france_statistical_analysis

October 15, 2024

1 Top 5 Leagues Historical Goals: Statistical Insight

1.1 Top 5 Leagues Historical Goals: France recent increase in goals

1.1.1 Import relevant libraries

```
[327]: import pandas as pd
import numpy as np

import matplotlib.pyplot as plt
import seaborn as sns

from scipy import stats
from scipy.stats import linregress
from scipy.stats import norm
```

1.1.2 Load the CSV file with the data

	di.nead()												
[328]:		Countries	1963-1964	1964-1965	196	5-1966	1966 ⁻	-1967	1967	7-1968	196	8-1969	\
	0	${\tt Germany}$	830	760		953		845		913		776	
	1	England	1132	1061		953		895		982		890	
	2	France	721	701		967		801		771		585	
	3	Spain	495	495		499		578		576		491	
	4	Italy	373	457		466		468		383		415	
		1969-1970	1970-1971	1971-1972	•••	2015-20	016	2016-20)17	2017-20)18	\	
	0	881	869	940	•••	3	360	3	360	3	390		
	1	836	736	783	•••	2	297	2	291	2	275		
	2	699	759	788	•••	5	552	6	803	5	515		
	3	516	474	596	•••	5	573	6	347	5	84		
	4	396	423	427		4	139	4	172	4	131		

```
2018-2019
              2019-2020 2020-2021 2021-2022
                                                 2022-2023
                                                              2023-2024
                                                                            sum
0
                                                                          39164
         384
                     364
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                                             618
         417
                     424
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                                             392
                                                        310
                                                                    321
                                                                          27814
```

[5 rows x 63 columns]

```
[329]: # Create a sub-dataframe that includes only the 5 nations with the most overall
       ⇔goals between 1994-2004
       thirty_years_ago = df.iloc[:5, [0,32,33,34,35,36,37,38,39,40,41]]
       # Add a column with its mean, use np.floor to avoid fractional goals.
       thirty_years_ago['Mean'] = np.floor(thirty_years_ago.iloc[:, 1:].mean(axis=1))
       # Make it an int.
       thirty_years_ago["Mean"] = thirty_years_ago["Mean"].astype(int)
       \# Create a sub-dataframe that includes only the 5 nations with the most overall \sqcup
        ⇔qoals between 2004-2014
       previous ten years = df.iloc[:5, [0,42,43,44,45,46,47,48,49,50,51]]
       # Add a column with its mean, use np.floor to avoid fractional goals.
       previous_ten_years['Mean'] = np.floor(previous_ten_years.iloc[:, 1:].
        →mean(axis=1))
       # Make it an int.
       previous_ten_years["Mean"] = previous_ten_years["Mean"].astype(int)
       # Create a sub-dataframe that includes only the 5 nations with the most overall,
       →goals between 2014-2024
       these ten_years = df.iloc[:5,[0,52,53,54,55,56,57,58,59,60,61]]
       # Add a column with its mean, use np.floor to avoid fractional goals.
       these_ten_years['Mean'] = np.floor(these_ten_years.iloc[:, 1:].mean(axis=1))
       # Make it an int.
       these_ten_years["Mean"] = these_ten_years["Mean"].astype(int)
```

