FLOW PLANNING

ASSIGNMENT 2

COSC364-19S1 INTERNET TECHNOLOGY AND ENGINEERING

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Figure 1: Traffic problems are not unique to computer networks.

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Date: 29-5-19 29/5/19

1 Problem Description

Given a network (figure 2) with X source nodes, Y transit nodes and Z destination nodes, a program was designed to generate an LP file that could be used by CPLEX to determine certain network characteristics.

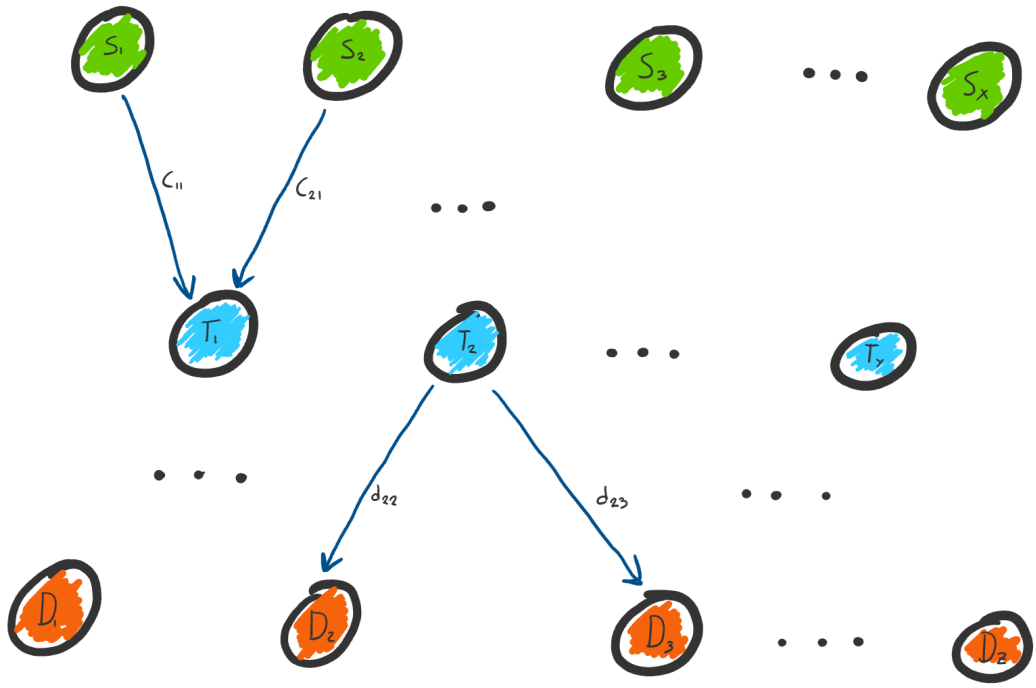

Figure 2: An example network showing nodes S_i, T_k and D_j and links c_{ik} and d_{kj}, $i \in \{1, \ldots, X\}, k \in \{1, \ldots, Y\}, j \in \{1, \ldots, Z\}$.

Traffic travelling from S_i to D_j must travel through exactly 2 transit nodes with a total demand volume of h_{ij} (equation 10). Furthermore, the load upon each transit node must be balanced.

2 Problem Formulation

This problem was solved with the use of binary variable constraints (equations 6, 7 and 9) and the minimisation of our objective function (equation 1). All normal non-negativity constraints were applied (equations 11, 12, 13 and 14).

The following network properties were solved for:

- The capacities of each link (equations 3 and 4).
- The load on each transit node (equation 5).
- The value of each flow (equations 2 and 8).

Notation:

- X is the number of source nodes.
- Y is the number of transit nodes.
- Z is the number of destination nodes.
- S_i is the ith source node.
- T_k is the kth transit node.
- D_j is the jth destination node.
- h_{ij} is the demand flow between S_i and D_j. This is equal to $2i + j$.
- c_{ik} is the link capacity between S_i and T_k.
- d_{kj} is the link capacity between T_k and D_j.
- x_{ikj} is the decision variable associated with the path S_i-T_k-D_j.
- u_{ikj} is the binary decision variable associated with x_{ikj}. These are required because h_{ij} must be split across exactly 2 transit nodes.
- l_k is the load on T_k.

Note: Due to the limitations of the LP file format, many of the following equations must be rearranged for use in CPLEX. Most notably, there cannot be any variables on the right hand side of an equality or inequality.

Python, BASH and PowerShell scripts (section 4.1) were used to automate the process (figure 3) of generating the LP files, analysing the CPLEX data, and producing graphs.

