Lab 05 - Error Computation

Numerical Solution of PDEs Using the Finite Element Method

MHPC P2.13_seed

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- 1. The topic of this lab session is a modified version of step-4 made available for you https://www.dealii. org/8.5.0/doxygen/deal.II/step 4.html
- 2. For more information about computing errors see step-7 (it is a bit more complicated though) https://www.dealii.org/8.5.0/doxygen/deal.II/step_7.html
- 3. Run the program and check the graphical and text output.
- 4. Where is the right-hand side defined and where do the boundary conditions come from?
- 5. Fix the right-hand side and boundary conditions to get the manufactured solution

$$u(x) = \sin(\pi x) \cdot \cos(\pi y)$$

and make sure the L2 errors are converging.

- 6. Increase the polynomial degree of the finite element space and check the convergence of the L2 error.
- 7. Implement the computation of the H1 error. For this you need to compute the gradient of the manufactured solution and implement it (see commented out code for a start).
- 8. Implement a suitable 3d manufactured solution and test the convergence.