# Boolean Combinations of Weighted Voting Games

Juan Pablo Royo Sales

Universitat Politècnica de Catalunya

January 2020

- Introduction
- 2 Preliminary Definitions
- 3 Boolean Weighted Voting Games
- 4 Shapley Value
- The Core

- Introduction
- 2 Preliminary Definitions
- 3 Boolean Weighted Voting Games
- 4 Shapley Value
- 5 The Core

#### Introduction

#### **Basic Notions**

- Based on Boolean Combinations of Weighted Voting Games paper BWVG<sup>1</sup>
- It is a natural Generalization over Weighted Voting Games
- Intuitively is a decision making process via multiple committees
- Each committee has the authority to decide the outcome "yes" or "no" about an issue.
- And each committee is a WVG
- Individuals can appear in multiple committees
- Different committees can have different Threshold values

<sup>&</sup>lt;sup>1</sup>Piotr Faliszewski, Edith Elkind, and Michael Wooldridge. 2009. Boolean combinations of weighted voting games. In Proceedings of The 8th International Conference on Autonomous Agents and Multiagent Systems - Volume 1 (AAMAS '09). International Foundation for Autonomous Agents and Multiagent Systems, Richland, SC, 185–192.

#### Introduction

#### Questions to be answered?

- Which coalitions might be able to bring the goal about?
- How important is a particular individual with respect to the achievement of the goal?

#### Introduction

#### Goals of the Paper

- Formal Definition of BWVG
- Investigate Computational Properties of BWVG

- Introduction
- 2 Preliminary Definitions
- Boolean Weighted Voting Games
- 4 Shapley Value
- 5 The Core

### Preliminary Definitions

#### Propositional Logic

- Let  $\Phi = \{p, q, \dots\}$  be a fixed non-empty vocabulary of Boolean variables
- ullet Let  ${\cal L}$  denote the set of formulas of propositional logic over  $\Phi$
- If " $\vee$ " and " $\wedge$ " are the only operators appearing in formula  $\varphi$ , se say that  $\varphi$  is **monotone**
- If  $\xi \subseteq \Phi$ , we write  $\xi \models \varphi$  mean that  $\varphi$  is true satisfied by valuation  $\xi$

- Introduction
- Preliminary Definitions
- 3 Boolean Weighted Voting Games
- 4 Shapley Value
- 5 The Core

### Boolean Weighted Voting Games

asdfasfsd

- Introduction
- 2 Preliminary Definitions
- Boolean Weighted Voting Games
- 4 Shapley Value
- 5 The Core

# Shapley Value

as d fasfs d

- Introduction
- Preliminary Definitions
- 3 Boolean Weighted Voting Games
- 4 Shapley Value
- The Core

#### The Core

as d fas fs d

# Thank you!!