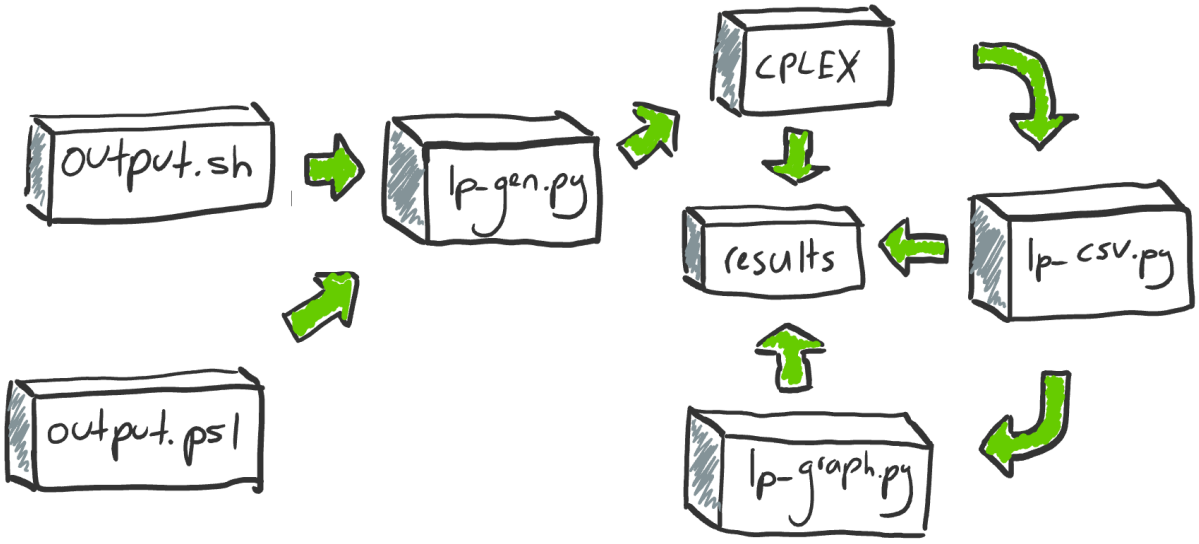

Figure 3: A graphical interpretation of the script execution used.

2.1 Objective Function

$$\text{minimize}_{[x,c,d,r]}\ r \tag{1}$$

2.2 Constraints

$$\sum_{k=1}^{Y} x_{ikj} = h_{ij} \qquad i \in \{1,\ldots,X\}, j \in \{1,\ldots,Z\} \tag{2}$$

$$\sum_{j=1}^{Z} x_{ikj} = c_{ik} \qquad i \in \{1,\ldots,X\}, k \in \{1,\ldots,Y\} \tag{3}$$

$$\sum_{i=1}^{X} x_{ikj} = d_{kj} \qquad k \in \{1,\ldots,Y\}, j \in \{1,\ldots,Z\} \tag{4}$$

$$\sum_{k=1}^{Y} x_{ikj} = l_{k} \qquad i \in \{1,\ldots,X\}, j \in \{1,\ldots,Z\} \tag{5}$$

$$\sum_{k=1}^{Y} u_{ikj} = 2 \qquad i \in \{1,\ldots,X\}, j \in \{1,\ldots,Z\} \tag{6}$$

$$x_{ikj} = \frac{u_{ikj} h_{ij}}{2} \qquad i \in \{1,\ldots,X\}, k \in \{1,\ldots,Y\}, j \in \{1,\ldots,Z\} \tag{7}$$

$$\sum_{i=1}^{X}\sum_{j=1}^{Z} x_{ikj} \leq r \qquad k \in \{1,\ldots,Y\} \tag{8}$$

$$u_{ikj} \in \{0,1\} \qquad i \in \{1,\ldots,X\}, k \in \{1,\ldots,Y\}, j \in \{1,\ldots,Z\} \tag{9}$$

$$h_{ij} = 2i + j \qquad i \in \{1,\ldots,X\}, j \in \{1,\ldots,Z\} \tag{10}$$

2.3 Non-Negativity Constraints

$$r \geq 0 \tag{11}$$

$$x_{ikj} \geq 0 \qquad i \in \{1,\ldots,X\}, k \in \{1,\ldots,Y\}, j \in \{1,\ldots,Z\} \tag{12}$$

$$c_{ik} \geq 0 \qquad i \in \{1,\ldots,X\}, k \in \{1,\ldots,Y\} \tag{13}$$

$$d_{kj} \geq 0 \qquad k \in \{1,\ldots,Y\}, j \in \{1,\ldots,Z\} \tag{14}$$

3 Results

LP files were generated with parameters $X = Z = 9, Y \in \{3, 4, 5, 6, 7, 8\}$. These were then processed with CPLEX, recording the time taken to solve each problem. Important data points were extracted from the CPLEX output and are listed in table 1.

Table 1: The raw data as extracted and processed from the CPLEX output.

Y	**Time (ms)**	**Links**	**Load Spread**	**Max. c_{ik}**	**Max. d_{kj}**
3	81.6132	52	0.0	94.500000	73.500000
4	117.3323	68	0.5	8.500000	9.500000
5	285.8704	83	0.0	9.500000	9.500000
6	443.1351	101	0.0	83.000000	9.500000
7	223.422	118	1.5	9.500000	9.500000
8	987.7775	134	0.5	9.500000	9.500000

An analysis of these results confirms many assumptions that were made about the problem. The number of non-zero link capacities increases linearly (figure 5), the transit node load spread is very close to (if not exactly) zero for most networks (figure 6), and the amount of time taken to solve the problem increases (almost) non-linearly as the number of transit nodes increases (figure 4). It is important to note that the load on the transit nodes was only able to be balanced in three of the networks, however the load spread on the remaining three networks is very low. CPLEX has done its best to equalise the loads on each transit node but could not balance them in some cases due to the demand flows and the number of nodes.

