

# COSC-364 FLOW PLANNING ASSIGNMENT

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# 1 Problem Formulation

## Notation:

- $X$  is the number of source nodes.
- $Y$  is the number of transit nodes.
- $Z$  is the number of destination nodes.
- $S_i$  is the  $i$ th source node.
- $T_k$  is the  $k$ th transit node.
- $D_j$  is the  $j$ th destination node.
- $c_{ik}$  is the link capacity between  $S_i$  and  $T_k$ .
- $d_{kj}$  is the link capacity between  $T_k$  and  $D_j$ .
- $x_{ikj}$  is the decision variable associated with the...
- $u_{ikj}$  is the binary decision variable associated with the...

## 1.1 Objective Function

$$\text{minimize}_{[r]} \quad (1)$$

## 1.2 Demand Constraints

$$\sum_{k=1}^Y x_{ikj} = 2i + j \quad i \in \{1, \dots, X\}, j \in \{1, \dots, Z\} \quad (2)$$

## 1.3 Capacity Constraints

$$\sum_{j=1}^Z x_{ikj} \leq c_{ik} \quad i \in \{1, \dots, X\}, k \in \{1, \dots, Y\} \quad (3)$$

$$\sum_{i=1}^X x_{ikj} \leq d_{kj} \quad k \in \{1, \dots, Y\}, j \in \{1, \dots, Z\} \quad (4)$$

$$\sum_{k=1}^Y x_{ikj} \leq r \quad i \in \{1, \dots, X\}, j \in \{1, \dots, Z\} \quad (5)$$

$$\sum_{k=1}^Y u_{ikj} = 2 \quad i \in \{1, \dots, X\}, j \in \{1, \dots, Z\} \quad (6)$$

## 1.4 Non-Negativity Constraints

$$r \geq 0 \quad (7)$$

$$x_{ijk} \geq 0 \quad i \in \{1, \dots, X\}, k \in \{1, \dots, Y\}, j \in \{1, \dots, Z\} \quad (8)$$

## 2 Results

## 3 Appendix

### 3.1 Source Code

#### 3.1.1 src/\_\_main\_\_.py

```

import sys
2
from lp_gen import generate_lp_file
4 from lp_utils import get_lp_filename, run_cplex

6 __TITLE__ = "COSC-364 Assignment 2"
__AUTHORS__ = [("Will Cowper", "81163265"), ("Jesse Sheehan", "53366509")]
8

10 def print_version():
    print( '{0} by {1}'.format(__TITLE__, ', '.join(
12         ["{0} ({1})".format(name, sid) for (name, sid) in __AUTHORS__])) )

14
16 def print_usage():
    print( 'Usage: {0} <x> <y> <z>'.format(sys.argv[0]) )

18
20 def get_problem_parameters():
    """ Returns a tuple containing the x, y and z parameters. """
    try:
22         x = int(sys.argv[1])
        y = int(sys.argv[2])
24         z = int(sys.argv[3])
    except:
26         print_usage()
        exit(-1)
28
    if x <= 0:
30         print("Error: x must be strictly positive")
        exit(-1)
32
    if y < 3:
34         print("Error: y must be greater than or equal to 3")
        exit(-1)
36
    if z <= 0:
38         print("Error: z must be strictly positive")
        exit(-1)
40

    return x, y, z

```

```

42
44 def save_lp_file(filename, data):
45     try:
46         f = open(filename, 'w')
47         f.write(data)
48         f.close()
49     except:
50         print("Error: could not save file '{0}'".format(filename))
51         exit(-1)
52
54 def main():
55     print_version()
56     if len(sys.argv) != 4:
57         print_usage()
58         exit(-1)
59     else:
60         x, y, z = get_problem_parameters()
61         data = generate_lp_file(x, y, z)
62         filename = get_lp_filename(x, y, z)
63         save_lp_file(filename, data)
64         print("Success: saved as '{0}'".format(filename))
65         run_cplex(filename)
66
68 if __name__ == "__main__":
69     main()

```

../src/\_main\_.py

### 3.1.2 src/lp\_utils.py

```

import functools
import subprocess

def get_lp_filename(x, y, z):
    """ Returns the filename that the LP data should be saved to. """
    return "problem_{0}_{1}_{2}.lp".format(x, y, z)

def run_cplex(filename):
    """ Runs cplex on the LP file. """
    subprocess.run(
        'cplex -c "read {0}" "optimize" "display solution variables -"'.
        format(filename))

def crange(first, last):
    """ Returns a list of characters between the two characters passed in (
    inclusive).
    >>> crange('A', 'C')
    ['A', 'B', 'C']
    >>> crange('A', 'A')
    ['A']
    """

```

```

24     if ord(first) > ord(last):
25         raise ValueError("last must come after first")
26
27     else:
28         return [chr(i) for i in range(ord(first), ord(last) + 1)]
29
30 def repeat(obj, n):
31     """ Returns a list with obj repeated n times.
32     >>> repeat(1, 1)
33     [1]
34     >>> repeat(42, 0)
35     []
36     >>> repeat(5, 4)
37     [5, 5, 5, 5]
38     >>> repeat([1, 2], 2)
39     [[1, 2], [1, 2]]
40     """
41     return [obj for _ in range(n)]
42
43
44 def perms(lists):
45     """ Returns all the permutations of the elements.
46     >>> perms([])
47     []
48     >>> perms(['a', 'b', 'c'])
49     [('a',), ('b',), ('c',)]
50     >>> perms(['a', 'b', 'c'], ['x', 'y', 'z'])
51     [('a', 'x'), ('a', 'y'), ('a', 'z'), ('b', 'x'), ('b', 'y'), ('b', 'z'),
52      ('c', 'x'), ('c', 'y'), ('c', 'z')]
53     """
54     if len(lists) == 0:
55         return []
56
57     elif (len(lists) == 1):
58         return [(x,) for x in lists[0]]
59
60     else:
61         return [(x,) + y for x in lists[0] for y in perms(lists[1:])]
62
63
64 def concat(permutations):
65     """ Returns the permutations concatenated as strings.
66     >>> concat(perms(['a', 'b', 'c']))
67     ['a', 'b', 'c']
68     >>> concat(perms(['a', 'b', 'c'], ['x', 'y', 'z']))
69     ['ax', 'ay', 'az', 'bx', 'by', 'bz', 'cx', 'cy', 'cz']
70     """
71     return [functools.reduce(lambda x, y: x + str(y), p, '') for p in
72             permutations]
73
74 if __name__ == "__main__":
75     import doctest
76     doctest.testmod()

