# Mini Project

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Load libraries

```
library(ggplot2)
library(factoextra)
```

## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa
library(rgl)

## Exploratroy data analysis

#### Organizing the data

First I read in the data from 'WisconsinCancer.csv" with the first column as the row names.

```
fna_data <- "WisconsinCancer.csv"
wisconsin_df <- read.csv(fna_data, row.names = 1)</pre>
```

Then I look at the data to asses the structure of the data.

str(wisconsin\_df)

```
## 'data.frame':
                    569 obs. of
                               32 variables:
                                    "M" "M" "M" "M" ...
##
   $ diagnosis
                             : chr
## $ radius_mean
                             : num
                                    18 20.6 19.7 11.4 20.3 ...
## $ texture_mean
                             : num
                                    10.4 17.8 21.2 20.4 14.3 ...
## $ perimeter_mean
                             : num
                                    122.8 132.9 130 77.6 135.1 ...
## $ area mean
                             : num
                                    1001 1326 1203 386 1297 ...
## $ smoothness_mean
                             : num
                                    0.1184 0.0847 0.1096 0.1425 0.1003 ...
## $ compactness_mean
                             : num
                                    0.2776 0.0786 0.1599 0.2839 0.1328 ...
##
   $ concavity_mean
                             : num
                                    0.3001 0.0869 0.1974 0.2414 0.198 ...
##
                                    0.1471 0.0702 0.1279 0.1052 0.1043 ...
   $ concave.points_mean
                             : num
## $ symmetry_mean
                                    0.242 0.181 0.207 0.26 0.181 ...
                             : num
## $ fractal_dimension_mean :
                                    0.0787 0.0567 0.06 0.0974 0.0588 ...
                              num
##
   $ radius_se
                             : num
                                    1.095 0.543 0.746 0.496 0.757 ...
## $ texture_se
                                    0.905 0.734 0.787 1.156 0.781 ...
                             : num
## $ perimeter_se
                            : num
                                    8.59 3.4 4.58 3.44 5.44 ...
                                    153.4 74.1 94 27.2 94.4 ...
## $ area_se
                             : num
                                    0.0064 0.00522 0.00615 0.00911 0.01149 ...
##
   $ smoothness_se
                            : num
                                    0.049 0.0131 0.0401 0.0746 0.0246 ...
## $ compactness se
                            : num
## $ concavity_se
                             : num
                                    0.0537 0.0186 0.0383 0.0566 0.0569 ...
                                    0.0159 0.0134 0.0206 0.0187 0.0188 ...
## $ concave.points_se
                             : num
   $ symmetry_se
                                    0.03 0.0139 0.0225 0.0596 0.0176 ...
                             : num
                                    0.00619 0.00353 0.00457 0.00921 0.00511 ...
## $ fractal_dimension_se
                             : num
## $ radius_worst
                             : num 25.4 25 23.6 14.9 22.5 ...
```

```
## $ texture_worst
                                     17.3 23.4 25.5 26.5 16.7 ...
                             : num
                                      184.6 158.8 152.5 98.9 152.2 ...
## $ perimeter_worst
                             : num
## $ area worst
                             : num
                                      2019 1956 1709 568 1575 ...
## $ smoothness_worst
                                      0.162 0.124 0.144 0.21 0.137 ...
                              : num
## $ compactness_worst : num 0.666 0.187 0.424 0.866 0.205 
## $ concavity_worst : num 0.712 0.242 0.45 0.687 0.4 ...
                                      0.666 0.187 0.424 0.866 0.205 ...
## $ concave.points_worst : num
                                      0.265 0.186 0.243 0.258 0.163 ...
## $ symmetry_worst
                              : num
                                      0.46 0.275 0.361 0.664 0.236 ...
    $ fractal_dimension_worst: num    0.1189    0.089    0.0876    0.173    0.0768    ...
##
                               : logi NA NA NA NA NA NA ...
```

The first row contains the diagnoses which are the outputs we are trying to derive from the data. This will be removed to generate the naive dataframe. Additionally, these results are saved as the vector 'diagnosis'.

```
# The data seems to have a extraneous ',' at the end of the column names
# Take out the artifact column 'X' from the read-in.
naive_wisconsin_df <- wisconsin_df[,c(-1, -ncol(wisconsin_df))]
diagnosis <- factor(wisconsin_df[,1])</pre>
```

#### Explore the data

```
nrow(wisconsin_df)
```

[Q01]: How many observations are in the dataset?