The most obvious feature of the results is the data for the $Y = 7$ network. It appears to be an outlier as it takes less time to solve than the $Y = 5$ network and has the highest transit node load spread by a factor of 3. **Explain this behaviour!!!**

The second odd feature of the data is the highest link capacities of the $Y = 3$ and $Y = 6$ networks (figure 7). **Also explain this behaviour!!!**

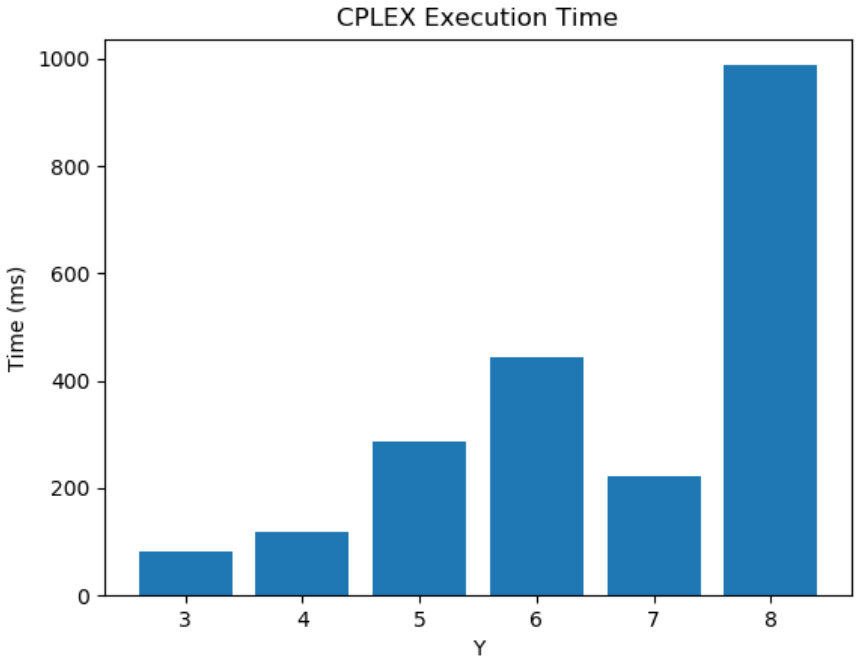

Figure 4: The time taken to execute the LP file in CPLEX for each network.

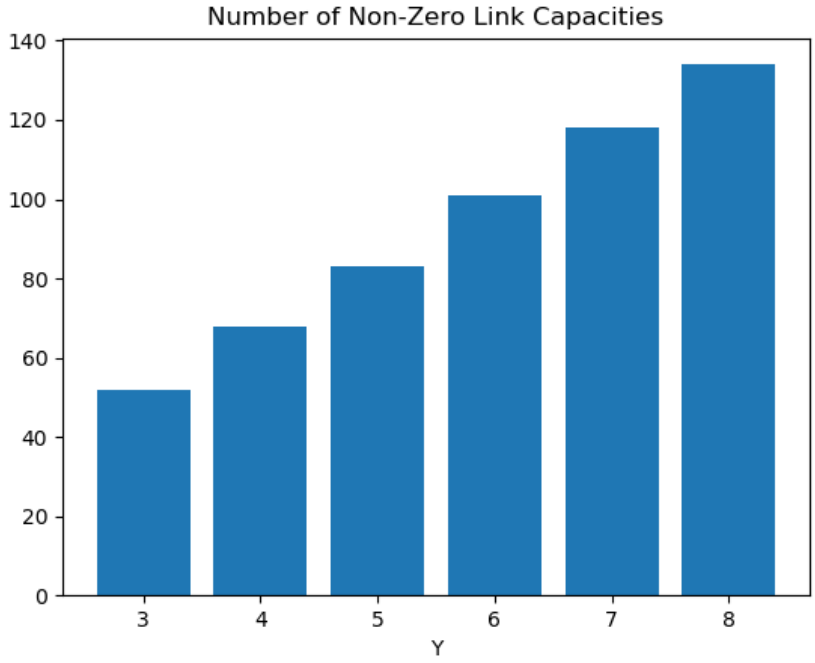

Figure 5: The number of non-zero link capacities in each network.

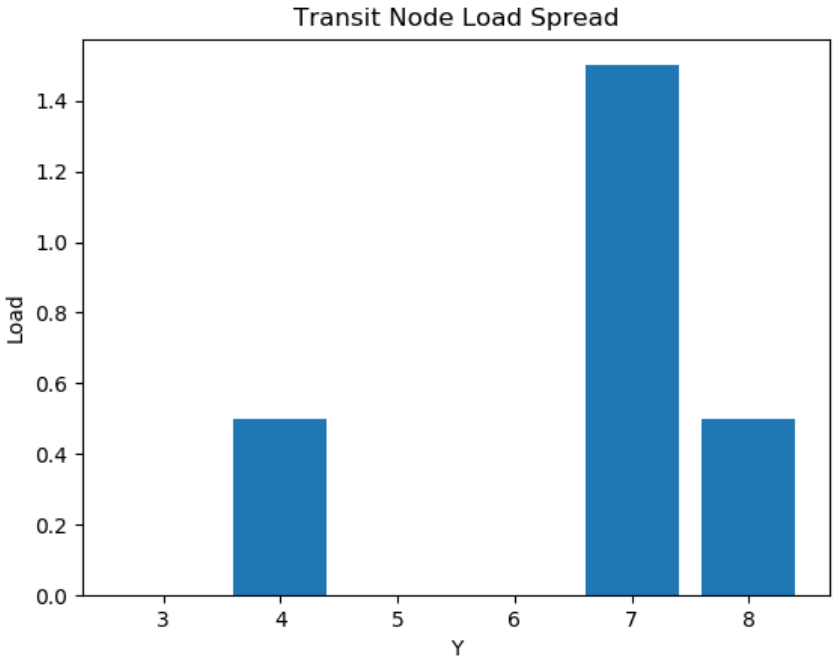

Figure 6: The amount of spread in the load for all transit nodes in each network.

