

In this example we consider the following benchmark problem from elasticity theory:

$$(\sigma(u), \varepsilon(\varphi)) = (g, \varphi)_{\Gamma_N}. \quad (1)$$

Here  $\tilde{\Omega}$  is a quadratic domain with side length 200 mm, where a circular hole with radius 10 mm around the center is cut out. Using symmetries of the domain, we restrict our actual computational domain  $\Omega$  to the upper left quarter of  $\tilde{\Omega}$ .

In the above equation,  $\varepsilon(v) := \frac{1}{2}(\nabla v + \nabla v^T)$  is the symmetric strain tensor, and

$$\sigma(v) := 2\mu\varepsilon(v)^D + \kappa \cdot \text{tr}(\varepsilon(v))I$$

denotes the symmetric stress tensor. Here  $\tau^D$  is the deviatoric part of a tensor  $\tau$ , in two dimensions defined as

$$\tau^D := \tau - \frac{1}{2}\text{tr}(\tau)I,$$

and the parameters  $\mu$  and  $\kappa$  are chosen as  $\mu = 80193.800283$  resp.  $\kappa = 190937.589172$ . The corner points of our computational domain are in anticlockwise order:  $(0, 0)$ ,  $(90, 0)$ ,  $(100, 10)$ ,  $(100, 100)$  and  $(0, 100)$ . We prescribe homogeneous Dirichlet boundary conditions in  $y$ -direction between  $(0, 0)$  and  $(90, 0)$  (lower boundary part), homogeneous Dirichlet boundary conditions in  $x$ -direction between  $(100, 10)$  and  $(100, 100)$  (right boundary part), and we interpret the righthand side of equation (1) with  $g = 450$  as a boundary condition between  $(0, 100)$  and  $(100, 100)$  (upper boundary part).

The goal of our computations is to match the following functional reference values taken from *E. Stein (editor), Error-controlled Adaptive Finite Elements in Solid Mechanics, Wiley (2003), pp. 386 - 387*:

Functional	$u_1$ at $(90, 0)$	$\sigma_{22}$ at $(90, 0)$	$u_2$ at $(100, 100)$
Reference value	0.021290	1388.732343	0.20951

Functional	$u_1$ at $(0, 100)$	$\int_{(100, 100)}^{(0, 100)} u_2$
Reference value	0.076758	20.40344