

Figure 1: Life cycle diagram and census points for pre-reproduction census of gizzard shad.

Graphical Abstract

- An integral projection model for gizzard shad (Dorosoma cepedianum) utilizing
- density-dependent age-0 survival
- ⁴ J. Peirce^{1,4}, G. Sandland^{3,4}, B. Bennie¹, R.A. Erickson²

5

- 6 Highlights
- An integral projection model for gizzard shad (Dorosoma cepedianum) utilizing
- $_{8}$ density-dependent age-0 survival
- ⁹ J. Peirce^{1,4}, G. Sandland^{3,4}, B. Bennie¹, R.A. Erickson²
- Research highlight 1
- Research highlight 2

An integral projection model for gizzard shad (*Dorosoma* cepedianum) utilizing density-dependent age-0 survival

J. Peirce^{1,4}, G. Sandland^{3,4}, B. Bennie¹, R.A. Erickson²

1 University of Wisconsin - La Crosse, Mathematics & Statistics Department
2 U.S.G.S. Upper Mississippi Environmental Science Center
3 University of Wisconsin - La Crosse, Biology Department
4 River Studies Center

$_{19}$ Abstract

12

13

14

15

16

17

18

Gizzard shad (Dorosoma cepedianum) are a common freshwater fish throughout the central and eastern portions of North America. Within these areas, gizzard shad play a number of critical roles in the freshwater community. Because of this, it is important that we understand how gizzard shad populations respond to environmental changes and what these changes may mean for aquatic communities in general and fish assemblages in particular. Here we introduce an integral projection model for gizzard shad based on empirical data and include density-dependent survival in age-0 fish. Integral projection models (IPM) are a generalization of stage-based, matrix population models that have been used to describe a wide range of organisms. IPMs are a natural choice for gizzard shad since many aspects of their life cycle have been studied. In this paper, we compared model outcomes to empirical patterns reported for this fish species at a key location along the Illinois River. Results of our work suggest that this model could serve as an important tool for predicting gizzard shad population responses to changing environmental conditions, including those mediated through species invasions.

- 20 Keywords: population dynamics, fisheries, Mississippi River basin, population ecology,
- 21 invasive species impact

2 1. Introduction

- Gizzard shad (*Dorosoma cepedianum*) is a laterally compressed, deep-bodied fish species
- 4 that occupies numerous aquatic systems throughout central, southern and eastern regions
- of the United States (Pierce et al., 1981; Vanni et al., 2005). In more eutrophic habitats,

such as reservoirs, gizzard shad can reach high abunadances and can come to dominate fish assemblages. Because of this, gizzard shad have the potential to influence freshwater systems in a number of ways. First, young shad often serve as a critical food source for many fish species, including those of commercial and recreational importance (such as walleye and largemouth bass)(Jester et al., 1972). Thus, this species can serve as an important trophic link within aquatic food webs. Second, because detritus can serve as a primary food source throughout much of gizzard shad development (i.e. from the age-0 stage onward), these fish can transport nutrients from benthic regions into pelagic habitats (Mather et al., 1995; Schaus and Vanni, 2000; Vanni et al., 2005). This process can result in an increase in the nutrients available to organisms within the water column leading to increases in phytoplankton biomass, algal blooms, and, due to these conditions, shifts in freshwater community structure (Aday et al., 2003; Schaus and Vanni, 2000). Finally, the fact that detritus can comprise a substantial portion of gizzard shad diet also makes this species an important connector between terrestrial inputs and aquatic processes (Schaus and Vanni, 2000). Given its potentially important role in aquatic ecosystems, interest has intensified in understanding how gizzard shad populations respond to environmental changes (both natural and anthropogenic) and what these changes may mean for freshwater communities in general and fish assemblages in particular.