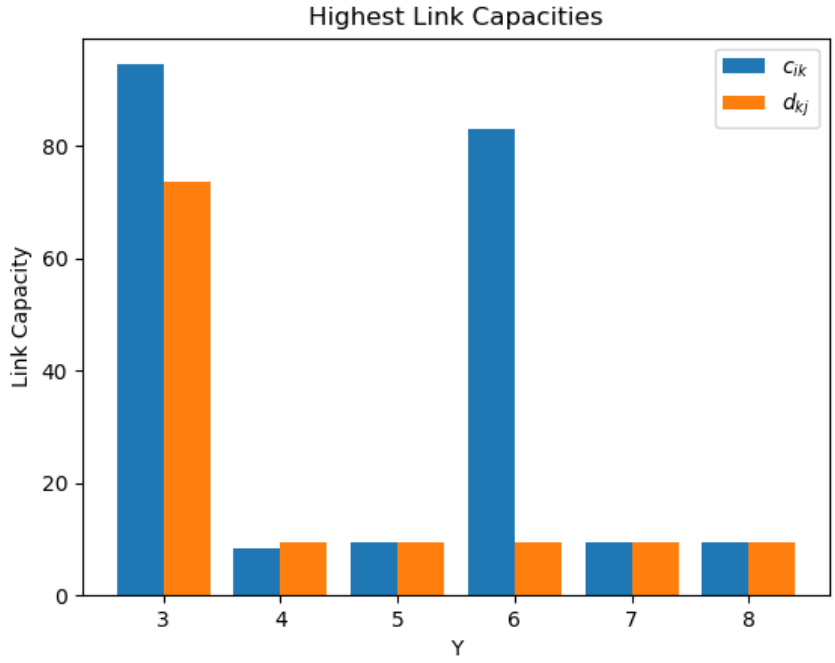

Figure 7: The highest capacity links for each network. Both the c_{ik} and d_{kj} links are listed.