```

../src/lp\_utils.py

## 3.1.3 src/lp\_gen.py

```

1 from lp_utils import perms, concat
2
3 template = """\
4 \\ COSC-364 Assignment 2, LP Output File
5 MINIMIZE
6     r
7 SUBJECT TO
8     \\ DEMAND CONSTRAINTS
9     {}
10    \\ CAPACITY CONSTRAINTS FOR LINKS BETWEEN SOURCE AND TRANSIT NODES
11    {}
12    \\ CAPACITY CONSTRAINTS FOR LINKS BETWEEN TRANSIT AND DESTINATION NODES
13    {}
14    \\ TRANSIT NODE LOAD CONSTRAINTS
15    {}
16    \\ BINARY VARIABLE CONSTRAINTS (ONLY 2 ACTIVE TRANSIT NODES)
17    {}
18 BOUNDS
19    \\ NON-NEGATIVITY CONSTRAINTS
20    r >= 0
21    {}
22 BIN
23    \\ BINARY VARIABLES
24    {}
25 END
26 """
27
28
29 def get_nodes(x, y, z):
30     """ Returns a tuple containing the source, transit and destination node
31     ids as integers. """
32     s = list(range(1, x + 1))
33     t = list(range(1, y + 1))
34     d = list(range(1, z + 1))
35     return s, t, d
36
37 def get_demand_constraints(s, t, d):
38     """ Returns a list of demand constraints. """
39     return [ ' + '.join(["X_{0}{1}{2}".format(i, k, j) for k in t]) + ' =
40             {0}'.format(2 * i + j)
41             for (i, j) in perms([s, d])]
42
43 def get_source_transit_capacity_constraints(s, t, d):
44     """ Returns a list of capacity constraints for the links between the
45     source and transit nodes. """
46     return \
47         [ ' + '.join(["X_{0}{1}{2}".format(i, k, j) for j in d]) +
48           ' - C_{0}{1} <= 0'.format(i, k) for (i, k) in perms([s, t])] #
49
50     + \
51     # [ ' + '.join(["C_{0}{1}".format(i, j) for i in s]) +
52     # ' - r <= 0' for j in d]
53     # don't know about the above commented lines

```

```

def get_transit_destination_capacity_constraints(s, t, d):
    """ Returns a list of capacity constraints for the links between the
    transit and destination nodes. """
    return \
        [ ' + '.join(["X-{}{}{}{}".format(i, k, j) for i in s]) +
          ' - D-{}{}{} <= 0'.format(k, j) for (k, j) in perms([t, d])]

def get_transit_load_constraints(s, t, d):
    """ Returns the list of transit load constraints. """
    return [ ' + '.join(["X-{}{}{}{}".format(i, k, j) for (i, j) in perms([
s, d])]) +
            ' - r <= 0' for k in t] # maybe change this line for the one
below?
# ' - L-{} <= 0'.format(k) for k in t]

def get_binary_constraints(s, t, d):
    """ Returns a list of binary variable constraints. """
    return [ ' + '.join(["U-{}{}{}{}".format(i, k, j) for k in t]) + ' = 2'
            for (i, j) in perms([s, d])]

def get_binary_variables(s, t, d):
    """ Returns a list of binary variables. """
    return ["U-{}{}{}{}".format(i, k, j) for (i, k, j) in perms([s, t, d])
]

def get_non_negativity_constraints(s, t, d):
    """ Returns a list of non-negativity constraints. """
    return ["X-{} >= 0".format(subscript) for subscript in concat(perms([s
, t, d]))]

def generate_lp_file(x, y, z):
    """ Returns the LP file contents as per the project specification. """
    s, t, d = get_nodes(x, y, z)

    demand_constraints = '\n\t'.join(get_demand_constraints(s, t, d))
    source_transit_capacity_constraints = '\n\t'.join(
        get_source_transit_capacity_constraints(s, t, d))
    transit_destination_capacity_constraints = '\n\t'.join(
        get_transit_destination_capacity_constraints(s, t, d))
    non_negativity_constraints = '\n\t'.join(get_non_negativity_constraints
(
        s, t, d))
    transit_load_constraints = '\n\t'.join(
        get_transit_load_constraints(s, t, d))
    binary_variable_constraints = '\n\t'.join(get_binary_constraints(s, t,
d))
    binary_variables = '\n\t'.join(get_binary_variables(s, t, d))

    return template.format(
        demand_constraints,
        source_transit_capacity_constraints,
        transit_destination_capacity_constraints,
        transit_load_constraints,

```

```
104 |         binary_variable_constraints ,  
    |         non_negativity_constraints ,  
106 |         binary_variables)
```

../src/lp-gen.py

## 3.2 Generated LP File

### 3.2.1 problem\_3\_2\_4.lp

## 3.3 Plagiarism Declaration