In interconnected aquatic systems, such as the Mississippi and Illinois Rivers, gizzard shad interact with each other, with other species and with abiotic features of their environment across space and time (Thorp et al., 2006). These change results in different densities of fishes in the river systems such as the Upper Mississippi River (Holland, 1986). Gizzard shad populations and the density feedback limiting gizzard shad tie into other species as well. For example, Love et al. (2018) examine how invasive bighead and silver carp impact gizzard shad. The invasive carps both out-compete smaller gizzard shad and impact the body condition of adults. These changes caused Love et al. (2018) to suspect that reducing competition from invasive bighead and silver carp may help the species by improving adult body condition and the reproductive possibility of the gizzard shad.

Although substantial empirical work on gizzard shad biology has accumulated over the decades, few if any studies have attempted to use these data to model the population dy-

namics of the gizzard shad. Work by Catalano and Allen (2010, 2011) used empirically-based simulations of gizzard shad and focused on population-level responses. This work did examine population-structure by examining length and did not explore different sources of density feedback on the population dynamics. Here, we introduce an integral projection model for gizzard shad based on empirical data with density-dependent survival in age-0 fish. We then compare model outcomes to dynamics reported for this fish species in the La Grange Station along the Illinois River. The model itself could be an important tool for predicting gizzard shad population responses to changing environmental conditions, including those mediated through species invasions (i.e., silver and bighead carp).

65 2. Model Development

66 2.1. Gizzard shad life history

Mating within this species can be temperature-dependent, but tends to occur between
May and June. Males and females aggregate and then broadcast gametes into the surrounding water; fertilized eggs then settle and adhere to the bottom substrates. After a period of
days, eggs hatch and fish develop from the larval stage to juveniles and eventually to adults.
In many habitats, individuals can reach sexual maturity within a year. As gizzard shad
mature, their diet preferences typically shift from phytoplankton and zooplankton early in
development to detritus and zooplankton as adults. Given the large number of eggs produced by shad females (> 300,000/year), there is evidence that intraspecific competition
can be intense during early developmental stages in this species. However, the strength
of competition can subside as fish transition to different food types during latter stages of
development.

78 2.2. Equations

We used an integral projection model to describe the life history of gizzard shad in the
Upper Mississippi River (UMR) system. Integral projection model (IPM) were introduced
by Easterling (Easterling et al., 2000), as a generalization of stage-based, matrix population
models. IPMs have been used to describe a wide range of organisms (Ellner et al., 2016;
Merow et al., 2014; Rees et al., 2014) and are a natural choice for gizzard shad since many

Table 1: A summary of parameters, their biological meaning, and source for mean values.

Parameter	Meaning (units)	Mean	Source
Logistic survival probability func-			
tion, $s(z)$			
s_{\min}	minimum survival	0.002	(Bodola, 1955)
$s_{ m max}$	maximum survival	$1 - 8.871K^{0.73}L_{\infty}^{-0.33}$	THEN 2015
α_s	inflection point	modeled	LTRM dataset
β_s	slope	-5	(Erickson et al., 2017)
Growth function, $G(z, z')$			
L_{∞}	maximum length (in mm)	394.30	(Catalano and Allen, 2010)
K_g	growth rate	0.26	(Michaletz, 2017)
σ_g	growth standard deviation	25	(Michaletz, 2017)
Normal distribution of length of age-			
$1, C_1(z')$			
μ_r	mean length of recruitment (in	105	(Michaletz, 2017)
	mm)		
σ_r	standard deviation of length	25	(Michaletz, 2017)
Eggs produced, $egg(z)$			
$\mathrm{egg}_{\mathrm{max}}$	maximum number of eggs pro-	742,094	Estimated from (Jons and Mi-
	duced		randa, 1997)
α_e	inflection point	314.44	Estimated from (Jons and Mi-
			randa, 1997)
eta_e	slope	-7.12	Estimated from (Jons and Mi-
			randa, 1997)
Survival of age-0, $s_0(d(t))$			
a_0	intercept	0.27	Estimated from (Michaletz, 2010)
b_0	decay rate	0.003	Estimated from (Michaletz, 2010)
Spawning			
ν	probability that egg becomes vi-	0.002	(Bodola, 1955)
	able		
p_b	probability that female spawns	0.90	