4 Appendix

4.1 Source Code

4.1.1 src/lp_gen.py

This script is responsible for producing a valid LP file from the given command line parameters.

```
# lp_gen.py
#
# COSC364 Assignment 2
# 30/05/2019
# Written by Will Cowper, Jesse Sheehan

import inspect
import functools
import sys
import os.path

__TITLE__ = "COSC-364 Assignment 2 LP Generator"
__AUTHORS__ = [("Will Cowper", "81163265"), ("Jesse Sheehan", "53366509")]

# Change these variables to alter the behaviour of the LP file generator
PATH_SPLIT = 2


def DEMAND_FLOW(i, j): return 2 * i + j


TEMPLATE = """\
\\ {}, LP Output File
\\ Written by {}
\\ Parameters: X={}, Y={}, Z={}, Split={}, Demand={}

MINIMIZE
\tr

SUBJECT TO

\t\\ DEMAND CONSTRAINTS
\t{}

\t\\ CAPACITY CONSTRAINTS FOR LINKS BETWEEN SOURCE AND TRANSIT NODES
\t{}

\t\\ CAPACITY CONSTRAINTS FOR LINKS BETWEEN TRANSIT AND DESTINATION NODES
\t{}

\t\\ OBJECTIVE FUNCTION LOAD CONSTRAINTS
\t{}

\t\\ TRANSIT NODE LOAD CONSTRAINTS
\t{}

\t\\ BINARY VARIABLE AND DECISION VARIABLE CONSTRAINTS
\t{}
```

```
\t\\ BINARY VARIABLE CONSTRAINTS (ONLY 2 ACTIVE TRANSIT NODES)
\t{}

BOUNDS

\t\\ NON-NEGATIVITY CONSTRAINTS
\tr >= 0
\t{}

BIN

\t\\ BINARY VARIABLES
\t{}

END
"""

# DEFINE SOME UTILITY FUNCTIONS


def get_lp_filename(x, y, z):
    """ Returns the filename that the LP data should be saved to. """
    return "problem_{0}_{1}_{2}.lp".format(x, y, z)


def crange(first, last):
    """ Returns a list of characters between the two characters passed in (
    inclusive).
    >>> crange('A', 'C')
    ['A', 'B', 'C']
    >>> crange('A', 'A')
    ['A']
    """
    if ord(first) > ord(last):
        raise ValueError("last must come after first")

    else:
        return [chr(i) for i in range(ord(first), ord(last) + 1)]


def repeat(obj, n):
    """ Returns a list with obj repeated n times.
    >>> repeat(1, 1)
    [1]
    >>> repeat(42, 0)
    []
    >>> repeat(5, 4)
    [5, 5, 5, 5]
    >>> repeat([1, 2], 2)
    [[1, 2], [1, 2]]
    """
    return [obj for _ in range(n)]


def perms(lists):
    """ Returns all the permutations of the elements.
    >>> perms([])
    []
```

```
    >>> perms([['a', 'b', 'c']])
    [('a',), ('b',), ('c',)]
    >>> perms([['a', 'b', 'c'], ['x', 'y', 'z']])
    [('a', 'x'), ('a', 'y'), ('a', 'z'), ('b', 'x'), ('b', 'y'), ('b', 'z')
    , ('c', 'x'), ('c', 'y'), ('c', 'z')]
    """
    if len(lists) == 0:
        return []

    elif (len(lists) == 1):
        return [(x,) for x in lists[0]]

    else:
        return [(x,) + y for x in lists[0] for y in perms(lists[1:])]


def concat(permutations):
    """ Returns the permutations concatenated as strings.
    >>> concat(perms([['a', 'b', 'c']]))
    ['a', 'b', 'c']
    >>> concat(perms([['a', 'b', 'c'], ['x', 'y', 'z']]))
    ['ax', 'ay', 'az', 'bx', 'by', 'bz', 'cx', 'cy', 'cz']
    """
    return [functools.reduce(lambda x, y: x + str(y), p, '') for p in
    permutations]


def get_function_source(fn):
    src = inspect.getsource(fn)
    return src[str(src).index('return')+7:]


def get_lines(strings):
    return '\n\t'.join(strings)

# DEFINE SOME FUNCTIONS SPECIFIC TO THE PROBLEM


def get_nodes(x, y, z):
    """ Returns a tuple containing the source, transit and destination node
    ids as integers. """
    s = list(range(1, x + 1))
    t = list(range(1, y + 1))
    d = list(range(1, z + 1))
    return s, t, d


def get_demand_constraints(s, t, d):
    """ Returns a list of demand constraints. """
    return [' + '.join(["x_{0}{1}{2}".format(i, k, j) for k in t]) + ' =
    {0}'.format(DEMAND_FLOW(i, j))
            for (i, j) in perms([s, d])]


def get_source_transit_capacity_constraints(s, t, d):
    """ Returns a list of capacity constraints for the links between the
    source and transit nodes. """
    return \
```

```
160         [' + '.join(["x_{0}{1}{2}".format(i, k, j) for j in d]) +
                ' - c_{0}{1} = 0'.format(i, k) for (i, k) in perms([s, t])]
162
164 def get_transit_destination_capacity_constraints(s, t, d):
        """ Returns a list of capacity constraints for the links between the
    transit and destination nodes. """
166     return \
            [' + '.join(["x_{0}{1}{2}".format(i, k, j) for i in s]) +
168             ' - d_{0}{1} = 0'.format(k, j) for (k, j) in perms([t, d])]
170
    def get_transit_load_constraints(s, t, d):
172     """ Returns the list of transit load constraints. """
        return [' + '.join(["x_{0}{1}{2}".format(i, k, j) for (i, j) in perms([
    s, d])]) +
174             ' - l_{0} = 0'.format(k) for k in t]
176
    def get_objective_function_load_constraints(s, t, d):
178     """ Returns the list of objective function load constraints. """
        return [' + '.join(["c_{0}{1}".format(i, j) for i in s]) +
180             ' - r <= 0' for j in d]
182
    def get_binary_and_decision_variable_constraints(s, t, d):
184     """ Returns the binary and decision variable constraints. """
        return ['{3} x_{0}{1}{2} - {4} u_{0}{1}{2} = 0'.format(i, k, j,
    PATH_SPLIT, DEMAND_FLOW(i, j)) for (i, k, j) in perms([s, t, d])]
186
188 def get_binary_constraints(s, t, d):
        """ Returns a list of binary variable constraints. """
190     return [' + '.join(["u_{0}{1}{2}".format(i, k, j) for k in t]) + ' = {}
    '.format(PATH_SPLIT)
                for (i, j) in perms([s, d])]
192
194 def get_binary_variables(s, t, d):
        """ Returns a list of binary variables. """
196     return ["u_{0}{1}{2}".format(i, k, j) for (i, k, j) in perms([s, t, d])
    ]
198
    def get_non_negativity_constraints(s, t, d):
200     """ Returns a list of non-negativity constraints. """
        return ["x_{0}{1}{2} >= 0".format(i, k, j) for (i, k, j) in perms([s, t
    , d])] + ["c_{0}{1} >= 0".format(i, k) for (i, k) in perms([s, t])] + ["
    d_{0}{1} >= 0".format(k, j) for (k, j) in perms([t, d])]
202
204 def generate_lp_file(title, authors, x, y, z):
        """ Returns the LP file contents as per the project specification. """
206     s, t, d = get_nodes(x, y, z)

208     demand_constraints = get_lines(get_demand_constraints(s, t, d))
        source_transit_capacity_constraints = get_lines(
210         get_source_transit_capacity_constraints(s, t, d))
```

```
    transit_destination_capacity_constraints = get_lines(
        get_transit_destination_capacity_constraints(s, t, d))
    non_negativity_constraints = get_lines(get_non_negativity_constraints(
        s, t, d))
    objective_function_load_constraints = get_lines(
        get_objective_function_load_constraints(s, t, d))
    transit_load_constraints = get_lines(
        get_transit_load_constraints(s, t, d))
    binary_and_decision_constraints = get_lines(
        get_binary_and_decision_variable_constraints(s, t, d))
    binary_variable_constraints = get_lines(get_binary_constraints(s, t, d)
    )
    binary_variables = get_lines(get_binary_variables(s, t, d))

    return TEMPLATE.format(
        title,
        authors,
        x,
        y,
        z,
        PATH_SPLIT,
        get_function_source(DEMAND_FLOW),
        demand_constraints,
        source_transit_capacity_constraints,
        transit_destination_capacity_constraints,
        objective_function_load_constraints,
        transit_load_constraints,
        binary_and_decision_constraints,
        binary_variable_constraints,
        non_negativity_constraints,
        binary_variables)


# DEFINE SOME HELPERS FOR GETTING THE THING RUNNING

def print_version():
    print('{0} by {1}'.format(__TITLE__, get_author_string()))


def print_usage():
    print('Usage: {0} <x> <y> <z> [output directory]'.format(sys.argv[0]))


def get_problem_parameters():
    """ Returns a tuple containing the x, y and z parameters. """
    try:
        x = int(sys.argv[1])
        y = int(sys.argv[2])
        z = int(sys.argv[3])
    except:
        print_usage()
        exit(-1)

    if x <= 0:
        print("Error: x must be strictly positive")
        exit(-1)

    if x >= 10:
```

```
268         print("Error: x must be less than ten")
            exit(-1)
270
    if y <= 0:
272         print("Error: y must be strictly positive")
            exit(-1)
274
    if y >= 10:
276         print("Error: y must be less than ten")
            exit(-1)
278
    if z <= 0:
280         print("Error: z must be strictly positive")
            exit(-1)
282
    if z >= 10:
284         print("Error: z must be less than ten")
            exit(-1)
286
    return x, y, z
288


290 def save_lp_file(filename, data):
    try:
292         f = open(filename, 'w')
            f.write(data)
294         f.close()
    except:
296         print("Error: could not save file '{0}'".format(filename))
            exit(-1)
298


300 def get_author_string():
    return ', '.join(
302         ["{0} ({1})".format(name, sid) for (name, sid) in __AUTHORS__])


304
def main():
306     print_version()
    if len(sys.argv) != 4 and len(sys.argv) != 5:
308         print_usage()
            exit(-1)
310     else:
            output_dir = '.'
312         if len(sys.argv) == 5:
                output_dir = sys.argv[4]
314
            x, y, z = get_problem_parameters()
316         data = generate_lp_file(__TITLE__, get_author_string(), x, y, z)
            filename = os.path.join(output_dir, get_lp_filename(x, y, z))
318         save_lp_file(filename, data)
            print("Success: saved as '{0}'".format(filename))
320


322 if __name__ == "__main__":
    main()
```