## [1] 569

There are 569 rows/observations.

```
table(diagnosis)
```

[Q02]: How many of the observations have a malignant diagnoses?

```
## diagnosis
## B M
## 357 212
```

212 of the observations have a "M" or malignant diagnoses.

```
length(grep("_mean", colnames(naive_wisconsin_df)))
```

[Q03]: How many variables/features in the data are suffixed with \_mean?

## [1] 10

There are 10 variables/features (columns) which are suffixed with \_mean.

## Principal Component Analysis

#### Performing PCA

Check the means and Standard deviations of the variables.

```
colMeans(naive_wisconsin_df)
```

```
##
               radius mean
                                        texture mean
                                                               perimeter mean
              1.412729e+01
                                        1.928965e+01
                                                                 9.196903e+01
##
##
                  area mean
                                     smoothness mean
                                                             compactness mean
##
              6.548891e+02
                                        9.636028e-02
                                                                  1.043410e-01
##
            concavity mean
                                 concave.points_mean
                                                                symmetry mean
              8.879932e-02
                                        4.891915e-02
                                                                 1.811619e-01
##
##
    fractal dimension mean
                                           radius se
                                                                    texture se
##
              6.279761e-02
                                        4.051721e-01
                                                                  1.216853e+00
##
              perimeter_se
                                                                 smoothness se
                                             area_se
##
              2.866059e+00
                                        4.033708e+01
                                                                 7.040979e-03
            compactness_se
                                        concavity_se
                                                            concave.points_se
##
              2.547814e-02
                                        3.189372e-02
                                                                  1.179614e-02
##
                                                                 radius_worst
               symmetry_se
                               fractal_dimension_se
##
              2.054230e-02
                                        3.794904e-03
                                                                  1.626919e+01
##
             texture_worst
                                     perimeter_worst
                                                                    area_worst
##
              2.567722e+01
                                        1.072612e+02
                                                                  8.805831e+02
##
          smoothness_worst
                                   compactness_worst
                                                              concavity_worst
##
              1.323686e-01
                                        2.542650e-01
                                                                  2.721885e-01
##
      concave.points_worst
                                      symmetry_worst fractal_dimension_worst
##
              1.146062e-01
                                        2.900756e-01
                                                                  8.394582e-02
apply(naive_wisconsin_df, 2, sd)
##
               radius_mean
                                        texture_mean
                                                               perimeter_mean
##
              3.524049e+00
                                        4.301036e+00
                                                                  2.429898e+01
```

## area\_mean smoothness\_mean compactness\_mean ## 3.519141e+02 1.406413e-02 5.281276e-02 ## concavity mean concave.points mean symmetry mean 7.971981e-02 ## 3.880284e-02 2.741428e-02 ## fractal dimension mean radius\_se texture se ## 7.060363e-03 5.516484e-01 2.773127e-01 ## perimeter\_se smoothness\_se area\_se ## 2.021855e+00 4.549101e+01 3.002518e-03 ## compactness\_se concavity\_se concave.points\_se ## 1.790818e-02 3.018606e-02 6.170285e-03 ## symmetry\_se fractal\_dimension\_se radius\_worst ## 8.266372e-03 2.646071e-03 4.833242e+00 ## texture\_worst perimeter\_worst area\_worst ## 6.146258e+00 3.360254e+01 5.693570e+02 ## smoothness\_worst compactness\_worst concavity\_worst ## 2.283243e-02 1.573365e-01 2.086243e-01 ## symmetry\_worst fractal\_dimension\_worst concave.points\_worst ## 6.573234e-02 6.186747e-02 1.806127e-02

Run the 'prcomp()' on the Wisconsin dataframe with scaling to account for different variables having varying scales of values.

```
wisconsin_pca <- prcomp(naive_wisconsin_df, scale = TRUE)
summary(wisconsin_pca)</pre>
```

```
## Importance of components:

## Standard deviation 3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172

## Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251

## Cumulative Proportion 0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010
```

```
##
                              PC8
                                     PC9
                                            PC10
                                                   PC11
                                                            PC12
                                                                    PC13
                                                                            PC14
## Standard deviation
                          0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
## Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
## Cumulative Proportion 0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
                             PC15
                                     PC16
                                             PC17
                                                     PC18
                                                              PC19
                                                                      PC20
                          0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
## Standard deviation
## Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
## Cumulative Proportion 0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
##
                             PC22
                                     PC23
                                            PC24
                                                    PC25
                                                             PC26
                                                                     PC27
                                                                             PC28
                          0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
## Standard deviation
## Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
## Cumulative Proportion 0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
##
                             PC29
                                     PC30
## Standard deviation
                          0.02736 0.01153
## Proportion of Variance 0.00002 0.00000
## Cumulative Proportion 1.00000 1.00000
```

```
summary(wisconsin_pca)$importance[2,1]
```

[Q04]: From your results, what proportion of the original variance is captured by the first principal component (PC1)?