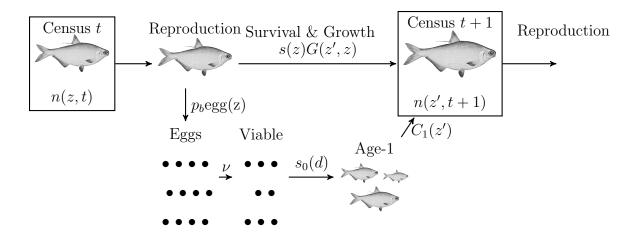


Figure 2: Life cycle diagram and census points for pre-reproduction census of gizzard shad.

aspects of their life cycle have been studied. Specifically, functions used in our model incorporate data from studies on egg production and adult size as well as the survival of the 85 age-0 stage and density. 86 We assumed that variations among individual gizzard shad can be summarized by its 87 length z (in mm) ranging from the minimum possible length L to the maximum value U. The state of the population at time t (in years) is described by the length distribution n(z,t). Specifically, for each time t, n(z,t) is a smooth function of z such that the number 90 of individuals of length z in the interval [a,b] at time t is $\int_{a}^{b} n(z,t) dz$. 91 Between times t and t+1, individual gizzard shad may grow, die, and produce offspring 92 that vary in length depending on the individuals current length (Figure ??). At time t+1 the 93 population will have a length distribution defined by n(z, t+1). For our model, we partition the life cycle of gizzard shad into two stages: 1) survival and growth, and 2) reproduction. 95 For an individual of length z at time t, $P(z',z)\Delta z$ is the probability that the individual is alive at time t+1, and its size is in the interval $[z', z' + \Delta z]$ (as with n(z,t) this is an 97 approximation that is valid for small Δz , and the exact probability is given by an integral like the one above). Similarly. $F(z',z)\Delta z$ is the number of new offspring in the interval $[z', z' + \Delta z]$ present at time t + 1, per length-z individual at time t.

101 2.2.1. Growth and survival

We define P(z'z) = s(z,T)G(z',z) where s(z) is the adult annual survival probability and G(z',z) describes the annual length transitions. We assumed that the survival function is a logistic function,

$$s(z,T) = s_{\min} + \frac{s_{\max} - s_{\min}}{1 + e^{\beta_s(\ln(z) - \ln(\alpha_s))}}.$$
(1)

with four parameters: the minimum survival rate s_{\min} ; a maximum survival rate, s_{\max} ; and intercept parameter, α_s ; and a slope parameter, β_s (Bolker, 2008).

We assumed that the growth function is a two-variable normal distribution centered around a modified von Bertalanffy function of the length at time t. The von Bertalanffy equation, commonly used to describe the length of a fish over time, is given by $z(t) = L_{\infty} \left(1 - e^{-K(t-t_0)}\right)$ where L_{∞} is maximum asymptotic length, K is the growth rate, and t_0 is the initial time. The expected length in the next year

$$z' = z(t+1) = L_{\infty} \left(1 - e^{-K(t+1-t_0)} \right) = L_{\infty} - L_{\infty} e^{-K(t-t_0)} e^{-K}$$
$$= L_{\infty} - (z(t) - L_{\infty}) e^{-K} = L_{\infty} \left(1 - e^{-K} \right) + z(t) e^{-K}.$$

Consequently, we assumed that $G(z',z) = \text{Prob}(z' | z, L_{\infty}, K_g) = \text{NormalPDF}(\mu_g, \sigma_g)$ where K_g is the individual growth rate, $\mu_g = L_{\infty} \left(1 - e^{-K_g}\right) + z(t)e^{-K_g}$, and σ_g is the standard deviation.

