

# Architecture for a High Speed SAR ADC

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## Problem Definition

Derive a topology that will minimize power while achieving 12 bits of resolution and 200MSPS speed . Make topology amenable for future interleaving that can improve speed.

## Problem Analysis

We are given an input  $x \in [-1, 1]$  and converter tries to find  $K$  such that

$$-1 + K\Delta \leq x \leq -1 + (K + 1)\Delta.$$

If input is uniformly distributed then the problem will require a minimum  $N = \log_2(2/\Delta)$  “Yes or No” questions with precise answers. From a circuit perspective “Yes or No” is that of a comparator comparing input with a threshold with infinite precision. If the comparison has finite precision i.e it is unreliable for  $|inp| < \epsilon$  then at the end of  $N$  questions input can be as far as  $\epsilon$  away from the said range.

A typical SAR ADC conversion proceeds as follows . We compare the input with a threshold  $V_{th}(k) = r(k) * (x_{max}(k) + x_{min}(k)) + \epsilon(k)$  where it's guaranteed by previous knowledge that  $x \in [x_{max}(k), x_{min}(k)]$ . At the end of comparison the input is guaranteed to be in  $[x_{max}(k), V_{th}(k)]$  or  $[x_{min}(k), V_{th}(k)]$  so by setting  $x_{max}(k+1)$  and  $x_{min}(k+1)$  accordingly we can guarantee that range in which input can lie  $S(k+1) = x_{max}(k+1) - x_{min}(k+1) < S(k)$  provided that we put the thresholds  $V_{th}(k) \in [x_{max}(k), x_{min}(k)]$  . This by iteration can guarantee that we can locate input to a finite precision in required number of steps.

## Sampling Circuit

Noise power due to Differential sampling referred to input

$$P_{noise} = 2 * \frac{KT}{C_s} * \frac{Cs + Cp}{Cs}$$

where  $Cs$  = sampling cap and  $Cp$  = parasitic cap on top-plate , assuming top plate switch is limiting bandwidth and contributing most of noise compared to bottom plate switch . This is a reasonable assumption as every attempt will be made to minimize the top plate switch to reduce charge injection offset. Input referred SNR assuming differential swing of  $\pm V_{REF}$

$$SNR = V_{REF}^2 / 2 * P_{noise}$$

Assuming a shrink of .8 and  $V_{REF} = 0.9$ , for a noise performance equaling 12 bit quantization noise

$$P_{noise} = \Delta^2 / 12$$

$$Cs = 600fF$$

## Clocked Comparator

In a latched comparator  $V_{in} * e^{t/\tau} = VDD$ . For a minimum resolution input  $V_\delta$  it will need a time  $T_\delta = \tau * \ln(VDD/V_\delta)$ . Input greater than  $V_\delta$  needs time less than  $T_\delta$ . An asynchronous ADC uses this fact for optimization by making every comparison time just enough to make accurate decision by checking output differential level against VDD or timing out after  $T_{max}$ . Hence

$$T_{cmp} = \tau * \ln(VDD/V_{in}).$$

This makes the conversion time input dependant and the worst case comparison time =  $N^2/2 * \tau * \ln(2)$  is a two fold improvement in comparison time. But power saving may be significantly higher if actives are powered down after conversion and negligible if all power is dynamic. For a latch  $\tau = Gm/C = \beta * \sqrt{w}/C_{oxl} * W + C_{load}$ . If offset is non critical (SAR) or calibrated (multibit) no optimization is possible in this end. At higher precision ( $V_\delta = 10mV = 8bit$ ) noise (thermal/capacitive coupling noise  $\propto \frac{1}{C}$ ) from this may become critical and a switch from a noisy to low noise latch may be required. This will increase W and hence  $\tau$ .

A Way to improve the comparison time from  $O(N^2)$  to  $O(N)$  will be to add gain stages in front of the Clocked comparator to the tune of  $2^k$  for  $k^{th}$  comparison. This will make comparison time constant for all clocks making comparison time  $N * \tau * \ln(2)$ . But this will add to settling portion of conversion time and will be a trade off. This will automatically improve noise performance w.r.t clocked comparator.

