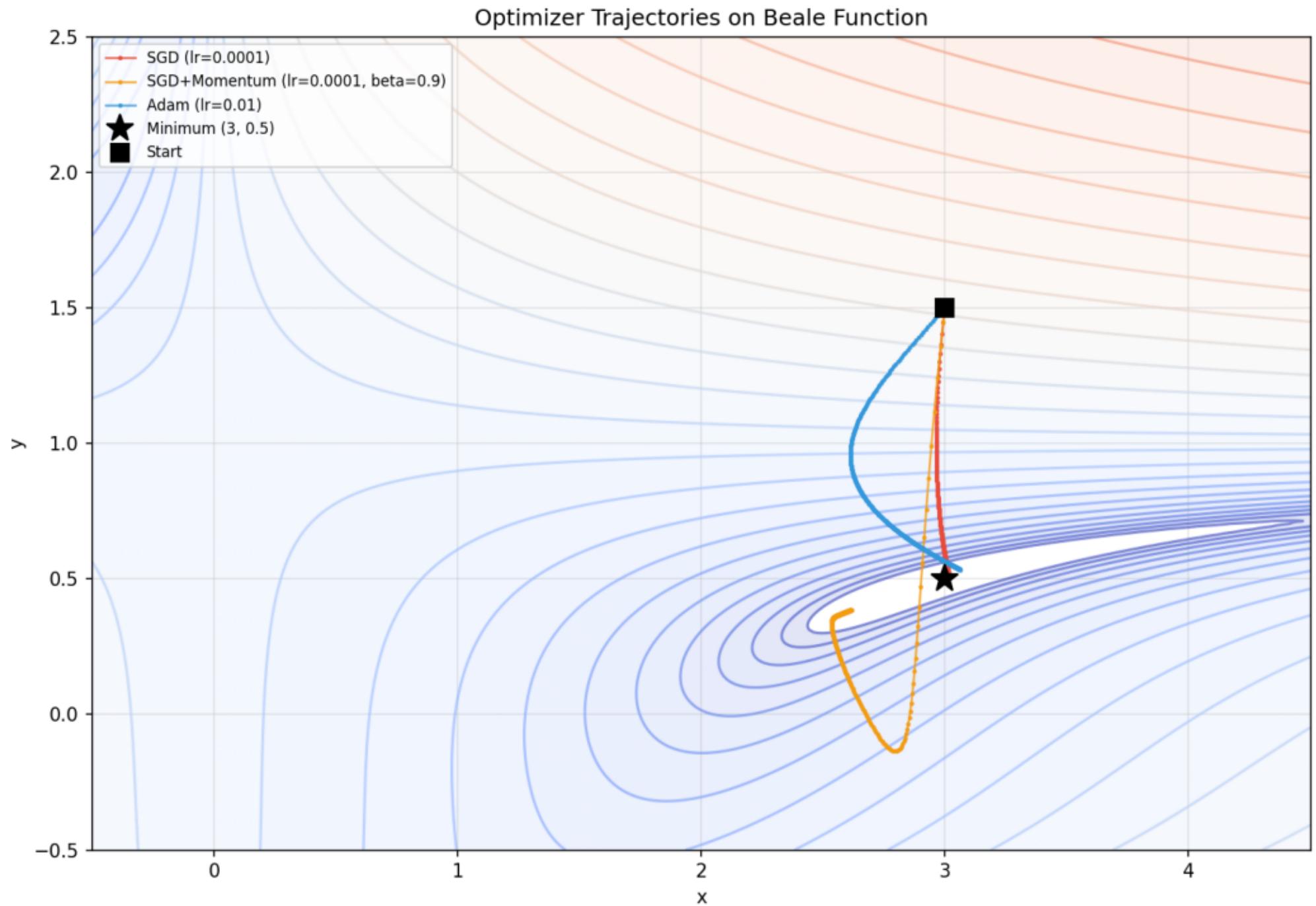
This report demonstrates optimizer behavior through 7 examples:

1. Optimizer trajectories on Beale function (2D contour)
2. Adam convergence on a quadratic (loss curve + trajectory)
3. Adam vs AdamW vs Adam+L2 weight distributions
4. Learning rate schedules (warmup+cosine, cosine, step decay)
5. Momentum effect in a ravine (SGD vs Momentum vs Nesterov)
6. Ill-conditioned quadratic (condition number = 100)
7. Bias correction effect in early Adam steps