110 2.3. Fecundity

We define the fecundity kernel,

$$F(z',z) = p_b \operatorname{egg}(z) \nu s_0(n(z,t)) C_1(z')$$
(2)

where p_b is the probability of reproducing, egg(z) is the mean number of eggs produced, ν is the probability that an egg is viable, $s_0(n(z,t))$ is the density-dependent probability of surviving to age-1, and $C_1(z')$ is the length distribution of new recruits at age-1 (when they are first censused).

We assumed that the mean number of eggs produced by females of a certain length is a three-parameter logistic function,

$$\operatorname{egg}(z) = \frac{\operatorname{egg}_{\max}}{1 + e^{\beta_e(\ln(z) - \ln(\alpha_e))}}.$$
 (3)

The probability of survival of gizzard shad during their first year may depend on many factors (Michaletz, 2010) such as mean temperature, mean total length, the present density of age-0 fish. In this study, we focus only on the density factor and define the probability of survival of age-0 fish as the exponential function

$$s_0(d(t)) = a_0 e^{-b_0 d(t)} (4)$$

where a_0 is the intercept, b_0 the decay rate, and d(t) is the density at time t of age-0 gizzard shad per 1000 m³,

$$d(t) = 10^{-3} \int_{L}^{U} p_b \operatorname{egg}(z) \nu n(z, t) dz.$$

Finally, after computing the total number of viable eggs produced and survive to age-1 fish, we multiplied this number with a normal distribution of length, $C_1(z') = \text{NormalPDF}(\mu_r, \sigma_r)$ where μ_r is the mean length of age-1 gizzard shad and σ_r is the standard deviation.

2.4. Dynamical Model

The population at time t+1 is the sum of the contributions from each individual alive at time t,

$$n(z', t+1) = \int_{L}^{U} K(z', z) n(z, t) dz, \tag{5}$$

where K(z',z) = s(z)G(z',z) + F(z',z) and [L,U] is the range of all possible lengths.

3. Methods

3.1. Study Area and LTRMP Data Collection

The 129 km long La Grange Reach is located between La Grange Lock and Dam (L&D) and Peoria L&D on the Illinois River, U.S., and is about midway between the Mississippi River, River and Lake Michigan. The Illinois River is a major tributary of the Mississippi River, draining nearly two-thirds of the state of Illinois. Along with the main channel of the UMR, the fish community of La Grange Reach has been monitored by the Long-term Resource Monitoring Program (LTRMP) from 1990 to the present, with approximately 500 random collections each year from 15 June to 31 October. The LTRMP fish collection methodology included a multiple gear approach (netting and electrofishing) to monitor the general fish

community of the UMR system through time (Gutreuter et al., 1995). The total lengths were recorded for all fishes captured. Methodology, protocols and modifications to the LTRMP can be found in Gutreuter et al. (1995), and Ickes and Burkhardt (2002).

The location of La Grange Reach has two important features motivation its choice for the 144 methods of our study. First, we parameterized the IPM using data from the main channel 145 of the UMR. As a part of Illinois River and UMR, La Grange Reach is upstream from the 146 main channel (should we include figure/map?). The proximity to, but relative independence 147 from, the main channel, made it a good choice. Secondly, La Grange Reach is a large pool 148 between the main channel of the Mississippi River and Lake Michigan. In recent years, 149 there have been concerns with the threatening introduction of invasive carp to the Great Lakes. Consequently, the impact of invasive carp on the native fish populations in the pools 151 leading to the Great Lakes have received an elevated level of attention. Understanding the 152 population dynamics of gizzard shad, may in the future make it easier to assess the impacts 153 carp has on native fish populations. 154

3.2. Parameterization

The parameters for the growth function were chosen as the mean values published on a 156 study of gizzard shad located in large impoundments (Michaletz, 2017). The survival rate 157 of adults gizzard shad dependent on their length is not well documented and required us 158 to make some additional modeling assumptions. An investigation of gizzard shad in Lake 159 Eerie (Bodola (1955)) provided the minimum and maximum survival rate of adults. In many 160 of the river domains included in our analysis, invasive carp are also present (LTRMP fish 161 dataset). Invasive carp is a well-studied invasive species along the Mississippi and Illinois 162 Rivers. Assuming that the resources that effect survival are similar, we use the published 163 (Erickson et al., 2017) slope parameter, β_s , for the gizzard shad population. Finally, we 164 used a least squares method to find the $alpha_s$ parameter that minimizes the total square-165 distance between the (observed) pre-carp LTRMP length distribution and (predicted) model 166 equilibrium, n(z, 100).