../src/lp_gen.py

4.1.2 src/lp_csv.py

This script is responsible for converting the output of the CPLEX log files into a single CSV file for further processing.

```
# lp_csv.py
#
# COSC364 Assignment 2
# 30/05/2019
# Written by Will Cowper, Jesse Sheehan

import csv
import sys
import os.path


def csvWrite(data):
    with open(sys.argv[2], 'a', newline='') as csvFile:
        writer = csv.writer(csvFile)
        writer.writerow(data)


def floatmap(enumerable):
    return list(map(lambda x: float(x), enumerable))


def openFile(Y):
    with open(os.path.join(sys.argv[1], '{0}.txt'.format(Y)), 'r') as
    in_file:
        stripped = [line.strip() for line in in_file.readlines()]
        lines = [line for line in stripped if line]
        data = []
        # Y
        data.append(Y)
        # elapsed time
        data.append(max(parseFile("elapsed_", lines)))
        # no of non-zero c and d links
        data.append(len(parseFile("c_", lines)) + len(parseFile("d_", lines
    )))
        # transit load spread (largest_transit_node_load -
    smallest_transit_node_load)
        data.append(max(floatmap(parseFile("l_", lines))) -
                    min(floatmap(parseFile("l_", lines))))
        # highest cap c network
        data.append(max(parseFile("c_", lines)))
        # highest cap d network
        data.append(max(parseFile("d_", lines)))
        csvWrite(data)


'''Returns a list of all values that start with the given string'''


def parseFile(string, lines):
    values = []
    for line in lines:
        if line.startswith(string):
            values.append(line.split()[1])
```

```
    return values


if __name__ == "__main__":
    if len(sys.argv) != 3:
        print("Usage: {0} <input directory> <csv file>".format(sys.argv[0])
    )
        exit(-1)

    # delete the CSV, otherwise we will append to it
    os.unlink(sys.argv[2])

    openFile(3)
    openFile(4)
    openFile(5)
    openFile(6)
    openFile(7)
    openFile(8)

    print("Saved CSV data to '{}'".format(sys.argv[2]))
```

../src/lp_csv.py

4.1.3 src/lp_graph.py

This script is responsible for reading the CSV file and producing several graphs.

```
# lp_graph.py
#
# COSC364 Assignment 2
# 30/05/2019
# Written by Will Cowper, Jesse Sheehan

import csv
import sys
import os.path

try:
    import numpy as np
except:
    print("Error: could not load 'numpy'. Install with 'pip install numpy'
    and then try again.")
    exit(-1)


try:
    import matplotlib.pyplot as plt
except:
    print("Error: could not load 'matplotlib'. Install with 'pip install
    matplotlib' and then try again.")
    exit(-1)


def get_data(data, key):
    return list(map(lambda d: d[key], data))