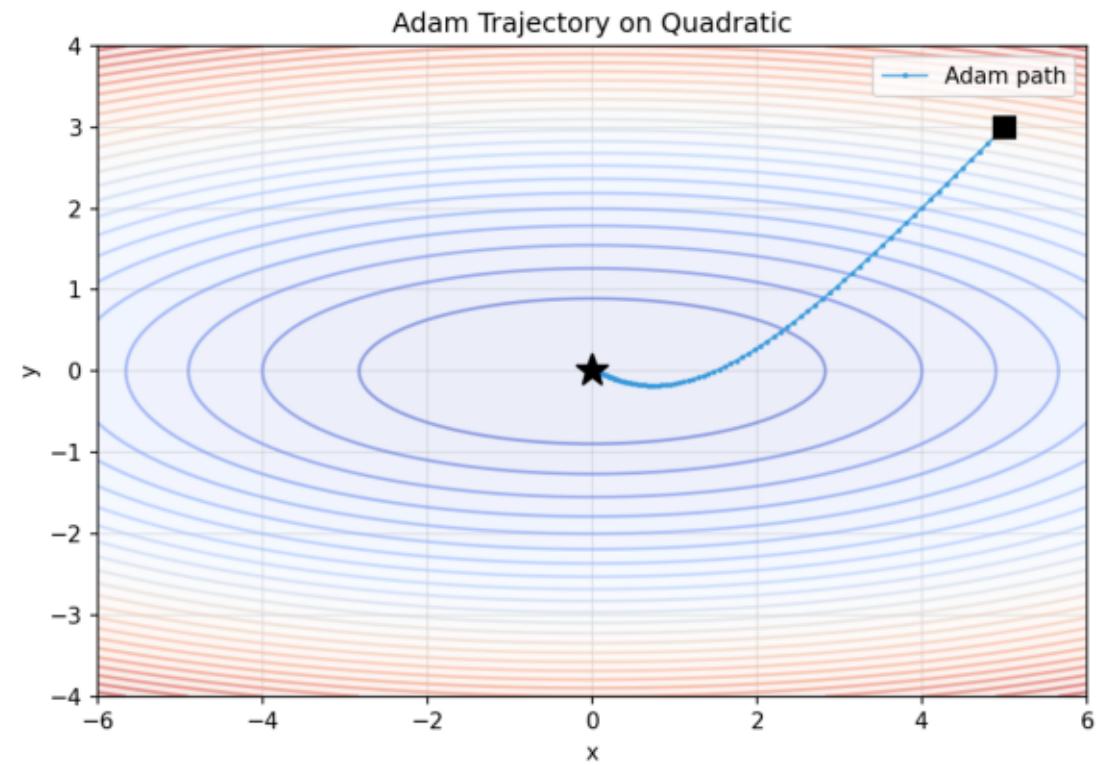
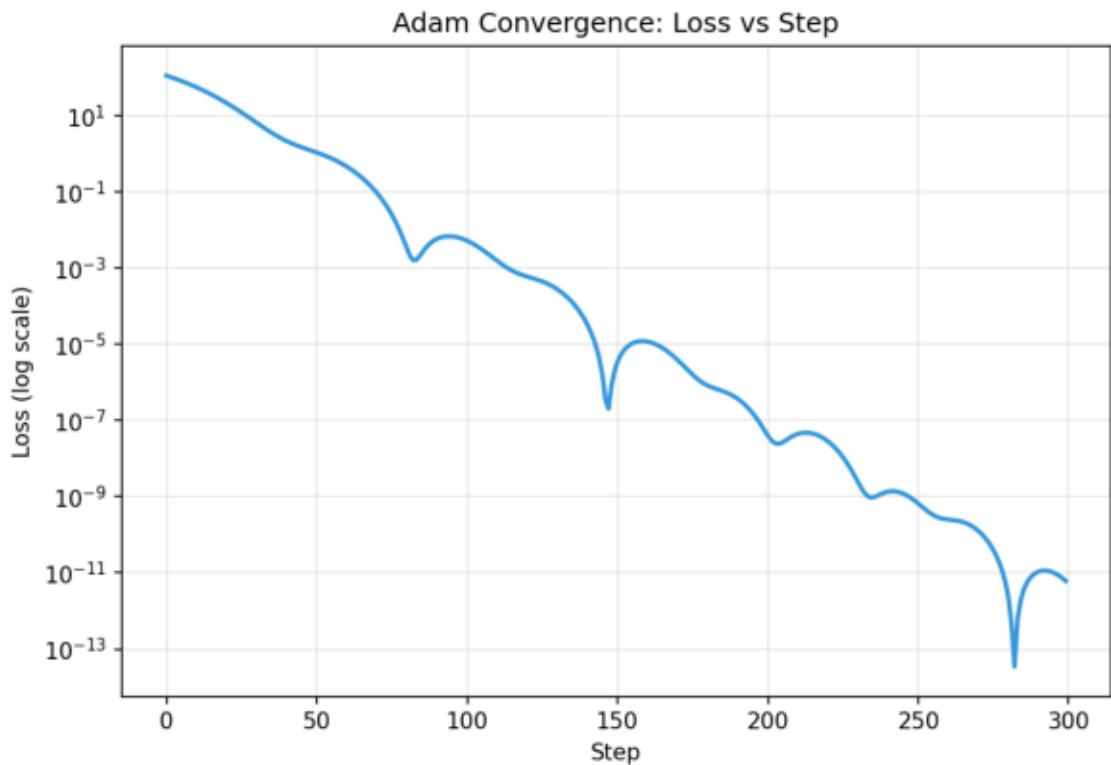
Key Findings

