## **Analysis**

```
## Loading required package: rJava
## Loading required package: xlsxjars
maindata <- read.xlsx("C:/Users/jaceline.preval/Desktop/717/BreastTissuedata.xl</pre>
sx", 1)
#Overview of data.
head(maindata)
     Case.. Class
                        ΙO
                               PA500
                                            HFS
                                                      DA
                                                              Area
                                                                        ADA
        1
               1 524.7941 0.1874484 0.03211406 228.8002 6843.598 29.91080
               1 330.0000 0.2268928 0.26529005 121.1542 3163.239 26.10920
               1 551.8793 0.2324779 0.06352998 264.8049 11888.392 44.89490
          3
               1 380.0000 0.2408554 0.28623400 137.6401 5402.171 39.24852
               1 362.8313 0.2007129 0.24434610 124.9126 3290.462 26.34213
        6
               1 389.8730 0.1500983 0.09773844 118.6258 2475.557 20.86862
                     DR
       MaxIP
                               Ρ
## 1 60.20488 220.73721 556.8283
## 2 69.71736 99.08496 400.2258
## 3 77.79330 253.78530 656.7694
## 4 88.75845 105.19857 493.7018
## 5 69.38939 103.86655 424.7965
## 6 49.75715 107.68616 429.3858
#Overall labels
Y2 <- as.matrix(maindata[,2])
#Overall data
Y1 <- as.matrix(maindata[,3:11])
#simple analysis
summary(Y1)
```

```
##
        ΙO
                   PA500
                                    HFS
                                                     DA
## Min. : 103.0 Min. :0.01239 Min. :-0.06632 Min. : 19.65
## 1st Qu.: 250.0 1st Qu.:0.06741 1st Qu.: 0.04398 1st Qu.: 53.85
## Median: 384.9 Median: 0.10542 Median: 0.08657 Median: 120.78
## Mean : 784.3 Mean :0.12013 Mean : 0.11469 Mean : 190.57
## 3rd Qu.:1488.0 3rd Qu.:0.16960 3rd Qu.: 0.16650 3rd Qu.: 255.33
## Max. :2800.0 Max. :0.35832 Max. :0.46775 Max. :1063.44
  Area
##
                       ADA
                                     MaxIP
                                                      DR
## Min. : 70.43 Min. : 1.596 Min. : 7.969 Min. : -9.258
## 1st Qu.: 409.65 1st Qu.: 8.180 1st Qu.: 26.894 1st Qu.: 41.781
## Median: 2219.58 Median: 16.134 Median: 44.216 Median: 97.833
## Mean : 7335.16 Mean : 23.474 Mean : 75.381 Mean :166.711
## 3rd Qu.: 7615.20 3rd Qu.: 30.953 3rd Qu.: 83.672 3rd Qu.:232.990
## Max. :174480.48 Max. :164.072 Max. :436.100 Max. :977.552
      Р
##
## Min. : 125.0
## 1st Qu.: 270.2
## Median : 454.1
## Mean : 810.6
## 3rd Qu.:1301.6
## Max. :2896.6
```

## First Step - Classification

```
##training data
data <- maindata[,2:11]

#Dividing training set with 70% of data and Test with 30%.
smp_size <- floor(0.70 * nrow(data))
set.seed(123)
train_ind <- sample(seq_len(nrow(data)), size = smp_size)

train <- scale(as.matrix(data[train_ind, ]))
test <- scale(as.matrix(data[-train_ind, ]))

#Training data
trainlabel <- as.matrix(train[,1])
traindata <- train[,2:10]

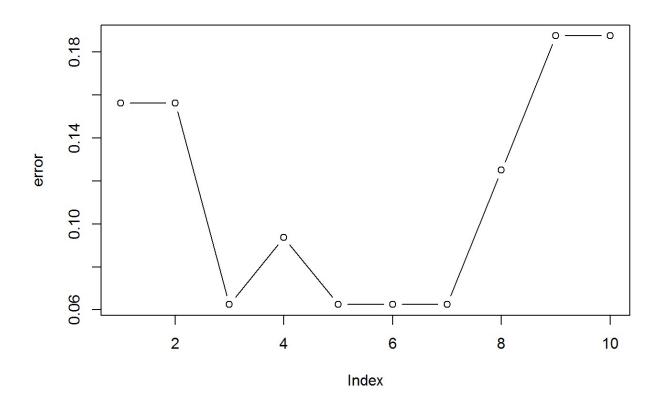
#test data
testlabel <- as.matrix(test[,1])
testdata <- test[,2:10]</pre>
```