## [1] 0.44272

0.44272 is the proportion of the variance captured by PC 1.

```
PC <- which(summary(wisconsin_pca)$importance[3,] >= 0.7)[1]
PC
```

[Q05]: How many principal components (PCs) are required to describe at least 70% of the original variance in the data?

## PC3 ## 3

summary(wisconsin\_pca)\$importance[3,PC]

## [1] 0.72636

Three PCs [PC1 - PC3], explains 72.636% of the original variance.

```
PC <- which(summary(wisconsin_pca)$importance[3,] >= 0.9)[1]
PC
```

[Q06]: How many principal components (PCs) are required to describe at least 90% of the original variance in the data?

## PC7 ## 7

summary(wisconsin\_pca)\$importance[3,PC]

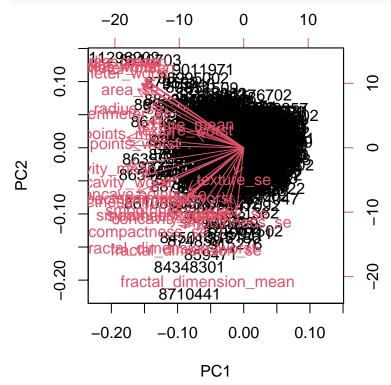
## [1] 0.9101

Seven PCs [PC1 - PC7], explains 91.010%.

## **Interpreting PCA Results**

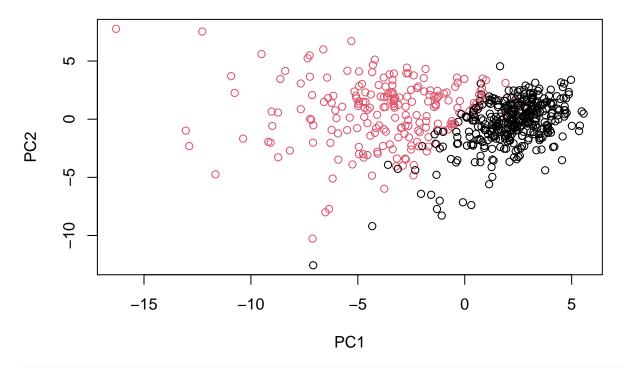
Biplot for the Wisconsin cancer data set principal component analysis.

biplot(wisconsin\_pca)

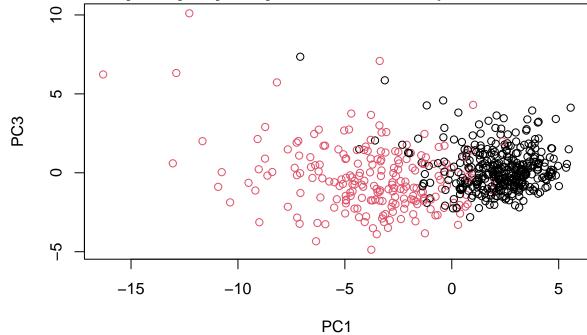


[Q07]: What stands out to you about this plot? Is it easy or difficult to understand? Why? While it shows a lot of data regarding the influence of each variable on the the visualized PCs, it is a bit overwhelming and difficult to extract any useful information from it.

Distribution of data points on PCs 1 and 2.



[Q08]: Generate a similar plot for principal components 1 and 3. What do you notice about these

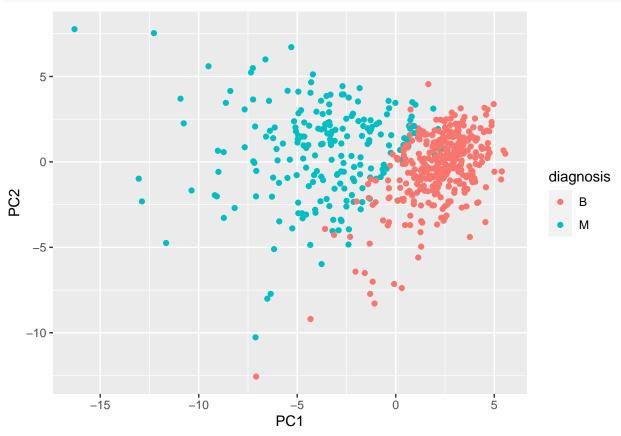


Since this plot uses PC 3 instead of PC 2, which explains less of the total variance than PC 2 does, the two groups in the data set, Benign and Malignant, appear less distinct.

plots?