1. SGD struggles on non-convex and ill-conditioned problems due to oscillation.
2. Momentum dampens oscillations by accumulating velocity in consistent gradient directions.
3. Nesterov momentum provides slightly faster convergence via lookahead gradient evaluation.
4. Adam adapts per-parameter learning rates, handling diverse gradient scales automatically.
5. AdamW applies weight decay directly to parameters (decoupled), producing tighter weight distributions.
6. Adam+L2 folds weight decay into gradients (coupled), resulting in non-uniform effective regularization.
7. Bias correction is critical in early training steps -- without it, moment estimates are biased toward zero.
8. Warmup + cosine decay is the standard LR schedule for LLM training (GPT, LLaMA, Mistral).

01 Beale Trajectories



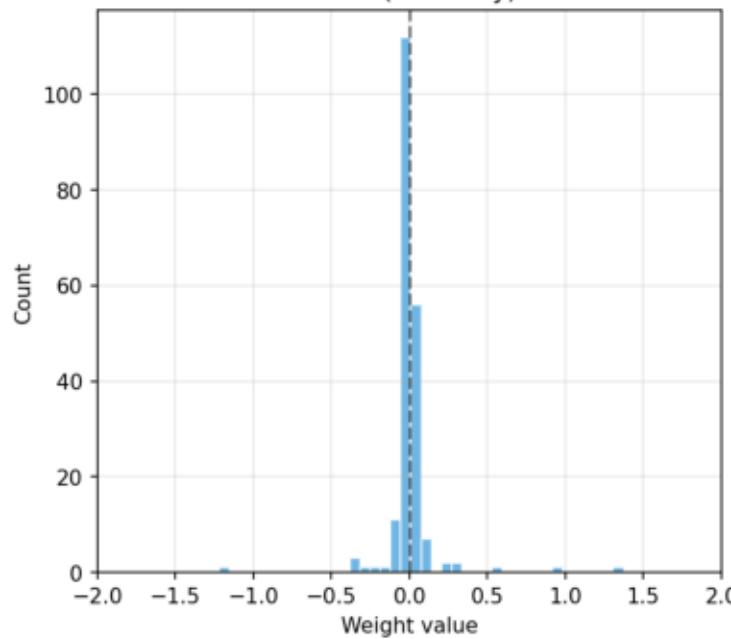
02 Adam Quadratic



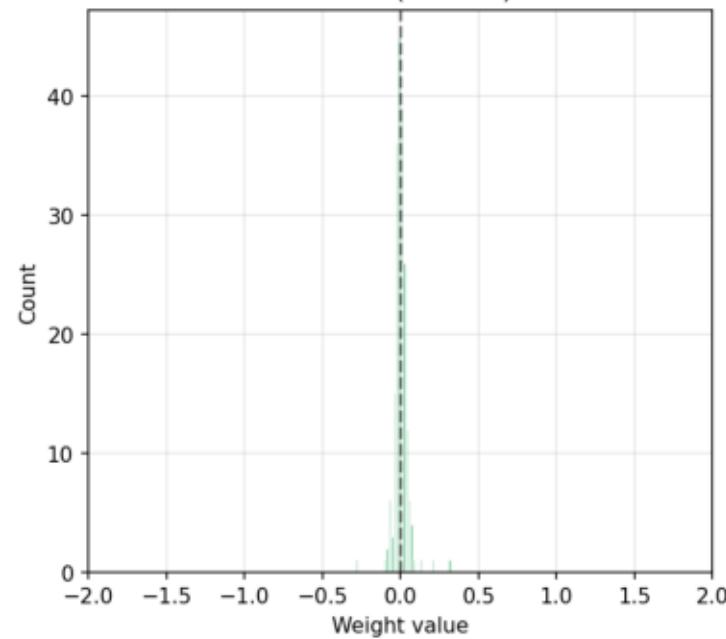
03 Adam Vs Adamw Weights

Weight Distributions After 1000 Steps of Noisy Gradient Descent

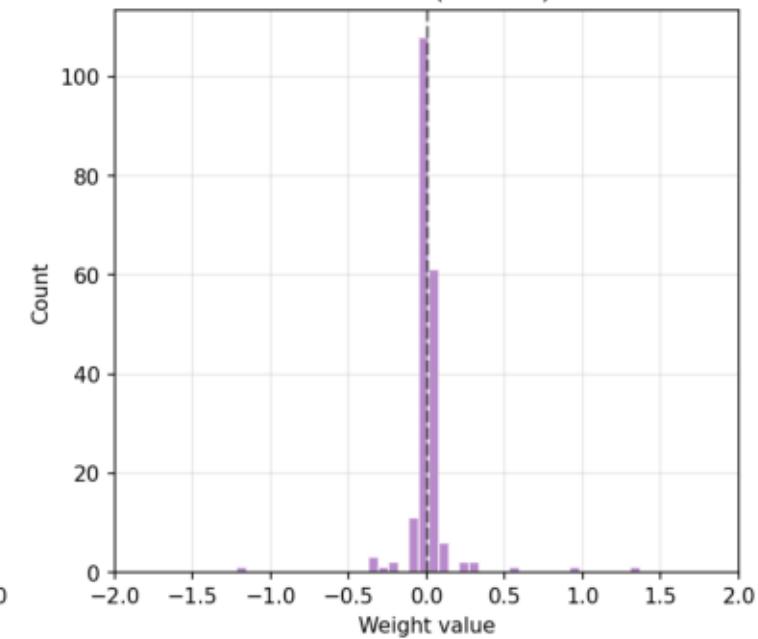
Adam (no decay)



AdamW (wd=0.1)