I will then create 10 K-Nearest Neighbor Classifier with k equals from 1 to 10.

```
library(class)

for(i in 1:10){
    #model
    assign(paste("knnmodel", i, sep = ""), knn(train=traindata, test = testdata,
    cl=trainlabel, k=i))
}
```

Plotting the apparent error rate results with this graph.



Clearly, k=3 or 5, 6,7 is the best one with the lowest error rate at 0.06

## **Second Step - Principal Component Analysis**

I will perform PCA on my overall data and test four different method to decide how many of my 9 components should I retain to effectively summarize my data. For Each Method test, I will perform 2-Nearest Neighbor Classifier to see if my classification rate was improved.

```
# Preprocessing data by centering
y.bar <- apply(Y1, 2, mean)
Y <- t(t(Y1)-y.bar)

#overview after preprocessing
head(Y)</pre>
```

```
PA500
                                    HFS
                                                                   ADA
              T ()
                                               DΑ
                                                        Area
## [1,] -259.4575 0.06731572 -0.08257673 38.23159 -491.5567 6.437019
## [2,] -454.2516 0.10676017 0.15059926 -69.41444 -4171.9157 2.635418
## [3,] -232.3723 0.11234522 -0.05116080 74.23629 4553.2367 21.421119
## [4,] -404.2516 0.12072280 0.17154321 -52.92853 -1932.9840 15.774740
## [5,] -421.4204 0.08058023 0.12965531 -65.65608 -4044.6927 2.868342
## [6,] -394.3786 0.02996568 -0.01695235 -71.94283 -4859.5981 -2.605164
##
                         DR
            MaxIP
## [1,] -15.176379 54.02664 -253.8098
## [2,] -5.663897 -67.62561 -410.4124
## [3,] 2.412038 87.07472 -153.8687
## [4,] 13.377187 -61.51201 -316.9363
## [5,] -5.991869 -62.84402 -385.8416
## [6,] -25.624110 -59.02441 -381.2523
```

```
#checking how correlated is the data
library(corrplot)
corrplot(cor(Y), method="number")
```