Another option is to add a pipelined clocked comparator to the first one but not wait for it. So output of second latch will be  $V_{in} * e^{(t1+t2)/\tau}$  making its resolution better. If decision of first and second latch are different it means previous decision was wrong and has to be corrected. It also means that next bit is immaterial and has to be opposite to correct decision. For example if input is 33 current dac level is 32 since input is very small coarse latch gave default value of 0 instead of correct value of 1 and fine latch gave 1 the correct value. Since conversion is allowed to proceed next threshold used will be 16 and output will be definitely 1 but instead of applying it we applying fine comparator output and its complement 3rd dac threshold 40 instead of 24 which is more precise and in correct range. This doesn't improve the performance in terms of  $O(.)$ . However since comparator need be only as precise as the next step we will need comparison time of  $N(N+1)/2$  instead of  $(N+K)*(N+K+1)/2$  allowed by redundancy. In the absence of redundancy this is very significant. The following comparator topology is proposed for implementing either of these schemes

DAC(1)	{C,F}	DAC(2)	{C,F}	DAC(3)
			{1,1}	56
			{0,1}	40
			{0,0}	24
	{1,x}	48		
32				
	{0,x}	16	{0,1}	40
			{1,0}	24
			{0,0}	8

Figure 1: Code convergence

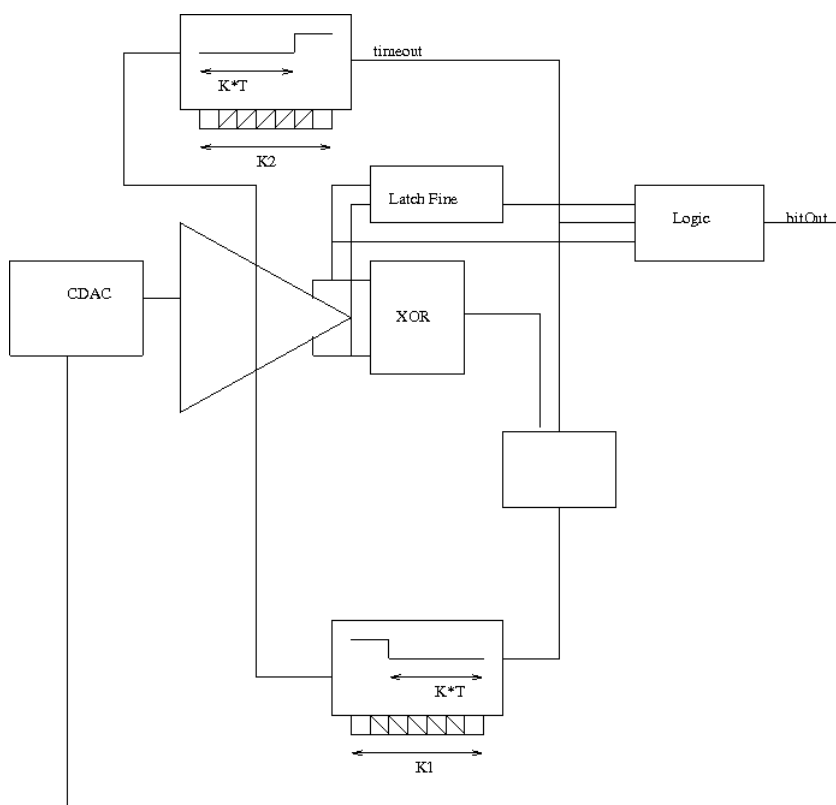


Figure 2: scheme

## Non binary SAR

In a SAR ADC without any redundancy  $k_{th}$  DAC step  $S(k)$  needs to settle to  $1LSB = VREF/2^N$  for ADC to converge correctly. In a constant clock environment this requires a time  $T_{dac} = \tau * N * \ln(2)$  corresponding to worst case first step and hence a total DAC time of  $\tau * N^2 * \ln(2)$ . If each DAC step gets a settling time just enough to meet the settling requirement then  $T_{dac}(k) = \tau * (N - k) * \ln(2)$  and total dac time will be  $\tau * N(N - 1)/2 * \ln(2)$ . To make  $T_{DAC}$  a constant we need redundancy propotional to current step so that an error  $S(k) * e^{-T_{dac}/\tau}$  can be tolerated. For this

$$\begin{aligned} \sum_{(k+1)}^N S(i) &= (1 + m) * S(k) \\ \sum_{(k+2)}^N S(i) &= (1 + m) * S(k + 1) \\ S(k + 1) &= (1 + m) * (S(k) - S(k + 1)) \\ S(k + 1) &= (1 + m)/(2 + m) * S(k) \end{aligned}$$

