PROBLEM 1.35

KNOWN: Thickness and initial temperature of an aluminum plate whose thermal environment is changed.

FIND: (a) Initial rate of temperature change, (b) Steady-state temperature of plate, (c) Effect of emissivity and absorptivity on steady-state temperature.

SCHEMATIC:

Air
$$T_{\infty} = 20 \, ^{\circ}\text{C}$$
 $h = 20 \, ^{\circ}\text{C}$ $h = 20 \, ^{\circ}\text{C}$ $h = 20 \, ^{\circ}\text{C}$ $h = 20 \, ^{\circ}\text{C}$ Special coating $\alpha_S = 0.80$ $\alpha_S = 0.80$ $\alpha_S = 0.25$ Initial temperature, $\alpha_S = 0.25$

ASSUMPTIONS: (1) Negligible end effects, (2) Uniform plate temperature at any instant, (3) Constant properties, (4) Adiabatic bottom surface, (5) Negligible radiation from surroundings, (6) No internal heat generation.

ANALYSIS: (a) Applying an energy balance, Eq. 1.11a, at an instant of time to a control volume about the plate, $\dot{E}_{in} - \dot{E}_{out} = \dot{E}_{st}$, it follows for a unit surface area.

$$\alpha_{\rm S}G_{\rm S}\left(1\,\mathrm{m}^2\right) - \mathrm{E}\left(1\,\mathrm{m}^2\right) - q_{\rm conv}''\left(1\,\mathrm{m}^2\right) = \left(\mathrm{d}/\mathrm{d}t\right)\left(\mathrm{McT}\right) = \rho\left(1\,\mathrm{m}^2 \times \mathrm{L}\right)\mathrm{c}\left(\mathrm{d}\mathrm{T}/\mathrm{d}t\right).$$

Rearranging and substituting from Eqs. 1.3 and 1.5, we obtain

$$dT/dt = (1/\rho Lc) \left[\alpha_S G_S - \varepsilon \sigma T_i^4 - h \left(T_i - T_\infty \right) \right].$$

$$dT/dt = \left(2700 \text{ kg/m}^3 \times 0.004 \text{ m} \times 900 \text{ J/kg} \cdot \text{K} \right)^{-1} \times$$

$$\left[0.8 \times 900 \text{ W/m}^2 - 0.25 \times 5.67 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4 \left(298 \text{ K} \right)^4 - 20 \text{ W/m}^2 \cdot \text{K} \left(25 - 20 \right)^\circ \text{C} \right]$$

$$dT/dt = 0.052^\circ \text{ C/s} .$$

(b) Under steady-state conditions, $\dot{E}_{\text{st}}=0,$ and the energy balance reduces to

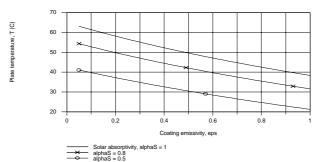
$$\alpha_{S}G_{S} = \varepsilon\sigma T^{4} + h(T - T_{\infty})$$

$$0.8 \times 900 \text{ W/m}^{2} = 0.25 \times 5.67 \times 10^{-8} \text{ W/m}^{2} \cdot \text{K}^{4} \times \text{T}^{4} + 20 \text{ W/m}^{2} \cdot \text{K}(T - 293 \text{ K})$$
(2)

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The solution yields $T = 321.4 \text{ K} = 48.4^{\circ}\text{C}$.

(c) Using the IHT First Law Model for an Isothermal Plane Wall, parametric calculations yield the following results.



COMMENTS: The surface radiative properties have a significant effect on the plate temperature, which decreases with increasing ε and decreasing α_S . If a low temperature is desired, the plate coating should be characterized by a large value of ε/α_S . The temperature also decreases with increasing h.