[330]: thirty_years_ago

[330]:		Countries	1994-1995	1995-1996	1996-1997	1997-1998	1998-1999	1999-2000	\
	0	Germany	695	593	572	563	508	445	
	1	England	779	604	541	489	437	433	
	2	France	670	616	671	568	565	558	
	3	Spain	558	734	638	402	469	559	
	4	Italy	487	544	568	611	489	463	
		2000-2001	2001-2002	2002-2003	2003-2004	Mean			
	0	403	361	269	302	471			
	1	422	397	361	346	480			
	2	525	555	577	570	587			

```
560
       3
                 617
                                          564
                                                       552
                                                             565
       4
                 503
                              518
                                          538
                                                       518
                                                             523
[331]: previous_ten_years
          Countries
                      2004-2005
                                  2005-2006
                                               2006-2007
                                                           2007-2008
                                                                       2008-2009
                                                                                    2009-2010
[331]:
            Germany
                             317
                                         327
                                                     302
                                                                  292
                                                                              295
                                                                                           312
       1
            England
                             367
                                         355
                                                     323
                                                                  327
                                                                              310
                                                                                           342
       2
             France
                             482
                                         438
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                                                                  519
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       3
              Spain
                             513
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                             635
                                         626
                                                     673
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                                                                                          569
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           2010-2011
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                                               2013-2014
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       0
                 348
                              365
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                                                       619
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       4
                 522
                              475
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                                                       474
                                                             574
[332]:
       these_ten_years
[332]:
          Countries
                      2014-2015
                                  2015-2016
                                              2016-2017
                                                           2017-2018
                                                                       2018-2019
                                                                                    2019-2020
       0
            Germany
                             370
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            England
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       1
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             France
                             514
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       3
              Spain
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                             433
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              Italy
                                                     472
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           2020-2021
                       2021-2022
                                   2022-2023
                                                2023-2024
                                                            Mean
       0
                 351
                              365
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                                                             380
       1
                 372
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       3
                 613
                              618
                                          503
                                                       546
                                                             584
       4
                 374
                              392
                                                       321
                                          310
                                                             401
       1.1.3 Extract the data relevant to France
```

```
[333]: # Extract the France values for the seasons 2004-2014 in a dataframe france_previous_ten_years = previous_ten_years.iloc[2:3, □ → [1,2,3,4,5,6,7,8,9,10]].iloc[0]

# Extract the France values for the seasons 2014-2024 in a dataframe france_these_ten_years = these_ten_years.iloc[2:3, [1,2,3,4,5,6,7,8,9,10]].

→iloc[0]
```

1.1.4 T-test for two samples

We want to perform a t-test for two samples to check whether the mean goals of France have increased in these last 10 years compared to the previous last 10 years (2004-2014). To do so, we have to make sure that: - The samples are independent between each other and random - This is true because each year has different goals that do not depend on historical data. Moreover, the goals scored per season can be approximated to random since they depend on the players' performance year by year. - The samples are assumed to be normally distributed - A Shapiro-Wilk test will be performed to determine this. - The variances are equal. - Levene's test can be performed to determine this.

We will consider a level of significance of 0.01

```
[334]: # Set alpha as a global variable.
alpha = 0.01
```

Assess for normality: Shapiro-Wilk test For each sample: if the p-value is higher than alpha, then the null hypothesis stating that the sample follows a normal distribution cannot be rejected, i.e., the sample is normally distributed if p-value > alpha.

```
Shapiro-Wilk Test for France's goals from 2004 to 2014: W = 0.9478259459792676, p-value = 0.6428542654489622
Shapiro-Wilk Test for France's goals from 2014 to 2024: W = 0.9403216198196231, p-value = 0.556597672066893
Both samples are normally distributed? True
```

Therefore, the samples are normally distributed.

Assess for equal variances: Levene's test We execute the test simultaneously for both samples: if the p-value is higher than alpha, then the null hypothesis stating that the variances of the

samples are equal cannot be rejected, i.e., the samples' variances are equal if p-value > alpha.

```
Levene's Test for both samples: Statistic = 2.358587346422444 , p-value = 0.14198606565081504 Both samples' variances are equal? True
```

Therefore, the samples' variances are equal.

The samples are independent, randomly selected, uniformly distributed and have equal variances.

