

COSC-364 FLOW PLANNING ASSIGNMENT

Will Cowper

ID: 81163265

wgc22@uclive.ac.nz

Contribution: 50%

Jesse Sheehan

ID: 53366509

jps111@uclive.ac.nz

Contribution: 50%

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1 Problem Formulation

Notation:

- X is the number of source nodes.
- Y is the number of transit nodes.
- Z is the number of destination nodes.
- S_i is the i th source node.
- T_k is the k th transit node.
- D_j is the j th destination node.
- h_{ij} is the demand flow between S_i and D_j . This is equal to $2i + j$.
- c_{ik} is the link capacity between S_i and T_k .
- d_{kj} is the link capacity between T_k and D_j .
- x_{ikj} is the decision variable associated with the...
- u_{ikj} is the binary decision variable associated with the... These are required because h_{ij} must be split across exactly two transit nodes.
- l_k is the load on T_k .

1.1 Objective Function

$$\text{minimize}_{[r]} \quad (1)$$

1.2 Demand Constraints

$$\sum_{k=1}^Y x_{ikj} = 2i + j \quad i \in \{1, \dots, X\}, j \in \{1, \dots, Z\} \quad (2)$$

1.3 Capacity Constraints

$$\sum_{j=1}^Z x_{ikj} = c_{ik} \quad i \in \{1, \dots, X\}, k \in \{1, \dots, Y\} \quad (3)$$

$$\sum_{i=1}^X x_{ikj} = d_{kj} \quad k \in \{1, \dots, Y\}, j \in \{1, \dots, Z\} \quad (4)$$

$$\sum_{k=1}^Y x_{ikj} = l_k \quad i \in \{1, \dots, X\}, j \in \{1, \dots, Z\} \quad (5)$$

$$\sum_{k=1}^Y u_{ikj} = 2 \quad i \in \{1, \dots, X\}, j \in \{1, \dots, Z\} \quad (6)$$

1.4 Non-Negativity Constraints

$$r \geq 0 \quad (7)$$

$$x_{ijk} \geq 0 \quad i \in \{1, \dots, X\}, k \in \{1, \dots, Y\}, j \in \{1, \dots, Z\} \quad (8)$$

2 Results

3 Appendix

3.1 Source Code

3.1.1 src/__main__.py

```

import sys
2
from lp_gen import generate_lp_file
4 from lp_utils import get_lp_filename, run_cplex

6 __TITLE__ = "COSC-364 Assignment 2"
__AUTHORS__ = [("Will Cowper", "81163265"), ("Jesse Sheehan", "53366509")]
8

10 def print_version():
    print(' {0} by {1}'.format(__TITLE__, ', '.join(
12         [" {0} ({1})".format(name, sid) for (name, sid) in __AUTHORS__]))

14
16 def print_usage():
    print('Usage: {0} <x> <y> <z>'.format(sys.argv[0]))

18
20 def get_problem_parameters():
    """ Returns a tuple containing the x, y and z parameters. """

```

```

22     try:
23         x = int(sys.argv[1])
24         y = int(sys.argv[2])
25         z = int(sys.argv[3])
26     except:
27         print_usage()
28         exit(-1)
29
30     if x <= 0:
31         print("Error: x must be strictly positive")
32         exit(-1)
33
34     if y < 0:
35         print("Error: y must be strictly positive")
36         exit(-1)
37
38     if z <= 0:
39         print("Error: z must be strictly positive")
40         exit(-1)
41
42     return x, y, z
43
44 def save_lp_file(filename, data):
45     try:
46         f = open(filename, 'w')
47         f.write(data)
48         f.close()
49     except:
50         print("Error: could not save file '{0}'".format(filename))
51         exit(-1)
52
53
54 def main():
55     print_version()
56     if len(sys.argv) != 4:
57         print_usage()
58         exit(-1)
59     else:
60         x, y, z = get_problem_parameters()
61         data = generate_lp_file(x, y, z)
62         filename = get_lp_filename(x, y, z)
63         save_lp_file(filename, data)
64         print("Success: saved as '{0}'".format(filename))
65         run_cplex(filename)
66
67
68 if __name__ == "__main__":
69     main()

