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ES 292

**Homework #9: 13.1, 13.4, 13.5**

**13.1**  
Using the diameter information from Table 13.1, calculate how many (a) gas molecules, (b) medium aerosol particles, and (c) fog drops make up the volume of a single medium raindrop. Use average diameters where applicable.

Volume of medium raindrops:

Vmr <- pi \* (2000^3) / 6   
  
print(Vmr) # Um ^3

## [1] 4188790205

dm\_gs <- .0005 # typical diameter of gas molecules, in um  
v\_gs <- pi \* (dm\_gs^3) / 6 #volume of typical gas molecule, in um^3  
print(Vmr/v\_gs) #The number of gas molecules in a medium raindrop.

## [1] 6.4e+19

dm\_map\_min <- .2 #um  
dm\_map\_max <- 1.0 #um  
ave\_dm\_map <- mean(dm\_map\_min, dm\_map\_max)  
v\_map <- pi \* (ave\_dm\_map^3) / 6  
print(v\_map) #Number of average medium aerosol particles in a medium raindrop

## [1] 0.00418879

dm\_fg\_min <- 10 #um  
dm\_fg\_max <- 20 #um  
ave\_dm\_fg <- mean(dm\_fg\_min, dm\_fg\_max)  
v\_fg <- pi \* (ave\_dm\_fg^3) / 6  
print(v\_fg) #Number of average fog droplets in a medium raindrop

## [1] 523.5988

**13.4**  
Calculate the number concentration of raindrops from the Marshall–Palmer distribution in the diameter ranges (a) 200–300 μm and (b) 800–900 μm, when R = 25 mm h−1. Why are the number concentrations different in the two size ranges?

EQ 13.30

EQ 13.9

#diameter ranges are 200 -300 um  
di\_lo\_a <- 200 #um  
di\_hi\_a <- 300 #um  
R <- 25 #mm h^-1  
lm\_r <- (4.1 \* (10^-3)) \* (R^-.21) #um ^-1  
n0\_a <- 8 \* (10^-6) # particles cm^ -3 um ^-1  
dd\_a <- di\_hi\_a - di\_lo\_a #um, diameter width   
ni\_a <- dd\_a \* n0\_a \* exp(-lm\_r \* di\_lo\_a) #particles cm^-3, number concentraion for bin a  
  
  
print(ni\_a)

## [1] 0.0005271608

#diameter ranges are 200 -300 um  
di\_lo\_b <- 800 #um  
di\_hi\_b <- 900 #um  
  
n0\_b <- 8 \* (10^-6) # particles cm^ -3 um ^-1   
dd\_b <- di\_hi\_b - di\_lo\_b #um, diameter width  
ni\_b <- dd\_b \* n0\_b \* exp(-lm\_r \* di\_lo\_b) #particles cm^-3, number concentraion for bin b  
  
  
print(ni\_b)

## [1] 0.0001508352

The number concentrations are constrained by the size of the droplets. In case a), ni = 5.271608510^{-4}, discrete particles are small and thus more particles will be found in a given area. In case b), ni = 1.508351710^{-4}, although the range of particle sizes is the same as case a) (100 um), the discrete particle sizes are larger. Thus, fewer droplets will be found in the same given space.

**13.5**  
Compare the number concentrations of drops between 18 and 22 μm in diameter at the base and at the top of a nimbostratus cloud using a modified gamma distribution. Why do you think the concentrations differ in the two cases?

EQ 13.31

r\_hi <- 22/2 # radius of largest droups in bin, um  
r\_lo <- 18/2 # radius of smallest drops in bin, um  
del\_r <- r\_hi - r\_lo #radius width of bin, um  
ri <- mean(r\_hi, r\_lo) # mean radius of bin  
  
#gamma parameters for base of nimbostratus cloud, given by table 13.4  
Ag\_b <- .080606  
al\_g\_b <- 5.0  
up\_g\_b <- 1.24  
r\_cg\_b <- 6.41 #um  
  
#gamma parameters for top of nimbostratus cloud, given by table 13.4  
Ag\_t <- 1.0969  
al\_g\_t <- 1.0  
up\_g\_t <- 2.41  
r\_cg\_t <- 9.67 #um  
  
#drop number concentration in bin i for base of nimbostratus cloud  
  
n\_base <- del\_r \* Ag\_b \* (ri ^ al\_g\_b) \* exp( -(al\_g\_b/up\_g\_b) \* ( (ri / r\_cg\_b) ^ up\_g\_b))  
  
#drop number concentration in bin i for top of nimbostratus cloud  
n\_top <- del\_r \* Ag\_t \* (ri ^ al\_g\_t) \* exp( -(al\_g\_t/up\_g\_t) \* ( (ri / r\_cg\_t) ^ up\_g\_t))  
  
print(n\_base) # particles cm ^-3

## [1] 9.847837

print(n\_top) # particles cm ^-3

## [1] 13.70104

The drop number concentration at the base and top of a nimbostratus cloud are 9.8478374 particles cm-3 and 13.7010394 particles cm-3 respectively. I suspect that if we look at different bin widths, we will see greater number concentrations at the base in small bin widths, while at the top, as temperatures drive condensation, we will see greater number concentrations in larger bin widths. In addition, these values seem accurate.

Nimbostratus clouds are heavy with precipitation, so 10~14 particles cm^-3 seem like an accurate value for this bin (micrometers).