1.1.5 Let's perform the t-test for two samples

- Null Hypothesis (H0): previous >= this (the mean of the goals scored by French players in the top 5 European Football Leagues between the seasons 2003-2024 and 2013-2024 is greater than or equal to the mean of the seasons 2013-2014 to 2023-2024)
- Alternative Hypothesis (Ha): previous < this (the mean of the goals scored by French players in the top 5 European Football Leagues between the seasons 2003-2024 and 2013-2024 is less than the mean of the seasons 2013-2014 to 2023-2024)

```
[337]: # Using scipy module stats, a statistical test is perfroemd.

t_statistic, p_value_France_Germany = stats.

ttest_ind(france_previous_ten_years, france_these_ten_years,u

alternative="less")

print("p-value =", p_value_France_Germany)

print("Reject the null hypothesis in favor of the alternative hypothesis?

",p_value_France_Germany < alpha)
```

```
p-value = 0.001274605152448159
Reject the null hypothesis in favor of the alternative hypothesis? True
```

- 1.1.6 We are Sure with a 99% Confidence Level that the mean of goals scored of French players in Europe Top 5 Football leagues has increased in these last 10 years with resepct to the previous last 10 years (2004-2014)
- 1.2 Top 5 Leagues Historical Goals: Who will be at the top in the next decade
- 1.2.1 Let's interpret our findings regarding France.

France players have score more goals this last decade with respect to the previous one... does that mean that this trend will continue?

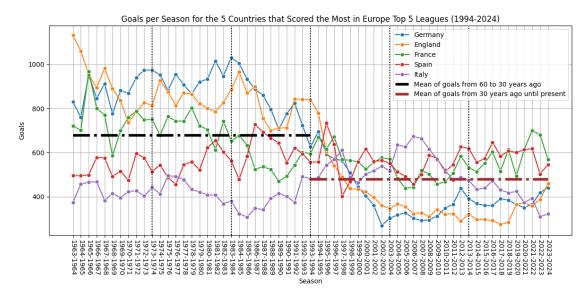
- Although computers and AI can do a lot for the Data Science domain, there is always the need for human insight. For example, it is true that France players have scored more this last decade, but does this mean that there will be a new increase the next decade? This is why it is very important to consider as much data as possible. In fact, this is why there is a different test for distributions of more than 30 samples.
- If we had only consider the previous result, we would have assumed an increase for the next decade, or we could have thought that it is reasonable to consider the average of the lsat decade only. However, this is a bad approximation. Goals scored by players per nation naturally vary throughout time.
- Modern football (the last 30 years) has become a more defensive game, leading to less goals. Moreover, globalization of the sport has brought great players from different countries, reducing the total sum of this historically frequent scoring countries. ##### This will be shown in the next graph

```
[338]: # Reshape the DataFrame using melt
                df melted = df.iloc[:5, :-1].melt(id vars='Countries', var name='Season', |
                   ⇔value_name='Goals')
                # Calculate the average for the first 30 years of the database and these last \Box
                   →30 years
                average_60_to_30_years_ago_top_countries = df.iloc[0:5, 1:32].mean().mean()
                average_30_to_present = df.iloc[0:5, 32:-1].mean().mean()
                print("From 1963-1993, on average, the top 5 countries scored", int(np.
                   floor(average_60_to_30_years_ago_top_countries-average_30_to_present)), __
                   →"goals than in the past 30 years.")
                # Create the line plot using Countries as hue
                plt.figure(figsize=(12, 6))
                sns.lineplot(data=df_melted, x='Season', y='Goals', hue='Countries', marker='o')
                # Title and labels of the plot
                plt.title('Goals per Season for the 5 Countries that Scored the Most in Europe⊔
                   →Top 5 Leagues (1994-2024)')
                plt.xticks(rotation=-90)
                plt.ylabel('Goals')
                plt.xlabel('Season')
                # Horizontal lines to show the average in their respective timeframe
                plt.hlines(y=average_60_to_30_years_ago_top_countries, xmin="1963-1964",_
                   oxmax="1993-1994", label="Mean of goals from 60 to 30 years ago", □
                   plt.hlines(y=average 30_to_present, xmin="1993-1994", xmax="2023-2024", __
                   ار العام العام العام العام والعام العام ا
                   →linestyle='-.', linewidth=4)
                # Vertical dotted lines to show decade division
                plt.axvline(x="1973-1974", color="black", linestyle='dotted')
```

```
plt.axvline(x="1983-1984", color="black", linestyle='dotted')
plt.axvline(x="1993-1994", color="black", linestyle='dotted')
plt.axvline(x="2003-2004", color="black", linestyle='dotted')
plt.axvline(x="2013-2014", color = "black", linestyle='dotted')

# Visualization
plt.grid()
plt.legend()
plt.tight_layout()
plt.show()
```

From 1963-1993, on average, the top 5 countries scored 198 goals than in the past 30 years.