#### Using ggplot

```
wisconsin_pca_df <- as.data.frame(wisconsin_pca$x)
wisconsin_pca_df$diagnosis <- diagnosis</pre>
```

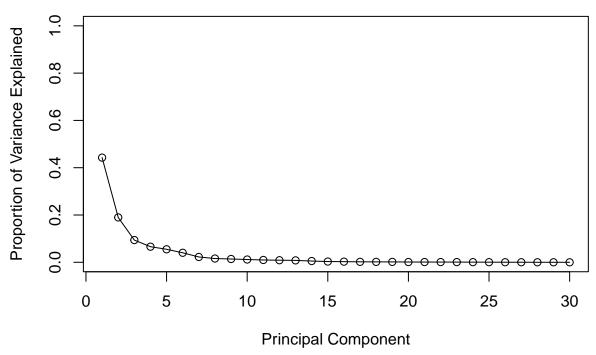


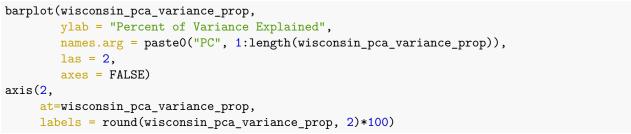
### Variance Explained

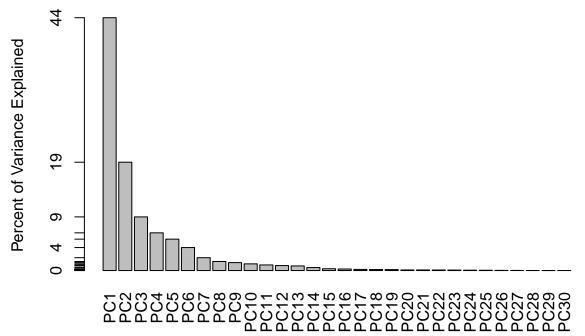
```
wisconsin_pca_variance <- wisconsin_pca$sdev^2
head(wisconsin_pca_variance)</pre>
```

```
## [1] 13.281608 5.691355 2.817949 1.980640 1.648731 1.207357
wisconsin_pca_variance_prop <- wisconsin_pca_variance / sum(wisconsin_pca_variance)
```

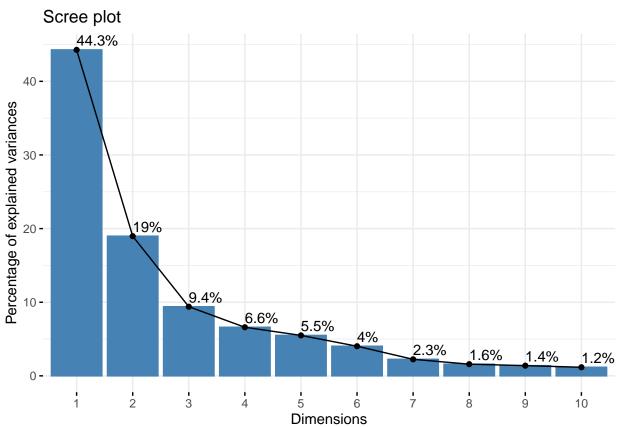
Scree Plots







#### Using the 'factoextra' package



#### Communicatin PCA Results

wisconsin\_pca\$rotation[grep("concave.points\_mean", row.names(wisconsin\_pca\$rotation)),1]

[Q09] For the first principal component, what is the component of the loading vector (i.e. wisc.pr\$rotation[,1]) for the feature concave.points\_mean?

## [1] -0.2608538

```
PC <- which(summary(wisconsin_pca)$importance[3,] >= 0.8)[1]
PC
```

[Q10] What is the minimum number of principal components required to explain 80% of the variance of the data?

## PC5 ## 5

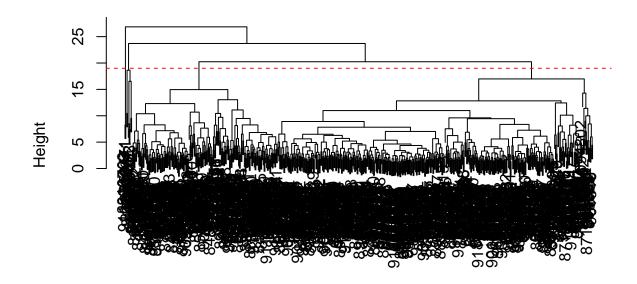
summary(wisconsin\_pca)\$importance[3,PC]

## [1] 0.84734

It takes a minimum of 5 PCs to explain 80% (84.734%) of the data.