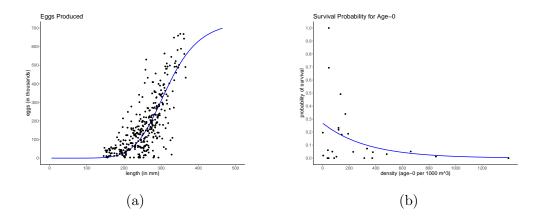


Figure 3: (a) Graph of egg(z). Data from (Jons and Miranda, 1997). (b) Graph of $s_0(d)$. Data from (Michaletz, 2010).

3.2.1. Fecundity and recruitment

169

170

171

172

173

Maturity of female gizzard shad corresponds with lengths of approximately 140 mm and the number of eggs produced increase as the females increase in size (Jons and Miranda, 1997). The mean eggs produced per female was described by a three-parameter logistic function (see Figure 1) whose parameters were estimated from data provided in Figure 1a. of (Jons and Miranda, 1997).

The survival to age-0 was assumed to be dependent on the density of age-0 gizzard shad (Figure 3b). We estimated the exponential parameters using data provided in Table 2 of (Michaletz, 2010). The parameters for the size distribution of age-1 fish were gleaned from a study of gizzard shad located in large impoundments (Michaletz, 2017) and the historic 1990-2020 LTRMP dataset of gizzard shad in La Grange Reach.

179 4. Analysis and Results

We numerically solved the integral model using the Midpoint Rule with large approximating matrices (Burden and Faires, 2005). The Midpoint Rule has been commonly used for integral projection models because of its simplicity and effectiveness (Ellner and Rees, 2006; Ramula et al., 2009; Merow et al., 2014). During the course of model development, we explored different step sizes for the Midpoint Rule and found that about 50 points provided numerically stable results. We integrated over lengths from 0 mm to 400 mm. The upper limit was chosen based upon numerical stability and consistency of the system (e.g., avoiding

eviction or the loss of individuals due to numerical errors (Williams et al., 2012)).

4.1. Initial conditions

We assumed that the initial density of gizzard shad $d_0 = 964.7$, the annual average density of gizzard shad observed in La Grange Reach from 1993-2019. The probability of an individual being length z at time t = 0 was assumed to be normally distributed with mean $0.5L_{\infty}$ and standard deviation $\sigma_0 = 30$, similar to observations (1990-2020) in LTRMP fish dataset. As a result, we initialized our model with

$$n(z,0) = d_0 \text{Norm}(0.5L_\infty, \sigma_0) = 964.7 \text{Norm}(166, 30).$$
 (6)

The model was coded in R (R Core Team, 2017) and the scripts are published on JP github page https://github.com/jppeirce.

196 4.1.1. Comparison with the LTRMP La Grange dataset

The total number of gizzard shad in our simulation reached a stable equilibrium (Figure 197 4a) within 50 years and, more relevantly, the length distribution at that equilibrium compares 198 favorably with the observations from La Grange found in the LTRMP fish dataset (Figure 199 4b). We notice that the peak frequencies are near the same length with the model predicting 200 slightly more adults lengths and fewer juvenile lengths than the observations. The location 201 of the maximum in the LTRMP data, corresponding to new recruits, suggests that there 202 may be smaller age-0 fish than in study from (Michaletz, 2017) that was used in the model 203 parameterization. 204