```

../src/__main__.py

3.1.2 src/lp_utils.py

```

1 import functools
2 import subprocess

```

```

4 def get_lp_filename(x, y, z):
6     """ Returns the filename that the LP data should be saved to. """
    return "problem-{0}-{1}-{2}.lp".format(x, y, z)
8
10 def run_cplex(filename):
12     """ Runs cplex on the LP file. """
    subprocess.run(
        'cplex -c "read {0}" "optimize" "display solution variables -"'.
        format(filename))
14
16 def crange(first, last):
18     """ Returns a list of characters between the two characters passed in (
    inclusive).
20     >>> crange('A', 'C')
    ['A', 'B', 'C']
22     >>> crange('A', 'A')
    ['A']
    """
    if ord(first) > ord(last):
24         raise ValueError("last must come after first")
    else:
26         return [chr(i) for i in range(ord(first), ord(last) + 1)]
28
30 def repeat(obj, n):
32     """ Returns a list with obj repeated n times.
    >>> repeat(1, 1)
    [1]
34     >>> repeat(42, 0)
    []
36     >>> repeat(5, 4)
    [5, 5, 5, 5]
38     >>> repeat([1, 2], 2)
    [[1, 2], [1, 2]]
40     """
    return [obj for _ in range(n)]
42
44 def perms(lists):
46     """ Returns all the permutations of the elements.
    >>> perms([])
    []
48     >>> perms(['a', 'b', 'c'])
    [('a',), ('b',), ('c',)]
50     >>> perms(['a', 'b', 'c'], ['x', 'y', 'z'])
    [('a', 'x'), ('a', 'y'), ('a', 'z'), ('b', 'x'), ('b', 'y'), ('b', 'z'),
    ('c', 'x'), ('c', 'y'), ('c', 'z')]
52     """
    if len(lists) == 0:
54         return []
    elif (len(lists) == 1):
56         return [(x,) for x in lists[0]]
58

```

```

    else:
        return [(x,) + y for x in lists[0] for y in perms(lists[1:])]

60
62
def concat(permutations):
    """ Returns the permutations concatenated as strings.
64
    >>> concat(perms([[ 'a ', 'b ', 'c ']]))
66
    [ 'a ', 'b ', 'c ' ]
    >>> concat(perms([[ 'a ', 'b ', 'c '], [ 'x ', 'y ', 'z ' ]]))
68
    [ 'ax ', 'ay ', 'az ', 'bx ', 'by ', 'bz ', 'cx ', 'cy ', 'cz ' ]
    """
    return [functools.reduce(lambda x, y: x + str(y), p, '') for p in
70
    permutations]

72
if __name__ == "__main__":
74
    import doctest
    doctest.testmod()

```

../src/lp_utils.py

3.1.3 src/lp_gen.py

```

from lp_utils import perms, concat
2
template = """\
4
\\ COSC-364 Assignment 2, LP Output File

6
MINIMIZE
\\ tr
8
SUBJECT TO
10
\\t\\ DEMAND CONSTRAINTS
12
\\t{}

14
\\t\\ CAPACITY CONSTRAINTS FOR LINKS BETWEEN SOURCE AND TRANSIT NODES
\\t{}

16
\\t\\ CAPACITY CONSTRAINTS FOR LINKS BETWEEN TRANSIT AND DESTINATION NODES
18
\\t{}

20
\\t\\ OBJECTIVE FUNCTION LOAD CONSTRAINTS
\\t{}

22
\\t\\ TRANSIT NODE LOAD CONSTRAINTS
24
\\t{}

26
\\t\\ BINARY VARIABLE AND DECISION VARIABLE CONSTRAINTS
\\t{}

28
\\t\\ BINARY VARIABLE CONSTRAINTS (ONLY 2 ACTIVE TRANSIT NODES)
30
\\t{}

32
BOUNDS
34
\\t\\ NON-NEGATIVITY CONSTRAINTS