## **Hierarchical Clustering**

[Q11]: Using the plot() and abline() functions, what is the height at which the clustering model **Cluster Dendrogram** 



wisconsin\_data\_distance hclust (\*, "complete")

#### has 4 clusters?

A height of 19 results in a clustering model with 4 clusters.

#### Selecting numbers of clusters

```
wisconsin_hclust_clusters_k4 <- cutree(wisconsin_data_hclust, k = 4)
table(wisconsin_hclust_clusters_k4, diagnosis)</pre>
```

```
## diagnosis
## wisconsin_hclust_clusters_k4 B M
## 1 12 165
## 2 2 5
## 3 343 40
## 4 0 2
```

```
for(i in 2:10){
  wisconsin_hclust_clusters <- cutree(wisconsin_data_hclust, k = i)
  cat(paste0(i, "\n", sep = ""))
  print(table(wisconsin_hclust_clusters, diagnosis))
}</pre>
```

[Q12]: Can you find a better cluster vs diagnoses match by cutting into a different number of clusters between 2 and 10?

```
## 2
##
                               diagnosis
## wisconsin_hclust_clusters
                                  В
                                      Μ
##
                              1 357 210
##
                                  0
                                      2
## 3
##
                               diagnosis
## wisconsin_hclust_clusters
                                  В
                              1 355 205
##
##
                              2
                                  2
                                      5
##
                              3
                                  0
                                      2
## 4
##
                               diagnosis
## wisconsin_hclust_clusters
                                  В
                                      М
                                12 165
##
##
                              2
                                  2
                                      5
##
                              3 343
                                     40
##
                                  0
                                      2
## 5
##
                               diagnosis
   {\tt wisconsin\_hclust\_clusters}
                                  В
##
##
                                 12 165
                              1
##
                              2
                                  0
                                      5
##
                              3 343
                                     40
                                  2
##
                                      0
##
                              5
                                  0
                                      2
##
                               diagnosis
##
##
   wisconsin_hclust_clusters
                                  В
##
                                12 165
##
                                  0
##
                              3 331
                                     39
##
                                  2
                                      0
                                 12
##
                              5
                                      1
##
                                  0
                                      2
##
##
                               diagnosis
##
   wisconsin_hclust_clusters
                                  В
                                 12 165
##
##
                              2
                                  0
                                      3
##
                              3 331
                                     39
##
                                  2
                                      0
##
                                12
                              5
                                      1
##
                                  0
                                      2
```

```
##
                                  0
## 8
##
                               diagnosis
## wisconsin_hclust_clusters
                                   В
##
                                  12
                                      86
##
                              2
                                   0
                                      79
##
                              3
                                   0
                              4 331
                                      39
##
##
                                  2
                                       0
##
                              6
                                 12
                                       1
##
                                       2
                                   0
                                       2
##
                              8
##
##
                               diagnosis
   wisconsin_hclust_clusters
                                  В
                                       Μ
##
                                  12
                                      86
##
                              2
                                   0
                                      79
##
                              3
                                   0
                                       3
##
                              4 331
                                      39
##
                                   2
                                       0
##
                              6
                                 12
                                       0
##
                              7
                                       2
##
                                   0
                                       2
                              8
##
## 10
                               diagnosis
##
   wisconsin_hclust_clusters
                                  В
##
                                  12
                                      86
                             1
                             2
                                      59
##
                                   0
##
                             3
                                   0
                                       3
##
                             4
                                331
                                      39
##
                             5
                                  0
                                      20
                             6
                                   2
##
                                       0
                             7
##
                                  12
                                       0
                             8
                                       2
##
                                   0
##
                             9
                                   0
                                       2
##
                             10
                                   0
```

### Using different methods

```
table(wisconsin_hclust_clusters_single, diagnosis)

[Q13]: Which method gives your favorite results for the same data.dist dataset? Explain your reasoning.
```

table(wisconsin\_hclust\_clusters\_average, diagnosis)

table(wisconsin\_hclust\_clusters\_wardD2, diagnosis)

table(wisconsin\_hclust\_clusters\_complete, diagnosis)

```
## diagnosis
## wisconsin_hclust_clusters_complete B M
## 1 357 210
## 2 0 2
```

Ward.D2 is my favorite since it is effective at splitting the data points into two groups which can differentiate between benign and malignant observations, unlike 'single', 'average', or 'complete' which essentially lump all of these observations together.