4.1.2. Survival and Relative Growth

205

The dependence on survival of next generation of age-0 fish on the present density of age-0 fish strongly influences the density, at all ages, of gizzard shad within the population. When the fish density is large, there may be more fish at longer lengths and consequently a greater number of eggs produced. More eggs leads to a higher density of age-0 fish and reflectively a reduction in the survival to age-1. If this reduced survival continues for a few years, the overall density of fish may decline and there may not be as many larger fish reproducing. If fewer eggs are spawned, there are less age-0 fish and the reduced density

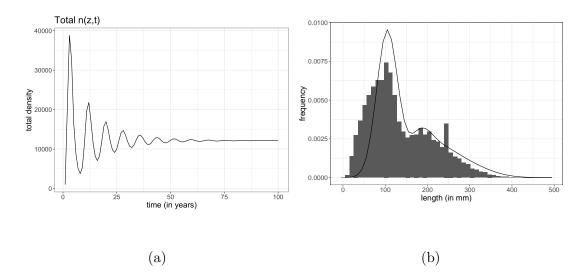


Figure 4: (a) The total number of gizzard shad in La Grange Reach predicted by IPM for first 50 year. (b) LTRMP observations of gizzard shad in La Grange Reach (histogram with 50 len) compared with the IPM length frequency at equilibrium (t = 100 years)

leads to a better survival probability. For these years we would expect the overall density to increase. This cycle of oscillation continues, reflected in our model by the time-dependent survival probability of age-0 (Figure 5a) and the relative growth rate

$$\lambda(t) = \int_{L}^{U} n(z, t+1) dz / \int_{L}^{U} n(z, t) dz$$

 $_{206}$ (Figure 5b).

211

212

213

214

215

of 4.2. Time Evolution of Initial State

Starting with n(z,0) defined by Equation 6, we computed the length distribution for 3 years. In year 1, there are two relative maximum frequencies corresponding to the recruitment of age-1 fish and the survival of the adults.

4.2.1. Dynamics of the Age-1 Over Time - Fixed Frame

The greatest value of n(z, 1) during year one is centered at the mean length of recruitment. In the following years, the decrease in the maximum value is a result of the two factors: the reduction in the density of adults and the density-dependent survival function for age-0 fish. Starting in year 1, there is a reduction in the number of egg-producing adults (lengths above

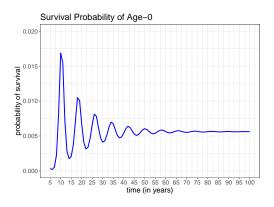


Figure 5

Figure 6: (a) Survival of age-0

140 mm) compared with the initial population. From Figure 3a, fewer longer adults implies fewer eggs produced. The eggs that are produced, however, may have a greater chance of survival to the age-1 census (Figure ??). This is evident in the increase in density of recruits (NEED TO SHOW?) but is illustrated in lower frequency of recruits (Figure 6b) [Theme: Dynamics of a cohort - moving frame] Figure XXX also demonstrates the growth in gizzard shad population. The peak length frequency of age-1 fish in n(z, 1) near z = 105mm is seen as a peak in n(z, 2) near 160 mm, and again as a peak in n(z, 3) at about 210

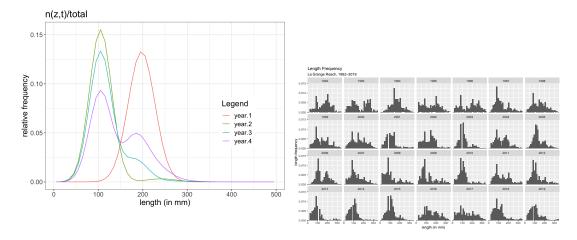
5. Discussion

233

mm. MORE DISCUSSION NEEDED

We compare a simulated length distribution with U.S. Geological Survey (USGS) Long-225 Term Resource Monitoring (LTRMP) data from the La Grange Reach of the Illinois River 226 from 1992-2019. The La Grange Reach of the Illinois River is a 125 km segment of the lower 227 Illinois River between the La Grange Lock and Dam at RKM 129 and the Peoria Lock and 228 Dam at RKM 254. It is characterized by a wide floodplain surrounding the main channel 229 and a mosaic of side channels, fully connected backwaters, and semi-connected backwaters. 230 [Comparison of Frequency plots vs Simulation - Similarities] In these data, we see similar 231 patterns as displayed in Figure XXX. Specifically, from years 2010-2012... 232

