

# The Determinant and the Inverse

Recall that a matrix,  $A \in \mathbb{R}^{n \times n}$  is invertible if and only if  $\det(A) \neq 0$ .

But what about  $\det(A^{-1})$ ?

We claim that  $\det(A^{-1}) = \frac{1}{\det(A)}$ .

## Finding $\det(A^{-1})$

Let  $A \in \mathbb{R}^{n \times n}$  such that  $\det(A) \neq 0$ . Since we know that for all  $A, B \in \mathbb{R}^{n \times n}$ ,  $\det(AB) = \det(A)\det(B)$ , we have:

$$\begin{aligned} 1 &= \det(I_n) \\ &= \det(AA^{-1}) \\ &= \det(A)\det(A^{-1}) \\ \frac{1}{\det(A)} &= \det(A^{-1}) \end{aligned}$$

## Last Content on Exam 1

The previous two slides are the last content that is fair game for the first exam