

$$\sqrt{1+2\sqrt{1+3\sqrt{1+4\sqrt{1+\dots}}}}$$

$$\sqrt{2}\sqrt{2}\sqrt{2}\sqrt{2}\dots$$