```

```
def get_time(data):
    return get_data(data, "time")


def get_len_nonzero_links(data):
    return get_data(data, "len_links")


def get_transit_load_spread(data):
    return get_data(data, "load_spread")


def get_max_cap_c(data):
    return get_data(data, "max_cap_c")


def get_max_cap_d(data):
    return get_data(data, "max_cap_d")


def get_Y(data):
    return get_data(data, "Y")


def save_execution_time_plot(filename, data):
    """ Saves a plot of execution time. """
    plt.bar(get_Y(data), get_time(data))
    plt.xlabel("Y")
    plt.ylabel("Time (ms)")
    plt.title("CPLEX Execution Time")
    plt.savefig(filename)
    plt.close()
    print("Saved '{}'".format(filename))


def save_num_nonzero_links_plot(filename, data):
    """ Saves a plot of the number of non-zero links. """
    plt.bar(get_Y(data), get_len_nonzero_links(data))
    plt.xlabel("Y")
    plt.ylabel("")
    plt.title("Number of Non-Zero Link Capacities")
    plt.savefig(filename)
    plt.close()
    print("Saved '{}'".format(filename))


def save_transit_load_spread_plot(filename, data):
    """ Saves a plot of the transit load spread. """
    plt.bar(get_Y(data), get_transit_load_spread(data))
    plt.xlabel("Y")
    plt.ylabel("Load")
    plt.title("Transit Node Load Spread")
    plt.savefig(filename)
    plt.close()
    print("Saved '{}'".format(filename))


def save_highest_capacity_links_plot(filename, data):
```

```
    """ Saves a plot of the transit load spread. """
    width = 0.4
    Ys = np.array(get_Y(data))
    cs = plt.bar(Ys, get_max_cap_c(data), width, label="$c_{ik}$")
    ds = plt.bar(Ys + width, get_max_cap_d(data), width, label="$d_{kj}$")
    plt.xticks(Ys + width / 2, map(lambda x: int(x), Ys))
    plt.legend(handles=[cs, ds])
    plt.xlabel("Y")
    plt.ylabel("Link Capacity")
    plt.title("Highest Link Capacities")
    plt.savefig(filename)
    plt.close()
    print("Saved '{}'".format(filename))


def get_data_from_csv(csv_filename):
    """ Returns an array of dictionaries containing the CSV data. """
    with open(csv_filename, newline='') as csv_file:
        csv_reader = csv.DictReader(csv_file, fieldnames=[
                                    "Y", "time", "len_links", "load_spread"
    , "max_cap_c", "max_cap_d"])
        rows = []
        for row in csv_reader:
            d = {}
            for key in row:
                d[key] = float(row[key])
            rows.append(d)
        return rows


def convert_csv_to_images(csv_filename, output_folder):
    """ Converts the data from the CSV into a set of graphs. """
    data = get_data_from_csv(csv_filename)
    base_filename = os.path.splitext(os.path.join(
        output_folder, os.path.basename(csv_filename)))[0]

    save_execution_time_plot(base_filename + "_time.png", data)
    save_num_nonzero_links_plot(base_filename + "_num_nonzero_links.png",
    data)
    save_transit_load_spread_plot(
        base_filename + "_transit_load_spread.png", data)
    save_highest_capacity_links_plot(
        base_filename + "_highest_capacity_links.png", data)


def print_usage():
    print("Usage: {0} <csv file> <output folder>")


if __name__ == "__main__":
    if len(sys.argv) != 3:
        print_usage()
        exit(-1)

    convert_csv_to_images(sys.argv[1], sys.argv[2])
```

../src/lp_graph.py

4.1.4 output.sh

This BASH script is responsible for executing the other scripts as well as timing and running CPLEX (under the Linux operating system).

```
#!/bin/bash
for y in 3 4 5 6 7 8
do
    python3 src/lp_gen.py 9 $y 9 lp_files
    start=$(date +%s%N)
    cplex -c "read lp_files/problem_9_${y}_9.lp" "optimize" "display
    solution variables -" > cplex_logs/$y.txt
    end=$(date +%s%N)
    duration=$(expr $end - $start)
    duration=$(expr $duration / 1000000)
    echo -e "\nelapsed_time: $duration ms" >> cplex_logs/$y.txt
done

python3 src/lp_csv.py cplex_logs lp_files/cplex_data.csv
python3 src/lp_graph.py lp_files/cplex_data.csv graphs
```

../output.sh

4.1.5 output.ps1

This PowerShell script is responsible for executing the other scripts as well as timing and running CPLEX (under the Windows operating system).

```
For ($i=3; $i -le 8; $i++) {
    python src/lp_gen.py 9 $i 9 lp_files
    $perf = Measure-Command -Expression {$data = cplex -c ("read lp_files/
    problem_9_" + $i + "_9.lp") "optimize" "display solution variables -"}
    $ms = $perf.TotalMilliseconds
    [System.IO.File]::WriteAllLines("cplex_logs/$i.txt", $data + "`
    nelapsed_time: $ms ms")
}

python src/lp_csv.py cplex_logs lp_files/cplex_data.csv
python src/lp_graph.py lp_files/cplex_data.csv graphs
```