As shown in the graph, there is a clear difference in these last 30 years compare to the previous ones.

• Moreover, the scoring trends in the last 30 years seems to have stabilized.

Which nation will be on top by the next decade?

• It would be interesting to consider the cumulative goals in the top 5 leagues since the birth of the most recent league (Bundesliga).

```
[339]: # Cumulative goals since 1963-1964. Table sorted by total sum df.iloc[:, [0,62]].sort_values("sum", ascending = False).head()
```

[339]: Countries sum 0 Germany 39164

```
1 England 37995
2 France 37713
3 Spain 34409
4 Italy 27814
```

4

Germany is on top currently, but how likely is it for them to stay on the top for another decade? Let's dive deeper into the average goals scored per decade these last years.

```
[340]: | # Concatenate all the means per decade to visualize it more easily.
      means_table = pd.concat([thirty_years_ago.iloc[:, [0,-1]], previous_ten_years.
        →iloc[:, [-1]], these_ten_years.iloc[:, [-1]]], axis=1)
       # Create an overall mean as int
      means_table["Mean Modern Football"] = np.floor(means_table.iloc[:, 1:].
        →mean(axis=1))
      means table["Mean Modern Football"] = means table["Mean Modern Football"].
        →astype(int)
      # Add the total goals sum per country
      means_table = pd.concat([means_table, df.iloc[0:5, [-1]]], axis=1)
      # Rename the columns
      means_table.columns = ["Countries", "Mean 30-20 years ago", "Mean 20-10 years_
        ⇒ago", "Mean 10 years ago to present", "Overall Mean Past 30 years", "Total
       # Show the table
      means_table.reset_index(drop=True, inplace=True)
      means table
```

[340]:	Countries	Mean 30-20	years ag	o Mean	20-10	years ag	;o \	
0	Germany		47	1		33	88	
1	England		48	0		32	27	
2	France		58	7		49	3	
3	Spain		56	5		54	2	
4	Italy		52	3		57	' 4	
	Mean 10 y	ears ago to	present	Overal	l Mean	Past 30	years	Total goals sum
0			380				396	39164
1			338				381	37995
2			585				555	37713
3			584				563	34409

401

Who could dethrone Germany in the next decade? Let's analyze the Overall Mean of goals per season in the past 30 years and the historical sum of goals. - England has had less goals on average this past 30 years per season than Germany. They cannot beat Germany. - Italy is more than 12000 goals away, they cannot dethrone Germany. - Spain and France have scored on average the same amount of goals per season (\pm 8 goals) in these last 30 years. Therefore, the closest one to Germany is the best candidate. This is France

499

27814

1.2.2 France vs Germany: race for gold

Let's perform a Normal Distribution problem where we provide the population standard deviations of means for each country. We will do a Linear Combination of random independent variables: - Var(1F - 1G) = 12xVar(F) + (-1)2xVar(F) - E(1F - 1G) = 1x F - 1x G