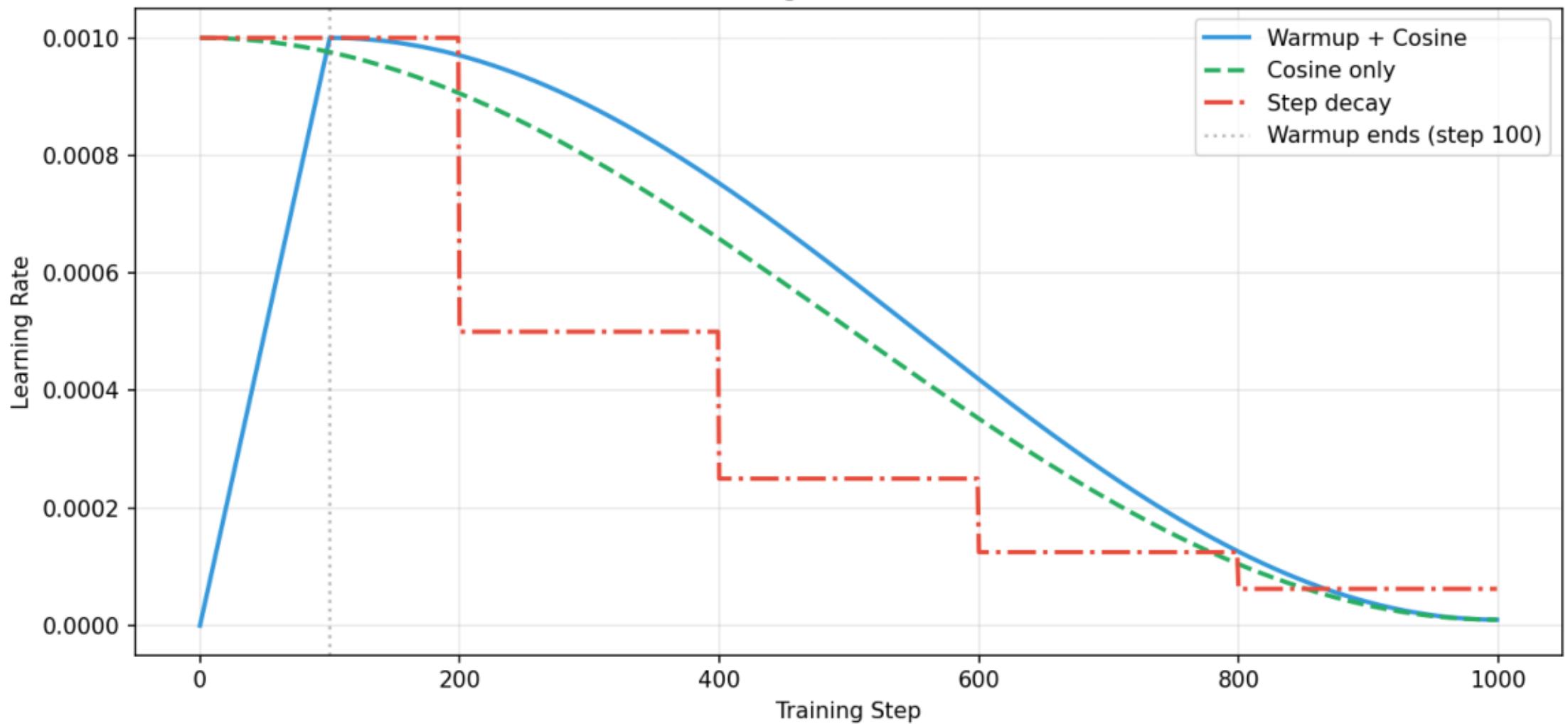


Adam+L2 (wd=0.1)



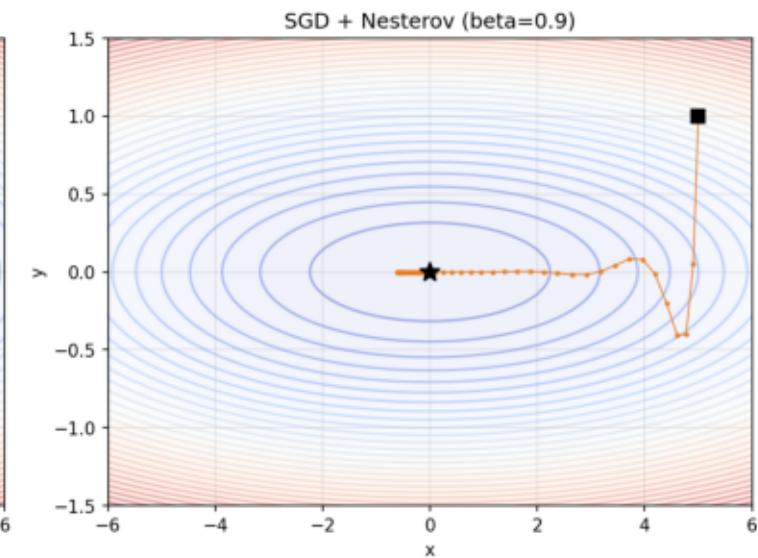