../output.ps1

4.2 Generated LP File

4.2.1 lp_files/problem_3_2_4.lp

```
\ COSC-364 Assignment 2 LP Generator, LP Output File
\ Written by Will Cowper (81163265), Jesse Sheehan (53366509)
\ Parameters: X=3, Y=2, Z=4, Split=2, Demand=2 * i + j


MINIMIZE
  r

SUBJECT TO

  \ DEMAND CONSTRAINTS
  x_111 + x_121 = 3
  x_112 + x_122 = 4
  x_113 + x_123 = 5
  x_114 + x_124 = 6
  x_211 + x_221 = 5
  x_212 + x_222 = 6
  x_213 + x_223 = 7
  x_214 + x_224 = 8
  x_311 + x_321 = 7
  x_312 + x_322 = 8
  x_313 + x_323 = 9
  x_314 + x_324 = 10

  \ CAPACITY CONSTRAINTS FOR LINKS BETWEEN SOURCE AND TRANSIT NODES
  x_111 + x_112 + x_113 + x_114 - c_11 = 0
  x_121 + x_122 + x_123 + x_124 - c_12 = 0
  x_211 + x_212 + x_213 + x_214 - c_21 = 0
  x_221 + x_222 + x_223 + x_224 - c_22 = 0
  x_311 + x_312 + x_313 + x_314 - c_31 = 0
  x_321 + x_322 + x_323 + x_324 - c_32 = 0

  \ CAPACITY CONSTRAINTS FOR LINKS BETWEEN TRANSIT AND DESTINATION NODES
  x_111 + x_211 + x_311 - d_11 = 0
  x_112 + x_212 + x_312 - d_12 = 0
  x_113 + x_213 + x_313 - d_13 = 0
  x_114 + x_214 + x_314 - d_14 = 0
  x_121 + x_221 + x_321 - d_21 = 0
  x_122 + x_222 + x_322 - d_22 = 0
  x_123 + x_223 + x_323 - d_23 = 0
  x_124 + x_224 + x_324 - d_24 = 0

  \ OBJECTIVE FUNCTION LOAD CONSTRAINTS
  c_11 + c_21 + c_31 - r <= 0
  c_12 + c_22 + c_32 - r <= 0
  c_13 + c_23 + c_33 - r <= 0
  c_14 + c_24 + c_34 - r <= 0

  \ TRANSIT NODE LOAD CONSTRAINTS
  x_111 + x_112 + x_113 + x_114 + x_211 + x_212 + x_213 + x_214 + x_311 +
    x_312 + x_313 + x_314 - l_1 = 0
  x_121 + x_122 + x_123 + x_124 + x_221 + x_222 + x_223 + x_224 + x_321 +
    x_322 + x_323 + x_324 - l_2 = 0

```

```
\ BINARY VARIABLE AND DECISION VARIABLE CONSTRAINTS
2 x_111 - 3 u_111 = 0
2 x_112 - 4 u_112 = 0
2 x_113 - 5 u_113 = 0
2 x_114 - 6 u_114 = 0
2 x_121 - 3 u_121 = 0
2 x_122 - 4 u_122 = 0
2 x_123 - 5 u_123 = 0
2 x_124 - 6 u_124 = 0
2 x_211 - 5 u_211 = 0
2 x_212 - 6 u_212 = 0
2 x_213 - 7 u_213 = 0
2 x_214 - 8 u_214 = 0
2 x_221 - 5 u_221 = 0
2 x_222 - 6 u_222 = 0
2 x_223 - 7 u_223 = 0
2 x_224 - 8 u_224 = 0
2 x_311 - 7 u_311 = 0
2 x_312 - 8 u_312 = 0
2 x_313 - 9 u_313 = 0
2 x_314 - 10 u_314 = 0
2 x_321 - 7 u_321 = 0
2 x_322 - 8 u_322 = 0
2 x_323 - 9 u_323 = 0
2 x_324 - 10 u_324 = 0

\ BINARY VARIABLE CONSTRAINTS (ONLY 2 ACTIVE TRANSIT NODES)
u_111 + u_121 = 2
u_112 + u_122 = 2
u_113 + u_123 = 2
u_114 + u_124 = 2
u_211 + u_221 = 2
u_212 + u_222 = 2
u_213 + u_223 = 2
u_214 + u_224 = 2
u_311 + u_321 = 2
u_312 + u_322 = 2
u_313 + u_323 = 2
u_314 + u_324 = 2

BOUNDS

\ NON-NEGATIVITY CONSTRAINTS
r >= 0
x_111 >= 0
x_112 >= 0
x_113 >= 0
x_114 >= 0
x_121 >= 0
x_122 >= 0
x_123 >= 0
x_124 >= 0
x_211 >= 0
x_212 >= 0
x_213 >= 0
x_214 >= 0
x_221 >= 0
x_222 >= 0
```

```
    x_223 >= 0
    x_224 >= 0
    x_311 >= 0
    x_312 >= 0
    x_313 >= 0
    x_314 >= 0
    x_321 >= 0
    x_322 >= 0
    x_323 >= 0
    x_324 >= 0
    c_11 >= 0
    c_12 >= 0
    c_21 >= 0
    c_22 >= 0
    c_31 >= 0
    c_32 >= 0
    d_11 >= 0
    d_12 >= 0
    d_13 >= 0
    d_14 >= 0
    d_21 >= 0
    d_22 >= 0
    d_23 >= 0
    d_24 >= 0

BIN

    \ BINARY VARIABLES
    u_111
    u_112
    u_113
    u_114
    u_121
    u_122
    u_123
    u_124
    u_211
    u_212
    u_213
    u_214
    u_221
    u_222
    u_223
    u_224
    u_311
    u_312
    u_313
    u_314
    u_321
    u_322
    u_323
    u_324

END
```

../lp_files/problem_3_2_4.lp