## K-means clustering

```
wisconsin_kmeans <- kmeans(wisconsin_data_scaled, centers = 2, nstart = 20)</pre>
```

```
table(wisconsin_kmeans$cluster, diagnosis)
```

[Q14]: How well does k-means separate the two diagnoses? How does it compare to your helust results?

```
## diagnosis
## B M
## 1 343 37
## 2 14 175
```

table(wisconsin\_hclust\_clusters\_k4, diagnosis)

```
## diagnosis
## wisconsin_hclust_clusters_k4 B M
## 1 12 165
## 2 2 5
## 3 343 40
```

```
## 4 0 2
```

For K-means, the resolution of two 'distinct' groups is achieved at k=2 while a similar resolution for hierarchical clustering is achieved at k=4. Additionally, taking groups 1, 2 and 4 as Malignant and 3 as Benign, the false positive and false negative rate for hclust at k=4 are both higher than k-means at k=2.

Compare the cluster assignments between helust and k-means.

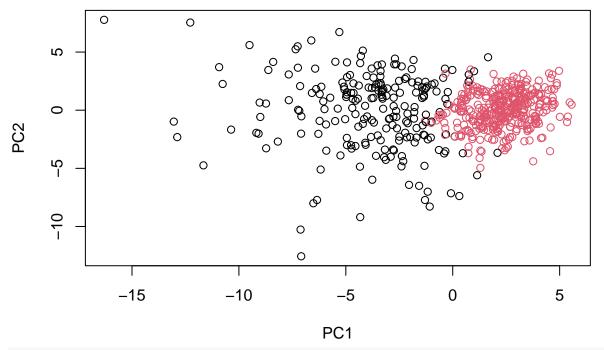
```
table(wisconsin_hclust_clusters_k4, wisconsin_kmeans$cluster)
```

```
## ## wisconsin_hclust_clusters_k4 1 2 ## 1 17 160 ## 2 0 7 ## 3 363 20 ## 4 0 2
```

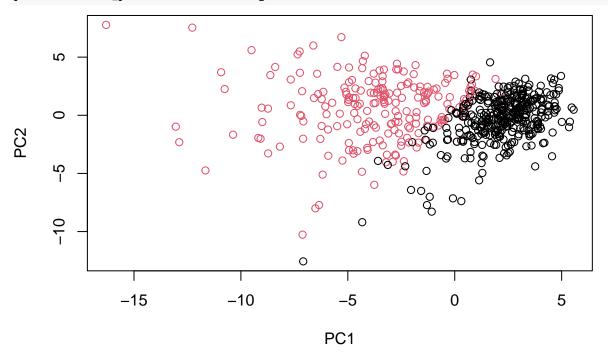
## Combining methods

### Clustering the PCA results

```
wisconsin_pr_hclust <- hclust(dist(wisconsin_pca$x[,1:7]), method = "ward.D2")</pre>
groups <- cutree(wisconsin_pr_hclust, k = 2)</pre>
table(groups)
## groups
##
   1
## 216 353
table(groups, diagnosis)
##
         diagnosis
## groups
            В
                 М
           28 188
##
        2 329
##
                24
Plot against PCs 1 and 2 while coloring by groups and then by diagnosis.
plot(wisconsin_pca$x[,1:2], col=groups)
```



plot(wisconsin\_pca\$x[,1:2], col=diagnosis)



The colors are flipped, so we can recolor by flipping the factor levels.

```
levels(re_group)

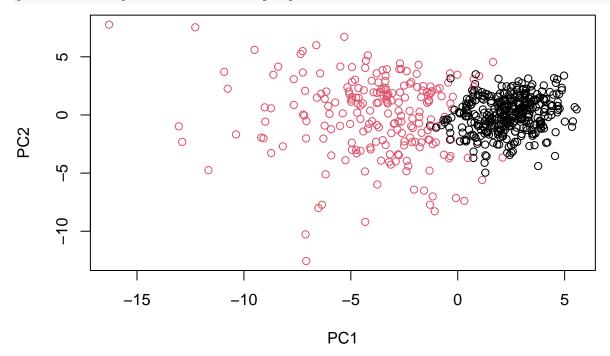
## [1] "1" "2"

re_group <- relevel(re_group, 2)
levels(re_group)</pre>
```