This Points to a non binary radix  $r = (1 + m)/(2 + m)$ . since redundancy greater than a step is not required  $m < 1$  and  $r < 2/3$ . Total conversion clock  $= \tau * \ln(1/m) * \ln(2) * \ln(m + 1)/\ln(2 + m)$ . Though this points to a near zero conversion time with  $m=1$  its a mathematical anomaly because of approximating error as  $S(k) * e^{-T_{dac}/\tau}$ . More correct Derivation is as follows (assumes non binary sar)

$$\begin{aligned} settlingerror &= \sum_1^k S(i) * e^{(-(k-i)*T_{clk}+T_{dac})/\tau} \\ S(k) &= 1/2 * r^{(k-1)} \\ settlingerror &= 1/2 * r^{(k-1)} * e^{-T_{dac}/\tau} * \sum_0^{k-1} r^{-i} * e^{-iT_{clk}/\tau} \\ settlingerror &= 1/2 * r^{(k-1)} * e^{-T_{dac}/\tau} * (1 - r^{-k} * e^{-k*T_{clk}/\tau}) / (1 - r^{-1} * e^{-T_{clk}/\tau}) \\ e^{-T_{clk}/\tau} &< r \text{ for Conevergence} \\ settlingerror &= 1/2 * r^{(k-1)} * e^{(-T_{dac}/\tau)} / (1 - r^{-1} * e^{-T_{clk}/\tau}) \\ settlingerror \text{ allowed by redundancy} &= m * 1/2 * r^{(k-1)} \\ T_{clk} &= T_{dac} \Leftarrow \text{a pessimistic approximation} \\ e^{-T_{dac}/\tau} &= mr / (r + m) \\ r &= 1/2 \\ T_{dac} &= 2 * \ln(2) * \tau; \end{aligned}$$

## Topology

From analysis of CDAC settling nature and from behavior of comparators if we use non binary SAR we get that

$$\begin{aligned}
 VDD * e^{-T_{cmp}/\tau_1} + S(k) * e^{-T_{dac}/\tau_2} &= S(k) * m \\
 \Rightarrow T_{decision}(k) &= k * T1 + T2 \\
 \Rightarrow T_{conversion} &= N^2 * T1 + T2 * N.
 \end{aligned}$$

The  $O(N^2)$  Term in this is what is Causing inefficiency in conversion and cannt be easily avoided without gain . Adding gain also adds its  $O(N^2)$  terms if given multiple steps . So following architecture is proposed .

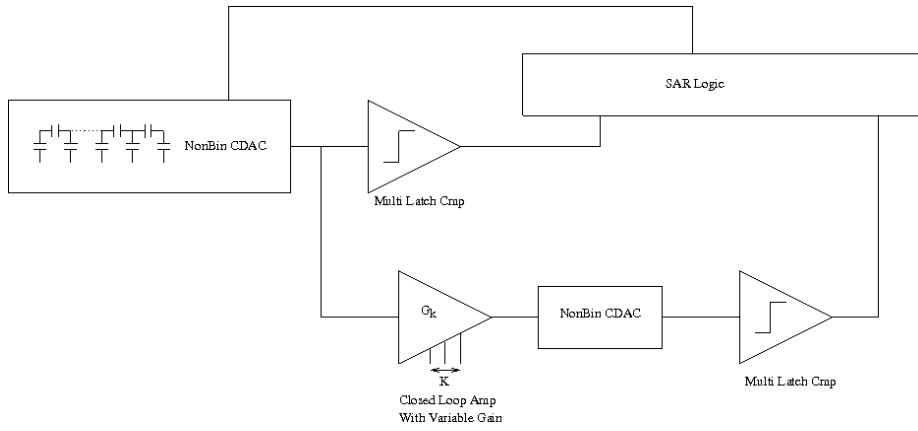


Figure 3: scheme