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## Hypothesis Representation

We could approach the classification problem ignoring the fact that y is discrete-valued, and use our old linear regression algorithm to try to predict y given x. However, it is easy to construct examples where this method performs very poorly. Intuitively, it also doesn't make sense for  $h_{\theta}(x)$  to take values larger than 1 or smaller than 0 when we know that y  $\in$  {0, 1}. To fix this, let's change the form for our hypotheses  $h_{\theta}(x)$  to satisfy  $0 \leq h_{\theta}(x) \leq 1$ . This is accomplished by plugging  $\theta^T x$  into the Logistic Function.

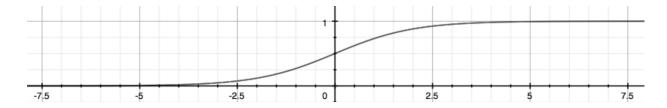
Our new form uses the "Sigmoid Function," also called the "Logistic Function":

$$h_{ heta}(x) = g( heta^T x)$$

$$z = heta^T x$$

$$g(z)=rac{1}{1+e^{-z}}$$

The following image shows us what the sigmoid function looks like:



The function g(z), shown here, maps any real number to the (0, 1) interval, making it useful for transforming an arbitrary-valued function into a function better suited for classification.

 $h_{\theta}(x)$  will give us the **probability** that our output is 1. For example,  $h_{\theta}(x) = 0.7$  gives us a probability of 70% that our output is 1. Our probability that our prediction is 0 is just the complement of our probability that it is 1 (e.g. if probability that it is 1 is 70%, then the probability that it is 0 is 30%).

$$h_{\theta}(x) = P(y = 1|x; \theta) = 1 - P(y = 0|x; \theta)$$
  
 $P(y = 0|x; \theta) + P(y = 1|x; \theta) = 1$ 