## [1] "2" "1"

re\_group <- as.factor(groups)</pre>

#### plot(wisconsin\_pca\$x[,1:2], col=re\_group)



Three dimensional plotting on PCs 1 through 3 while coloring by groups.

```
table(groups, diagnosis)
```

[Q15]: How well does the newly created model with four clusters separate out the two diagnoses?

```
## diagnosis

## groups B M

## 1 28 188

## 2 329 24

(188 + 329)/(length(diagnosis))
```

## [1] 0.9086116

In terms of accuracy, the model is approximately 91% accurate.

```
table(wisconsin_kmeans$cluster, diagnosis)
```

[Q16]: How well do the k-means and hierarchical clustering models you created in previous sections (i.e. before PCA) do in terms of separating the diagnoses? Again, use the table()

function to compare the output of each model (wisc.km\$cluster and wisc.hclust.clusters) with the vector containing the actual diagnoses.

```
##
      diagnosis
##
         В
     1 343 37
##
     2 14 175
##
(175 + 343)/length(diagnosis)
## [1] 0.9103691
table(wisconsin_hclust_clusters_k4, diagnosis)
##
                                diagnosis
## wisconsin_hclust_clusters_k4
##
                                 12 165
##
                                   2
                                       5
                                      40
##
                               3 343
##
                                   0
                                       2
(165 + 5 + 2 + 343)/length(diagnosis)
```

## [1] 0.9050967

Sensitivity

hclust-no\_pca: 357/(357+210)

## [1] 0.6296296 kmeans-no\_pca:

The original kmeans before PCA had an accuracy of ~91% and the original helust model had an accuracy of ~90%. Indicating that with PCA the helust method became marginally more accurate.

## Sensitivity and Specifity

```
hclust-pca:

165/(165 + 47)

## [1] 0.7783019

hclust-no_pca:

2/(2+210)

## [1] 0.009433962

kmeans-no_pca:

175/(175+37)

## [1] 0.8254717

Specificity
hclust-pca:

351/(351+47)

## [1] 0.8819095
```

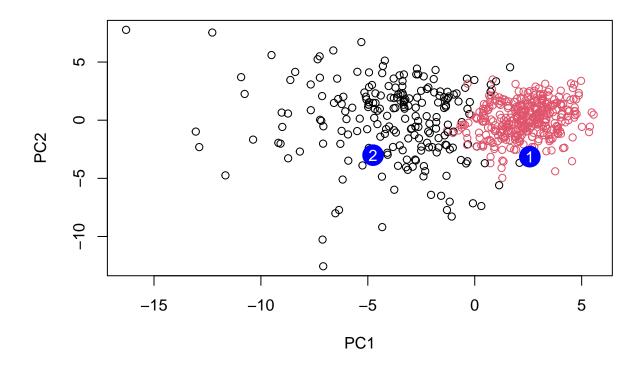
```
343/(343+37)
```

## [1] 0.9026316

[Q17]: Which of your analysis procedures resulted in a clustering model with the best specificity? How about sensitivity? K-means, much like with accuracy, showed the highest specificity and sensitivity of all three models.

#### Prediction

```
url <- "https://tinyurl.com/new-samples-CSV"</pre>
new <- read.csv(url)</pre>
npc <- predict(wisconsin_pca, newdata=new)</pre>
npc
##
             PC1
                       PC2
                                  PC3
                                             PC4
                                                      PC5
                                                                 PC6
## [1,] 2.576616 -3.135913 1.3990492 -0.7631950 2.781648 -0.8150185 -0.3959098
## [2,] -4.754928 -3.009033 -0.1660946 -0.6052952 -1.140698 -1.2189945
                                                                      0.8193031
              PC8
##
                        PC9
                                  PC10
                                            PC11
                                                     PC12
                                                               PC13
                                                                        PC14
## [1,] -0.2307350 0.1029569 -0.9272861 0.3411457 0.375921 0.1610764 1.187882
## [2,] -0.3307423 0.5281896 -0.4855301 0.7173233 -1.185917 0.5893856 0.303029
                                                          PC19
##
            PC15
                       PC16
                                   PC17
                                               PC18
                                                                     PC20
## [1,] 0.3216974 -0.1743616 -0.07875393 -0.11207028 -0.08802955 -0.2495216
0.25591230 -0.4289500
##
             PC21
                        PC22
                                   PC23
                                              PC24
                                                         PC25
                                                                      PC26
## [1,] 0.1228233 0.09358453 0.08347651 0.1223396 0.02124121 0.078884581
## [2,] -0.1224776 0.01732146 0.06316631 -0.2338618 -0.20755948 -0.009833238
##
               PC27
                           PC28
                                        PC29
                                                    PC30
## [1,] 0.220199544 -0.02946023 -0.015620933 0.005269029
## [2,] -0.001134152  0.09638361  0.002795349 -0.019015820
plot(wisconsin_pca$x[,1:2], col=groups)
points(npc[,1], npc[,2], col="blue", pch=16, cex=3)
text(npc[,1], npc[,2], c(1,2), col="white")
```