```

```

36 \tr >= 0
37 \t{}
38 BIN
39
40 \t\\ BINARY VARIABLES
41 \t{}
42
43 END
44 """
45
46 def get_nodes(x, y, z):
47     """ Returns a tuple containing the source, transit and destination node
48         ids as integers. """
49     s = list(range(1, x + 1))
50     t = list(range(1, y + 1))
51     d = list(range(1, z + 1))
52     return s, t, d
53
54 def get_demand_constraints(s, t, d):
55     """ Returns a list of demand constraints. """
56     return [ ' + '.join(["X-{}{}{}".format(i, k, j) for k in t]) + ' =
57         {}'.format(2 * i + j)
58         for (i, j) in perms([s, d])]
59
60 def get_source_transit_capacity_constraints(s, t, d):
61     """ Returns a list of capacity constraints for the links between the
62         source and transit nodes. """
63     return \
64         [ ' + '.join(["X-{}{}{}".format(i, k, j) for j in d]) +
65           ' - C-{}{}{} <= 0'.format(i, k) for (i, k) in perms([s, t])]
66
67 def get_transit_destination_capacity_constraints(s, t, d):
68     """ Returns a list of capacity constraints for the links between the
69         transit and destination nodes. """
70     return \
71         [ ' + '.join(["X-{}{}{}".format(i, k, j) for i in s]) +
72           ' - D-{}{}{} <= 0'.format(k, j) for (k, j) in perms([t, d])]
73
74 def get_transit_load_constraints(s, t, d):
75     """ Returns the list of transit load constraints. """
76     return [ ' + '.join(["X-{}{}{}".format(i, k, j) for (i, j) in perms([
77         s, d])]) +
78         ' - l-{} = 0'.format(k) for k in t]
79
80 def get_objective_function_load_constraints(s, t, d):
81     """ Returns the list of objective function load constraints. """
82     return []
83     #return [ ' + '.join(["X-{}{}{}".format(i, k, j) for (i, j) in perms
84         ([s, d])]) +
85         ' - r <= 0' for k in t]
86
87 def get_binary_and_decision_variable_constraints(s, t, d):

```

```

88     """ Returns the binary and decision variable constraints. """
89     return []
90
91 def get_binary_constraints(s, t, d):
92     """ Returns a list of binary variable constraints. """
93     return [ ' + '.join(["U-{{0}}{{1}}{{2}}".format(i, k, j) for k in t]) + ' = 2'
94             for (i, j) in perms([s, d])]
95
96 def get_binary_variables(s, t, d):
97     """ Returns a list of binary variables. """
98     return ["U-{{0}}{{1}}{{2}}".format(i, k, j) for (i, k, j) in perms([s, t, d])
99             ]
100
101 def get_non_negativity_constraints(s, t, d):
102     """ Returns a list of non-negativity constraints. """
103     return ["X-{{0}} >= 0".format(subscript) for subscript in concat(perms([s
104     , t, d]))]
105
106 def generate_lp_file(x, y, z):
107     """ Returns the LP file contents as per the project specification. """
108     s, t, d = get_nodes(x, y, z)
109
110     demand_constraints = '\n\t'.join(get_demand_constraints(s, t, d))
111     source_transit_capacity_constraints = '\n\t'.join(
112         get_source_transit_capacity_constraints(s, t, d))
113     transit_destination_capacity_constraints = '\n\t'.join(
114         get_transit_destination_capacity_constraints(s, t, d))
115     non_negativity_constraints = '\n\t'.join(get_non_negativity_constraints
116     (
117         s, t, d))
118     objective_function_load_constraints = '\n\t'.join(
119         get_objective_function_load_constraints(s, t, d))
120     transit_load_constraints = '\n\t'.join(
121         get_transit_load_constraints(s, t, d))
122     binary_and_decision_constraints = '\n\t'.join(
123         get_binary_and_decision_variable_constraints(s, t, d))
124     binary_variable_constraints = '\n\t'.join(get_binary_constraints(s, t,
125     d))
126     binary_variables = '\n\t'.join(get_binary_variables(s, t, d))
127
128     return template.format(
129         demand_constraints,
130         source_transit_capacity_constraints,
131         transit_destination_capacity_constraints,
132         objective_function_load_constraints,
133         transit_load_constraints,
134         binary_and_decision_constraints,
135         binary_variable_constraints,
136         non_negativity_constraints,
137         binary_variables)

```

../src/lp-gen.py

3.2 Generated LP File

3.2.1 problem_3_2_4.lp

3.3 Plagiarism Declaration