We are evaluating over 30 different seasons, so z-tests can be performed

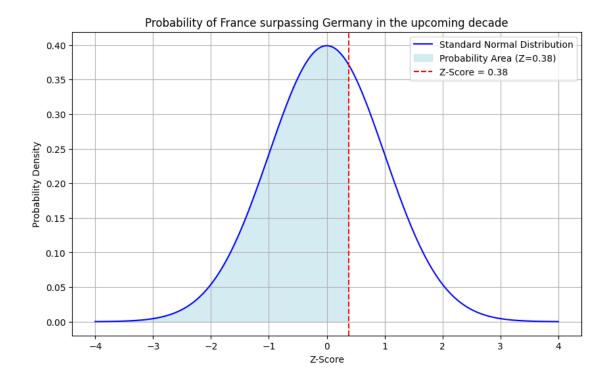
```
[341]: # Historical averages and population standard deviations. Also the current lead
       →in accumulated goals is calculated
      avg_france_goals_last_30 = means_table.iloc[2,4]
      avg_germany_goals_last_30 = means_table.iloc[0,4]
      std_france_goals_last_30 = df.iloc[2, 32:-1].std()
      std_germany_goals_last_30 = df.iloc[4, 32:-1].std()
      current_lead_germany = means_table.iloc[0,5] - means_table.iloc[2,5]
       # Number of seasons to project
      n_seasons = 10
       # Linear combination of continuous random independent variables
      mean_difference = avg_france_goals_last_30 - avg_germany_goals_last_30
      std_france_and_germany = np.sqrt(std_france_goals_last_30**2 +__
       ⇒std_germany_goals_last_30**2)
       # Account for 10 years (it is NOT a linear combination, the variance gets \Box
       →multiplied by 10 and not 10 squared.)
      mean_diff_10_years = mean_difference * n_seasons # Cumulative mean difference_
       ⇔over 10 seasons
      std_diff_10_years = std_france_and_germany * np.sqrt(n_seasons) # Cumulative_
        standard deviation over 10 seasons
       # Calculate the Z-score for the current lead of Germany
      z_score = (mean_diff_10_years - current_lead_germany) / std_diff_10_years
      probability = norm.cdf(z_score)
      # Calculate the probability using the standard normal distribution
      p_value_france_germany = round(1 - probability,4)
      print(p_value_france_germany)
      # Output the result
      print(f"Probability that France will surpass Germany in {n_seasons} seasons:
       print(f"Reject null hypothesis (France surpasses Germany)?", 
        →p_value_france_germany < alpha )</pre>
```

0.3538

Probability that France will surpass Germany in 10 seasons: 64.62122179514941% Reject null hypothesis (France surpasses Germany)? False

We cannot conclude that France will surpass Germany with a 95% confidence level. The probability that France does surpass Germany is 64.62% ### Let's visualize the findings

```
[342]: # Create an array of x values from -4 to 4
       x = np.linspace(-4, 4, 1000)
       # Calculate the y values for the normal distribution
       y = norm.pdf(x)
       # Create the plot
       plt.figure(figsize=(10, 6))
       plt.plot(x, y, label='Standard Normal Distribution', color='blue')
       # Shade the area under the curve to the right of the Z-score
       plt.fill_between(x, y, where=(x <= z_score), color='lightblue', alpha=0.5,
        →label=f'Probability Area (Z={z_score:.2f})')
       # Vertical line for the Z-score
       plt.axvline(z_score, color='red', linestyle='--', label=f'Z-Score = {z_score:.
        # Add labels and title
       plt.title('Probability of France surpassing Germany in the upcoming decade')
       plt.xlabel('Z-Score')
       plt.ylabel('Probability Density')
       plt.legend()
       plt.grid()
       # Show the plot
       plt.show()
```



1.2.3 Findings

- The whole point of this code is to show that it is easy to jump into wrong conclusions when not all the data is present.
- The increase of goals scored per season by France in the top 5 leagues in this decade with respect to the previous one is a fact (the null hypothesis was indeed rejected). However, this doesn't mean that the goals on next decade will also increase. Moreover, it doesn't even mean that the average will stay the same. It is necessary to account for as much data as possible.
- In this case, it was found that France has been rather monotonous this past 30 years in terms of goals scored per season in Europe's top 5 Football leagues.
- Furthermore, we were interested in predicting when is Germany going to be dethroned by most likely France. It was found that this is rather unlikely (64.62%) by the next decade. However, if the statistics follow the assumptions made, France will surpass Germany in 13 years and 7 months.