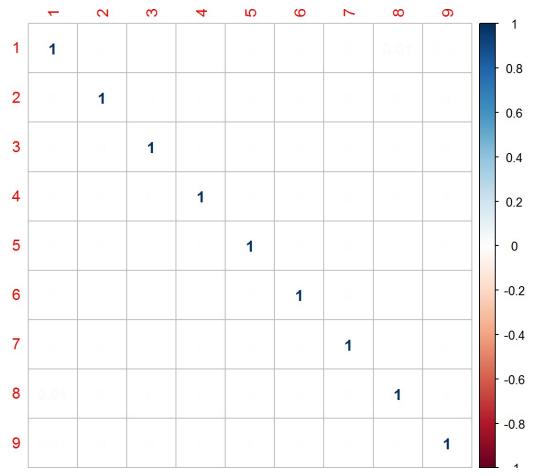


```
#getting all the principal components
S <- cov(Y)
C = matrix(round(eigen(S)$vectors, digits = 7),nrow=9,ncol=9)
A = t(C)</pre>
C
```

```
##
                        [,2]
                                  [,3]
                                             [,4]
             [,1]
                                                       [,5]
                                                                  [,6]
## [1,] 0.0227685 0.7007091 -0.2193015 -0.5895295 -0.3075227 0.0003377
   [2,] 0.0000003 -0.0000390 -0.0000217 0.0007528 0.0001727 -0.0013386
## [3,] 0.0000011 -0.0000073 0.0001281 0.0011740 -0.0004305 -0.0008730
  [4,] 0.0075117 0.1020608 -0.5611537 0.4437489 -0.2254843 0.6530514
##
   [5,] 0.9994061 -0.0339408 0.0046135 -0.0037133 0.0002891 0.0003822
   [6,] 0.0010433 0.0055121 0.0309353 0.1580544 0.1183112 -0.0107986
##
## [7,] 0.0032208 0.0473363 0.0813509 0.4243511 -0.7574393 -0.4869511
##
   [8,] 0.0065973 0.0810894 -0.6979450 0.1439556 0.3825269 -0.5798804
## [9,] 0.0236150 0.6989933 0.3772132 0.4793202 0.3471997 0.0046603
##
              [,7]
                        [,8]
                                   [,9]
## [1,] -0.1351980 -0.0011181 -0.0000585
## [2,] -0.0021257 -0.2585212 0.9660020
## [3,] 0.0037134 -0.9659991 -0.2585143
## [4,] 0.0200221 -0.0001106 0.0006054
## [5,] 0.0004506 -0.0000018 0.0000023
## [6,] -0.9797443 -0.0027936 -0.0030619
## [7,] -0.0148059 0.0013880 -0.0005274
## [8,] 0.0542329 0.0008199 -0.0006578
## [9,] 0.1350655 0.0009453 0.0001577
#eigen values
V <- matrix(round(eigen(S)$values, digits = 7),nrow=1,ncol=9)</pre>
            [,1] [,2] [,3] [,4] [,5] [,6] [,7]
## [1,] 345637606 788042.2 25486.66 2939.197 950.0759 96.7578 35.5838
            [,8] [,9]
## [1,] 0.0048272 0.001191
```

# Rotated data
Z = Y%\*%t(A)

# Getting uncorrelated data.
corrplot(cor(Z), method="number")



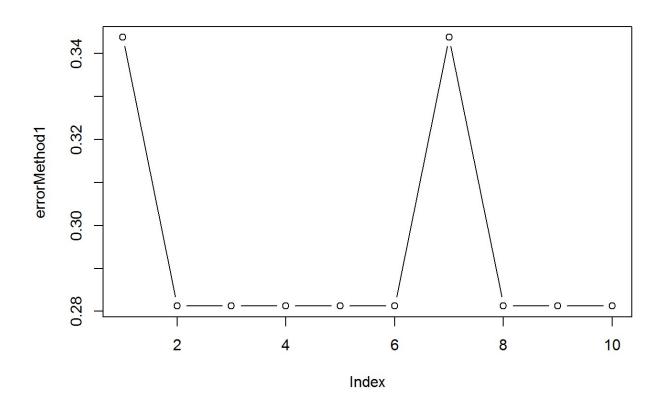
#### Method 1 - Getting the eigenvector with the highest eigenvalues

```
#getting the principal component witht the highest eigenvalue.
al <- C[,1]
#combining labels and the new data.
finaldataMethod1 <- cbind(Y2,Y%*%a1)</pre>
```

Perform another K-Nearest Neighbor Classifier with k equals from 1 to 10 on this new data given by this method. I will check to see if error was lower for k=2.

```
##train data
data <- finaldataMethod1</pre>
#Dividing training set with 70% of data and Test with 30%.
smp size <- floor(0.70 * nrow(data))</pre>
set.seed(123)
train ind <- sample(seq len(nrow(data)), size = smp size)</pre>
train <- scale(as.matrix(data[train ind, ]))</pre>
test <- scale(as.matrix(data[-train ind, ]))</pre>
#Train data
trainlabel <- as.matrix(train[,1])</pre>
traindata <- as.matrix(train[,2])</pre>
#test data
testlabel <- as.matrix(test[,1])</pre>
testdata <- as.matrix(test[,2])</pre>
library(class)
for(i in 1:10) {
  #model
  assign(paste("knnmodel", i, sep = ""), knn(train=traindata, test = testdata,
cl=trainlabel, k=i))
}
```

Plotting the apparent error rate results with this graph.