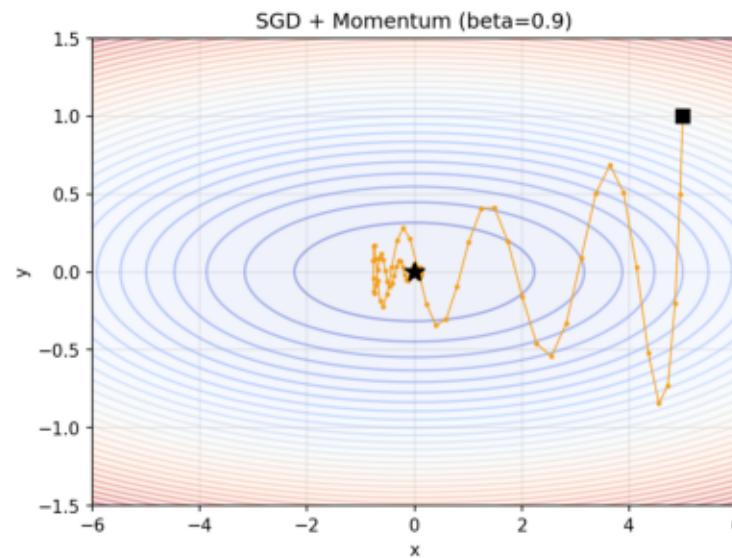
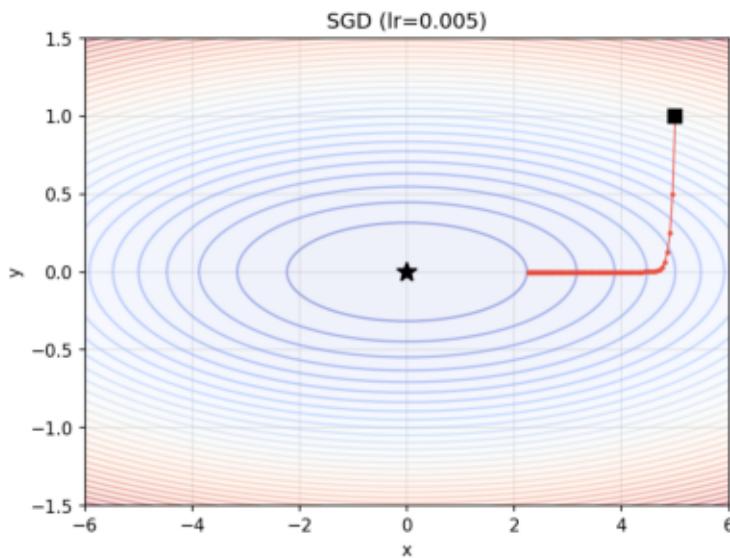
04 Lr Schedules