[Comparison of Frequency plots vs Simulation - Differences]



(a) Simulated frequency of lengths of Giz- (b) Simulated frequency of lengths of Giz-zard Shad. Initial density and N=xxx zard Shad. Initial density and N=xxx

Figure 7: (a) Simulated length distributions. (b) LTRMP gizzard shad density from La Grange Reach 1992-2020

- [Possible explanation of differences and future direction]
- [More future direction two species model]
 - 1. Summary of findings and key discussion points
- (a) Comparison to empirical data

236

238

239

240

241

242

243

245

246

248

249

- (b) Deviations from empirical data
- (c) discussion about sameness and differences
- (d) Sources of density within our model
- 2. Comparison to existing literature
 - (a) Talk about Matt's work (Catalano and Allen, 2010, 2011)
 - (b) Broader need for models such as this
- 3. Implications for management of species
 - (a) Invasive species
 - (b) Impact of size on harvest
- (c) impact of size on movement
 - 4. Future ideas to explore
 - (a) Multi-species model

- (b) Spatial impacts
- (c) Climate on density
- (d) Changing climate scenarios

253 6. Acknowledgments

These data are a product of the U.S. Army Corps of Engineer's Upper Mississippi River 254 Restoration Program (UMRR) Long Term Resource Monitoring (LTRMP) element imple-255 mented by the U.S. Geological Survey in collaboration with the five Upper Mississippi River 256 System (UMRS) states of Illinois, Iowa, Minnesota, Missouri, and Wisconsin. The U.S. 257 Army Corps of Engineers (Corps) provides guidance and has overall program responsibility. 258 We thank the U.S. Geological Survey Biothreats program and Great Lakes Restoration 259 Initiative for funding. In addition, research was supported by NSF-DMS Grant #1852224, 260 "REU Site: Ecological Modeling of the Mississippi River Basin". 261

References

- R. J. Pierce, T. E. Wissing, B. A. Megrey, Aspects of the feeding ecology of gizzard shad in acton lake, ohio, Transactions of the American Fisheries Society 110 (1981) 391–395.
- M. J. Vanni, K. K. Arend, M. T. Bremigan, D. B. Bunnell, J. E. Garvey, M. J. Gonzalez,
 W. H. Renwick, P. A. Soranno, R. A. Stein, Linking landscapes and food webs: effects of
 omnivorous fish and watersheds on reservoir ecosystems, BioScience 55 (2005) 155–167.
- D. B. Jester, B. L. Jensen, et al., Life history and ecology of the gizzard shad, *Dorosoma* cepedianum (le sueur) with reference to Elephant Butte Lake (1972).
- M. E. Mather, M. J. Vanni, T. E. Wissing, S. A. Davis, M. H. Schaus, Regeneration of nitrogen and phosphorus by bluegill and gizzard shad: effect of feeding history, Canadian Journal of Fisheries and Aquatic Sciences 52 (1995) 2327–2338.
- M. H. Schaus, M. J. Vanni, Effects of gizzard shad on phytoplankton and nutrient dynamics: role of sediment feeding and fish size, Ecology 81 (2000) 1701–1719.

