- 1. (Binomial Formula)
 - (a) Prove that for $n \ge 1$ and $1 \le r \le n$,

$$\binom{n}{r} + \binom{n}{r-1} = \binom{n+1}{r}.$$

- (b) Use this formula to explain why Pascal's triangle works. You do not have to submit your work for this part.
- (c) Prove the binomial formula by mathematical induction.
- 2. (Horses again!) Someone claims to have proved by mathematical induction that all the horses in the world have the same color. Here is his formulation. Let n be the number of horses in any group of horses. For all $n \geq 1$, the proposition is that all the horses in the group have the same color. Here is the proof:
 - (a) The proposition is obviously true for n = 1.
 - (b) Assume that the proposition is true for some $n \geq 1$. Now consider any group of n+1 horses. By the induction hypothesis, Horses 1 to n, which is a group of n horses, have the same color. Again by the induction hypothesis, Horses 2 to n+1 have the same color. Since Horses 2 to n are common to both groups of n horses, the two groups of n horses must have the same color. Therefore, we conclude that Horses 1 to n+1 all have the same color.

Are you convinced?

Textbook Problems 1.2.1, 1.2.2, 1.3.2, 1.3.4, 1.3.5, 1.4.1, 1.4.2, 1.4.5, 1.4.6.