Learning Rate Schedules

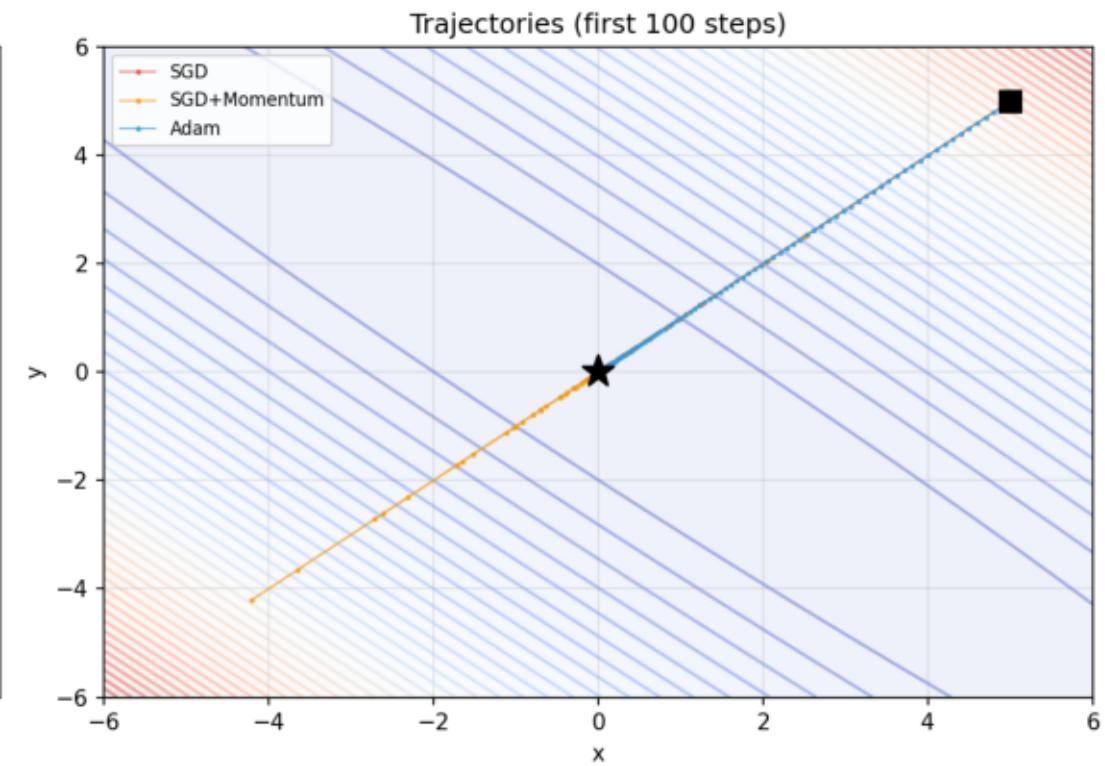
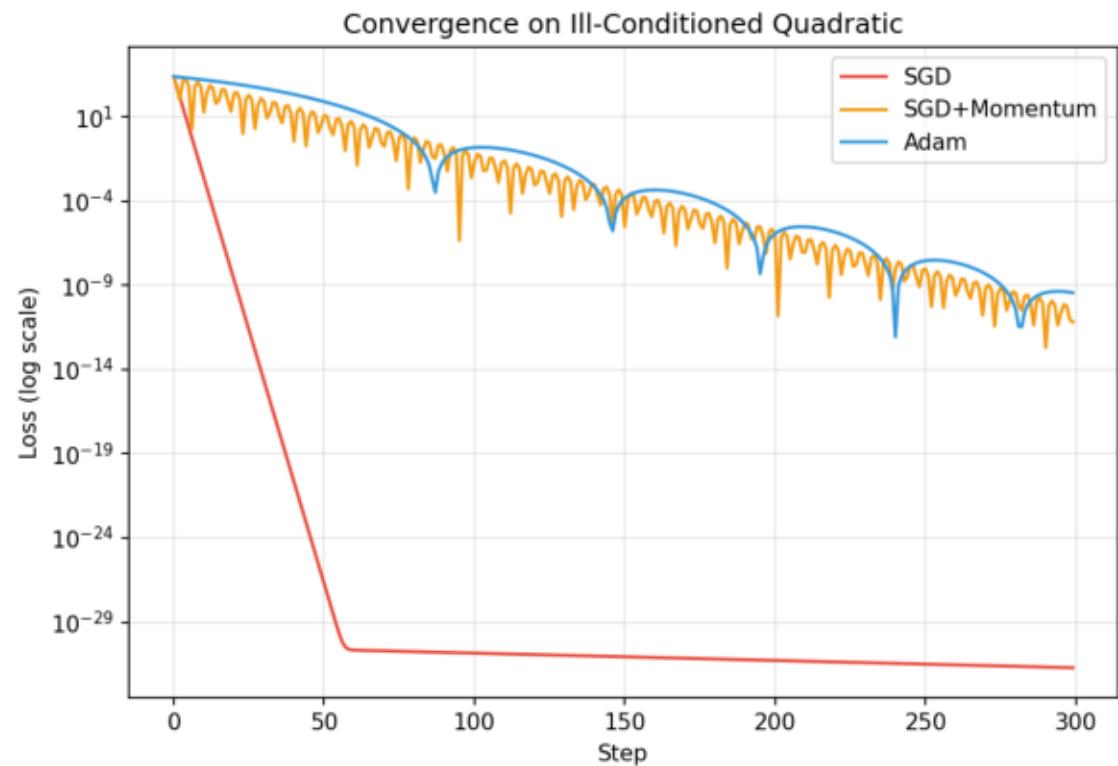