- D. D. Aday, R. J. H. Hoxmeier, D. H. Wahl, Direct and indirect effects of gizzard shad on bluegill growth and population size structure, Transactions of the American Fisheries Society 132 (2003) 47–56.
- J. H. Thorp, M. C. Thoms, M. D. Delong, The riverine ecosystem synthesis: biocomplexity in river networks across space and time, River Research and Applications 22 (2006) 123–147.
- L. E. Holland, Distribution of early life history stages of fishes in selected pools of the upper mississippi river, Hydrobiologia 136 (1986) 121–130.
- S. A. Love, N. J. Lederman, R. L. Anderson, J. A. DeBoer, A. F. Casper, Does aquatic invasive species removal benefit native fish? the response of gizzard shad (dorosoma cepedianum) to commercial harvest of bighead carp (hypophthalmichthys nobilis) and silver carp (h. molitrix), Hydrobiologia 817 (2018) 403–412.
- M. J. Catalano, M. S. Allen, A size-and age-structured model to estimate fish recruitment, growth, mortality, and gear selectivity, Fisheries Research 105 (2010) 38–45.
- M. J. Catalano, M. S. Allen, A whole-lake density reduction to assess compensatory responses
 of gizzard shad dorosoma cepedianum, Canadian Journal of Fisheries and Aquatic Sciences
 68 (2011) 955–968.
- A. Bodola, The life history of the gizzard shad, Dorosoma cepedianum, in western Lake Erie,
 Ph.D. thesis, Doctoral dissertation. Ohio State University, Columbus, 1955.
- R. A. Erickson, E. A. Eager, M. K. Brey, M. J. Hansen, P. M. Kocovsky, An integral projection model with yy-males and application to evaluating grass carp control, Ecological Modelling 361 (2017) 14–25.
- P. Michaletz, Variation in characteristics among gizzard shad populations: The role of impoundment size and productivity, Fisheries Management and Ecology 24 (2017) 361–371.
- G. Jons, L. Miranda, Ovarian weight as an index of fecundity, maturity, and spawning periodicity, Journal of Fish Biology 50 (1997) 150–156.

- P. H. Michaletz, Overwinter survival of age-0 gizzard shad in missouri reservoirs spanning a productivity gradient: roles of body size and winter severity, Transactions of the American Fisheries Society 139 (2010) 241–256.
- M. R. Easterling, S. P. Ellner, P. M. Dixon, Size-specific sensitivity: applying a new structured population model, Ecology 81 (2000) 694–708.
- S. P. Ellner, D. Z. Childs, M. Rees, et al., Data-driven modelling of structured populations,

 A practical guide to the Integral Projection Model. Cham: Springer (2016).
- C. Merow, J. P. Dahlgren, C. J. E. Metcalf, D. Z. Childs, M. E. Evans, E. Jongejans,
 S. Record, M. Rees, R. Salguero-Gómez, S. M. McMahon, Advancing population ecology
 with integral projection models: a practical guide, Methods in Ecology and Evolution 5
 (2014) 99–110.
- M. Rees, D. Z. Childs, S. P. Ellner, Building integral projection models: a user's guide, Journal of Animal Ecology 83 (2014) 528–545.
- B. M. Bolker, Ecological models and data in R, Princeton University Press, 2008.
- S. Gutreuter, R. Burkhardt, K. S. Lubinski, Long term resource monitoring program procedures [microform] (1995).
- B. S. Ickes, R. W. Burkhardt, Evaluation and proposed refinement of the sampling design for the Long Term Resource Monitoring Program's fish component, Technical Report, Geological Survey La Crosse WI Upper Midwest Environmental Sciences Center, 2002.
- R. Burden, J. D. Faires, Numerical analysis 8th ed, Thomson Brooks/Cole (2005).
- S. P. Ellner, M. Rees, Integral projection models for species with complex demography, The
 American Naturalist 167 (2006) 410–428.
- S. Ramula, M. Rees, Y. M. Buckley, Integral projection models perform better for small demographic data sets than matrix population models: a case study of two perennial herbs, Journal of Applied Ecology 46 (2009) 1048–1053.

- J. L. Williams, T. E. Miller, S. P. Ellner, Avoiding unintentional eviction from integral projection models, Ecology 93 (2012) 2008–2014.
- R Core Team, R: A Language and Environment for Statistical Computing, R Foundation for Statistical Computing, Vienna, Austria, 2017. URL: https://www.R-project.org/.