



Algorithmic Methods for Mathematical Models (AMMM)

Local Search

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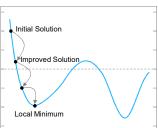
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Local Search (LS)

- LS is as an iterative search procedure that, starting from an initial feasible solution, progressively improves it by applying a series of local modifications (or moves).
- At each iteration, the search moves to an improving feasible solution that differs only slightly from the current one.
- The search terminates when it encounters a local optimum with respect to the transformations that it considers.



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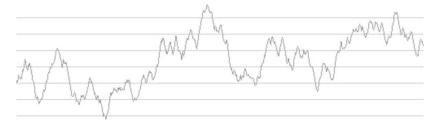
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Quality of the solutions

• Unless one is extremely lucky, this local optimum is often a **fairly mediocre solution**.



 The quality of the solution and computing times are usually highly dependent upon the "richness" of the set of moves considered at each iteration.

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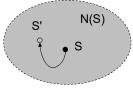


Algorithm and Search Strategies

Given a solution Swhile S is not locally optimal **do** Find S' in N(S) s.t. f(S') < f(S) $S \leftarrow S$ '

return S

 N(S) is the set of solutions that can be created by exchanging elements in the solution and elements not in the solution.



- A new solution is then created by removing from the solution a set A of elements in S and adding to the solution another set B not in S, where |A|>0 and |B|≥0.
- Examples:
 - **Removing one** element from S (|A|=1 and |B|=0)
 - Removing by exchanging two elements in S and adding one element in C\S (|A|=2 and |B|=1).
 - Exchanging one element in S and adding one element in C\S (|A|=1 and |B|=1).
- Simple neighborhoods (N(S)) are usually defined.

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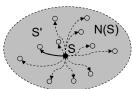
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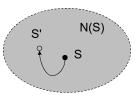




Search Strategies

- The neighborhood search may be implemented using either a *best-improving* or a *first-improving* strategy.
 - Best-improving strategy: all neighbors are investigated and the current solution is replaced by the best neighbor.
 - First-improving strategy: the current solution moves to the first neighbor whose cost function value is smaller than that of the current solution.

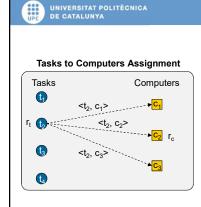




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Neighborhoods

- Reassignment neighborhood: reassignment of a task from a computer to another (one-element exchange).
 - Advantages: Easy and flexible: O(|T|*|C|)
 - Weaknesses: Limited improvement is obtained when computers are very busy.



- Assignment exchange neighborhood: reassignment of tasks between computers (k=1). (two-element exchange).
 - Advantages: the number of feasible exchanges is increased
 - Weaknesses: higher complexity O(|T|²) and maintains the structure of the solution from the one obtained with a greedy.



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