05 Momentum Ravine

Ravine Optimization: $f(x,y) = x^2 + 50y^2$

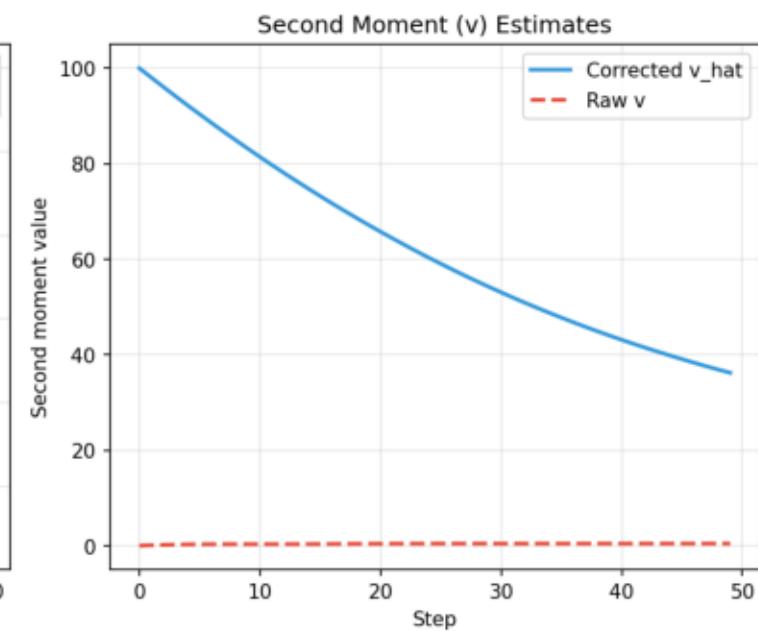
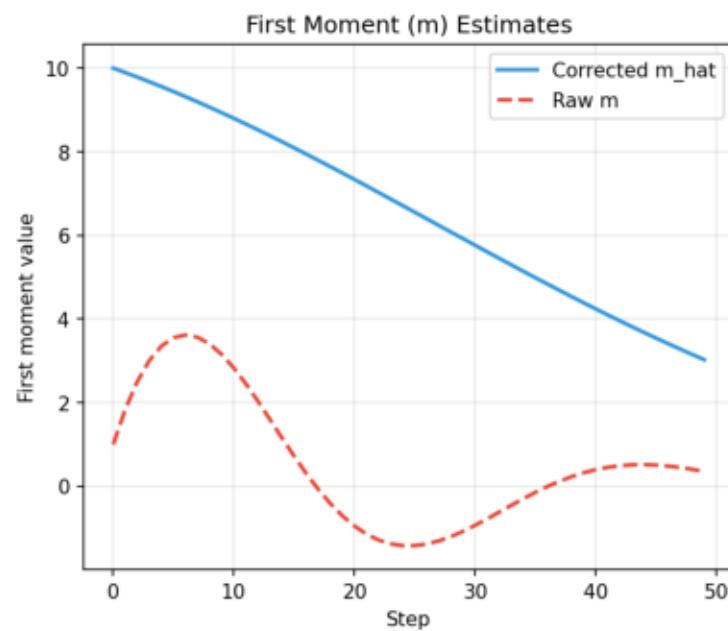
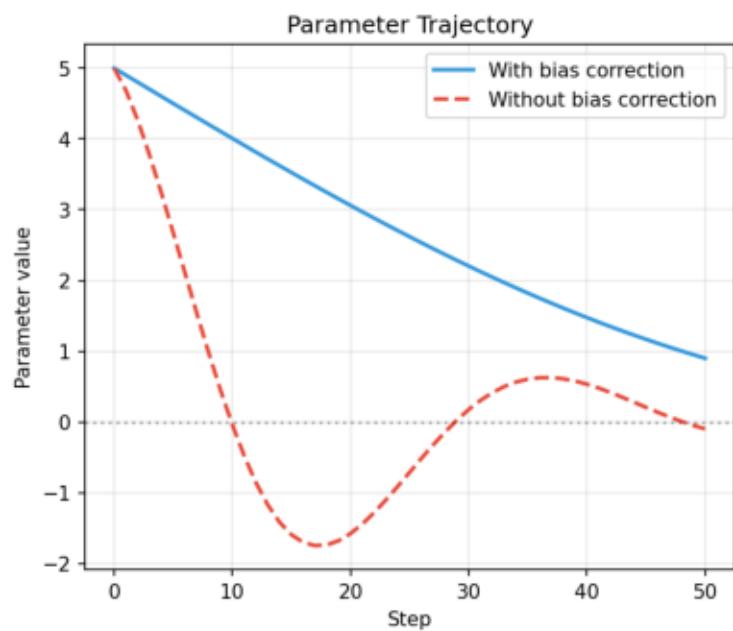