Clearly with this method, my error rate for k= 2 did not improved. My error rate increased from .06 to .28. This method failed completly to improve my error rate with the lowest rate being at .28.

# Method 2 - getting the eigenvectors with the eigenvalues greater than the average

```
S <- cov(Y)
lambda <-eigen(S)$value
average <- sum(lambda)/9
lambda[1]> average
## [1] TRUE
```

```
lambda[2]> average
```

```
## [1] FALSE
```

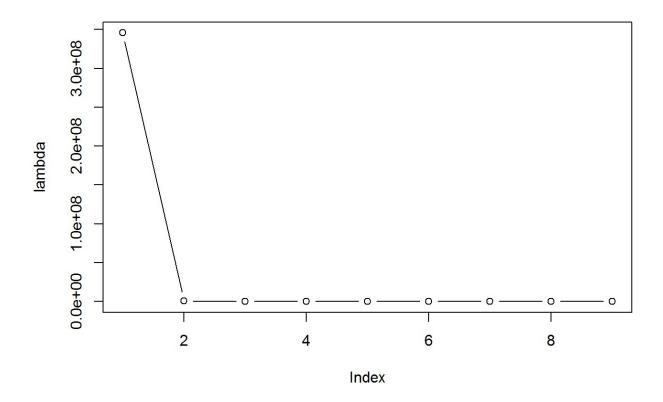
```
lambda[3]> average
```

```
## [1] FALSE
```

Since This method results with the same eigenvector as Method 1, We skip to metod #3.

#### Method 3 - use scree graph.

```
plot(lambda, type = "b")
```



Looking at the graph the first two eigenvectors should be retained.

```
a3 <- C[,2]
finalMethod3<- cbind(Y2,Y%*%a3)
```

Perform another K-Nearest Neighbor Classifier with k equals from 1 to 10 on this new data given by this method. I will check to see if error was lower for k=2.

```
# Redoing first sep again

##train data
data <- finalMethod3

#Dividing training set with 70% of data and Test with 30%.

smp_size <- floor(0.70 * nrow(data))
set.seed(123)
train_ind <- sample(seq_len(nrow(data)), size = smp_size)

train <- scale(as.matrix(data[train_ind, ]))
test <- scale(as.matrix(data[-train_ind, ]))

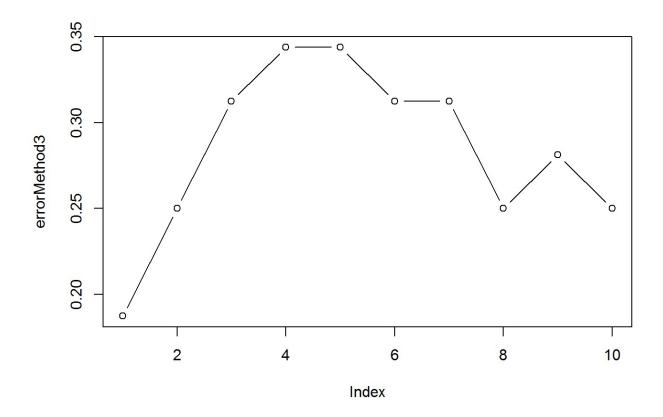
#Train data
trainlabel <- as.matrix(train[,1])
traindata <- as.matrix(train[,2])

#test data
testlabel <- as.matrix(test[,1])
testdata <- as.matrix(test[,2])</pre>
```

```
library(class)

for(i in 1:10){
    #model
    assign(paste("knnmodel", i, sep = ""), knn(train=traindata, test = testdata, cl=trainlabel, k=i))
}
```

Plotting the apparent error rate results with this graph.



With Method 3, my error rate for k= 2 did not improved. The error rate also increased from .06 to .25. This method failed completly to improve my error rate with the lowest rate being again at .19.