table(groups, diagnosis)

[Q18]: Which of these new patients should we prioritize for follow up based on your results?

```
## groups B M
## 1 28 188
## 2 329 24
```

Since observations which cluster as group 1 are more likely to be malignant than benign and vice-versa for observations which cluster as group 2, I would prioritize patient '2' for a follow up, given they cluster with group 1 on the PCA plot.

### **Session Information**

#### sessionInfo()

```
## R version 4.1.1 (2021-08-10)
## Platform: x86_64-pc-linux-gnu (64-bit)
## Running under: Arch Linux
##
## Matrix products: default
           /usr/lib/libblas.so.3.10.0
## LAPACK: /usr/lib/liblapack.so.3.10.0
##
## locale:
    [1] LC_CTYPE=en_US.UTF-8
                                   LC_NUMERIC=C
##
##
    [3] LC_TIME=en_US.UTF-8
                                   LC_COLLATE=en_US.UTF-8
##
    [5] LC_MONETARY=en_US.UTF-8
                                   LC_MESSAGES=en_US.UTF-8
    [7] LC_PAPER=en_US.UTF-8
                                   LC NAME=C
   [9] LC_ADDRESS=C
                                   LC_TELEPHONE=C
##
```

```
## [11] LC_MEASUREMENT=en_US.UTF-8 LC_IDENTIFICATION=C
##
## attached base packages:
## [1] stats
                graphics grDevices utils
                                               datasets methods
                                                                   base
## other attached packages:
## [1] rgl 0.107.14
                        factoextra_1.0.7 ggplot2_3.3.5
##
## loaded via a namespace (and not attached):
## [1] tidyselect_1.1.1 xfun_0.24
                                            purrr_0.3.4
                                                              haven_2.4.1
                          colorspace_2.0-2
## [5] carData_3.0-4
                                            vctrs_0.3.8
                                                              generics_0.1.0
## [9] htmltools_0.5.1.1 yaml_2.2.1
                                            utf8_1.2.1
                                                              rlang_0.4.11
                          ggpubr_0.4.0
## [13] pillar_1.6.1
                                            foreign_0.8-81
                                                              glue_1.4.2
## [17] withr_2.4.2
                          DBI_1.1.1
                                            readxl_1.3.1
                                                              lifecycle_1.0.0
## [21] stringr_1.4.0
                          cellranger_1.1.0
                                            munsell_0.5.0
                                                              ggsignif_0.6.3
## [25] gtable_0.3.0
                          zip_2.2.0
                                            htmlwidgets_1.5.4 evaluate_0.14
## [29] forcats_0.5.1
                          rio_0.5.27
                                            labeling_0.4.2
                                                              knitr_1.33
                          curl 4.3.2
## [33] extrafont 0.17
                                            fansi 0.5.0
                                                              Rttf2pt1 1.3.8
## [37] highr_0.9
                          broom_0.7.8
                                            Rcpp_1.0.7
                                                              scales_1.1.1
## [41] backports 1.2.1
                          jsonlite_1.7.2
                                            abind 1.4-5
                                                              farver 2.1.0
## [45] hms_1.1.0
                          digest_0.6.27
                                            openxlsx_4.2.4
                                                              stringi_1.7.2
## [49] rstatix 0.7.0
                          dplyr_1.0.7
                                            ggrepel_0.9.1
                                                              grid_4.1.1
## [53] tools_4.1.1
                          magrittr_2.0.1
                                            tibble_3.1.2
                                                              crayon_1.4.1
                                                              pkgconfig_2.0.3
## [57] extrafontdb 1.0
                          tidyr 1.1.3
                                            car 3.0-11
## [61] ellipsis_0.3.2
                          data.table_1.14.0 assertthat_0.2.1 rmarkdown_2.11
## [65] R6_2.5.0
                          compiler_4.1.1
```