06 Illconditioned Quadratic



07 Bias Correction

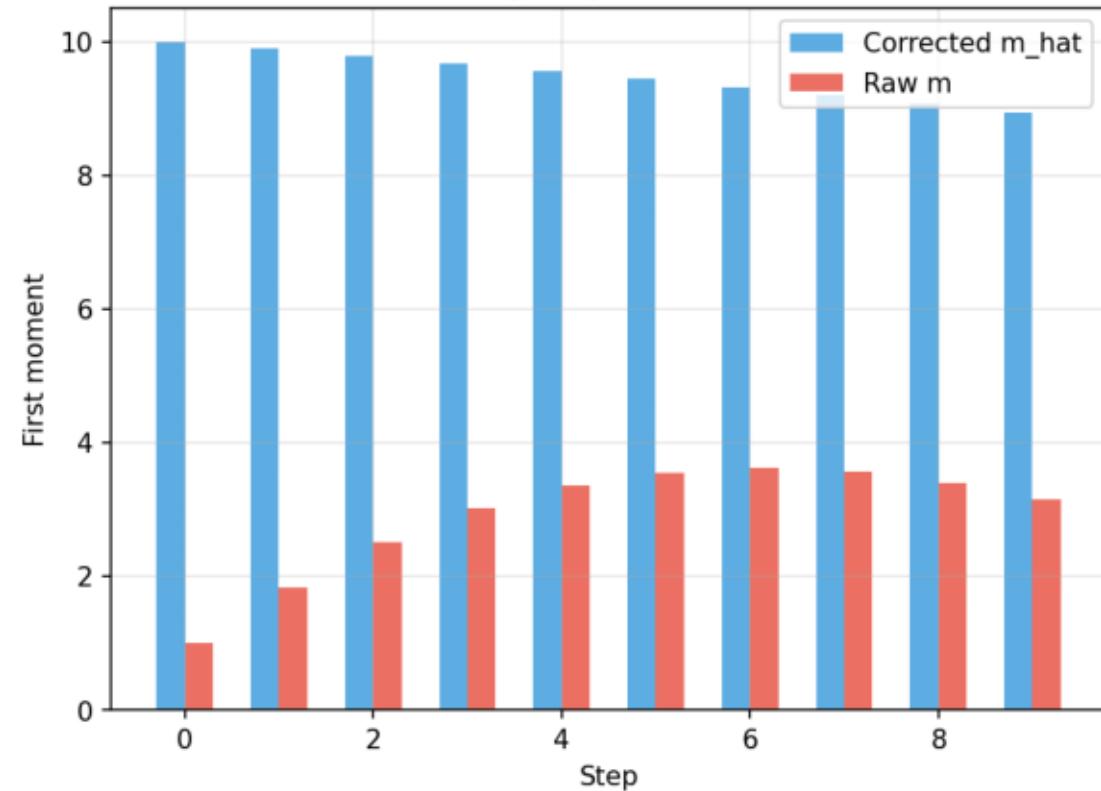
Effect of Bias Correction in Adam (first 50 steps)



07B Bias Correction Zoom

Bias Correction Zoomed: Steps 0-9

First Moment: Early Steps (bias correction effect)



Second Moment: Early Steps (bias correction effect)

